

# APPLICATION OF THE PFEM TO THE STUDY OF BLOOD FLOWS AND THEIR INTERACTIONS WITH ARTERY WALLS

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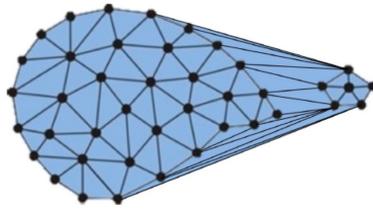
**20<sup>th</sup> International Symposium on Computer Methods in Biomechanics  
and Biomedical Engineering**

# 1 The Particle Finite Element Method (PFEM)

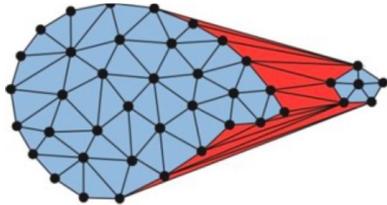
Boundaries identification using the  $\alpha$ -shape technique



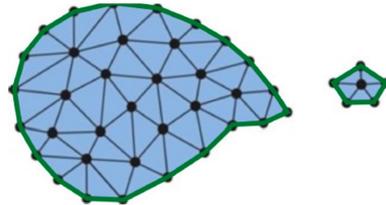
(a) Cloud of particles



(b) Delaunay triangulation

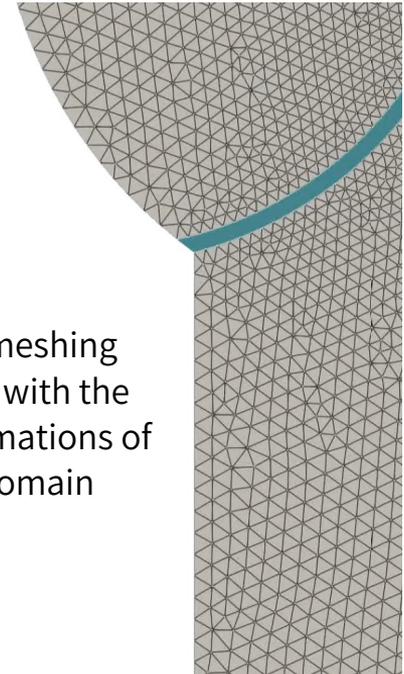


(c) Deletion of spurious triangles  
(in red)



(d) Identification of boundaries  
(in green)

Efficient remeshing  
compatible with the  
large deformations of  
the blood domain



## Solid model (blood vessel)

**Metafor**

Updated Lagrangian / Arbitrary  
Lagrangian Eulerian



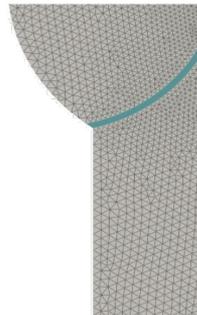
Hyperelastic laws (nonlinear  
elastic, Mooney-Rivlin, ...)

## CFD model (blood)

**PFEM3D**

Particle method

Reconstruction of a mesh  
based on particles

**Dirichlet-Neumann paradigm**

1

Predictor displacement  $\mathbf{u}_S^\Gamma$

2

$$\mathbf{t}_F^\Gamma = \mathcal{F}(\mathbf{u}_S^\Gamma)$$

4

$$\hat{\mathbf{u}}_S^\Gamma = \mathcal{S}(\mathbf{t}_F^\Gamma)$$

**Solid****Fluid**

Surface tractions  $\mathbf{t}_F^\Gamma$

3

S = solid

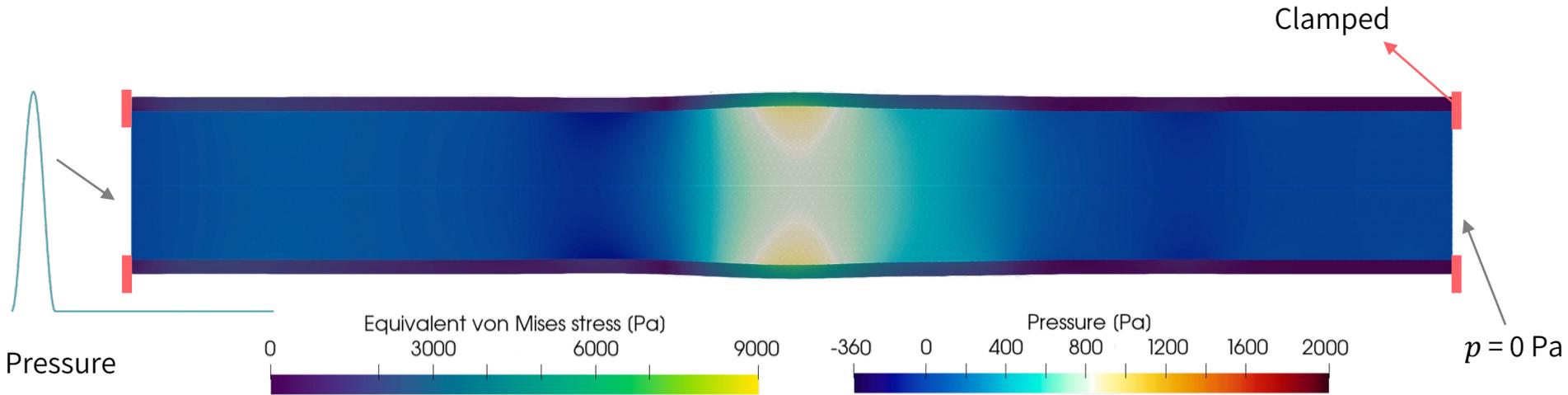
F = fluid

 $\Gamma$  = interface

Solved iteratively until  $\hat{\mathbf{u}}_S^\Gamma \approx \mathbf{u}_S^\Gamma$

## 3

## Propagation of a pressure pulse



Verification against  
Moens-Korteweg theory:

$$c_0 = \sqrt{\frac{Eh}{\rho d}}$$

$E$  = Artery wall Young's modulus

$h$  = Wall thickness

$\rho$  = Blood density

$d$  = Undeformed diameter

- Newtonian:  $\tau = \mu \dot{\gamma}$
- **Casson** model

Shear stress  $\tau$

Asymptotic viscosity  $\mu_\infty$

Viscosity  $\mu$

Yield stress  $\tau_y$

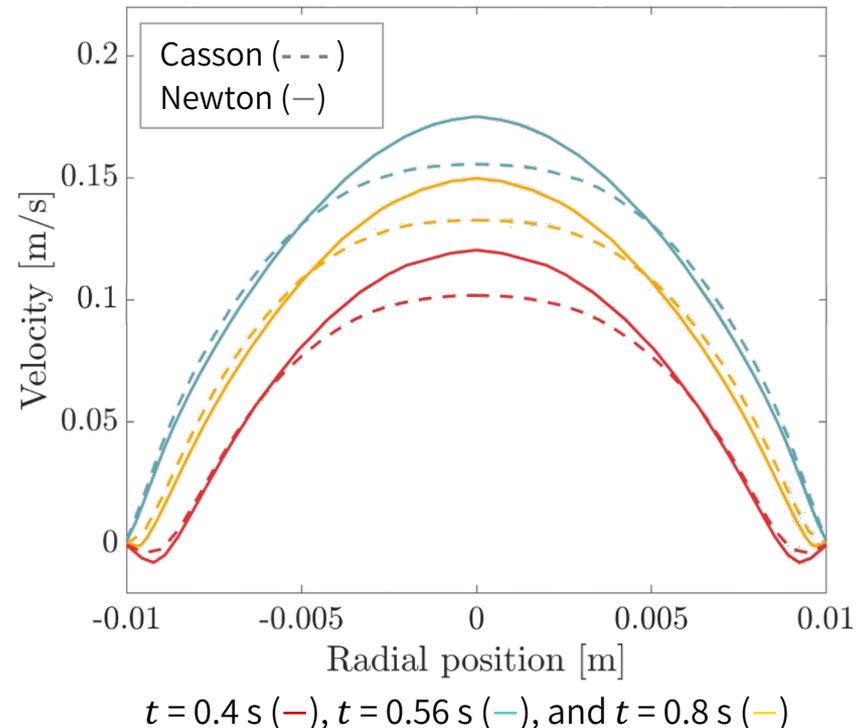
Shear rate  $\dot{\gamma}$

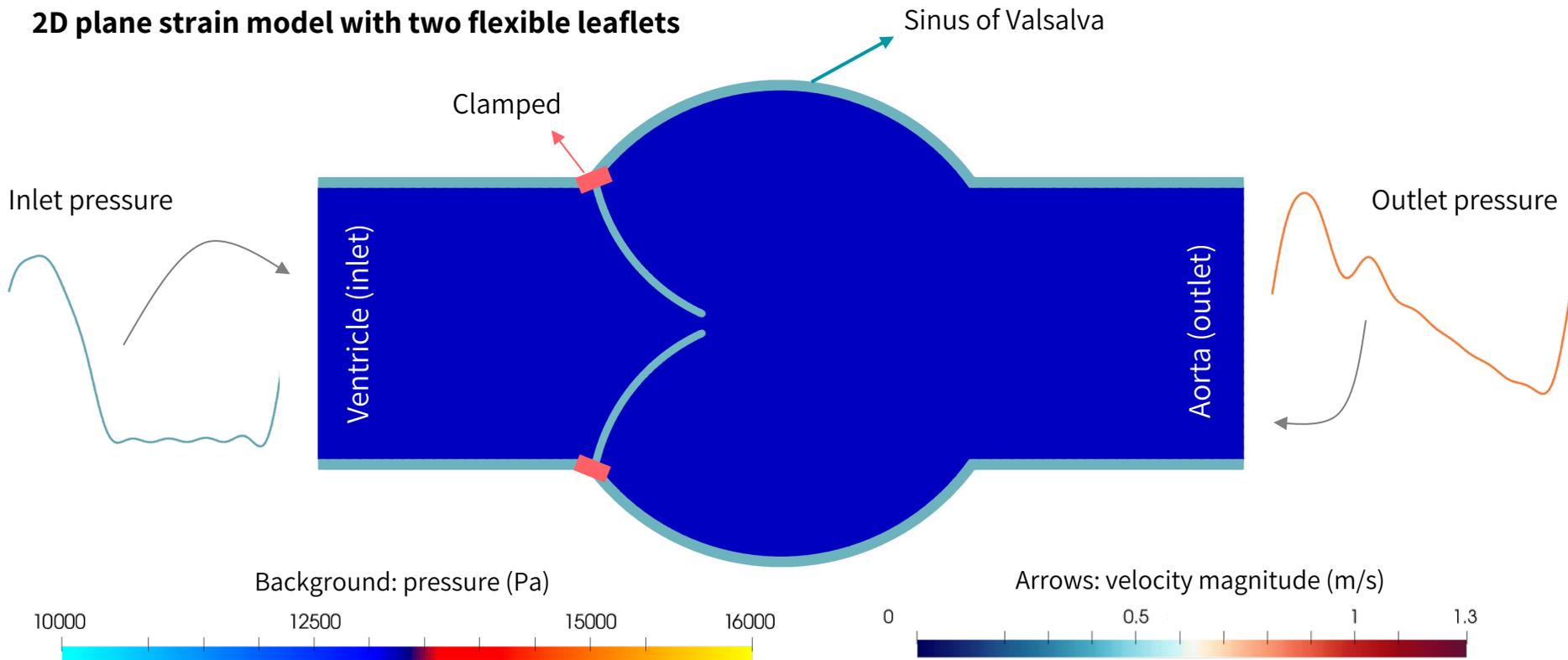
$$\begin{cases} \tau = \mu(\dot{\gamma})\dot{\gamma} & \text{if } |\tau| \geq \tau_y \\ \dot{\gamma} = 0 & \text{if } |\tau| < \tau_y \end{cases}$$

$$\mu(\dot{\gamma}) = \left( \sqrt{\mu_\infty} + \sqrt{\frac{\tau_y}{|\dot{\gamma}|}} \right)^2$$

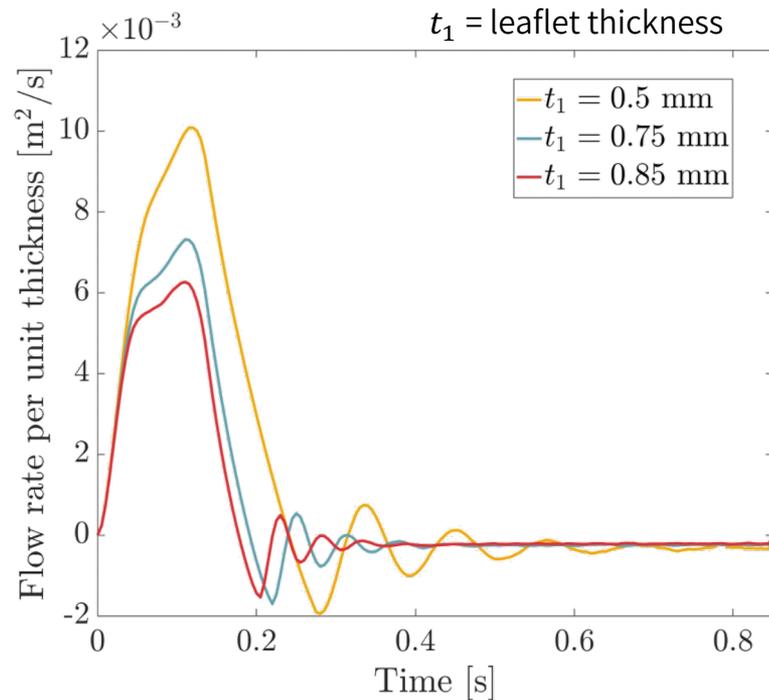
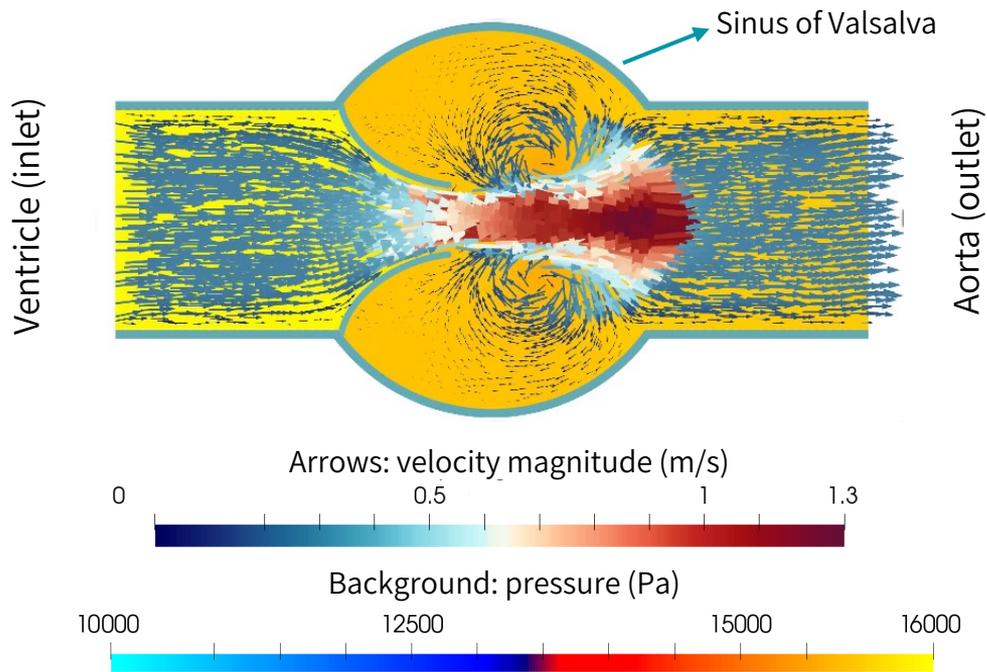
Negligible difference in case of **high shear**  
and/or **highly pulsatile** flow.

Velocity profiles at successive times of the cardiac cycle in **the inferior vena cava**.



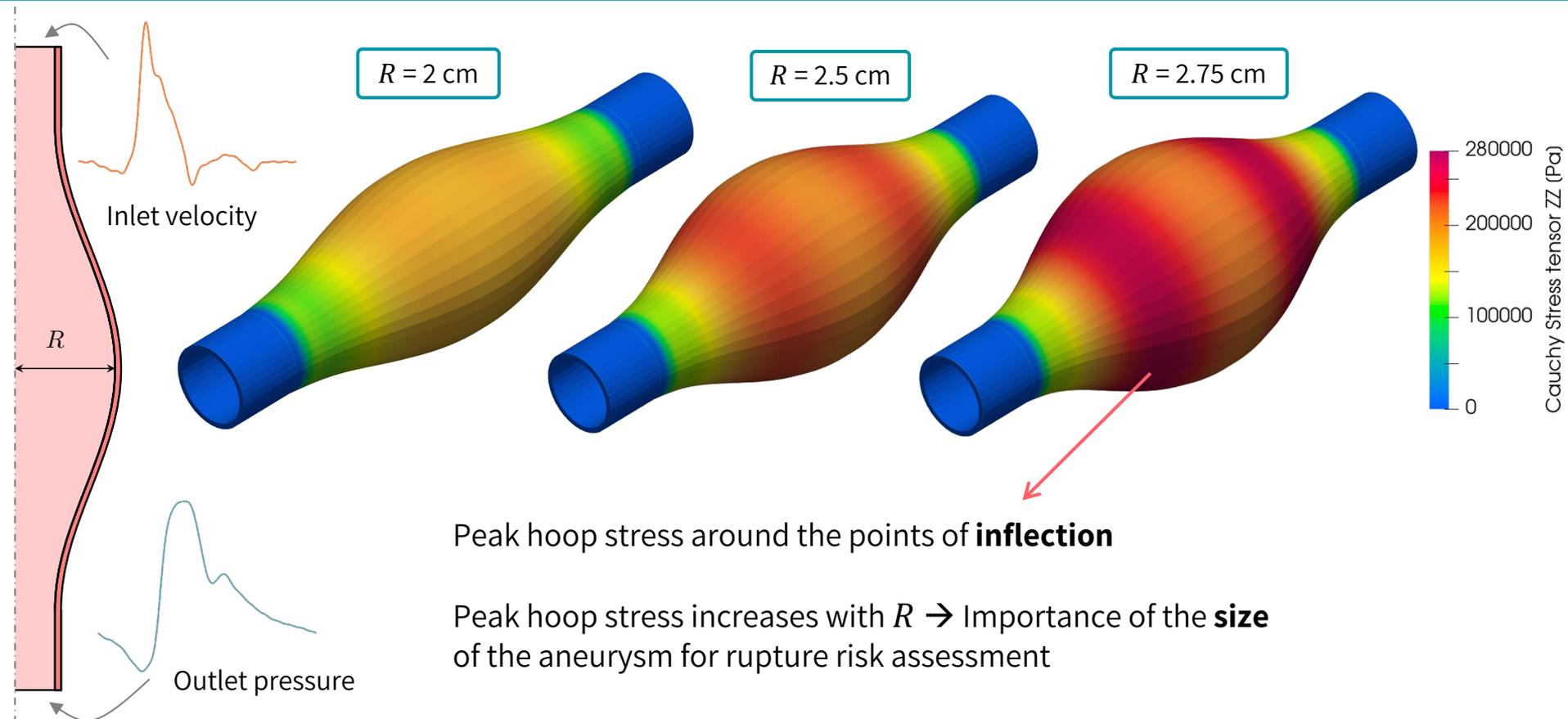
**2D plane strain model with two flexible leaflets**

2D plane strain model with two flexible leaflets

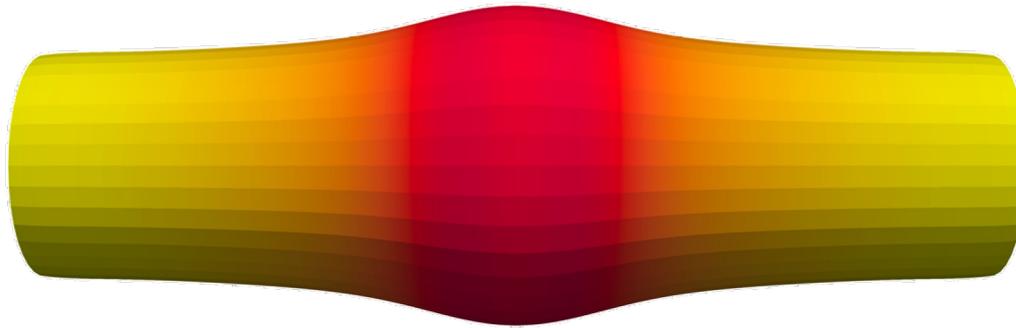


Impact of calcification on the heart ability to pump blood throughout the body

# 6 Axisymmetric abdominal aortic aneurysm



$E = 0.675$  MPa (stiffness of healthy artery)  
Thickness reduced by 50% in the middle of the artery:

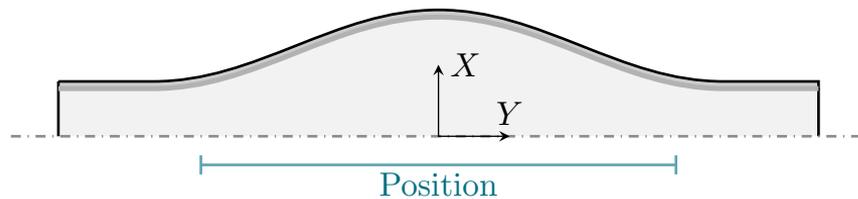
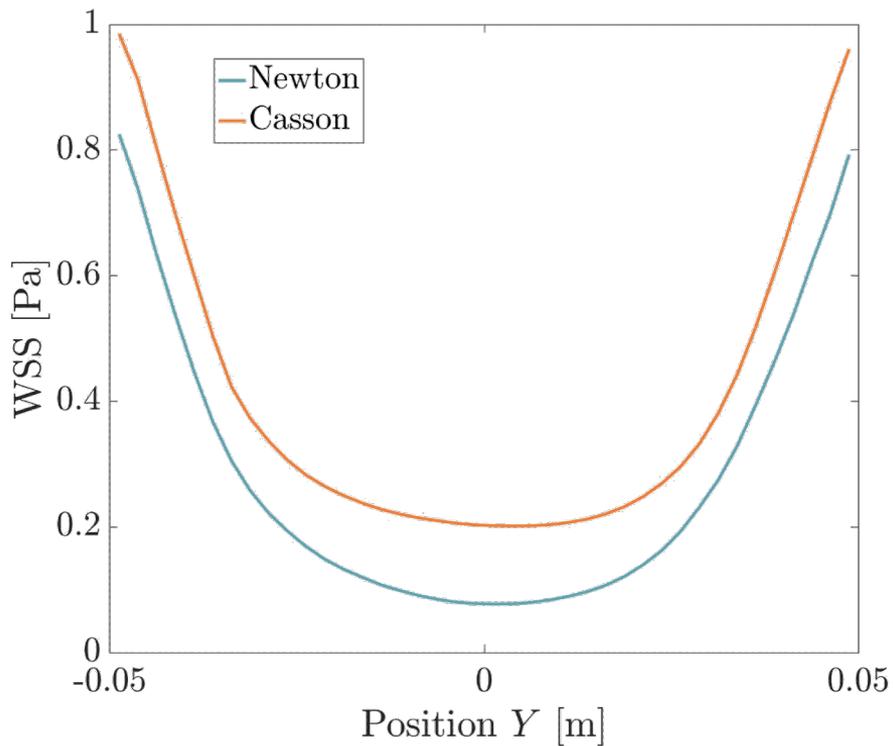


Rupture risk depends on the **stiffness** of the wall and the **size** of the aneurysm.



Initial **weakness** should be compensated by **remodeling** to avoid instability and rupture.

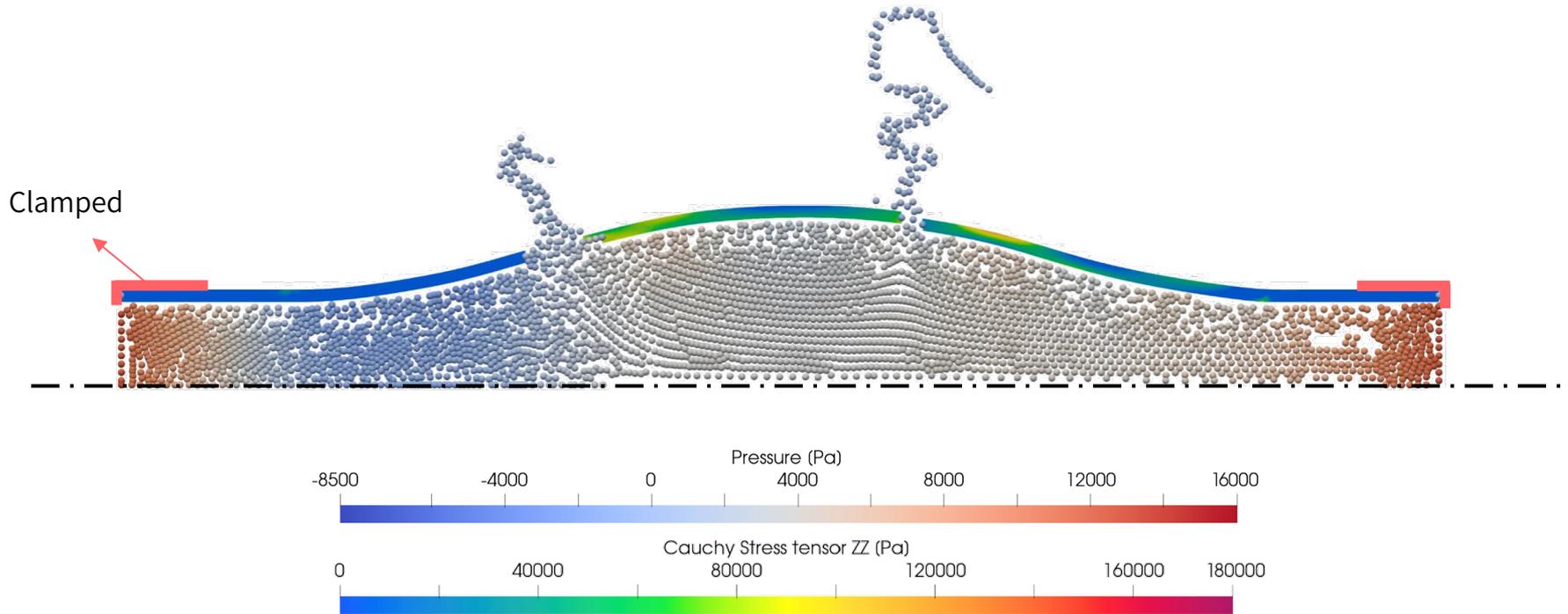
Time-averaged wall shear stress along the aneurysm



Physiological importance  
of the **wall shear stress (WSS)**

- Low WSS is pathological  
(risks of atherosclerosis and aneurysm rupture)
- Importance of fluid model for accurate diagnosis

**Validation** against clinical results: rupture occurs close to an **inflection** point of the aneurysm.



**First application** of the PFEM to the study of blood flows and their interactions with artery walls

Numerical  
improvements?

- Turbulence model
- Boundary conditions to cope with signal propagation

Perspectives?

- More realistic arterial constitutive laws (anisotropy)
- Improved geometries (three-dimensional, patient-specific)

Thank you for your attention!



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