



Flexural buckling of mild and high-strength steel hot-rolled sections

Improvement proposal for the flexural buckling design rules

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$$\chi = \frac{1}{\phi + \sqrt{\phi^2 - \bar{\lambda}^2}}$$
 but $\chi \le 1$

Where $\phi = 0.5 * [1 + \alpha * (\bar{\lambda} - 0.2) + \bar{\lambda}^2]$



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Key

Relative slenderness $\overline{\lambda}$ Reduction factor χ

Figure 8.5 — Buckling curves



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 but $\chi \le 1$

Where $\phi = 0.5 * [1 + \alpha * (\overline{\lambda} - 0.2) + \overline{\lambda}^2]$ Imperfection parameter



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Figure 8.5 — Buckling curves





Imperfection factor α

0,13

0,21

0,34

0,76

0,49



76

Column resistance – design procedure acc. to EC3

	$\chi = rac{1}{\phi}$. Here ϕ =	1 ⊢ √φ 0.5 ∗ [: In	$\frac{1}{2^2 - \overline{\lambda}^2} b^2$ 1 + $\alpha \cdot (\overline{\lambda} - 0)$ nperfection p	ut $\chi \leq$ (0.2) + $\bar{\lambda}^2$]	1	Imper	fection	factor	X FPrEN19 1,1 1 0,9 0,8 0,7 0,6 0,5 0,4 0,3 0,3 0,4 0,3 0,4 0,3 0,4 0,5 0,4 0,5 0,4 0,5 0,5 0,4 0,5 0,5 0,5 0,4 0,5 0,5 0,5 0,5 0,5 0,5 0,5 0,5	93-1-1:20			
				EN1993-1-2	1:2005	FprEN199	93-1-1:2022	0,2 0,1					
Cross-section			Limits	Buckling about axis	S235-S420	S460	S235- S420	S460 up to S700 inclusive	$\frac{0}{0} 0,2 0,4 0,6 0,8 1,0 1,2 1,4 1,6 2$ Key Relative slenderness $\overline{\lambda}$ Reductive factor χ	,8 2 2,2 2,4	4 2,6 2,8 3	3 7	
	1		t < 10	v-v	а	a.	а	a		ioi bucking cu	Ives		
ons	± z	1.2	$l_f \leq 40 \ mm$	<u> </u>	b	a	b	a	Buckling curve a_0 a Imperfection factor α 0.13 0.21	0.34	C 0.49	0	
ecti		$\sim q$	t > 10 mm	<u>v-v</u>	b	a	b	a		0,34	0,49	0	
H-S	= v - v	u/u	$l_f > 40 mm$	<i>z-z</i>	с	a	с	b					
- or		5	$t_{\epsilon} < 100 mm$	у-у	b	а	b	а					
ed I		, , ,	-,	<i>z-z</i>	с	a	с	b					
colle	z	< <i>q</i> ,	$t_f > 100 mm$	у-у	d	с	d	с			6		
Ł	← Ŭ →	/y	,	z-z	d	с	d	с					



Column resistance – design procedure acc. to EC3

	$\chi = rac{1}{\phi}$ H	1 - √φ 0.5 * [:	$\frac{1}{2^2 - \overline{\lambda}^2} b^2$	$\operatorname{ut} \chi \leq 0.2) + \overline{\lambda}^2]$	1		for the second	factor	x FprEN1993-1-1:2022 1,1					
		In	nperfection p	arameter		Imper	rection	Tactor						
					EN1993-1-2	1:2005	FprEN199	93-1-1:2022						
C	ross-section	Limits		Buckling about axis	S235-S420	S460	S235- S420	S460 up to S700 inclusive	0 - 0 - 0 - 0 - 0 - 0 - 0 - 0 - 0 - 0 -					
				<i>v-v</i>	я	a.	а	a.						
suc	t z	1.2	$t_f \leq 40 \ mm$	<u>y y</u> 7-7	b the second sec	a ₀	h h	a	Buckling curve a_0 a b c d					
ecti		P = q	t > 10 mm	v-v	b	a	b	a						
H-S-	< v v	u/u	$l_f > 40 mm$	<i>z-z</i>	с	a	с	b						
- or		5	$t_{\epsilon} \leq 100 mm$	у-у	b	а	b	а	Superior buckling resistance for HSS is					
ed I		-1:		<i>z-z</i>	с	a	с	b						
soll	z	< <i>q</i> ,	$t_f > 100 mm$	у-у	d	с	d	с	still contemplated but, with few changes 7					
ц	→	/y		<i>z-z</i>	d	с	d	с	between the two standard versions					



Literature review and research objective

Type of sections	Maquoi, 1982	Jönsson & Stan, 2016	Somodi & Kövesdi, 2017	Meng & Gardner, 2020
Hot-rolled (y-y)	$a^* + (\overline{2} - 0.2)$	$\alpha * (\overline{\lambda}\varepsilon - 0, 2)$ with; $\varepsilon = \sqrt{\frac{235}{f_y}}$ Class 4 neglected, only for	/	/
Hot-rolled (z-z)	$\boldsymbol{u} * (\lambda = 0, 2)$	/	/	/
Welded I-sections	$\alpha^* = \alpha * \left(\frac{235}{f_y}\right)^n$ n=0.8, Maquoi, 1982 ;	/	$\boldsymbol{\alpha}^* * (\overline{\lambda} - 0, 2)$ $\boldsymbol{\alpha}^* = \boldsymbol{\alpha} * \left(\frac{235}{f_y}\right)^{0.6}$	/
Hot-finished tubes	n=1.0, Johansson, 2005 ;	/	/	$\pmb{lpha}^* * (\overline{\lambda} - 0, 1)$
Cold-formed tubes		/	$\boldsymbol{\alpha}^* * (\overline{\lambda} - 0.2)$ $\boldsymbol{\alpha}^* = \boldsymbol{\alpha} * \left(\frac{235}{f_y}\right)^{0.5}$	$\alpha^*=0.24\epsilon$ for hot-finished $\alpha^*=0.56\epsilon \text{ for cold-formed}$



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Research objective: to define a new modified imperfection factor for hot-rolled sections in order to restore the continuity in the design procedure 9



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	$\alpha^* * (\overline{\lambda} - 0.2)$	strong axis buckling		
Hot-rolled (z-z)	u (<i>n</i> 0,2)	/	/	/
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Support conditions & Initial bow imperfection



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Limits	Designation	h [mm]	b [mm]	t _w [mm]	t _f [mm]	r [mm]	Class in S460	Class in S690
h/b > 1.2	HEB400	400	300	13.5	24	27	2 21	3
/ t, ≤ 40mm	HEM500	524	306	21	40	27	1	2



Validation on existing buckling tests

The validation was performed on the experimental tests carried out on heavy hot-rolled sections at the Fritz Engineering Laboratory in 1972



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A good correspondence between numerical simulations and the new upcoming standard FprEN1993-1-1: 2022 has been contemplated.















Intermediate grades are categorized within the same buckling curve as S235, which has been evaluated as very conservative.



Proposal of a new modified imperfection factor



Proposal of a new modified imperfection factor $\alpha^* * (\overline{\lambda} - 0.2) \Rightarrow \alpha^* = \alpha * \left(\frac{235}{f_y}\right)^{0.7}$



Proposal of a new modified imperfection factor

$$\alpha^* * (\overline{\lambda} - 0, 2) \Rightarrow \alpha^* = \alpha * \left(\frac{235}{f_y}\right)^*$$

This exponent is chosen to respect the current recommended factors for S235 and S460



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 α_{FEM} evaluated for each f_y





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Benefit in terms of buckling resistance





Benefit in terms of buckling resistance









Advantage of this proposal: to keep the same buckling curve denomination for S235 ; to continuously account for the yield strength and thus to induce weight saving. Indeed, even a small increase of buckling resistance may lead to a gain of one or several profiles when designing a steel column.





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					Buckling curves		
Cr	oss-section	Limits		Buckling about axis	S235 S275 S355 S420	S460 up to S700 inclusive	
ions	÷ z	>1.2	t < 10 mm	у-у	а	a ₀	
-sect		<d h<="" td=""><td>$l_f \leq 40 mm$</td><td>z-z</td><td>b</td><td>а</td></d>	$l_f \leq 40 mm$	z-z	b	а	
d I- or H	e y y	≤1.2	$t_f \leq 100 \ mm$	у-у	b	а	
Rolled		≥d/h	,	Z-Z	с	b	

Table 8.3 of FprEN1993-1-1: 2022

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Table 8.3 of Fpr<u>EN</u>1993-1-1: 2022



	Cross-section		Limits	Buckling about axis	Buckling curve
ions	÷ z	>1.2	t₂ ≤ 40 mm	у-у	а
l-sect		;d/h	$t_f \leq 40 mm$	z-z	b
d - or H	z y y	≤1.2	$t_f \leq 100 mm$	у-у	b
Rolled	z b	-d/h		z-z	с

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- The approach can be applied to other section typologies in order to generalize the conclusions;







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- Buckling tests should be realised to confirm the numerical results and calibrate the partial safety coefficient.







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Extended version

Journal paper: *L. Saufnay, J-P Jaspart and J.-F. Demonceau.* "Improvement of the prediction of the flexural buckling resistance of hot-rolled mild and high-strength steel members" Engineering Structures, Elsevier, 2024 [Manuscript accepted – in production]







Proposal of modification



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Thank you for your attendance !

Questions?

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