

Transit-timing variations in the AU Mic system observed with CHEOPS*

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ABSTRACT

Context. AU Mic is a very active M dwarf star with an edge-on debris disk and two known transiting sub-Neptunes with a possible third planetary companion. The two transiting planets exhibit significant transit-timing variations (TTVs) that are caused by the gravitational interaction between the bodies in the system.

Aims. Using photometrical observations taken with the CHaracterizing ExOPlanet Satellite (CHEOPS), we aim to constrain the planetary radii, the orbital distances, and the periods of AU Mic b and c. Furthermore, our goal is to determine the superperiod of the TTVs for AU Mic b and to update the transit ephemeris for both planets. Additionally, based on the perceived TTVs, we study the possible presence of a third planet in the system.

Methods. We conducted ultra-high precision photometric observations with CHEOPS in 2022 and 2023. We used Allesfitter to fit the planetary transits and to constrain the planetary and orbital parameters. We combined our new measurements with results from previous years to determine the periods and amplitudes of the TTVs. We applied dynamical modelling based on TTV measurements from the 2018–2023 period to reconstruct the perceived variations.

Results. We found that the orbital distances and periods for AU Mic b and c agree with the results from previous works. However, the values for the planetary radii deviate slightly from previous values, which we attribute to the effect of spots on the stellar surface. AU Mic c showed very strong TTVs, with transits that occurred ~ 80 minutes later in 2023 than in 2021. Through a dynamical analysis of the system, we found that the observed TTVs can be explained by a third planet with an orbital period of ~ 12.6 days and a mass of $0.203_{0.024}^{0.022} \, M_{\oplus}$. We explored the orbital geometry of the system and found that AU Mic c has a misaligned retrograde orbit. The limited number of AU Mic observations prevented us from determining the exact dynamical configuration and planetary parameters. Further monitoring of the system with CHEOPS might help to improve these results.

Key words. planets and satellites: fundamental parameters

1. Introduction

AU Mic is a young M1-type dwarf star with an age of 22±3 Myr (Mamajek & Bell 2014) that hosts two sub-Neptune-type planets (Plavchan et al. 2020; Martioli et al. 2021) and a complex debris disk that is viewed edge-on (Mathioudakis & Doyle 1991; Kalas et al. 2004). It is a fairly close system with a distance of 9.71 pc (Gaia Collaboration 2023), which makes it an excellent target for investigating a planetary system in the early stages of evolution.

AU Mic is a very active M dwarf star (Butler et al. 1981; Tsikoudi & Kellett 2000; Gilbert et al. 2022) with a strong magnetic field (Kochukhov & Reiners 2020). It produces frequent flare events (Ilin & Poppenhaeger 2022) and has large stellar spots (Hebb et al. 2007; Plavchan et al. 2020). Given the relative proximity of the planets to the host star, signs of star-planet interactions are expected (Kavanagh et al. 2021) and may be reflected in the distribution of stellar flares (Ilin & Poppenhaeger 2022). On the other hand, the spots on the stellar surface may influence the planetary parameters derived from transit modelling for AU Mic b and c (Oshagh et al. 2013). A better understanding of

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the activity of the host may therefore be beneficial for refined radii of the planets. We study the activity of AU Mic in an accompanying publication (Kriskovics et al., in prep.).

AU Mic hosts an extended debris disk that is viewed edge-on (Kalas et al. 2004). Infrared observations confirmed the size of the disk, which has an inner radius of about 9 AU (MacGregor et al. 2013; Matthews et al. 2015) and a peak brightness of about 40 AU (MacGregor et al. 2013). Its outer halo extends to 210 AU (Kalas et al. 2004). The disk exhibits complex structures from large radial cavities to clumps and warps. It also shows asymmetries in the vertical distribution of the dust (Schneider et al. 2014; Wisniewski et al. 2019).

The two known transiting planets in the system, AU Mic b and c, are both Neptune-sized bodies, with masses of $11.7\pm5.0~M_{\oplus}$ and $22.2\pm6.7~M_{\oplus}$, respectively (Zicher et al. 2022). The radii of planets b and c were determined to be $3.55\pm0.13~R_{\oplus}$ and 2.56±0.12 R_⊕ (Szabó et al. 2022), respectively. However, because of the strong activity and the spot-covered surface of the host star AU Mic, the precision of the estimates on the planetary radii may be lower. The inner planet, AU Mic b, has a mean orbital period of about 8.463 days (Gilbert et al. 2022) and is in a 7:4 spin-orbit resonance with the star (Szabó et al. 2021). The outer planet, AU Mic c, has a mean orbital period of 18.859 days (Gilbert et al. 2022). Both planets exhibit significant transittiming variations (TTVs) of the order of tens of minutes (Szabó et al. 2022). These large variations are likely due to the gravitational effects of additional planets in the system. Wittrock et al. (2023) found that the observed TTVs could be explained with an Earth-sized planet that orbits between AU Mic b and c. A more precise determination of the superperiod of the TTVs may help us to confirm the presence of AU Mic d.

The CHaracterizing ExOPlanet Satellite (CHEOPS) is a small-class ESA mission with the primary objective of conducting follow-up studies of known exoplanetary systems using ultra-high precision photometry (Benz et al. 2021). With its observational strategy, stability, the effective aperture of 30 cm, and the broad bandpass of 330–1100 nm (Deline et al. 2020), CHEOPS is suitable for detecting planetary transits over an extended portion of the sky around a large variety of host stars (Fortier et al. 2024). In recent years, CHEOPS has proven to be a valuable tool for constraining planetary radii (Lendl et al. 2020; Delrez et al. 2021; Bonfanti et al. 2021) and determining TTV in multiplanet systems (Szabó et al. 2022; Delrez et al. 2023).

We present high-precision photometric observations of the transits of AU Mic b and c that were carried out by CHEOPS. In Sect. 2, we describe our observations and data reduction methods. In Sect. 3, we analyse the transit light curves and describe the dynamical analysis of the system based on the TTV measurements. We present and discuss our results in Sect.4.

2. Observations and data reduction

2.1. CHEOPS photometry

We observed six and three transits of AU Mic b and c during the observation period 2022, respectively. In 2023, seven additional transits were observed by CHEOPS for AU Mic b, and four more transit for AU Mic c. On two occasions, a double transit of both planets b and c was observed, once in each year. Since AU Mic is a relatively bright star with a brightness of G=7.843 in the Gaia G band (Gaia Collaboration 2023), it was possible to perform short-cadence photometry (with exposures of 3 seconds). However, due to the strong flaring activity of the star, only eight transits of planet b and six for planet c were appropriate for

further analysis following visual inspection. The efficiency of the observations varied between 50.2–79.1% in 2022 and 50.0–79.3% in 2023. The observation log for the entire campaign of 2022–2023 is available here.

In this analysis, photometry was extracted using the CHEOPS imagettes alone. The imagettes are small images centred around the target star, with a radius of 30 pixels, and unlike sub-array images, they do not have to be co-added on board of the telescope. They can instead be downloaded individually. Photometric extraction of imagettes was carried out using PSF imagette photometric extraction (PIPE), a tool that was specifically developed for this purpose using point-spread function (PSF) photometry (Brandeker et al. 2024). In this case, the PIPE photometry has a shorter cadence than the CHEOPS data reduction pipeline (DRP) on the aperture photometry of the subarrays, but the signal-to-noise ratio (S/N) is similar. The shorter cadence of the imagettes can be of crucial importance in the case of active stars, such as AU Mic, to better identify and adequately analyse flares. We provide a detailed analysis of the flares of AU Mic in an accompanying publication (Kriskovics et al., in prep.).

Since CHEOPS continuously rolls during its 98.77-minute orbit in order to keep the radiators from facing towards Earth, the field of view of the telescope also rotates around the target. This effect, combined with the irregularly shaped CHEOPS PSF, causes systematic variations in the background flux in phase with the roll angle, which has to be appropriately handled before the data are analysed.

AU Mic belongs to the most active stars, which are characterised by very frequent energetic flares and usually complex flares. All transit light curves were contaminated by more or less separated short flares, which could have been successfully removed before the fitting process with Allesfitter, described in Sect. 3.1. However, several transit light curves of both AU Mic b and AU Mic c were compromised by longlasting flare complexes that occurred very close to the transit or appeared during the transit. Their contamination deteriorated the transit shape so much they could not be reliably separated if the precision of the parameters from clearer transits was to be achieved. Therefore, we decided to remove these severely contaminated transits from the transit analysis. The CHEOPS light curves of the transits we selected for parameter fitting are shown in Fig. 1, and the transit light curves that we omitted because of severe flare contamination are plotted in Fig. A.1.

2.2. Pre-processing of the light curves

The CHEOPS light curves of AU Mic were corrected for roll-angle systematics using a parametric estimation derived from the data, with the photometric points phased by the roll angle. After we mased out the transits and the evident flares, the data were phased in the roll-angle domain. A further 2.5σ clipping was applied to exclude outliers such as potential flares and light-curve transients. The roll systematics model was a sixth-order Fourier polynomial, whose coefficients were determined by a least-squares fit to the phased out-of-transit points, and we then subtracted the derived parametric model from the entire dataset. The corrected data set was then used as input for the light-curve modeller.

This correction method was simpler than the non-parametric models we applied in our earlier work (e.g. Szabó et al. 2021) because the new-generation fitting algorithms can properly handle the flares and the high-order residuals of the rolling systematics that survived the subtraction of the Fourier polynomial. We

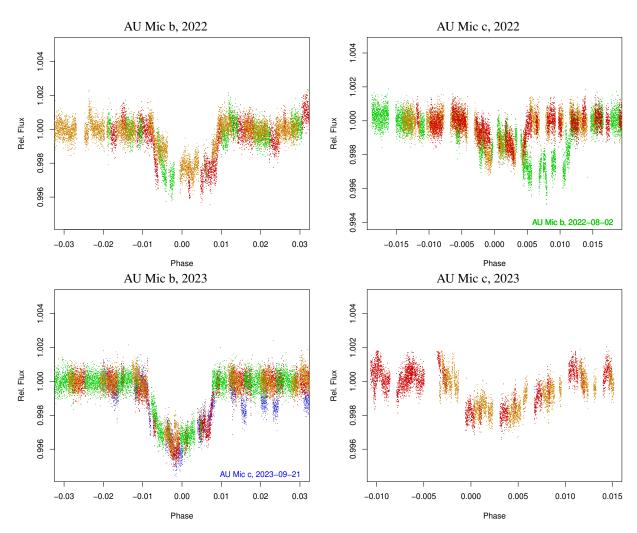


Fig. 1. Phased transit light curves of the 2022 and 2023 measurements of the AU Mic b (left panels) and c transits (right panels) after flare removal. The ephemeris and period used here are $T_{0,b} = 2\,458\,330.38416$ d and $P_b = 8.4631427$ d, and $T_{0,c} = 2459454.8973$ BJD, $P_c = 18.85882$ d. The TTV is very prominent for both planets compared to the earlier ephemeris. AU Mic b transited after the AU Mic c transit on 22 August 2022 (top right panel), and similarly, planet c transited after planet b on 21 September 2023 (bottom left panel).

achieved a more reliable estimate of the planet parameter uncertainties and a more robust handling of the data in general by letting the fitting procedure separate the various systematics in the light curve.

The flares of AU Mic are known to appear frequently, and their amplitude can well exceed the transit depth of the planets. Quite often, several flares merge into a flare complex with a timescale commensurable to the duration of the transits (Szabó et al. 2021, 2022). The flares can therefore introduce biases in the estimation of the baseline flux (which propagates to the transit parameters, most importantly, the transit depth), and if they appear during the transit, they can compress the transit depth and distort the shape of the light curve.

To filter out flares, manual removal was followed in our earlier publications (Szabó et al. 2021, 2022). In this current work, we changed this to a semi-automated process. First, light-curve segments that certainly had significant flares were marked by an artificial-intelligence application, which is the same process as for collecting the database of AU Mic flares for a dedicated analysis (see Kriskovics et al., in prep. for more details). The marked segments of the light curve were then removed. In the next step, we repeated the manual flare-removal process that we followed in our earlier publications, and we removed the low-amplitude

flares that were not identified by the AI algorithms, with the aim of filtering out all suspicious light curve parts and possible biases due to flares from the analysis. Figure 1 shows the phased transit light curves after the complete flare-filtering process, and this data set was the input for the light-curve analysis.

3. Data analysis

3.1. Refining the transit parameters

In order to derive orbital and planetary parameters of AU Mic b and c based on the CHEOPS photometry, we employed the Allesfitter¹ software package (Günther & Daylan 2019, 2021). This is a public software for modelling photometric and radial-velocity (RV) data. It can accommodate multiple exoplanets, multi-star systems, star spots, stellar flares, transit-time variations, and various noise models. It automatically runs a nested-sampling or Markov chain Monte Carlo fit. We opted for the nested-sampling fit with default settings. Several fundamental parameters were optimised during the fitting procedure, including the reference mid-transit time $T_{\rm c}$, the orbital period $P_{\rm orb}$, the

See https://www.allesfitter.com

Table 1. Overview of the Allesfitter priors and best-fitting parameters of AU Mic b and c obtained based on the data from 2022 and 2023.

Parameter [unit]	Prior	Value (2022)	Value (2023)
	Orbital and planetary parar	neters: AU Mic b	
$T_{\rm c}~[{\rm BJD_{TDB}}]$	$\mathcal{U}(2459769.0500, 2459769.2000)^{(1)}$	$2459769.12638 \pm 0.00035$	$2460149.95497^{+0.0012}_{-0.00086}$
	$\mathcal{U}(2460149.9000, 2460150.0500)^{(2)}$		
$P_{\rm orb}$ [d]	$\mathcal{N}(8.4631427, 0.0000005)^{(3)}$	$8.46314271 \pm 0.00000050$	$8.46314280^{+0.00000046}_{-0.00000051}$
$R_{\rm p}/R_{\rm s}$	U(0.01, 0.1)	$0.04700^{+0.00077}_{-0.00073}$	0.0517 ± 0.0011
$(R_{\rm p} + R_{\rm s})/a$	U(0.05, 0.06)	$0.0556^{+0.0016}_{-0.0013}$	$0.0578^{+0.0014}_{-0.0016}$
$\cos i$	$\mathcal{U}(0.0, 0.0349)$	$0.0154^{+0.0047}_{-0.0054}$	$0.0213^{+0.0035}_{-0.0045}$
	Orbital and planetary parar	meters: AU Mic c	
$T_{\rm c}~[{\rm BJD_{TDB}}]$	$\mathcal{U}(2459756.6000, 2459756.7500)^{(1)}$	$2459756.6677^{+0.0040}_{-0.0052}$	$2460133.8718^{+0.0096}_{-0.0074}$
	$\mathcal{U}(2460133.8000, 2460133.9500)^{(2)}$	0.0032	0.0071
$P_{\rm orb}$ [d]	$\mathcal{N}(18.85882, 0.00005)^{(3)}$	18.858819 ± 0.000049	$18.858827^{+0.000049}_{-0.000052}$
$R_{\rm p}/R_{\rm s}$	U(0.01, 0.1)	0.0354 ± 0.0016	$0.0309^{+0.0028}_{-0.0033}$
$(R_{\rm p}+R_{\rm s})/a$	$\mathcal{U}(0.030, 0.036)$	0.0338 ± 0.0011	$0.0336^{+0.0011}_{-0.0010}$
$\cos i$	$\mathcal{U}(0.0, 0.0349)$	$0.0200^{+0.0027}_{-0.0037}$	$0.0214^{+0.0033}_{-0.0074}$
	LD and GP para	meters	
q_1	$\mathcal{N}(0.5100, 0.1)$	0.485 ± 0.089	0.619 ± 0.085
q_2	$\mathcal{N}(0.2324, 0.1)$	0.279 ± 0.091	0.380 ± 0.092
$\log \sigma$ [log relative flux]	$\mathcal{U}(-10.0, -6.0)$	$-7.7085^{+0.0039}_{-0.0037}$	-7.7548 ± 0.0044
$\log S_0$	$\mathcal{U}(-25.0, -15.0)$	-21.05 ± 0.12	$-20.66^{+0.11}_{-0.11}$
$\log \omega_0 [\log d^{-1}]$	U(4.0, 8.0)	5.599 ± 0.051	5.898 ± 0.047

Notes. The additional priors were set as follows: $T_{\rm eff} = 3665 \pm 31 \text{ K}$, $R_{\rm s} = 0.82 \pm 0.02 \text{ R}_{\odot}$, and $M_{\rm s} = 0.60 \pm 0.04 \text{ M}_{\odot}$ (Donati et al. 2023). (1) The prior for the mid-transit time in 2022. (2) The prior for the mid-transit time in 2023. (3) Based on Szabó et al. (2022).

planet-to-star radius ratio R_p/R_s , the scaled sum of the fractional radii $(R_p + R_s)/a$, and the cosine of the orbit inclination angle (cos i). The quadratic limb-darkening (LD) law was applied during the fitting procedure. The u_1 and u_2 LD coefficients were first linearly interpolated based on the stellar parameters of $T_{\text{eff}} = 3665 \pm 31 \text{ K}$ and $\log g = 4.52 \pm 0.05 \text{ [cgs]}$ found by Donati et al. (2023). We used the tables of coefficients calculated for the CHEOPS passband using the PHOENIX-COND models by Claret (2021). We then converted these LD coefficients into q_1 and q_2 (Kipping 2013). The q_1 and q_2 parameters were fitted during the procedure. In order to model the flux baseline, we applied a Gaussian process (GP) regression method using the SHOTerm (simple harmonic oscillator – SHO) plus JitterTerm kernel, implemented in the Celerite² (Kallinger et al. 2014; Foreman-Mackey et al. 2017; Barros et al. 2020) package, with a fixed quality factor of $Q_0 = 1/\sqrt{2}$, as is common for quasi-periodic stellar variability. The regression was made by using $\log \omega_0$ and $\log S_0$ with bounds on the values of these parameters to be input by the user. The parameter $\log \omega_0$ reflects the frequency (period), and $\log S_0$ reflects the scaled power (amplitude) of the signal. The instrumental noise in the CHEOPS data was sampled using the $\log \sigma$ parameter. We assumed a circular orbit of AU Mic b and c.

During the analysis with Allesfitter, we followed the strategy described below. We simultaneously fitted all AU Mic b and c transits per observing year, that is, the transits from 2022 and 2023 were fitted separately. The main reason for splitting the data into two groups was the possibility of comparing the evolution of the transit parameters of the planets. In most cases, we applied broad uniform priors on the parameters. The applied

3.2. TTV analysis

The O-C diagrams of the transit mid-time for AU Mic b and c are shown in Fig. 3. Observations from previous years are complemented with CHEOPS data from the 2022 and 2023 observation periods. Both planets showed large-amplitude TTVs, and planet c deviated significantly from those of previous years. The difference between the mid-transit times reached ~90 minutes. Tables 3 and 4 show the exact mid-transit times and O-C values for planets b and c, respectively. Based on $T_c = 2458330.38416$ d and $P_{\text{mean}} = 8.4631427$ d for planet b and $T_c = 2459454.8973$ and $P_{\text{mean}} = 18.85882$ d for planet c. The superperiod of the TTVs exhibited by planet b (according to the fit in Fig. 3) is 1150 days, which is slightly shorter than reported in Szabó et al. (2022). The reason is the longer dataset that is now available (almost 1.5 superperiods) than was the case of the analysis in Szabó et al. (2022) (less than one superperiod), and the pattern is better defined. The peak-to-peak TTV amplitude of the best-fit periodic TTV model to AU Mic b is 24.5 minutes, which agrees well with the predictions in Szabó et al. (2022). The presence of a third planet, AU Mic d, has been suggested by Wittrock et al. (2023) based on TTV signals. In order to test this possibility, we conducted dynamical simulations assuming a third planet in the system.

We used TRADES³ (Borsato et al. 2014, 2019, 2021), a Fortran90-Python software, to model four configurations of

priors and the fitted parameters are listed in Table 1 and the derived parameters are listed in Table 2. The corresponding transit light curves, overplotted with the best-fitting Allesfitter models, are shown in Fig. 2.

² See https://celerite.readthedocs.io/en/stable

³ https://github.com/lucaborsato/trades

Table 2. Overview of the Allesfitter-derived parameters of AU Mic b and c obtained based on the data from 2022 and 2023.

Parameter [unit]	Value (2022)	Value (2023)
Orbital a	nd planetary parameters:	AU Mic b
$R_{\rm s}/a$	$0.0531^{+0.0016}_{-0.0013}$	$0.0550^{+0.0013}_{-0.0015}$
$a/R_{\rm s}$	$18.83^{+0.47}_{-0.54}$	$18.18^{+0.51}_{-0.42}$
$R_{\rm p}/a$	$0.002497^{+0.000094}_{-0.000083}$	$0.002843^{+0.000098}_{-0.00011}$
$R_{\rm p} \ [{ m R}_{\oplus}]$	4.20 ± 0.12	4.62 ± 0.15
$R_{\rm p} \left[{\rm R}_{\rm Jup} \right]$	0.375 ± 0.011	0.412 ± 0.013
$a[R_{\odot}]$	15.42 ± 0.56	$14.92^{+0.55}_{-0.49}$
<i>a</i> [au]	0.0717 ± 0.0026	$0.0694^{+0.0025}_{-0.0023}$
i [deg]	$89.12^{+0.31}_{-0.27}$	$88.78^{+0.26}_{-0.20}$
b	$0.290^{+0.077}_{-0.098}$	$0.386^{+0.057}_{-0.074}$
$T_{14}^{(\star)}[h]$	$3.457^{+0.021}_{-0.019}$	$3.480^{+0.048}_{-0.062}$
$T_{23}^{(\star\star)}$ [h]	$3.118^{+0.021}_{-0.022}$	$3.084^{+0.056}_{-0.074}$
$T_{\rm eq}^{\diamond}$ [K]	$546.4^{+8.9}_{-8.1}$	555.7 ^{+7.9} _{-8.6}
$T_{\rm d}^{(\ddagger)}$ [relative flux]	0.002633 ± 0.000088	0.00330 ± 0.00011
Orbital a	nd planetary parameters:	AU Mic c
D /	* . *. *.	0.02260+0.0010

Orbital aı	nd planetary parameters:	AU Mic c
$R_{\rm s}/a$	$0.0326^{+0.0011}_{-0.0010}$	$0.03260^{+0.0010}_{-0.00098}$
$a/R_{\rm s}$	30.7 ± 1.0	30.68 ± 0.96
$R_{\rm p}/a$	0.001155 ± 0.000069	$0.00100^{+0.00010}_{-0.00011}$
$R_{\rm p} [{\rm R}_{\oplus}]$	3.17 ± 0.16	$2.76^{+0.26}_{-0.29}$
$R_{\rm p} \left[{\rm R}_{\rm Jup} \right]$	0.283 ± 0.014	$0.246^{+0.023}_{-0.026}$
$a [R_{\odot}]$	25.14 ± 1.0	25.14 ± 1.0
<i>a</i> [au]	0.1169 ± 0.0047	0.1169 ± 0.0047
$i [\deg]$	$88.85^{+0.21}_{-0.16}$	$88.78^{+0.43}_{-0.19}$
b	$0.615^{+0.074}_{-0.11}$	$0.658^{+0.093}_{-0.23}$
$T_{14}^{(\star)}$ [h]	$3.90^{+0.31}_{-0.25}$	$3.73^{+0.64}_{-0.40}$
$T_{23}^{(\star\star)}$ [h]	$3.48^{+0.36}_{-0.30}$	$3.34^{+0.74}_{-0.48}$
$T_{\text{eq}}^{(\circ)}$ [K] $T_{\text{d}}^{(\ddagger)}$ [relative flux]	428.0 ± 7.8	428.0 ± 7.8
$T_{\rm d}^{(\ddagger)}$ [relative flux]	0.001376 ± 0.000087	$0.00104^{+0.00012}_{-0.00014}$
	Stellar parameters	

d [relative max]	0.001270 ± 0.000007	0.00101-0.00012
	Stellar parameters	
u_1	0.39 ± 0.13	0.60 ± 0.15
u_2	$0.30^{+0.14}_{-0.13}$	0.19 ± 0.14
$\rho_{\rm s}$ [g cm ⁻³]	1.65 ± 0.19	$1.56^{+0.14}_{-0.12}$

Notes. (*)Total transit duration between first and fourth contact. (**)Full transit duration between second and third contact. (*)Assuming an albedo of 0.3 and uniform heat redistribution. (‡)Transit depth.

the AU Mic system. In the initial configuration (1), we focused exclusively on the system comprising the two transiting planets, b and c, and only modelled the transit times during the orbital integration. In the subsequent two configurations (2) and (3), we additionally incorporated planet d (Wittrock et al. 2023), and as for (1), we only modelled the transit times of b and c. Only in the fourth configuration (4) did we also include the SERVAL RVs from Zicher et al. (2022). Another difference between the four configurations is the parameters that were fitted in the analysis. Generally, we set the stellar mass from Plavchan et al. (2020), and fitted (as in Nascimbeni et al. 2023) for the planet-to-star mass ratios (M_p/M_{\star}) , the periods (P), the eccentricities (e) and argument of pericenters (ω) in the form $\sqrt{e}\cos\omega$, $\sqrt{e}\sin\omega$, and the mean longitude (λ^4) for all the planets. We fitted the

longitude of the ascending node (Ω) of planet c in all four configurations, and of d in configurations (2), (3), and (4). The inclination (i) of planet c in configurations (3), (4) and of d in (2), (3), and (4) was fitted as well. In configuration (4) we also fitted for an RV offset (γ) and a jitter term (in log₂). The RV data are characterised by strong activity; but by default, TRADES does not implement an activity model. Because the problem is so complex, we decided not to test it. The total numbers of fitted parameters were 11, 18, 19, and 21 for configurations (1), (2), (3), and (4), respectively. All parameters were defined at the reference time BJD_{TDB} – 2450000 = 8329. All priors on the parameters are listed in Table B.1 The parameters of b and c were set to the values in Table 2, and Ω_b was set to 180° (assuming the same reference system as in Winn 2010 and adopted in Borsato et al. 2014).

For each configuration, we first performed a run of TRADES with PyDE (Parviainen et al. 2016) allowing for 200 000 steps and used the best-fit configuration set as a starting point for EMCEE (Foreman-Mackey et al. 2013). Then we ran EMCEE for 1 000 000 steps (with a conservative thinning factor of 100). For each configuration, we used as walkers for EMCEE the same number of parameter sets as used in PYDE, 100 for configurations (1), (2), and (3), and 200⁵ for (4). Within EMCEE we used a 80% ÷ 20% combination of the differential evolution (Nelson et al. 2014) and snooker (ter Braak & Vrugt 2008) proposal samplers. After we confirmed that the chains converged through visual inspection, auto-correlation function (ACF), Gelman-Rubin statistics (Gelman & Rubin 1992), and the Geweke criterion (Geweke 1991), we discarded the first 350 000, 500 000, 600 000, and 800 000 steps as burn-in for configurations (1), (2), (3), and (4), respectively.

We computed the high-density interval (HDI) at 68.27% as the 1σ equivalent for each fitted and physical parameter of the posterior distribution. We defined the maximum-a-posteriori (MAP) configuration set as the best-fit parameter, that is, the set of parameters that maximised the log-probability $^6 \ln \mathcal{P}$, whose parameters were completely within all fitted 1σ HDI. The best-fit solution with 100 random samples drawn from the 1σ posterior distribution is shown in Figs. B.1, B.2, B.3, and B.4 with the O-C plots for planets b and c for all four configurations, and the RV model in Fig. B.5 for configuration (4).

4. Results and discussion

4.1. Fundamental planetary parameters

In Tables 5 and 6, we compare the fundamental transit parameters observed between 2018 and 2023, taken from this paper and from five earlier analyses in the literature. Here, Plavchan et al. (2020) contains the analysis of 2018 TESS data, Gilbert et al. (2022) and Martioli et al. (2021) are based on the combined TESS 2018–2020 data, and Szabó et al. (2021) and Szabó et al. (2022) are based on the CHEOPS observations from 2020 and 2021, respectively. We sorted the table columns according to the time of observation; and therefore, moving from left to right, the columns show the measurements in a decreasing order of the time of the observations.

Most parameters are consistent within the uncertainties, with the important exceptions of R_p/R_s and b for planet b. In the

⁴ The mean longitude is defined as $\lambda + \mathcal{M} + \omega + \Omega$, where \mathcal{M} is the mean anomaly and Ω is the longitude of the ascending node.

⁵ We doubled the number of parameter sets/walkers due to the increased number of fitting parameters and the availability of a much more performing server.

 $^{^6}$ In case of all uniform-uninformative priors, the log-probability $\ln\mathcal{P}$ is equal to the log-likelihood $\ln\mathcal{L}.$

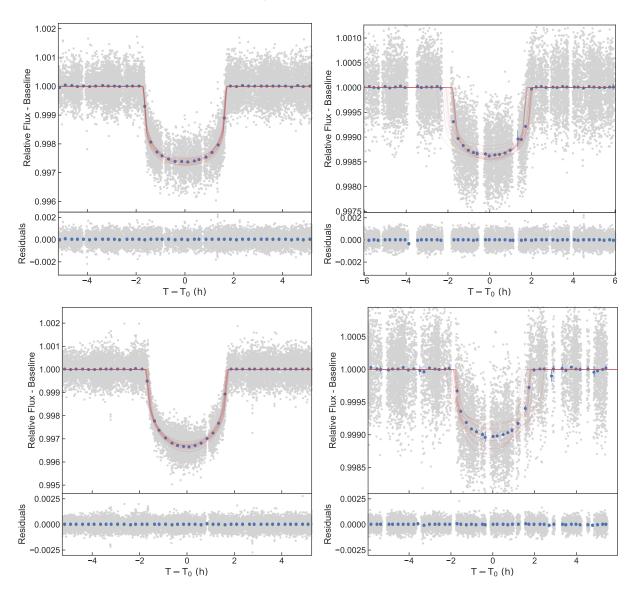


Fig. 2. Stacked and binned CHEOPS transit light curves of AU Mic b (left panels) and AU Mic c (right panels) from 2022 (top panels) and from 2023 (bottom panels), overplotted with the best-fitting Allesfitter models (20 curves from random posterior samples). The residuals are also shown.

case of AU Mic b, the R_p/R_s parameter was found to be smaller in 2022 than in 2023 (0.0470 versus 0.0517). The transit depth in 2022 was slightly larger than what we observed in 2021 (0.0433 \pm 0.001, Szabó et al. 2022), while it was determined to be in the interval of 0.0512-0.0531 in 2018 and 2020 (Szabó et al. 2022), which is compatible to the transit depth parameter that we observed in 2023. The transit depth parameters of AU Mic c are comparable to each other, with a slight decrease in the 2023 value.

The impact parameter *b* has an average value of 0.22 in the case of AU Mic b, but since the 2023 CHEOPS data and 2020 CHEOPS data are two outliers (with values of 0.386 and 0.09, respectively), the dataset is barely consistent. The values for the impact parameter of AU Mic c are consistent within the uncertainties, but appear to be slightly higher in the case of the more recent CHEOPS data.

We followed the working hypothesis that the main reason for the varying transit parameters of the two planets can be the actual realisation of the spot distribution on the surface and their biases on the transit shape (Szabó et al. 2021). This is also corroborated by the observation that CHEOPS measurements seem to be more strongly biased (more year-to-year variations) than the TESS measurements, and CHEOPS is bluer and more sensitive to inhomogeneities in the surface temperature. Therefore, assuming a common reason behind the biases and expecting similarities (correlation, anti-correlation, at least in part) in the actual values of the parameters, we tested a possible correlation between the transit depth and the impact parameters of AU Mic b and c, and also possible correlations between the same parameter (R_p/R_s) and impact parameter of the two planets in comparison). We calculated Pearson's correlation coefficient (testing linear dependence) and Spearman's rank correlation coefficient (testing any monotonic dependence). We found no significant correlation (a coefficient value of zero was always within the error interval, and we also observed p > 0.1 in all cases). However, the lack of a significant correlations does not rule out activity as a reason for the observed biases of the parameters, but is instead a result of the low number statistics, which is still not enough for a conclusive result. This will be better determined in the future when AU Mic has been observed for more years.

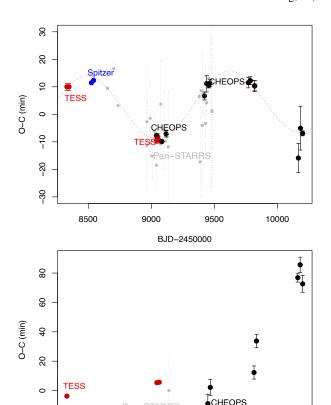


Fig. 3. TTV diagrams of AU Mic b (upper panel) calculated with $T_c = 2458\,330.38416$ and $P_{\rm mean} = 8.4631427$ d, and AU Mic c (lower panel) calculated with $T_c = 2459\,454.8973$ and $P_{\rm mean} = 18.85882$ d. We included Transiting Exoplanet Survey Satellite (TESS, red symbols), Spitzer (blue symbols), Earth-based Pan-STARRS (light grey symbols) and CHEOPS (black symbols) measurements. The harmonic fit to AU Mic b data (dotted red line) illustrates the most probable shape of a periodic TTV fitted to the data. This is shown to illustrate the trend of the distribution without any dynamical interpretation.

BJD-2450000

9000

9500

10000

Ŗ

8500

The observed instability of the transit parameters on a timescale of years confirms our observation that the transit parameter depends significantly on the actual spot pattern on the stellar disk, which is reproducible (we see similar biases for transits that repeat at similar stellar rotational longitudes; Szabó et al. 2021). This proves that in case of AU Mic, the transit depth parameter is not exclusively characteristic of the planet itself, but the actual spot distribution causes bias the observed value. (Hence, calling it the "transit depth parameter" is more accurate because it is an R_p/R_s value, but biased by the actual spot distribution).

4.2. Possible solutions for AU Mic d and concluding remarks

The parameters of the planets in the AU Mic system based on the dynamical analysis are shown in Table B.1. Configuration (1), in which only two planets, b and c, were assumed, is unable to explain the observed TTVs, as shown in Fig. B.1 and in the first column of Table B.1. We found that in accordance with Wittrock et al. (2023), the TTVs exhibited by planets b and c can be explained by the presence of an additional third planetary body in the system on an orbit that falls between the orbits of the two transiting planets. It is worth noting, however, that the shapes

Table 3. Observed mid-transit times and O - C values of AU Mic b based on TESS, Spitzer, and CHEOPS observations.

Designation	Transit time [BJD-2450000]	<i>O</i> – <i>C</i> [min]	Err [min]
TESS S1#1 (a)	8330.3911±0.0009	10.00	1.33
TESS S1#2 (a)	8347.3174±0.0009	10.02	1.33
Spitzer#1 (b)	8525.04509 ± 0.0010	12.45	1.43
TESS S27#1 (a)	9041.2816±0.0008	-9.42	1.17
TESS S27#2 (a)	9049.7457±0.0008	-8.05	1.17
TESS S27#3 (a)	9058.2080±0.0008	-9.40	1.17
CHEOPS 20-07-10 (a)	9041.2828±0.0006	-7.70	0.87
CHEOPS 20-08-21 (a)	9083.5970±0.0004	-9.88	0.58
CHEOPS 20-09-24 (a)	9117.4515±0.0008	-7.08	1.17
CHEOPS 21-07-26 (c)	9422.1342±0.0010	8.40	1.43
CHEOPS 21-08-12 (c)	9439.0636±0.0021	9.55	3.15
CHEOPS 21-08-29 (c)	9455.9895±0.0007	10.65	1.0
CHEOPS 21-09-06 (c)	9464.4531±0.0009	11.25	1.27
CHEOPS 22-08-08 (d)	9769.1264±0.0013	11.49	1.9
CHEOPS 22-08-25 (d)	9786.0532±0.0013	12.23	1.9
CHEOPS 22-08-28 (d)	9819.9045±0.0013	10.26	1.9
CHEOPS 23-08-10 (d)	10166.8751 ± 0.0037	-15.88	5.2
CHEOPS 23-08-27 (d)	10183.8089 ± 0.0055	-5.06	7.9
CHEOPS 23-09-13 (d)	10200.7339 ± 0.0064	-6.91	9.2

Notes. $T_c = 2458330.38416 \,\mathrm{d}$ and $P_{\mathrm{mean}} = 8.4631427 \,\mathrm{d}$ were used to determine O–C values. The references for the transit times are ^(a)Szabó et al. (2021), ^(b)Plavchan et al. (2020), ^(c)Szabó et al. (2022), ^(d)This research.

Table 4. Observed mid-transit times and O - C values of AUMic c based on TESS and CHEOPS observations.

Designation	Transit time [BJD-2450000]	O-C [min]	Err [min]
TESS S1#1 (a)	8342.22432±0.0004	-3.75	0.71
TESS S27#1 (a)	9040.00697±0.0005	5.34	0.88
TESS S27#2 (a)	9058.86596±0.0006	5.58	0.98
CHEOPS 21-08-09 (b)	9436.0323±0.0045	-8.90	6.48
CHEOPS 21-08-28 (b)	9454.8988±0.0050	2.16	5.47
CHEOPS 22-08-02 (c)	9794.3646±0.0032	12.30	4.7
CHEOPS 22-08-21 (c)	9813.2383±0.0031	33.72	4.6
CHEOPS 23-07-08 (c)	10133.8682±0.0028	76.87	4.0
CHEOPS 23-07-27 (c)	10152.7331±0.0036	85.62	5.2

Notes. $T_c = 2459454.8973 \,\mathrm{d}$ and $P_{\mathrm{mean}} = 18.85882 \,\mathrm{d}$ were used to determine O - C values. The references for the transit times are ^(a)Gilbert et al. (2022), ^(b)Szabó et al. (2022), ^(c)This research.

and amplitudes of the fitted TTV signals of planets b and c differed significantly in the remaining three configurations, where a third perturbing body was always assumed. This resulted in differences between the derived parameters from configurations (2), (3), and (4). Since the BIC value was lowest for configuration (2), it was treated as the main solution. Therefore, our discussion continues with the parameters of configuration (2), which are shown in the second column of Table B.1. We found the orbital period of planet d to be around 12.6 days, which is compatible with the 12.6–12.7 -day AU Mic d solutions of Wittrock et al. (2023), and most importantly, narrows the possible AU Mic d

Table 5. Best-fitting parameters of AU Mic b compared to results from previous works.

	2023(*)	2022(*)	2021(**)	2020(*)	2018-2020(‡)	2018-2020(*)	2018(•)
R_p/R_{\star}	0.0517 ± 0.00011	$0.04700^{+0.00077}_{-0.00073}$	0.0433 ± 0.0017	0.0531 ± 0.0023	0.0512 ± 0.0020	$0.0526^{+0.0003}_{-0.0002}$	0.0514 ± 0.0013
a/R_{\star}	$18.18^{+0.51}_{-0.42}$	$18.83^{+0.47}_{-0.54}$	18.95 ± 0.35	19.24 ± 0.37	19.07	$19.1^{+0.2}_{-0.4}$	$19.1^{+1.8}_{-1.6}$
$R_p [R_{\oplus}]$	4.62 ± 0.15	4.20 ± 0.12	3.55 ± 0.13	4.36 ± 0.18	4.27 ± 0.17	4.07 ± 0.17	4.29 ± 0.20
a [AU]	$0.0694^{+0.0025}_{-0.0023}$	0.0717 ± 0.0026	0.0654 ± 0.0012	0.0678 ± 0.0013	$0.0644^{+0.0056}_{-0.0054}$	0.0645 ± 0.0013	$0.066^{+0.007}_{-0.006}$
b	$0.386^{+0.057}_{-0.074}$	$0.290^{+0.077}_{-0.098}$	0.17 ± 0.11	0.09 ± 0.05	$0.26^{+0.13}_{-0.17}$	0.18 ± 0.11	$0.16^{+0.14}_{-0.11}$

Notes. The parameters are compared to the results of Plavchan et al. (2020, P2020), Martioli et al. (2021, M2021), Szabó et al. (2022, Sz2021), Gilbert et al. (2022, G2022), and Szabó et al. (2022, Sz2022). (*)This work, (**)Sz2022, (*)Sz2021, (*)G2022, (*)M2021, (*)P2020.

Table 6. Best-fitting parameters of AU Mic c compared to the results of M2021, G2022, and Sz2022.

	2023 ^(*)	2022 ^(*)	2021 ^(**)	$2018-2020^{(\ddagger)}$	2018-2020(*)
$R_{\rm p}/R_{\star}$	$0.0309^{+0.0028}_{-0.0033}$	0.0354 ± 0.0016	0.0313 ± 0.0016	$0.0340^{+0.0033}_{-0.0034}$	0.0395 ± 0.0011
a/R_{\star}	30.68 ± 0.96	30.7 ± 1.0	28.8 ± 2.4	$31.7_{2.6}^{+2.7}$	29 ± 3.0
$R_{\rm p} [{\rm R}_{\oplus}]$	$2.76^{+0.26}_{-0.29}$	3.17 ± 0.16	2.56 ± 0.12	$2.79^{+0.31}_{-0.30}$	3.24 ± 0.16
a [AU]	0.1169 ± 0.0047	0.1169 ± 0.0047	0.0993 ± 0.0085	$0.110^{+0.010}_{-0.010}$	0.1101 ± 0.0022
b	$0.658^{+0.093}_{-0.23}$	$0.615^{+0.074}_{-0.11}$	0.58 ± 0.13	$0.30^{+0.21}_{-0.20}$	0.51 ± 0.21

Notes. (*)This work, (**)Sz2022, (‡)G2022, (*)M2021.

solutions to the class of middle AU Mic d models, that is, planet d is between the orbits of planets b and c. The mass of this third perturbing body is expected to be far lower than that of planets c or b, around $0.1M_{\oplus}$, which suggests that it falls into the category of rocky exoplanets. The sub-Earth mass agrees with the result of Wittrock et al. (2023) (with values of about 0.5 and 1.0 M_{\oplus} for the 12.6 d and 12.7 d solutions, respectively), but our mass parameter is still below these determinations and is about two Mars masses.

The derived planetary masses for planets b and c in the different configurations differed significantly. While the mass of planet b in configuration (2) is higher than other published values, the mass of planet c is significantly lower than the masses provided in previous works. Although the latter is compatible with Martioli et al. (2021), the estimated 4.4 M_{\odot} for AU Mic c disagrees with the values provided by Cale et al. (2021); Zicher et al. (2022), or Donati et al. (2023). On the other hand, configuration (3), whose BIC value was only slightly lower, resulted in completely different planetary masses, to the point that in this case, AU Mic c had the higher mass. This configuration agrees with Zicher et al. (2022); Donati et al. (2023), and most recently, Mallorquín et al. (2024). This type of discrepancy between the masses of b and c is not new; the derived planetary masses in previous studies also contradicted each other (e.g. Cale et al. 2021 and Zicher et al. 2022). However, an activity model was not incorporated in our dynamical analysis, which may explain the difference from the published values. Moreover, the orbital configurations may further contribute to the discrepancies between the estimated values of the planetary masses.

In order to gain further insight into the geometry of the system, we calculated the angle between the rotational axis of the star and the normal of the transit chord of the planet, λ_{RM} , such that $\lambda_{RM}=0^\circ$ if the orbital motion is prograde and the orbit of the planet is aligned with the stellar equator, and $\lambda_{RM}=90^\circ$ and 270° for a prograde and retrograde polar orbit, respectively. The λ_{RM} for each transit was calculated based on the parameters from the dynamical analysis, such that a planet with $\Omega=180^\circ$ and

 $i=90^\circ$ corresponded to an aligned orbit ($\lambda_{RM}=0^\circ$). The evolution of the λ_{RM} in time due to the interactions between the planets is shown in Fig. B.6. The resulting orbit for planet b shows an aligned system with a mean value of $\lambda_{RM}=0.02^\circ$. Planet c, on the other hand, exhibited a misaligned orbital geometry with a mean value of $\lambda_{RM}=171.91^\circ$, suggesting that planet c is significantly misaligned and presumably has a retrograde orbit. In agreement with our research, recent results based on Rossiter-McLaughlin measurements also suggest a misaligned orbit of AU Mic c (Yu et al. 2025).

The value for Ω of AU Mic c and planet d differs by $225^{\circ}.$ This suggests that the orbital geometry of AU Mic d does not allow observable transits. Moreover, the inferred low mass (in Wittrock et al. 2023 and this work) suggests a small radius and that the individual AU Mic d transits would not be detectable by the currently working exoplanet telescopes (TESS and CHEOPS) because the transit depth is shallow.

The above dynamical analysis is based on a limited number of epochs (AU Mic years), distributed to 5–5 self-consistent groups of transits, and the fit has 12 derived parameters, which exceeds the number of transits currently available for AU Mic c. The current best-fit results mostly show the preferred parameter space of possible AU Mic d solutions rather than their exact quantitative values. We conclude that more data are needed to constrain the planetary parameters of planet d better. Several future AU Mic visits are expected by CHEOPS (at least until 2026) and TESS (at least one sector in August 2025), with additional targeted JWST and Earth-based observations. The orbit solutions will be upgraded in the close future, and we expect to see a convergence for the possible AU Mic d solution in a few years.

Data availability

This research made use of observations of AU Mic carried out with the CHEOPS telescope in 2022 and 2023. The full list of CHEOPS observations from the 2022–2023 campaign

can be reached here along with the start and end date of each observation.

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Appendix A: Observations of AU Mic with CHEOPS

Transits shown in Fig. A.1 were omitted from the analysis, due to the significant flaring activity of the host star during the planetary transits.

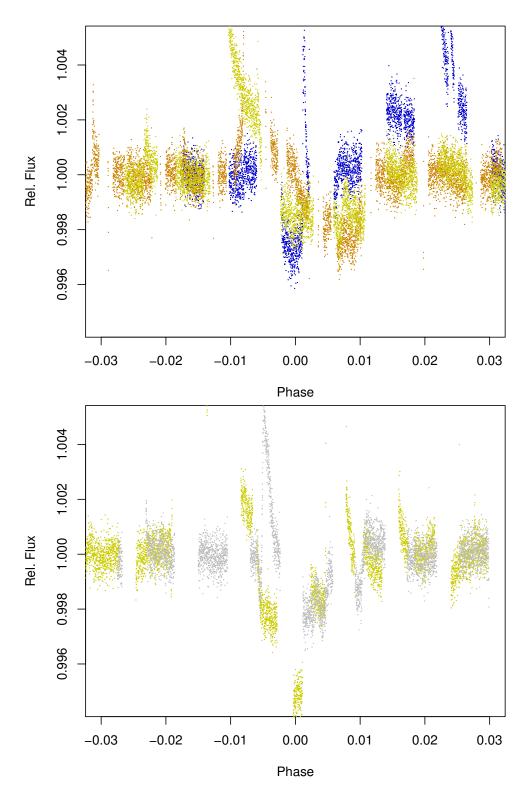


Fig. A.1. Light curves of AU Mic b in 2022 (upper panel) and 2023 (lower panel) that were omitted from parameter fitting due to flare complexes during the transits.

Appendix B: Dynamical analyses

Summary of the results of the four dynamical analyses with TRADES. Priors and MAP best-fit solution for each configuration are listed in Table B.1. Observed-Calculated diagrams of the MAP dynamical solution are shown in Fig. B.1, B.2, B.3, and B.4 for configurations (1), (2), (3) and (4), respectively. In Fig. B.5 the RV model from the MAP for the TRADES configuration (4) is shown. Figure B.6 shows the evolution of the projected spin-orbit misalignment (λ_{RM}) of the configuration (2) at synthetic and observed transit times of planet b and c, respectively.

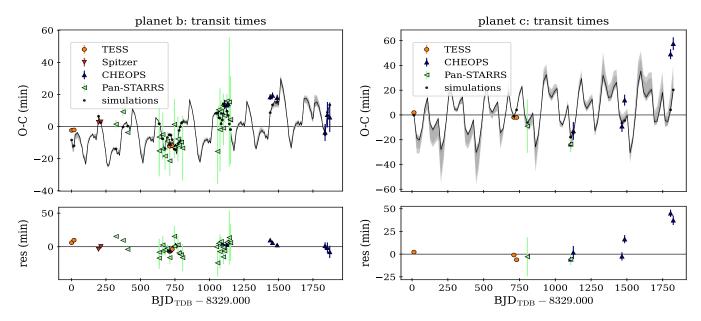


Fig. B.1. TRADES modelling of AU Mic b (left panels) and AU Mic c (right panels) of configuration (1). Top panel: (O-C) diagram, observed T_0 s are plotted with coloured markers with black stroke (different colour and marker for each telescope), while the simulated O-C values computed by the best-fit TRADES dynamical model are plotted as black line with black circles (corresponding to the observations). Grey-shaded areas correspond to 1, 2, and 3σ of random samples drawn from the posterior distribution of TRADES. Bottom panel: Residuals computed as the difference between observed and simulated T_0 s.

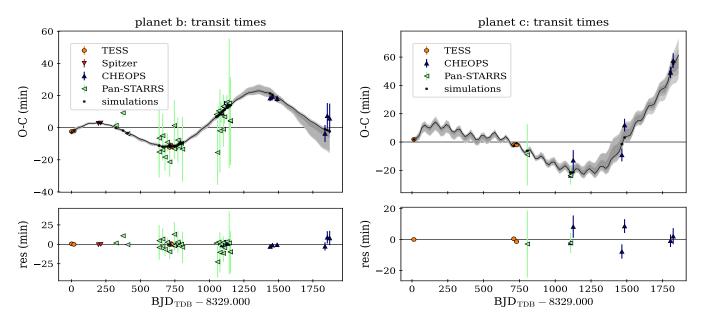


Fig. B.2. TRADES modelling of AU Mic b (left panels) and AU Mic c (right panels) of configuration (2). See Fig. B.1 for a description.

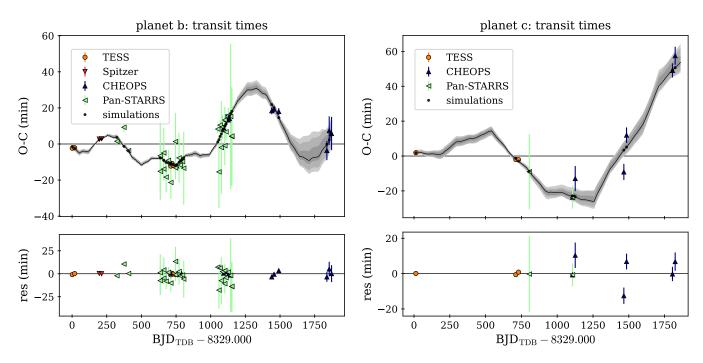


Fig. B.3. TRADES modelling of AU Mic b (left panels) and AU Mic c (right panels) of configuration (3). See Fig. B.1 for a description.

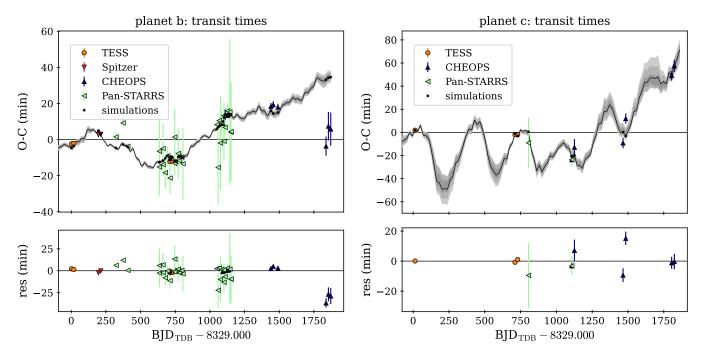


Fig. B.4. TRADES modelling of AU Mic b (left panels) and AU Mic c (right panels) of the configuration (4). See Fig. B.1 for a description.

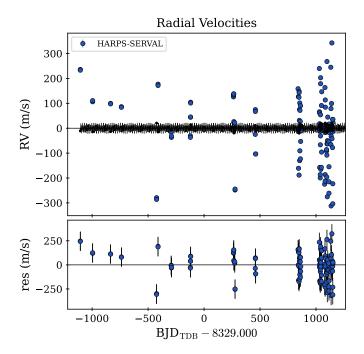


Fig. B.5. TRADES RV modelling of AU Mic system of the configuration (4). Black error bars in the lower panel (residuals) take into account the RV jitter term summed in quadrature to the observed uncertainty.

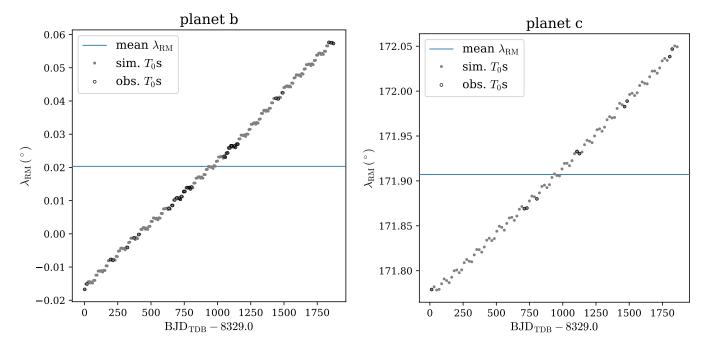


Fig. B.6. Projected spin-orbit misalignment (λ_{Rm}) evolution computed at simulated transit during TRADES modelling of AU Mic b (left panels) and AU Mic c (right panels) of configuration (2). Gray circles are all the synthetic transit times, highlighted as black-open circle the corresponding observed transit times. The horizontal-blue line is the mean value of λ_{Rm} .

Table B.1. Posterior and derived parameters of the AU Mic system from the four dynamical analyses with TRADES.

configuration	D	<u> </u>	(2)		٣	(3)	(4)	
planets	b,	b, c	b, c, d	p,	b, 0	b, c, d	b, c, d	p
	i _c fixed,	i _c fixed, no RV	i _c fixed, no RV	no RV	i _c fitted	ic fitted, no RV	ic fitted, with RV	ith RV
Parameter (unit)	Prior	MAP (HDI)	Prior	MAP (HDI)	Prior	MAP (HDI)	Prior	MAP (HDI)
fitted parameters								
$M_{\rm b}/M_{\star}~(M_{\odot}/M_{\star})\times 10^{-6}$	$\mathcal{U}(0.057, 319.520)$	110^{+6}_{-4}	$\mathcal{U}(0.057, 319.520)$	159^{+9}_{-10}	$\mathcal{U}(0.057, 319.520)$	28+3	$\mathcal{U}(0.057, 319.520)$	187^{+16}_{-15}
$P_{\rm b}$ (days)	$\mathcal{U}(8.3, 8.6)$	$8.461705^{+0.000016}_{-0.000099}$	$\mathcal{U}(8.3, 8.6)$	$8.463364_{-0.000031}^{+0.000017}$	$\mathcal{U}(8.3, 8.6)$	$8.462697^{+0.000037}_{-0.000035}$	$\mathcal{U}(8.3, 8.6)$	$8.463067^{+0.000053}_{-0.000084}$
$\sqrt{e}\cos\omega_{\mathrm{b}}$	$\mathcal{U}(-0.71, 0.71)$	$0.5429^{+0.0098}_{-0.0206}$	$\mathcal{U}(-0.71, 0.71)$	$0.120^{+0.027}_{-0.028}$	$\mathcal{U}(-0.71, 0.71)$	$0.05568_{-0.05032}^{+0.00096}$	$\mathcal{U}(-0.71, 0.71)$	$-0.027^{+0.011}_{-0.020}$
$\sqrt{e}\sin\omega_{ m b}$	$\mathcal{U}(-0.71, 0.71)$	$0.452^{+0.014}_{-0.023}$	$\mathcal{U}(-0.71, 0.71)$	$0.5369^{+0.0259}_{-0.0028}$	$\mathcal{U}(-0.71, 0.71)$	$-0.30225^{+0.00069}_{-0.01469}$	$\mathcal{U}(-0.71, 0.71)$	$0.060^{+0.032}_{-0.025}$
$\lambda_{\mathrm{b}}\left(^{\circ}\right)$	$\mathcal{U}(0, 360)$	$176.66^{+1.75}_{-0.70}$	$u_{(0,360)}$	205^{+1}_{-2}	$\mathcal{U}(0, 360)$	208.69+1.81	$u_{(0,360)}$	$211.094^{+0.178}_{-0.084}$
$M_{\rm c}/M_{\star}(M_{\odot}/M_{\star})\times 10^{-6}$	$\mathcal{U}(0.057, 319.520)$	127^{+2}_{-6}	$\mathcal{U}(0.057, 319.520)$	26^{+7}_{-1}	$\mathcal{U}(0.057, 319.520)$	86+8	$\mathcal{U}(0.057, 319.520)$	86+8
$P_{\rm c}$ (days)	$\mathcal{U}(18.6, 19.0)$	$18.859052^{+0.000432}_{-0.000013}$	$\mathcal{U}(18.6, 19.0)$	$18.86404^{+0.00135}_{-0.00014}$	$\mathcal{U}(18.6, 19.0)$	$18.859167^{+0.000101}_{-0.000077}$	$\mathcal{U}(18.6, 19.0)$	$18.85263^{+0.00063}_{-0.00057}$
$\sqrt{e}\cos\omega_{\mathrm{c}}$	$\mathcal{U}(-0.71, 0.71)$	$0.1608^{+0.0043}_{-0.0074}$	$\mathcal{U}(-0.71, 0.71)$	$0.012^{+0.012}_{-0.016}$	$\mathcal{U}(-0.71, 0.71)$	$0.0230^{+0.0250}_{-0.0028}$	$\mathcal{U}(-0.71, 0.71)$	$-0.049^{+0.016}_{-0.018}$
$\sqrt{e}\sin\omega_{\mathrm{c}}$	$\mathcal{U}(-0.71, 0.71)$	$-0.4473^{+0.0039}_{-0.0129}$	$\mathcal{U}(-0.71, 0.71)$	$0.0510^{+0.0035}_{-0.0587}$	$\mathcal{U}(-0.71, 0.71)$	$-0.0548^{+0.0076}_{-0.0246}$	$\mathcal{U}(-0.71, 0.71)$	$-0.142^{+0.023}_{-0.017}$
λ _c (°)	$\mathcal{U}(0, 360)$	$202.46^{+1.17}_{-0.31}$	$u_{(0,360)}$	189+4	U(0, 360)	$155.51^{+0.57}_{-2.29}$	$u_{(0,360)}$	72^{+1}_{-1}
i _c (°)	fixed		fixed	•	$\mathcal{U}(80, 100)$	$90.89^{+0.98}_{-0.46}$	$\mathcal{U}(80, 100)$	$90.55^{+0.37}_{-1.05}$
Ω_{c} (°)	$\mathcal{U}(0, 360)$	$15.09^{+1.36}_{-0.33}$	$u_{(0,360)}$	352^{+4}_{-2}	$\mathcal{U}(0, 360)$	$318.09^{+0.59}_{-2.26}$	$u_{(0,360)}$	233^{+2}_{-1}
$M_{\rm d}/M_{\star}~(M_{\odot}/M_{\star})\times 10^{-6}$			$\mathcal{U}(0.057, 319.520)$	$1.22_{-0.12}^{+0.10}$	$\mathcal{U}(0.057, 319.520)$	$1.4562^{+0.1593}_{-0.0061}$	$\mathcal{U}(0.057, 319.520)$	$5.91^{+0.50}_{-0.40}$
$P_{\rm d}$ (days)			U(11, 15)	$12.6173_{-0.0114}^{+0.0050}$	$\mathcal{U}(11, 15)$	$13.6140^{+0.0026}_{-0.0016}$	$\mathcal{U}(11, 15)$	$13.9276^{+0.0052}_{-0.0043}$
$\sqrt{e}\cos\omega_{ m d}$			$\mathcal{U}(-0.71, 0.71)$	$-0.2041^{+0.0084}_{-0.0423}$	$\mathcal{U}(-0.71, 0.71)$	$0.059^{+0.038}_{-0.012}$	$\mathcal{U}(-0.71, 0.71)$	$0.3067^{+0.0133}_{-0.0049}$
$\sqrt{e}\sin\omega_{ m d}$			$\mathcal{U}(-0.71, 0.71)$	$0.4993^{+0.0035}_{-0.0189}$	$\mathcal{U}(-0.71, 0.71)$	$0.50045^{+0.00069}_{-0.01099}$	$\mathcal{U}(-0.71, 0.71)$	$-0.2443^{+0.0219}_{-0.0078}$
$\lambda_{\mathrm{d}}\left(^{\circ}\right)$			U(0, 360)	18^{+8}_{-2}	U(0, 360)	$348.65^{+0.60}_{-2.99}$	U(0, 360)	7 ⁺¹ -3
i _d (°)	•		$\mathcal{U}(50, 130)$	$127.08^{+2.44}_{-0.52}$	$\mathcal{U}(50, 130)$	$108.86^{+1.54}_{-0.89}$	$\mathcal{U}(50, 130)$	$101.07^{+0.40}_{-2.73}$
$\Omega_{ m d}\left(^{\circ} ight)$			U(0, 360)	120^{+5}_{-1}	$\mathcal{U}(0, 360)$	$184.39^{+0.22}_{-2.17}$	U(0, 360)	$211.15^{+0.86}_{-1.33}$
$\gamma_{\rm RV}~({\rm m~s^{-1}})$					ı		$\mathcal{U}(-5412, 5243)$	-100^{+3}_{-10}
$\log_2\sigma_{ m jitter,RV}$					1		$\mathcal{U}(-49.8, 6.6)$	$6.6346^{+0.0091}_{-0.0041}$
derived parameters								
$M_{ m b}(M_\oplus)$	$\mathcal{B}(0.01, 50)$	18^{+2}_{-1}	$\mathcal{B}(0.01, 50)$	26^{+2}_{-2}	$\mathcal{B}(0.01, 50)$	$4.70_{-0.40}^{+0.55}$	$\mathcal{B}(0.01, 50)$	31^{+3}_{-3}
$e_{\rm b}$	$\mathcal{B}(0.0, 0.5)$	$0.4988^{+0.0012}_{-0.0148}$	$\mathcal{B}(0.0, 0.5)$	$0.303^{+0.040}_{-0.013}$ (2 σ)	$\mathcal{B}(0.0,0.5)$	$0.0945^{+0.0063}_{-0.0029}$	$\mathcal{B}(0.0, 0.5)$	$0.0044^{+0.0033}_{-0.0023}$
$\omega_{ m b}$ (°)	$\mathcal{U}(0, 360)$	40^{+2}_{-2}	U(0, 360)	77+3	$\mathcal{U}(0, 360)$	$-80^{+3}_{-15} (2\sigma)$	$\mathcal{U}(0,360)$	114^{+17}_{-22}
$\mathcal{M}_{\mathrm{b}}\left(^{\circ}\right)$	$\mathcal{U}(0, 360)$	$316.89^{+1.35}_{-0.40}$	$\mathcal{U}(0,360)$	$307.30^{+0.99}_{-2.04}$	$\mathcal{U}(0, 360)$	$108.249^{+11.401}_{-0.030}$	$\mathcal{U}(0,360)$	-83^{+22}_{-17}
$M_{ m c}\left(M_\oplus ight)$	$\mathcal{B}(0.01, 50)$	21^{+1}_{-2}	$\mathcal{B}(0.01, 50)$	$4.40^{+1.28}_{-0.23}$	$\mathcal{B}(0.01, 50)$	$14.24^{+1.71}_{-1.00}$	$\mathcal{B}(0.01, 50)$	$14.31^{+1.76}_{-0.73}$
e _c	$\mathcal{B}(0.0, 0.5)$	$0.2260^{+0.0105}_{-0.0037}$	$\mathcal{B}(0.0, 0.5)$	$0.0027^{+0.0057}_{-0.0027}(2\sigma)$	$\mathcal{B}(0.0, 0.5)$	$0.00353_{-0.00023}^{+0.00287}$	$\mathcal{B}(0.0, 0.5)$	$0.0226^{+0.0045}_{-0.0042}$
$\omega_{\mathrm{c}}\left(^{\circ}\right)$	$\mathcal{U}(0, 360)$	$289.77^{+0.52}_{-1.17}$	U(0, 360)	77+40	$\mathcal{U}(0, 360)$	-67^{+19}_{-9}	$\mathcal{U}(0,360)$	-109^{+8}_{-7}
$\mathcal{M}_{\mathrm{c}}(^{\circ})$	$\mathcal{U}(0, 360)$	$257.60^{+1.45}_{-0.80}$	U(0, 360)	121^{+58}_{-40}	${\cal U}(0,360)$	265^{+9}_{-19}	$\mathcal{U}(0,360)$	307^{+7}_{-8}
$M_{ m d}(M_\oplus)$			$\mathcal{B}(0.01, 50)$	$0.203^{+0.022}_{-0.024}$	$\mathcal{B}(0.01, 50)$	$0.2424^{+0.0333}_{-0.0084}$	$\mathcal{B}(0.01, 50)$	$0.983^{+0.106}_{-0.087}$
$e_{ m d}$			$\mathcal{B}(0.0, 0.5)$	$0.2910^{+0.0028}_{-0.0057}$	$\mathcal{B}(0.0, 0.5)$	$0.2539^{+0.0017}_{-0.0086}$ (2 σ)	$\mathcal{B}(0.0, 0.5)$	$0.1537^{+0.0033}_{-0.0059}$
$\omega_{ m d}$ (°)			U(0, 360)	$112.23^{+5.02}_{-0.87}$	$\mathcal{U}(0, 360)$	83+1	$\mathcal{U}(0,360)$	321^{+3}_{-2}
$\mathcal{M}_{d}\left(^{\circ} ight)$			U(0, 360)	$145.02^{+0.87}_{-1.89}$	U(0, 360)	$80.97^{+3.67}_{-0.82}$	U(0, 360)	$194.56_{-4.14}^{+0.96}$
$\sigma_{ m jitter,RV}~({ m m~s^{-1}})$					1		$\mathcal{B}(10^{-15}, 100)$	$99.36^{+0.63}_{-0.28}$
BIC = $-2 \ln \mathcal{P} + n_{\text{fit}} \ln n_{\text{data}}$	208.1	8.1	-536.6	9.9	-52	-520.3	1115.2	.2

distribution, and as \mathcal{B} (lower, upper) means the values have been used to force the boundaries, e.g we sampled uniformly in $\sqrt{e}\cos(\omega)$ and $\sqrt{e}\sin(\omega)$, but we checked that e was within the boundaries. A is the mean longitude, that is $A = \omega + \Omega + M$, where ω is the argument of the pericentre (or periastron), Ω is the longitude of the ascending node, and M is mean anomaly. In some cases, the physical parameter converted from the MAP fitted parameters was not within the HDI at 68.27%, so we reported also the value of the 2σ uncertainty from the HDI at 95.5%. **Notes.** All the parameters have been defined at the reference time $BJD_{TDB} - 2450000 = 8329$. Priors indicated as $\mathcal{N}(\mu, \sigma)$ means Gaussian-Normal distribution, as $\mathcal{U}(lower, upper)$ means Uniform