



# Partitioning coefficients between olivine and silicate melts

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## Abstract

Variation of Nernst partition coefficients ( $D$ ) between olivine and silicate melts cannot be neglected when modeling partial melting and fractional crystallization. Published natural and experimental  $^{olivine/liquid}D$  data were examined for covariation with pressure, temperature, olivine forsterite content, and melt  $\text{SiO}_2$ ,  $\text{H}_2\text{O}$ ,  $\text{MgO}$  and  $\text{MgO}/\text{MgO}+\text{FeO}^{\text{total}}$ . Values of  $^{olivine/liquid}D$  generally increase with decreasing temperature and melt  $\text{MgO}$  content, and with increasing melt  $\text{SiO}_2$  content, but generally show poor correlations with other variables. Multi-element  $^{olivine/liquid}D$  profiles calculated from regressions of  $D$  REE–Sc–Y vs. melt  $\text{MgO}$  content are compared to results of the Lattice Strain Model to link melt  $\text{MgO}$  and:  $D_0$  (the strain compensated partition coefficient),  $E_M^{3+}$  (Young's Modulus), and  $r_0$  (the size of the M site).  $\ln D_0$  varies linearly with  $\ln \text{MgO}$  in the melt;  $E_M^{3+}$  varies linearly with melt  $\text{MgO}$ , with a dog-leg at ca. 1.5%  $\text{MgO}$ ; and  $r_0$  remains constant at 0.807 Å. These equations are then used to calculate  $^{olivine/liquid}D$  for these elements using the Lattice Strain Model. These empirical parameterizations of  $^{olivine/liquid}D$  variations yield results comparable to experimental or natural partitioning data, and can easily be integrated into existing trace element modeling algorithms. The  $^{olivine/liquid}D$  data suggest that basaltic melts in equilibrium with pure olivine may acquire small negative Ta–Hf–Zr–Ti anomalies, but that negative Nb anomalies are unlikely to develop. Misfits between results of the Lattice Strain Model and most light rare earth and large ion lithophile partitioning data suggest that kinetic effects may limit the lower value of  $D$  for extremely incompatible elements in natural situations characterized by high cooling/crystallization rates. © 2005 Elsevier B.V. All rights reserved.

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## 1. Introduction

### 1.1. Olivine and $D$

The Nernst partition coefficient ' $D$ ' is the ratio of the concentration of a trace element in a solid phase

divided by its concentration in the equilibrium liquid, and is used extensively to model magmatic processes (e.g. Shaw, 1970, 2000; O'Hara, 1977, 1995; Hofmann, 1988; Langmuir, 1989; Bodinier et al., 1990; Bédard, 1994, 1999, 2001; Spera and Bohrsen, 2002; Niu et al., 2002; Weyer et al., 2003; MacLennan et al., 2003). Uncertainties with regard to values of  $D$  are a major source of uncertainty in modeling crystal/liquid fractionation or melting, and in applying inversion

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models to cumulates and mantle melting residues (Bédard, 1994, 2001). Olivine: is the most common upper mantle phase on Earth (e.g. Nixon, 1987) and other terrestrial planets and planetesimals (e.g. Barrat et al., 2002; Hsu, 2003; Karner et al., 2003); is an important cumulus phase in many intrusions, ophiolites and the lower oceanic crust (Cawthorn, 1996; Dilek and Robinson, 2003); crystallizes from a wide diversity of melts, including komatiite, basalt, ferrobasalt, and high-temperature granites and syenites (e.g. Barker et al., 1975; Arndt, 1977; Bédard et al., 1987; Grove and Juster, 1989; Blatter and Carmichael, 2001); and may play a role in generating the depletions in high field strength cations (HFSC: Ti, Zr, Ta, Nb) thought characteristic of arc environments (e.g. Kelemen et al., 1990). However, despite olivine's petrogenetic importance, relatively few data on  $D^{\text{olivine/liquid}}$  are available, and these data show wide ranges in value. It is now widely accepted that  $D^{\text{mineral/liquid}}$  are variable (e.g. Mysen and Virgo, 1980; Blundy and Wood, 1994b; Gaetani and Grove, 1995; Hill et al., 2000), but there have been few attempts to constrain how  $D^{\text{olivine/liquid}}$  varies. The purpose of this paper is to provide an objective parameterization of the dominant trend of variation of  $D$  values that can be used to model igneous processes in common magmatic suites.

### 1.2. Data sources

All experimental and natural mineral/melt partitioning studies for which essential data were published or could be recovered from the authors were compiled, and are available as Supplementary data in the Appendix. Table 1 gives data sources and the corresponding letter/number acronyms that appear in some figures. Partitioning data originating from analysis of phenocrysts in lavas or intrusions are referred to as 'natural' data, and have a number code, while experimental partitioning data are given a letter code. Mineral/mineral partitioning studies were not considered because of subsolidus reequilibration effects (e.g. McDonough et al., 1992; Loucks, 1996). Information on partitioning of Ti, Cr, Na, Al and K was also gleaned from phase equilibrium studies. By considering these data together, it may be possible to unravel the causes of  $D^{\text{olivine/liquid}}$  variations, and to express them quantitatively. For simplicity, sub/superscripts will be left out henceforth,

Table 1

#### Data sources

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#### Experimental data

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a=Elkins-Tanton and Grove, 2003
b=Brenan et al., 2003
c=Canil, 1997
d=Walter, 1998
e=Beattie, 1993
f=Toplis and Carroll, 1996
g=Baker and Eggler, 1987
h=Longhi, 1995
i=Kinzler and Grove, 1992
j=McDade et al., 2003
k=Elkins-Tanton et al., 2000, 2003 and personal communication 2003
m,M=McKay, 1986, Mare and LKFM
n=Moore and Carmichael, 1998
o=Colson et al., 1988
p=Parman and Grove, 2004
q=Baker and Stolper, 1994
r=Blatter and Carmichael, 2001
s=Kohn and Schofield, 1994
t=Richter and Carmichael, 1996
u=Purton et al., 2000
v=Scailliet and MacDonald, 2001
w=Wasylenki et al., 2003
x=Berndt, 2002
y=Mysen, 1978
z=Schwab and Johnson, 2001
A=Hanson and Jones, 1998
B=Shimizu et al., 1982
C=Pickering-Witter and Johnston, 2000
Ca=Capobianco et al., 1991
D=Dunn, 1987
Du=Duke, 1976
E=Canil and Fedortchouk, 2001
F=Grove and Juster, 1989
G=Nielsen et al., 1992
H=Longhi et al., 1999
I=Richter et al., 2004
J=Beattie, 1994
K=Kennedy et al., 1993
L=Kelemen et al., 1990
La=Laporte et al., 2004
N=Gaetani and Grove, 1998
Ne=Nekvasil et al., 2004
O=Hesse and Grove, 2003
P=Parman et al., 1997
Q=Longhi, 2002
R=Kinzler, 1997
S=Grove et al., 1982
Sc=Schmidt et al., 2004
T=Toplis et al., 1994
U=Adam and Green, personal communication, 2003
V=Grove et al., 2003

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Table 1 (continued)

Experimental data
W=Sweeney et al., 1995
Y=Yang et al., 1996
Z=Herzberg and Zhang, 1996
Natural data
1=Dostal et al., 1983
2=Schnetzler and Philpotts, 1970
3=Brunet and Chazot, 2001
4=Mahood and Stimac, 1990
5=Mahood and Hildreth, 1983
6=Dunn and Sen, 1994
7=Francalanci, 1989
8=Dostal and Capedri, 1975
9=LeMarchand et al., 1987
10=Larsen, 1979
11=Villemant et al., 1980
12=Luhr and Carmichael, 1980
13=Fujimaki et al., 1984
14=Wörner et al., 1983
15=Shimizu et al., 1982
16=Burton et al., 2002
17=Puchtel et al., 2004

The letter and number codes are used in figures.

with the understanding that ‘*D*’ will always refer to olivine/liquid  $D$ ; e.g.  $D_{\text{Sc}} = D$ .

### 1.3. Choice of input parameter

What should be the input variable for the parameterization? The ability to reproduce the data is the main criterion, but ease of application must also be considered. It has been proposed that the composition of the melt is the main control on  $D$  variations, and attempts have been made to parameterize  $D$  variations against complex functions of melt chemistry, typically involving ratios of network-forming and network-modifying cations and anions (e.g. Nielsen and Drake, 1979; Mysen, 1983; Nielsen, 1985; Hanson and Jones, 1998; Colson et al., 2000). Two inherent problems with this approach are that some cations ( $\text{Al}^{3+}$ ,  $\text{Fe}^{3+}$ ,  $\text{Ti}^{4+}$ ,  $\text{P}^{5+}$ ) can fulfill different structural roles, and that the influence of volatile species is poorly constrained. Furthermore, to be accurate, these complex functions require that the melt composition be known exactly. While this applies to well-constrained experimental situations where equilibrium glasses can be analyzed; unaltered glass is rarely present in most pre-Mesozoic lavas, and so melt composition must equated with the

whole-rock analysis, or be calculated. In addition, some elements ( $\text{CaO}$ ,  $\text{Na}_2\text{O}$ ,  $\text{K}_2\text{O}$ ,  $\text{SiO}_2$ ) are easily remobilized by hydrothermal alteration and metamorphism; and, when looking at cumulate or mantle rocks, it is rarely possible to know exactly the original temperature, pressure and melt composition at and from which the crystals formed. Consequently, simpler indices of melt compositional evolution are considered here, the values of which can be: (a) constrained empirically from lava or glass analyses; (b) calculated from the mineral analysis itself (e.g.  $\text{MgO}$  or  $\text{MgO}\# = \text{MgO}/(\text{MgO} + \text{FeO total})$ ) through the application of exchange and distribution coefficients (e.g. Roeder and Emslie, 1970; Sugawara, 2000; MacLennan et al., 2003); or in the case of  $\text{SiO}_2$ , (c) calculated with a thermodynamic approach (e.g. Carmichael et al., 1970). Other investigators have favoured a mineral-compositional control on  $D$  variations, since distortions of the crystal structure resulting from solid-solutions are known to affect the size of the site(s) into which trace elements enter (e.g. Blundy and Wood, 1991, 2003; Gaetani and Grove, 1995). The mineral-compositional parameter considered in this paper is the molar forsterite content ( $\text{Fo} = 100 \times \text{Mg}/(\text{Mg} + \text{Fe}^{\text{total}})$ ) which is interlinked with liquid  $\text{FeO}/\text{MgO}$  (Roeder and Emslie, 1970).

### 1.4. Sources of error and uncertainty

This is a compilation of data from both experimental and natural partitioning studies, which were analyzed over a span of 25 years with different methods in different laboratories; so that one has to consider the probability of inter-laboratory biases, the progressive improvements in precision and accuracy that have occurred, the possibility that kinetic or pneumatolytic effects may have perturbed some experiments or observations, and finally, the probability of occasional experimental or typographical errors. Partitioning data obtained from phenocryst/matrix pairs are not as well constrained as experimental data because: (a)  $D$  is commonly calculated assuming that the matrix or bulk composition represents the liquid composition, (b) equilibrium may not always obtain, and (c) the potential effects of mineral or melt inclusions in mineral separates are not always considered. Nevertheless, these ‘natural’ partitioning values are also considered here because there are no

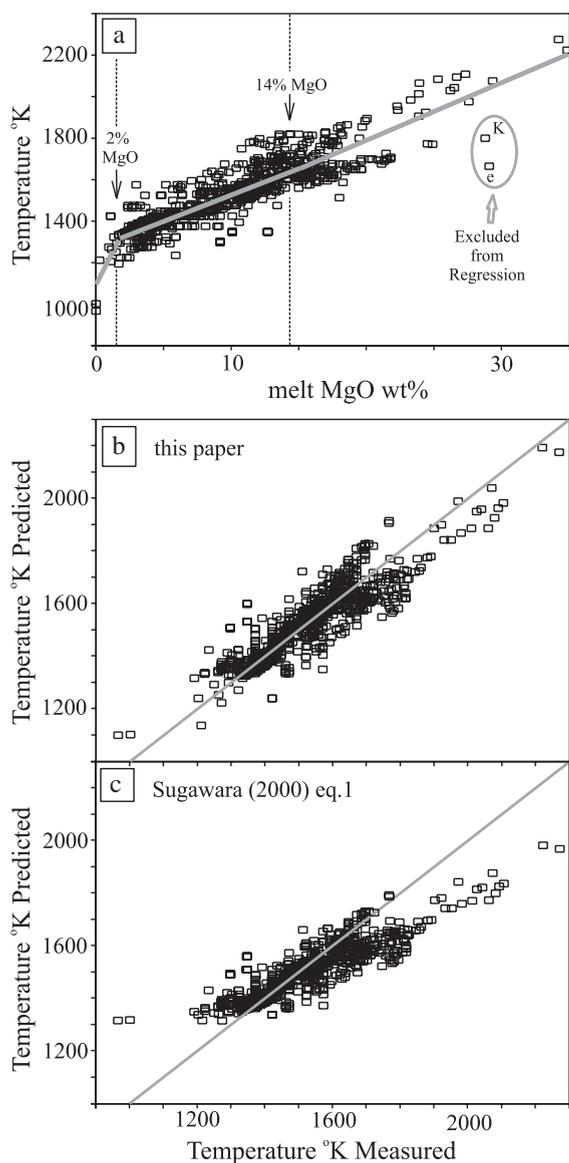


Fig. 1. (a) Experimental temperature in °K vs. melt MgO wt.% for the data compiled here. The data were regressed as three segments (0–2, 2–14 and >14 wt.% MgO), shown as thick grey lines (Table 2). Two datapoints were excluded from the high-MgO regression. (b) and (c) Comparison of measured temperatures with (b) temperatures calculated from the experimental MgO of the liquid using the regressions of Table 2, and (c) with Eq. (1) of Sugawara (2000).

experimental data available for some elements and melt compositional ranges. A potential problem with partitioning data obtained from phase equilibrium studies (Ti, Cr, Na, Al, K) is that olivine minor

element analyses may not have been controlled as carefully as in the dedicated partitioning studies.

When analyzing the partitioning data, discrepant datapoints were excluded from some regressions. These exclusions are discussed below on a case-by-case basis. While discrepant data that result from experimental errors can safely be neglected, data outliers could reflect systematic differences in pressure,  $f_{O_2}$ , volatile activity, bulk composition, crystal chemistry... , etc. These alternatives were investigated where the database was adequate, but it was not always possible to determine why some datapoints or datasets were discrepant.

### 1.5. Approach

Because  $TiO_2$  is easily analyzed with the electron microprobe, the  $D_{Ti}$  dataset is large enough to allow

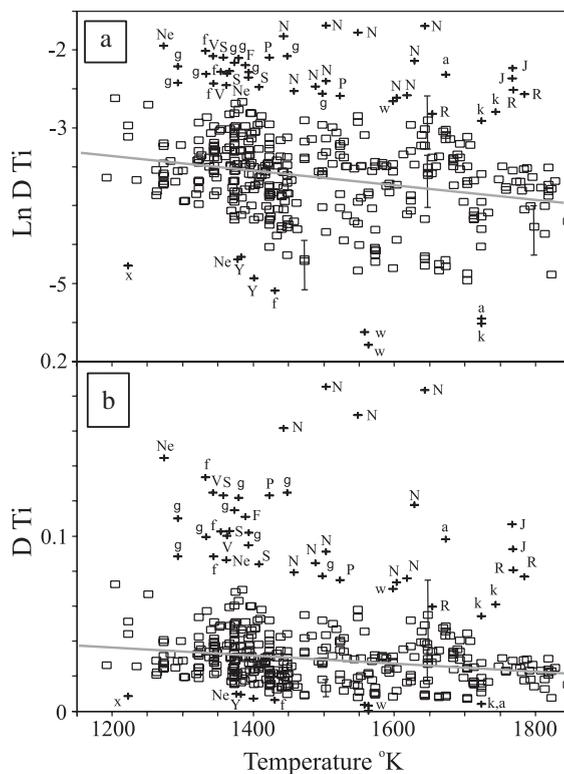


Fig. 2. (a)  $\ln D_{Ti}$  and (b)  $D_{Ti}$  vs. Temperature in °K. Crosses are discrepant data from this figure, and the letter and number codes are from Table 1. The thick grey lines are regressions (Table 2). Representative error estimates from some of the partitioning studies are shown.

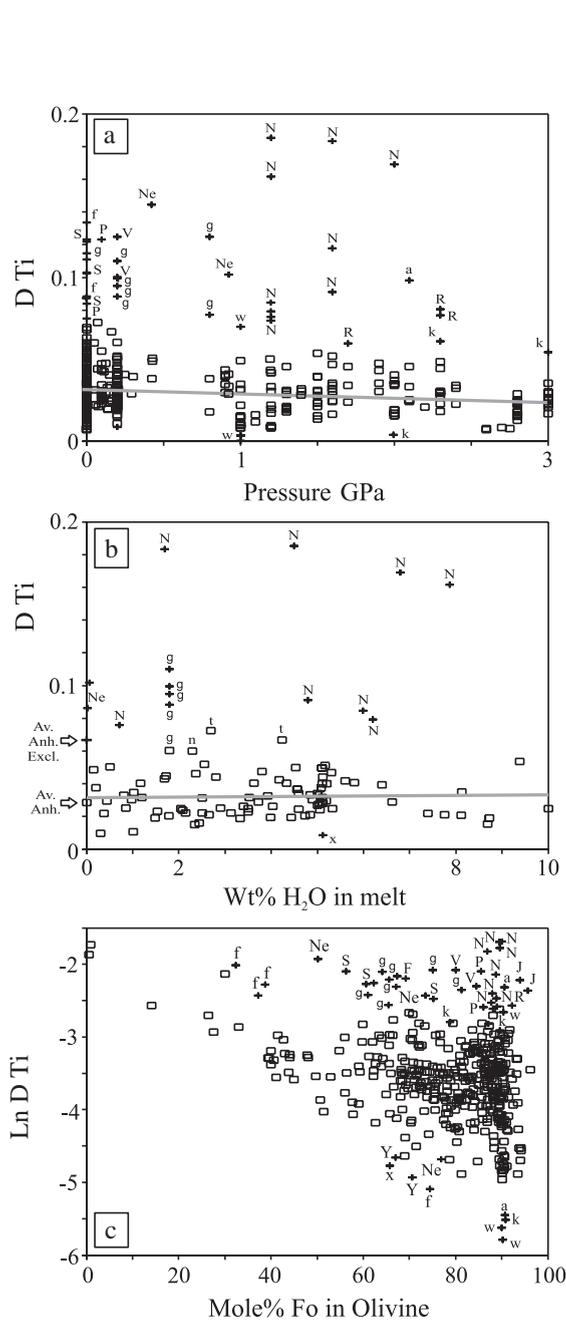


Fig. 3. (a)  $D_{Ti}$  vs. Pressure in GPa, (b)  $D_{Ti}$  vs.  $H_2O$  wt.% in melt, and (c)  $\ln D_{Ti}$  vs. mol% Forsterite content of olivine. Crosses are discrepant data from Fig. 2, and the letter and number codes are from Table 1. The cross marked 'Av. Anh. Excl.' is the average of excluded anhydrous data; while the box marked 'Av. Anh.' is the average of anhydrous data included in the regression, and weighted as if it represented 10 datapoints. The thick grey lines are regressions (Table 2).

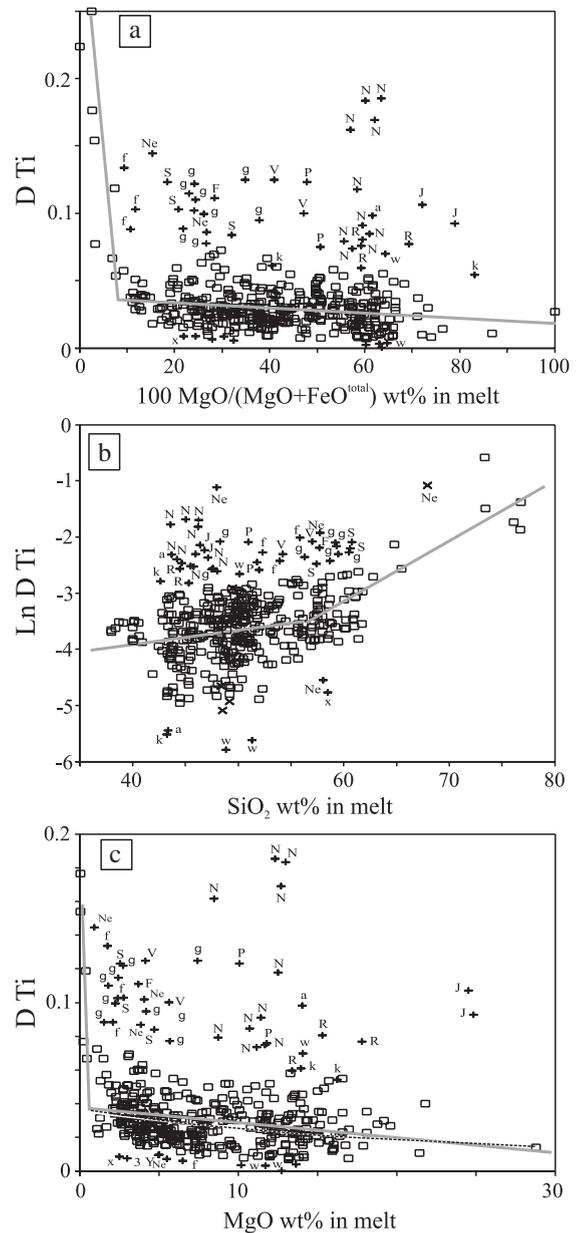


Fig. 4. (a)  $D_{Ti}$  vs.  $100\text{MgO}/(\text{MgO} + \text{FeO}^{\text{total}})$  wt.% in melt, (b)  $\ln D_{Ti}$  vs.  $\text{SiO}_2$  wt.% in melt, and (c)  $D_{Ti}$  vs. MgO wt.% in melt. Crosses are discrepant data from Fig. 2, and the letter and number codes are from Table 1. In 'b' some of the discrepant data were included in the regression, and these are marked as 'x'. The thick grey lines are regressions (Table 2). In 'c' the preferred regression of  $\ln D_{Ti}$  vs. MgO is shown as a heavy dotted line.

some of the causal mechanisms to be deduced (Figs. 1–4), and to determine the optimal input variable against which to parameterize  $D$  variations. A similar

exercise carried out for other elements showed similar systematics (e.g. *D* Sc, Fig. 5). Afterwards, most partitioning data will be regressed against the same variable (Figs. 6–12, Table 2). Elements for which insufficient partitioning data were available to allow regression were averaged (Table 2). Comparisons of the regression results for *D* REE–Y–Sc (Table 2) with the Lattice Strain Model of Blundy and Wood (1994a,b) are then used to derive equations linking MgO with *D*<sub>0</sub> (the strain compensated partition coefficient), *E* (Young’s Modulus), and *r*<sub>0</sub> (the size of the M site) (Figs. 13 and 14, Table 3). From these equations (Table 3), values of *D* REE–Y–Sc can be calculated with the Lattice Strain Model, generating a composite parameterization that is consistent with theory, which can easily be integrated into existing spreadsheets and modeling

algorithms, and that applies to a wide range of melt compositions (Fig. 15).

This simple and partly empirical approach is not meant as a substitute for thermodynamically based partitioning models (e.g. Beattie et al., 1991; Blundy et al., 1996; Colson et al., 2000; O’Neill and Eggins, 2002). Yet, despite considerable progress in developing such models (see Blundy and Wood (2003) for an overview), it is not yet possible to obtain the values of *D* for all elements and *P*–*T*–*X* conditions of interest in this way, and realistically, it will be many years before this becomes possible. For those needing a set of *D* values to model a given magmatic suite, a commonly used, common-sense approach has been to choose a set of *D* values from an experiment done at appropriate *P*–*T* conditions on a melt composition that is ‘similar’

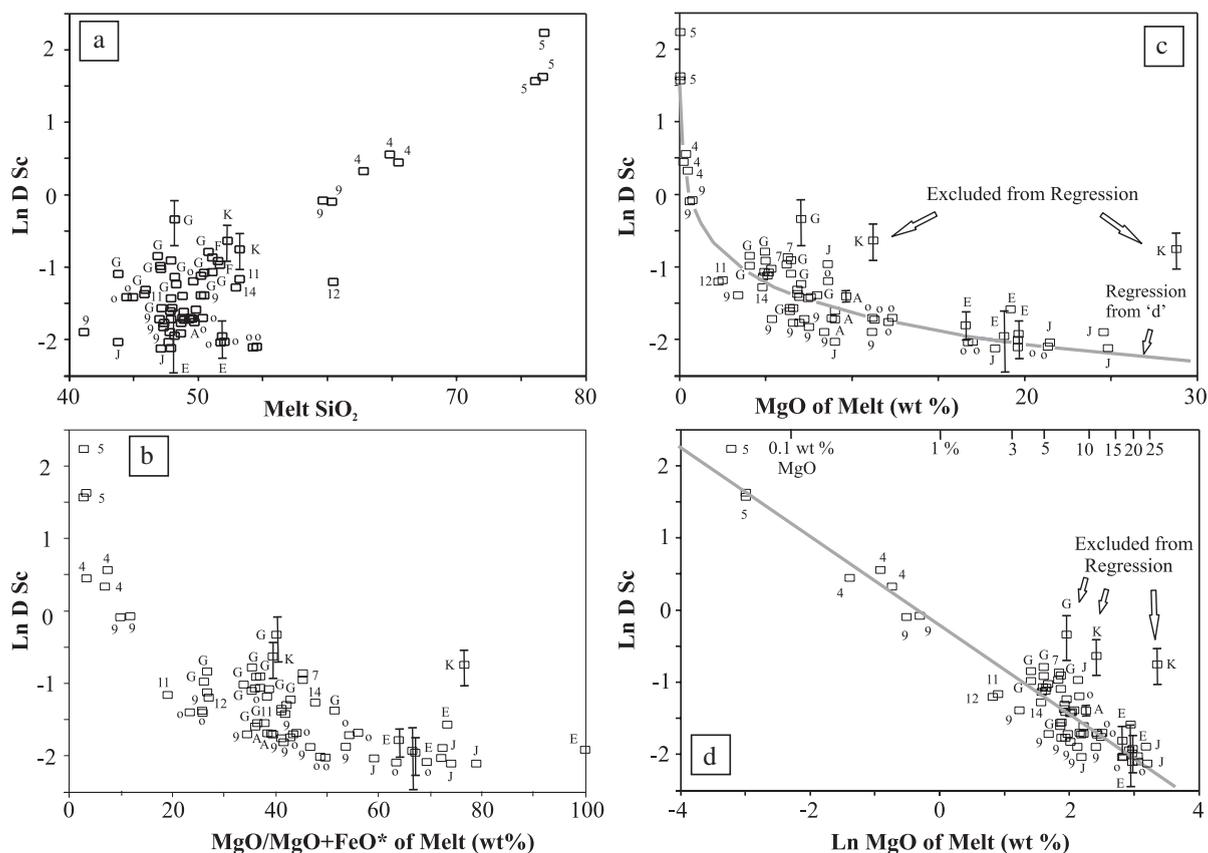
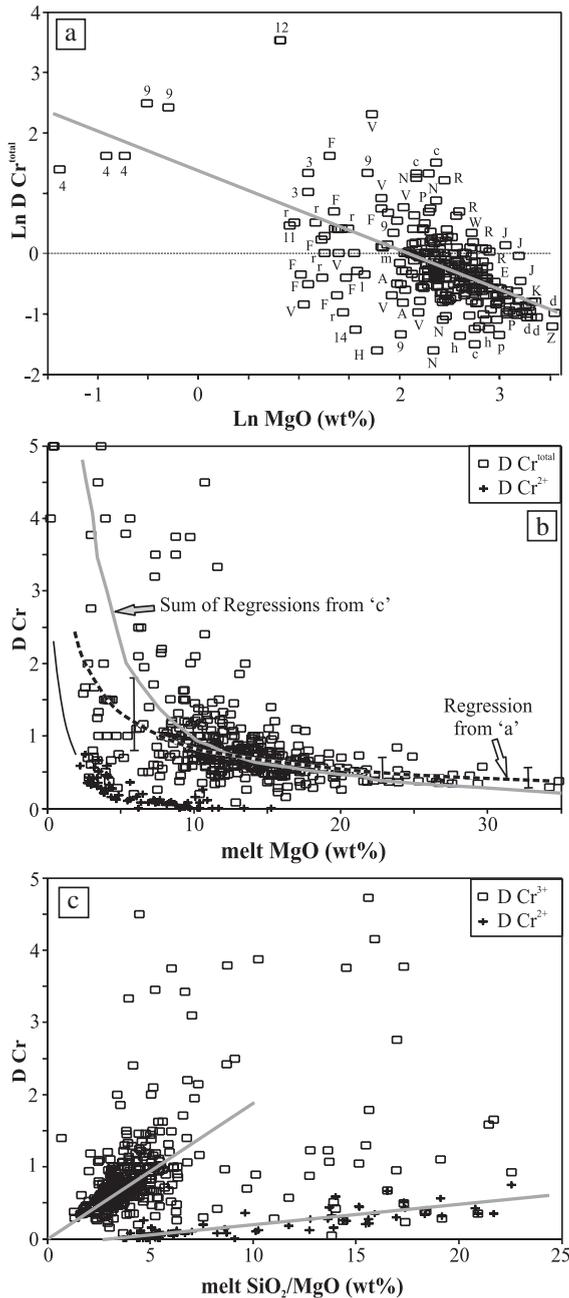


Fig. 5. *Ln D* Sc data (*D* Sc). Some data are annotated by letter or number codes (see Table 1 for key) and show representative error estimates. Data are plotted vs.: (a) melt SiO<sub>2</sub>, (b) melt MgO/MgO+FeO<sup>total</sup> (wt.%), (c) melt MgO (wt.%) and (d) Ln MgO (wt.%) in the melt. The thick grey line in ‘c’ and ‘d’ are regressions (Table 2).

to the suite being investigated. However: (a) few bulk compositions have been investigated in enough detail to do this; (b) few partitioning studies consider the entire geochemical spectrum, handicapping users of multi-element plots (e.g. Thompson et al., 1983); and (c) the variation of  $D$ 's with

changing  $P$ – $T$ – $X$  conditions would still not be accounted for. Given the need for a systematic, quantitative, multi-element estimate of  $D_{\text{olivine/liquid}}$ , and for how these  $D$ 's vary, the partly empirical parameterization proposed here may furnish an interim, practical solution.



## 2. Variations of $D_{\text{Ti}}$ ( $D_{\text{Ti}}$ )

### 2.1. Temperature, pressure, and $\text{H}_2\text{O}$

#### 2.1.1. Temperature–MgO

Temperature and melt MgO content are closely linked (Fig. 1). The data were regressed as three segments (0–2%, 2–14%, +14% MgO) to quantify variations of liquid MgO vs. temperature (Table 2). The equations will be used to link liquid MgO and temperature when applying the Lattice Strain Model (see below).

#### 2.1.2. Temperature– $D_{\text{Ti}}$

There is a diffuse trend of increasing  $D_{\text{Ti}}$  with decreasing temperature for ultramafic, mafic and intermediate melt compositions (Fig. 2). Data from two low-temperature rhyolites from Scaillet and MacDonald (2001) have significantly higher  $D_{\text{Ti}}$  and plot above this trend. A number of data that plot above or below the main trend are shown as crosses on Fig. 2. These anomalous datapoints are also shown as crosses in the next figures (Figs. 3 and 4), emphasizing the fact that the anomalous  $D_{\text{Ti}}$  data are not unusual in terms of temperature, pressure,  $f_{\text{O}_2}$  conditions, or melt composition (including  $\text{H}_2\text{O}$ ). Some of the very low  $D_{\text{Ti}}$  data may represent  $\text{TiO}_2$

Fig. 6. (a)  $\text{Ln } D_{\text{Cr}^{\text{total}}}$  vs.  $\text{Ln MgO (wt\%)}$  in melt. Thick grey line is a regression against all of the data (Table 2). (b)  $D_{\text{Cr}^{\text{total}}}$  and  $D_{\text{Cr}^{2+}}$  vs.  $\text{MgO (wt\%)}$  in melt. Values of  $D_{\text{Cr}^{2+}}$  were calculated as proposed by Hanson and Jones (1998, Table 2), with a low-MgO extension marked in schematically. For  $\text{MgO} > 5\%$ , values of  $D_{\text{Cr}^{2+}}$  are small. The heavy dotted line with error bars shows the value of  $D_{\text{Cr}^{\text{total}}}$  calculated from the regression of 'a' (Table 2); and is very similar to the thick grey line, which shows the trend of the sum of the values of  $D_{\text{Cr}^{3+}}$  and  $D_{\text{Cr}^{2+}}$  calculated from the regressions of 'c' (Table 2). Note that these two parameterizations are very similar for  $\text{MgO} > 5\%$ . (c)  $D_{\text{Cr}^{3+}}$  and  $D_{\text{Cr}^{2+}}$  vs.  $\text{SiO}_2/\text{MgO (wt\%)}$  in melt. Values of  $D_{\text{Cr}^{2+}}$  were calculated as in 'b', with  $D_{\text{Cr}^{3+}} = D_{\text{Cr}^{\text{total}}} - D_{\text{Cr}^{2+}}$ .

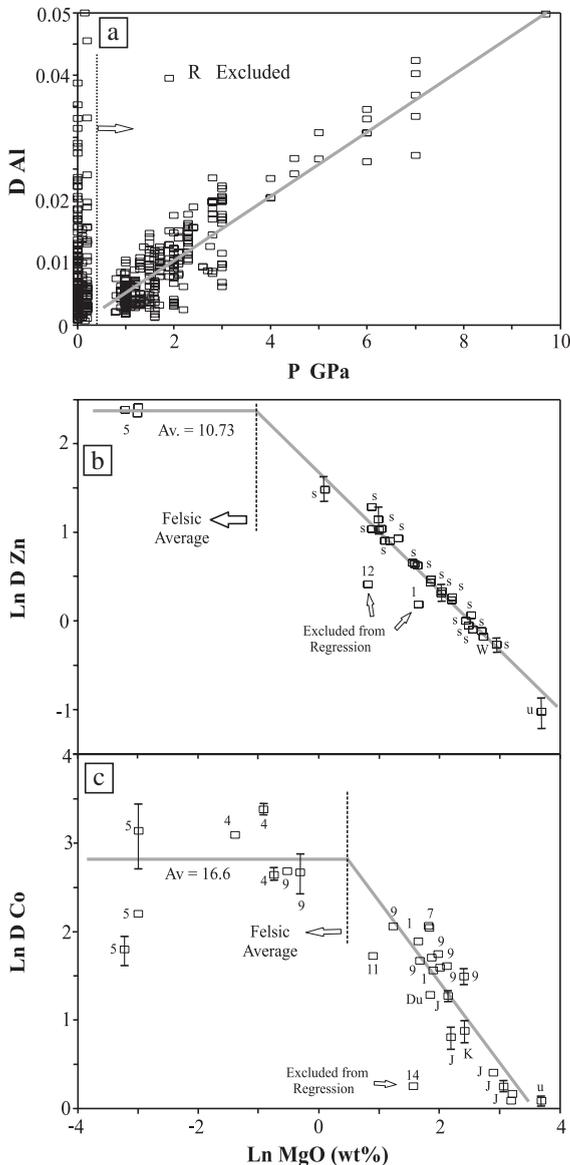


Fig. 7. (a)  $\ln D_{Al}$  vs. Pressure in GPa, (b)  $\ln D_{Zn}$ , and (c)  $\ln D_{Co}$  vs.  $\ln MgO$  (wt.%). Thick grey lines are regressions or averages (Table 2).

detection problems: e.g.  $TiO_2$  in olivine from runs #12 and #27C of Wasylenki et al. (2003, ‘w’) were 0.00125 and 0.000001 wt.%, respectively. The numerous high  $D_{Ti}$  outliers constitute a more difficult problem. For example, consider experimental runs B304 and B333 of Gaetani and Grove (1998, ‘N’). Although these two runs are virtually indistin-

guishable in terms of melt composition, were equilibrated at similar  $P, T, f_{O_2}$  conditions, with similar melt  $H_2O$  contents; run B304 yields a  $D_{Ti}$  of 0.085 (discrepant), while run B333 yields a  $D_{Ti}$  of 0.033 (concordant). Since no obvious reason could be established for the anomalous  $D_{Ti}$  of most outliers, I infer that they may reflect systematic analytical biases or experimental errors, and so excluded them from the  $D_{Ti}$  regressions.

### 2.1.3. Pressure– $D_{Ti}$

When all of the mafic  $D_{Ti}$  data (>1% MgO liquids) are considered together, a very shallow trend of  $D_{Ti}$  increase with pressure decrease is observed (Fig. 3a). However, errors on this regression are large and the correlation coefficient is low (Table 2), suggesting that any influence of pressure on  $D_{Ti}$  is probably overshadowed by other effects.

### 2.1.4. $H_2O$ – $D_{Ti}$

Recent work (Wood and Blundy, 2002) implies that differences in melt volatile contents affect clinopyroxene  $D$  values, and a similar effect might be suspected for olivine. However, olivine  $D_{Ti}$  data show only a diffuse and shallow rate of increase vs. the  $H_2O$  content of the melt (Fig. 3b); suggesting that any effect that melt  $H_2O$  content may have is probably drowned out by other factors.

## 2.2. Mineral–chemical controls ( $Fo = 100 \times Mg / (Mg + Fe^{total})$ )

Plots of  $D_{Ti}$  against the Fo-content of olivine (Fig. 3c) show considerable scatter, and no regression was attempted. An additional complication is that olivine Fo-content and partitioning behaviour may be perturbed by sub-liquidus exchanges with other minerals (chromite or sulphide: e.g. Bédard and Hébert, 1998; Li et al., 2003), or evolved interstitial melt (Barnes, 1986).

## 2.3. Melt compositional controls ( $MgO\#, SiO_2, MgO$ )

### 2.3.1. $MgO\#$ ( $100MgO / (MgO + FeO^{total})$ )

Values of  $D_{Ti}$  increase gradually with decreasing  $MgO\#$  for mafic melts, with a steeper increase in felsic melts (Fig. 4a). The trends of increase vs.  $MgO\#$  are poorly defined, however. The data were regressed

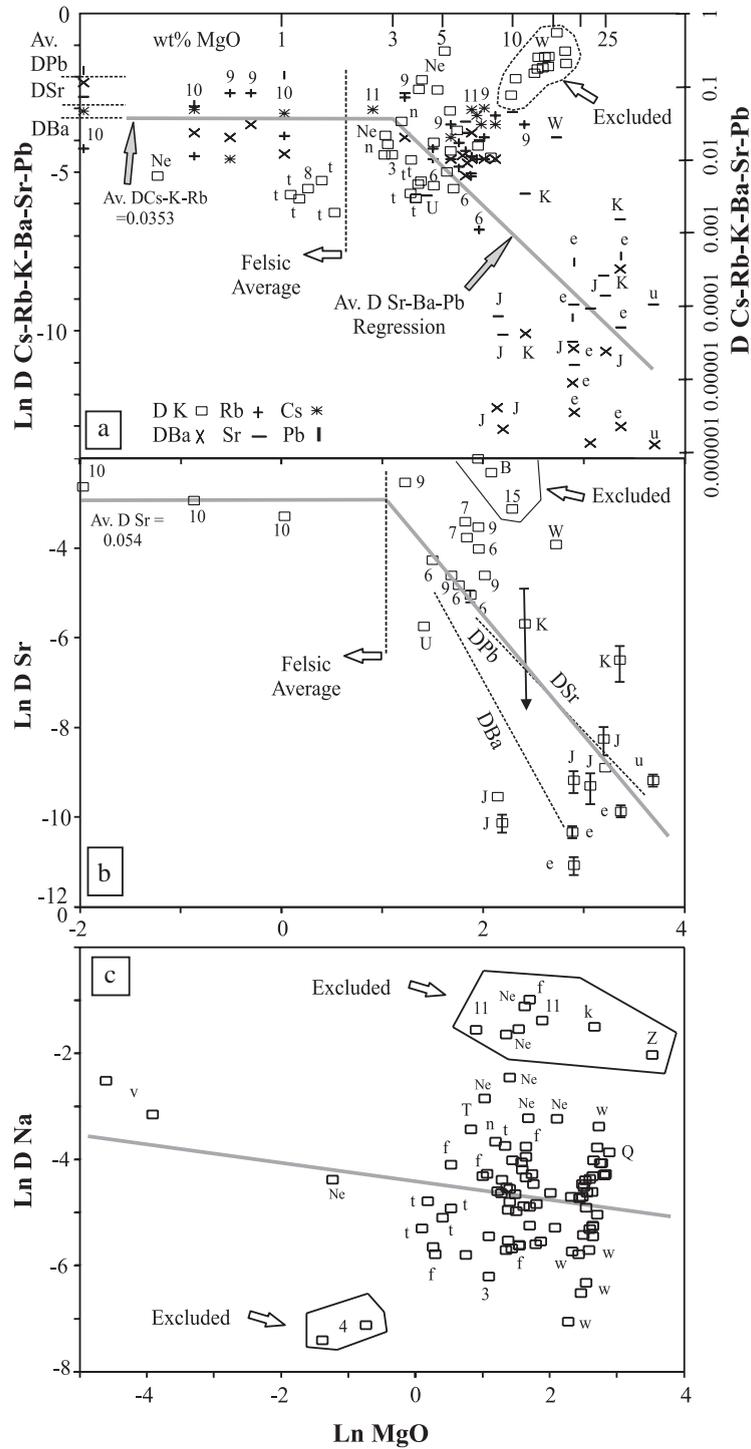


Fig. 8. (a)  $\ln D$  (Sr, Ba, Rb, Cs, K, Pb), (b)  $\ln D$  Sr, (c)  $\ln D$  Na vs.  $\ln \text{MgO}$  (wt.%). Representative error estimates for some data, and mafic-ultramafic regressions for  $D$  Ba and  $D$  Pb, are shown in 'b'. Linear equivalents for MgO and  $D$  data are shown for comparison in 'a'. Thick grey and dotted lines are regressions or averages from Table 2.

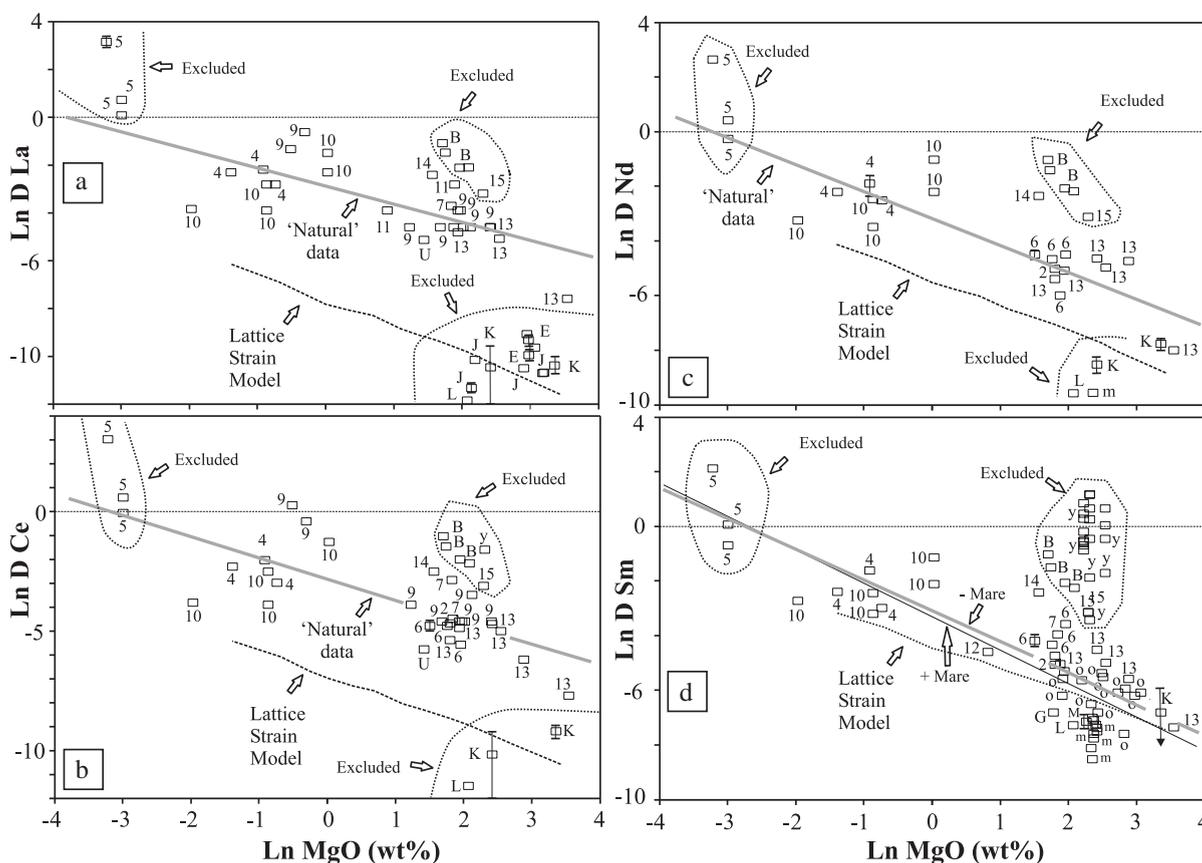


Fig. 9. (a) Ln *D* La, (b) Ln *D* Ce, (c) Ln *D* Nd, and d) Ln *D* Sm vs. Ln MgO (wt.%). Predictions of the Lattice Strain Model (see below) are generally lower than the regression results. Thick grey lines are regressions or averages of mostly ‘natural’ data (Table 2). Ln *D* regressions that exclude and include Lunar Mare data (–Mare and +Mare, respectively) are shown.

as two segments with a cusp at MgO# = 8.35 (Table 2). The mafic trend applies to data with SiO<sub>2</sub> < 60 wt.%; while the felsic trend was calculated for data with MgO# < 10. One potential cause of scatter in MgO# is the decoupling of melt FeO and temperature (e.g. Sugawara, 2000, his Fig. 2), which generates variability in the FeO/MgO ratios of the melt and the minerals crystallizing from it at a given temperature and melt MgO content.

### 2.3.2. SiO<sub>2</sub>

For mafic and ultramafic melts, values of Ln *D* Ti show extensive scatter below 55 wt.% SiO<sub>2</sub> (2 Ln units, Fig. 4b), with a better defined increase in *D* Ti for melt SiO<sub>2</sub> > 55 wt.%. The data were regressed as two segments with a cusp at 55 wt.% SiO<sub>2</sub> (Table 2). The ‘X’ symbols are discrepant data (crosses in Figs.

2 and 3) that were included in the regression against SiO<sub>2</sub>. The extensive scatter of *D* Ti values in the 44–55% SiO<sub>2</sub>-range may reflect the fact that melts perched on the olivine–plagioclase–clinopyroxene cotectic can evolve considerably in terms of temperature and MgO content with little corresponding change in SiO<sub>2</sub> content.

### 2.3.3. MgO

Values of *D* Ti for melts of ultramafic to intermediate composition define a diffuse trend of increase as MgO decreases, with low-MgO felsic melts showing a steeper trend of *D* Ti increase (Fig. 4c). The data were regressed as distinct mafic and felsic segments with a cusp at 0.493 wt.% MgO. The Ln *D* Ti vs. MgO regression for mafic melts showed marginally better statistics, with correlation coeffi-

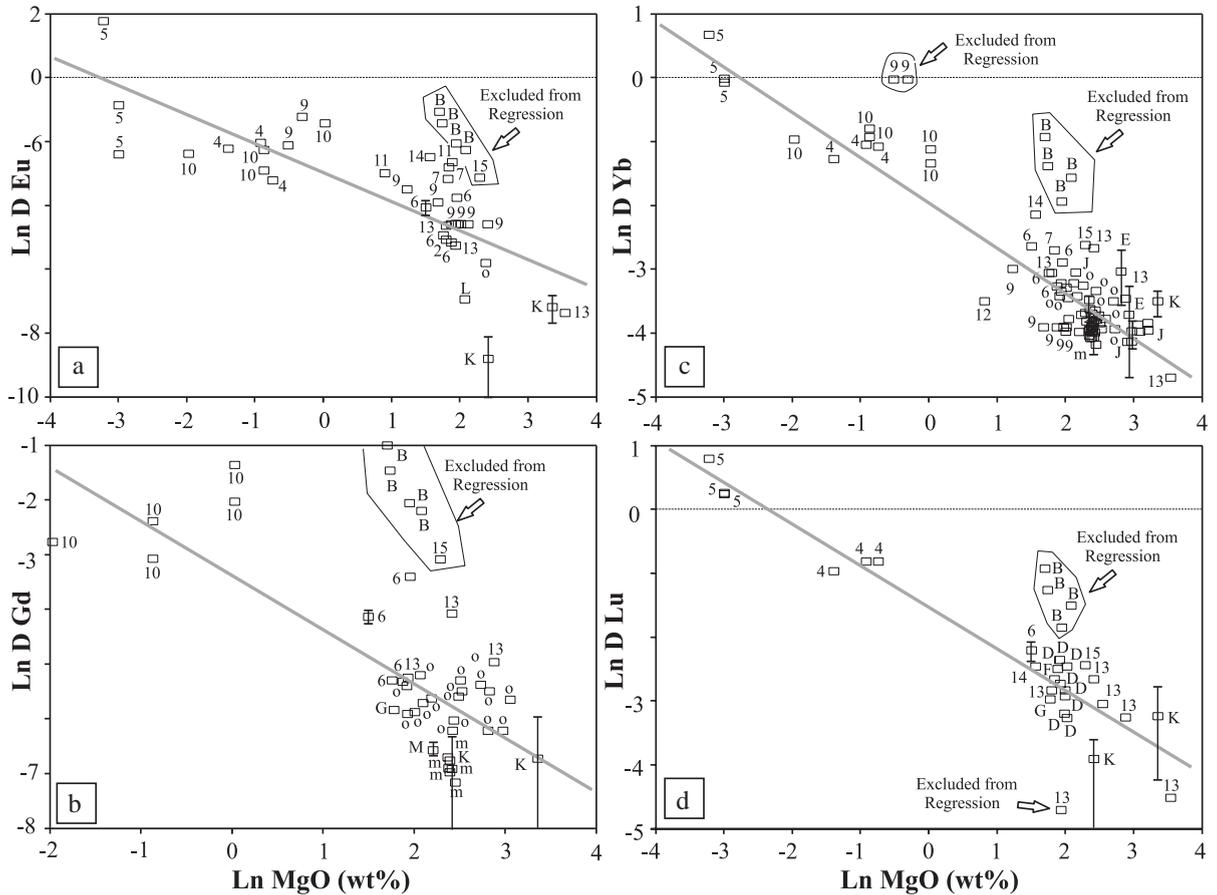


Fig. 10. (a) Ln  $D$  Eu, (b) Ln  $D$  Gd, (c) Ln  $D$  Yb, and (d) Ln  $D$  Lu vs. Ln MgO (wt%). Thick grey lines are regressions or averages (Table 2).

icients of the same order as the regression against temperature (Table 2).

### 3. Parameterization of $D^{\text{olivine/liquid}}$ for trace elements

#### 3.1. Choice of input variable for the parameterization

Regressions of  $D$  Ti (and other elements) against temperature show reasonable trends (e.g. Fig. 2), but temperature is difficult to estimate in natural situations, and there are few felsic data with which to constrain the low-temperature end of the spectrum. Trends of  $D$  Ti vs. pressure, water content, and olivine forsterite content are unconvincing (Fig. 3a–c), and the Fo-content is sensitive to subsolidus effects (see

above, Section 2.2). Although valid in some contexts, use of complex melt functions was not considered for the reasons explained previously (Section 1.3). Among the simple melt compositional parameters examined, the correlations against melt MgO# were generally quite diffuse (Fig. 4a), although tighter trends were observed for some other elements (e.g.  $D$  Sc, Fig. 5b). Plots against melt SiO<sub>2</sub> are scattered for melts of ultramafic to intermediate composition (Figs. 4b and 5a), but yield reasonable regressions for felsic melts. For most of the partitioning data examined, melt MgO content provided the best correlations (Figs. 4c and 5c,d). Consequently, melt MgO content was chosen as the variable against which to parameterize  $D$  variations for all trace elements, in part to minimize errors on calculated  $D/D$  ratios. Using melt MgO content also has many advantages for the

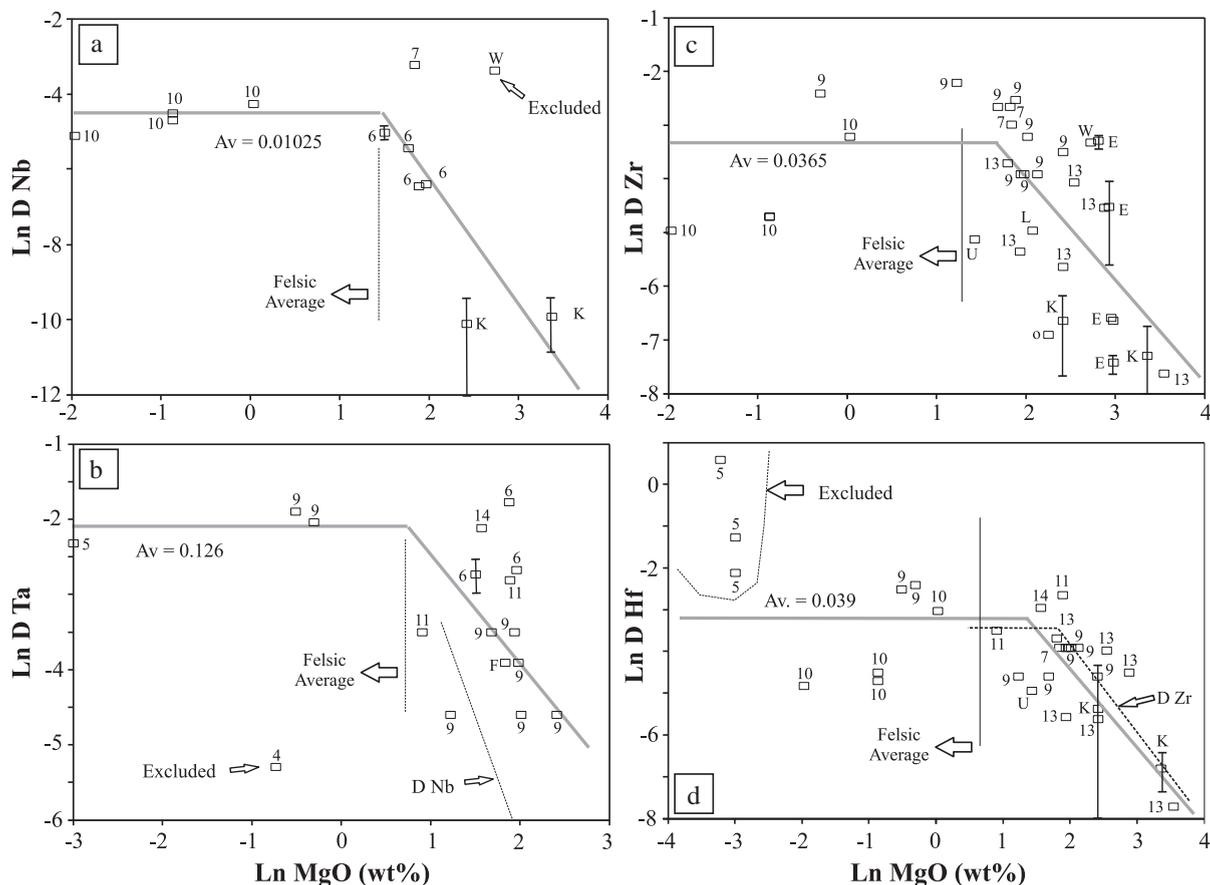


Fig. 11. (a)  $\text{Ln } D \text{ Nb}$ , (b)  $\text{Ln } D \text{ Ta}$ , (c)  $\text{Ln } D \text{ Zr}$ , and (d)  $\text{Ln } D \text{ Hf}$  vs.  $\text{Ln MgO (wt\%)}$ . Thick grey lines are regressions or averages (Table 2). In 'b' the  $D \text{ Ta}$  line was fit by eye, and the  $D \text{ Nb}$  regression is shown for comparison.

geochemical modeler, inasmuch as MgO is closely linked to temperature (Sugawara, 2000, and Fig. 1a; Table 2), and can be calculated from mineral analyses (e.g. MacLennan et al., 2003).

### 3.2. Metals (Sc, Cr, Al, Zn, Co, Ru, Rh, Re, Os, Ni, V)

#### 3.2.1. D Sc

Values of  $\text{Ln } D \text{ Sc}$  increase systematically for melt  $\text{SiO}_2 > 60 \text{ wt\%}$  (Fig. 5a), but exhibit considerable dispersion for  $\text{SiO}_2$  between 40% and 55%. The plots against liquid  $\text{MgO\#}$  (Fig. 5b) or Fo-content (not shown) show much scatter. The plot against the MgO-content of the liquid shows a good correlation (Fig. 5c,d), and arguably, scatters least. Representative error estimates from the original papers are shown, and most data appear to be within

error of the regression. Two  $D \text{ Sc}$  determinations from Kennedy et al. (1993, 'K') and a Datum from Nielsen et al. (1992, 'G') have  $D \text{ Sc}$  that plot much higher than do other determinations at a similar MgO contents (Fig. 5bc). The synthetic melts ('K') have unusually high  $\text{SiO}_2$  (Fig. 5a), high FeO (9–17 wt%), and no alkalis. Which of these features (if any) are responsible for the high  $D \text{ Sc}$  values of these two runs is not clear. Because of these uncertainties, these three discrepant points were excluded from the regressions.

#### 3.2.2. D Cr

For MgO contents >10%, the  $D \text{ Cr}$  data are very coherent (Fig. 6b), and the vast majority of  $D \text{ Cr}$  determinations can be regressed together (Fig. 6a). At lower MgO contents, the data show

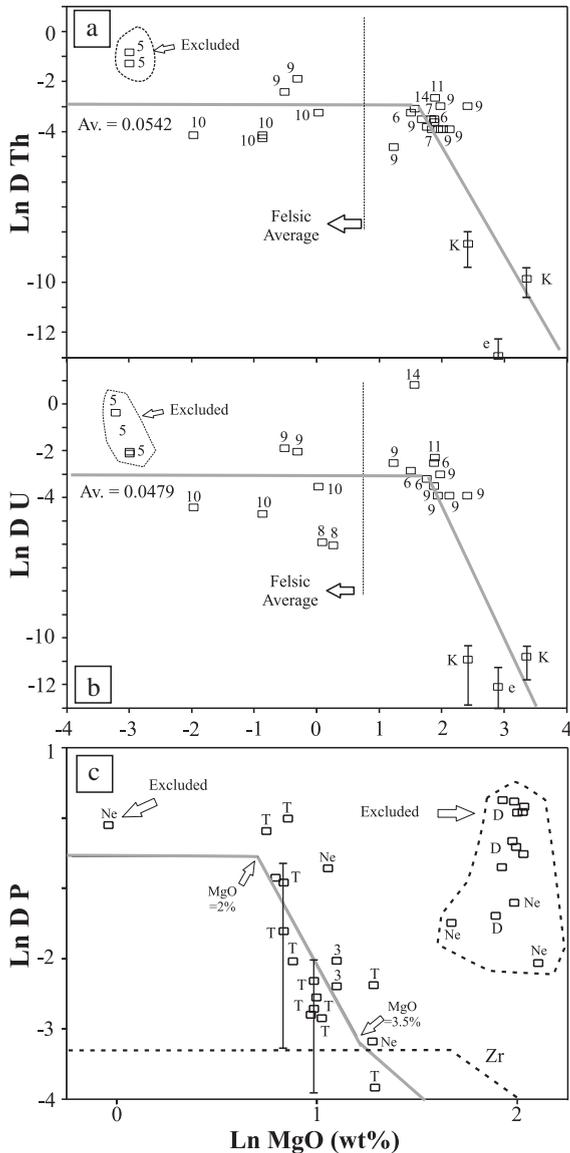


Fig. 12. (a)  $\text{Ln } D_{\text{Th}}$ , (b)  $\text{Ln } D_{\text{U}}$ , (c)  $\text{Ln } D_{\text{P}}$  vs.  $\text{Ln MgO}$  (wt.%). Thick grey lines are regressions or averages (Table 2). Values of the  $D_{\text{Nb}}$  and  $D_{\text{Zr}}$  regressions are shown in 'c' for comparison. Values of  $D_{\text{P}}$  are assumed to plateau out for compositions more felsic than  $\text{MgO}=2$  wt.%. For values of  $\text{MgO}>3.5\%$ , the  $\text{Ln } D_{\text{P}}$  vs.  $\text{Ln MgO}$  line was assumed to have a slope similar to that of the  $D_{\text{Zr}}$  regression.

considerable scatter, presumably reflecting the combined effects of variations in oxygen fugacity, temperature, melt composition, Cr speciation in the melt and crystal-field effects (Schreiber and Haskin, 1976; Suzuki and Akaogi, 1995; Hanson and

Jones, 1998; Colson et al., 2000). In addition, most low-MgO melts are poor in Cr, suggesting that  $D_{\text{Cr}^{2+}}$  values for low MgO melts may be less accurate and precise than those from Cr-rich, high-MgO experiments.

Strongly reduced lunar magmas are expected to have a large proportion of  $\text{Cr}^{2+}$  in the melt, while more oxidized terrestrial magmas have little or none (Schreiber and Haskin, 1976). Values of  $D_{\text{Cr}^{2+}}$  calculated from the expression in Hanson and Jones (1998,  $D_{\text{Cr}^{2+}}=0.66(10,000/T \text{ K})-4.48$ ), applicable to terrestrial magmas, are zero at temperatures  $>1473.2$  K, and increase slowly until about 1200 K, after which values rise more quickly (Fig. 6b). Values of  $D_{\text{Cr}^{2+}}$  are typically very much smaller than  $D_{\text{Cr}^{\text{total}}}$  and should have little impact on  $D_{\text{Cr}^{\text{total}}}$  for  $\text{MgO}>5$  wt.%. Hanson and Jones (1998) also proposed that  $D_{\text{Cr}^{3+}}=-0.39(\text{NBO}/T)+1.29$ , where NBO/T is the ratio of non-bridging oxygens to tetrahedrally coordinated cations (Mysen, 1983). Not all of the data needed to calculate NBO/T have been compiled here, but the ratio of  $\text{SiO}_2/\text{MgO}$  wt.% (network former/modifier) may serve as a proxy. Plots of  $D_{\text{Cr}^{2+}}$  vs.  $\text{SiO}_2/\text{MgO}$  wt.% appear to define a straight line (Fig. 6c) which was regressed (Table 2). Subtracting the value of  $D_{\text{Cr}^{2+}}$  calculated as suggested by Hanson and Jones (1998) from the measured value of  $D_{\text{Cr}^{\text{total}}}$  yields a value for  $D_{\text{Cr}^{3+}}$ , which seems well clustered when plotted against  $\text{SiO}_2/\text{MgO}$  wt.% (Fig. 6c), except for high- $\text{SiO}_2/\text{low MgO}$  data, which scatter widely and which were not included in the regression (only data for  $\text{MgO}>2.5$  wt.% were included). Both approaches yield comparable results (Fig. 6b) for mafic melts, and so the simpler  $D_{\text{Cr}^{\text{total}}}$  regression is preferred.

### 3.2.3. $D_{\text{Al}}$

$D_{\text{Al}}$  data show a clear trend of increase with increasing pressure for mafic–ultramafic melts (Fig. 7a; Table 2). Low-pressure ( $<0.5$  GPa) data for  $D_{\text{Al}}$  show very scattered trends against melt MgO content (not shown), and two averages (for  $\text{MgO}>3\%$  and  $\text{MgO}<3\%$ ) were calculated (Table 2).

### 3.2.4. $D_{\text{Zn}}$

Most  $D_{\text{Zn}}$  data are from Kohn and Schofield (1994) and yield very good correlations (Fig. 7b).  $D_{\text{Zn}}$

Table 2  
Regression results

	Range	Y intercept	Standard error Y	R <sup>2</sup>	N	Slope X	Standard error X
<i>vs. temperature in K</i>							
D Ti	Mafics	0.064768	0.012245	0.0797	354	−2.373e−05	4.2969e−06
Ln D Ti	Mafics	−2.25688	0.449943	0.0880	354	−0.0009202	0.0001579
<i>vs. pressure in GPa</i>							
D Ti	SiO <sub>2</sub> <60%	0.031200	0.012548	0.0330	354	−0.002472	0.000713
D Al	P>0.8 GPa	0	0.003200	0.8187	299	0.0051600	8.350e−05
<i>vs. wt.% H<sub>2</sub>O in melt</i>							
D Ti		0.031795	0.011777	0.0008	97	0.000130	0.000494
<i>vs. 100MgO/MgO+FeO<sup>total</sup> wt.% in melt</i>							
D Ti	SiO <sub>2</sub> <60%	0.0373594	0.012286	0.0587	366	−0.0001927	4.0443e−05
D Ti	MgO#<8.35	0.3199849	0.109968	0.5402	10	−0.034200	0.011156
<i>vs. SiO<sub>2</sub> wt.% in melt</i>							
Ln D Ti	SiO <sub>2</sub> <57.0967%	−4.956987	0.478451	0.0339	298	0.026060	0.008092
Ln D Ti	SiO <sub>2</sub> >57.0967%	−9.718522	0.447954	0.5787	81	0.109454	0.010506
Ln D Sc	All	−6.603421	0.486269	0.7032	70	0.105354	0.008299
<i>vs. MgO wt.% in melt</i>							
T °K	MgO<2%	1097.2721	96.32468	0.4217	17	128.5956	38.88502
T °K	MgO 2–14%	1269.8519	70.00587	0.6203	635	25.78361	0.801853
T °K	MgO>14%	1217.6602	82.36312	0.5817	203	27.98546	1.673959
D Ti	MgO>0.493%	0.0378058	0.019702	0.0477	366	−0.000940	0.000220
D Ti	MgO<0.493%	0.287680	0.134368	0.3821	8	−0.518924	0.269424
Ln D Ti	MgO>0.493%	−3.341999	0.457732	0.1108	366	−0.034417	0.005111
D Re	MgO 6–16%	0.434801	0.038140	0.9181	7	−0.025012	0.003340
D Os	MgO 6–16%	0.076084	0.008095	0.8964	7	−0.004664	0.000709
<i>vs. Ln MgO wt.% in melt</i>							
Ln D Cs,K,Rb	MgO>1.11%	0.052277				−3.048573	
Ln D Ba	MgO>1.125%	1.220691	2.492188	0.5937	20	−4.078261	0.795201
Ln D Sr	MgO>1.04%	−0.103745	2.040069	0.4795	24	−2.701496	0.600062
Ln D Pb	MgO>0.45%	−0.960117	1.286470	0.7468	5	−2.365962	0.795375
Ln D Th	MgO>4.9037%	3.805739	1.857101	0.5826	18	−4.221746	0.893387
Ln D U	MgO>5.91%	7.079996	2.155782	0.7038	14	−5.674872	1.062760
Ln D Nb	MgO>4.47%	0.281997	1.637831	0.6511	7	−3.295911	1.079028
Ln D Ta	MgO>4.4%	0				−1.5	
Ln D P	MgO>3.5%	−0.2				−2.5	
Ln D P	2<MgO<3.5%	2.922448	0.705766	0.5922	15	−4.993652	1.149384
Ln D Zr	MgO>5.2%	−0.254395	1.291158	0.4313	27	−1.879372	0.431619
Ln D Hf	MgO>1.38%	−2.985779	1.002827	0.6808	23	−0.760857	0.113676
Ln D La	Natural	−2.896755	1.067633	0.5152	26	−0.749805	0.148474
Ln D Ce	Natural	−2.855783	1.204564	0.5359	29	−0.906973	0.162432
Ln D Nd	Natural	−3.166716	1.461593	0.5434	20	−0.980556	0.211838
Ln D Sm	−Mare	−3.261860	1.152858	0.6395	44	−1.143695	0.132508
Ln D Sm	+Mare	−3.378820	1.224925	0.6034	53	−2.334665	0.138915
Ln D Eu	All	−2.966757	1.241378	0.6342	37	−0.905163	0.116190
Ln D Gd	All	−3.407878	0.917655	0.6146	37	−0.977639	0.130870
Ln D Tb	All	−2.697347	0.942221	0.7674	30	−0.865027	0.090000
Ln D Dy	All	−2.641279	0.770337	0.8724	21	−0.904799	0.079403
Ln D Y	All	−2.673573	1.101424	0.4249	19	−0.661902	0.186190

(continued on next page)

Table 2 (continued)

	Range	Y intercept	Standard error Y	R <sup>2</sup>	N	Slope X	Standard error X
Ln D Ho	All	-2.316611	0.843870	0.6993	16	-0.83043	0.145549
Ln D Er	All	-2.229420	0.710297	0.7006	19	-0.697091	0.110519
Ln D Yb	All	-1.952636	0.418793	0.8561	76	-0.713368	0.033992
Ln D Lu	All	-1.523311	0.360950	0.9261	26	-0.643206	0.037087
Ln D Cr	All	1.346400	0.504824	0.3650	421	-0.654416	0.042170
Ln D Co	MgO>0.5%	3.238143	0.308432	0.8017	22	-0.899993	0.100081
Ln D Zn	MgO>1%	1.695972	0.093334	0.9766	28	-0.674038	0.020442
Ln D Sc		-0.207763	0.255686	0.9196	67	-0.614241	0.022531
Ln D Na		-4.507033	0.850363	0.0637	84	-0.179334	0.075907

vs. SiO<sub>2</sub>/MgO wt.% in melt for MgO>2.5%

D Cr <sup>2+</sup>	T<1473 K	-0.086472	0.105407	0.7225	66	0.027712	0.002147
D Cr <sup>3+</sup>	MgO>4%	0	0.704659	0.0543	392	0.187641	0.007579

		Averages	N Data	Standard deviation	Source
D Cs–K–Rb	MgO<1.11%	0.0353	17	0.0334	
D Ba	MgO<1.125%	0.036	6	0.0343	
D Pb	MgO<0.45%	0.132	4	0.0449	
D Sr	MgO<1.04%	0.054	3	0.0143	
D Th	MgO<4.904%	0.0542	6	0.0504	
D U	MgO<5.91%	0.0479	7	0.0591	
D Nb	MgO<4.4%	0.01025	4	0.00303	
D Ta	MgO<3.79%	0.126	3	0.0214	
D Zr	MgO<5.2%	0.0365	4	0.0336	
D Hf	MgO<1.38%	0.0394	7	0.0318	
D P	MgO<2%	0.5834	assumed		
D Co	MgO<0.5%	16.63	8	7.27	
D Al	MgO>3%, P<0.8 GPa	0.00889	211	0.01177	
D Al	MgO<3%, P<0.8 GPa	0.01184	31	0.01430	
D Zn	MgO<1%	10.73	3	0.29	(5)
D Cu		0.11	2	–	(1,u)
D Ag		0.38	1	–	(W)
D Au		0.1258	1	–	(I)
D Li		0.198	2	–	(u,U)
D Be		0.2475	2	0.2125	(6)
D Mo		0.1034	5	0.4000	(10,6)
D Sn		0.119	1	–	(10)
D Sb		0.1938	8	0.1668	(11,9)
D Mo		0.1034	5	0.0400	(6,10)
D Sb	Mafic	0.0925	4	0.0334	(9)
D Sb	Felsic	0.44	2	–	(9)
D Ga		0.1026	4	0.1243	(E)
D Cd		0.082	1	–	(u)
D Pd	(carbonatite)	2.3	1	–	(W)
D Pd	(silicate melt)	0.02604	12	0.03181	(b,I,17, exclude 1 value from Ca)
D Pt		0.05136	2	0.01340	(17)
D Ru		0.66575	7	0.37070	(b,I,17,Ca: exclude 1 value from b)
D Rh		2.69581	9	1.41070	(b,Ca)
D Re	MgO<8 wt.%	0.27048	2	0.07292	(16)
D Re	MgO>8 wt.%	0.03816	8	0.01856	(I,16)
D Os	MgO<20 wt.%	0.01448	7	0.02126	(16)
D Os	MgO>20 wt.%	0.53437	2	0.10393	(17)
D Ir		0.42619	2	0.07381	(17)

Zn measurements from some older studies are discrepant and were not included in the regression. The scanty felsic data were averaged (Table 2).

### 3.2.5. *D* Co

Data for *D* Co yield a good regression (Fig. 7c) for mafic melt compositions. A single datum from Wörner et al. (1983, '14') was excluded, since the melt MgO content for this datum is poorly constrained. A separate average value was calculated for low MgO melts (Table 2).

### 3.2.6. *Pt*, *Pd*, *Ru*, *Rh*, *Re*, *Os*, *Ir*

Data on Platinum Group Elements are sparse, and few systematic trends were seen (Table 2). Data on *D* Pd from a carbonatite (*D* Pd=2.3, Sweeney et al., 1995) is much higher than data from silicate melts (av.=0.026). A single, very high value of *D* Ru=2.2 from Brenan et al. (2003) was excluded from the average. Data on *D* Re appear to define two groups, with two data from melts with MgO<8 wt.% being much higher than data from melts with MgO>8 wt.%. Data for *D* Os shows the opposite pattern, with two data from melts with MgO>20 wt.% from Puchtel et al. (2004) being much higher than data from Burton et al. (2002) from melts with lower MgO contents.

### 3.2.7. *D* Ni, *D* V

Many papers deal with how *D* Ni varies with melt composition, the more recent of which (Kinzler et al., 1990; Li et al., 2003, see Table 2) incorporate the effects of the melt FeO/MgO ratio and olivine Fo-

content, yielding prediction errors of ca. 13%. Canil and Fedortchouk (2001) have recently parameterized how *D* V varies with oxygen fugacity (Table 2).

### 3.3. Large ion lithophile elements (LILE): (*Cs*, *Rb*, *K*, *Na*, *Ba*, *Sr*; *Pb*)

Data for *D* Cs, *D* Rb and *D* K are sparse, scattered, and apart from some imprecise *D* K measurements calculated from the data in phase equilibrium studies, are unavailable for high-MgO systems (Fig. 8a). Data for *D* Sr, *D* Ba and *D* Pb also show considerable scatter, but do include values from high-MgO melts (Fig. 8a,b). A further complication is the tendency for these partitioning data to form three non-colinear clusters. Cluster 1 comprises very low *D* values from high-MgO melts (Kennedy et al., 1993 'K'; Beattie, 1993 'e' and 1994 'J'; Purton et al., 2000 'u'). Cluster 2 is constituted mostly of natural data from basaltic to intermediate melts, and have higher *D* values than the 1st cluster. Cluster 3 comprises data from low-MgO melts, with *D* values only slightly higher than the 2nd cluster.

Why are there three clusters? The high-MgO, low-*D* cluster is principally constituted by data from Beattie (1993, 1994) and Kennedy et al. (1993). The error estimates (e.g. see *D* Sr, Fig. 8b) would imply that the extremely low *D* values are not analytical artefacts. The other clusters are constituted by data from many different studies, which would seem to preclude a systematic analytical or laboratory errors. Since the 2nd (basaltic) cluster is constituted principally of natural data, the high *D* values of

#### Notes to Table 2:

$D_{\text{olivine/liquid}}$  *D* parameterization. Gives values of the slope 'X' and intercept 'Y' allowing *D* values to be calculated from the melt MgO (wt.%) content, and estimates of the errors on the regressions and the fit ( $R^2$ ). Average values are given where data were inadequate to allow regression, as well as the applicable MgO range. Some of the data from Mahood and Hildreth (1983) were excluded from the felsic averages for Th, U, Hf and LILE because of probable trace mineral contamination (Michael, 1988). Equations for *D* Ni are from Arndt (1977), Hart and Davis (1978), Kinzler et al. (1990), and Li et al. (2001). The *D* V equation is from Canil and Fedortchouk (2001). Equations for *D* Cr are from Hanson and Jones (1998).

Expressions from the literature

$D_{\text{Ni}} = 115/(\text{MgO wt.}\%) - 2.1$  (Arndt, 1977).

$D_{\text{Ni}} = 124/(\text{MgO wt.}\%) - 0.9$  (Hart and Davis, 1978).

$\text{Ln } (D_{\text{Ni wt/Fo mole fraction}}) = 0.355 - 1.263 \text{ Ln MgO (mol\% in liquid)}$  (Kinzler et al., 1990).

$\text{Ln } D_{\text{Ni}} = 5.67 - 1.38 \text{ Ln MgO (wt.}\%) - 0.25 (\text{FeO/MgO})$  (Li et al., 2001).

$\text{Log } D_{\text{V}} = -0.23 \Delta \text{NNO} - 1.46$  (Canil and Fedortchouk, 2001).

$D_{\text{Cr}^{2+}} = 0.66 (10,000/T \text{ } ^\circ\text{K}) - 4.48$  (Hanson and Jones, 1998).

$D_{\text{Cr}^{3+}} = -0.39 (\text{NBO/T}) + 1.29$  (Hanson and Jones, 1998; Mysen, 1983).

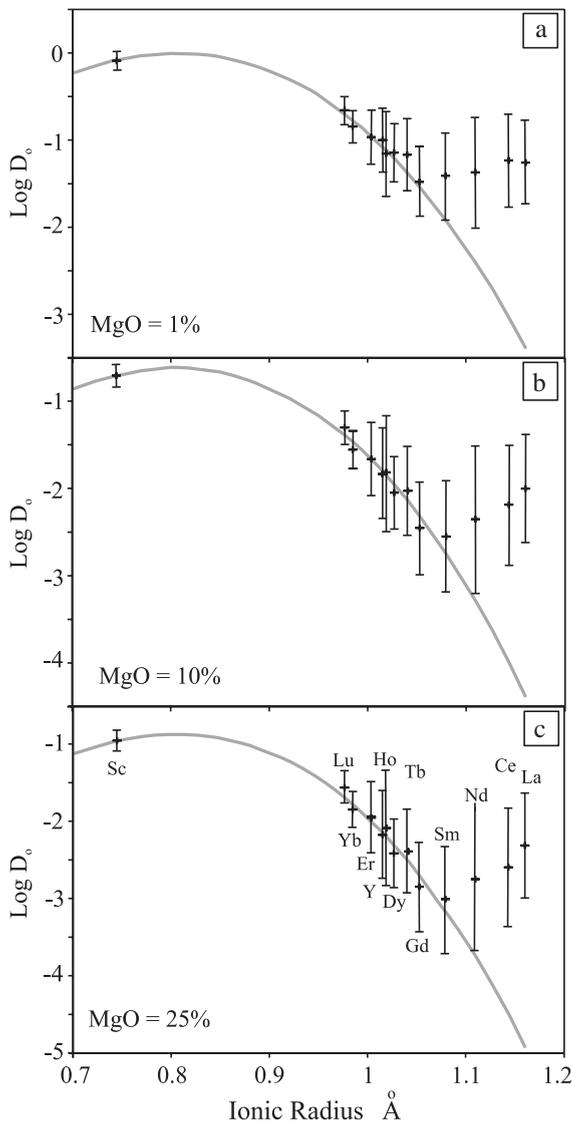


Fig. 13. (a) Comparison of predicted values of  $\text{Log } D$  from the Lattice Strain Model (Eq. (1), grey curve), with regressions of Table 2 (crosses) for three representative liquid MgO contents. Values of  $E_M^{3+}$ ,  $r_0$ , and  $D_0$  were allowed to vary until a satisfactory visual fit was obtained. Only  $D$ 's for the middle and heavy REE, Y and Sc were used to adjust the fit. Temperature was calculated using equations in Table 2 (Fig. 1a). Note that values of  $D$  La,  $D$  Ce and  $D$  Nd calculated with the Lattice Strain Model are significantly below most experimental and natural values, which form a plateau, interpreted to be due to kinetic effects (Kennedy et al., 1993). Note that this plateau effect appears to become more pronounced as the MgO content decreases. Ionic radii are from Shannon (1976).

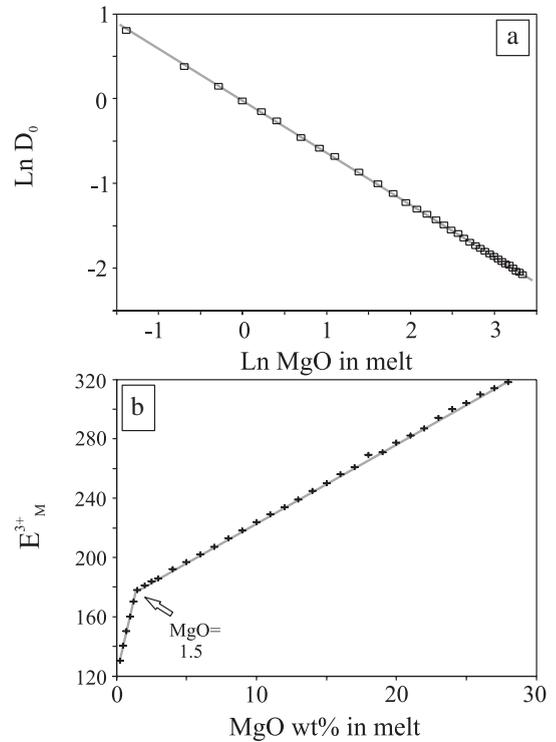


Fig. 14. (a)  $\text{Ln } D_0$  (strain-compensated partition coefficient) vs.  $\text{Ln MgO wt.\% in melt}$ , and (b)  $E_M^{3+}$  (Young's Modulus) vs.  $\text{MgO wt.\% in melt}$ . Datapoints were derived by fits like those of Fig. 13. Thick grey lines are regressions from Table 3.

the 2nd cluster may reflect the presence of melt or solid inclusions in the analyzed material (cf. Kennedy et al., 1993). The lack of continued increase in  $D$  values as MgO decreases (cluster 3) might be attributed to a change in the crystal chemistry of Fe-rich olivines; but cell parameters increase linearly from forsterite to fayalite (Brown, 1982), which suggests that this cannot be the explanation.

Until these problems are resolved, any parameterization of  $D$  for the LILE will remain uncertain. Nevertheless, as a 1st approximation, data from ultramafic and mafic melt compositions (clusters 1 and 2, Fig. 8b) for  $D$  Sr,  $D$  Ba and  $D$  Pb were regressed for each of these elements (Table 2). Data from felsic melt compositions were averaged for each element (Table 2; Fig. 8a). Because of their sparsity, felsic data for  $D$  K,  $D$  Rb and  $D$  Cs were averaged together (Fig. 8a). Two  $D$  K determinations from

Table 3  
Results of regressions for  $D_0$  and  $E_M^{3+}$

	Y intercept	Standard error Y	$R^2$	#	Slope X	Standard error X
vs. Ln MgO						
Ln $D_0$ All	-0.02713243	0.00891947	0.999	34	-0.6126633	0.0011471
vs. MgO						
$E_M^{3+}$ MgO > 1.5%	170.1960	0.809903	0.999	29	5.346736	0.018326
$E_M^{3+}$ MgO < 1.5%	120.6667	0.690066	0.999	6	38.85714	0.659829

Parameterization for  $E_M^{3+}$  and  $D_0$  vs. MgO or Ln MgO (respectively), which feed into the Brice (1975) equation (Eq. (1)), allowing calculation of  $D$  REE,  $D$  Y, and  $D$  Sc from MgO in the liquid. Values of  $r_0$  were assumed constant at 0.807 Å.

Scaillet and MacDonald (2001) plot offscale, but were included in the averages.  $D$  K data for high-MgO melts from the phase equilibrium study of Wasylenki et al. (2003) plot anomalously and were not used. Since there are no reliable high-MgO partitioning data for K, Rb and Cs, I assumed that

they would be in the same range as Sr, Ba and Pb, and computed an average regression from the  $D$  Sr–Ba–Pb data (Fig. 8a).

Scattered  $D$  Na data increase as MgO decreases (Fig. 8c), but no other obvious trends were detected against any other variable.

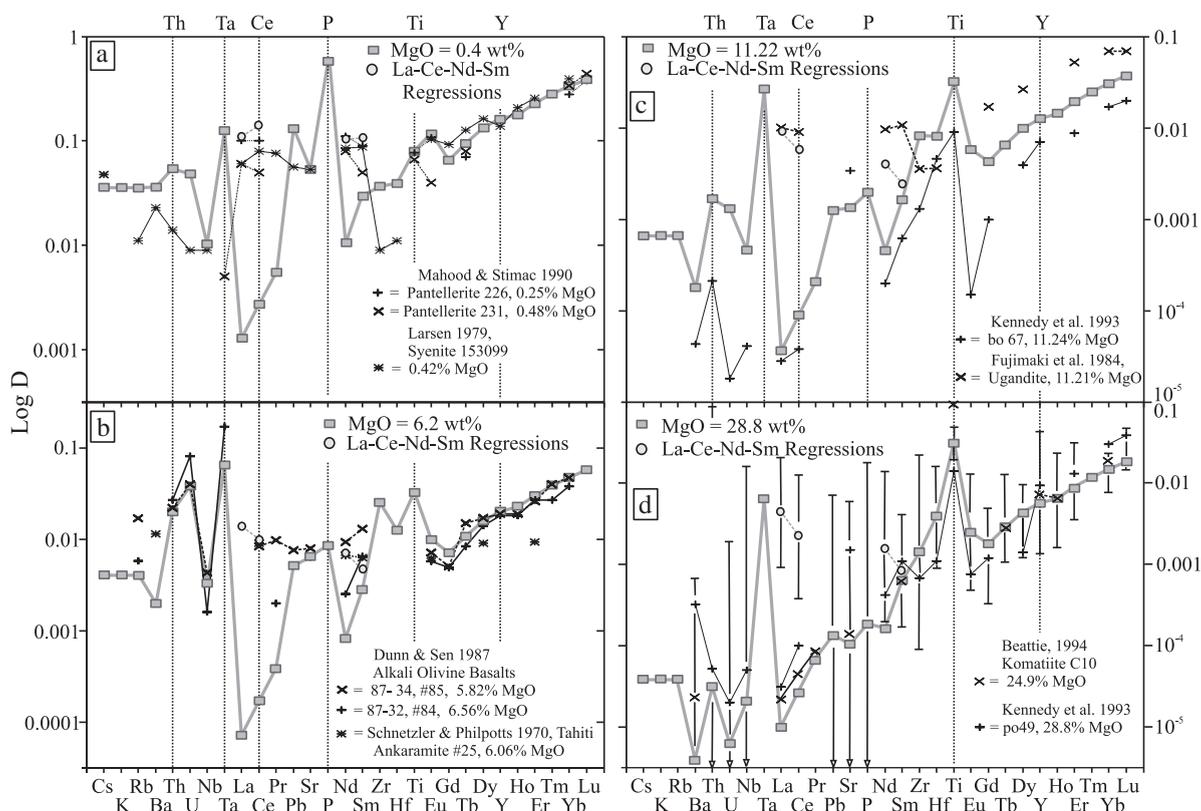


Fig. 15. Comparison of typical experimental partitioning data with results (grey boxes) of the composite parameterization (Tables 2 and 3). The circles show results of the  $D$  La,  $D$  Ce,  $D$  Nd and  $D$  Sm regressions (Table 2), to illustrate the ‘plateau’ effect for these data. Error estimates for the regressions of Table 2 are shown in ‘d’.

### 3.4. Highly charged cations (rare earths, Y, Nb, Ta, U, Th, Zr, Hf, P)

#### 3.4.1. Rare earths, Y

Variations of *D* REE are constrained by reasonably large datasets (Figs. 9 and 10) that extend from high- to low-MgO melt compositions. The middle and heavy REE (Sm, Gd, Tb, Dy, Ho, Er, Tm, Yb and Lu) display coherent behaviour, with all except the oldest data forming a single trend that was regressed (Fig. 10; Table 2). In contrast, partitioning data for the Light REE (LREE) La, Ce, Nd, Sm (Fig. 9) and Eu (Fig. 10) display a complex distribution similar to the one observed for the LILE (Fig. 8). The LREE partitioning data from Kennedy et al. (1993), Beattie (1994), Canil and Fedortchouk (2001) and McKay (1986) tend to plot below the main trend of the data, while some older data (Shimizu et al., 1982, 'B' and '15'; Mysen, 1978, 'y') plot above it. As a first approximation, I calculated regressions for the mafic to felsic spectrum, ignoring the low-*D* high-MgO data cluster. The data that were regressed are almost entirely 'natural' data and provide a benchmark against which to compare results of the Lattice Strain Model (see below). A few natural data with uncertain MgO contents (LeMarchand et al., 1987, '9') were excluded from the regressions, as were the data of Mahood and Hildreth (1983, '5') which are probably contaminated with LREE-enriched trace phases (Michael, 1988).

#### 3.4.2. *D* Nb, *D* Ta, *D* Zr, *D* Hf, *D* Th, *D* U

There are few *D* Nb and *D* Ta data, and there is considerable scatter, making regressions problematic (Fig. 11a,b). For *D* Nb, ultramafic–mafic data were regressed, while felsic data were averaged (Fig. 11a; Table 2). A single datum from Sweeney et al. (1995, 'W') was excluded from the regression. This datum is from a carbonatitic melt, and as there was no equivalent *D* Ta determination, I excluded the *D* Nb value to avoid creating a bias when comparing *D* Nb to *D* Ta. The *D* Ta data scatter considerably and did not yield a reasonable regression, and so a line was passed through the main cloud of *D* Ta data to join the felsic *D* Ta average. Note that all existing *D* Ta data is 'natural'. More experimental *D* Ta and *D* Nb data are badly needed.

For *D* Zr, *D* Hf, *D* Th, *D* U, partitioning data from ultramafic–mafic melts were regressed, while *D* data

from felsic melts were averaged (Figs. 11c,d and 12a,b; Table 2). *D* Hf data from Mahood and Hildreth (1983) were not included in the average because they appear to be anomalously high, and may have been perturbed by trace mineral inclusions (Michael, 1988).

#### 3.4.3. *D* P

Most of the *D* P data define a reasonable correlation (Fig. 12c), but the range of MgO contents controlling the regression is narrow (2.1–3.6 wt.% MgO), and the steep slope is quite different from that of other highly charged cations. Use of such a steep slope would generate prominent negative *D* P anomalies in the *D* profiles for high-MgO melt compositions, and large positive anomalies for felsic melt compositions. To avoid these modeling artefacts, I assumed that *D* P will behave similarly to other HFSC and assigned a slope similar to the slope of the *D* Zr regression for MgO contents >3.5%. Since high P<sub>2</sub>O<sub>5</sub> is not reported from Fe-rich olivines, I assumed that *D* P plateaus out for MgO contents <2 wt.%. The data of Dunn (1987, 'D') appear to be anomalously high and were not included in the regression. Data from Nekvasil et al. (2004) also show considerable scatter, and were not included in the regression.

## 4. Comparison with the Lattice Strain Model (LSM)

It has long been known that trace element partition coefficients show a maximum value centered at the ionic radius of the host site (Onuma et al., 1968). This has been formalized by Brice (1975) and Blundy and Wood (1994a,b) and is commonly referred to as the Lattice Strain Model (LSM), or as the Brice equation. The LSM posits a parabolic distribution of Log *D* values around the ionic radius of the host site '*r*<sub>0</sub>', which gives the position of the curve apex on the ionic radius axis (e.g. Fig. 13). The Blundy and Wood (1994a,b) expression is:

$$D_i = D_0 \exp(-4\pi EN_A((r_0/2)(r_i - r_0)^2 + 1/3(r_i - r_0)^3)/RT) \quad (1)$$

where *D*<sub>0</sub> is the strain compensated partition coefficient, giving the *D* value of the curve's apex; *r*<sub>0</sub> is the ionic radius of the cation of interest (taken from

Shannon, 1976);  $E$  is the Young's Modulus of the host site, which affects the shape of the model curve;  $N_A$  is Avogadro's number;  $R$  is the gas constant and  $T$  is temperature in degrees Kelvin, here calculated from the temperature–MgO regressions of Table 2 (Fig. 1a).

Values of  $D_0$ ,  $E$  and  $r_0$  are commonly determined by fitting the LSM to sets of experimental partitioning data (e.g., see Wood and Blundy, 1997; Hill et al., 2000). Trace element  $D$  values for the rare earths, Y and Sc obtained from the regressions of Table 2 were compared visually to results of the LSM for many different MgO contents (Fig. 13). The position and shape of the model curves are extremely sensitive to changes in  $D_0$ ,  $E$  and  $r_0$ , which were allowed to vary so as to pass the model curves through the main Sc–HREE–MREE distribution (HREE and MREE are heavy and middle rare earth elements, respectively). As suggested by Kennedy et al. (1993),  $D$  Sc is near the apex of the model curves and a constant value of  $r_0=0.807 \text{ \AA}$  was found to yield reasonable fits for all models. Derived values of  $E_M^{3+}$  yield tight linear correlations with MgO in the liquid, with an inflection at MgO=1.5 wt.% (Fig. 14a). The decrease in  $E_M^{3+}$  implies that the  $D$  profile will 'flatten' as the melt evolves. Trivalent cations such as Cr, Sc and the REE appear to enter olivine as a coupled substitution with Al (Schreiber and Haskin, 1976; Beattie, 1994), partitioning into two non-equivalent octahedral sites (Brown, 1982). Consequently, the values of  $E_M^{3+}$  derived here represent composites for the two olivine M sites. Ln  $D_0$  is also very well correlated with Ln MgO (Table 3; Fig. 14b), and shows a steady increase. These excellent correlations (Fig. 14) suggest that  $D_0$  and  $E_M^{3+}$  are adequately parameterized in this manner, and that the LSM can be used in conjunctions with the equations in Table 3 to calculate equilibrium values of  $D$  for these elements at any MgO content.

Although the  $D$  values for middle- and heavy-REE, Y and Sc plot along the trends predicted by the LSM, the  $D$  for the LREE (Nd–Ce–La) form a plateau (Fig. 13), with the plateau effect extending to  $D$  Sm as melts become cooler and more evolved (Fig. 13a). In contrast, modern high-quality experimental data plot along the trend expected from the Lattice Strain Model (Figs. 4 and 15). Kennedy et al. (1993) concluded that high cooling rates (>500 °C/h) prevent the establishment of complete equilibrium, with the trace element enrichment (plateau effect) being

accounted for by the incorporation of small amounts (<1%) of trapped melt (cf. Beattie, 1994).

## 5. Discussion

Results of the LSM parameterization (Table 3) for calculation of  $D$  REE–Y–Sc are combined with the regressions for other elements (Table 2) to produce multi-element  $D$  plots for different MgO contents (0.4, 6.2, 11.22, 28.8 wt.% MgO, Fig. 15). Fig. 15d compares the model  $D$  profile (boxes) at 28.8% MgO to experiment po49 from Kennedy et al. (1993) and C10 from Beattie (1994). Overall, the data from Kennedy et al. (1993) and Beattie (1994) are very similar to the model profile. Note the prominent positive  $D$  Ti and  $D$  Ta anomalies in the model, and the absence of a  $D$  Nb anomaly. If the model  $D$  values are taken at face value, the implication is that high-MgO komatiitic melts equilibrating with dunitic residua should develop small negative Ti–Ta anomalies, and might fractionate Nb from Ta, and Zr from Hf.

With further cooling and melt evolution (Fig. 15c), the overall model  $D$  abundances increase progressively (cf. Fig. 14a), and the profile shape flattens (cf. Fig. 14b). The model profile shape for primitive basalts (11.22 wt.% MgO) is broadly similar to those of available experimental  $D$  profiles (Fig. 14c). The slowly cooled experiments (bo67) of Kennedy et al. (1993) conform to the model  $D$  profile predicted by the LSM (boxes), while the natural data of Fujimaki et al. (1984) more closely resemble the regressions of Table 2 (circles), perhaps indicating a kinetic limit on partitioning of the LREE, as proposed by Kennedy et al. (1993). Note also that the positive  $D$  Zr,  $D$  Hf, and  $D$  Ti anomalies have increased in size, the apparent  $D$  Ta anomaly remains prominent, and that the  $D$  Zr/ $D$  Hf ratio has increased (Fig. 15c).

For basaltic melt compositions, the model  $D$  profile shape closely resembles the existing experimental data (6.2% MgO, Fig. 15b), except for the  $D$  LREE data, which show the plateau effect discussed above. Positive  $D$  U and  $D$  Th anomalies have appeared, the  $D$  Ta anomaly remains prominent, while the  $D$  Ti anomaly has decreased in size (Fig. 15b). The positive  $D$  Zr and  $D$  Hf anomalies have increased in size and  $D$  Zr/ $D$  Hf has increased. However, the scatter for  $D$  Zr and  $D$  Hf is extensive

(Fig. 11d), and the changes in model  $D$  Zr/ $D$  Hf are probably not significant. For more evolved melts, the absolute values of  $D$  continue to increase for most elements (Figs. 14a and 15a), and fit the sparse  $D$  data reasonably well, with the exception of the  $D$  LREE, which are higher than values predicted by the LSM (Fig. 9).

The observation of a plateau effect for the extremely incompatible elements (La, Ce, Nd; Figs. 13 and 15) in most natural and some experimental partitioning studies suggests that effective  $D$  values for other extremely incompatible elements (Cs, K, Rb, Ba, Th, Nb) may also be higher than they should if full equilibrium were to have prevailed. Perhaps the cooling and crystallization rates in natural magmatic systems are sufficiently high that equilibrium partitioning is the exception, rather than the rule, and the effective  $D$  values bottom out for kinetic reasons? In terms of modeling, this suggests that different strategies may pertain to different petrogenetic scenarios. If the process to be simulated is melting of a slowly upwelling mantle diapir, or a slowly cooled layered intrusion (<500 °C/hr) then values of  $D$  La–Ce–Nd–Sm calculated with the LSM would apply. If

one wishes to model intra-crustal fractional crystallization of a fast-cooling magma sheet, or any process where timescales are short, then a constant  $D$  LREE value= $D$  Sm may be more germane. Alternatively, if Kennedy et al. (1993) and Beattie (1994) are correct in attributing the LREE plateau effect to incorporation of a small amount of trapped melt (ca. 0.3% to 1%) in the growing crystal, then an effective  $D$  value could be calculated simply by incorporating the effects of a trapped melt fraction.

$$D_e = (D(1 - a)) + a \quad (2)$$

where  $D_e = D$  effective, and  $a =$  the fraction of trapped melt with  $D = 1$  (e.g., see Bédard, 2001).

It has been suggested that  $^{olivine/liquid}D_{HFSC} > ^{olivine/liquid}D_{REE}$  (HFSC=High Field Strength Cations, REE=Rare Earth Elements), and that melts percolating through the mantle that assimilate orthopyroxene and crystallize olivine acquire ‘arc’-like geochemical signatures as a result (Kelemen et al., 1990). The ubiquitous presence of positive  $D$  Ti and  $D$  Ta anomalies for all mafic–ultramafic melt compositions, and of positive  $D$  Zr and  $D$  Hf anomalies for basaltic compositions (Fig. 15), suggests that crystallization of

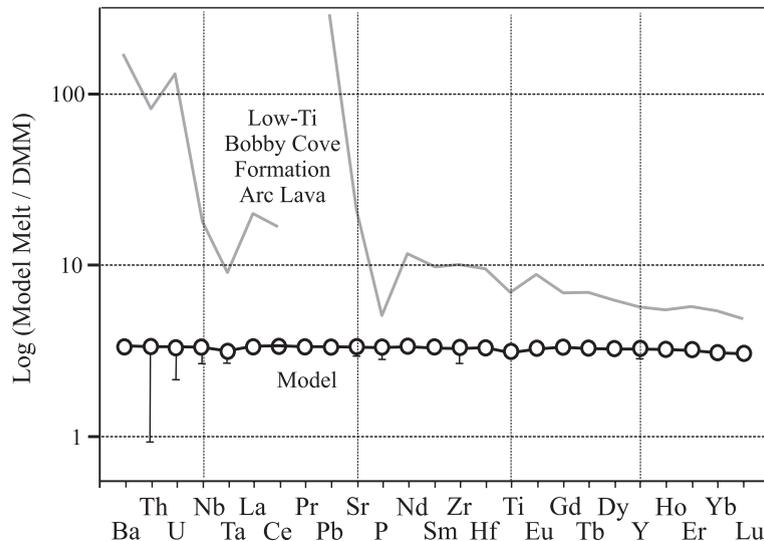


Fig. 16. Model melt derived from a mid-ocean ridge basalt source (DMM from Bédard, 1999; Workman and Hart, submitted for publication) through 30% equilibrium melting ( $C_L = C_o / (D + F(1 - D))$ ,  $C_L =$  concentration in the liquid,  $C_o =$  concentration in the source,  $F =$  melt fraction) with a dunitic residue and 10 wt.% MgO in the melt. Error bars are values from the regressions against melt MgO (Table 2). No error bars are shown for Ta and Pr because these elements were not regressed. Symbols are generally larger than errors. Typical Arc melt from Bédard et al. (2000).

olivine, or decompressive melt-rock reactions involving precipitation of olivine, could perhaps generate perceptible negative anomalies for Ta, Ti, Zr and Hf. The general absence of a positive  $D$  Nb anomaly, on the other hand (Fig. 15), seems inconsistent with generation of a true ‘arc’ signature as a result of such a process. As an example, Fig. 16 shows the composition of a 10% MgO melt formed by 30% equilibrium melting of fertile MORB mantle (DMM) with a dunitic residue (Bédard, 1999). The error bars represent the uncertainties resulting solely from the regressions of  $D$  from Table 2. The MORB-normalized model melt has a flat profile, with only weak HFSC anomalies, very different from typical arc-type magmas (Fig. 16).

## 6. Conclusions

Nernst partition coefficient data between olivine and silicate melt ( $D^{\text{olivine/liquid}}$ ) show significant variability for many trace elements of petrological interest. Variations of  $D^{\text{olivine/liquid}}$  are parameterized against the MgO wt.% of the melt, and typically show trends of increasing  $D$  with decreasing MgO. Comparisons of the  $D^{\text{olivine/liquid}}$  regressions to results of the Lattice Strain Model (LSM) yield well-constrained relationships between liquid MgO,  $D_0$ ,  $E_M^{3+}$ , with constant  $r_0$ , allowing  $D^{\text{olivine/liquid}}$  REE–Y–Sc to be calculated with the LSM for any MgO content (Tables 2 and 3). The parameterizations proposed here should provide improved solutions to trace element models applied to olivine-bearing systems. The  $D$  data suggest that basaltic melts in equilibrium with olivine may acquire weak negative Hf–Zr–Ti–Ta anomalies, but that negative Nb anomalies are unlikely to develop. The misfits between results of the Lattice Strain Model and most LREE and LILE partitioning data suggest that kinetic effects may limit the lower value of  $D$  for extremely incompatible elements in natural situations characterized by high cooling/crystallization rates.

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## Appendix A. Supplementary data

Supplementary data associated with this article can be found, in the online version, at [doi:10.1016/j.lithos.2005.03.011](https://doi.org/10.1016/j.lithos.2005.03.011).

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