Inverting scientific images with deep generative models

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From a noisy observation y...

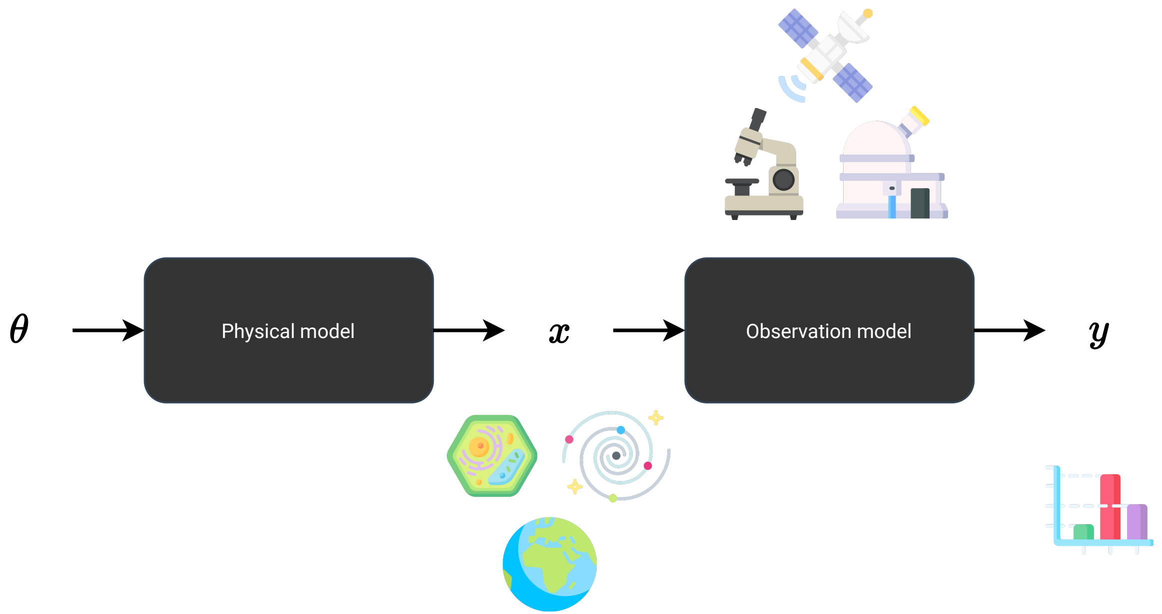

… can we recover
all plausible states x?

$$\dot{u} = -u\nabla u + \frac{1}{Re}\nabla^2 u - \frac{1}{\rho}\nabla p + f$$

$$0 = \nabla \cdot u$$

... or model parameters

$\theta = \{Re, \rho, f\}$**?**



Inverse problems in science

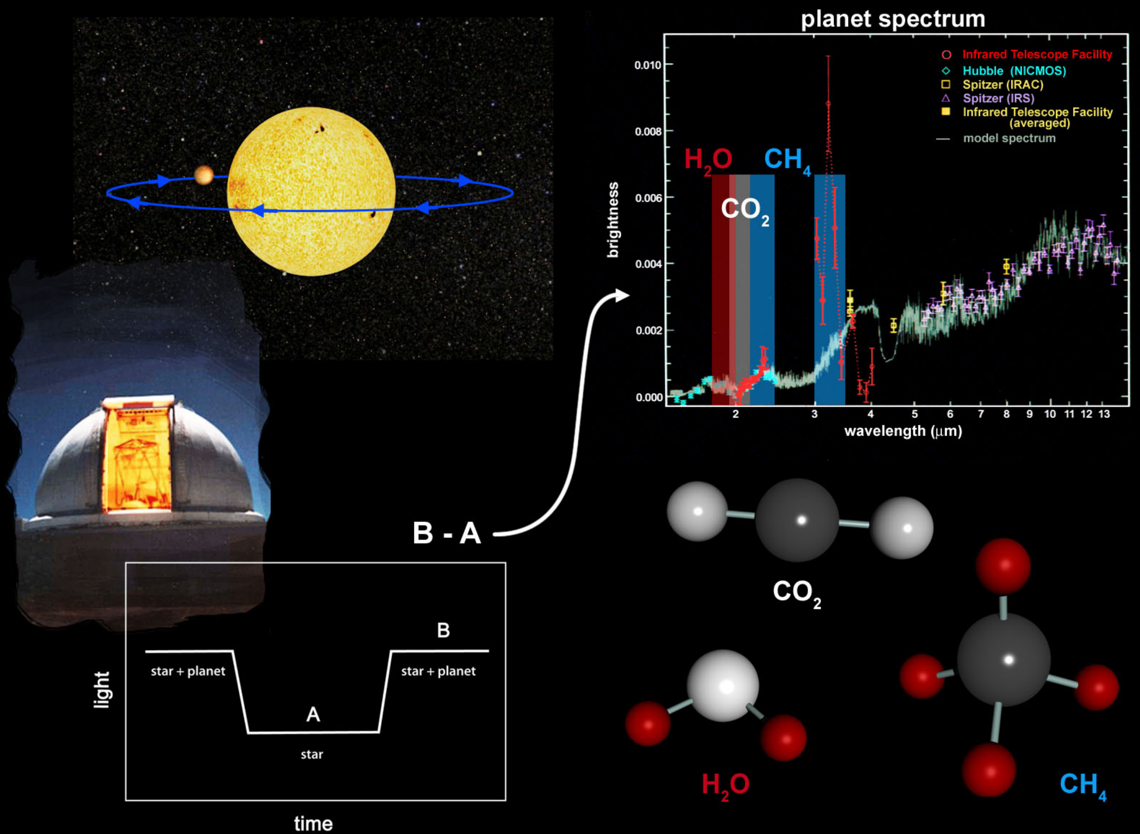
Given noisy observations y, estimate either

- the posterior distribution $p(x|y) \propto p(x)p(y|x)$ of latent states x, or
- the posterior distribution $p(\theta|y)$ of model parameters θ.

Part 1: Low-dimensional inverse problems

$p(\theta|x)$, with $\theta \in \mathbb{R}^d$, $d = O(10)$.

Exoplanet atmosphere characterization



What are the atmospheres of exoplanets made of?

How do they form and evolve? Do they host life?

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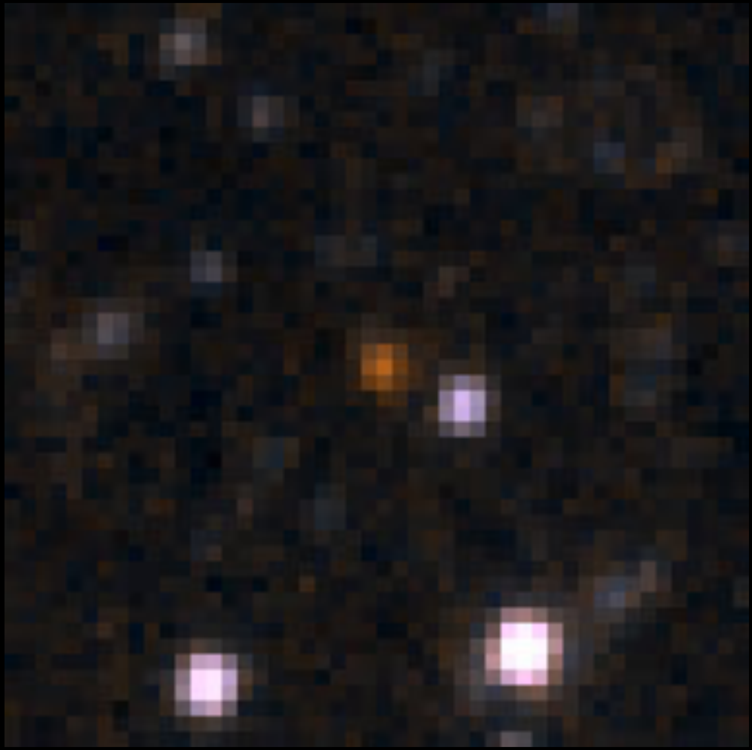
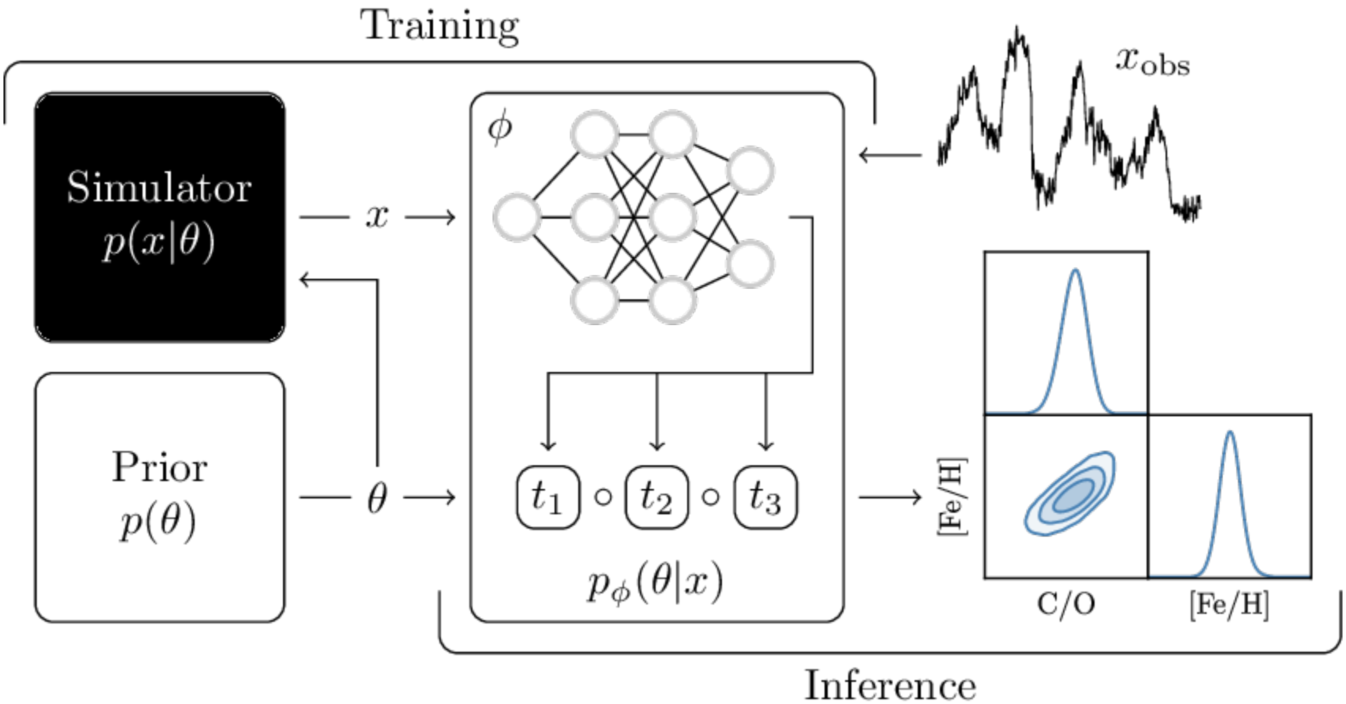
Credits: NSA/JPL-Caltech, 2010.



WISE 1738+2732, a brown dwarf 25 light-years away.



Using **Neural Posterior Estimation** (NPE), we approximate the posterior distribution $p(\theta|x)$ of atmospheric parameters θ with a **normalizing flow** trained on pairs (θ, x) simulated from a physical model of exoplanet atmospheres.

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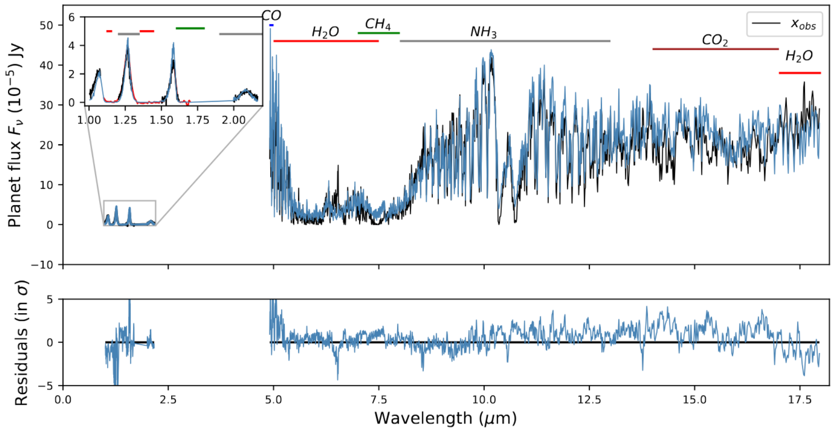
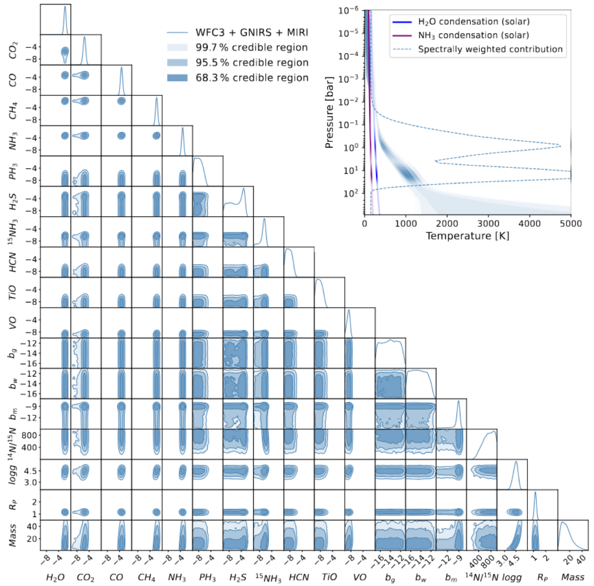
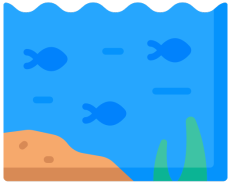
Credits: Vasist et al, 2023 (arXiv:2301.06575).





Panchromatic characterization of WISE 1738+2732 using JWST/MIRI.



Part 2: Large inverse problems

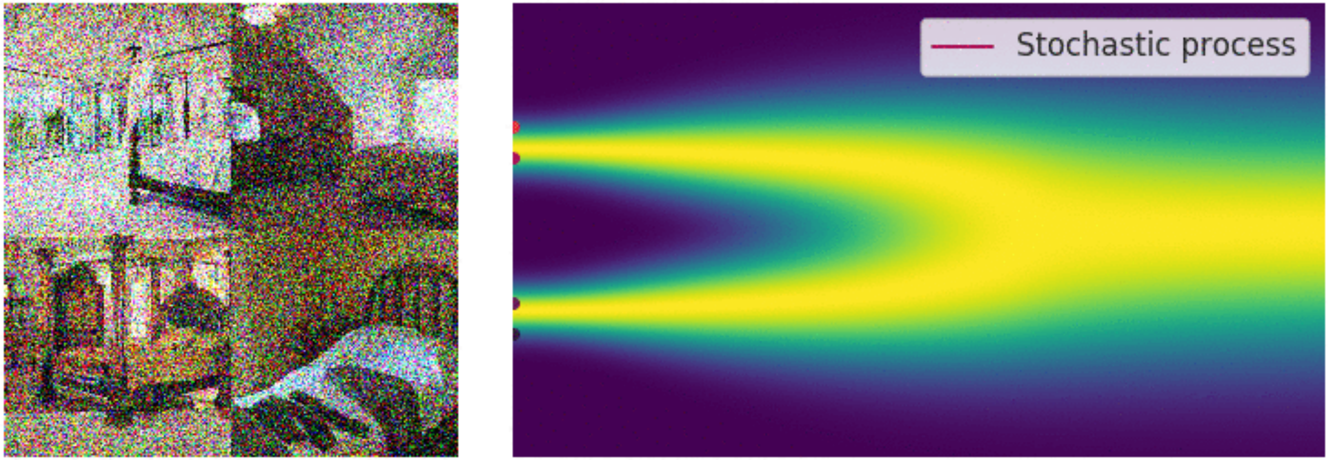
$p(x|y)$, with $x \in \mathbb{R}^d$, $d = O(10^5)$.

Diffusion models 101

Samples $x \sim p(x)$ are progressively perturbed through a diffusion process described by the forward SDE

$$\mathrm{d}x_t = f_t x_t \mathrm{d}t + g_t \mathrm{d}w_t,$$

where x_t is the perturbed sample at time t.



Forward diffusion process.

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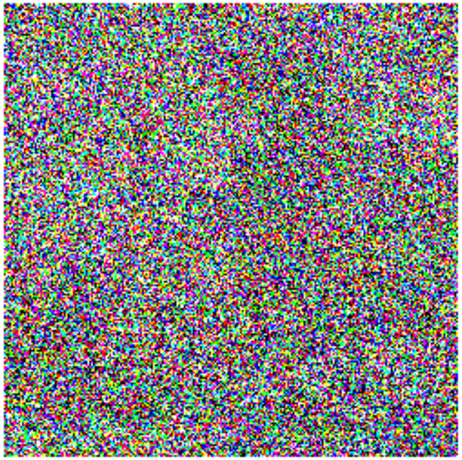
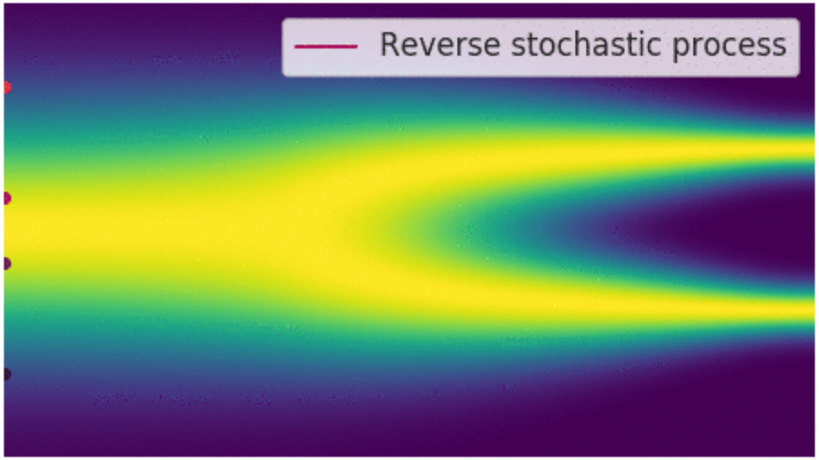
Credits: Song, 2021.

The reverse process satisfies a reverse-time SDE that can be derived analytically from the forward SDE as

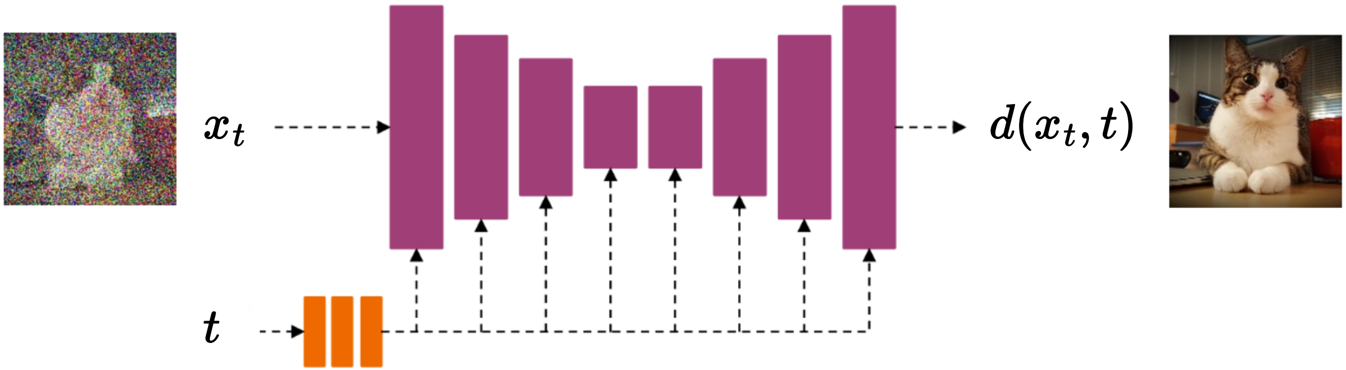
$$\mathrm{d}x_t = \left[f_t x_t - g_t^2 \nabla_{x_t} \log p(x_t)\right] \mathrm{d}t + g_t \mathrm{d}w_t.$$

Therefore, to generate data samples $x_0 \sim p(x_0) \approx p(x)$, we can draw noise samples $x_1 \sim p(x_1) \approx \mathcal{N}(0, \Sigma_1)$ and gradually remove the noise therein by simulating the reverse SDE from $t = 1$ to 0.





Reverse denoising process.



The **score function** $\nabla_{x_t} \log p(x_t)$ is unknown, but can be approximated by a neural network $d_\theta(x_t, t)$ by minimizing the denoising score matching objective

$$\mathbb{E}_{p(x)p(t)p(x_t|x)} \left[||d_\theta(x_t, t) - x||_2^2 \right].$$

The optimal denoiser d_θ is the mean $\mathbb{E}[x|x_t]$ which, via Tweedie's formula, allows to use

$$s_\theta(x_t, t) = \Sigma_t^{-1}(d_\theta(x_t, t) - x_t)$$

as a score estimate of $\nabla_{x_t} \log p(x_t)$ in the reverse SDE.

Inverting single observations

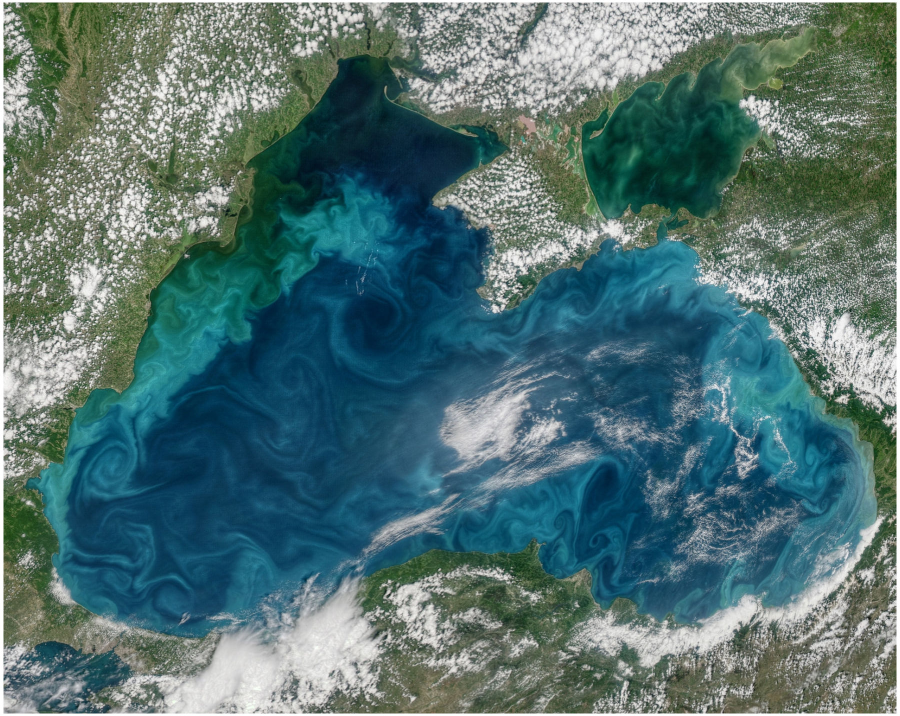
To turn a diffusion model $p_\theta(\mathbf{x})$ into a conditional model $p_\theta(\mathbf{x}|y)$, we can **hard-wire** conditioning information y as an additional input to the denoiser $d_\theta(x_t, t, y)$ and train the model on pairs (x, y).

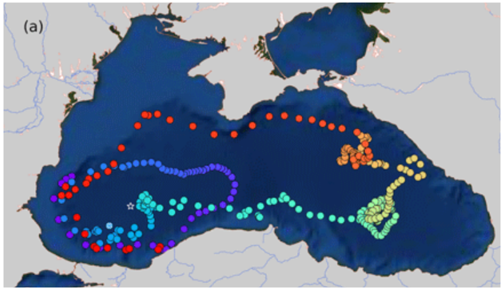
Using the Bayes' rule, the posterior score $\nabla_{x_t} \log p(x_t|y)$ to inject in the reverse SDE can be decomposed as

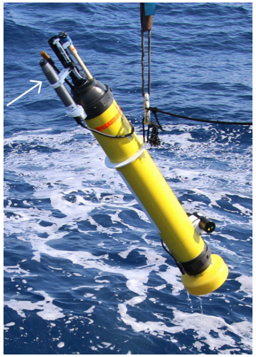
$$\nabla_{x_t} \log p(x_t|y) = \nabla_{x_t} \log p(x_t) + \nabla_{x_t} \log p(y|x_t) - \cancel{\nabla_{x_t} \log p(y)}.$$

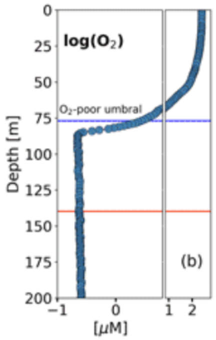
This enables **zero-shot posterior sampling** from a diffusion prior $p(x_0)$ without having to hard-wire the neural denoiser to the observation model $p(y|x)$.


Nowcasting Black Sea hypoxia from satellite observations









How do hypoxic zones evolve in response to climate change? Can we monitor them from space or with sparse measurements?

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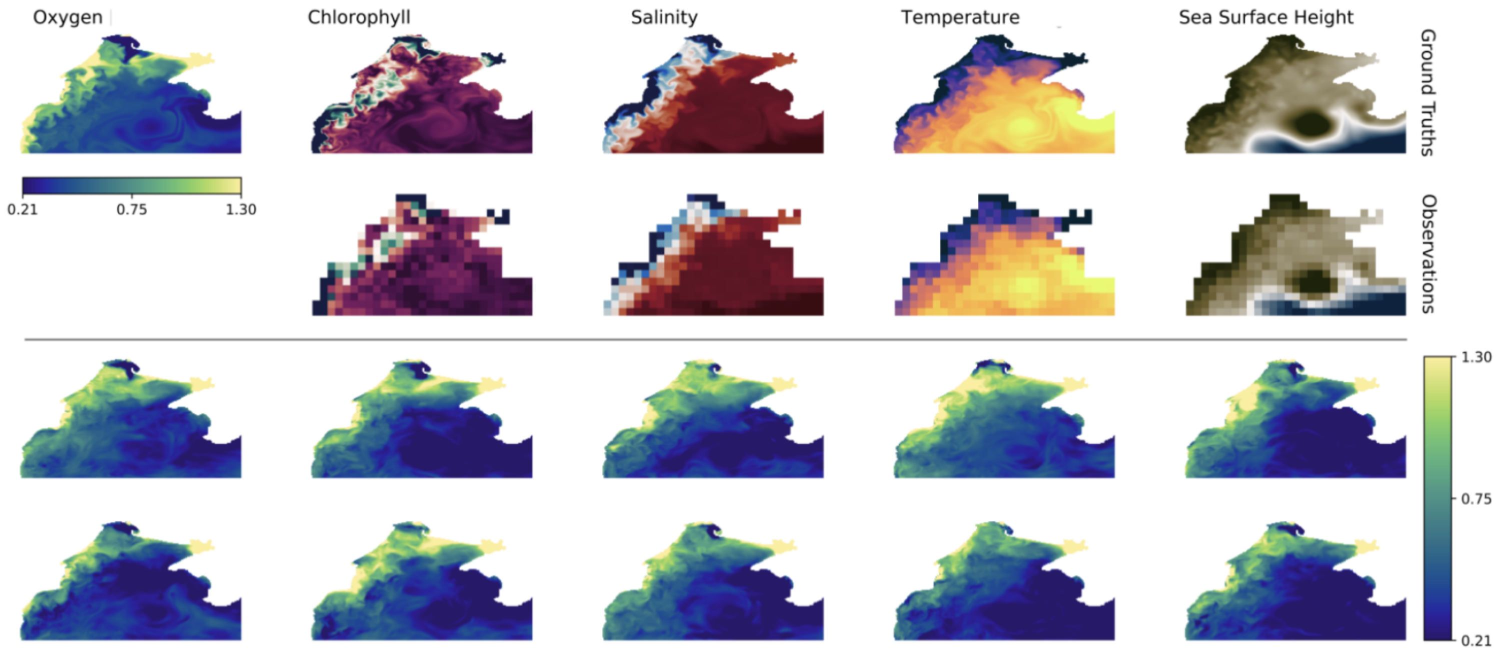
Credits: Work in progress with Victor Mangeleer and Marilaure Grégoire.

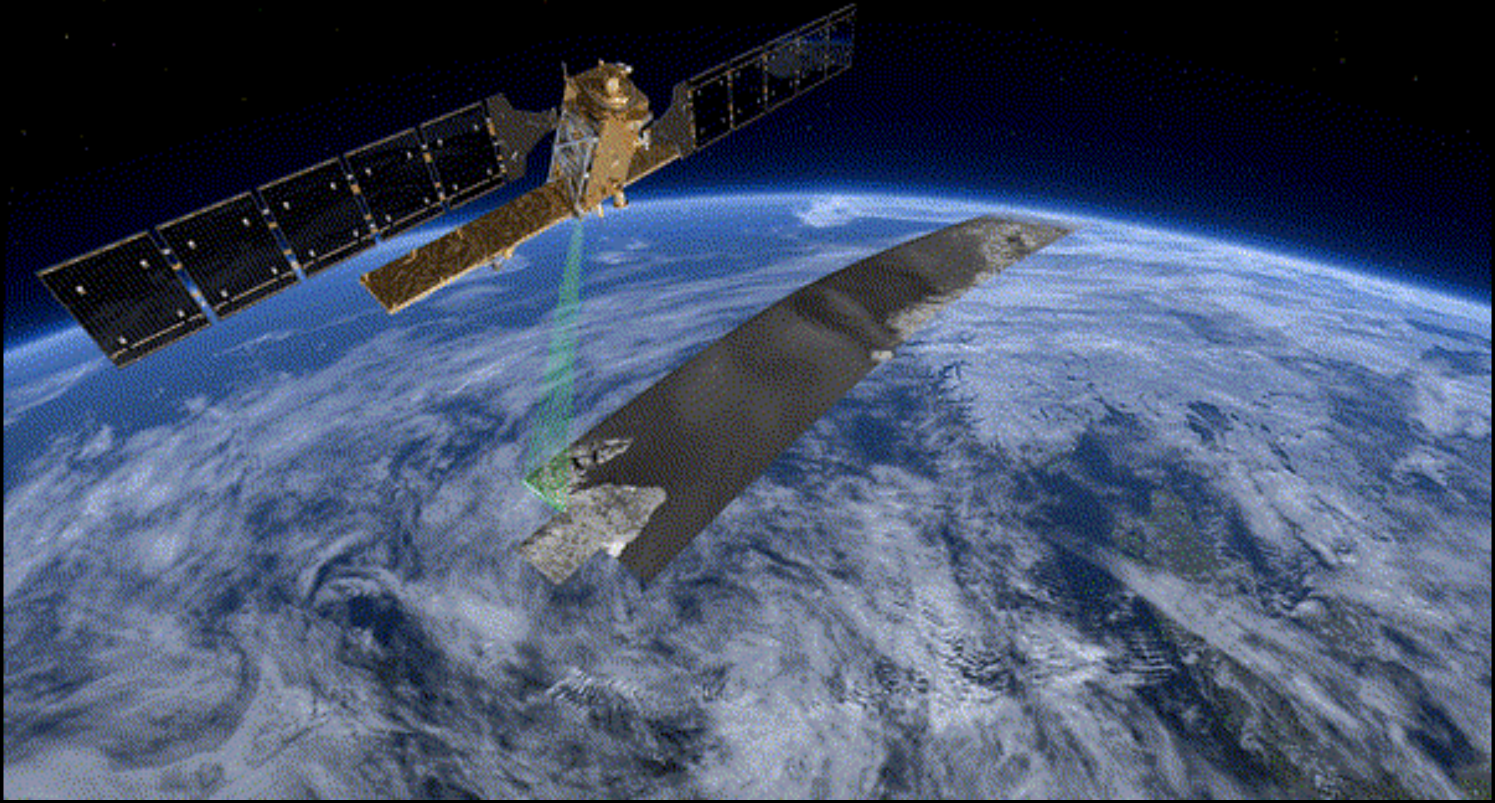


Posterior oxygen maps $p(x|y)$ can be recovered from satellite observations y of the surface, by zero-shot posterior sampling from a diffusion prior $p(x)$ of the Black Sea dynamics.

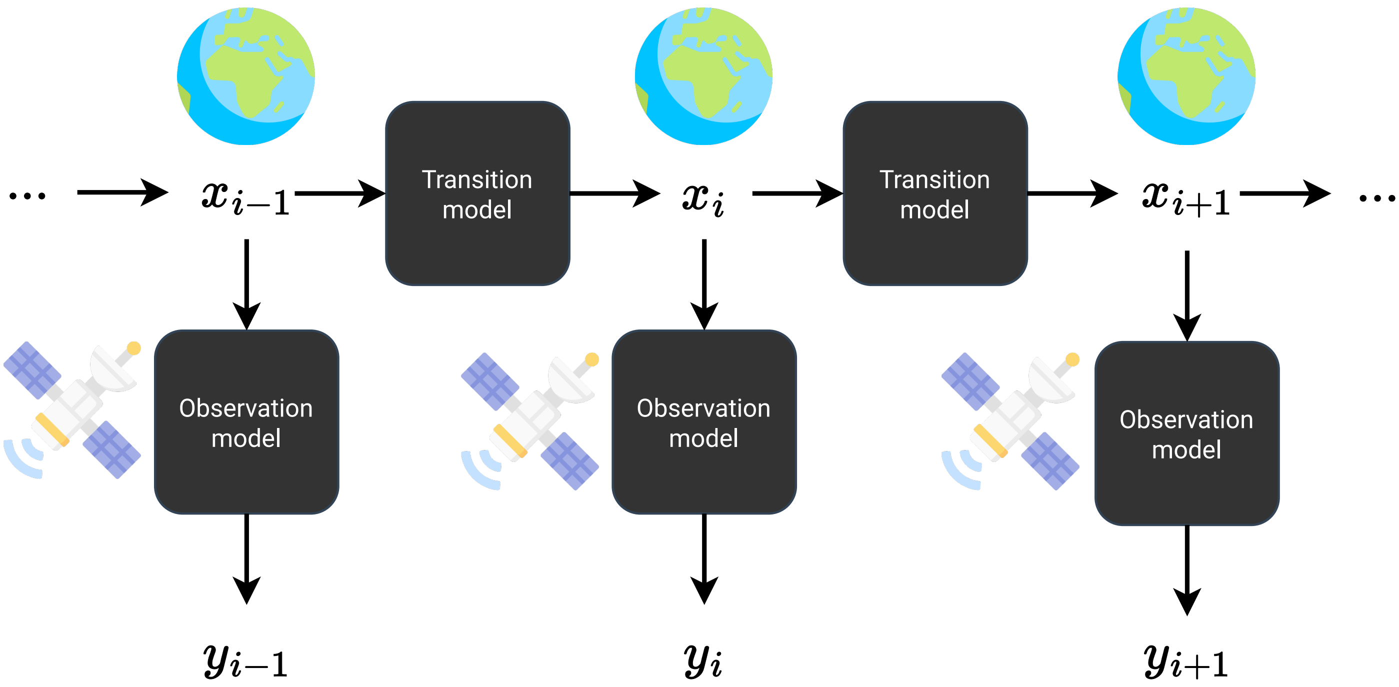
Credits: Work in progress with Victor Mangeleer and Marilaure Grégoire.

Part 3: Extra-large inverse problems

$p(x|y)$, with $x \in \mathbb{R}^d$, $d = O(10^6+)$.

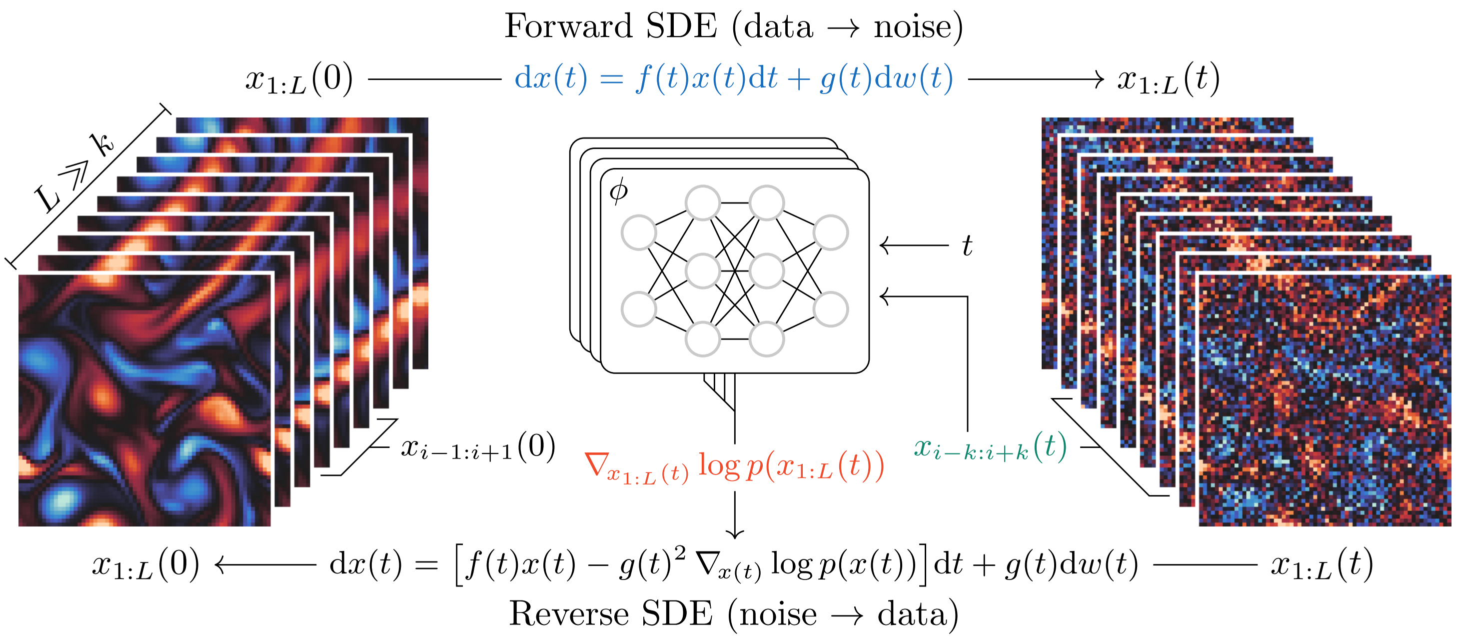


How can we create a comprehensive record of Earth's atmospheric evolution to understand climate change and improve weather prediction?



The goal of **data assimilation** is to estimate plausible trajectories $x_{1:L}$ given one or more noisy observations y (or $y_{1:L}$) as the posterior

$$p(x_{1:L}|y) = \frac{p(y|x_{1:L})}{p(y)} p(x_0) \prod_{i=1}^{L-1} p(x_{i+1}|x_i).$$



Score-based data assimilation

- Build a score-based generative model $p(x_{1:L})$ of arbitrary-length trajectories*.
- Use zero-shot posterior sampling to generate plausible trajectories from noisy observations y.

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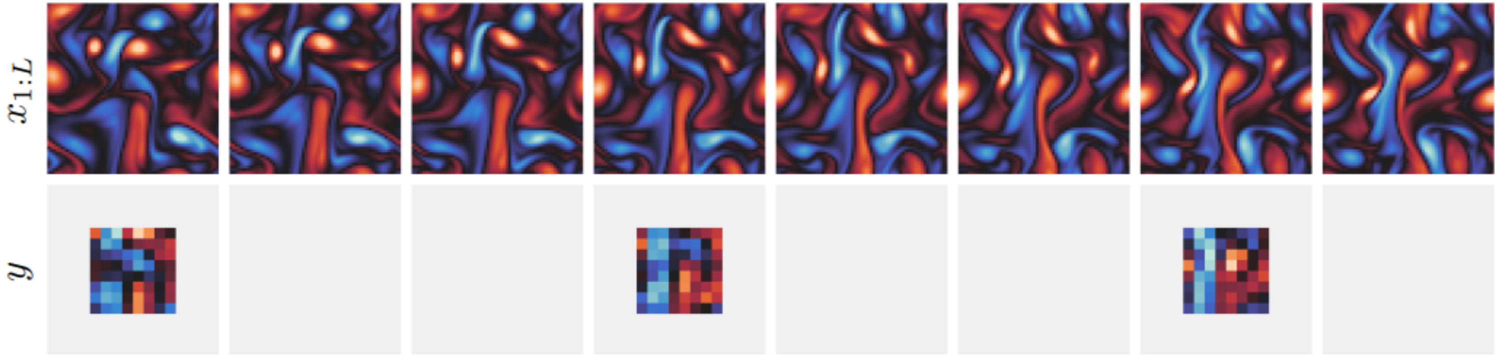
Credits: Rozet and Louppe, 2023 (arXiv:2306.10574).



Sampling trajectories $x_{1:L}$ from
noisy, incomplete and coarse-grained observations y.

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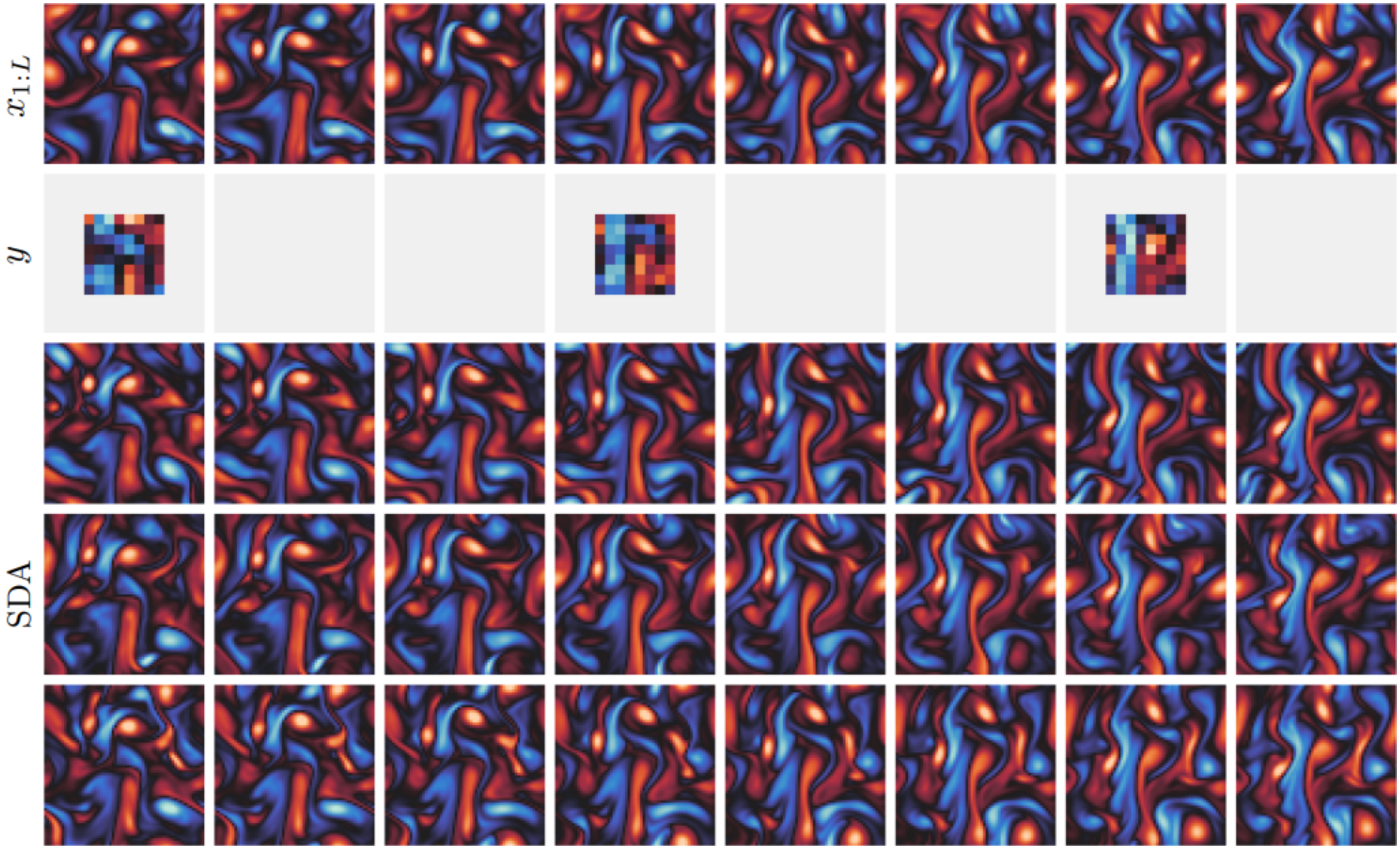
Credits: Rozet and Louppe, 2023 (arXiv:2306.10574).



Sampling trajectories $x_{1:L}$ from
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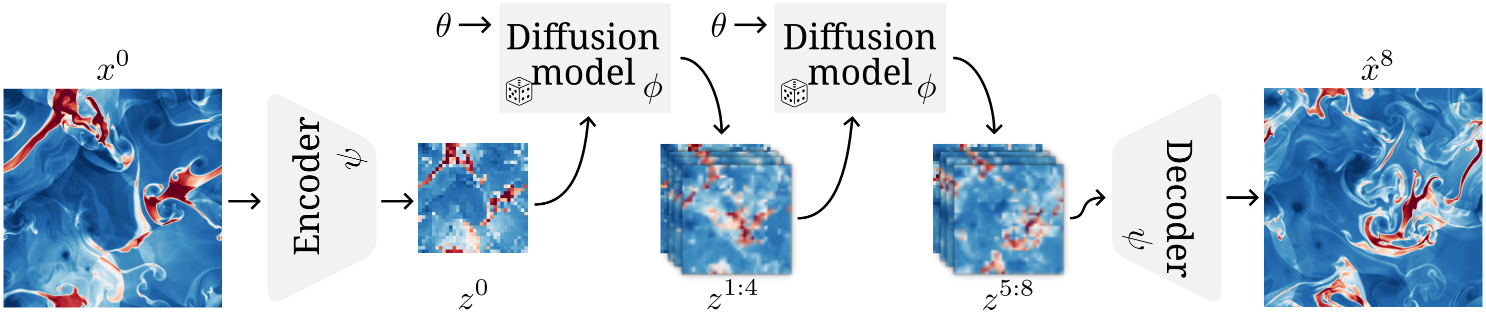
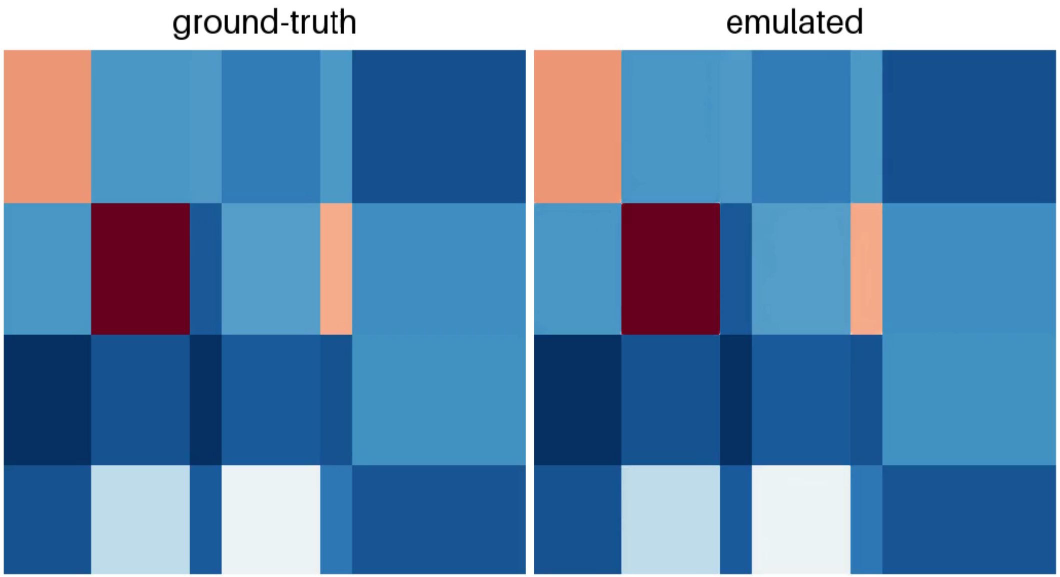
... but does it scale to a whole Earth model?

At 0.25° resolution, for 6 atmospheric variables, 13 pressure levels, hourly time steps, and 14 days of simulation, a trajectory $x_{1:L}$ contains
$\mathbf{721 \times 1440 \times 6 \times 13 \times 24 \times 14 = 27 \times 10^9}$ variables.

$O(10^9)$ variables (or more) is needed to capture the complexity of the atmosphere.

Latent diffusion models for physics emulation





LDMs trained on compressed latent states $z = E(x)$ remain accurate even at high compression rates.

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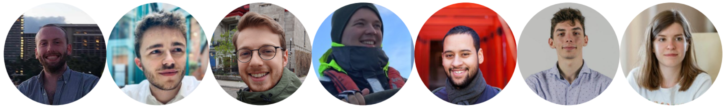
Credits: Rozet et al, 2025 (arXiv:2507.02608).



Appa: Bending weather dynamics with LDMs

Appa is made of three components:

- a 500M-parameter **autoencoder** that compresses the data space x into a latent space z with a 450x compression factor;
- a 1B-parameter **latent diffusion model** that generates latent trajectories $z_{1:L}$;
- a **posterior sampling algorithm** adapted from MMPS (Rozet et al, 2024) that samples from the posterior distribution $p(z_{1:L} | y)$.

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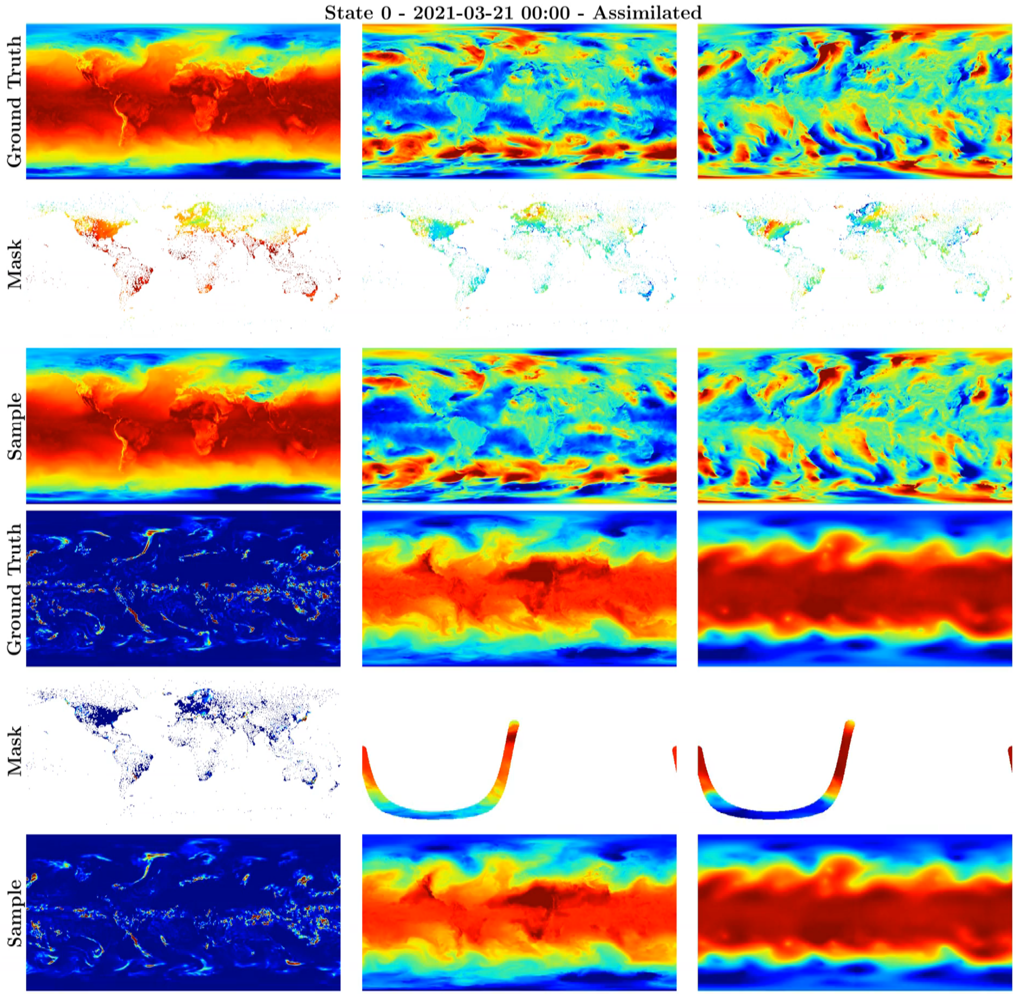
Credits: Andry et al, 2025 (arXiv:2504.18720). New version soon on arXiv!



Reanalysis of past data $p(x_{1:L} | y_{1:L})$.

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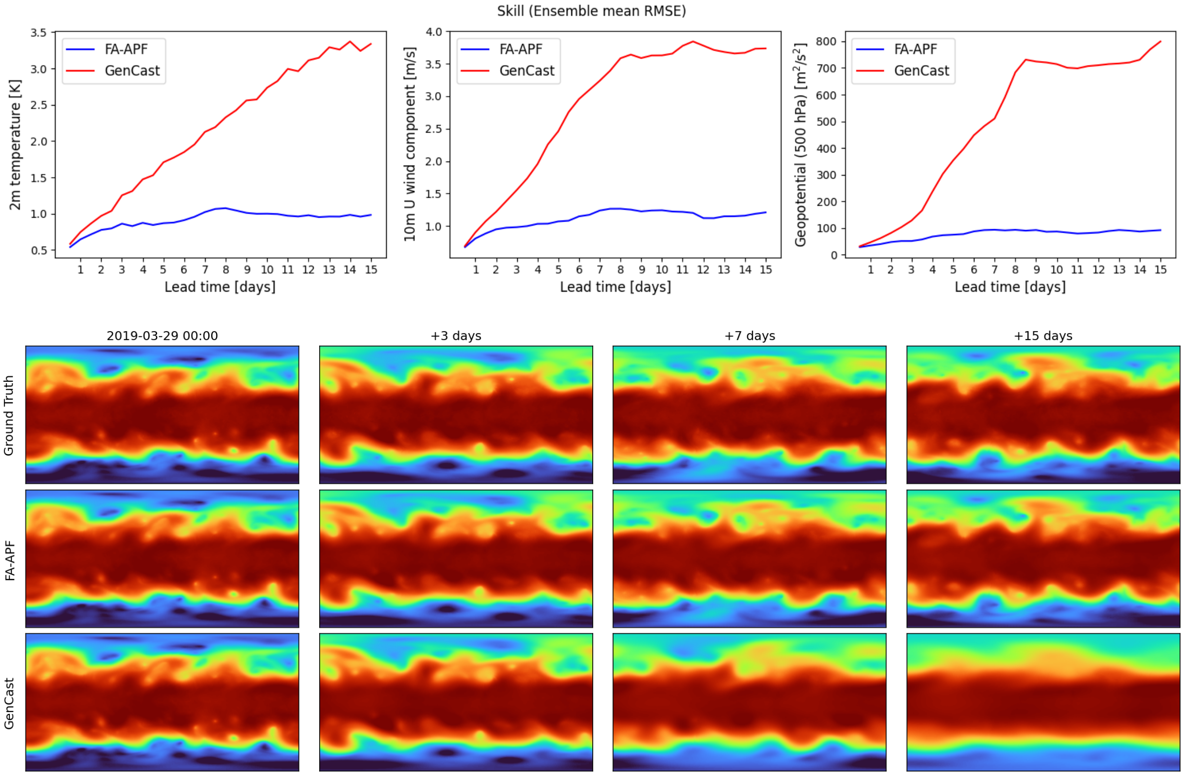
Credits: Andry et al, 2025 (arXiv:2504.18720). New version soon on arXiv!

Bonus: Training-free data assimilation with GenCast

The score decomposition can also be used to turn autoregressive weather models $p(x_{k+1}|x_k)$ into samplers of the optimal proposal distribution $p(x_{k+1}|x_k, y_{k+1})$ **without any change to the model or any training**, enabling online data assimilation with a particle filter.



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Credits: Soon on arXiv!

Conclusions

Deep generative models unlock high-dimensional Bayesian inference in complex physical models: **new scientific questions become accessible**.

Next challenges:

- Rigorous validation: when and why these methods work (or not).
- Resolution (in space and time): can we go higher?
- Misspecification: what if the prior, the physical, or the observation models are wrong?

(Gérome, François, Victor, Omer, Sacha, Matthias, Elise, Malavika, Thomas)

The end.