

# The Arizona-Montréal Spectroscopic Survey of hot subluminescent stars★

M. Latour<sup>1,★</sup>, E. M. Green<sup>2</sup>, M. Dorsch<sup>3</sup>, V. Van Grootel<sup>4</sup>, P. Chayer<sup>5</sup>, S. Charpinet<sup>6</sup>,  
U. Heber<sup>7</sup>, S. K. Randall<sup>8</sup>, and X.-Y. Ma<sup>4</sup>

<sup>1</sup> Institut für Astrophysik und Geophysik, Georg-August-Universität Göttingen, Friedrich-Hund-Platz 1, 37077 Göttingen, Germany

<sup>2</sup> Steward Observatory, University of Arizona, 933 N. Cherry Avenue, Tucson, AZ 85721, USA

<sup>3</sup> Institut für Physik und Astronomie, Universität Potsdam, Haus 28, Karl-Liebknecht-Str. 24/25, 14476 Potsdam, Germany

<sup>4</sup> Space sciences, Technologies and Astrophysics Research (STAR) Institute, Université de Liège, 19C Allée du 6 Août, 4000 Liège, Belgium

<sup>5</sup> Space Telescope Science Institute, 3700 San Martin Drive, Baltimore, MD 21218, USA

<sup>6</sup> Institut de Recherche en Astrophysique et Planétologie, CNRS, Université de Toulouse, CNES, 14 Avenue Edouard Belin, 31400 Toulouse, France

<sup>7</sup> Dr. Karl Remeis-Observatory and Erlangen Centre for Astroparticle Physics, Friedrich-Alexander-Universität Erlangen-Nürnberg, Sternwartstr. 7, 96049 Bamberg, Germany

<sup>8</sup> ESO, Karl-Schwarzschild-Str. 2, 85748 Garching bei München, Germany

Received 19 September 2025 / Accepted 3 November 2025

## ABSTRACT

**Context.** Hot subdwarf B (sdB) and O (sdO) type stars are evolved helium-burning objects that lost their hydrogen envelope before the helium flash when their progenitors were close to the tip of the red giant branch (RGB). They populate the extreme horizontal branch (EHB) in the Hertzsprung-Russell diagram (HRD). The mass distribution of canonical hot subdwarfs is expected to peak at the core mass required for helium ignition under degenerate conditions in the 0.45–0.5  $M_{\odot}$  range. However, non-degenerate helium ignition from intermediate-mass progenitors and non-canonical pathways, such as the merger of helium white dwarfs and delayed helium flashes, are also expected to contribute to the hot subdwarf population.

**Aims.** Using high-quality, homogeneous spectra of 335 hot subluminescent star candidates from the Arizona-Montréal Spectroscopic Survey, we aim to improve our understanding of the atmospheric and stellar properties of hot subdwarf stars. Our focus is on the mass distribution of the different types of hot subdwarfs and their connections to the various formation scenarios.

**Methods.** We used large grids of model atmospheres to fit the observed spectra and derived their atmospheric parameters: effective temperature ( $T_{\text{eff}}$ ), surface gravity, and helium abundance. The model grids were further utilized to fit the spectral energy distribution of each star and the *Gaia* parallax was used to compute the stellar parameters radius, luminosity, and mass.

**Results.** Our spectroscopic sample mostly consists of H-rich sdBs and sdOs, but also contains 41 He-rich sdOs. Additionally, the sample includes 11 intermediate-helium stars and 19 horizontal branch objects with  $T_{\text{eff}} \geq 14$  kK. We detected the presence of helium stratification in six sdB stars with  $T_{\text{eff}}$  around 30 kK, making them good candidates for also showing  $^3\text{He}$  enrichment in their atmospheres. Our sdB distribution along the EHB shows a gap near 33 kK, visible in both the Kiel ( $\log g - T_{\text{eff}}$ ) diagram and HRD, corroborating previous observations and predictions. The mass distributions of H-rich sdBs and sdOs are similar and centered around 0.47  $M_{\odot}$ , consistent with the canonical formation scenario of helium ignition under degenerate conditions. Among the H-rich hot subdwarfs, we found no difference between the mass distributions of close binaries and apparently single stars. The He-sdOs have a significantly wider mass distribution than their H-rich counterparts, with an average mass of about 0.78  $M_{\odot}$ . In the HRD, the He-sdOs lie on the theoretical helium main sequence for masses between 0.6 and 1  $M_{\odot}$ . This strongly favors a merger origin for these He-rich objects. We identified a small number of candidate low-mass (<0.45  $M_{\odot}$ ) sdBs located below the EHB that might have originated from more massive progenitors. These low-mass sdBs preferentially show low helium abundances. Finally, we identified more than 80 pulsating stars in our sample and found that they fall into well-defined *p*- and *g*-mode instability regions.

**Key words.** stars: atmospheres – stars: fundamental parameters – Hertzsprung-Russell and C-M diagrams – stars: horizontal-branch – subdwarfs

## 1. Introduction

The majority of hot subdwarf B and O type stars (sdBs and sdOs) are evolved helium-burning objects that have been stripped of their hydrogen envelope before the helium flash, when their low-mass ( $\lesssim 2.3 M_{\odot}$ ) progenitors were at the tip of the red giant branch (RGB, Heber 2009, 2016, 2024, 2026). This is what is

referred to as the canonical formation scenario (Sweigart 1987; Dorman et al. 1993). Hot subdwarfs essentially sit at the very hot end of the horizontal branch and are also referred to as extreme horizontal-branch stars (EHB). The mass distribution of the canonical hot subdwarfs is expected to peak at the core mass required for helium ignition under degenerate conditions, which lies in the 0.45–0.5  $M_{\odot}$  range (Iben 1967; Sweigart 1987; Salaris & Cassisi 2005). The evolution of intermediate-mass progenitors ( $\gtrsim 2.3 M_{\odot}$ ), igniting core-He burning under non-degenerate

\* Dedicated to the memory of Prof. Gilles Fontaine.

\*\* Corresponding author: marilyn.latour@uni-goettingen.de

conditions, is expected to produce lower core and total masses, down to  $\sim 0.33 M_{\odot}$  (Montalbán & Noels 2013; Noels-Grotsch & Miglio 2025). The part of the Hertzsprung-Russell diagram (HRD) where hot subdwarfs are located can also be crossed by stars in other evolutionary phases, such as low-mass post asymptotic giant branch (post-AGB, Heber 1991) stars and stars cooling down as He-core white dwarfs (WDs, Driebe et al. 1998; Istrate et al. 2016). More exotic stellar products, resulting from (among other possibilities) the merger of two He-core WDs, can also end up as core-He burning objects and be found close to the EHB and the adjacent helium main sequence in the HRD (Webbink 1984; Saio & Jeffery 2002).

One way to disentangle the various evolutionary phases populating the HRD in the hot subdwarf region is via the masses of the stars. However, precise stellar mass measurements independent of evolutionary tracks can readily be obtained only for certain special cases, such as eclipsing binary systems. For hot subdwarfs, it has also been possible to derive accurate masses from asteroseismology for pulsating sdBs (Charpinet et al. 2002, 2005b) and through light curve modeling coupled with spectroscopic observations for close binaries exhibiting eclipses, reflection effects, or ellipsoidal deformations (Vučković et al. 2007; For et al. 2010). A compilation of literature masses derived for 22 hot subdwarf pulsators and binaries led to a first empirical mass distribution for hot subdwarfs, peaking at  $0.47 M_{\odot}$  with a narrow range of  $0.44\text{--}0.50 M_{\odot}$  containing 68% of the stars (Fontaine et al. 2012). This aligned very well with the expectations from canonical stellar evolution theory. Moreover, the seismic models obtained for the 14 pulsators in the sample yielded predicted distances in good agreement with the parallaxes from the second *Gaia* data release (Fontaine et al. 2019).

The availability of accurate parallaxes, and thus distances, for most of the nearby ( $\lesssim 3$  kpc) hot subdwarfs from the third *Gaia* data release (EDR3, Gaia Collaboration 2021) has finally enabled the mass to be estimated for large samples of hot subdwarfs based on the fit of their spectral energy distribution (SED). However, this requires a few additional key ingredients: observed magnitudes in different filters, theoretical model grids to compute the expected flux in these filters, and reliable estimates of the atmospheric parameters of the star; most notably, the effective temperature and surface gravity (Heber et al. 2018). Mass distributions obtained from a combination of spectroscopic analysis, parallaxes, and SED fits for a large sample of hot subdwarfs were first presented in Lei et al. (2023) using LAMOST spectra. While the authors found an average mass ( $\sim 0.47 M_{\odot}$ ), in line with the theoretical expectations for their hydrogen-rich sdBs, their distribution is very broad, extending from  $0.2$  to  $1.0 M_{\odot}$ . Their mass distribution for hydrogen-rich sdO masses revealed itself to be unrealistically flat, with a very low mean mass of  $0.36 M_{\odot}$ . Similarly, the mass estimates of hot subdwarfs in globular clusters, whose distances are relatively well constrained by methods other than parallax measurements, remain systematically lower than expected, despite significant improvements in model atmospheres and data obtained over the years (see, e.g., Moni Bidin et al. 2011; Latour et al. 2018). We note that most of the dispersion seen in the mass distributions from parallaxes and SED fits in the literature is due to the uncertainty on the atmospheric parameters (rather than intrinsic to the stars themselves). In particular, this is the case for the surface gravity, which dominates the error budget in the mass determination.

Atmospheric parameters derived from high-quality and homogeneous spectroscopic samples are crucial for minimizing the scatter in the masses derived from parallaxes and SED fits

and yielding distributions of sufficient quality for a meaningful comparison to predictions from different formation scenarios and population synthesis models (Han et al. 2002, 2003). This is what we aim to do with our samples of hot subdwarf spectra from the Arizona-Montréal spectroscopic program, whose early results were reported in conference proceedings (Green et al. 2004, 2005, 2008; Fontaine et al. 2014). The spectroscopic data consist of two samples with different wavelength coverage and resolution. The larger sample, which we refer to as the Bok sample, comprises spectra for 335 stars obtained at the 2.3m Bok telescope at the Kitt Peak observatory. The second sample consists of spectra for a subset of 116 stars (all from the Bok sample), observed with the MMT telescope. This sample is referred to as the MMT sample. All of these high-quality Bok and MMT spectra were fit with synthetic model spectra to estimate their atmospheric parameters: effective temperature ( $T_{\text{eff}}$ ), surface gravity ( $\log g$ ), and helium abundance ( $\log N(\text{He})/N(\text{H})$ ). The atmospheric parameters were then used, along with the *Gaia* parallaxes and magnitudes from various photometric surveys, to perform SED fits and derive the stellar parameters: radius ( $R$ ), luminosity ( $L$ ), and mass ( $M$ ).

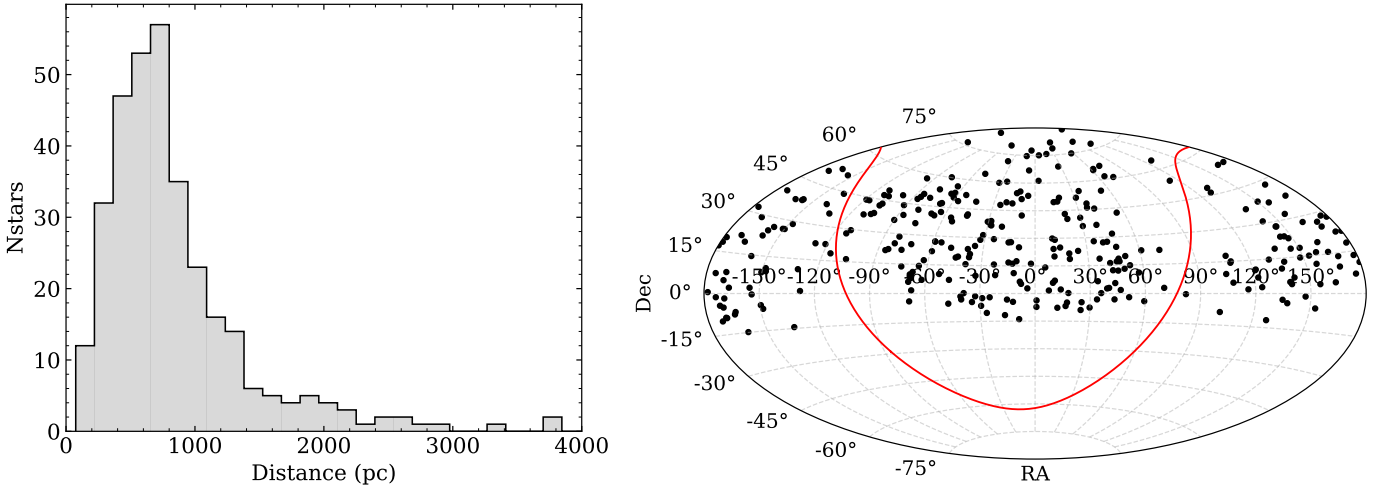
We present the results of our work as follows. Sections 2 and 3 include the description of our observational material and analysis methods. Section 4 gives the results of our spectroscopic and SED fits for the Bok and MMT samples separately. In the discussion (Sect. 5), we focus on the mass distributions (Sects. 5.1 to 5.3) and examine the properties of the pulsating hot subdwarfs included in our sample in Sect. 5.4. Finally, a summary of our work and our main conclusions are presented in Sect. 6.

## 2. Observational material

### 2.1. Low-resolution Bok spectra

Low-resolution spectra for 335 hot subluminal star candidates were obtained by one of us (E. M. Green) as part of a project aiming to better characterize the hot subdwarf population (Green et al. 2008). The stars were selected as relatively bright ( $V \lesssim 14.5$ ) blue objects visible from Arizona. They were mainly identified from early small-scale surveys of blue objects, such as Palomar-Green (Green et al. 1986), Feige (Feige 1958), and Kitt Peak Downes (Downes 1986). All objects, except for the sdB binary NGC 188 2019 (Sandage 1962; Green et al. 2005), are members of the galactic field. The distances derived from the *Gaia* EDR3 parallaxes and the sky distribution of these 335 stars are shown in Fig. 1.

The spectra were obtained at the Bok 2.3m telescope of the Steward Observatory on Kitt Peak, mainly between 1999 and 2004. The standard setup for the spectroscopic survey was to use the Boller & Chivens Cassegrain spectrograph with the  $400 \text{ mm}^{-1}$  first-order grating with a  $2.5''$  slit. This results in a typical resolution of  $9 \text{ \AA}$  over the wavelength interval  $3620\text{--}6900 \text{ \AA}$ . Before each exposure, the instrument rotator was set to align with the parallactic angle. HeAr comparison spectra were taken immediately following the stellar exposures. The spectra were bias-subtracted, flat-fielded, background-subtracted, optimally extracted, wavelength-calibrated, and flux-calibrated using standard IRAF (Tody 1986, 1993) tasks. The flux calibration was performed using observations of the standard stars Feige 34 or BD+28°4211. All individual spectra were also corrected for heliocentric velocities. The number of observations per object varies from star to star but is typically between one and ten. For stars with more than one observation, the



**Fig. 1.** Distance and sky distribution of the stars in the Bok sample. Six objects are located beyond 4000 pc, but they are all most likely MS B-type stars (see Sect. 4.1.2). The red line indicates the position of the galactic plane on the sky projection.

radial velocity (RV) was measured via cross-correlation with the highest signal-to-noise (S/N) spectrum for each given star. The spectra were then aligned in radial velocity prior to being combined into a single spectrum. We note that this way of extracting the RV is independent of synthetic spectra but provides only relative, rather than absolute, RVs. Except for a few faint objects, the S/N values of the final spectra lie in the range 100–500. The median S/N of the sample is 197.

## 2.2. Medium-resolution MMT spectra

Additional medium-resolution spectra were obtained for a subset of 116 stars in the Bok sample by one of us (E.M.G.) with the blue spectrograph attached to the 6.5 m MMT telescope, between 1996 and 2003 as part of a radial velocity program (Green et al. 2004, 2005). Throughout the observing seasons, the same experimental setup was consistently used: the  $832 \text{ mm}^{-1}$  grating in second order and a  $1''$  slit that provided a resolution  $R$  of  $\sim 4250$  ( $1.0 \text{ \AA}$ ) over a wavelength range of  $4000\text{--}4950 \text{ \AA}$ . The spectra were reduced and combined in the same way as those obtained with the Bok telescope.

The MMT sample consists of hydrogen-rich sdBs and sdOs cooler than 45 kK. Again, a number (between two and eight) of individual spectra were combined. The S/N for the combined spectra typically ranges from 100 to 200. Exposure times were mostly kept below 15 min and depended on the brightness of the star. Fig. E.1 shows our MMT spectral atlas: the combined spectrum for each star, ordered by increasing effective temperature.

## 2.3. Light curves

Most of the stars in the MMT sample were also observed as part of a photometric monitoring campaign (see Green et al. 2003, 2004) by one of us (E.M.G.) at the 1.6 m Kuiper Telescope at Mount Bigelow (Steward Observatory) and at the 2.3 m Telescope on Kitt Peak with conventional 2K CCDs binned  $3 \times 3$  ( $0.45'' \text{ pixel}^{-1}$ ). Integration times were kept short, between 10 and 60 s, depending on the brightness of the target. The stars were typically observed for a total duration of 2–20 hours. Differential magnitudes were derived from aperture photometry of the

sdB relative to reference stars of comparable magnitude within each frame. As a result of these observations, we have information on the pulsation properties for all but six stars in the MMT sample, and can classify them as rapid ( $p$ -mode), slow ( $g$ -mode) or hybrid pulsators, or non-pulsating objects.

Given that these ground-based observations date from earlier than 2005, many of the targets have since also been monitored for variability from space. We cross-checked our information from the ground-based data with the light curves obtained from the Transiting Exoplanet Survey Satellite (TESS, Ricker et al. 2014). For all stars in our Bok sample, we retrieved and examined, when available, the Lomb-Scargle Periodograms of the TESS data, using our dedicated software FELIX (Charpinet et al. 2010; Zong et al. 2016), to search for pulsation signals. In addition, we searched for pulsators among the list of sdB pulsators from the Kepler extended K2 mission (W. Zong, priv. commun.) and the literature compilation of pulsators made by Uzundag et al. (2024). In total, we identified 22  $p$ -mode pulsators, 53  $g$ -mode pulsators, and nine hybrid pulsators in our sample. The light curves of 201 stars did not show any signal that could be associated with  $p$ - or  $g$ -modes pulsations and we classified them as non-pulsating. Finally, 44 stars did not have any TESS light curves and their pulsation status was unknown. The pulsating stars and their properties are further discussed in Sect. 5.4.

## 3. Analysis methods

### 3.1. Atmospheric parameters

Our samples include a large variety of hot subluminal stars, from cool blue horizontal branch (BHB) stars to extremely helium-enhanced sdO stars. To cover all the atmospheric parameter ranges of these stars, two different types of model atmospheres were used.

For the spectral fit of the hydrogen-rich hot subdwarfs and BHB stars, we used the grids of hybrid LTE and NLTE models that have been used in similar studies (e.g., Geier et al. 2024, Dawson et al. 2026, Heber et al., in prep.). The model grid extends from 9 kK to 75 kK, from  $\log g = 3.0\text{--}7.0$ , and from  $\log N(\text{He})/N(\text{H}) = -5.0\text{--}2.5$ . The lower limit on the surface gravity gradually increases to  $\log g = 5.25$ , for models at 75 kK,

with increasing effective temperature, following the Eddington limit (see Heber et al., in prep., for a figure showing the grid coverage). The models are constructed using the combination of ATLAS12/DETAIL/SURFACE (ADS) codes. ADS is a hybrid LTE/NLTE method, which was first developed by Przybilla et al. (2006) and Nieva & Przybilla (2007) and further improved by Przybilla et al. (2011) and Irrgang et al. (2014, 2018, 2021, 2022). The improvements include a proper treatment of level dissolution for hydrogen (Hubeny et al. 1994) and the implementation of the Stark broadening line profiles of hydrogen and He I (Tremblay & Bergeron 2009; Beauchamp et al. 1997). The synthetic spectra are obtained by running the three codes mentioned above in succession. First, a LTE line-blanketed, plane-parallel, homogeneous, and hydrostatic model atmosphere is calculated using ATLAS12 (Kurucz 1996). The LTE atmospheric structure is then used by DETAIL (Giddings 1981; Butler & Giddings 1985) to calculate the population numbers of hydrogen and helium (Przybilla & Butler 2004; Przybilla 2005) assuming NLTE and appropriate model atoms. The other chemical species are treated in LTE. In this work, we use metal abundances that reflect the typical abundance patterns of hot subdwarfs (see e.g., Blanchette et al. 2008; Pereira 2011; Naslim et al. 2013). Most notably, iron-peak elements are enhanced by a factor of 10 with respect to solar, except iron itself, which is kept at the solar value. The final synthetic spectra are computed with SURFACE (Giddings 1981; Butler & Giddings 1985) and include only lines of hydrogen and helium.

The second type of model atmospheres we used are tailored to the helium-enhanced objects. These models were used in Dorsch (2024) and are described in their Sect. 2.2. The model atmospheres and synthetic spectra were computed with TLUSTY, version 205, and SYNSPEC, version 51 (Hubeny & Lanz 2011a,b, but see also Hubeny & Lanz 2017a,b,c for the specificity of the versions used here), respectively. They are NLTE models that include line-blanketing from C, N, O, Ne, Si, P, S, Fe, and Ni. The abundances are set to the solar values (Asplund et al. 2009) except for C ( $2\times$  solar), O ( $0.1\times$  solar), Ne ( $2\times$  solar), Fe ( $1.5\times$  solar), and Ni ( $10\times$  solar), which roughly represent the abundance patterns of most helium-enriched hot subdwarfs. Specific improvements were made in SYNSPEC regarding the treatment of He I, the most important being the consideration of Stark broadening following the line profiles calculated by Beauchamp et al. (1997) and implemented in SYNSPEC by Bédard et al. (2020). For the He I lines at  $4472 \text{ \AA}$  and  $4922 \text{ \AA}$ , the Stark profiles of Gigosos & González (2009) and Lara et al. (2012) were used. The grid extends from  $T_{\text{eff}} = 25$  to  $65 \text{ kK}$ , from  $\log g = 3.0$  to  $6.5$  and from  $\log N(\text{He})/N(\text{H}) = -1.75$  to  $+4.0$ . However, the lower limit on the surface gravity gradually reaches  $\log g = 4.5$  (for models at  $65 \text{ kK}$ ) as the effective temperature increases, following the Eddington limit.

The atmospheric parameters, namely  $T_{\text{eff}}$ ,  $\log g$ , and  $\log N(\text{He})/N(\text{H})$ , were derived for each stellar spectrum using a full spectral fit to one of the model grids described above. The fit to a given star is not restricted to one specific grid, instead, the best-fit solution can be found in either of the two grids, as long as the parameters do not lie on the grid's edge. These fits were performed using the Interactive Spectral Interpretation System (ISIS, Houck & Denicola 2000) with a modified version of the  $\chi^2$  minimization method presented by Irrgang et al. (2014). The spectral continuum was modeled using a spline with anchor points spaced every  $100 \text{ \AA}$ , but avoiding the hydrogen and helium lines. This continuum spline was fitted simultaneously with the atmospheric parameters, which is necessary to account for correlations.

### 3.2. Spectral energy distribution and stellar parameters

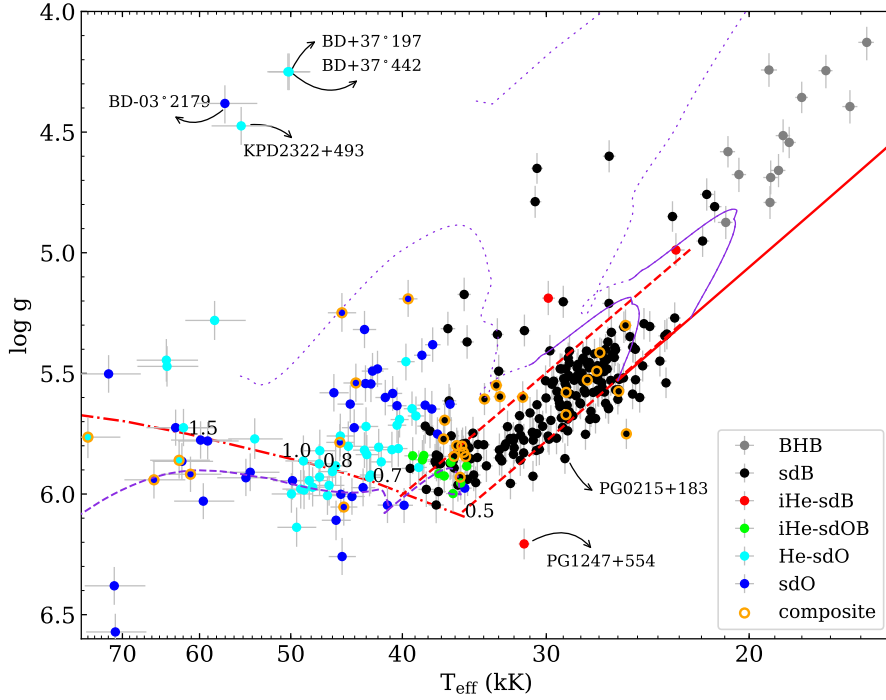
To complement the spectral analysis, we also derive the stellar radius, luminosity, and mass for each star by performing a fit of its SED combined with the *Gaia* parallax. The method was first described in Heber et al. (2018) and is explained in more detail in Sect. 2.3 of Dorsch (2024). Here we briefly summarize the main points. For each star, observed magnitudes are queried via a table access protocol (TAP) using the Astronomical Data Query Language (ADQL). This way, many photometric surveys can be queried through the Vizier database or other databases such as the Astro Data Lab (Fitzpatrick et al. 2014). Some of the major surveys providing magnitudes for the stars in our sample are Sloan Digital Sky Survey (SDSS, Alam et al. 2015), Two Micron All Sky Survey (2MASS, Skrutskie et al. 2006), Pan-STARRS DR2 (Flewelling 2018), GALEX (Bianchi et al. 2017), and *Gaia* (Gaia Collaboration 2021). Also, relevant here are the *Gaia* DR3 photometric low-resolution spectra (De Angeli et al. 2023) that were used to construct a sequence of 14 box filters. An exhaustive list of the photometric catalogs queried is presented in Culpán et al. (2024).

During the SED fit procedure, the distance to the star was kept fixed to the value derived from the *Gaia* EDR3 parallax ( $\varpi$ ). We corrected the parallax for its zero-point offset following Lindegren et al. (2021) and inflate the corresponding uncertainty using the function suggested by El-Badry et al. (2021). The effective temperature,  $\log g$ , and helium abundance of the star are fixed to the value obtained from the spectroscopic fit of the Bok spectra. Thus, the only parameters left to optimize are the angular diameter,  $\Theta = 2R/D$ , or in terms of the parallax,  $\Theta = 2\varpi R$ , as well as the interstellar color excess,  $E(44-55)$ <sup>1</sup>. To account for the interstellar extinction, we used the functions of Fitzpatrick et al. (2019) and adopted the standard parameter  $R(55)=3.02$ . The model atmospheres used to compute the synthetic fluxes in the various photometric passbands are the same as used for the spectroscopic fits, meaning the emergent flux from ATLAS12 and TLUSTY, including metal lines. From the value of  $\Theta$ , we directly obtained the radius,  $R$ , of the star and we compute the luminosity and the mass via the formulae,

$$L = 4\pi R^2 \sigma T_{\text{eff}}^4 \quad \text{and} \quad M = \frac{gR^2}{G}.$$

All uncertainties are propagated using the Monte Carlo method. The resulting best-fit values (for  $R$ ,  $L$ ,  $M$ ) are stated as the median with the 68% ( $1\sigma$ ) uncertainties. For these computations, we included systematic uncertainties, alongside the statistical uncertainties, for the spectroscopic  $T_{\text{eff}}$  and  $\log g$  measurements, adding them in quadrature following the prescription detailed in Dawson et al. (2026). The authors used their spectroscopic observations of hot subdwarfs within 500 pc to characterize the systematic uncertainties arising from three sources: variability in data reduction, offsets between different instruments, and the choice of metallicity in the model atmospheres used to fit the spectra. As a result, they provided third-order polynomial functions to evaluate systematic uncertainties as a function of  $T_{\text{eff}}$  for the three atmospheric parameters ( $T_{\text{eff}}$ ,  $\log g$ , and  $\log N(\text{He})/N(\text{H})$ ). The systematic uncertainties are about 0.07 dex for  $\log g$  and 1.5% for  $T_{\text{eff}}$ , although the uncertainty

<sup>1</sup>  $E(44-55)$  is analogous to  $E(B-V)$ , but with the monochromatic measures of the extinction at  $4400$  and  $5500 \text{ \AA}$  substituting for measurements with the  $B$  and  $V$  filters. Conversion factors to the  $UBV$  systems are given in Table 4 of Fitzpatrick et al. (2019). They are close to 1 for hot stars.



**Fig. 2.** Surface gravity ( $\log g$ ) as a function of  $T_{\text{eff}}$  (Kiel diagram) for the stars in the Bok sample. The six spectral groups are indicated with symbols of different colors. Stars with IR excess are marked with an additional orange circle (see Sect. 4.1.2). The ZAEHB and TAEHB computed with STELUM for a core mass of  $0.47 M_{\odot}$  are shown with red dashed lines. The ZAEHB extension below 20 kK (solid red line) is from BaSTI models. Two BaSTI evolutionary tracks are shown in purple, the solid part represents the core-He burning phase, while the dotted part is the post-EHB phase. The dashed purple track is from a late-flasher model. The dashed-dotted red line is the ZAHAMS with the stellar masses indicated along the line. References for the theoretical models are listed in Sect. 4.1.1.

on  $T_{\text{eff}}$  steadily increases to 5% for stars hotter than 40 kK. The surface gravity is typically the atmospheric parameter with the largest uncertainty and is also more affected by systematics (e.g., from fitting different spectra of the same star, see Dawson et al. 2026). Because the stellar parameters  $R$  and  $L$  do not strongly depend on  $\log g$ , they can be relatively well constrained, provided that the *Gaia* parallax is well determined. On the other hand, because  $M$  depends linearly on the surface gravity, we are typically left with rather large uncertainties on the masses derived from the combination of spectroscopy, SED fits, and parallaxes ( $\sim 16$ – $20\%$ ; see Sect. 5).

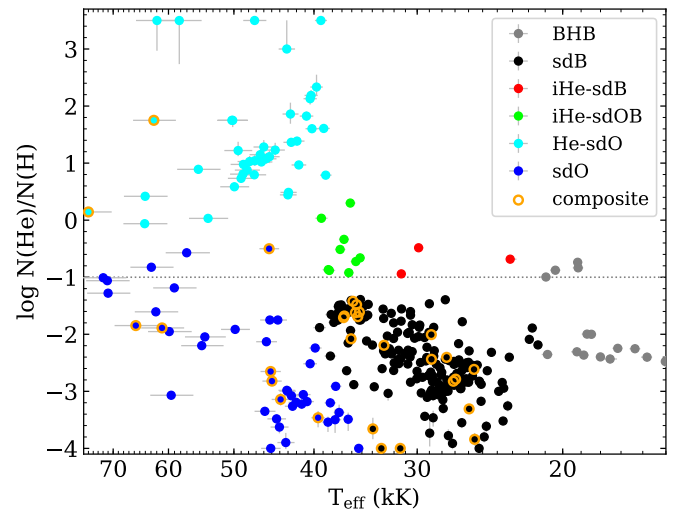
For some of our targets, the SED fit indicates an IR excess, attributed to the target being a binary system with a cool companion that is bright enough to emit more IR flux than the hot subdwarf itself (see Appendix A). This is typically the case for main sequence companions earlier than spectral type M. In such cases, we fit the flux contribution of the companion with synthetic spectra for main sequence stars from the Göttingen spectral library (Husser et al. 2013) by including two additional parameters: the surface ratio  $A_{\text{MS}}/A_{\text{sd}}$  between the MS companion and the hot subdwarf and  $T_{\text{eff}}$  of the companion. We assume the companion star to have a  $\log g$  typical of MS stars ( $\log g = 4$ ) and a metallicity of  $[\text{Fe}/\text{H}] = -0.3$ , which is a mean value for the F/G/K-type companions (Vos et al. 2018).

## 4. Results

### 4.1. The Bok sample

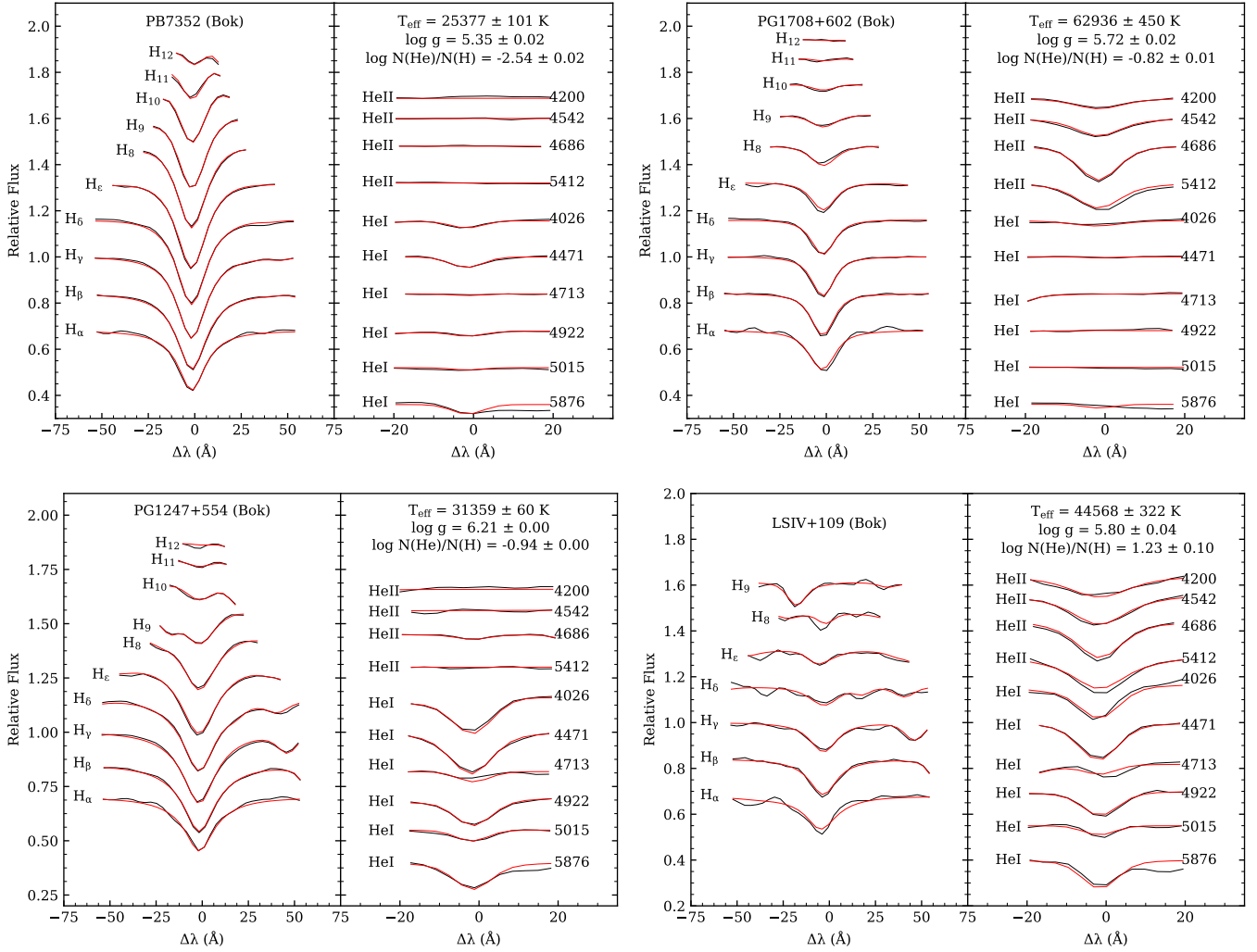
#### 4.1.1. Atmospheric parameters

All of the Bok spectra were fit following the method described in Sect. 3.1. From the inspection of the spectral fits, five peculiar objects stood out and were removed from the sample because their spectra could not be modeled adequately. They are listed in Appendix B and their spectra are shown in Fig. B.1. In Figs. 2 and 3, we show the distribution of the hot subdwarfs



**Fig. 3.** Helium abundance as a function of  $T_{\text{eff}}$  for the stars in the Bok sample. The spectral groups are indicated following the same color scheme as in Fig. 2. The solar helium abundance is indicated with the dotted line.

from the Bok sample in the  $T_{\text{eff}}-\log g$  plane (hereafter Kiel diagram) and in the  $T_{\text{eff}}-\text{He}$  plane. Given the low resolution of the Bok spectra, the helium abundance in the most He-poor stars ( $\log N(\text{He})/N(\text{H}) \sim -4$ ) should be considered as an upper limit. Figure 4 shows the Bok spectrum and best-fitting model for four stars of various  $T_{\text{eff}}$  and helium abundances. The best fit for all stars in the Bok sample are available as supplementary figures online (see Data availability paragraph). The atmospheric parameters obtained for all stars in the Bok sample are listed in Table D.1. This table also includes the stellar parameters obtained from the parallax and SED fits, as well as additional information on the pulsation and binary properties of each star. An extended version of Table D.1, with additional columns, is



**Fig. 4.** Bok spectrum (black) and best fit solution (red) for four stars in our sample. PB7352 is a typical hydrogen-rich sdB and PG1708+602 is a hot sdO. PG1247+554 is an iHe-sdB located below the EHB in the Kiel diagram. LSIV+10<sup>4</sup> is a He-sdO where the He II Pickering series blends with the Balmer lines.

only available online at the CDS (see Data availability paragraph). In Table 1, we present an excerpt of Table D.1 for 15 stars.

**Evolutionary models.** On the Kiel diagram (Fig. 2) and some other figures in this work, we include evolutionary tracks that we describe here. The zero-age and terminal-age extreme horizontal branches (respectively ZAEHB and TAEHB) shown in Figs. 2, 5, and 6 are those predicted from static stellar models computed with STELUM for a fixed core mass of  $0.47 M_{\odot}$  and various hydrogen envelope thicknesses (see Baran et al. 2024 and Sect. 5.2 for a detailed description of the models). We extended the ZAEHB to the cooler HB region with a model taken from the BaSTI database (Hidalgo et al. 2018)<sup>2</sup> for solar metallicity. Two EHB evolutionary tracks from BaSTI and one late flasher model track (Miller Bertolami et al. 2008) are also included. The two BaSTI tracks show that the cooler sdBs, having a thicker hydrogen envelope, decrease in  $\log g$  during their post-EHB evolution. In contrast, sdBs at the hot end of the EHB, modeled as the products of a delayed helium flash, have very little hydrogen envelope left and evolve towards hotter temperatures at almost constant  $\log g$  (see also Xiong et al. 2017). Finally, we also indicate the

zero age helium main sequence (HeZAMS, Paczyński 1971) that is located at the hot end of the EHB.

**Spectral classification.** We divided the stars into different groups based on their helium abundance and effective temperature, following the classification presented in Fig. 4.1.4 of Dorsch (2024). Besides bona fide hot subdwarf stars, our sample also includes some cooler objects that are mostly BHB stars, with ten potential main sequence (MS) B stars<sup>3</sup> (see Sect. 4.1.2). Our classification uses the following categories (see also Fig. 3): BHB for the cooler HB objects ( $T_{\text{eff}} < 21$  kK), sdB and sdO for the objects that have an hydrogen-rich atmosphere, iHe-sdOB and iHe-sdB for the few intermediate-helium objects with  $\log N(\text{He})/N(\text{H})$  between about  $-1.0$  and  $0.6$ , and, finally, He-sdOs for the hot stars ( $T_{\text{eff}} \geq 38$  kK) with a helium dominated atmosphere.

The solar helium abundance has been traditionally used as a divide between helium-poor and helium-rich sdBs, however from our distribution we see that the helium abundances in none of our sdBs reach the solar value. Instead, the abundances clearly plateau at about  $\log N(\text{He})/N(\text{H}) = -1.4$ . This plateau of the sdB helium abundances is also conspicuous among the 500 pc sample (Dawson et al. 2026) and consistent with the early results

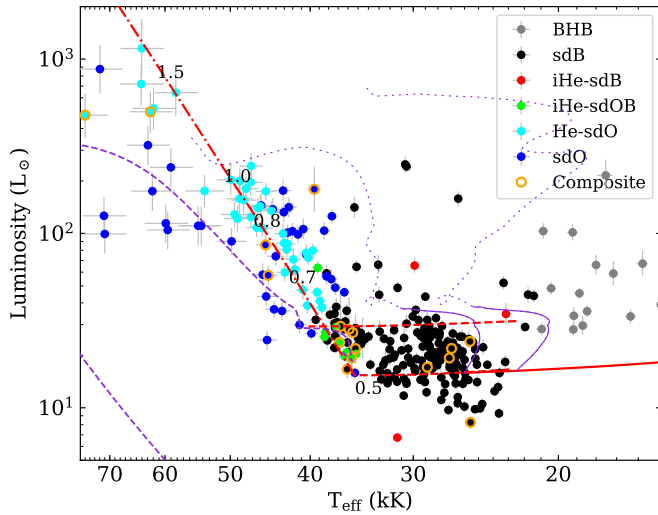
<sup>2</sup> <http://basti-iac.oa-teramo.inaf.it/>

<sup>3</sup> These are not included in the figures.

**Table 1.** Excerpt from the table of results for 15 stars.

Star	Type	$T_{\text{eff}}$ (K)	$\log g$ ( $\text{cm s}^{-2}$ )	$\log N(\text{He})/N(\text{H})$	$R$ ( $R_{\odot}$ )	$L$ ( $L_{\odot}$ )	$M$ ( $M_{\odot}$ )	IR-excess	<i>Gaia</i> ruwe	Pulsation	Binarity
PG0001+275	sdB	27 019 $^{+42}_{-74}$	5.58 $^{+0.01}_{-0.01}$	-2.85 $^{+0.03}_{-0.03}$	0.187 $^{+0.005}_{-0.004}$	16.9 $^{+1.1}_{-1.0}$	0.48 $^{+0.08}_{-0.07}$	No	1.01	g	Binary
PG0004+133	sdB	28 650 $^{+71}_{-149}$	5.46 $^{+0.01}_{-0.01}$	-1.88 $^{+0.02}_{-0.02}$	0.204 $^{+0.004}_{-0.004}$	25.2 $^{+1.5}_{-0.6}$	0.43 $^{+0.07}_{-0.06}$	No	0.93	No	Binary
PG0009+036	MS-B	18 698 $^{+188}_{-221}$	4.55 $^{+0.03}_{-0.03}$	-1.90 $^{+0.04}_{-0.03}$	1.884 $^{+0.392}_{-0.283}$	390.3 $^{+182.4}_{-110.5}$	4.66 $^{+2.37}_{-1.43}$	No	1.01	...	...
PG0011+221	sdO	42 039 $^{+179}_{-176}$	5.48 $^{+0.02}_{-0.02}$	-3.19 $^{+0.05}_{-0.05}$	0.191 $^{+0.007}_{-0.007}$	103.1 $^{+12.1}_{-10.8}$	0.41 $^{+0.08}_{-0.07}$	No	0.97	No	Binary
PG0011+283	sdB	24 742 $^{+152}_{-176}$	5.47 $^{+0.02}_{-0.01}$	-3.61 $^{+0.08}_{-0.09}$	0.176 $^{+0.004}_{-0.004}$	10.5 $^{+0.8}_{-0.7}$	0.33 $^{+0.06}_{-0.05}$	No	0.68	g	Single
PG0014+068	sdB	35 638 $^{+102}_{-178}$	5.93 $^{+0.02}_{-0.02}$	-1.62 $^{+0.02}_{-0.02}$	0.116 $^{+0.018}_{-0.014}$	19.5 $^{+6.6}_{-4.5}$	0.42 $^{+0.16}_{-0.11}$	Yes	1.15	p	...
PG0032+247	sdO	38 221 $^{+147}_{-159}$	5.63 $^{+0.02}_{-0.02}$	-3.20 $^{+0.07}_{-0.07}$	0.172 $^{+0.008}_{-0.008}$	56.7 $^{+6.9}_{-6.0}$	0.46 $^{+0.10}_{-0.08}$	No	0.99	...	Single
PG0033+266	sdB	26 706 $^{+158}_{-108}$	5.58 $^{+0.02}_{-0.02}$	-2.45 $^{+0.03}_{-0.03}$	0.182 $^{+0.007}_{-0.007}$	15.2 $^{+1.4}_{-1.3}$	0.46 $^{+0.08}_{-0.07}$	No	1.11	No	Single
PG0039+135	He-sdO	47 860 $^{+145}_{-156}$	5.97 $^{+0.03}_{-0.03}$	1.03 $^{+0.08}_{-0.06}$	0.195 $^{+0.008}_{-0.007}$	180.6 $^{+30.2}_{-26.3}$	1.31 $^{+0.29}_{-0.24}$	No	0.95	No	...
PG0057+155	sdB	34 736 $^{+65}_{-72}$	5.75 $^{+0.01}_{-0.01}$	-1.68 $^{+0.01}_{-0.01}$	0.143 $^{+0.003}_{-0.003}$	26.9 $^{+1.7}_{-1.0}$	0.42 $^{+0.07}_{-0.06}$	No	1.03	No	Single
PG0101+039	sdB	27 108 $^{+151}_{-72}$	5.53 $^{+0.01}_{-0.01}$	-2.75 $^{+0.03}_{-0.03}$	0.187 $^{+0.004}_{-0.004}$	17.0 $^{+1.0}_{-1.0}$	0.43 $^{+0.07}_{-0.06}$	No	0.85	g	sd+WD
PG0105+276	He-sdO	64 031 $^{+800}_{-710}$	5.47 $^{+0.04}_{-0.04}$	0.42 $^{+0.03}_{-0.00}$	0.275 $^{+0.046}_{-0.035}$	1150.5 $^{+546.4}_{-357.0}$	0.82 $^{+0.36}_{-0.23}$	No	0.94	...	...
PG0108+195	sdO	45 672 $^{+284}_{-326}$	6.11 $^{+0.03}_{-0.03}$	-2.13 $^{+0.05}_{-0.05}$	0.122 $^{+0.006}_{-0.005}$	58.0 $^{+9.1}_{-8.1}$	0.69 $^{+0.16}_{-0.13}$	No	0.93	No	Single
PG0123+159	sdB	29 215 $^{+104}_{-133}$	5.62 $^{+0.02}_{-0.02}$	-2.41 $^{+0.03}_{-0.04}$	0.185 $^{+0.008}_{-0.007}$	22.4 $^{+2.2}_{-1.9}$	0.52 $^{+0.10}_{-0.08}$	No	1.09	No	Single
PG0133+114	sdB	29 112 $^{+104}_{-145}$	5.68 $^{+0.01}_{-0.02}$	-2.43 $^{+0.02}_{-0.02}$	0.155 $^{+0.005}_{-0.005}$	15.5 $^{+1.3}_{-1.2}$	0.42 $^{+0.07}_{-0.06}$	No	0.83	No	sd+WD

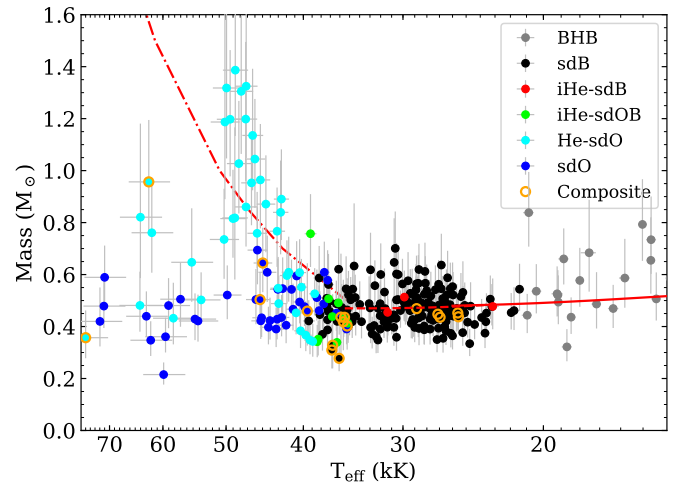
**Notes.** Uncertainties on the atmospheric parameters ( $T_{\text{eff}}$ ,  $\log g$ , and,  $\log N(\text{He})/N(\text{H})$ ) are only statistical.



**Fig. 5.** Luminosity of our stars versus their  $T_{\text{eff}}$  (essentially the HRD). The different spectral types are color-coded as in the previous figures. We indicate the composite objects with an additional orange circle around the symbols. The evolutionary tracks are the same as in the Kiel diagram (Fig. 2). The four luminous post-AGB stars noted in Sect. 4.1.1 are outside the luminosity range shown here.

of Edelman et al. (2003). Thus, we believe that the separation between the H-rich sdBs and the intermediate-helium subdwarfs should be made at a value of  $\log N(\text{He})/N(\text{H}) = -1.2$ , rather than  $-1.0$ .

We note that our classification is intended to examine and compare mass distributions by class. Thus, the separation between the sdBs and sdOs mainly aims at separating the typical hydrogen-rich subdwarfs on the EHB (sdBs) from their hotter evolved post-EHB counterparts (sdOs) and is not strictly based on effective temperature or strength of the He II lines. The transition from sdB to sdO is gradual, and both classes are connected from an evolutionary perspective (Heber 2009). The separation between the cool sdBs and the BHB is also ambiguous. The position of the Momany jump separating the BHB stars from the EHB is known to be around 18–20 kK (Newell & Graham 1976; Momany et al. 2002; Brown et al. 2016). When looking at our stars in Figs. 2 and 3 we see instead a discontinuity around



**Fig. 6.** Mass as a function of  $T_{\text{eff}}$  for the stars in the Bok sample. The spectral types are indicated following the same color scheme as in Fig. 5. The masses expected from the STELUM and BaSTI models for the ZAEHB are indicated by dashed and solid red lines respectively. Masses expected from the ZAHems are indicated with the dashed-dotted line.

23 kK, with the cooler stars being found at lower  $\log g$ , close to the TAEHB in Fig. 2, and clustering at a helium abundance close to  $\log N(\text{He})/N(\text{H}) = -2$  (Fig. 3). Whether the few stars between 20 and 23 kK are sdBs or BHBs remains uncertain.

**Peculiar objects.** Our sample contains four luminous hot stars (50–60 kK) with  $\log g \leq 4.5$  (indicated in Fig. 2). These are the two very similar extreme-He stars BD+37° 1977 and BD+37° 442, which likely have surface gravities slightly below the limit of our model grid at 50 kK (i.e.,  $\log g < 4.25$ , see Jeffery 2020 and references therein), the He-sdO KPD2322+4933 ( $\log N(\text{He})/N(\text{H}) = 0.9$ ), and the sdO BD-3° 2179 ( $\log N(\text{He})/N(\text{H}) = -0.6$ ). These luminous objects are likely associated with the post-AGB phase. Another interesting object is the He-sdO GSC03214-02615 ( $T_{\text{eff}} = 43$  kK,  $\log g = 5.7$ ,  $\log N(\text{He})/N(\text{H}) = 0.44$ ) that is a candidate magnetic sdO. Its spectrum, displayed in Fig. B.1, shows the strong absorption feature around 4620 Å, which is still of unidentified origin. This feature is present in other stars with similar atmospheric

parameters, whether they show the Zeeman splitting indicative of magnetic field or not (Dorsch et al. 2024).

#### 4.1.2. Stellar parameters

Having determined the atmospheric parameters of our stars, we proceed with the fit of the SEDs as described in Sect. 3.2. The main goal of the SED fits is to derive reliable stellar parameters for the stars in our sample. This requires the *Gaia* parallax to be well measured. Thus, in the figures and the analyses involving  $R$ ,  $L$ , and  $M$ , we always exclude stars with a parallax error larger than 20% and those with  $\text{ruwe}^4 > 1.4$  (El-Badry et al. 2021). We also inspected the SED fit result for each star and removed stars that could not be properly reproduced. For example, the SED of PB5450 (also known as EQ Psc) is strongly affected by the irradiation of its companion (see Baran et al. 2019). We show in Fig. 5 the distribution of the 300 remaining stars in terms of luminosity versus  $T_{\text{eff}}$  (via the HRD). From the masses derived with the parallaxes and SED fits, we identified ten stars among the BHB sample that have masses above  $3 M_{\odot}$ , indicating that they are more likely to be MS objects although the less massive ones might be intermediate-mass stripped stars (Irrgang et al. 2022; Villaseñor et al. 2023). From the SED fits, we identified 29 stars with an IR excess consistent with MS companions of  $T_{\text{eff}}$  between 3000 and 5900 K (see Fig. A.1), which are marked with an additional orange circle<sup>5</sup> in Figs. 2–6. The properties of these systems are listed in Table A.1 and several are discussed in Appendix A. The composite systems include a few known short and long period binaries (e.g., Maxted et al. 2000; Saffer et al. 1998; Vos et al. 2019). We note that the spectra of these composite systems were fitted in the same way as all stars, only with a model atmosphere for the hot subdwarf component. For most of them, we do not see contamination from the companion in the Bok spectrum. This is the case for PG0014+068, among others (see Fig. E.2). Only in stars with more luminous G-type companions, such as PG1701+359 we do see spectral features from the companion, such as the Mg triplet lines ( $\sim 5170 \text{ \AA}$ ). The wavelength regions contaminated by features from the companion are ignored during the spectral fit. Nevertheless, the atmospheric parameters obtained for the stars with the strongest IR-excess might be less accurate than for the other stars.

On the HRD, most of the sdBs are found on the theoretical HB, but a noticeable fraction are located below the ZAEHB. These “underluminous” stars are further discussed in Sect. 5.3. The luminous sdBs and the sdOs are consistent with a post-EHB phase as suggested by the evolutionary tracks. Interestingly, the hydrogen-rich sdOs are mainly divided into two groups, found on each side of the ZAHeMS. The group on the hot side of the ZAHeMS (the hottest sdOs) is consistent with the evolutionary track starting at the hot end of the EHB, meaning they probably evolved from the hottest sdBs (those with the smallest hydrogen envelope, often called sdOBs), while the cooler post-EHB stars may be the progeny of cooler sdBs. This division of the sdOs into two regions is also visible in the Kiel diagram (Fig. 2). Another noteworthy feature visible in both the HR and Kiel diagrams is a gap in the  $T_{\text{eff}}$  distribution of sdB stars around 33–34 kK, corresponding to a luminosity of about  $20 L_{\odot}$ . Such a drop in the

density of sdBs along the EHB was also reported in Geier et al. (2022) who noticed a void of stars around 33 kK and  $\log g = 5.7$  in the Kiel diagram of their hot subdwarfs sample. This separation of the sdBs into two regions, with one populating the very hot end of the EHB is reminiscent of the dichotomy found by Xiong et al. (2017) in their evolutionary models. In their models, the hotter sdBs are those with almost no H-rich envelope left because they experienced flash-mixing in their atmosphere due to a delayed He-flash. This is essentially the late-flasher scenario, first presented in D’Cruz et al. (1996) to explain the population of blue hook stars in some massive globular clusters. As for the cooler sdBs, they follow the canonical formation scenario where the He-flash happens at the tip of the RGB. We note that the presence of a gap between the canonical EHB stars and the hotter He-enriched blue-hook stars is also observed in  $\omega$  Cen and NGC 2808 (Brown et al. 2016) and happens around 32–33 kK (Latour et al. 2018). Finally, the position of the majority of He-sdOs is remarkably consistent with that of the helium main sequence of Paczyński (1971). Following the theoretical masses along this sequence, our He-sdOs would have masses that increase with  $T_{\text{eff}}$ , mainly from 0.6 to  $1.0 M_{\odot}$ .

Figure 6 shows that our masses do not have a trend with  $T_{\text{eff}}$ <sup>6</sup>, with the exception of the He-sdOs. This is the expected behavior because the effective temperatures of EHB stars are determined by the extent of their hydrogen envelopes, which are always negligible in mass ( $\lesssim 0.02 M_{\odot}$ ) compared to the core. Even for the BHB stars, the increase in mass is very small as shown by the BaSTI track.

For the He-sdOs, we observe the expected mass increase for stars between 40 and 50 kK. However, compared to the masses inferred from their positions near the ZAHeMS on the HRD, the masses obtained from the SEDs appear underestimated at the cool end and overestimated at the hot end. This discrepancy likely arises from a  $T_{\text{eff}}$ -dependent bias in our  $\log g$  measurements. Indeed, in the Kiel diagram, the cool He-sdOs are found above the ZAHeMS while the hot He-sdOs are slightly below it (Fig. 2), which is somewhat inconsistent with their more precise location on the HRD. The spectra of the He-sdOs remain challenging to model, and it is possible that their atmospheric parameters, especially  $\log g$ , still suffer from some systematics.

## 4.2. The MMT sample

### 4.2.1. Atmospheric and stellar parameters

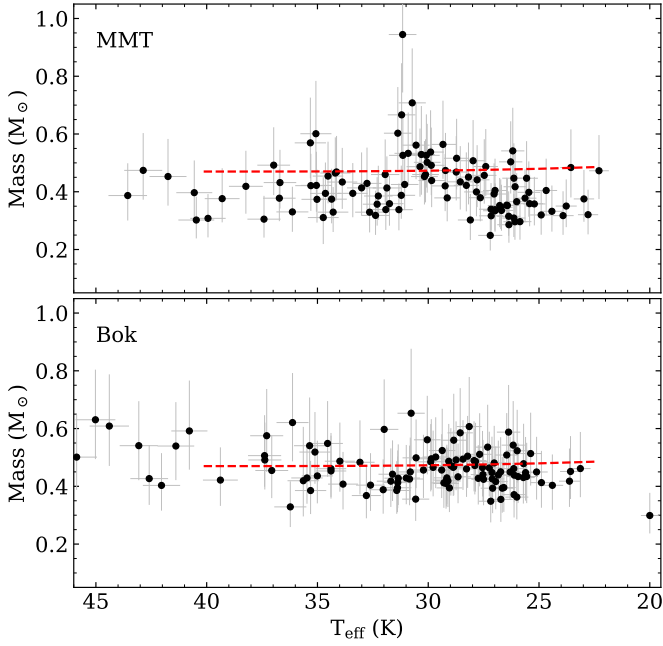
The MMT spectra were fit in the same way as described earlier, and from their atmospheric parameters we also derived the stellar parameters via the SED fitting method. Although these spectra have a higher resolution than the Bok spectra, they cover a smaller wavelength range (4000–4950  $\text{\AA}$ ) that includes only three Balmer lines ( $H_{\beta}$ ,  $H_{\gamma}$ , and  $H_{\delta}$ ). All stars in the MMT sample are shown in the MMT spectral atlas included in Fig. D.1. When inspecting the resulting masses, we noticed an obvious mass trend as seen in the top panel of Fig. 7. There is a significant increase in masses for the stars around 30 kK. The MMT sample consists of hydrogen-rich sdBs and sdOs only, thus no visible mass dependency over  $T_{\text{eff}}$  is expected, as seen for the masses derived with the atmospheric parameters obtained from the Bok spectra of these same stars (Fig. 7, bottom panel).

We then inspected the differences in atmospheric parameters obtained from the MMT and the Bok spectra for the 116 stars

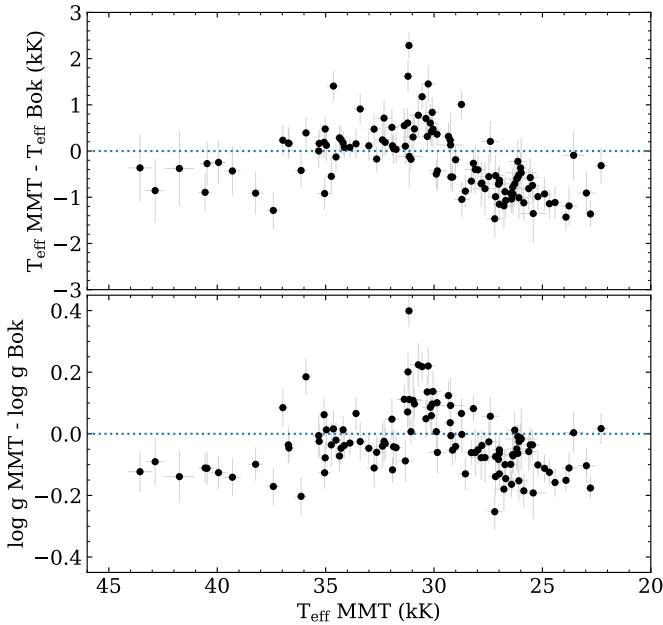
<sup>6</sup> This could not be achieved for the MMT sample, see Sect. 4.2.1.

<sup>4</sup> The re-normalized unit-weight error is a measure of the astrometric goodness of fit.

<sup>5</sup> We note that many of the stars with an IR-excess have  $\text{ruwe} > 1.4$  and thus do not appear in the Figs. 5 and 6. However they are all listed in Table A.1.



**Fig. 7.** Mass versus  $T_{\text{eff}}$  for the stars in the MMT sample. The masses obtained when using the atmospheric parameters from the MMT spectra (top) and the Bok spectra (bottom). The dashed line shows the canonical,  $0.47 M_{\odot}$ , expected for EHB stars.



**Fig. 8.** Comparison between the atmospheric parameters,  $T_{\text{eff}}$  and  $\log g$ , obtained from the MMT and Bok spectra.

present in both samples. From the results shown in Fig. 8, we observe a trend in  $T_{\text{eff}}$  and  $\log g$  for stars between 25 and 30 kK. Generally speaking, the MMT spectra of the “cool” sdBs are fit with lower  $T_{\text{eff}}$  and lower  $\log g$  compared to the Bok spectra. The opposite happens for the sdBs hotter than  $\sim 35$  kK; their MMT spectra result in higher  $T_{\text{eff}}$  and higher  $\log g$  than their Bok spectra. We thus conclude that the restricted wavelength range of the MMT spectra does not allow us to derive atmospheric parameters that are accurate enough to obtain reliable masses

from the SED fits, even if the spectra are of excellent quality. This highlights the importance of the high Balmer lines in the determination of the atmospheric parameters, especially that of the surface gravity (Hubeny et al. 1994). Nevertheless, there are things to be learned from the MMT spectra. We discuss the presence of helium stratification in the following subsection and the particular case of PG0215+183 is presented in Appendix C.

#### 4.2.2. Helium stratification

While examining the best-fit solutions of the MMT spectra, we noticed that the helium lines in a few stars were poorly reproduced (see Fig. 9 for two examples). One of these stars is BD+48°2721, which is a cool sdB, or possibly a BHB, known to show the  $^3\text{He}$  anomaly (Edelmann et al. 2001). The  $^3\text{He}$  anomaly implies that neutral He absorption lines feature contributions from both the  $^3\text{He}$  and  $^4\text{He}$  isotopes. In addition, Schneider et al. (2018) found that the strongest He I lines in BD+48°2721 could not be properly reproduced by the model spectra: the line cores are shallower in the observations. This phenomenon is attributed to a vertical stratification of He in the stellar atmosphere. In fact, the vertical stratification and the presence of  $^3\text{He}$  are both a manifestation of atomic diffusion taking place in the atmosphere. Besides this object, Schneider et al. (2018) also detected He stratification in three  $^3\text{He}$  sdB stars with  $T_{\text{eff}}$  between 26.5 and 29 kK.

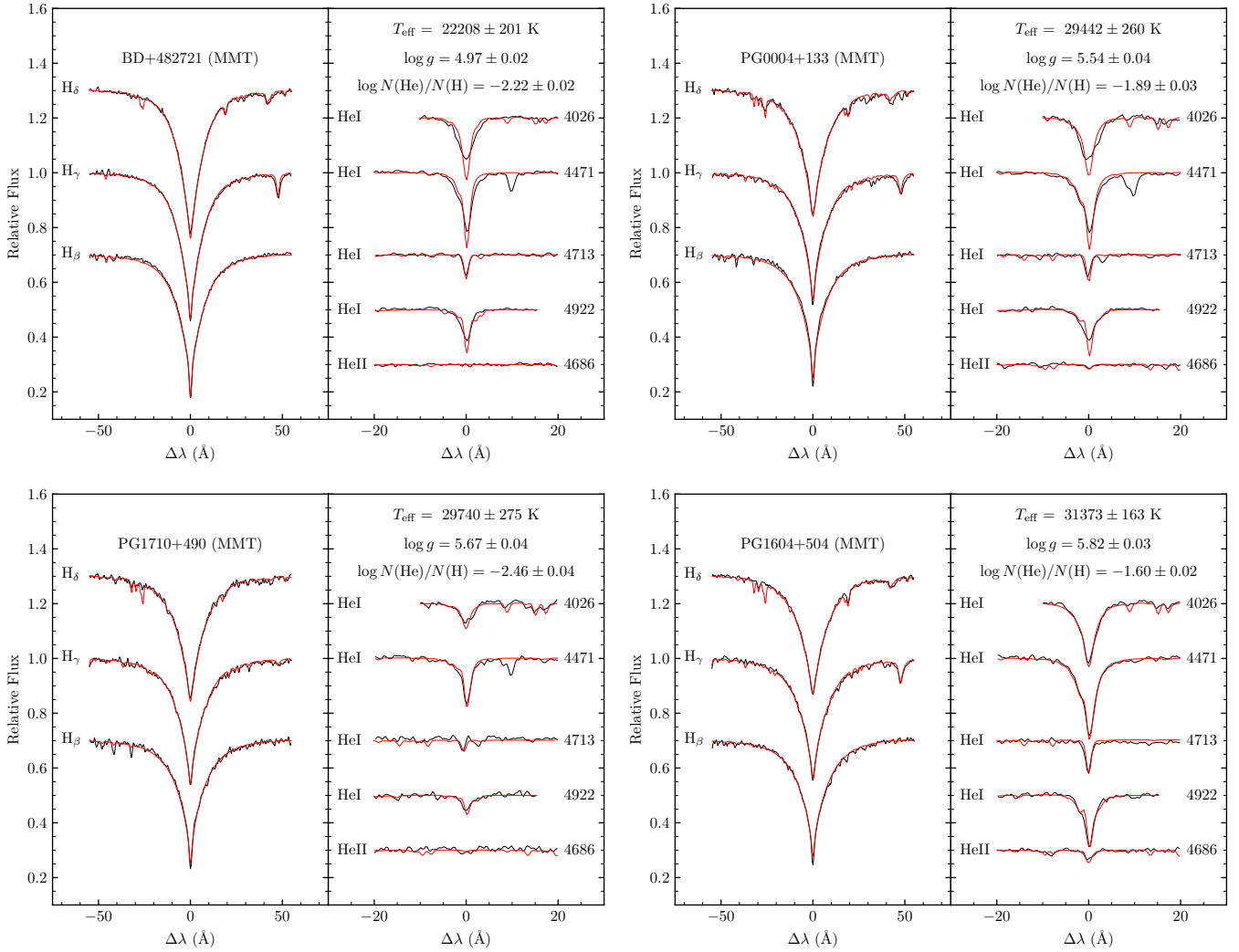
The mismatch between the observed and modeled He lines in the spectrum of BD+48°2721 is caused by He stratification. Similar mismatches are seen in BD+42°3250, PG0004+133 (see Fig. 9), PG1738+505, PG0242+132, and possibly PG1512+244 and PG1519+640, indicating that they also have He stratification. Figure 10 shows the position of these stars in the  $T_{\text{eff}}$ -helium plane. The  $T_{\text{eff}}$  of these six objects are between 28 and 31 kK, which is consistent with the  $T_{\text{eff}}$  range of the known  $^3\text{He}$  and stratified stars (Schneider et al. 2018; Geier et al. 2013).

It is likely that the six new He-stratified objects are also enriched in  $^3\text{He}$ , but the isotopic shift of the He lines in the MMT spectral range is too small (0.2–0.3 Å) to be detectable at a resolution of 1 Å. Up until now, He stratification has only been reported in  $^3\text{He}$  stars. However, not all  $^3\text{He}$  stars show evidence of stratification. Our sample also includes two known  $^3\text{He}$  stars that do not show evidence of He stratification: PG0133+114, and PG1710+490 (see Fig. 9). The latter was included in the analysis of Schneider et al. (2018) while the former was only reported by Edelmann et al. (2001). In light of these results, it appears that the stratification of helium, and possibly of other elements (Geier 2013), and also the presence of  $^3\text{He}$ , is more common than previously thought in sdBs with  $T_{\text{eff}}$  around 28–31 kK.

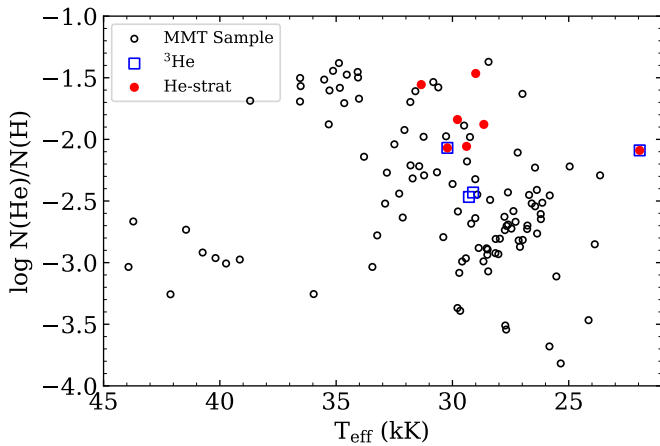
## 5. Discussion

### 5.1. Mass distributions

Using the masses presented in Sect. 4.1.2, we now examine the mass distribution of our hot subdwarfs. For this discussion, we always exclude the stars that were fitted with an IR excess, unless stated otherwise. We first concentrate on the three most populated spectral types: sdB, sdO and He-sdO. We show in Fig. 11 the mass distributions for these three spectral types. Along with the mass distributions, we also calculated the average mass ( $\bar{M}$ ) as a weighted mean for each spectral type. Because the uncertainties ( $\epsilon$ ) are proportional to the mass itself, we used the



**Fig. 9.** Upper panel: best fit of the Balmer and helium lines in selected stars from the MMT sample. Top: BD+48°2721, a known <sup>3</sup>He star, and PG0004+133. The mismatch between the predicted and observed He lines is due to the stratification of helium in the atmosphere. Bottom: PG1710+490, a known <sup>3</sup>He star with no indication of stratification (also according to Schneider et al. 2018) and PG1604+504, that shows no indication of stratification.



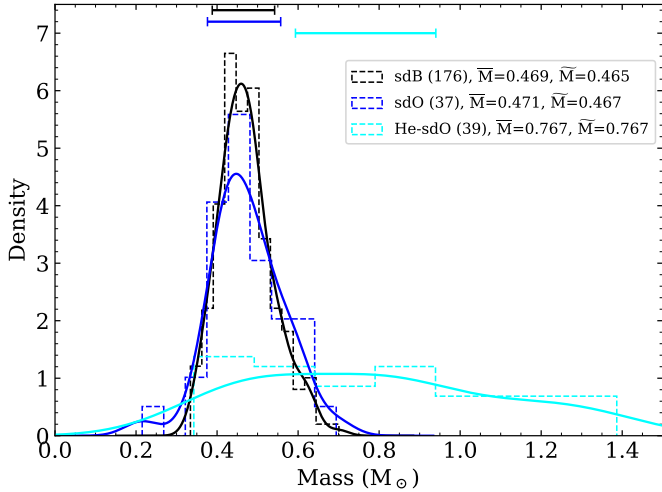
**Fig. 10.** Position of the stars from the MMT sample in the  $T_{\text{eff}}$ –He plane. Stars showing indication of He-stratification in their MMT spectrum are indicated with filled red circles. Stars having <sup>3</sup>He in their atmosphere are indicated with blue squares (from Schneider et al. 2018 and Geier et al. 2013).

relative uncertainty as weight, leading to

$$\bar{M} = \frac{\sum w_i M_i}{\sum w_i}, \text{ where } w_i = \frac{M_i^2}{\epsilon_i^2}.$$

We also computed the median mass ( $\bar{M}$ ) of the distributions. Both of these values are reported in Fig. 11 and in Table 2. In the table, we include three additional diagnostics: the median value of the uncertainties ( $M_{\text{err}}$ ), the standard deviation ( $\sigma$ ) of the mass distribution, and its 68% interquartile range ( $Q_{16}$ – $Q_{84}$ ). Both  $M_{\text{err}}$  and  $\sigma$  are expressed as a percentage to remove the correlation between the masses and their absolute uncertainties.

As shown in Fig. 11, the sdB and sdO distributions are very similar and peak around  $0.47 M_{\odot}$ . This agrees with theoretical expectations, since the two types are thought to be evolutionarily linked and have comparable average masses close to this (canonical) value. Our mean and median values for the sdBs are also consistent with the  $0.47 M_{\odot}$  obtained by Fontaine et al. (2012) from 22 sdBs with masses derived from asteroseismology and the light curve analysis of binary systems. Our distribution is wider than that of Fontaine et al. (2012), but masses obtained from asteroseismology and light curve modeling typically have



**Fig. 11.** Mass distribution obtained from parallaxes and SED fits for the sdBs, sdOs, and He-sdOs in our sample. The dashed lines show the normalized histograms for each spectral group and the solid curves are the associated kernel density function. The stars with a composite SED were excluded. In the legend, we indicated the number of stars in parenthesis as well as the average ( $\bar{M}$ ) and median ( $\tilde{M}$ ) mass for each spectral type. The error bars on top are indicative of the mass uncertainty for each spectral type (see  $M_{\text{err}}$  in Table 2).

smaller uncertainties than those derived from SED fits and parallaxes. The typical uncertainty on the individual masses ( $M_{\text{err}}$ ) and the standard deviation ( $\sigma$ ) of the sdO distribution are similar, while for the sdBs we found  $\sigma$  to be smaller than the typical error. This means that the broadening of our sdB and sdO distributions can be fully explained by the uncertainties. The consistency between our sdB and sdO mass distribution is a significant improvement compared to the results of Lei et al. (2023), who obtained a relatively flat mass distribution for their sdO stars. Their unrealistic sdO masses are most likely caused by the lack of metallic opacities in the model atmospheres they used to derive the atmospheric parameters and compute the SEDs of their hot sdOs. It is especially important to take into account both NLTE effects and line-blanketing when modeling the spectra of hot sdO stars (Werner 1996; Latour et al. 2013, 2015).

Intriguingly, the mass distribution of the He-sdOs is very different from that of the H-rich hot subdwarfs: it is much broader, with 68% of the stellar masses falling between 0.48 and 1.18  $M_{\odot}$ , and it does not show a distinct peak. The dispersion is significantly larger than the typical uncertainties, suggesting the presence of an intrinsic dispersion. The weighted mean and median mass of the He-sdOs are around 0.77  $M_{\odot}$ , which is significantly larger than the canonical core-helium burning mass. However, caution is advised when assessing the masses derived for the He-sdOs. As mentioned in Sect. 4.1.2, the masses obtained from SED fits and parallaxes of the He-sdOs are somewhat different from those expected from the position of the stars in the HRD. We also calculated masses for the He-sdOs from their position on the HRD, meaning that we projected each star onto the nearest point along the ZAHems. Uncertainties in  $T_{\text{eff}}$  and  $L$  were taken into account to estimate the corresponding uncertainties on the masses, which are notably lower than those obtained from the SED fits. The HRD masses are included in the extended version of Table D.1 and we also include their statistics in Table 2. Masses from the HRD were not computed for the 3 He-sdOs that are post-AGB objects (see Sect. 4.1.1). The

**Table 2.** Mass properties by spectral group and binary type in our sample.

Type	$N_{\text{star}}$	$\bar{M}$ [ $M_{\odot}$ ]	$\tilde{M}$ [ $M_{\odot}$ ]	$M_{\text{err}}$ [%]	$\sigma$ [%]	$Q_{16}-Q_{84}$ [ $M_{\odot}$ ]
		(1)	(2)	(3)	(4)	(5)
Spectral groups						
sdB	176	0.469	0.465	16.2	14.4	0.408–0.542
sdO	37	0.471	0.467	19.3	18.8	0.403–0.554
He-sdO (SED)	39	0.767	0.767	20.4	39.4	0.482–1.183
He-sdO (HRD)	36	0.753	0.845	4.2	24.9	0.696–0.964
iHe-sdOB	9	0.449	0.432	18.2	28.4	0.344–0.502
BHB	19	0.565	0.536	19.0	23.7	0.466–0.690
Binary types						
sd+WD	38	0.452	0.442	16.2	12.8	0.399–0.522
sd+dM	15	0.499	0.504	15.9	14.9	0.411–0.573
single	133	0.468	0.470	17.1	15.8	0.413–0.524
Binary	92	0.469	0.460	16.2	15.7	0.400–0.551

**Notes.** (1) Weighted average. (2) Median. (3) Median of the individual mass uncertainties. (4) Standard deviation. (5) Interquartile range, 16th–84th percentile.

He-sdO masses obtained from the HRD are mostly distributed between 0.6 and 1  $M_{\odot}$  without any distinct peak. The four He-sdOs hotter than 58 kK have masses around 1.4  $M_{\odot}$ . Analyses of He-sdO samples including mass estimates are still scarce in the literature, but the mass distribution of He-sdOs shown in Dorsch (2024, Fig. 4.1.7) also has an extended high-mass tail with values above 1  $M_{\odot}$ . On the other hand, the position of He-sdOs from the SALT spectroscopic survey (Jeffery et al. 2021) in the HRD shown in Dorsch et al. (2024) suggests that they have masses between 0.6 and 1.0  $M_{\odot}$  according to the helium main sequence of Paczyński (1971). This is very similar to what is seen in our sample, although this might not be surprising given that the model atmospheres and analysis method used in Dorsch et al. (2024) are the same as in this work. Given the systematic uncertainties on the  $\log g$  values of the He-sdOs, it is likely that the masses derived from the HRD positions are more accurate. In any case, both the masses obtained from the SED fits and the position of He-sdO stars in the HRD indicate that they are, on average, more massive and span a wider mass range than the hydrogen-rich sdBs and sdOs. The higher masses of the He-sdOs and their broader distribution are fully consistent with a stellar merger origin (see, e.g., Han et al. 2003; Justham et al. 2011; Saio & Jeffery 2000; Zhang & Jeffery 2012). This hypothesis, although long suspected, was recently further supported by the discovery of several magnetic He-sdOs (Dorsch et al. 2024, 2022; Pelisoli et al. 2022) and the low fraction of short-period binaries among He-sdOs (Geier et al. 2022; Snowdon et al. 2025).

As for the BHB stars, they are expected to be slightly more massive than canonical H-rich subdwarfs, with masses between 0.50 and 0.55  $M_{\odot}$ , depending on the metallicity. From our observations, we derive a median mass of about 0.54  $M_{\odot}$ , which is in good agreement with the expectation. Finally considering the iHe-sdOBs and iHe-sdBs, our samples are too small, with nine and three stars respectively, to derive a statistically significant mass distribution. Saying that, the average mass of these stars appears to be consistent with the canonical hot subdwarf mass of around 0.5  $M_{\odot}$ . While the three iHe-sdBs are rather scattered on the Kiel and HR diagrams, their masses are all fairly close to the canonical values (see Fig. 6). The iHe-sdB that is significantly below the ZAEHB in both the Kiel and HR diagrams is

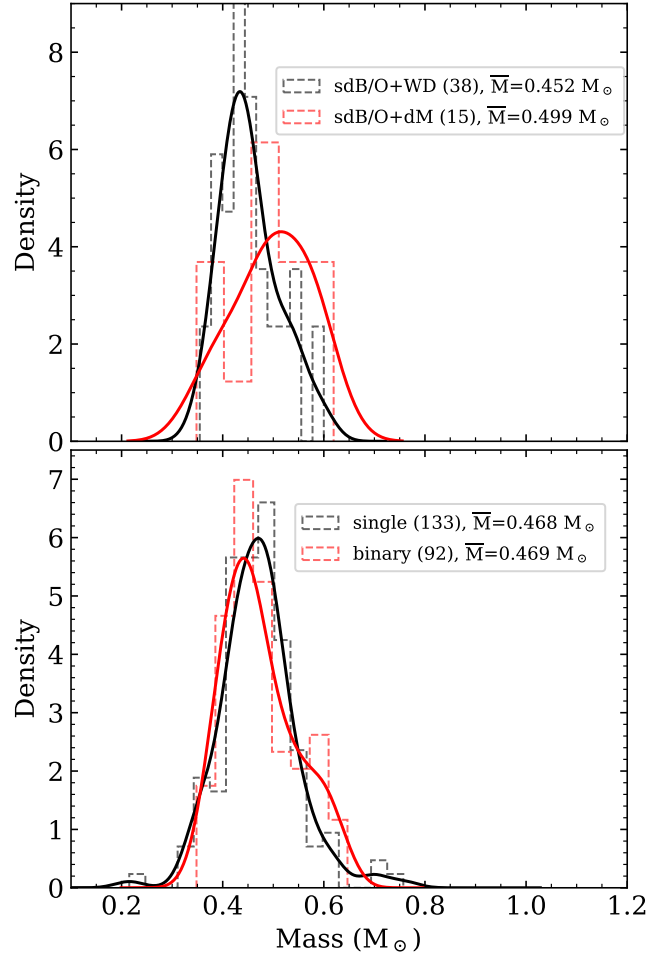
PG1247+554 (also known as GD 319), whose best-fit is shown in Fig. 4. This is a particular system comprising an iHe-sdB in a 0.6 day period binary and cool MS star located about 1'' away (Maxted et al. 2000; Mason et al. 2001), however the MS star is most likely a background star (S. Geier, priv. commun. 2025). The hot subdwarf and the MS star are resolved by *Gaia* and our SED fit is solely based on the *Gaia* XP spectra of the hot subdwarf. Although this star was a promising low-mass hot subdwarf candidate from its location on the HRD, the normal mass that we obtained from the SED fit does not match this interpretation.

### 5.2. Mass distribution and binarity

To investigate a possible dependence of mass on binarity in the stars of our Bok sample, we divided them into binary groups based on information available from the literature. Notably, Schaffenroth et al. (2022) classified many hot subdwarf binaries, mostly sdBs but also a few sdOs with  $T_{\text{eff}} \sim 40$  kK, into two different categories based on their TESS light curve properties: sdB/O+dM (HW Vir systems and reflection effects) and sdB/O+WD (ellipsoidal and beaming effects). For some of these systems, the authors estimated masses from parallaxes and SED fits and found that the mass distribution of hot subdwarfs in sdB/O+WD systems peaks at a lower mass than those having a M-dwarf (dM) companion.

To investigate this topic further, we cross-matched the stars in our sample with the stars listed in Table A.3 and A.4 of Schaffenroth et al. (2022) and extracted binary information for a few additional targets of ours from other sources: PG0101+039 (Maxted et al. 2002; Geier et al. 2008), PG2345+318 (Green et al. 2004), KIC007668647 (Telting et al. 2014), and KIC011558725 (Telting et al. 2012) as sdB+WD systems and PG1438-029 (Green et al. 2004), HS2231+2441 (Østensen et al. 2008), FBS1531+381 (For et al. 2010), and UVO1758+36 (Schaffenroth priv. comm. 2025) as sdB+dM systems. This yielded a subsample of 38 sdB/O+WD and 15 sdB/O+dM systems<sup>7</sup>. We show the resulting mass distributions in the top panel of Fig. 12. Interestingly, there is a distinct difference between the mean mass and the mass distribution of the two types of binaries (see also Table 2). The sdB/O+WD systems have an average mass close to  $0.45 M_{\odot}$ , while the sdB/O+dM have a slightly larger average mass of  $0.5 M_{\odot}$ . This is in line with the finding of Schaffenroth et al. (2022) that the hot subdwarfs with dM companions appear to be, on average, slightly more massive than those with WD companions. To verify whether the difference is significant, we ran 1000 iterations of the Kolmogorov-Smirnov test (KS-test) using masses drawn from a normal distribution based on the individual errors and we obtained an average  $p$ -value ( $p_{\text{KS}}$ ) of 0.30. This means that if the two underlying distributions were the same, we would get the observed difference at least 30% of the time. Thus we cannot conclude that the difference between the two mass distributions are significant. In this case, we are likely limited by the small number of sdB/O+dM, only 15, identified in our sample. It is also worth noting that in sdB/O+dM systems, the atmospheric parameters of the hot subdwarf vary with the phase when the reflection effect is sufficiently strong, adding additional uncertainties on the atmospheric parameters derived from a single spectrum (see, e.g., Heber et al. 2004; For et al. 2010).

We also looked at the mass distribution of non-composite binaries, essentially meaning close binaries with companions



**Fig. 12.** Top: mass distributions of the hot subdwarf components in close binary systems with WD and dM companions. For most of the systems, the type of binarity was classified by Schaffenroth et al. (2022). The weighted average mass of both categories is also indicated. Bottom: mass distribution for hot subdwarfs that are candidate single stars compared to those found in close binary systems.

that are detected only from radial velocity or light curve variations (without producing IR-excess), to compare it with that of the apparently single stars. For this comparison, we only considered the He-poor and intermediate-He hot subdwarfs, thus excluding the He-sdOs and BHBS. To build our list of close binary stars, we started with the 53 systems identified previously (the sdB/O+WD and sdB/O+dM), to which we added known binaries from radial velocity surveys in the literature (e.g., Saffer et al. 1998; Maxted et al. 2001; Copperwheat et al. 2011; Morales-Rueda et al. 2003; Geier et al. 2022; He et al. 2025) and suspected binaries from the RV measurements of the MMT spectra and from on-going RV monitoring (F. Mattig, priv. comm. 2025). In his way, we were able to increase our number of binary stars to 92 objects. The 133 remaining stars, for which we had no evidence of binarity or information about their RVs, were considered as single star candidates. The resulting mass distributions for binaries and single hot subdwarfs are shown in the bottom panel of Fig. 12 and their characteristics are listed in Table 2. Both distributions appear very similar and our series of KS-tests did not find a statistically significant difference between the two distributions ( $p_{\text{KS}} = 0.57$ ); however, this does not necessarily imply that the underlying distributions are identical.

<sup>7</sup> Those are 15 systems that do not show IR-excess in their SED.

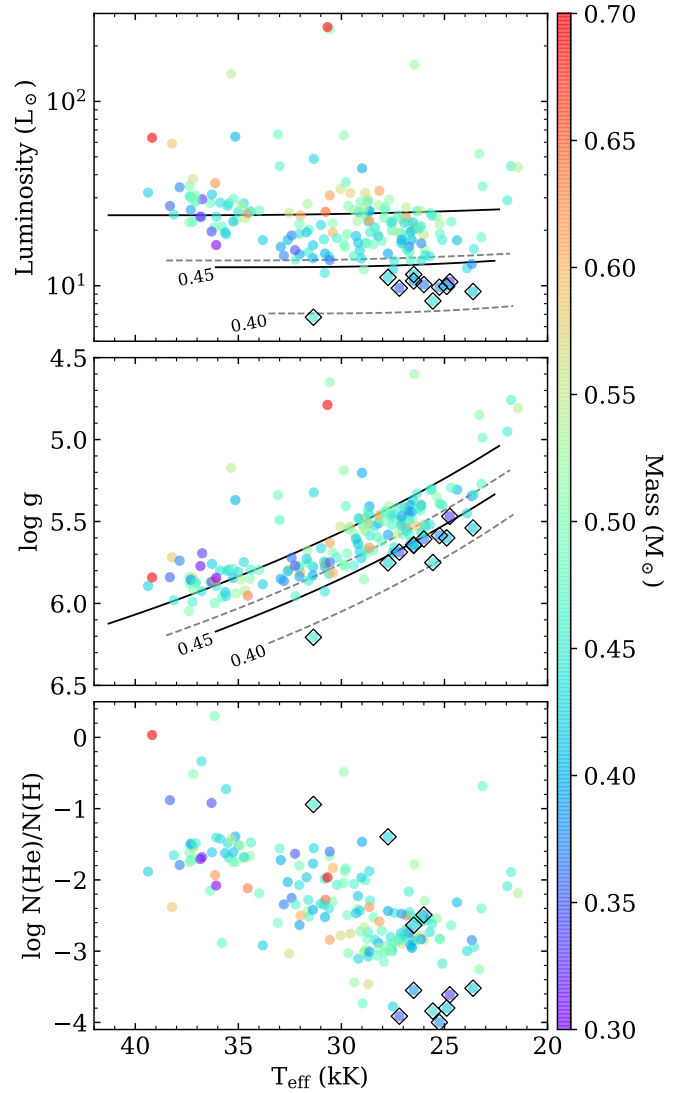
The formation of single hot subdwarfs remains challenging to explain from a theoretical point of view. One potential formation channel is via the merger of two low-mass stars (e.g., two He-core WDs, CO-core and He-core WDs, or low-mass MS + He-core WD; Han et al. 2003; Politano et al. 2008; Hall & Jeffery 2016). According to Han et al. (2003, see their Fig. 12), the predicted mass distribution for sdBs originating from the merger channel is broader and shifted to higher masses (0.5–0.55  $M_{\odot}$ ) compared to those formed via common-envelope ejection. If a majority of our candidate single He-poor sdB/Os were merger products, we would expect their mass distribution to be different to that of He-poor sdB/Os in close binary systems, formed via the common envelope channel. However, given the similarity of the two mass distributions, we find no evidence that a substantial fraction of the He-poor single star candidates are formed via the merger channel.

The close binary fraction of our hot subdwarf sample is 41%<sup>8</sup> (92/225). Close binary fractions from the literature ranges from 30% (Geier et al. 2022; He et al. 2025) to 48% (Maxted et al. 2001; Copperwheat et al. 2011), with the SPY sample giving an intermediate value of 39% for sdBs (Napiwotzki et al. 2004). The number of close binaries identified in our sample thus seems reasonable although there is certainly some binaries remaining in our single star sample, for example due to low inclination, or because the companion could be too faint or distant to be detectable. However, they are unlikely to be numerous enough to change our conclusion concerning their mass distributions. It is also worth mentioning that there are hints that the iHe-sdBs and iHe-sdOBs have different binary properties than the rest of the hydrogen-rich hot subdwarfs (see the discussions in Geier et al. 2022 and Dorsch 2024), but we decided to keep them in our hydrogen-rich sample as they are only 12 stars and they represent less than 5% of our sample.

### 5.3. Low-mass hot subdwarfs

Most hot subdwarfs are the progeny of low-mass MS stars ( $\sim 0.8$ – $2 M_{\odot}$ ) that experienced a helium flash, meaning that helium ignition happened under degenerate conditions. This occurs when the helium core reaches a mass in the range of 0.46–0.51  $M_{\odot}$ , almost regardless of the progenitor mass for MS stars below  $\sim 1.6 M_{\odot}$  (see Fig. 1 of Montalbán & Noels 2013 and chapter 6 of Noels-Grotsch & Miglio 2025). Instead, the exact mass of the He-core at the onset of the He-flash depends on the metallicity (and helium content) of the progenitor, higher metallicity stars experiencing the He-flash at a lower core mass (Iben 1967; Dorman et al. 1993; Salaris & Cassisi 2005). The He-flash may occur at a slightly lower (by about 0.01  $M_{\odot}$ ) core mass if it is delayed until after the progenitor has left the RGB (Brown et al. 2001; Miller Bertolami et al. 2008). Hot subdwarfs less massive than 0.45  $M_{\odot}$  are unlikely to have undergone a He-flash. For an sdB with  $M \leq 0.45 M_{\odot}$  to be burning helium in its core, it must have evolved from a higher mass progenitor ( $\sim 2.3$ – $3.5 M_{\odot}$ ) that ignited helium quiescently under non-degenerate or semi-degenerate conditions. In such cases, helium ignition can happen at core masses that are as low as  $\sim 0.33 M_{\odot}$  (Salaris & Cassisi 2005; Han et al. 2002; Hu et al. 2008; Arancibia-Rojas et al. 2024; Rodríguez-Segovia & Ruitter 2025).

<sup>8</sup> This is when excluding the composite systems, some of which also are close-binary systems, such as PG0940+068 and PG1101+249 (see Appendix A). When including all 27 composite systems (the two He-sdOs composites being excluded) it reaches 48%. Our binary fraction is not corrected for inclination effects.



**Fig. 13.** Position of the underluminous sdBs (black diamonds) in the HRD (top), Kiel diagram (middle), and  $T_{\text{eff}}-\log N(\text{He})/N(\text{H})$  plane. The underluminous sdBs were selected from their position below the ZAEHB for a core mass of 0.45  $M_{\odot}$ . The ZAEHB and TAEHB computed with STELUM for core masses of 0.45  $M_{\odot}$  (solid lines) and 0.40  $M_{\odot}$  (dashed lines) are indicated. All stars are color-coded with the mass obtained from the SED fits. We only show the stars with spectral types that can be associated with the EHB region: sdB, iHe-sdB, and iHe-sdOB.

Any such low-mass sdBs should be mostly found below the ZAEHB in the Kiel and HR diagrams. Because the luminosity is less affected by systematic uncertainties than the surface gravity, as explained in Sect. 3.2, we selected our candidate low-mass sdBs from the HRD. We found 11 stars with a luminosity lower than the STELUM ZAEHB track for a 0.45  $M_{\odot}$  core (see Fig. 13, top panel). We refer to these as “underluminous” sdBs. Their positions in the HRD are consistent with masses between 0.40 and 0.45  $M_{\odot}$ . The luminosity of the theoretical EHB band increases with increasing core mass and this effect is visible when color-coding the stars according to their mass (Fig. 13): we see a general increase of the masses with luminosity. On the Kiel diagram (Fig. 13, middle panel), the 11 underluminous sdBs are located below or very close to the ZAEHB.

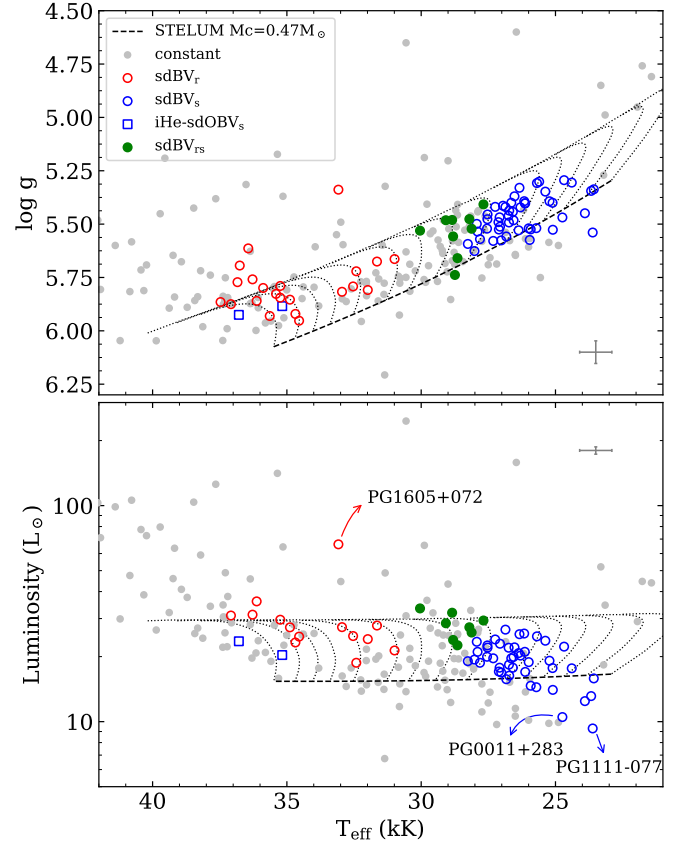
To verify whether the masses of the underluminous sdBs are indeed lower than the canonical mass, we computed the weighted average and median mass for the 10 underluminous sdBs that have no IR excess<sup>9</sup>. We obtained a weighted average and median mass of  $0.40 M_{\odot}$ . As a comparison sample, we used the remaining 178 non-composite stars classified as sdBs, iHe-sdBs, and iHe-sdOBs (shown as colored circles in Fig. 13). We restrict our comparison sample to these spectral types, because the sdOs and He-sdOs are not positioned on the EHB, thus they cannot be found in the region below the ZAEHB. For this comparison sample, we obtained a weighted average and median mass of  $0.47 M_{\odot}$ . This confirms that the underluminous sdBs are, on average, less massive than stars on the canonical EHB. With the exception of PG1247+554 (see Sect. 5.1), these underluminous sdBs are good candidates for originating from massive progenitors ( $\sim 2\text{--}3.5 M_{\odot}$ ). Our fraction of underluminous sdBs is 5.7% (11/190). This fraction is lower than that obtained by Dawson et al. (2026) in their 500 pc sample, which is around 11%<sup>10</sup>.

An interesting feature of the underluminous sdBs is that more than half of them are found to be at the “low-helium” end of the  $T_{\text{eff}}\text{--He}$  sequence (see Fig. 13, bottom panel). A similar behavior is also seen in the 500 pc sample of Dawson et al. (2026). Another remarkable peculiarity of the most helium-poor sdBs is the weakness of their metal lines. This is most noticeable when looking at the MMT spectral atlas in Fig. E.1: the spectra with weak or absent He I lines also have very weak metallic lines compared to other spectra of stars at similar  $T_{\text{eff}}$ . Three underluminous stars with especially low helium are seen on the first panel of Fig. E.1: PG1111–077, PG0856+121, and, PG0250+189. The low-helium sdBs are mainly found below the ZAEHB, consequently they have higher surface gravity than other sdBs at the same temperature. This likely affects the diffusion processes in the atmosphere, because a higher surface gravity means a stronger gravitational pull on the individual atoms. This could explain why low helium and low metal abundances appear to be correlated.

#### 5.4. Pulsators

Figure 14 shows the hot subdwarfs in the Bok sample for which we have information on the pulsation status, obtained according to the methodology described in Sect. 2.3. We plot them in the Kiel diagram (top panel) and in the HRD (bottom panel). The different types of pulsators are indicated with various symbols, with the sdBV<sub>r</sub> being the rapid  $p$ -mode pulsators, sdBV<sub>s</sub> the slow  $g$ -mode pulsators, and sdBV<sub>rs</sub> the hybrid pulsators showing both  $p$ - and  $g$ -modes (Kilkenny et al. 2010). As in the Kiel and HR diagrams (Figs. 2 and 5), we observe a lack of sdBV<sub>r</sub> pulsators around 33 kK (see Sect. 4.1.2 for more details about this feature). Feige 46 and LS IV–14° 116 are two known slow pulsators belonging to the very small group of iHe-sdOBV (or V366 Aqr). This class of pulsator only includes three members so far, which all share very similar pulsation and atmospheric properties (Green et al. 2011; Latour et al. 2019; Østensen et al. 2020), including the extreme heavy-metal abundances characteristic of iHe-sdOBs.

The observational instability regions for the different types of pulsations are well defined, and separated, in both diagrams shown in Fig. 14. The gravity modes are excited from  $\sim 23.5$  kK



**Fig. 14.** Position of the pulsating stars in the Kiel (top) and HRD (bottom) diagram. The different types of pulsators are indicated with various symbols: rapid pulsators sdBV<sub>r</sub> (open red circles), slow pulsators sdBV<sub>s</sub> (open blue circles), and hybrid pulsators sdBV<sub>rs</sub> (green filled circles). Stars found to be constant are indicated with grey filled circles. Feige 46 and LS IV–14° 116 (blue open squares) are peculiar slow pulsators belonging to the small class of iHe-sdOBV (V366 Aqr). The ZAEHB (dashed line) is indicated for a core mass of  $0.47 M_{\odot}$  and corresponding evolutionary sequences of the core-helium burning phase are shown for different H-envelope masses (dotted lines). Stars with a poor parallax measurement are excluded in the bottom panel. Representative errors are shown in each panel.

to about  $\sim 30$  kK in the hottest hybrid pulsators, while pressure modes are found in the 27.5–38 kK range. Our distribution of rapid pulsators is similar to that presented in Baran et al. (2024), with the difference that we do not see any pure  $p$ -mode pulsators below 31 kK. However, the number of rapid pulsators in the sample of Baran et al. (2024) is about two times larger than ours, so this could be a selection effect. The constant and pulsating stars are similarly distributed in the Kiel diagram, but in the HRD we noticed that at a given effective temperature, the pulsators are preferentially located at higher luminosities compared to the non-pulsating stars. This trend may be related to the time it takes to build-up the iron and nickel reservoir in the Z-bump region (responsible for the driving of the modes; Charpinet et al. 1997; Fontaine et al. 2003; Jeffery & Saio 2006, 2007) through competing radiative levitation, gravitational settling and other processes (Fontaine & Chayer 1997; Fontaine et al. 2006; Théado et al. 2009; Hu et al. 2011). Stars too close to the ZAEHB may not yet have had time to accumulate enough metals and trigger pulsations.

We also find that within their instability strip, the slow pulsators are very common, and only a few sdB stars colder than

<sup>9</sup> PG0250+186 is the only underluminous sdB with IR excess.

<sup>10</sup> Note that if we use the same criteria as Dawson et al. (2026) to select our underluminous sdBs (i.e.,  $\log L/L_{\odot} \leq 1.05$ ), we are left with six stars only, leading to an even lower fraction of 3%.

28 kK are found to be non-pulsating from our ground-based and TESS light curves. This is in line with the early estimate of 75% for the fraction of  $g$ -mode pulsators (Green et al. 2011), which was further supported by results from the Kepler survey of compact pulsators (Østensen et al. 2011), although based on a smaller number of stars (12 pulsators out of 16 sdBs). In comparison, the rapid pulsators are much less common among the hotter sdB stars. This is especially remarkable taking into account the generally much lower amplitude of  $g$ -modes ( $\lesssim 0.1\%$ ) compared to  $p$ -modes ( $\lesssim 1\%$ ) and the fact that the latter should be easier to find. The fraction of  $p$ -mode pulsators is estimated to be around 10% (Østensen et al. 2010).

The distribution of pulsators on Fig. 14 is compatible with the canonical  $0.47 M_{\odot}$  EHB. However, three pulsators stand out as being farther away from the canonical mass EHB. Two of them are found below the ZAEHB and are among the low-mass sdB candidates discussed in Sect. 5.3: PG0011+283 and PG1111–077. Both of these stars also have a very low helium abundance ( $\log N(\text{He})/N(\text{H}) \lesssim -3.5$ ) and their SED masses are smaller than  $0.45 M_{\odot}$ . We believe they are good candidates for having evolved from a higher-mass progenitor and, as such, are interesting objects for future asteroseismic analyses. The third outlier is PG1605+075, which is located well above the TAEHB (Heber et al. 1999), indicating that the star is in the post-EHB evolutionary phase, which is supported by the canonical mass derived from the SED fit ( $0.49 \pm 0.1 M_{\odot}$ ). It has unusually high-amplitudes pulsations with five modes above 1%, and a very rich pulsation spectrum (Kilkenny et al. 1999). Several hypotheses have been proposed to explain its unusual pulsation properties, without a convincing picture emerging (richness of the pulsation spectrum explained by fast rotation or by linear combinations between a few high-amplitude pulsation modes; Van Grootel 2008; Van Grootel et al. 2010). Nine sdB pulsators in our Bok sample have masses and radii derived by asteroseismic modeling (PG0014+068, PG1047+003, PG1219+534, Feige 48, PG1325+102, PG0911+456, Balloon090100001, PG1336-018, and KPD0629-0016; Fontaine et al. 2012). We compared the masses and radii from our SED fits to those seismically derived. All measurements agree quite well, within or close to 1-sigma of the SED errors. The only exception is PG0911+456 (Randall et al. 2007), for which radius and mass estimates are a bit different from asteroseismology, but still within 2-sigma of the SED errors.

In Fig. 14, we noticed that the sdBV<sub>r</sub> stars are mainly located above the ZAEHB, and are instead found closer to the TAEHB for a core-mass of  $0.47 M_{\odot}$ . This is especially notable for those hotter than 33 kK and was also reported in Baran et al. (2024) from their sample of TESS  $p$ -mode pulsators. However, it is not a property unique to the pulsators, but common to all stars located at the very hot end of the EHB: they sit at higher luminosities than their cooler counterparts. Such a shift could be explained if these stars have slightly higher than canonical masses ( $\sim 0.50 M_{\odot}$ ), but this requires further investigation.

## 6. Summary and conclusions

We analyzed the spectra of more than 325 relatively bright hot subluminal stars observed with the 2.3 m Bok telescope at the Kitt Peak observatory. The combination of size, quality, and homogeneity of this spectroscopic sample is unprecedented. We performed the analysis of the stars in two steps. First, we fit the observed spectra with state-of-the-art model atmospheres, synthetic spectra, and fitting techniques, to derive the

atmospheric parameters of the stars (i.e., their  $T_{\text{eff}}$ ,  $\log g$ , and helium abundance). Secondly, we performed SED fits using parallaxes from *Gaia* DR3 and magnitudes retrieved from various photometric catalogs to derive the stellar parameters radius  $R$ , luminosity  $L$ , and mass  $M$ . The sample includes a wide variety of hot subdwarfs that we separate into different categories based on their atmospheric parameters: sdBs, sdOs, iHe-sdBs, iHe-sdOBs, He-sdOs, and BHBs. From our SED fits, we also identified 29 composite systems with an IR-excess indicative of a MS companion. For a subset of 116 stars from the Bok sample, we analyzed additional spectra taken with the MMT telescope. Compared to the Bok spectra, the MMT spectra have a higher resolution but a shorter wavelength coverage. We summarize below the conclusions drawn from the various aspects of our analysis:

- Spectra must cover the high Balmer lines to constrain the atmospheric parameters with enough accuracy to derive meaningful spectroscopic masses from parallaxes and SED fits. This is the case for our Bok spectra but not for the MMT spectra, which only cover  $H_{\beta}$ ,  $H_{\gamma}$ , and  $H_{\delta}$ . As a result, the atmospheric parameters derived from the MMT spectra lead to mass estimates that show unrealistic trends with  $T_{\text{eff}}$ . In contrast, the masses obtained from the atmospheric parameters of the Bok spectra yield nearly constant masses across the  $T_{\text{eff}}$  range of the sdBs and sdOs (Sect. 4.2.1), which constitutes an important reliability check;
- The distribution of sdBs along the EHB is not continuous. There is a paucity of stars around 33 kK that is clearly visible in both the Kiel and the HR diagrams (Figs. 2 and 5). This is also observed among pulsators, with a void of sdBV<sub>r</sub> pulsators around 33 kK (Fig. 14). Such a discontinuity was also noticed in the sdB sample of Geier et al. (2022) and is recovered from the evolutionary sequences computed by Xiong et al. (2017). According to these sequences, the stars on opposite sides of the gap experienced the He-flash at different times during their evolution: the hotter ones when they were contracting on the WD cooling track (the hot- or late-flasher scenario), while the cooler ones when they were at the tip of the RGB. A late-flasher origin for the sdB hotter than  $\sim 33$  kK is consistent with the fact that we derive, on average, canonical masses for these sdBs;
- The helium abundances in our sdBs follow the well-documented trend of helium increasing with  $T_{\text{eff}}$ , first noticed by Edelmann et al. (2003). In the hottest sdBs, the helium abundances plateau around  $\log N(\text{He})/N(\text{H}) = -1.4$  (Fig. 3), not quite reaching the solar value of  $\log N(\text{He})/N(\text{H}) = -1.0$ , which is commonly used to distinguish between H-rich and He-rich (or intermediate-He) subdwarfs. Based on this observation, we believe that a helium abundance of  $\log N(\text{He})/N(\text{H}) = -1.2$  constitutes a more appropriate separator between the H-rich and intermediate-He classes (Sect. 4.1.1). We find that the low  $T_{\text{eff}}$  and low helium ( $\log N(\text{He})/N(\text{H}) \lesssim -3$ ) tail of the He– $T_{\text{eff}}$  relation is sparsely populated and the most He-poor sdBs show very weak metal lines in their MMT spectra (Fig. E.1), if any. In addition, many of the most He-poor sdBs are also located below the ZAEHB for a core-mass of  $0.45 M_{\odot}$ ;
- Our sample includes more than 80 pulsating hot subdwarfs and we found the different types of pulsators ( $g$ -mode,  $p$ -mode, and hybrid) to be well separated in both the Kiel and the HR diagrams. We noted that at a given  $T_{\text{eff}}$ , the pulsating sdBs are preferentially found at higher luminosity than their constant counterparts. This trend is possibly related to the time it takes for the iron and nickel reservoir to build-up

in the Z-bump region at a sufficient level, via radiative levitation (in competition with other processes), to start driving effectively pulsations;

- Among the stars with MMT spectra, we identified seven objects that show hints of helium stratification from the inspection of the fit of their helium lines, six of which were not known to exhibit such features. They have  $T_{\text{eff}}$  in a narrow range between 28 and 31 kK, in line with the few stars already known to display helium stratification (Schneider et al. 2018; Geier et al. 2013). Unfortunately, the resolution of our MMT spectra is too low to detect the presence of  $^3\text{He}$ . We believe that stratification, and the presence of  $^3\text{He}$ , is more common than suspected in this temperature range, but detecting it requires at least medium spectral resolution, sufficiently high S/N, and a detailed inspection of the spectral fits (Sect. 4.2.2);
- The H-rich sdBs and sdOs have a similar mass distribution, with a median value around  $0.47 M_{\odot}$  (Table 2), in good agreement with the theoretical expectation for the canonical mass at the He-core flash. The dispersions of the sdB and sdO mass distributions are consistent with the uncertainties of the individual mass measurements, which are around 18% ( $\sim 0.08 M_{\odot}$ ), suggesting no significant intrinsic scatter in the masses of these stars. We see no significant low-mass or high-mass tail in their mass distributions (Sect. 5.1, Fig. 11). Combined with the fact that there is no significant difference between the mass distribution of the close binaries (identified from RV variations) and the single hot subdwarfs, we believe that the merger channels do not significantly contribute to the formation of hydrogen-rich hot subdwarfs (Sect. 5.2);
- Candidate low-mass sdBs ( $M < 0.45 M_{\odot}$ ) selected from their position in the HRD only represent a small fraction ( $< 6\%$ ) of our EHB population (Sect. 5.3). Their masses from parallax and SED fits are, on average, lower than canonical and they are likely the progeny of intermediate-mass MS stars ( $2\text{--}3.5 M_{\odot}$ ) that ignited helium in a non-degenerate core;
- The positions of the He-sdOs in the HRD follow the theoretical helium main sequence remarkably well (Fig. 5). According to their position along this sequence, the majority of them have masses between  $0.6$  and  $1.0 M_{\odot}$ , indicating a wider mass range than derived for their H-rich counterparts. The masses obtained from the parallax and SED fits also span a wide range, with 68% of them ( $Q_{16}\text{--}Q_{84}$ ) falling within  $0.48\text{--}1.14 M_{\odot}$  and a median mass of  $0.78 M_{\odot}$ . Their mass dispersion is larger than expected from the individual uncertainties alone (Table 2). A dominant contribution by merger channels is the most likely explanation for this wide mass distribution and relatively large average mass (Sect. 5.1).

## Data availability

An extended version of Table D.1 including additional information (i.e., columns) for each star is available at the CDS via <https://cdsarc.cds.unistra.fr/viz-bin/cat/J/A+A/705/A248>. All of the Bok spectra analyzed here are available as ascii files at the CDS. Table D.1, and additional figures in Appendix E can be found on Zenodo at <https://zenodo.org/records/17523833>. This includes the MMT spectral atlas, and figures showing the best-fit solutions for the Bok spectra and SED fits of the stars in our sample.

*Acknowledgements.* We are forever grateful to Gilles Fontaine, who started this project with Betsy Green two decades ago. Thanks to the data and records that he kept, we were able to bring his work to completion and achieve much more than would have been possible in 2005. G.F. would have thanked Pierre Bergeron for his help in the very early phase of this project. We are thankful for those who shared with us their unpublished data to help us track down pulsators and RV variable stars: W. Zong, S. Geier, F. Mattig, H. Dawson, and V. Schaffenroth. M.L. acknowledges funding from the Deutsche Forschungsgemeinschaft (grant LA 4383/4-1). M.D. was supported by the Deutsches Zentrum für Luft- und Raumfahrt (DLR) through grant 50-OR-2304. V.V.G. is a F.R.S.-FNRS Research Associate. S.C. acknowledge support from the Centre National d'Études Spatiales (CNES, France), focused on the mission TESS. This work has made use of data from the European Space Agency (ESA) mission *Gaia* (<https://www.cosmos.esa.int/gaia>), processed by the *Gaia* Data Processing and Analysis Consortium (DPAC, <https://www.cosmos.esa.int/web/gaia/dpac/consortium>). Funding for the DPAC has been provided by national institutions, in particular the institutions participating in the *Gaia* Multilateral Agreement. This work has made use of IRAF, which was distributed by the National Optical Astronomy Observatory, USA, which is operated by the Association of Universities for Research in Astronomy, Inc., under a cooperative agreement with the National Science Foundation. This research has made use of NASA's Astrophysics Data System Bibliographic Services, of the SIMBAD database (Wenger et al. 2000), operated at CDS, Strasbourg, France, and of the VizieR catalogue access tool (Ochsenbein et al. 2000), CDS, Strasbourg Astronomical Observatory, France (DOI : 10.26909/cds/vizieR). This research has made use of TOPCAT (Taylor 2005) and the PYTHON packages pandas (pandas development team 2020) and MATPLOTLIB (Hunter 2007).

## References

- Ahmad, A., Jeffery, C. S., & Fullerton, A. W. 2004, *A&A*, 418, 275
- Alam, S., Albareti, F. D., Allende Prieto, C., et al. 2015, *ApJS*, 219, 12
- Arancibia-Rojas, E., Zorotovic, M., Vučković, M., et al. 2024, *MNRAS*, 527, 11184
- Asplund, M., Grevesse, N., Sauval, A. J., & Scott, P. 2009, *ARA&A*, 47, 481
- Baran, A. S., Telting, J. H., Jeffery, C. S., et al. 2019, *MNRAS*, 489, 1556
- Baran, A. S., Charpinet, S., Østensen, R. H., et al. 2024, *A&A*, 686, A65
- Barlow, B. N., Corcoran, K. A., Parker, I. M., et al. 2022, *ApJ*, 928, 20
- Beauchamp, A., Wesemael, F., & Bergeron, P. 1997, *ApJS*, 108, 559
- Bédard, A., Bergeron, P., Brassard, P., & Fontaine, G. 2020, *ApJ*, 901, 93
- Bianchi, L., Shiao, B., & Thilker, D. 2017, *ApJS*, 230, 24
- Blanchette, J. P., Chayer, P., Wesemael, F., et al. 2008, *ApJ*, 678, 1329
- Brassard, P., Fontaine, G., Billères, M., et al. 2001, *ApJ*, 563, 1013
- Brown, T. M., Sweigart, A. V., Lanz, T., Landsman, W. B., & Hubeny, I. 2001, *ApJ*, 562, 368
- Brown, T. M., Cassisi, S., D'Antona, F., et al. 2016, *ApJ*, 822, 44
- Butler, K., & Giddings, J. 1985, Newsletter on the analysis of astronomical spectra No. 9. University of London
- Charpinet, S., Fontaine, G., Brassard, P., et al. 1997, *ApJ*, 483, L123
- Charpinet, S., Fontaine, G., Brassard, P., & Dorman, B. 2002, *ApJS*, 139, 487
- Charpinet, S., Fontaine, G., Brassard, P., et al. 2005a, in *Astronomical Society of the Pacific Conference Series*, 334, 14th European Workshop on White Dwarfs, eds. D. Koester, & S. Moehler, 619
- Charpinet, S., Fontaine, G., Brassard, P., Green, E. M., & Chayer, P. 2005b, *A&A*, 437, 575
- Charpinet, S., Green, E. M., Baglin, A., et al. 2010, *A&A*, 516, L6
- Copperwheat, C. M., Morales-Rueda, L., Marsh, T. R., Maxted, P. F. L., & Heber, U. 2011, *MNRAS*, 415, 1381
- Culpan, R., Dorsch, M., Geier, S., et al. 2024, *A&A*, 685, A134
- Dawson, H., Dorsch, M., Geier, S., et al. 2026, *A&A*, in press, <https://doi.org/10.1051/0004-6361/202558123>
- D'Cruz, N. L., Dorman, B., Rood, R. T., & O'Connell, R. W. 1996, *ApJ*, 466, 359
- De Angeli, F., Weiler, M., Montegriffo, P., et al. 2023, *A&A*, 674, A2
- Dorman, B., Rood, R. T., & O'Connell, R. W. 1993, *ApJ*, 419, 596
- Dorsch, M. 2024, PhD thesis, Friedrich Alexander University of Erlangen-Nuremberg, Germany
- Dorsch, M., Reindl, N., Pelisoli, I., et al. 2022, *A&A*, 658, L9
- Dorsch, M., Jeffery, C. S., Philip Monai, A., et al. 2024, *A&A*, 691, A165
- Downes, R. A. 1986, *ApJS*, 61, 569
- Driebe, T., Schoenberner, D., Bloeker, T., & Herwig, F. 1998, *A&A*, 339, 123
- Edelmann, H. 2003, PhD thesis, Friedrich Alexander University of Erlangen-Nuremberg, Germany
- Edelmann, H., Heber, U., & Napiwotzki, R. 2001, *Astron. Nachr.*, 322, 401
- Edelmann, H., Heber, U., Hagen, H. J., et al. 2003, *A&A*, 400, 939
- Edelmann, H., Heber, U., Lisker, T., & Green, E. M. 2004, *Ap&SS*, 291, 315
- El-Badry, K., Rix, H.-W., & Heintz, T. M. 2021, *MNRAS*, 506, 2269

- Feige, J. 1958, *ApJ*, **128**, 267
- Filiz, S., Werner, K., Rauch, T., & Reindl, N. 2024, *A&A*, **691**, A290
- Fitzpatrick, M. J., Olsen, K., Economou, F., et al. 2014, *SPIE Conf. Ser.*, **9149**, 91491T
- Fitzpatrick, E. L., Massa, D., Gordon, K. D., Bohlin, R., & Clayton, G. C. 2019, *ApJ*, **886**, 108
- Flewelling, H. 2018, in *American Astronomical Society Meeting Abstracts*, 231, 436.01
- Fontaine, G., & Chayer, P. 1997, in *The Third Conference on Faint Blue Stars*, eds. A. G. D. Philip, J. Liebert, R. Saffer, & D. S. Hayes, 169
- Fontaine, G., Brassard, P., Charpinet, S., et al. 2003, *ApJ*, **597**, 518
- Fontaine, G., Brassard, P., Charpinet, S., & Chayer, P. 2006, *Mem. Soc. Astron. Italiana*, **77**, 49
- Fontaine, G., Brassard, P., Charpinet, S., et al. 2012, *A&A*, **539**, A12
- Fontaine, G., Green, E., Brassard, P., Latour, M., & Chayer, P. 2014, in *Astronomical Society of the Pacific Conference Series*, 481, 6th Meeting on Hot Subdwarf Stars and Related Objects, eds. V. van Grootel, E. Green, G. Fontaine, & S. Charpinet, 83
- Fontaine, G., Bergeron, P., Brassard, P., et al. 2019, *ApJ*, **880**, 79
- For, B. Q., Green, E. M., Fontaine, G., et al. 2010, *ApJ*, **708**, 253
- Gaia Collaboration (Brown, A. G. A., et al.) 2021, *A&A*, **649**, A1
- Geier, S. 2013, *A&A*, **549**, A110
- Geier, S., Nesslinger, S., Heber, U., et al. 2008, *A&A*, **477**, L13
- Geier, S., Heber, U., Edelmann, H., et al. 2013, *A&A*, **557**, A122
- Geier, S., Dorsch, M., Pelisoli, I., et al. 2022, *A&A*, **661**, A113
- Geier, S., Heber, U., Irrgang, A., et al. 2024, *A&A*, **690**, A368
- Giddings, J. R. 1981, PhD thesis, Moscow University
- Gigosos, M. A., & González, M. Á. 2009, *A&A*, **503**, 293
- Green, R. F., Schmidt, M., & Liebert, J. 1986, *ApJS*, **61**, 305
- Green, E. M., Fontaine, G., Reed, M. D., et al. 2003, *ApJ*, **583**, L31
- Green, E. M., For, B., Hyde, E. A., et al. 2004, *Ap&SS*, **291**, 267
- Green, E. M., For, B. Q., & Hyde, E. A. 2005, in *Astronomical Society of the Pacific Conference Series*, 334, 14th European Workshop on White Dwarfs, eds. D. Koester, & S. Moehler, 363
- Green, E. M., Fontaine, G., Hyde, E. A., For, B. Q., & Chayer, P. 2008, in *Astronomical Society of the Pacific Conference Series*, 392, Hot Subdwarf Stars and Related Objects, eds. U. Heber, C. S. Jeffery, & R. Napiwotzki, 75
- Green, E. M., Guvenen, B., O'Malley, C. J., et al. 2011, *ApJ*, **734**, 59
- Hall, P. D., & Jeffery, C. S. 2016, *MNRAS*, **463**, 2756
- Han, Z., Podsiadlowski, P., Maxted, P. F. L., Marsh, T. R., & Ivanova, N. 2002, *MNRAS*, **336**, 449
- Han, Z., Podsiadlowski, P., Maxted, P. F. L., & Marsh, T. R. 2003, *MNRAS*, **341**, 669
- He, R., Meng, X., Lei, Z., Yan, H., & Lan, S. 2025, *A&A*, **693**, A121
- Heber, U. 1991, in *IAU Symposium*, 145, Evolution of Stars: the Photospheric Abundance Connection, eds. G. Michaud, & A. V. Tutukov, 363
- Heber, U. 2009, *ARA&A*, **47**, 211
- Heber, U. 2016, *PASP*, **128**, 082001
- Heber, U. 2024, arXiv e-prints [arXiv:2410.11663]
- Heber, U. 2026, in *Encyclopedia of Astrophysics*, 2, 488
- Heber, U., Reid, I. N., & Werner, K. 1999, *A&A*, **348**, L25
- Heber, U., Drechsel, H., Østensen, R., et al. 2004, *A&A*, **420**, 251
- Heber, U., Irrgang, A., & Schaffenroth, J. 2018, *Open Astron.*, **27**, 35
- Hidalgo, S. L., Pietrinferni, A., Cassisi, S., et al. 2018, *ApJ*, **856**, 125
- Houck, J. C., & Denicola, L. A. 2000, in *Astronomical Society of the Pacific Conference Series*, 216, Astronomical Data Analysis Software and Systems IX, eds. N. Manset, C. Veillet, & D. Crabtree, 591
- Hu, H., Dupret, M. A., Aerts, C., et al. 2008, *A&A*, **490**, 243
- Hu, H., Tout, C. A., Glebbeek, E., & Dupret, M. A. 2011, *MNRAS*, **418**, 195
- Hubeny, I., & Lanz, T. 2011a, Synspec: General Spectrum Synthesis Program, Astrophysics Source Code Library [record ascl:1109.022]
- Hubeny, I., & Lanz, T. 2011b, TLUSTY: Stellar Atmospheres, Accretion Disks, and Spectroscopic Diagnostics, Astrophysics Source Code Library [record ascl:1109.021]
- Hubeny, I., & Lanz, T. 2017a, arXiv e-prints [arXiv:1706.01859]
- Hubeny, I., & Lanz, T. 2017b, arXiv e-prints [arXiv:1706.01935]
- Hubeny, I., & Lanz, T. 2017c, arXiv e-prints [arXiv:1706.01937]
- Hubeny, I., Hummer, D. G., & Lanz, T. 1994, *A&A*, **282**, 151
- Hunter, J. D. 2007, *Comput. Sci. Eng.*, **9**, 90
- Husser, T.-O., Wende-von Berg, S., Dreizler, S., et al. 2013, *A&A*, **553**, A6
- Iben, Jr., I. 1967, *ApJ*, **147**, 624
- Irrgang, A., Przybilla, N., Heber, U., et al. 2014, *A&A*, **565**, A63
- Irrgang, A., Kreuzer, S., Heber, U., & Brown, W. 2018, *A&A*, **615**, L5
- Irrgang, A., Geier, S., Heber, U., et al. 2021, *A&A*, **650**, A102
- Irrgang, A., Przybilla, N., & Meynet, G. 2022, *Nat. Astron.*, **6**, 1414
- Istrate, A. G., Marchant, P., Tauris, T. M., et al. 2016, *A&A*, **595**, A35
- Jeffery, C. S. 2020, *MNRAS*, **496**, 718
- Jeffery, C. S., & Saio, H. 2006, *MNRAS*, **371**, 659
- Jeffery, C. S., & Saio, H. 2007, *MNRAS*, **378**, 379
- Jeffery, C. S., Miszalski, B., & Snowdon, E. 2021, *MNRAS*, **501**, 623
- Justham, S., Podsiadlowski, P., & Han, Z. 2011, *MNRAS*, **410**, 984
- Kilkenny, D., Koen, C., O'Donoghue, D., et al. 1999, *MNRAS*, **303**, 525
- Kilkenny, D., Fontaine, G., Green, E. M., & Schuh, S. 2010, *Inform. Bull. Variable Stars*, **5927**, 1
- Koen, C. 2011, *MNRAS*, **415**, 3042
- Kurucz, R. L. 1996, in *Astronomical Society of the Pacific Conference Series*, 108, M.A.S.S., Model Atmospheres and Spectrum Synthesis, eds. S. J. Adelman, F. Kupka, & W. W. Weiss, 2
- Lara, N., González, M. Á., & Gigosos, M. A. 2012, *A&A*, **542**, A75
- Latour, M., Fontaine, G., Chayer, P., & Brassard, P. 2013, *ApJ*, **773**, 84
- Latour, M., Fontaine, G., Green, E. M., & Brassard, P. 2015, *A&A*, **579**, A39
- Latour, M., Randall, S. K., Calamida, A., Geier, S., & Moehler, S. 2018, *A&A*, **618**, A15
- Latour, M., Green, E. M., & Fontaine, G. 2019, *A&A*, **623**, L12
- Lei, Z., He, R., Németh, P., et al. 2023, *ApJ*, **953**, 122
- Lindgren, L., Bastian, U., Biermann, M., et al. 2021, *A&A*, **649**, A4
- Mason, B. D., Wycoff, G. L., Hartkopf, W. I., Douglass, G. G., & Worley, C. E. 2001, *AJ*, **122**, 3466
- Maxted, P. F. L., Moran, C. K. J., Marsh, T. R., & Gatti, A. A. 2000, *MNRAS*, **311**, 877
- Maxted, P. F. L., Heber, U., Marsh, T. R., & North, R. C. 2001, *MNRAS*, **326**, 1391
- Maxted, P. F. L., Marsh, T. R., Heber, U., et al. 2002, *MNRAS*, **333**, 231
- Miller Bertolami, M. M., Althaus, L. G., Unglaub, K., & Weiss, A. 2008, *A&A*, **491**, 253
- Moehler, S., & Heber, U. 1998, *A&A*, **335**, 985
- Momany, Y., Piotto, G., Recio-Blanco, A., et al. 2002, *ApJ*, **576**, L65
- Moni Bidin, C., Villanova, S., Piotto, G., Moehler, S., & D'Antona, F. 2011, *ApJ*, **738**, L10
- Montalbán, J., & Noels, A. 2013, in *European Physical Journal Web of Conferences*, 43, 03002
- Morales-Rueda, L., Maxted, P. F. L., Marsh, T. R., North, R. C., & Heber, U. 2003, *MNRAS*, **338**, 752
- Napiwotzki, R., Karl, C. A., Lisker, T., et al. 2004, *Ap&SS*, **291**, 321
- Naslim, N., Jeffery, C. S., Hibbert, A., & Behara, N. T. 2013, *MNRAS*, **434**, 1920
- Newell, B., & Graham, J. A. 1976, *ApJ*, **204**, 804
- Nieva, M. F., & Przybilla, N. 2007, *A&A*, **467**, 295
- Noels-Grotsch, A., & Miglio, A. 2025, *The Golden Gift of Red Giants (IOP Publishing)*, 2514
- Norris, J. M., Wright, J. T., Wade, R. A., Mahadevan, S., & Gettel, S. 2011, *ApJ*, **743**, 88
- Ochsenbein, F., Bauer, P., & Marcout, J. 2000, *A&AS*, **143**, 23
- Østensen, R., Heber, U., Silvotti, R., et al. 2001, *A&A*, **378**, 466
- Østensen, R., Heber, U., & Maxted, P. 2005, in *Astronomical Society of the Pacific Conference Series*, 334, 14th European Workshop on White Dwarfs, eds. D. Koester, & S. Moehler, 435
- Østensen, R. H., Oreiro, R., Hu, H., Drechsel, H., & Heber, U. 2008, in *Astronomical Society of the Pacific Conference Series*, 392, Hot Subdwarf Stars and Related Objects, eds. U. Heber, C. S. Jeffery, & R. Napiwotzki, 221
- Østensen, R. H., Oreiro, R., Solheim, J. E., et al. 2010, *A&A*, **513**, A6
- Østensen, R. H., Silvotti, R., Charpinet, S., et al. 2011, *MNRAS*, **414**, 2860
- Østensen, R. H., Jeffery, C. S., Saio, H., et al. 2020, *MNRAS*, **499**, 3738
- Paczynski, B. 1971, *Acta Astron.*, **21**, 1
- pandas development team, T. 2020, <https://doi.org/10.5281/zenodo.3509134>
- Pelisoli, I., Dorsch, M., Heber, U., et al. 2022, *MNRAS*, **515**, 2496
- Pereira, C. 2011, PhD thesis, Queens University Belfast, Ireland
- Politano, M., Taam, R. E., van der Sluys, M., & Willems, B. 2008, *ApJ*, **687**, L99
- Przybilla, N. 2005, *A&A*, **443**, 293
- Przybilla, N., & Butler, K. 2004, *ApJ*, **609**, 1181
- Przybilla, N., Butler, K., Becker, S. R., & Kudritzki, R. P. 2006, *A&A*, **445**, 1099
- Przybilla, N., Nieva, M.-F., & Butler, K. 2011, in *Journal of Physics Conference Series*, 328, 012015
- Randall, S. K., Green, E. M., Van Grootel, V., et al. 2007, *A&A*, **476**, 1317
- Ricker, G. R., Winn, J. N., Vanderspek, R., et al. 2014, *SPIE Conf. Ser.*, **9143**, 914320
- Rodríguez-Segovia, N., & Ruiters, A. J. 2025, *MNRAS*, **539**, 3273
- Saffer, R. A., Bergeron, P., Koester, D., & Liebert, J. 1994, *ApJ*, **432**, 351
- Saffer, R. A., Livio, M., & Yungelson, L. R. 1998, *ApJ*, **502**, 394
- Saio, H., & Jeffery, C. S. 2000, *MNRAS*, **313**, 671
- Saio, H., & Jeffery, C. S. 2002, *MNRAS*, **333**, 121
- Salaris, M., & Cassisi, S. 2005, *Evolution of Stars and Stellar Populations* (Chichester, UK: John Wiley & Sons)
- Sandage, A. 1962, *ApJ*, **135**, 333
- Schaffenroth, V., Pelisoli, I., Barlow, B. N., Geier, S., & Kupfer, T. 2022, *A&A*, **666**, A182

- Schneider, D. 2022, PhD thesis, Friedrich-Alexander-Universität Erlangen-Nürnberg
- Schneider, D., Irrgang, A., Heber, U., Nieva, M. F., & Przybilla, N. 2018, *A&A*, **618**, A86
- Şener, H. T., & Jeffery, C. S. 2014, *MNRAS*, **440**, 2676
- Silvotti, R., Østensen, R., Heber, U., et al. 2002, *A&A*, **383**, 239
- Silvotti, R., Ostensen, R. H., & Telting, J. H. 2020, <https://doi.org/10.5281/zenodo.3662729>
- Skrutskie, M. F., Cutri, R. M., Stiening, R., et al. 2006, *AJ*, **131**, 1163
- Snowdon, E. J., Jeffery, C. S., Schlagenhauf, S., & Dorsch, M. 2025, *MNRAS*, **537**, 2079
- Stark, M. A., & Wade, R. A. 2003, *AJ*, **126**, 1455
- Sweigart, A. V. 1987, *ApJS*, **65**, 95
- Taylor, M. B. 2005, in *Astronomical Society of the Pacific Conference Series*, 347, Astronomical Data Analysis Software and Systems XIV, eds. P. Shopbell, M. Britton, & R. Ebert, 29
- Telting, J. H., Østensen, R. H., Baran, A. S., et al. 2012, *A&A*, **544**, A1
- Telting, J. H., Baran, A. S., Nemeth, P., et al. 2014, *A&A*, **570**, A129
- Théado, S., Vauclair, S., Alecian, G., & LeBlanc, F. 2009, *ApJ*, **704**, 1262
- Tody, D. 1986, *SPIE Conf. Ser.*, **627**, 733
- Tody, D. 1993, in *Astronomical Society of the Pacific Conference Series*, 52, Astronomical Data Analysis Software and Systems II, eds. R. J. Hanisch, R. J. V. Brissenden, & J. Barnes, 173
- Tremblay, P. E., & Bergeron, P. 2009, *ApJ*, **696**, 1755
- Uzundag, M., Krzesinski, J., Pelisoli, I., et al. 2024, VizieR Online Data Catalog: Pulsating hot subdwarf B stars (Uzundag+, 2024), *VizieR On-line Data Catalog: J/A+A/684/A118*. Originally published in: 2024A&A...684A.118U
- Van Grootel, V. 2008, PhD thesis, University of Montreal, Canada
- Van Grootel, V., Charpinet, S., Fontaine, G., & Brassard, P. 2010, *Ap&SS*, **329**, 217
- Villaseñor, J. I., Lennon, D. J., Picco, A., et al. 2023, *MNRAS*, **525**, 5121
- Vos, J., Németh, P., Vučković, M., Østensen, R., & Parsons, S. 2018, *MNRAS*, **473**, 693
- Vos, J., Vučković, M., Chen, X., et al. 2019, *MNRAS*, **482**, 4592
- Vučković, M., Aerts, C., Østensen, R., et al. 2007, *A&A*, **471**, 605
- Webbink, R. F. 1984, *ApJ*, **277**, 355
- Wenger, M., Ochsenbein, F., Egret, D., et al. 2000, *A&AS*, **143**, 9
- Werner, K. 1996, *ApJ*, **457**, L39
- Werner, K., Reindl, N., Geier, S., & Pritzkeleit, M. 2022, *MNRAS*, **511**, L66
- Williams, T., McGraw, J. T., & Grashuis, R. 2001, *PASP*, **113**, 490
- Xiong, H., Chen, X., Podsiadlowski, P., Li, Y., & Han, Z. 2017, *A&A*, **599**, A54
- Zhang, X., & Jeffery, C. S. 2012, *MNRAS*, **419**, 452
- Zong, W., Charpinet, S., Vauclair, G., Giammichele, N., & Van Grootel, V. 2016, *A&A*, **585**, A22

## Appendix A: Stars with composite SED

Twenty nine stars in our sample were found to have IR excess that could be reproduced by a MS companion. The stars are listed in Table A.1, where the atmospheric parameters of the hot subdwarfs are indicated, as well as the  $T_{\text{eff}}$ , radius  $R$  and luminosity  $L$  of the companion according to the best fit of the SED. Some of these systems are long period binaries for which the *Gaia* single-star astrometric solution is not necessarily accurate (when  $\text{ruwe} \gtrsim 1.4$ ), thus we also indicate the value of this parameter in the Table. In Fig. A.1, we show the  $T_{\text{eff}}$  and luminosity of the MS companions as well as the position of the zero-age MS track for two different metallicities. Not all of the stars for which we detected IR-excess were already known to be binaries, and for some of the known binaries, it was not previously clear from the RVs whether the companion was a WD or a low-mass MS star. We briefly discuss a few cases that are of particular interest or that have not been previously reported as composite systems.

HD149382 is the brightest known hot subdwarf. It has been claimed to have a substellar companion on the basis of radial velocity measurements, however no RV variations were detected in follow-up studies (Norris et al. 2011; Silvotti et al. 2020). The star has a visual companion  $1''$  (75 AU) away that is probably the source of the IR-excess (Ostensen et al. 2005), and likely constitute a background object (Schneider 2022).

PB7032 is a slow pulsator (Koen 2011) that has not been reported to be part of a binary system previously. Our SED fit indicates the presence of a M-dwarf companion ( $T_{\text{eff}} \sim 3400$  K). The quality of the TESS data for this star are poor and we find no hint of low-frequency variability in the Lomb-Scargle periodogram (LSP) that could be associated with a reflection effect.

PG0014+068 is a rapid pulsator that has been extensively observed with time-series photometry and well-studied from an asteroseismic point of view (Brassard et al. 2001; Charpinet et al. 2005a). It has always been considered a single star and the RVs of the MMT spectra do not show large variations ( $\sigma=2.2$  km s $^{-1}$  for 4 measurements taken within 12 days). However, the SED of the star shows a strong IR excess that can be reproduced with a K-type companion ( $T_{\text{eff}} \sim 4700$  K). The TESS light curve of PG0014+068 does not show any sign of a reflection effect. The system possibly has a period of the order of tens of days, or longer.

PG0250+189 shows an IR-excess that corresponds to an early M or late K star ( $T_{\text{eff}} \sim 3800$  K). This star is among the few objects located below the ZAEHB (see Fig. 13, but also Saffer et al. 1994). Unfortunately, neither a TESS light curve nor RV measurements were found in the literature.

PG0940+068 is a slowly pulsating sdB and a known binary with a period of 8.33 d (Maxted et al. 2000), however it was initially not clear whether the companion is a WD or dM star. Based on the absence of variations in the TESS light curve, Schaffenroth et al. (2022) classified the companion as a WD. The star's SED shows a mild IR-excess that can be reproduced with a late M-type star ( $T_{\text{eff}} \sim 3250$  K).

PG1340+607 is a slowly pulsating sdB that has not previously been reported to be part of a binary system. However, the radial velocities measured from the two MMT spectra showed a difference of 10 km s $^{-1}$ , thus suggesting a possible binary nature. The SED of the star shows a mild IR-excess that can be reproduced with a late M-type star ( $T_{\text{eff}} \sim 3300$  K). The LSP of the TESS light curve shows a peak (SNR=8.7) at 3.8h that is separated from the  $g$ -modes found at shorter periods. This peak could be due to a reflection effect, although a long-period  $g$ -mode can

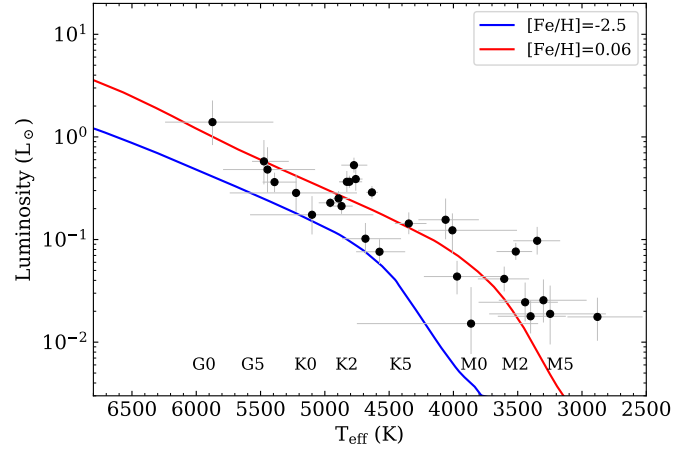


Fig. A.1: HR diagram for the stellar companions of the hot subdwarfs with composite spectra. The parameters are derived from the fits of SED. The solid lines show the expected parameters for MS stars at  $[\text{Fe}/\text{H}] = 0.06$  (red) and  $-2.5$  (blue) as obtained from BaSTI isochrones.

not be ruled out. Additional RV measurements are needed to establish the orbital period.

PG2151+100 has been reported as an RV variable star with a faint MS companion but unknown period (Green et al. 2005; Edelmann 2003). Our SED fit suggests the presence of a late M-dwarf star ( $T_{\text{eff}} \sim 3300$  K). In addition, the LSP of the TESS data shows a strong signal at 40.06h in an otherwise featureless light curve. The TESS signal is most likely due to the stellar spots on the companion's surface.

PG1101+249 (Feige 36) is a known binary with a period of 8.5 h (Saffer et al. 1998) and a companion that was believed to be a WD. However, the SED shows a mild IR-excess that we reproduce with a stellar companion at  $T_{\text{eff}} \sim 3300$  K. The TESS light curve does not show any variability at the orbital period.

PG2317+046 (PB5333) is a known binary for which Edelmann et al. (2004) reported a period of 22.2 h. The SED shows a strong IR excess that we reproduce with an early-M type star ( $T_{\text{eff}} \sim 3500$  K). The periodogram of the TESS data show a clear peak at 19.87 h and the presence of the first harmonic. However recent investigations by Schaffenroth et al. (priv. comm. 2024) found the system to have a much longer period ( $\sim 92$  days) and a somewhat hotter companion (K8V).

PG1154-070 is not a known binary, and did not show large RV variations in the study of Saffer et al. (1998). Its IR-excess indicates a late K-type companion ( $T_{\text{eff}} \sim 4000$  K).

HS2151+0857 (a  $p$ -mode pulsator according to Østensen et al. 2001), HS1824+5745 and PG2303+019 (also known as HS2303+0152, and a  $p$ -mode pulsator according to Silvotti et al. 2002) have IR-excesses that suggest the presence of late K-type companions. The three stars are also part of the sample analyzed by Heber et al. (in prep.) who found similar properties for the companions.

PG0823+546 and PG2158+082 are two hot He-sdO composites with a visible IR-excess that corresponds to early K or late G companions (see also Williams et al. 2001). These are interesting objects given that the fraction of composite systems among He-sdOs is relatively small ( $\sim 9\%$ , Dorsch 2024) compared to that of sdBs ( $\sim 30\%$ , Stark & Wade 2003).

Table A.1: Properties of the hot subdwarf systems with IR-excess

Star	$T_{\text{eff}}$ (K)	$\log g$ ( $\text{cm s}^{-2}$ )	$\log N(\text{He})/N(\text{H})$	$T_{\text{eff, comp}}$ (K)	$R_{\text{comp}}$ ( $R_{\odot}$ )	$\log(L_{\text{comp}})$ ( $L_{\odot}$ )	<i>Gaia</i> ruwe
HD149382	35519	5.80	-1.48	2879 <sup>+233</sup> <sub>-350</sub>	0.54 <sup>+0.08</sup> <sub>-0.05</sub>	-1.75 <sup>+0.19</sup> <sub>-0.23</sub>	1.20
PG0940+068	26953	5.41	-2.79	3247 <sup>+474</sup> <sub>-433</sub>	0.44 <sup>+0.08</sup> <sub>-0.07</sub>	-1.72 <sup>+0.28</sup> <sub>-0.30</sub>	1.02
PG1340+607	25606	5.30	-2.62	3299 <sup>+347</sup> <sub>-336</sub>	0.49 <sup>+0.06</sup> <sub>-0.06</sub>	-1.59 <sup>+0.20</sup> <sub>-0.22</sub>	1.07
PG2151+100	33946	5.61	-3.66	3348 <sup>+186</sup> <sub>-178</sub>	0.93 <sup>+0.11</sup> <sub>-0.09</sub>	-1.01 <sup>+0.13</sup> <sub>-0.13</sub>	2.17
PG1101+249	28841	5.67	-2.01	3399 <sup>+255</sup> <sub>-274</sub>	0.39 <sup>+0.04</sup> <sub>-0.03</sub>	-1.75 <sup>+0.15</sup> <sub>-0.17</sub>	0.95
PB7032	27122	5.49	-2.82	3442 <sup>+362</sup> <sub>-254</sub>	0.44 <sup>+0.05</sup> <sub>-0.06</sub>	-1.61 <sup>+0.19</sup> <sub>-0.19</sub>	0.94
PG2317+046	44970	6.05	-2.82	3515 <sup>+149</sup> <sub>-127</sub>	0.74 <sup>+0.04</sup> <sub>-0.04</sub>	-1.12 <sup>+0.08</sup> <sub>-0.08</sub>	0.93
FEIGE34	61095	5.92	-1.89	3601 <sup>+204</sup> <sub>-192</sub>	0.52 <sup>+0.05</sup> <sub>-0.04</sub>	-1.38 <sup>+0.12</sup> <sub>-0.12</sub>	2.24
PG0250+189	25562	5.75	-3.84	3858 <sup>+933</sup> <sub>-511</sub>	0.27 <sup>+0.04</sup> <sub>-0.03</sub>	-1.82 <sup>+0.37</sup> <sub>-0.29</sub>	1.10
PG1154-070	27637	5.53	-2.40	3971 <sup>+257</sup> <sub>-343</sub>	0.45 <sup>+0.05</sup> <sub>-0.04</sub>	-1.36 <sup>+0.15</sup> <sub>-0.17</sub>	3.11
PG1618+563	35405	5.83	-1.69	4006 <sup>+268</sup> <sub>-501</sub>	0.75 <sup>+0.08</sup> <sub>-0.08</sub>	-0.91 <sup>+0.17</sup> <sub>-0.23</sub>	1.98
HS2151+0857	35883	5.80	-1.42	4060 <sup>+211</sup> <sub>-258</sub>	0.80 <sup>+0.19</sup> <sub>-0.13</sub>	-0.81 <sup>+0.21</sup> <sub>-0.19</sub>	0.99
HS1824+5745	35248	5.84	-1.61	4345 <sup>+129</sup> <sub>-154</sub>	0.67 <sup>+0.08</sup> <sub>-0.07</sub>	-0.85 <sup>+0.11</sup> <sub>-0.11</sub>	1.20
PG2303+019	36839	5.77	-1.71	4574 <sup>+181</sup> <sub>-199</sub>	0.44 <sup>+0.05</sup> <sub>-0.04</sub>	-1.12 <sup>+0.12</sup> <sub>-0.12</sub>	1.03
PG1647+253	36073	5.84	-2.08	4633 <sup>+44</sup> <sub>-46</sub>	0.83 <sup>+0.06</sup> <sub>-0.06</sub>	-0.54 <sup>+0.06</sup> <sub>-0.06</sub>	1.42
PG0014+068	35638	5.93	-1.62	4684 <sup>+181</sup> <sub>-277</sub>	0.49 <sup>+0.08</sup> <sub>-0.06</sub>	-0.99 <sup>+0.15</sup> <sub>-0.15</sub>	1.15
PHL1079	32910	5.60	-2.19	4759 <sup>+48</sup> <sub>-53</sub>	0.92 <sup>+0.12</sup> <sub>-0.11</sub>	-0.41 <sup>+0.11</sup> <sub>-0.11</sub>	4.67
PG1610+519	43897	5.54	-3.14	4773 <sup>+98</sup> <sub>-103</sub>	1.07 <sup>+0.08</sup> <sub>-0.07</sub>	-0.28 <sup>+0.07</sup> <sub>-0.07</sub>	1.98
PG1206+165	28833	5.58	-2.44	4808 <sup>+76</sup> <sub>-75</sub>	0.87 <sup>+0.05</sup> <sub>-0.05</sub>	-0.44 <sup>+0.06</sup> <sub>-0.06</sub>	2.02
PG1018-047	31448	5.60	-4.00	4828 <sup>+61</sup> <sub>-118</sub>	0.87 <sup>+0.11</sup> <sub>-0.09</sub>	-0.44 <sup>+0.10</sup> <sub>-0.10</sub>	3.48
TON357	65722	5.94	-1.85	4870 <sup>+66</sup> <sub>-86</sub>	0.65 <sup>+0.06</sup> <sub>-0.05</sub>	-0.67 <sup>+0.08</sup> <sub>-0.07</sub>	1.51
PG0749+658	25958	5.57	-3.31	4893 <sup>+40</sup> <sub>-85</sub>	0.70 <sup>+0.05</sup> <sub>-0.05</sub>	-0.60 <sup>+0.07</sup> <sub>-0.07</sub>	4.49
PG0934+553	45326	5.79	-0.50	4957 <sup>+89</sup> <sub>-107</sub>	0.65 <sup>+0.02</sup> <sub>-0.02</sub>	-0.64 <sup>+0.05</sup> <sub>-0.05</sub>	1.15
PG0823+546	75000	5.76	0.14	5099 <sup>+482</sup> <sub>-477</sub>	0.53 <sup>+0.06</sup> <sub>-0.05</sub>	-0.76 <sup>+0.18</sup> <sub>-0.19</sub>	1.09
PG2158+082	62500	5.86	1.75	5224 <sup>+516</sup> <sub>-473</sub>	0.65 <sup>+0.06</sup> <sub>-0.05</sub>	-0.55 <sup>+0.18</sup> <sub>-0.18</sub>	0.94
PG1701+359	33152	5.55	-4.00	5391 <sup>+92</sup> <sub>-172</sub>	0.70 <sup>+0.07</sup> <sub>-0.06</sub>	-0.44 <sup>+0.09</sup> <sub>-0.10</sub>	3.51
HS0252+1025	45138	5.25	-2.65	5445 <sup>+345</sup> <sub>-370</sub>	0.78 <sup>+0.19</sup> <sub>-0.15</sub>	-0.32 <sup>+0.22</sup> <sub>-0.22</sub>	3.75
PG0154+182	36755	5.69	-1.68	5473 <sup>+92</sup> <sub>-193</sub>	0.86 <sup>+0.23</sup> <sub>-0.19</sub>	-0.24 <sup>+0.21</sup> <sub>-0.22</sub>	1.02
HS0127+3146	39543	5.19	-3.46	5871 <sup>+370</sup> <sub>-473</sub>	1.16 <sup>+0.26</sup> <sub>-0.21</sub>	0.14 <sup>+0.21</sup> <sub>-0.22</sub>	1.04

**Notes.** The atmospheric parameters of the hot subdwarfs ( $T_{\text{eff}}$ ,  $\log g$ , and  $\log N(\text{He})/N(\text{H})$ ) are obtained from the fit of the Bok spectra. The  $T_{\text{eff}}$ ,  $R$ , and  $L$  of the companions are derived from the SED fits and parallaxes.

## Appendix B: Stars removed from the Bok sample

We list here the stars removed from the Bok sample, but whose spectra are still available at the CDS and shown in Fig. B.1.

- PG1704+222 is a low-mass ( $\sim 0.55 M_{\odot}$ ) post-AGB giant star (Moehler & Heber 1998). The fit resulted in  $T_{\text{eff}} = 17.5$  kK,  $\log g = 2.8$  and a helium abundance close to solar, in agreement with the estimates of Moehler & Heber (1998). This places the star at the lower limit of the model grid in terms of surface gravity.
- PG1544+488 is a sdB binary composed of two similar He-rich sdB stars. This is, up to now, the only known binary system comprising two hot subdwarf stars (Ahmad et al. 2004; Şener & Jeffery 2014). The two components cannot be disentangled in our Bok spectra.
- KPD0311+4801 (WD0311+480) is a very hot DA white dwarf (see e.g., Filiz et al. 2024).
- FBS0132+370 could not be well reproduced by our model atmospheres. We estimate a relatively large  $T_{\text{eff}}$  of 54 kK, a  $\log g = 6$  and some helium enrichment. The spectrum shows a few relatively strong absorption features that correspond to C IV lines. It is an object similar to those recently identified by Werner et al. (2022) as hot subdwarf stars with atmospheres strongly enhanced in carbon and oxygen, now identified as CO-sdO.

- PG1348+369 shows emission lines in its spectrum. The high Balmer lines (around 3800 Å) and  $H_{\alpha}$  are in emission. A LAMOST spectrum was analyzed by Lei et al. (2023) and the authors classified it as a hot sdO star ( $T_{\text{eff}} = 65$  kK). They did not report anything peculiar about the object. Our SED fit of the object suggests the presence of an infrared excess, at least when fitting the SED with a stellar  $T_{\text{eff}}$  of 70 kK. The star is definitely hot as indicated by the strong He II 5412 Å line. The TESS light curve shows a conspicuous periodic signal at 3.316 days along with the first harmonic. This is consistent with the interpretation of Barlow et al. (2022) that this is a reflection effect system in which the emission lines come from the heated side of the dM companion.

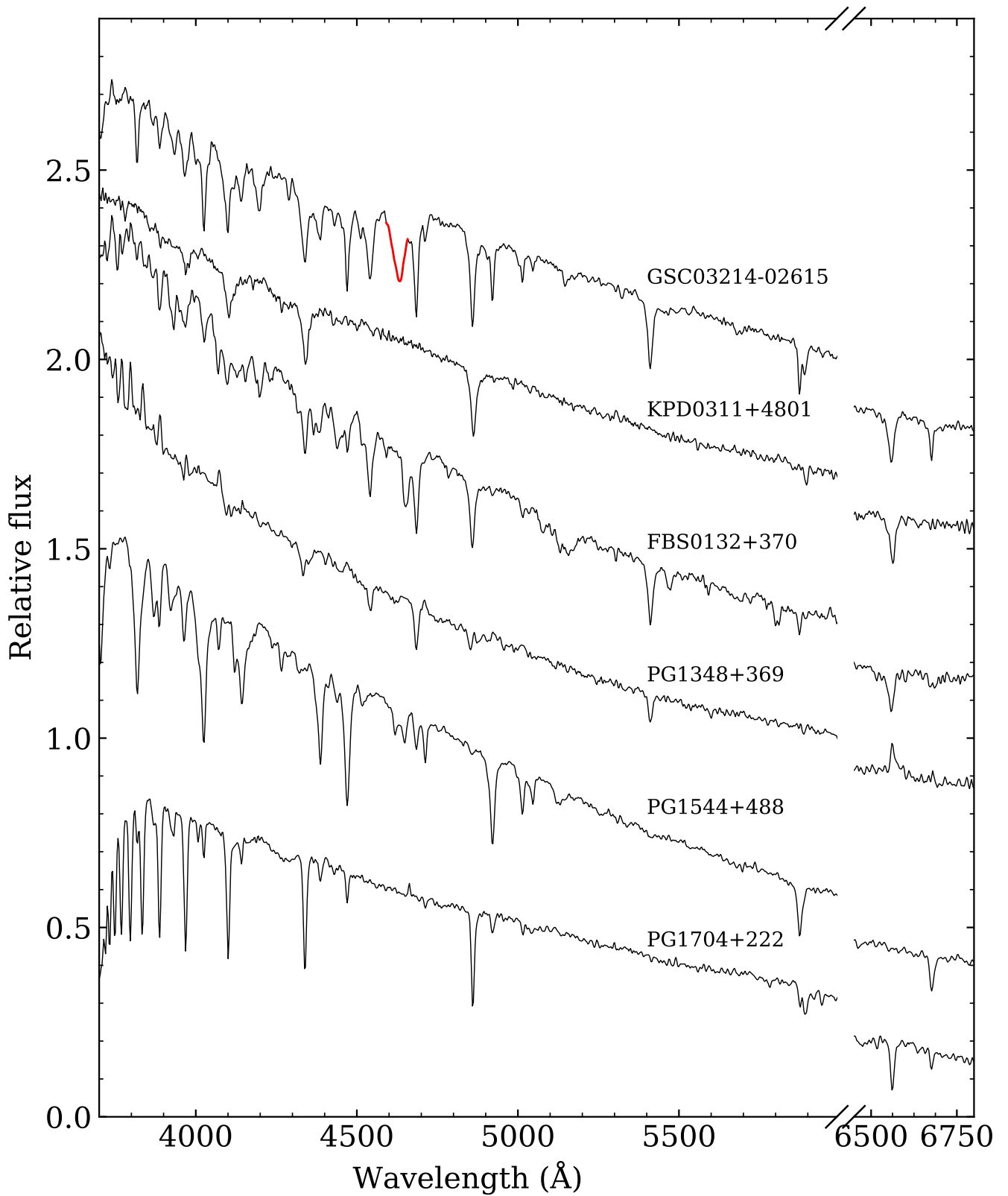


Fig. B.1: Bok spectra of six particular stars. The candidate magnetic star GSC03214-02615 is shown on top, with the distinctive absorption feature around 4600 Å highlighted in red. The five other stars were discarded from the analysis as explained in Sect. 4.1.

### Appendix C: PG0215+183

Among the stars in the MMT sample, PG0215+183 stands out because of its high surface gravity obtained from the MMT spectrum. With a  $\log g$  of 6.2 and a  $T_{\text{eff}}$  of 31 kK, the star lies well below the ZAEHB. Its He abundance is low and only He I 4471 Å is visible in the MMT spectrum. At first sight, the fit is good, although a thorough inspection shows that the cores of  $H_{\beta}$  and  $H_{\gamma}$  are slightly narrower than the model prediction and  $H_{\delta}$  is slightly wider than the model (see Fig. C.1). The atmospheric parameters obtained from the Bok spectrum are significantly different with  $T_{\text{eff}} = 29$  kK and  $\log g = 5.8$ . This is the star with a large  $\log g$  difference of 0.4 dex in Fig. 8. Although the atmospheric parameters from the Bok spectrum places the star close to the ZAEHB, and the resulting mass of  $0.51 M_{\odot}$  derived from the parallax and SED fit is normal, the atmospheric fit is obviously poor, as seen in Fig. C.1. We verified that the difference in atmospheric parameters obtained from the two spectra comes from the wavelength range used: fitting the Bok spectrum over the 4000–4950 Å range leads to the same atmospheric parameters as obtained with the MMT spectrum. Currently we do not know why the spectrum of that star cannot be properly reproduced. There are no RV variations from the eight individual MMT spectra ( $\sigma_{rv} = 2.5 \text{ km s}^{-1}$ ), the star is not pulsating and has no IR excess. The spectral fit of spectra taken with a different instrument resulted in the same mismatch between the observed and modeled Balmer lines (H. Dawson, priv. comm. 2025). The effective temperature of the star is in the range where  $^3\text{He}$  and stratification are observed, but the Balmer lines in the Bok spectra of the stratified stars discussed in Sect. 4.2.2 are properly reproduced (see also Fig. C.1).

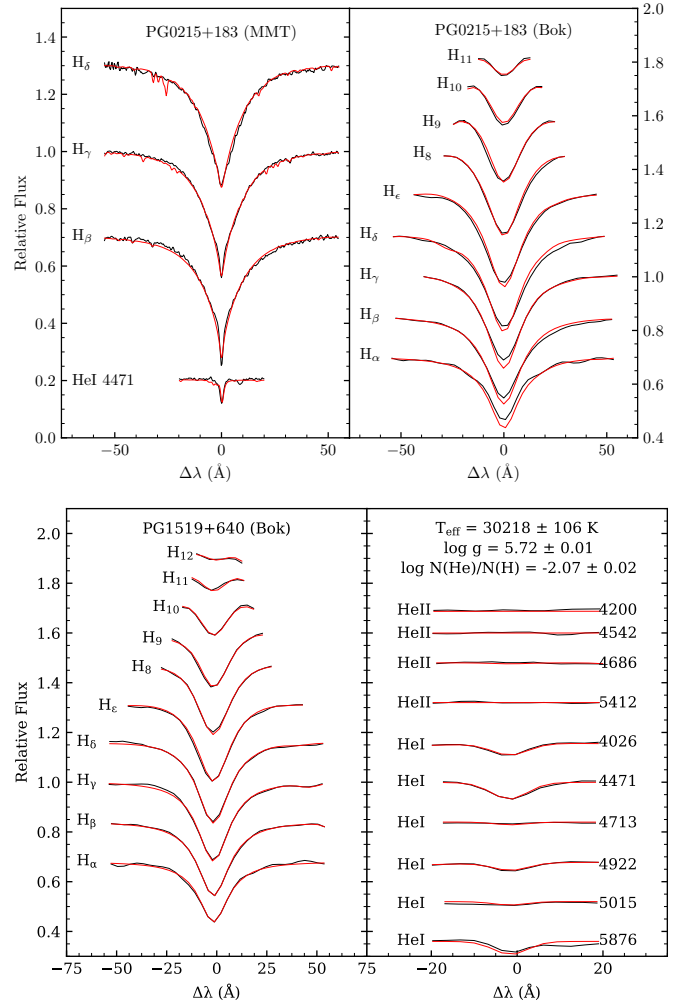


Fig. C.1: Top: respective best fits to the MMT (31.2 kK,  $\log g = 6.18$ ,  $\log N(\text{He})/N(\text{H}) = -2.8$ ) and Bok (28.9 kK,  $\log g = 5.85$ ,  $\log N(\text{He})/N(\text{H}) = -3$ ) spectra of PG0215+183. Bottom: Best fit to the Bok spectrum of PG1519+640, a star with similar atmospheric parameters as PG0215+183 and showing hints of He stratification in its MMT spectrum.