

Large Scale Groundwater Modelling in the Scope of the EU Water Directive



Challenges and first steps in the Walloon part of the Meuse basin

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General context

□ EU Water directive

- IWRM at the scale of main EU water districts
(e.g. Rhine, Meuse...)
- (ground)water body = management unit
- Focuses more on diffuse pollution problems
(e.g. nitrates)
- Short terms deadlines (2015...) and ~strict rules
and regulations
- All territories to be covered (no « gaps »)

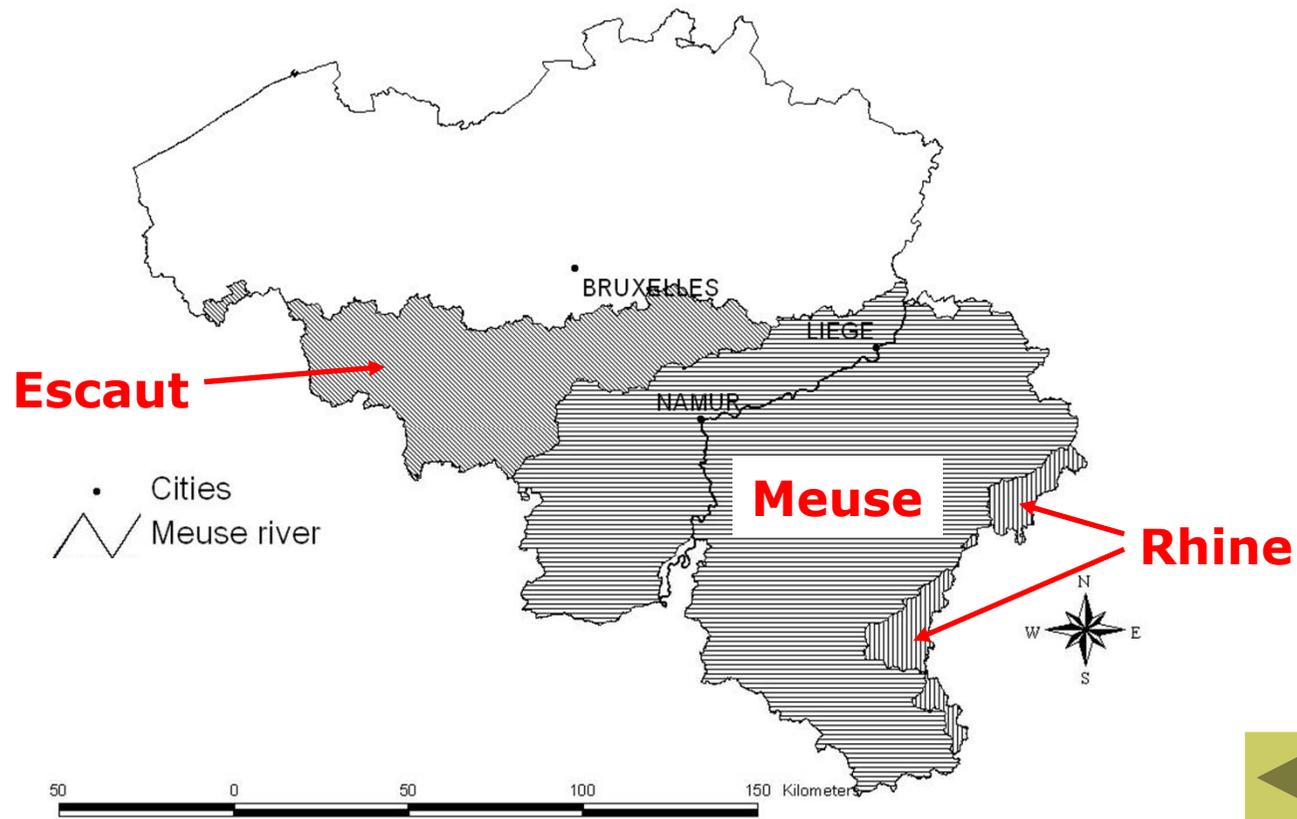
Challenges

- Developing a large-scale groundwater modelling approach is challenging:
 - Working scale: GW body → Water district
 - Large variability in geological and hydrogeological contexts
 - Large variability in the assessment of hydrogeological conditions and complexity of processes
 - Data requirements and handling
 - Integrated modelling approach in perspective
 - Computation requirements and accuracy of results

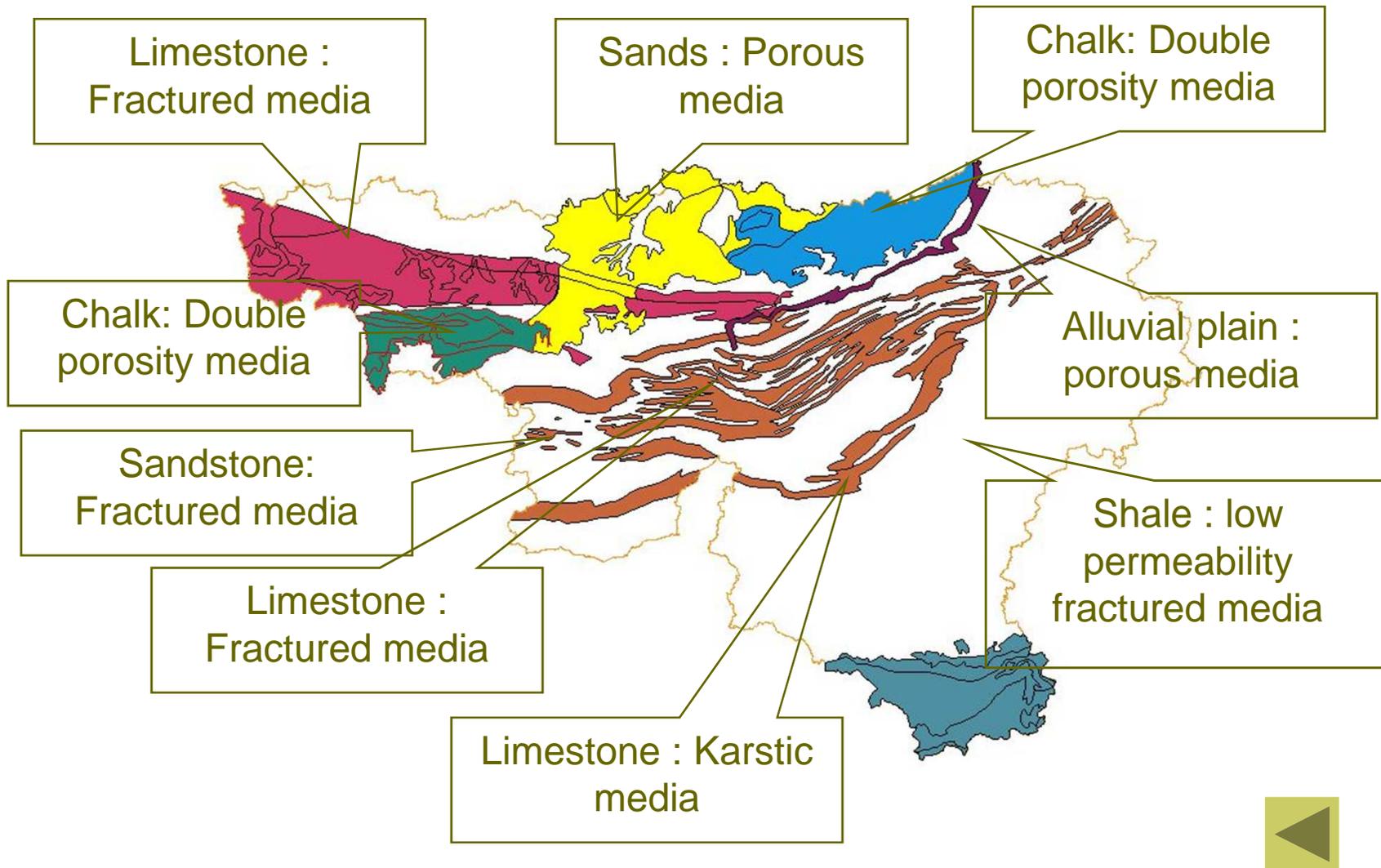
Working scale in the Walloon region

WFD : Management of water by hydrological districts

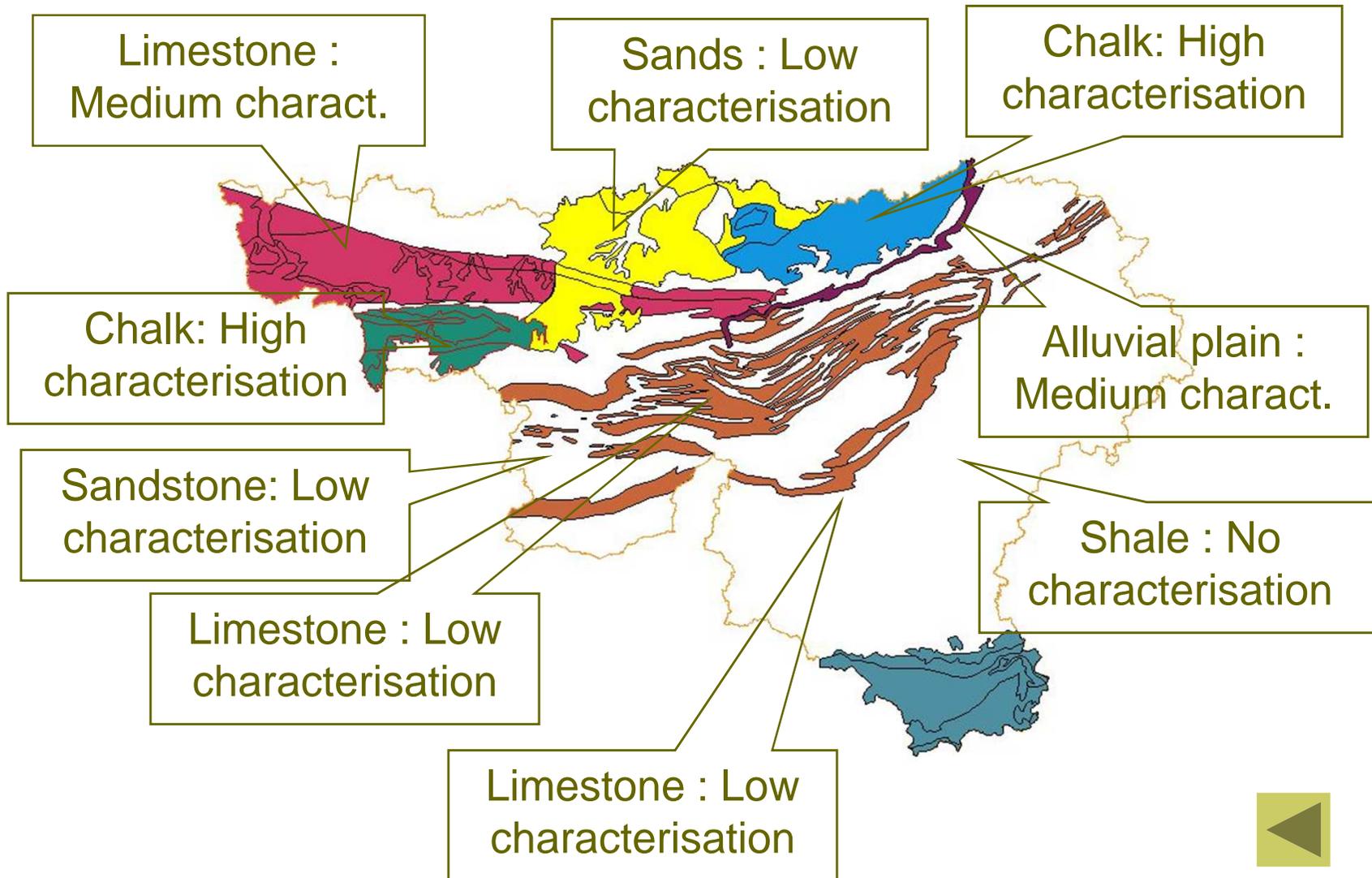
=> In the Walloon region, 3 hydrological districts



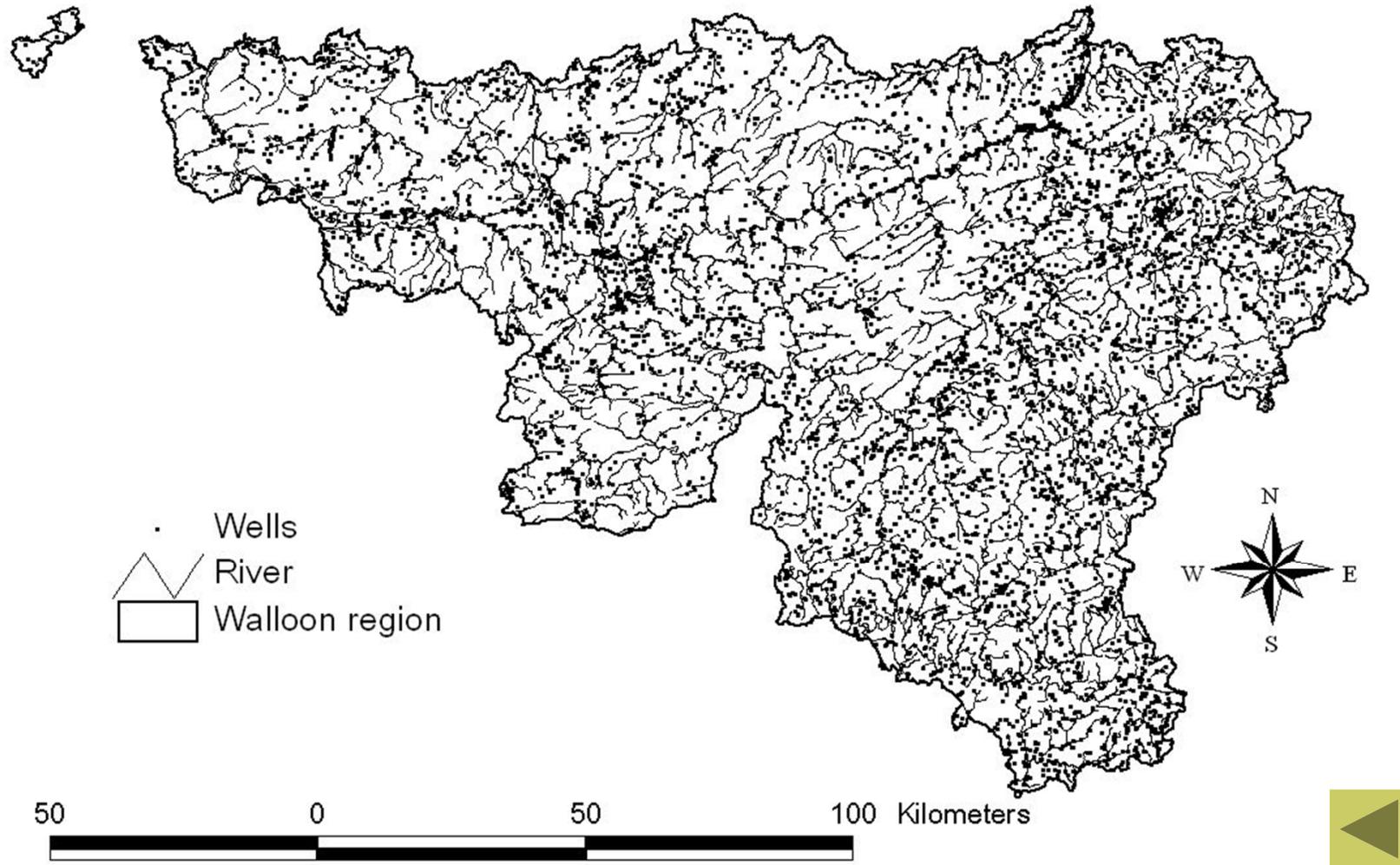
Variable geological contexts



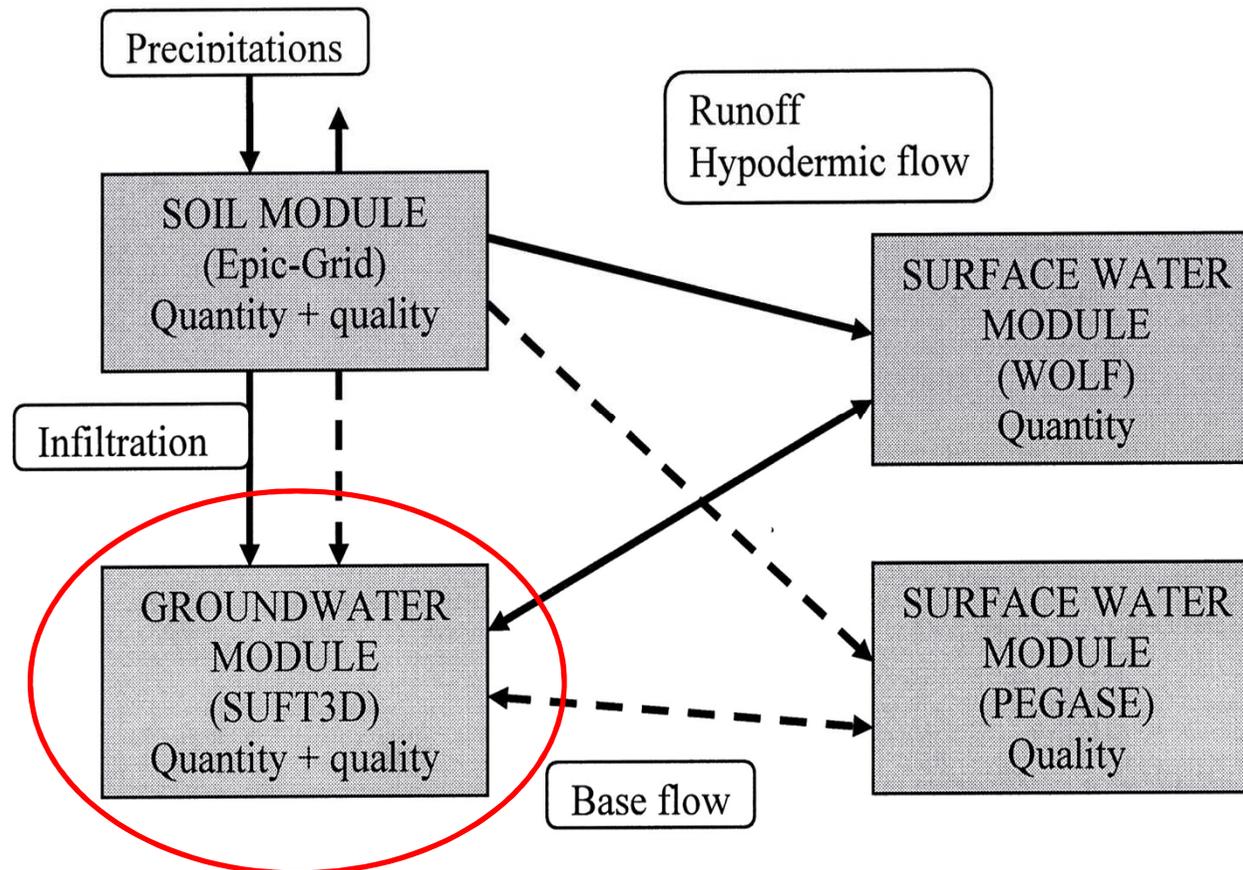
Variable knowledge on hydrogeological conditions



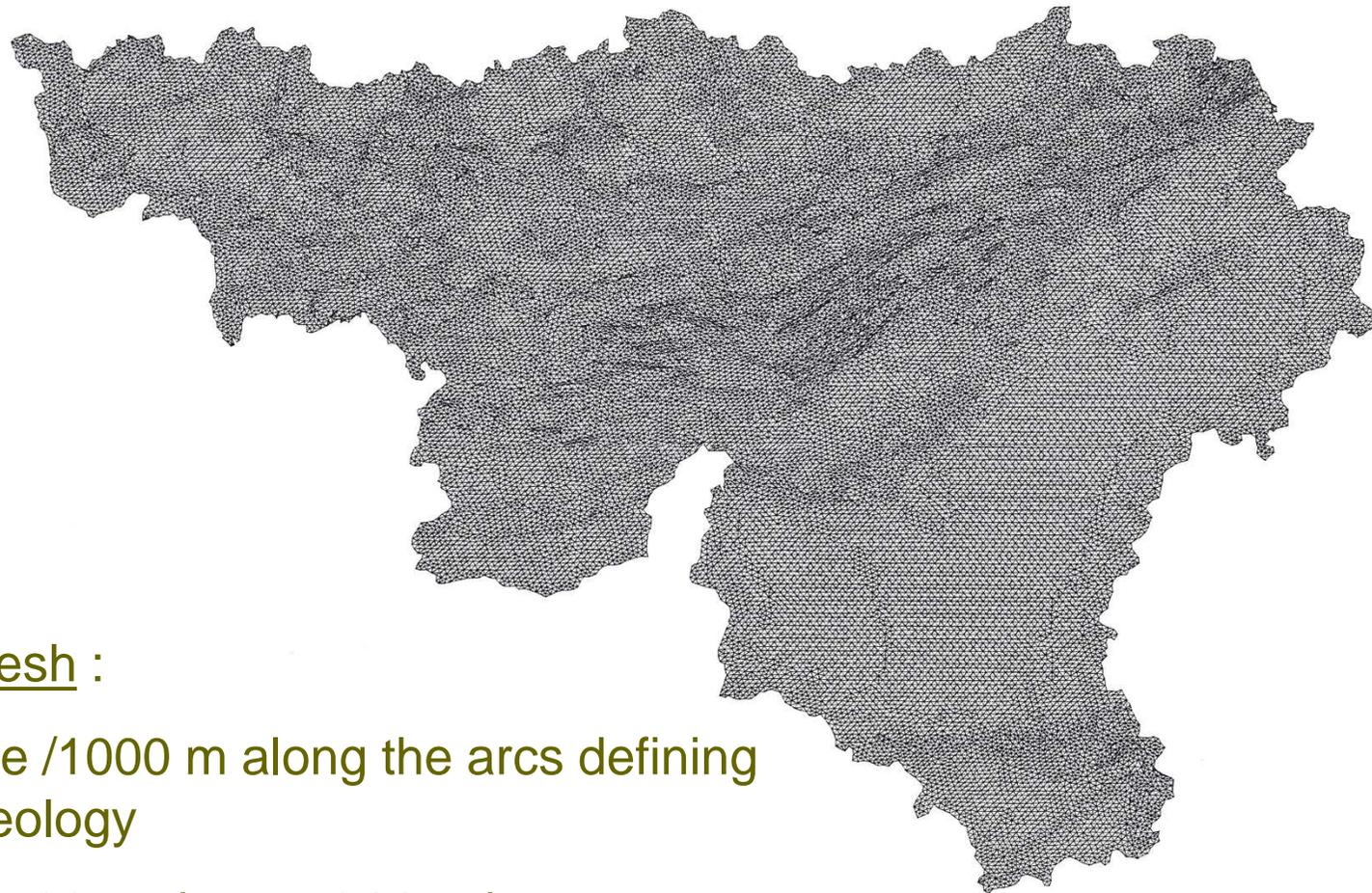
Data requirements and handling



Integrated Modelling of the Water cycle



Computational requirements

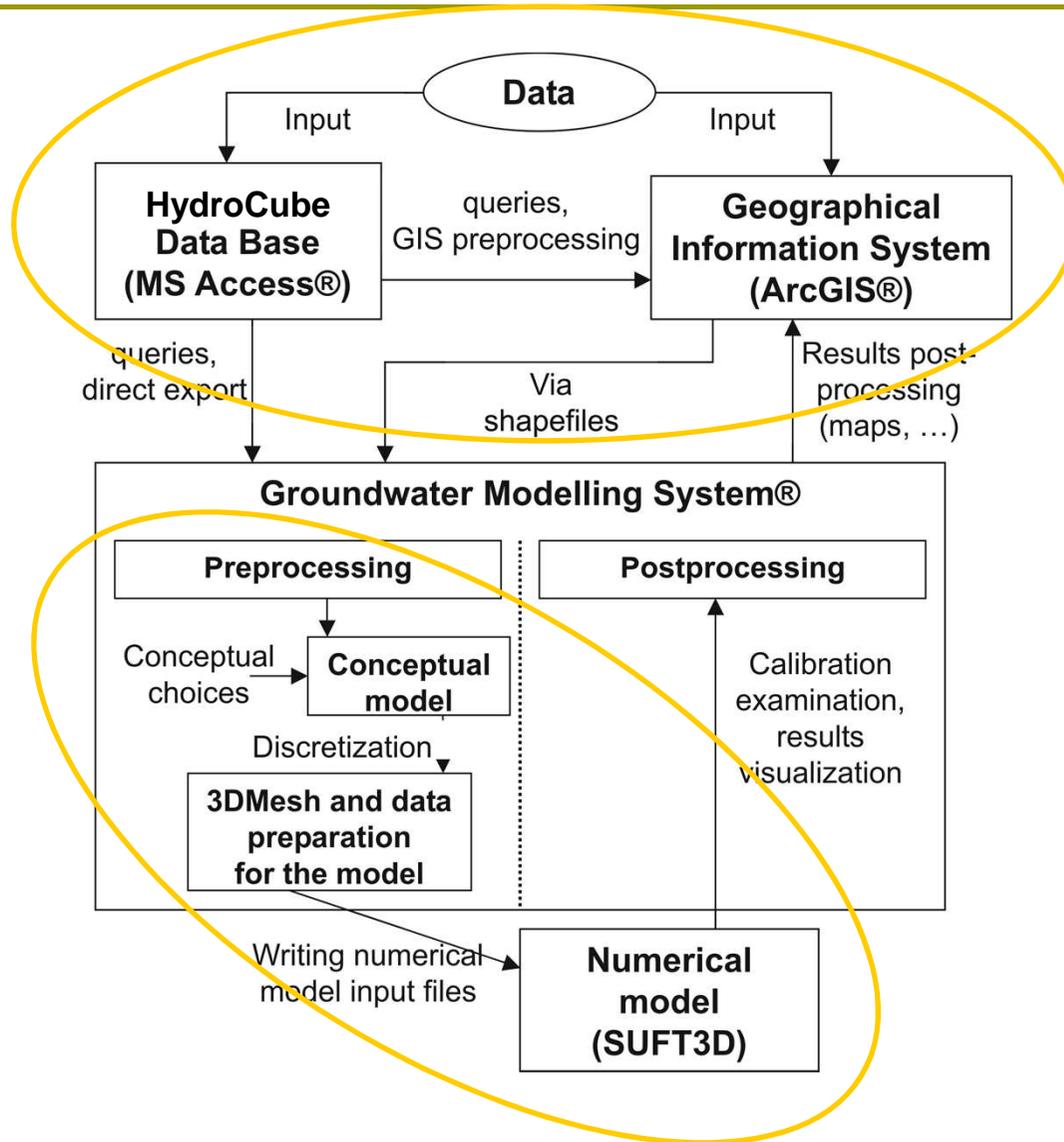


2D Mesh :

1 node /1000 m along the arcs defining
the geology

=> 28768 nodes – 56447 elements

General methodology for GW Modelling



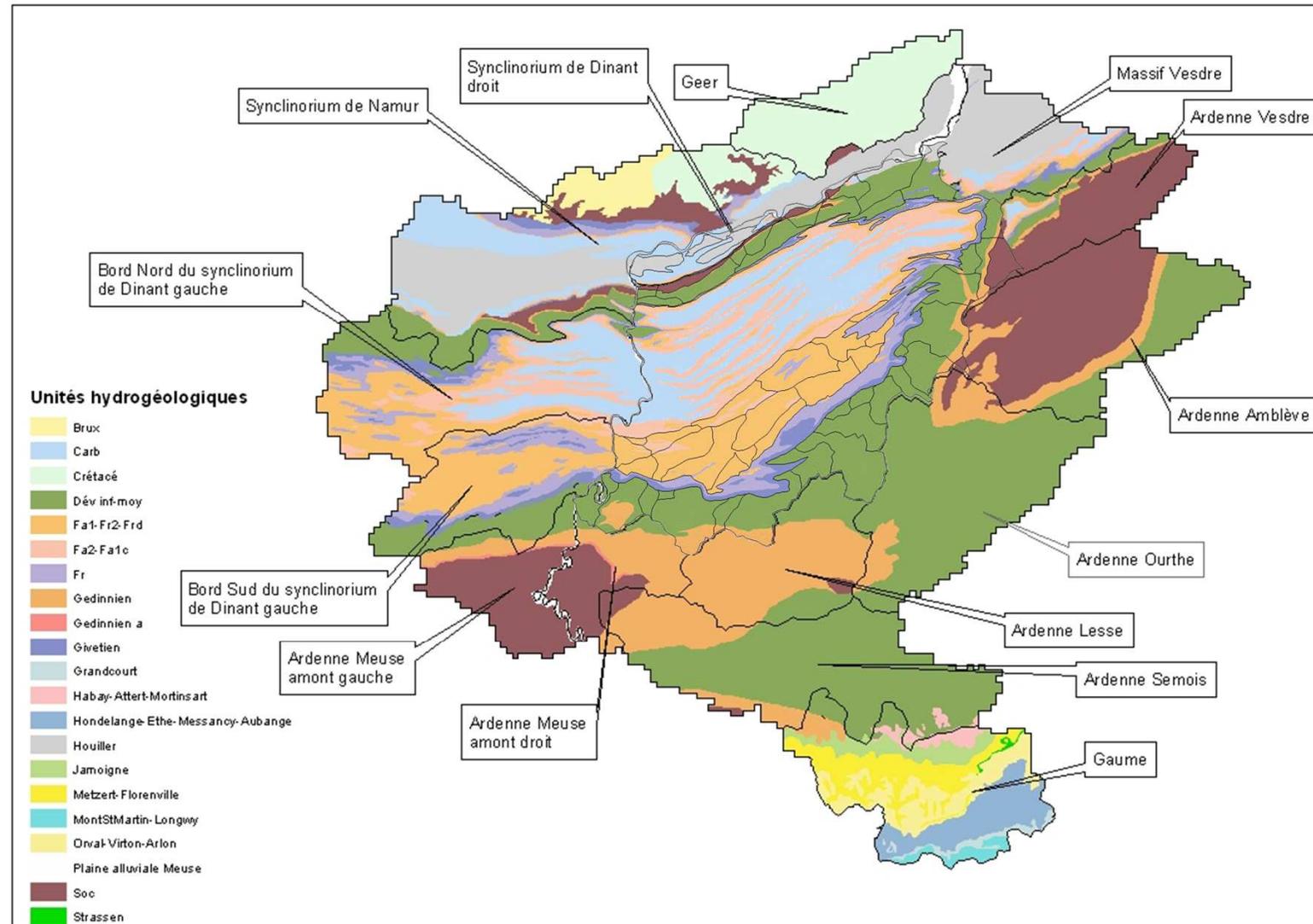
Data management :
Database and GIS

Model :
Conceptualisation
Equations

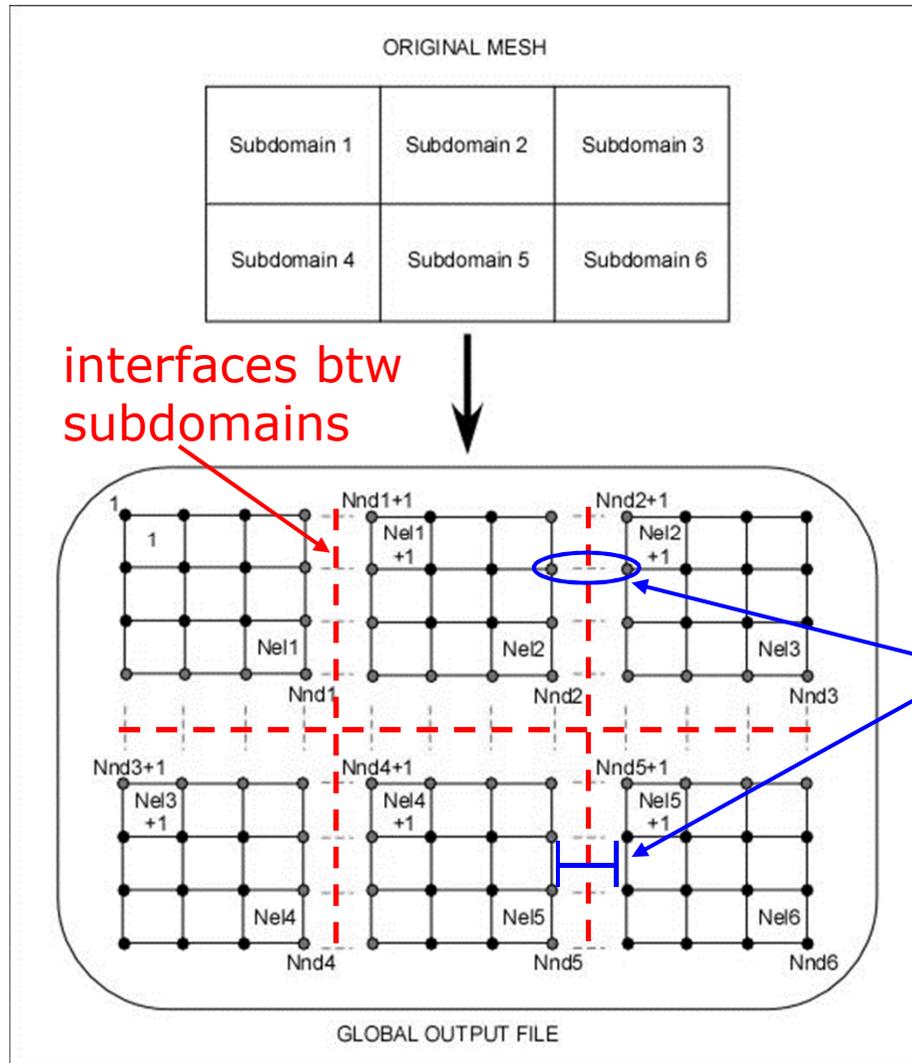
Geometrical discretization choices

- Global Model = $\sum \text{subModels}(\text{subDomains})$
 - SubModel = hydrogeologically independent subregion of a hydrological basin or district
 - no water exchanged between subModels
 - Exchange of water and contaminants through “external” boundaries only
 - SubDomain = subdivision of a subModel with:
 - “Given” degree of hydrogeological assessment (rough, detailed...)
 - Similar hydrogeological conditions (karst, porous media...)
 - Appropriate set of more or less complex flow and transport equations selected
 - Separated by “zero-D” interfaces = “internal” boundary conditions, across which water and contaminants can be exchanged (e.g. thin confining units not explicitly considered in the 3D discretization)

SubModels and subDomains in the Meuse basin



Mesh renumbering with subDomains



interfaces btw subdomains

3Dmesh =>

$$\begin{pmatrix} 1 \\ \dots \\ ne_1 \end{pmatrix} = SD_1 = 3DMesh_1$$

$$\begin{pmatrix} ne_{1+1} \\ \dots \\ ne_2 \end{pmatrix} = SD_2 = 3DMesh_2$$

$$\begin{pmatrix} ne_{2+1} \\ \dots \\ ne_3 \end{pmatrix} = SD_3 = 3DMesh_3$$

node-node or face-face internal BCs

=> Potentials for parallel computing, sub-modelling...

Mathematical and numerical solutions

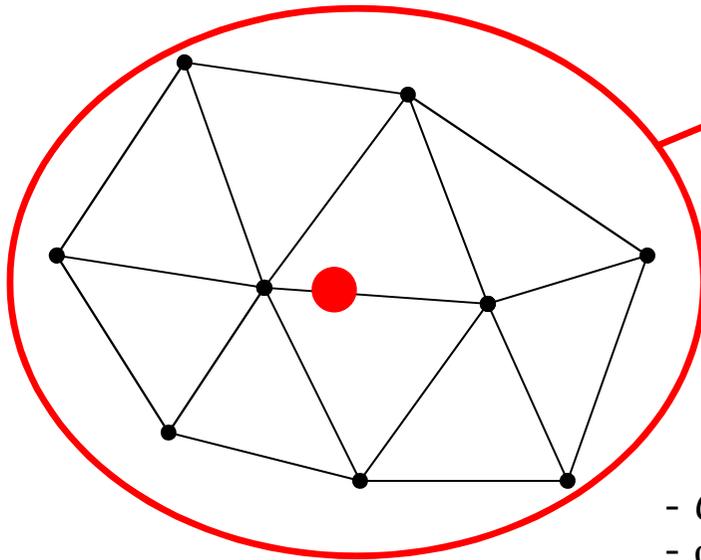
□ SUFT3D: Saturated – Unsaturated Flow and Transport in 3D

- Control volume finite element method (CVFE)
- For large scale applications
 - Flexible discretization / meshing approach
 - Progressive evolution to a OO approach + Full dynamic allocation of arrays
 - Mathematical models of various (increasing) complexities for flow and transport (Hybrid Mixing Cell Finite Element approach)

		TRANSPORT		
		<i>Simple Reservoir (Linear...)</i>	<i>Distributed Mixing Model</i>	<i>Advection- dispersion</i>
FLOW	<i>Simple Reservoir (Linear...)</i>	OK	impossible	impossible
	<i>Distributed Reservoir (Linear...)</i>	OK	OK	impossible
	<i>Flow in porous media</i>	OK	OK	OK

Mathematical and Numerical solutions

□ Simple (linear) reservoir



N nodes but 1 unknown
e.g. the mean water level
In the reservoir

$$Q_{res} = S A_{res} \frac{d\bar{H}}{dt} = -\alpha_{res} (\bar{H} - H_{ref}) + Q_{\pm}$$

- Q_{res} = Flow rate entering or leaving the reservoir
- α = recession coefficient
- H_{ref} = reference (drainage) level
- Q_{\pm} = lumped pumping rate in the reservoir

□ Ex: modelling a karstic basin of unknown geometry

Mathematical & Numerical Solutions

□ Distributed reservoir

- Generalization of the simple linear reservoir to the case of multiple interconnected reservoirs (along the 3 dimensions)

$$\frac{\partial V_{w,I}}{\partial t} = S A_{res,I} \frac{\partial H_I}{\partial t} = \sum_{J \in \eta_I} \alpha_{IJ} (H_J - H_I) + Q_I$$

- Reservoirs = FE control volumes

□ « Classical GW flow equation based on Darcy's law (CVFE formulation)

$$V_I \frac{\partial \theta_I}{\partial t} - \sum_{J \in \eta_I} (H_J - H_I) \int_V \underline{\nabla} N_I \cdot \underline{\underline{K}} \cdot \underline{\nabla} N_J dV - Q_I = 0$$

Mathematical & Numerical Solutions

- Simple (linear) reservoir for transport

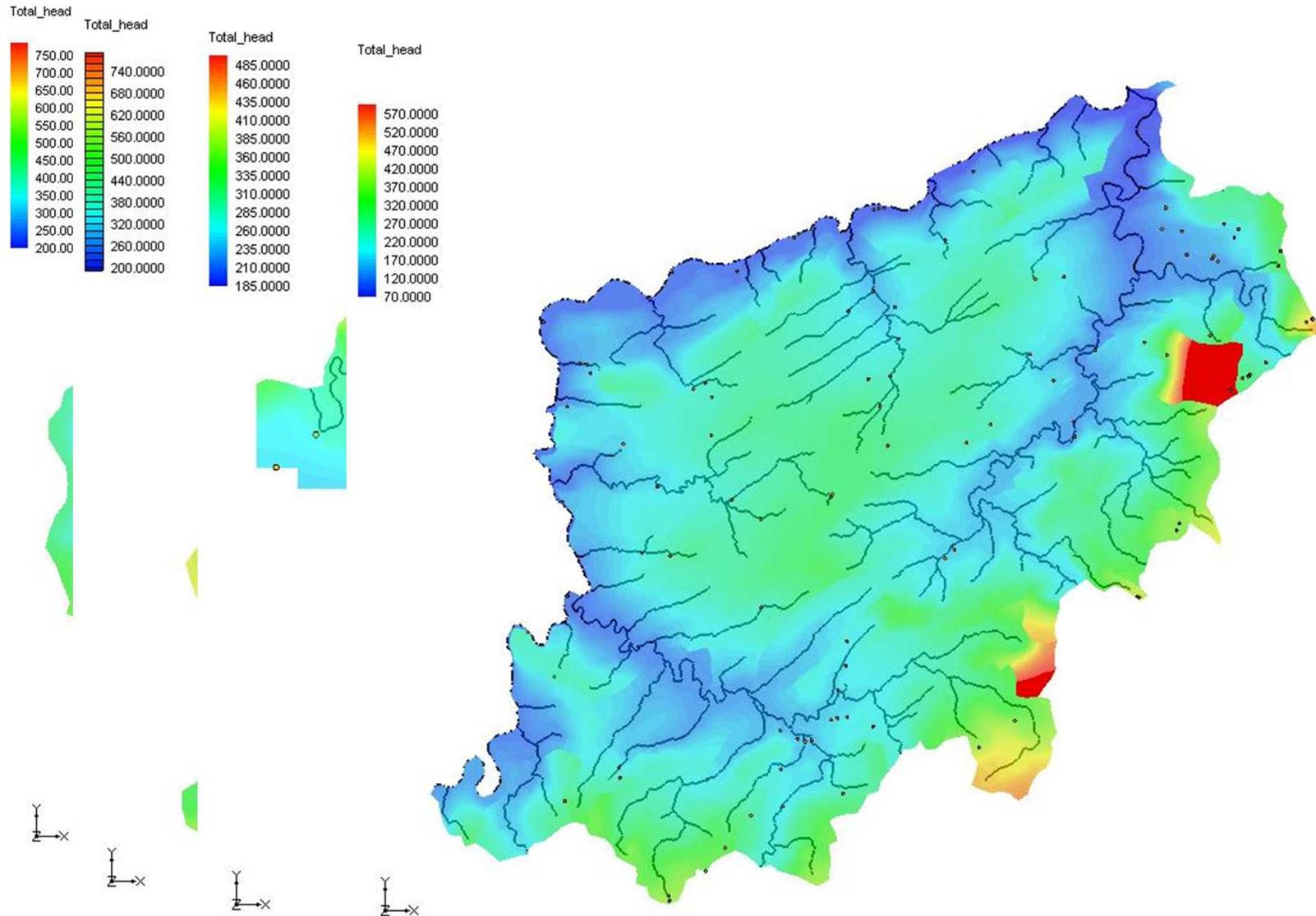
$$\frac{\partial(V_{eff,res} \bar{C})}{\partial t} = Q_{in} C_{in} - Q_{out} \bar{C}$$

- Distributed mixing cell approach

$$V_{res,I} \frac{\partial(\theta_I C_I)}{\partial t} - \sum_{J \in \eta_I} \alpha_{IJ} C_{ups}^{(I,J)} (H_J - H_I) - Q_{CI} = 0$$

- Unconditionnaly stable
 - Dispersion governed by the size of the mixing cells only; however, for diffuse pollution, the spatial dispersion of the source is dominant
- « Classical AD transport equation

Preliminary results for the Meuse basin



Perspectives & Conclusions

□ Further steps

- Finalize the coding of some concepts
- Calibration and validation for the Walloon region Meuse basin
- Integration in the integrated model

□ Possible applications

- Impact of land practices (e.g. agricultural manure) and contaminant trend forecasting (e.g. nitrates)
- Impact of climate changes on (ground)water resources at regional scale
- Modelling regional GW systems (isotopic data...)



Thank you!

Boundary conditions

□ External boundaries

- Recharge : Flux-type (Neumann) BC
- Pumping wells : Element-based source/sink
- Exchanges with rivers: Head dependent flux node/face (Cauchy) BC

□ Internal boundaries

- Nodal prescribed head or nodal/face head dependent (Cauchy) flux