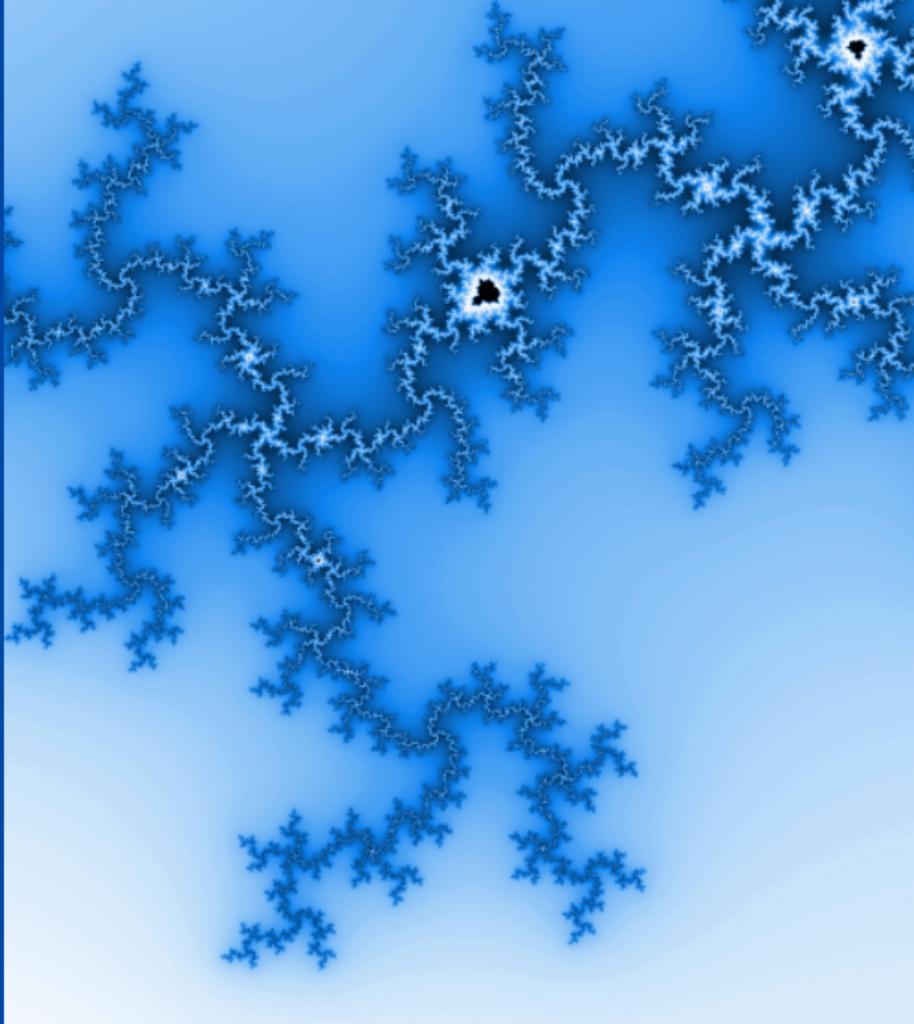


Numerical simulation of Hermite processes

31st Annual Meeting of the Royal
Statistical Society of Belgium –
Ghent

Laurent Loosveldt

8th November 2024



Main definitions

A stochastic process $\{X_t\}_{t \geq 0}$ has:

- ▶ stationary increments if, for every $h > 0$, the stochastic processes

$$\{X_t\}_{t \geq 0} \text{ and } \{X_{t+h} - X_h\}_{t \geq 0}$$

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- ▶ is H -self-similar if, for every $c > 0$, the stochastic processes

$$\{X_{ct}\}_{t \geq 0} \text{ and } \{c^H X_t\}_{t \geq 0}$$

are equal in finite-dimensional distributions.

Long-range dependence

If $\{X_t\}_{t \geq 0}$ is centred with stationary increments, we consider the correlation kernel

$$\rho(k - \ell) := \mathbb{E}[(X_{k+1} - X_k)(X_{j+1} - X_j)] \quad j, k \in \mathbb{N}.$$

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The process $\{X_t\}_{t \geq 0}$ has long-range dependence if

$$\sum_{j \in \mathbb{Z}} |\rho(j)| = \infty.$$

Correlation decays slowly as the lag tends to infinity.

Applications

Such phenomena arise, for instance, in

- ▶ astronomy,
- ▶ biology,
- ▶ climatology,
- ▶ hydrology,
- ▶ image processing,
- ▶ internet traffic modelling,
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We need good models !

Gaussian case : Fractional Brownian Motion

Definition

Given $H \in (0, 1)$, a fractional Brownian motion of Hurst parameter H is a centred continuous Gaussian process $\{B_t^H\}_{t \geq 0}$ with covariance function

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It has stationary increments and is H -self-similar. If $H > \frac{1}{2}$, it has long-range dependence.

Non-Gaussian case

Definition

Given $d \in \mathbb{N}$ and $H \in (1/2, 1)$, the Hermite process of order d and Hurst parameter H is defined as

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- ▶ $d = 1$, it is the Fractional Brownian Motion;
- ▶ $d \geq 2$, it is a non-Gaussian process;
- ▶ has stationary increments, is H -self-similar with long-range dependence.

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$d \geq 3$

Pipiras, in his paper from 2004, raised the question of providing a wavelet-type expansion for any Hermite processes.

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$$f \in L^2(\mathbb{R}^d)$$

Projection onto the subspace spanned by

$$\sum_{\mathbf{k}} \langle f, \otimes_{\ell=1}^d 2^{J/2} \phi(2^J \cdot - k_\ell) \rangle \otimes_{\ell=1}^d 2^{J/2} \phi(2^J \cdot - k_\ell)$$

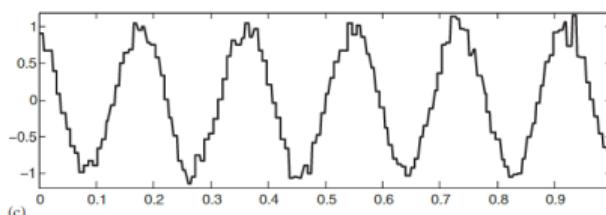
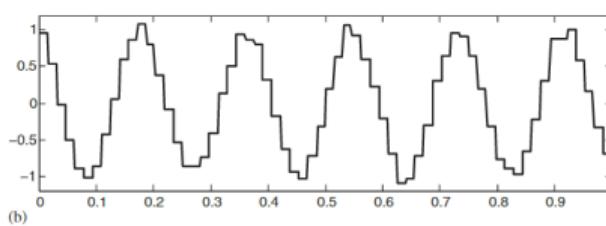
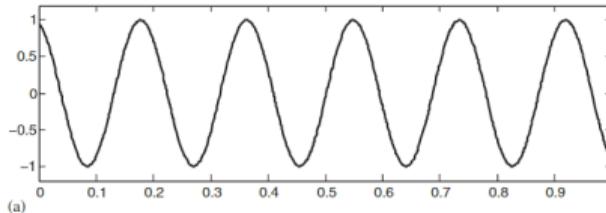
APPROXIMATION

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DETAILS

Multiresolution analysis



Wavelet approximation for stochastic integral

$$I_d : L^2(\mathbb{R}^d) \rightarrow L^2(\Omega) : f \mapsto \int_{\mathbb{R}^d} f \, dB(x_1) \dots dB(x_d)$$

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Wavelet approximation for chaotic processes

We consider stochastic processes of the form

$$\{I_d(K(t, \bullet))\}_{t \geq 0}$$

with, for all $t \geq 0$, $K(t, \bullet) \in L^2(\mathbb{R}^d)$. For the Hermite process, we have

$$K(t, \mathbf{x}) = \frac{1}{c_H} \int_0^t \prod_{\ell=1}^d (s - x_\ell)_+^{\frac{H-1}{d} - \frac{1}{2}} ds.$$

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But, generally, we want a stronger convergence: almost surely uniformly on compact sets.

(A. Ayache, J. Hamonier, L. L. - 2024)

The random series

$$X_{H,J}^{(d)}(t) = 2^{-J(H-1)} \sum_{\mathbf{k} \in \mathbb{Z}^d} \sigma_{J,\mathbf{k}}^{(H)} \int_0^t \prod_{\ell=1}^d \Phi_{\Delta}^{(1/2 + \frac{H-1}{d})}(2^J s - k_{\ell}) ds, \quad (1)$$

is almost surely, for each $J \in \mathbb{N}$, uniformly convergent in t on each compact interval $I \subset \mathbb{R}_+$. Moreover, for all such I , there exists an almost surely finite random variable (depending on I) for which one has, almost surely, for each $J \in \mathbb{N}$,

$$\|X_H^{(d)} - X_{H,J}^{(d)}\|_{I,\infty} = \left\| \sum_{\substack{(\mathbf{j}, \mathbf{k}) \in (\mathbb{Z}^d)^2 \\ \max_{\ell \in [[1,d]]} j_{\ell} \geq J}} 2^{(\frac{H-1}{d})(j_1 + \dots + j_d)} \varepsilon_{\mathbf{j}, \mathbf{k}} \int_0^t \prod_{\ell=1}^d \psi_{h_{\ell}}(2^{j_{\ell}} s - k_{\ell}) ds \right\|_{I,\infty} \leq C J^{\frac{d}{2}} 2^{-J(H-1/2)}.$$

$$\sigma_{J,\mathbf{k}}^{(H)}$$

$$\sigma_{J,\mathbf{k}}^{(\mathbf{h})} = \sum_{m=0}^{\lfloor d/2 \rfloor} (-1)^m \sum_{P \in \mathcal{P}_m^{(d)}} \prod_{r=1}^m \mathbb{E}[Z_{J,k_{\ell_r}}^{(1/2 + \frac{H-1}{d})} Z_{J,k_{\ell'_r}}^{(1/2 + \frac{H-1}{d})}] \prod_{s=m+1}^{d-m} Z_{J,k_{\ell''_s}}^{(1/2 + \frac{H-1}{d})}. \quad (2)$$

where, for $J \in \mathbb{Z}$, we consider the sequence $(g_{J,k}^\phi)_{k \in \mathbb{Z}}$ of i.i.d. $\mathcal{N}(0,1)$ Gaussian random variable defined, for all $k \in \mathbb{Z}$, by $g_{J,k}^\phi := 2^{J/2} \int_{\mathbb{R}} \phi(2^J x - k) dB(x)$. and for $\delta \in (-1/2, 1/2)$, the Gaussian FARIMA $(0, \delta, 0)$ sequence $(Z_{J,\ell}^{(\delta)})_{\ell \in \mathbb{Z}}$ associated to $(g_{J,k}^\phi)_{k \in \mathbb{Z}}$ is given, for all $\ell \in \mathbb{Z}$, by

$$Z_{J,\ell}^{(\delta)} := g_{J,\ell}^\phi + \sum_{p=1}^{+\infty} \gamma_p^{(\delta)} g_{J,\ell-p}^\phi, \text{ with } \delta_p^{(\delta)} := \frac{\delta \Gamma(p + \delta)}{\Gamma(p + 1) \Gamma(\delta + 1)}$$

“Approximation process”

$$X_{H,J}^{(d)}(t) = 2^{-J(H-1)} \sum_{\mathbf{k} \in \mathbb{Z}^d} \sigma_{J,\mathbf{k}}^{(H)} \int_0^t \prod_{\ell=1}^d \Phi_{\Delta}^{(1/2 + \frac{H-1}{d})}(2^J s - k_{\ell}) ds,$$

$$\text{with } \hat{\Phi}_{\Delta}^{(\delta)}(\xi) = \left(\frac{1-e^{-i\xi}}{i\xi} \right)^{\delta} \hat{\phi}(\xi)$$

Not computable, only because of the series.

Strategy

To deduce the inequality

$$\|X_H^{(d)} - X_{H,J}^{(d)}\|_{I,\infty} = \left\| \sum_{\substack{(\mathbf{j},\mathbf{k}) \in (\mathbb{Z}^d)^2 \\ \max_{\ell \in [[1,d]]} j_\ell \geq J}} 2^{(\frac{H-1}{d})(j_1 + \dots + j_d)} \varepsilon_{\mathbf{j},\mathbf{k}} \int_0^t \prod_{\ell=1}^d \psi_{h_\ell}(2^{j_\ell} s - k_\ell) ds \right\|_{I,\infty} \leq C J^{\frac{d}{2}} 2^{-J(H-1/2)}.$$

we somehow remarked that this rate of convergence is mainly determined by the terms in the series for which the corresponding indices belongs to

$$D_j^1(t) := \{k \in \mathbb{Z} : [k2^{-j} - 2^{-ja}, k2^{-j} + 2^{-ja}] \subseteq [0, t]\} \text{ with } a \in (1/2, 1)$$

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Set

$$\mathcal{J}_J^1(t) := \{\mathbf{k} \in (D_J^1(t))^d : \max_{\ell, \ell' \in [[1,d]]} |k_\ell - k_{\ell'}| \leq 2^{\varepsilon J}\} \text{ with } \varepsilon > 0.$$

Simulation process

(A. Ayache, J. Hamonier, L. L. - 2024)

For all $J \in \mathbb{N}$, the *simulation process at scale J* of the generalized Hermite process $\{X_H^{(d)}(t)\}_{t \in \mathbb{R}_+}$ is the process defined, for all $t \in \mathbb{R}_+$, by

$$S_{H,J}^{(d)}(t) = 2^{-JH} \sum_{\mathbf{k} \in \mathcal{J}_J^1(t)} \sigma_{J,\mathbf{k}}^{(\mathbf{h})} \int_{\mathbb{R}} \prod_{\ell=1}^d \Phi_{\Delta}^{(1/2 + \frac{H-1}{d})}(s - k_{\ell}) ds. \quad (3)$$

For any compact interval $I \subset \mathbb{R}_+$, there exists an almost surely finite random variable C (depending on I) for which one has, almost surely, for each $J \in \mathbb{N}$,

$$\|X_H^{(d)} - S_{H,J}^{(d)}\|_{I,\infty} \leq CJ^{\frac{d}{2}} 2^{-J(H-1/2)}. \quad (4)$$

Python routine (using some R packages) for the Hermite processes of order 1,2 and 3 available upon request.

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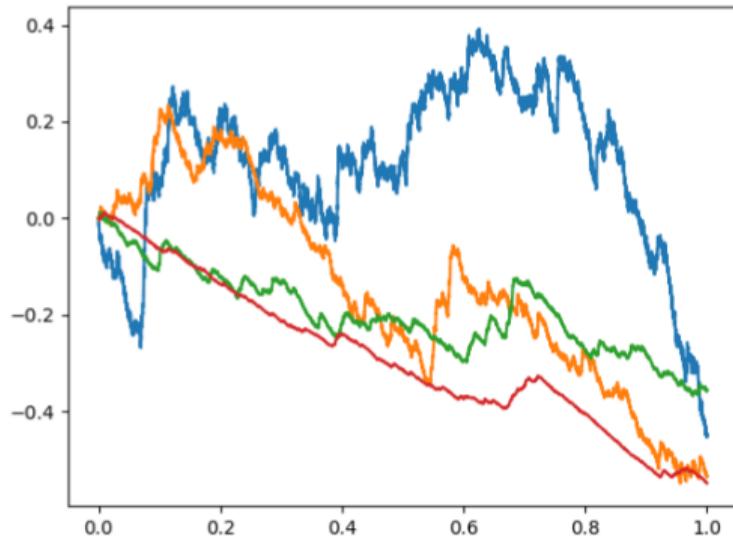


Figure: Paths of the Rosenblatt process of Hurst parameter 0,6 (blue), 0,7 (orange), 0,8 (green) and 0,9 (red).

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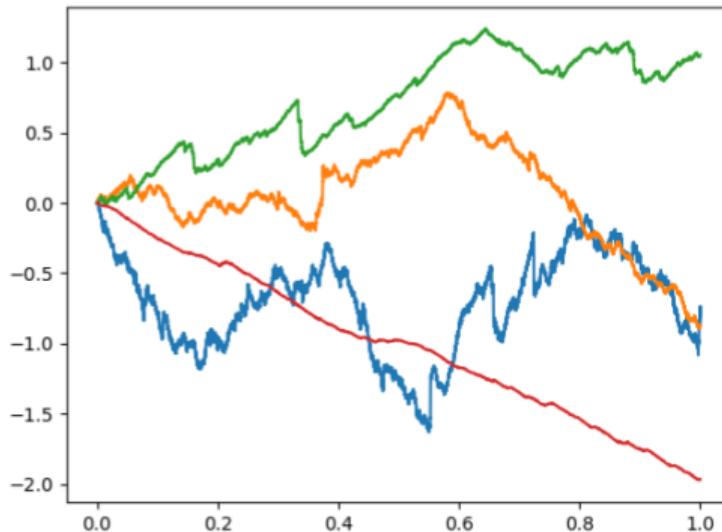


Figure: Paths of the Hermite process of order 3 of Hurst parameter 0,6 (blue), 0,7 (orange), 0,8 (green) and 0,9 (red).

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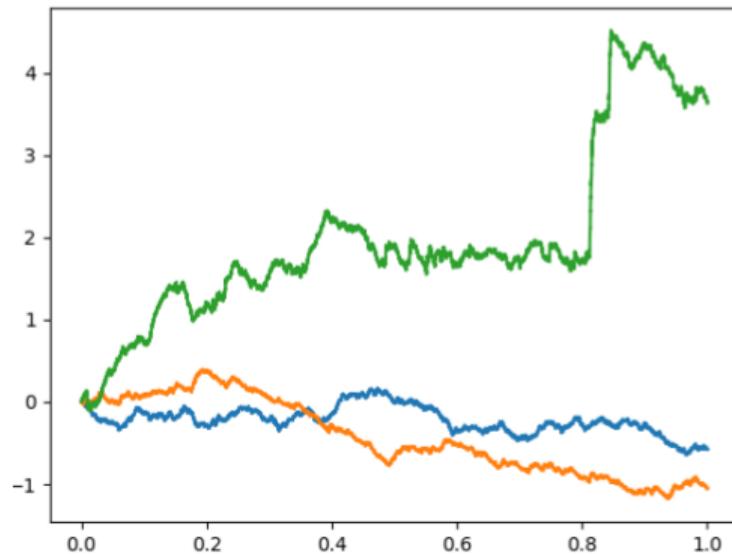


Figure: Paths of the Fractional Brownian Motion (blue), the Rosenblatt process (orange) and the Hermite process of order 3 (green) with Hurst parameter 0,6.

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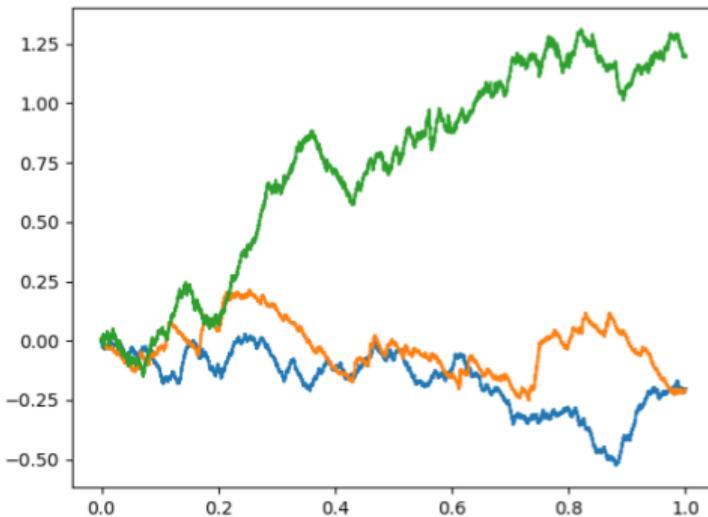


Figure: Paths of the Fractional Brownian Motion (blue), the Rosenblatt process (orange) and the Hermite process of order 3 (green) with Hurst parameter 0,7.

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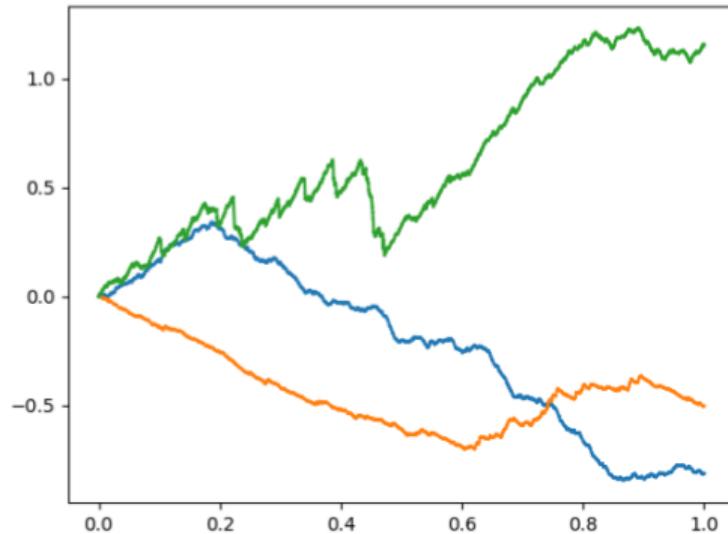


Figure: Paths of the Fractional Brownian Motion (blue), the Rosenblatt process (orange) and the Hermite process of order 3 (green) with Hurst parameter 0,8.

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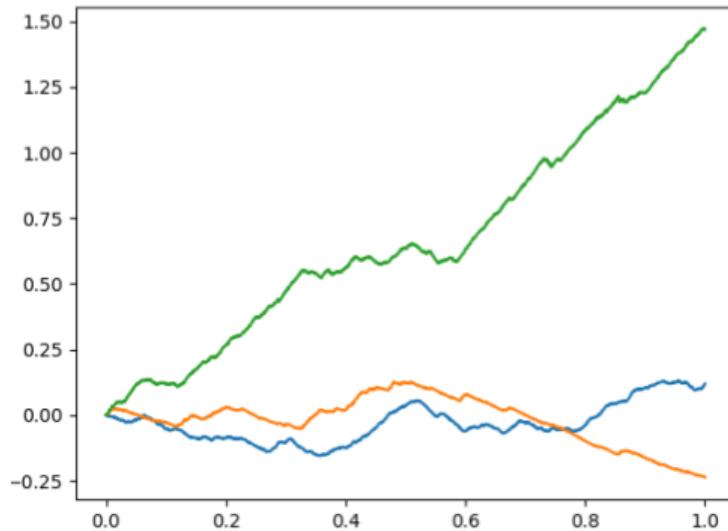


Figure: Paths of the Fractional Brownian Motion (blue), the Rosenblatt process (orange) and the Hermite process of order 3 (green) with Hurst parameter 0,9.

Applications (work in progress)

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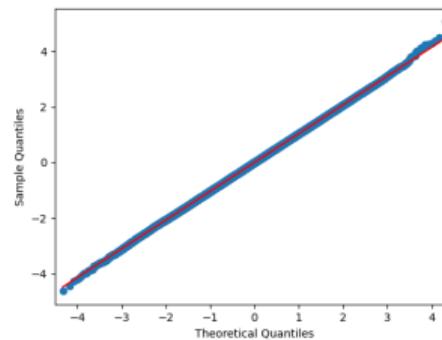


Figure: QQplot for the distribution of a fractional Brownian motion, compared with a $\mathcal{N}(0,1)$

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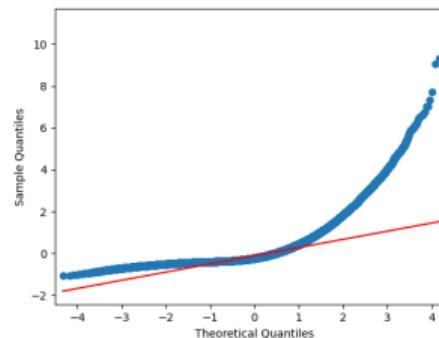


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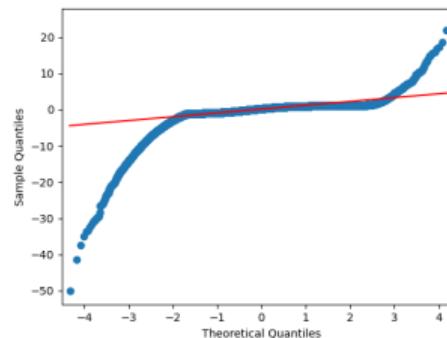


Figure: QQplot for the distribution of a Hermite process of order 3, compared with a $\mathcal{N}(0,1)$