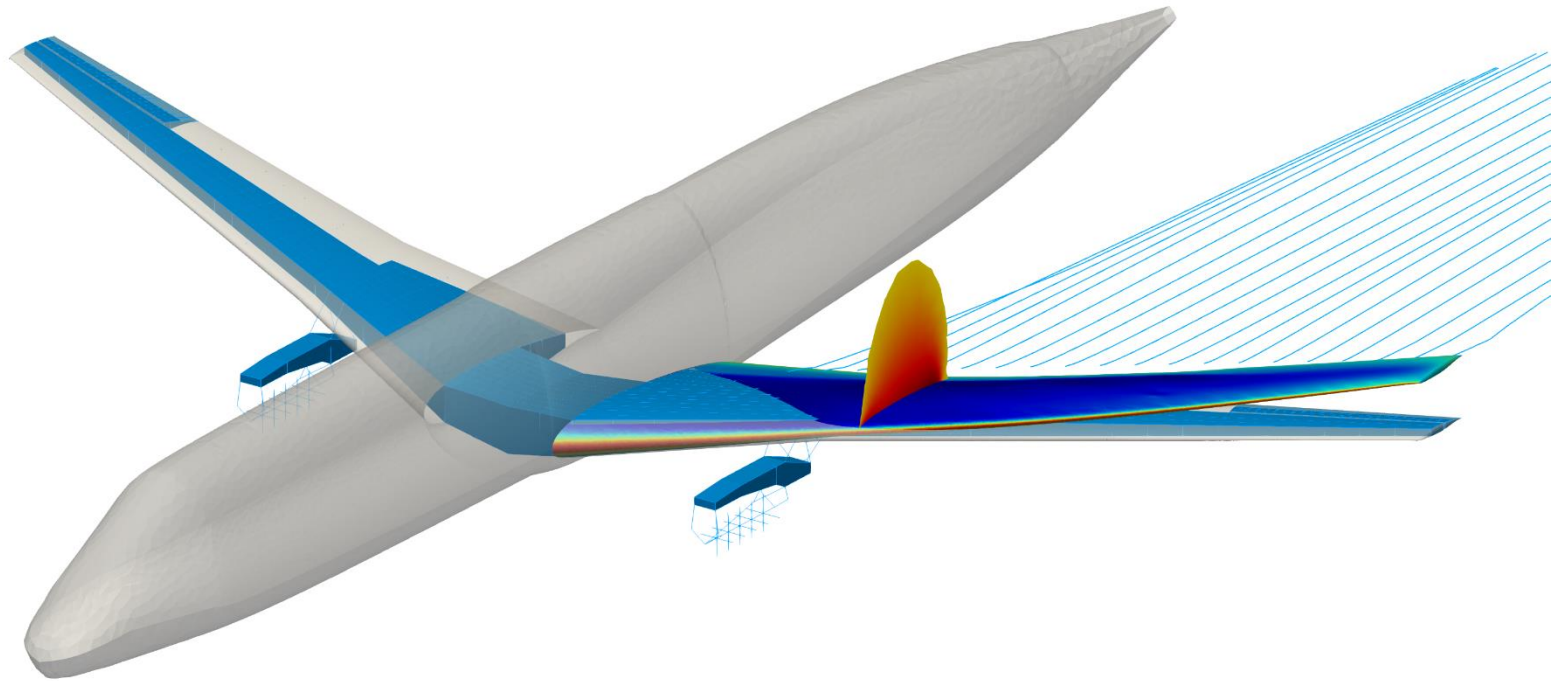


Aerostructural modeling for preliminary aircraft design

Adrien Crovato



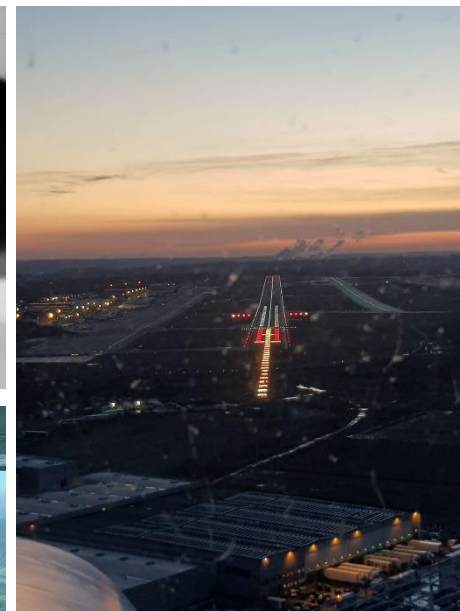
About me

Professional

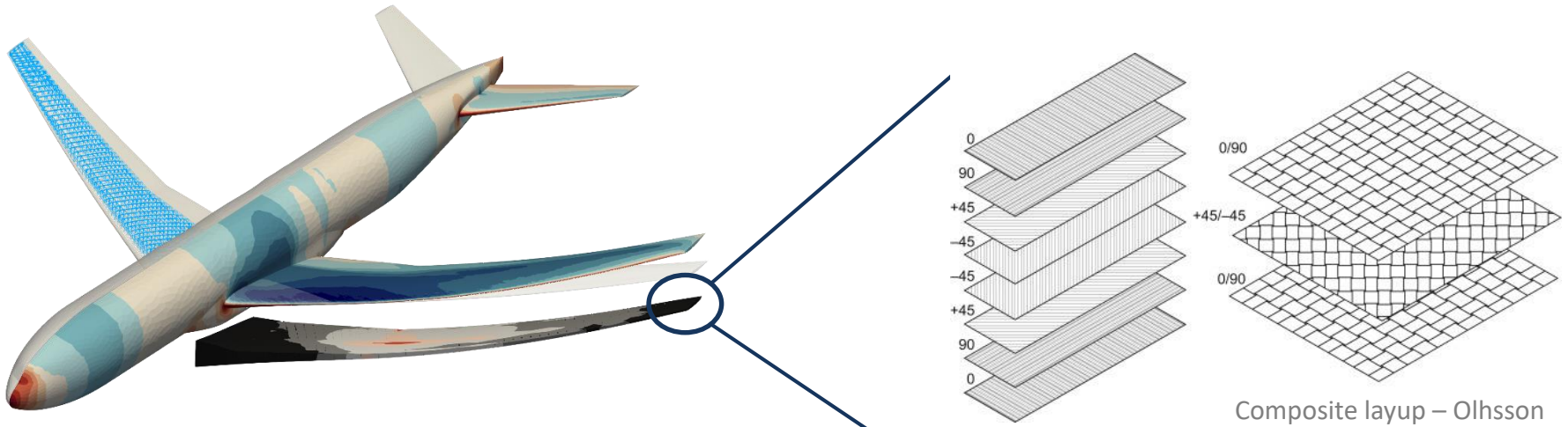
- MSc in Aerospace Eng., 2015
- PhD in Aerospace Eng., 2020
- Post-doc in Aerospace Eng., since 2020
- Teaching activities, since 2015
- ULiège with Embraer

Personal

- Martial artist
- Private pilot



Aerostructural optimization

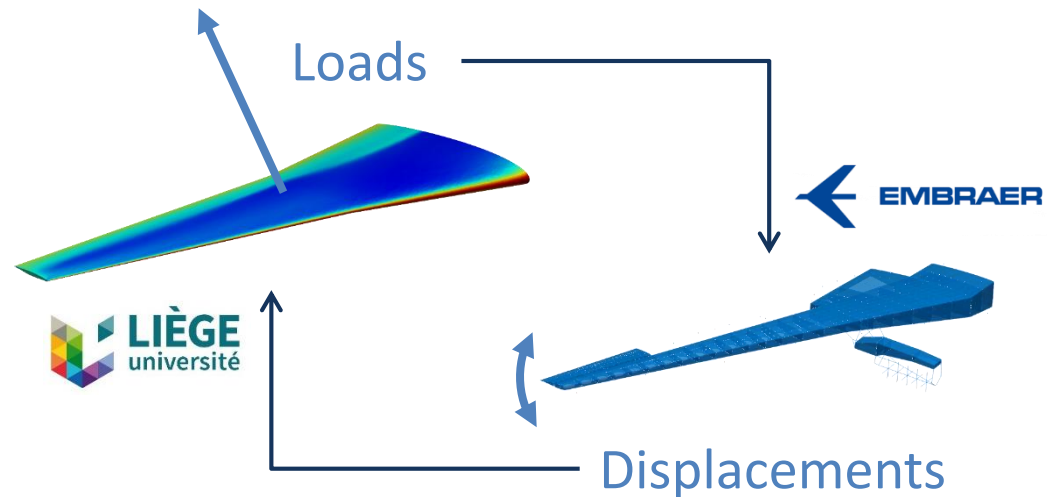


Optimize shape and laminates

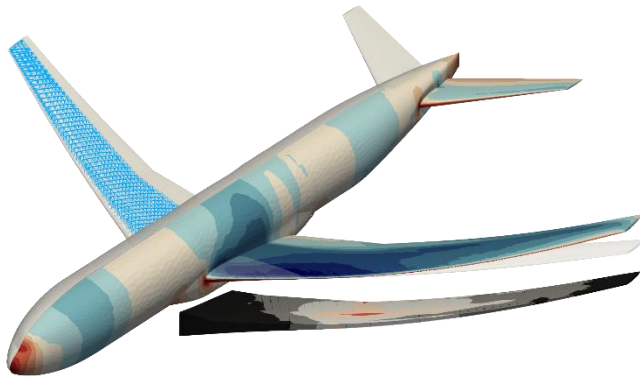
- Decrease fuel burn

Such that

- No failure
- No flutter



Preliminary aircraft design



Numerical model (9%)

- Global design
- Optimization
- Performance

Results must be obtained **quickly**
Adequate models must be chosen

Outline

Optimization

- Mathematical formulation
- Gradients calculation

Static aeroelasticity

- Steady aerodynamic modeling
- DART

Dynamic aeroelasticity

- Unsteady aerodynamic and flutter modeling
- SDPM and PyPk

Benchmark case

- Problem description
- Optimization results

Optimization formulation

Gradient-based approach

$$d_x F(u; x) \rightarrow 0$$

$$\text{s.t. } \begin{cases} R(u; x) = 0 \\ C(u; x) = 0 \end{cases}$$

“perturbation”

$$\begin{cases} d_x F(u; x) \rightarrow 0 \\ R(u; x) = 0 \end{cases}$$

“chain rule”

$$\begin{cases} R(u(x + \delta x)) = 0 \\ d_x F = \Delta \left\{ \frac{F(u(x + \delta x))}{\delta x} \right\} \end{cases}$$

$$\begin{cases} R(u(x)) = 0 \\ d_x F = \partial_x F - \partial_u F \partial_u R^{-1} \partial_x R \end{cases}$$

Computational cost analysis

Finite differences

$$\begin{cases} R(u(x)) = 0 \\ R(u^+(x + \delta x)) = 0 \\ d_x F = \frac{F(u^+) - F(u)}{\delta x} + O(\delta x) \end{cases}$$

Complex step

$$\begin{cases} R(u(x)) = 0 \\ R(u^+(x + i\delta x)) = 0 \\ d_x F = \text{Im} \left\{ \frac{F(u^+)}{\delta x} \right\} + O(\delta x^2) \end{cases}$$

→ Cost \sim n. o. **design variables** \times time to solve **nonlinear** equations

Direct and adjoint

$$\begin{cases} R(u(x)) = 0 \\ d_x F = \partial_x F - \boxed{\partial_u F \partial_u R^{-1} \partial_x R} \end{cases}$$

$\partial_u R^T \lambda = \partial_u F^T$
Adjoint

$\partial_u R \lambda = \partial_x R$
Direct

→ Cost (adjoint) \sim n. o. **functionals** \times time to solve **linear** equations

Calculation of the derivatives



Hand differentiation

- ✓ Most effective
- × Difficult, sometimes not feasible

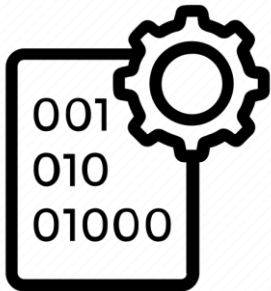


Finite differences

- ✓ Very easy
- × Inaccurate

Complex step

- ✓ Accurate
- × Complex arithmetic



Automatic differentiation

- ✓ Straightforward
- × Increased memory usage

Outline

Optimization

- Mathematical formulation
- Gradients calculation

Static aeroelasticity

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- DART

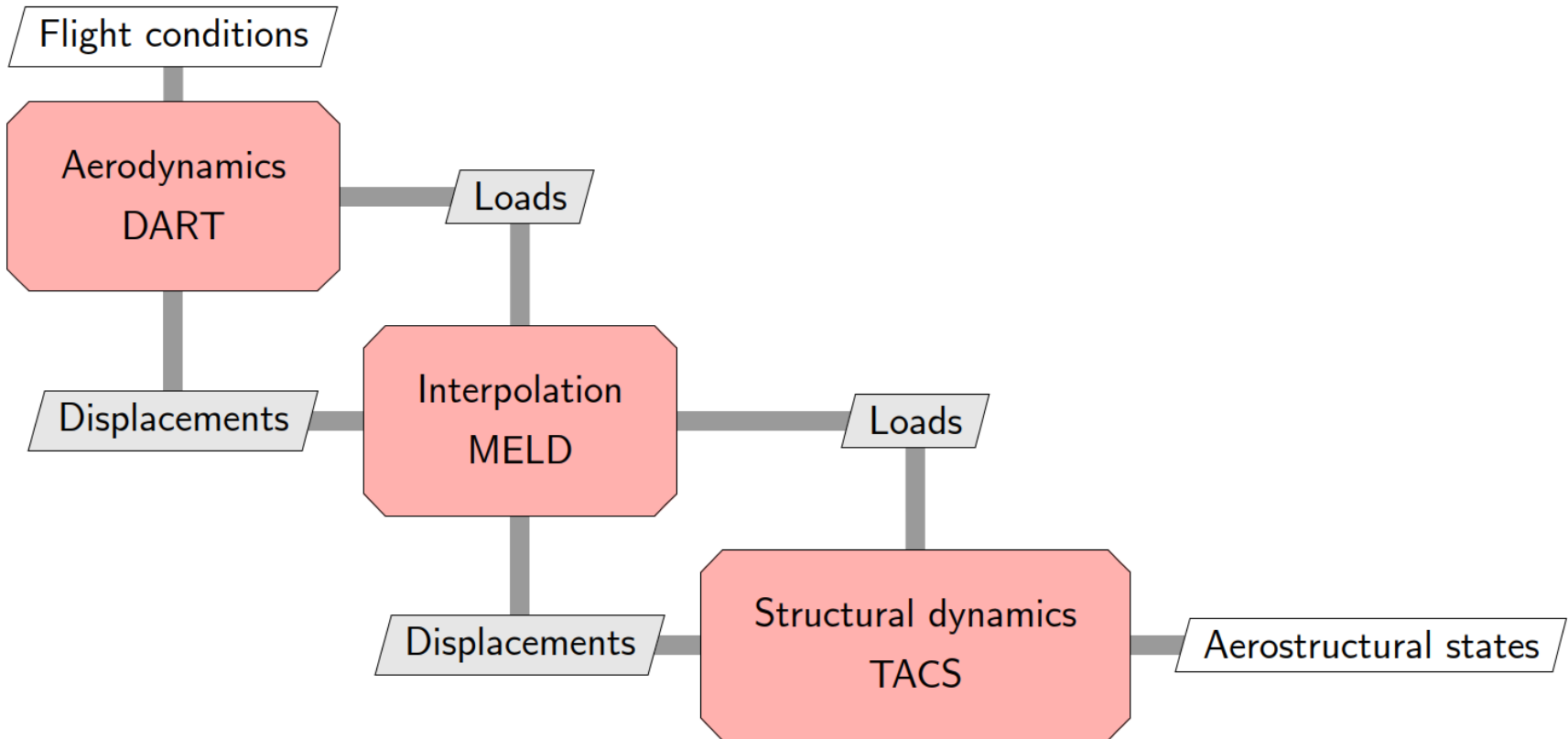
Dynamic aeroelasticity

- Unsteady aerodynamic and flutter modeling
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Benchmark case

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Analysis process



<https://openmdao.org>



<https://github.com/openmdao/mphys>

Aerodynamic models for aircraft design

RANS equations

- Subsonic
- Supersonic
- Transonic
- Viscous

Euler equations

- Subsonic
- Supersonic
- Transonic
- **Inviscid**

Full potential equation

- Subsonic
- Supersonic
- **~Transonic**
- Inviscid

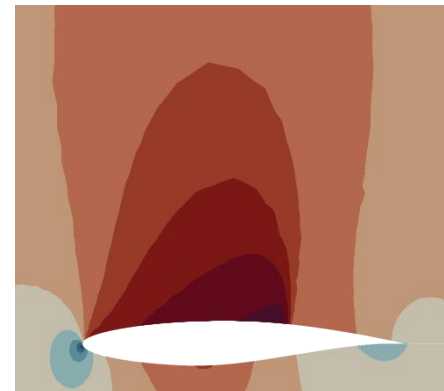
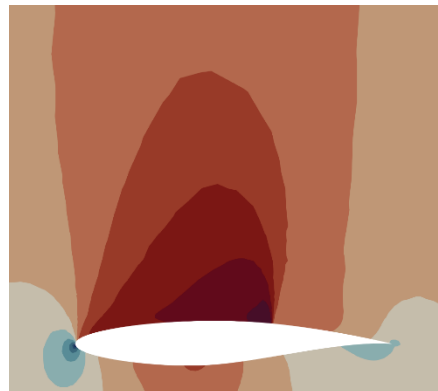
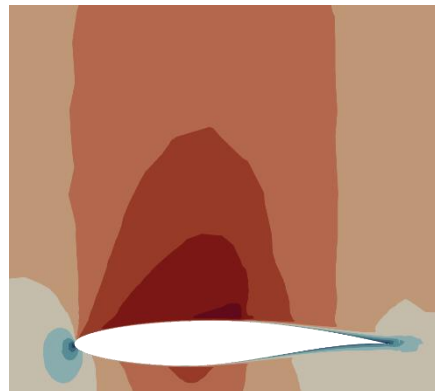
Linear potential equation

- **~Subsonic**
- **~Supersonic**
- ~~Transonic~~
- Inviscid

→
Inviscid

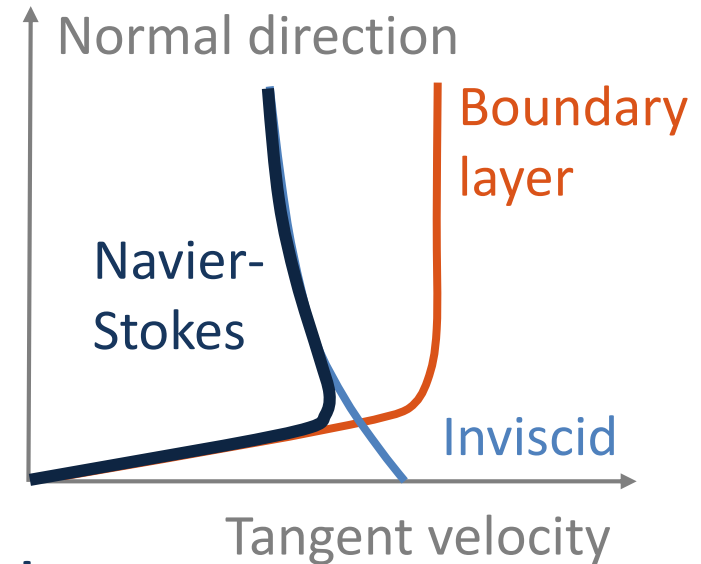
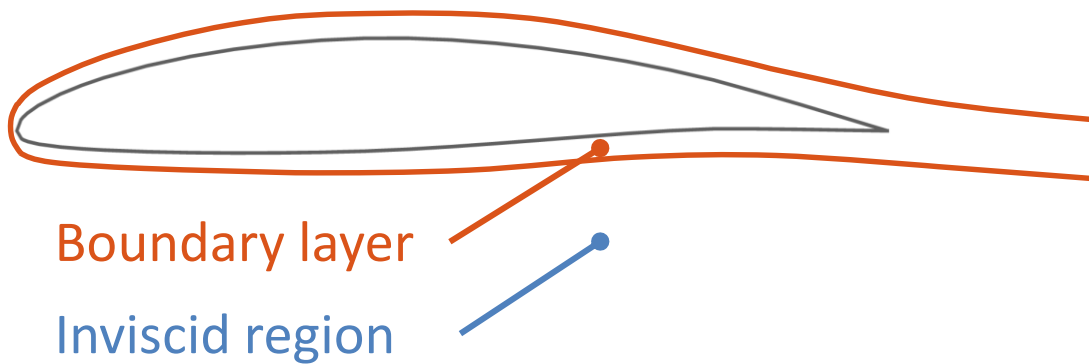
→
Isentropic

→
Linear

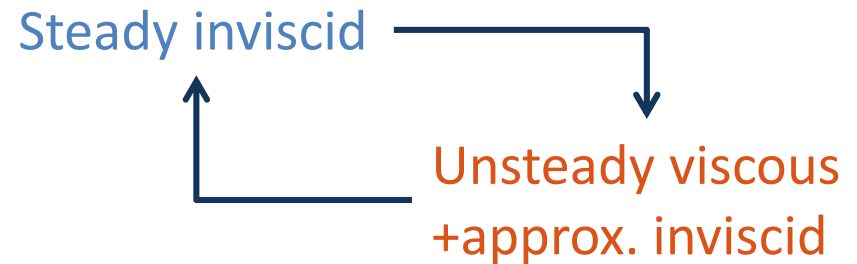
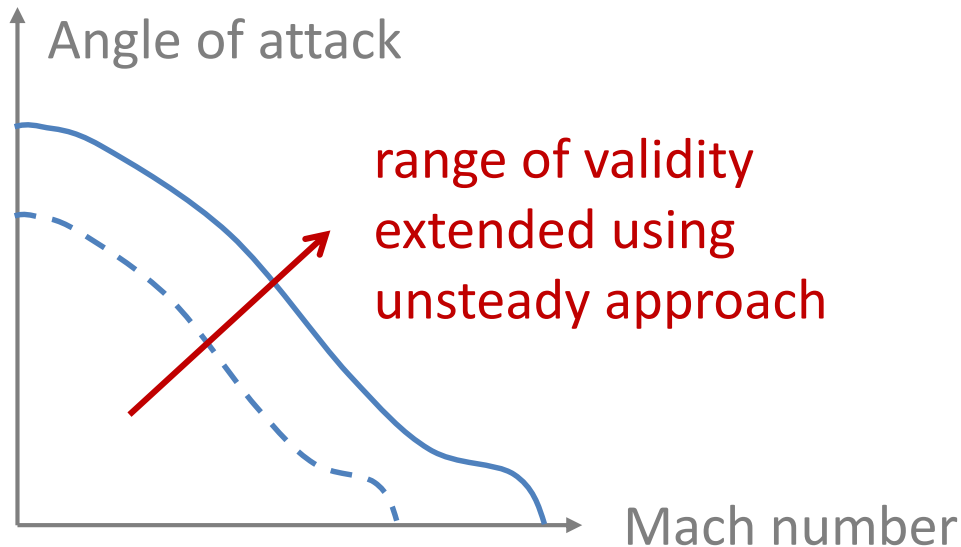


Mach number

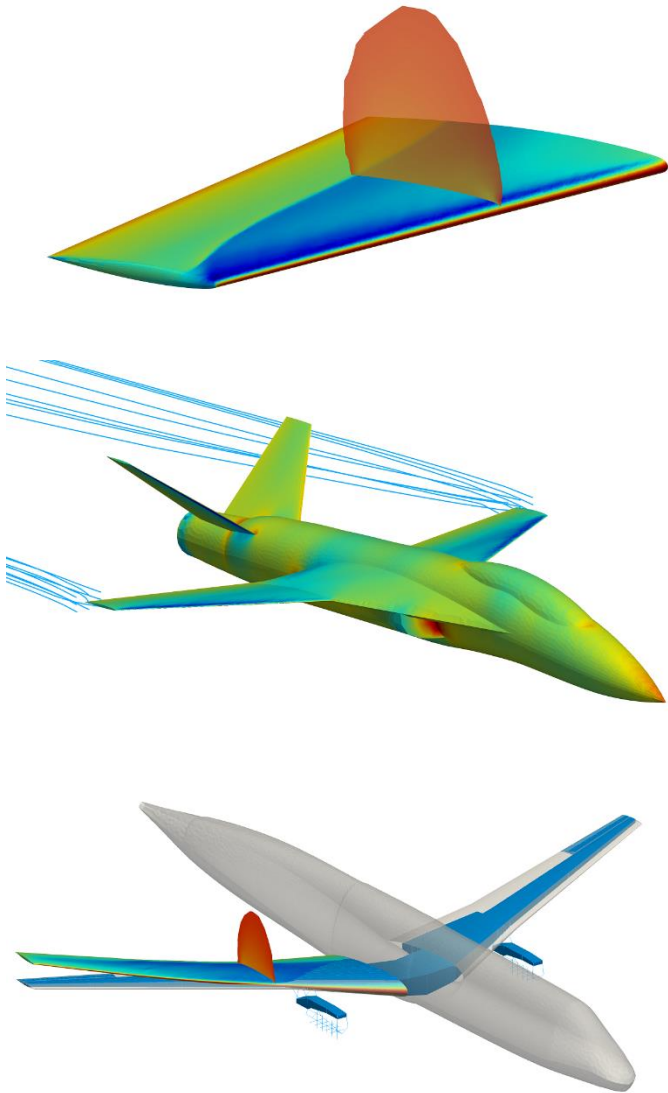
Viscous-inviscid interaction



Quasi-simultaneous pseudo-unsteady approach



DART



Discrete Adjoint for Rapid Transonic Flows

- Steady full potential formulation
- Finite element discretization
- Unstructured tetrahedral grid
- Analytical discrete adjoint
- Mesh morphing
- Viscous-inviscid interaction
- C++ with Python API

Performance (712k elements @ 3.4GHz)

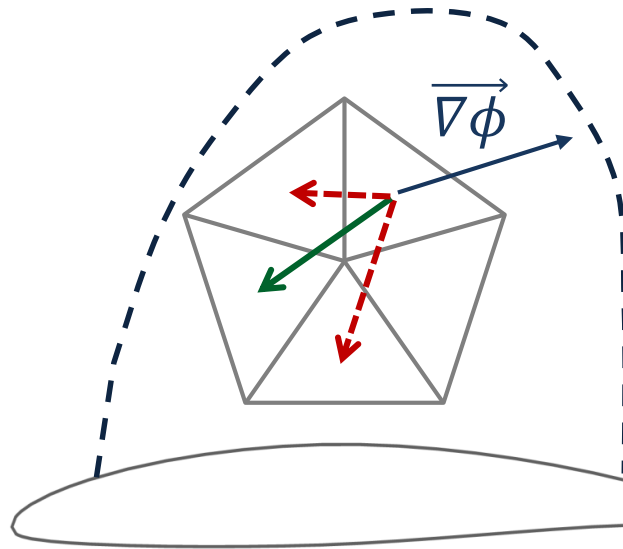
- Solution – 100 s
- Morphing – 25 s
- Gradient – 45 s

Formulation and implementation

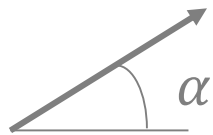
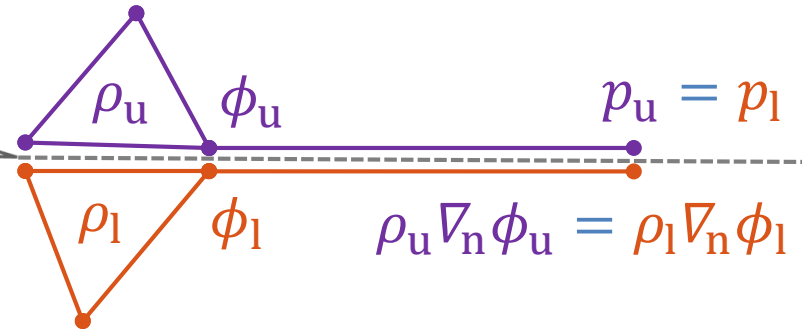
$$\nabla \cdot (\rho \nabla \phi) = 0$$

$$\rho \leftarrow \rho - v \overleftarrow{\Delta} \rho$$

$$v = v_{c\downarrow} \left(1 - \frac{M_{c\uparrow}^2}{M_e^2} \right)$$



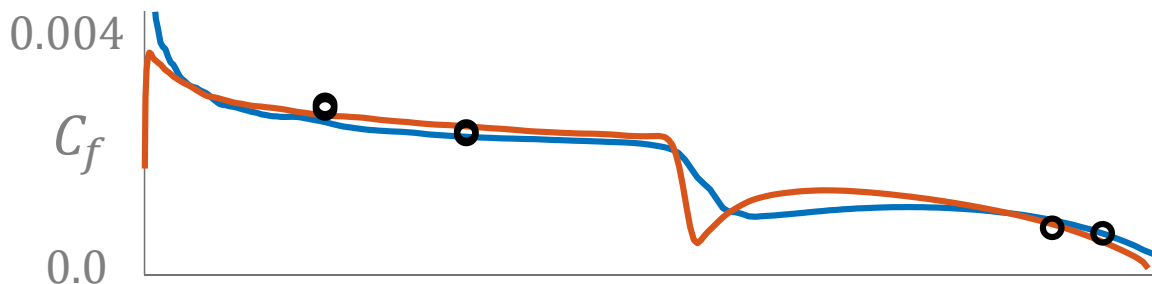
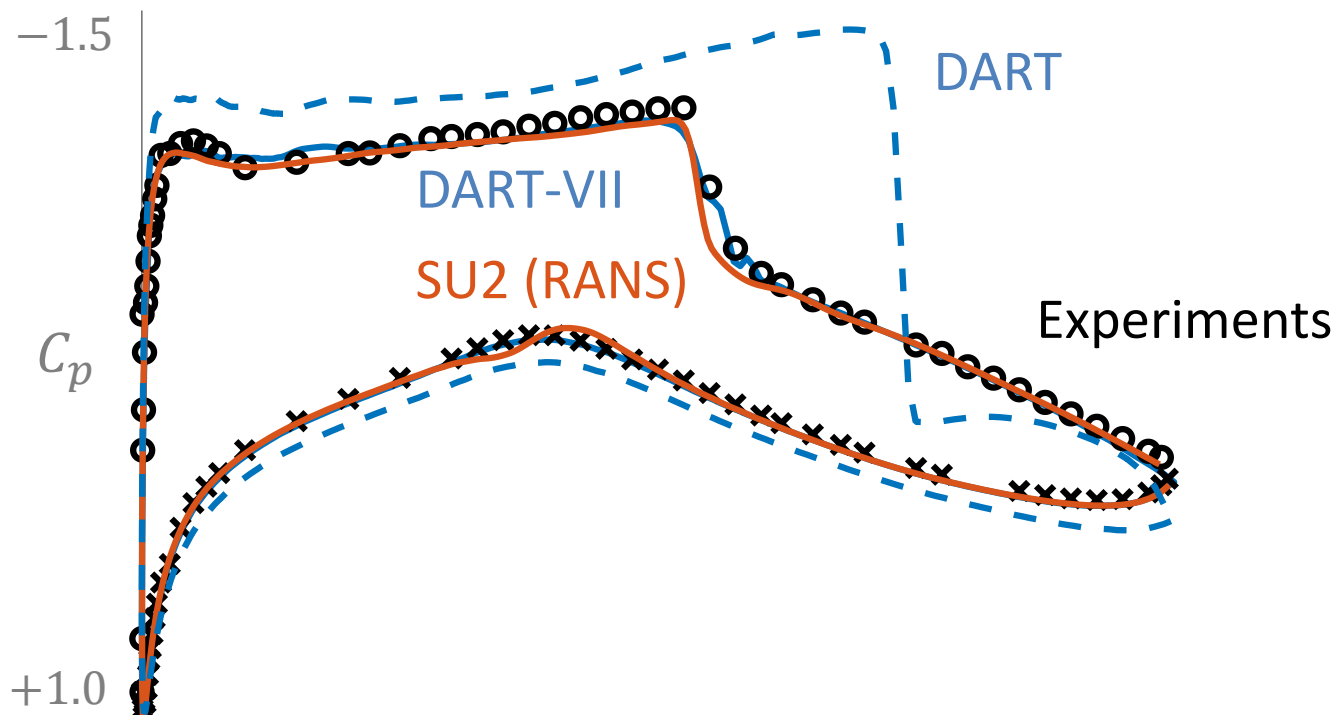
$$\rho \nabla \phi \cdot n = 0$$



$$\rho_\infty U_\infty = [\cos\alpha, \sin\alpha]$$

$$\nabla \phi \cdot n = \rho_\infty U_\infty \cdot n$$

Two-dimensional viscous analysis

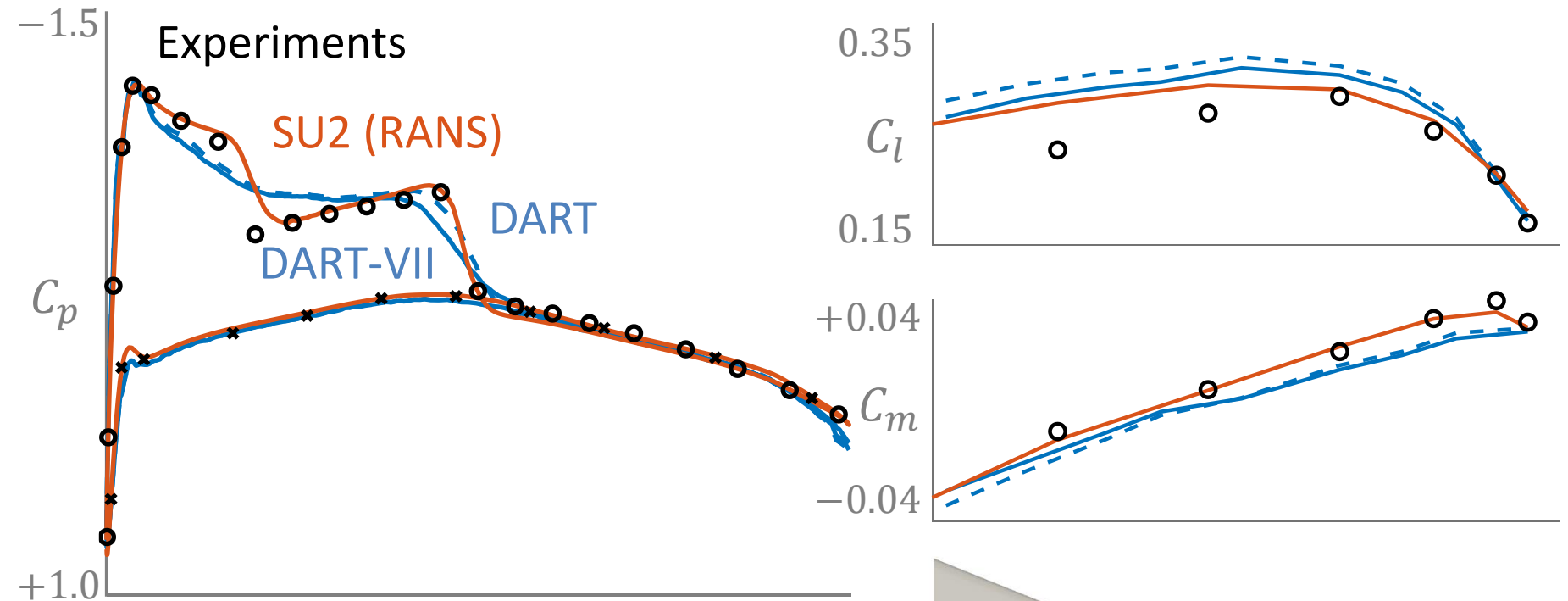


$M_\infty = 0.73$
 $Re = 6.5 \text{ M}$

 2.3°



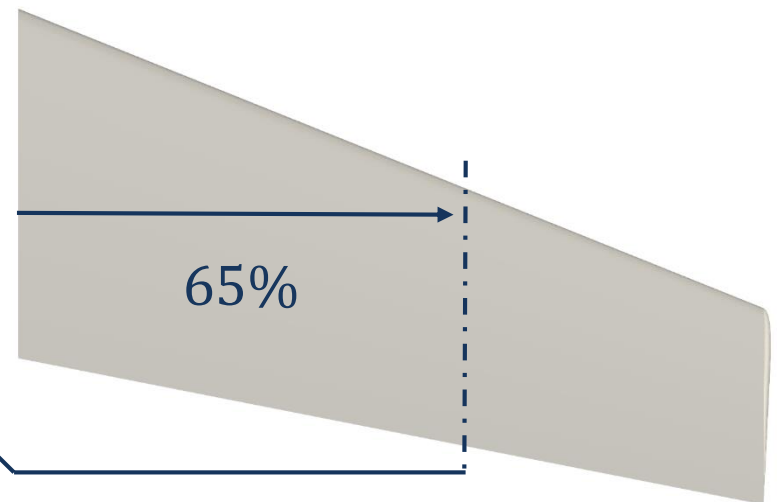
Three-dimensional viscous analysis



3.1°

$$M_\infty = 0.94$$

$$Re = 11.7 \text{ M}$$



Outline

Optimization

- Mathematical formulation
- Gradients calculation

Static aeroelasticity

- Steady aerodynamic modeling
- DART

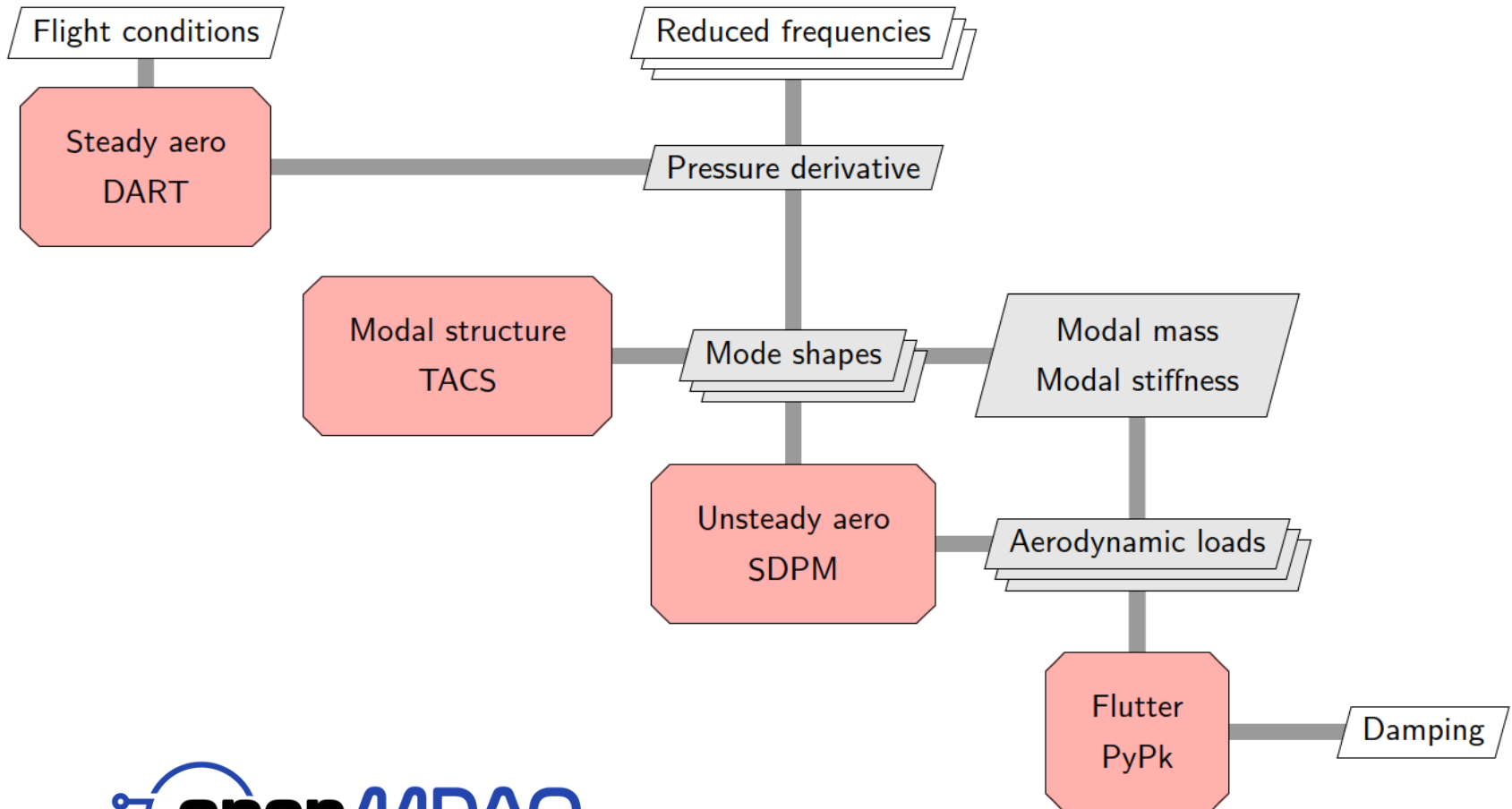
Dynamic aeroelasticity

- Unsteady aerodynamic and flutter modeling
- SDPM and PyPk

Benchmark case

- Problem description
- Optimization results

Analysis process



<https://openmdao.org>

<https://gitlab.uliege.be/am-dept/omflut>

Unsteady aerodynamics for flutter

Flutter equation

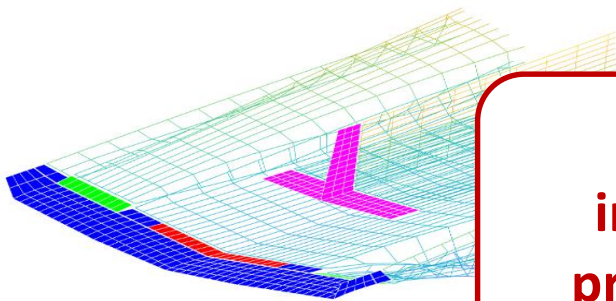
$$M\ddot{q}(t) + C\dot{q}(t) + Kq(t) = F(t) \quad \rightarrow \quad (p^2(\omega)M_r + K_r - Q_r(\omega))q_r = 0$$

Boundary element method

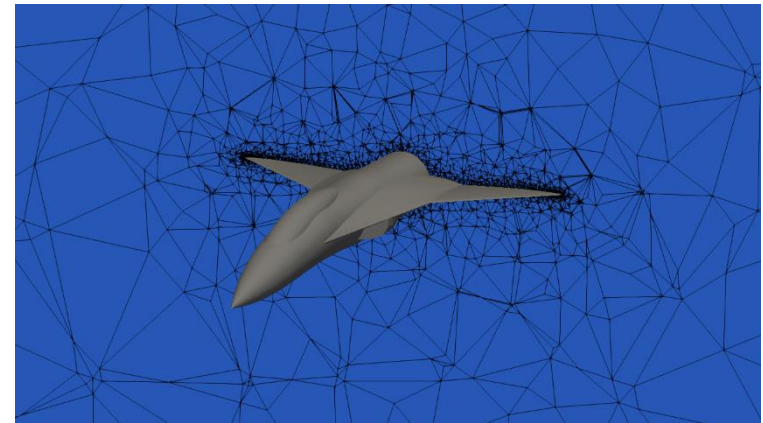
- Only boundary is discretized
- Linear equations only
- Panel/lattice methods

Field method

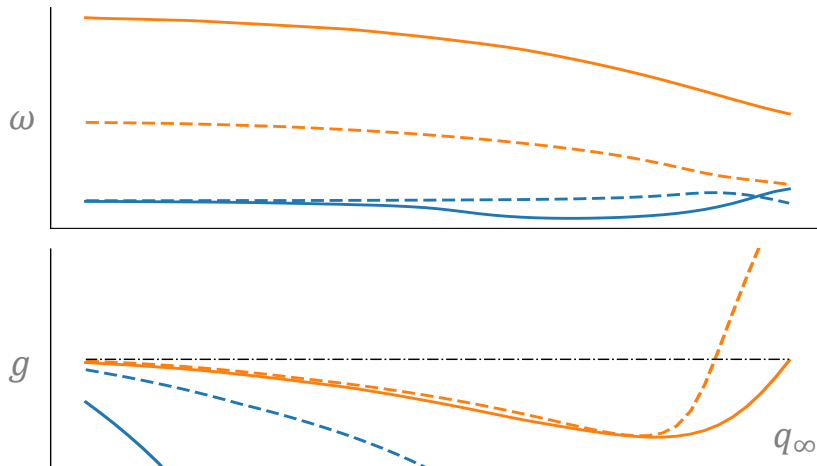
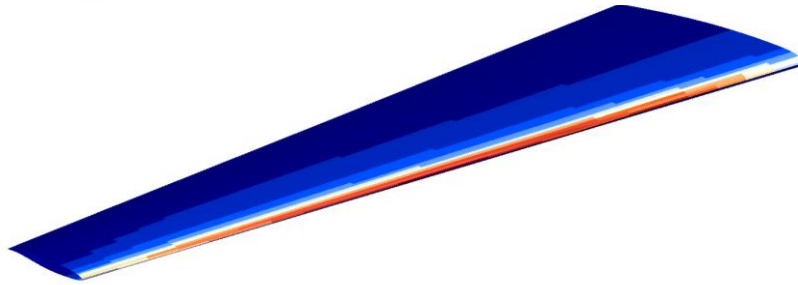
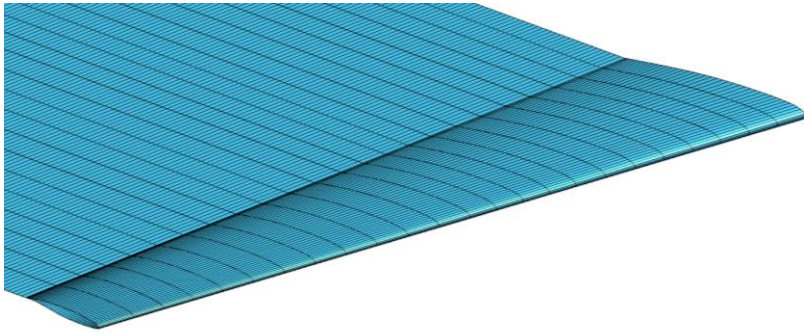
- Whole field is discretized
- Linear and nonlinear equations
- Finite volume/element methods



**Current
industrial
practice for
aeroelastic
computations**



SDPM and PyPk



Source and Doublet Panel Method

- Unsteady potential formulation
- Panel discretization
- Unstructured quadrangular grid
- Transonic correction
- Reverse automatic differentiation
- C++ with Python API

<https://gitlab.uliege.be/am-dept/sdpm>

Python p-k flutter methods

- Standard and non-iterative p-k
- Mode tracking
- Analytical gradients
- Python

<https://gitlab.uliege.be/am-dept/pypk>

Unsteady source and doublet panel method

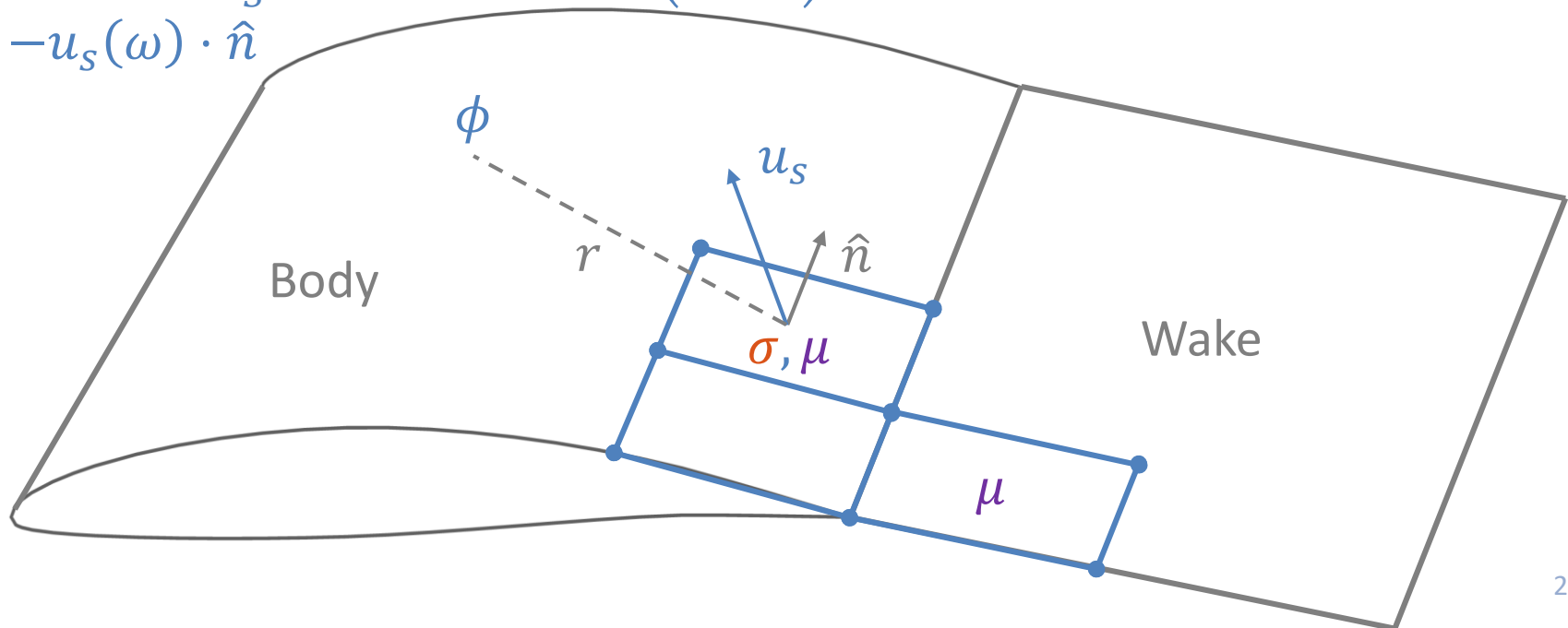
Formulation

$$\phi(\omega) = -\frac{1}{4\pi} \int_S \hat{n} \cdot \left(\nabla \phi \frac{E(\omega)}{r} - \phi \nabla \left(\frac{E(\omega)}{r} \right) \right) dS$$

Panel discretization

$$\phi(\omega) = -\frac{1}{4\pi} \int_S \sigma \frac{E(\omega)}{r} - \mu \hat{n} \cdot \nabla \left(\frac{E(\omega)}{r} \right) dS$$

$$\sigma = -u_s(\omega) \cdot \hat{n}$$



Transonic correction

Linearized pressure coefficient derivative

$$c_p(0) \simeq \frac{2}{\beta} \left(\partial_x^S \mu(0) + \hat{n}_x \sigma(0) \right)$$

$$\partial_\alpha c_p(0) \simeq \frac{2}{\beta} \left(\partial N_x^S A^{-1} B \hat{n}_z + \hat{n}_x \hat{n}_z \right)$$

$$\partial_\alpha c_p^{\text{ref}}(0) \simeq \frac{2}{\beta} \left(\partial N_x^S D^{\text{corr}} A^{-1} B \hat{n}_z + \hat{n}_x \hat{n}_z \right)$$

Procedure

1. Compute pressure derivative $\partial_\alpha c_p^{\text{ref}}(0)$ from steady CFD
2. Solve for correction: $\frac{2}{\beta} \partial N_x^S D^{\text{corr}} A^{-1} B \hat{n}_z = \partial_\alpha c_p^{\text{ref}}(0) - \hat{n}_x \hat{n}_z$
3. Compute doublets: $\mu(\omega) = A^{-1} B \sigma(\omega, u_{S_{x,y}}) + D^{\text{corr}} A^{-1} B \sigma(\omega, u_{S_z})$

Flutter solution

Flutter equation

$$\left(\frac{u_\infty^2}{l_{\text{ref}}^2} p^2 M + K - \frac{1}{2} \rho_\infty u_\infty^2 Q(k) \right) q = 0$$
$$p = gk + ik$$

Frequency matching (p-k)

1. Guess $k = \omega_N \frac{l_{\text{ref}}}{u_\infty}$
2. Compute $Q(k)$
3. Solve eigenvalue problem for p
4. Compute $k = \Im(p)$
5. Repeat 2-4 until k has converged



Computation of Q is costly

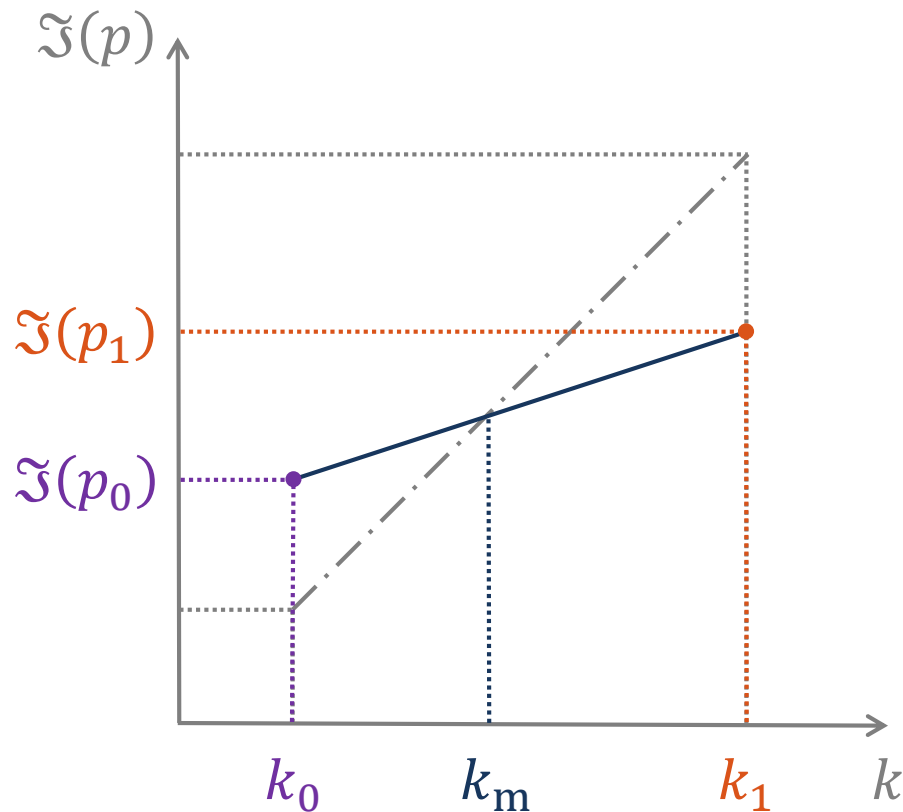


Interpolate Q or k

Non-iterative p-k method

Algorithm

1. Compute $Q_i(k_i)$ for a set of k_i
2. Solve eigenvalue problem for p_i
3. Interpolate k_m such that $\Im(p_m) - k_m = 0$



AGARD 445.6 wing



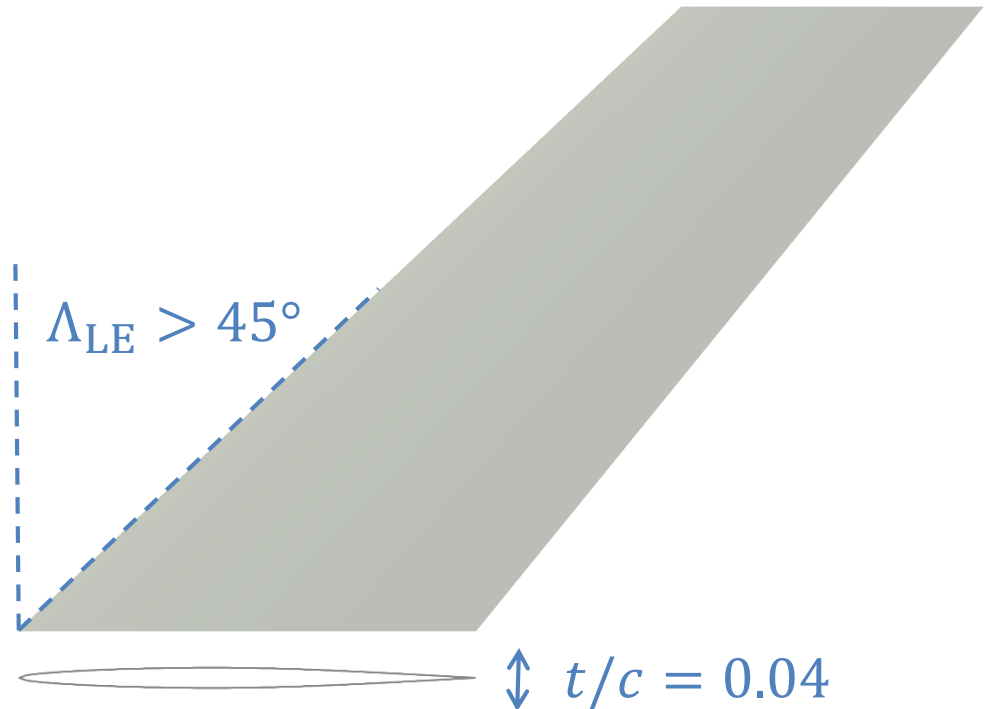
$$M_{\infty,1} = 0.50$$

$$M_{\infty,2} = 0.68$$

$$M_{\infty,3} = 0.90$$

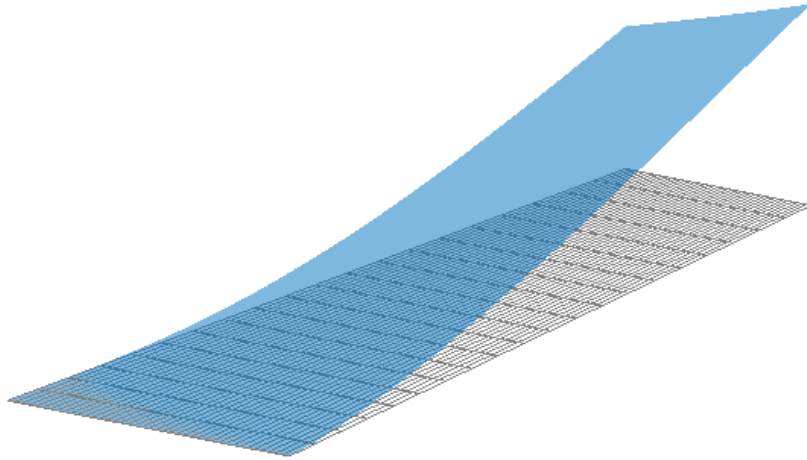
$$M_{\infty,4} = 0.96$$

$$\alpha = 0^\circ$$

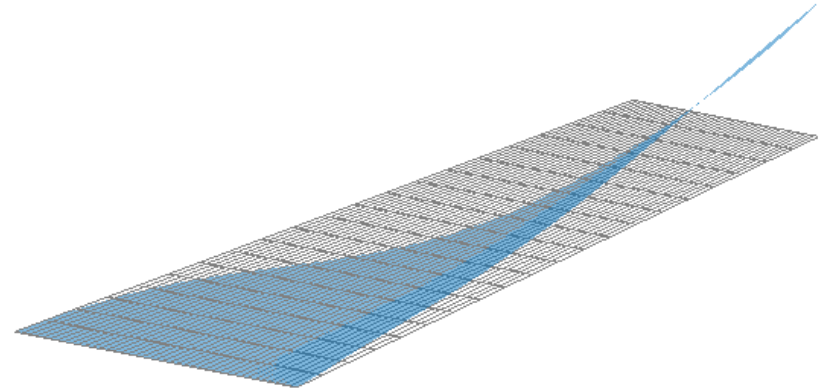


Mode shapes

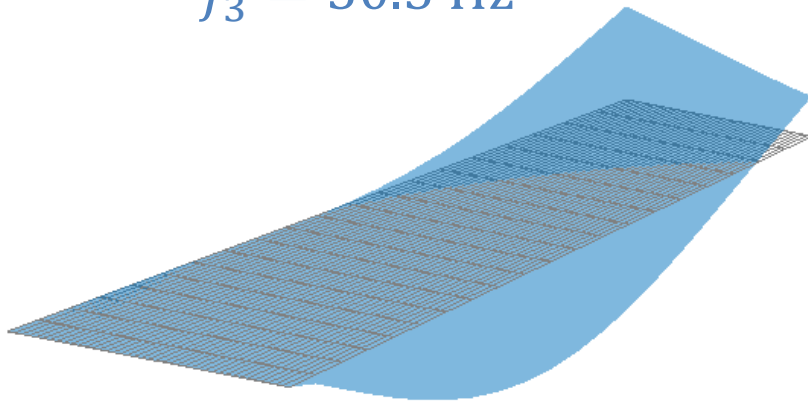
$$f_1 = 9.7 \text{ Hz}$$



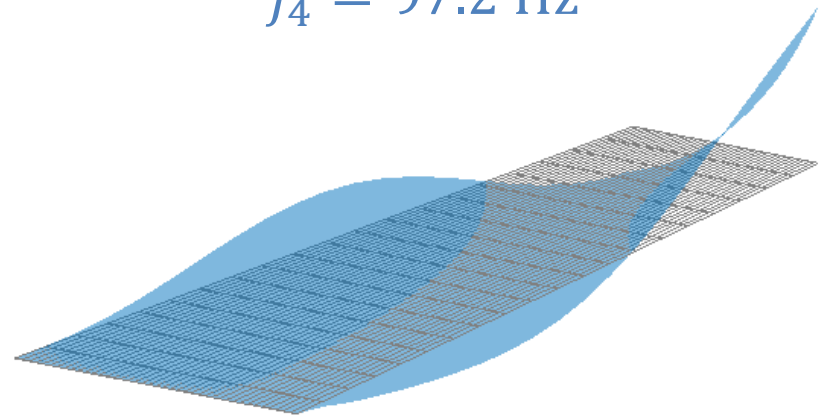
$$f_2 = 40.2 \text{ Hz}$$



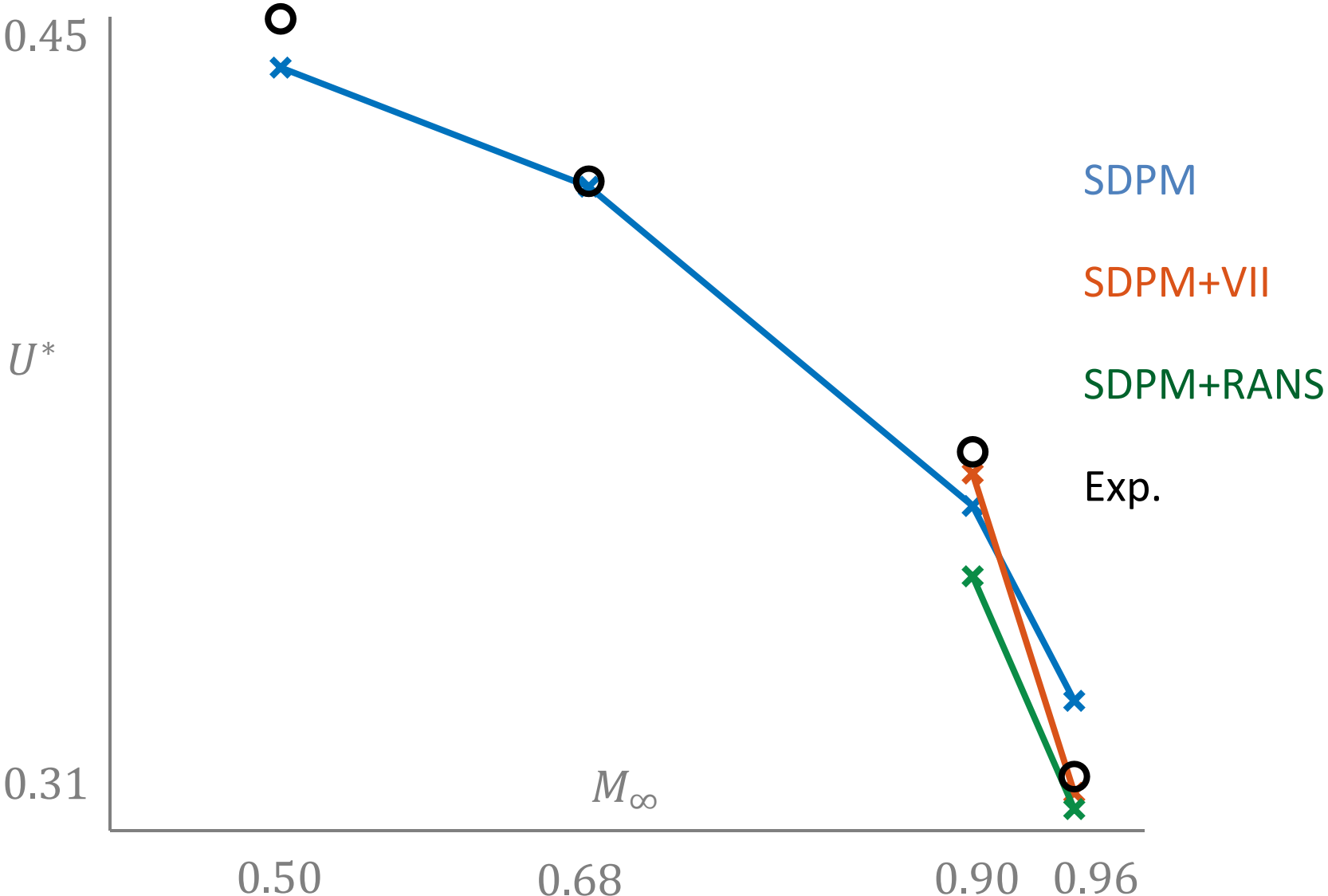
$$f_3 = 50.5 \text{ Hz}$$



$$f_4 = 97.2 \text{ Hz}$$



Flutter boundary



Outline

Optimization

- Mathematical formulation
- Gradients calculation

Static aeroelasticity

- Steady aerodynamic modeling
- DART

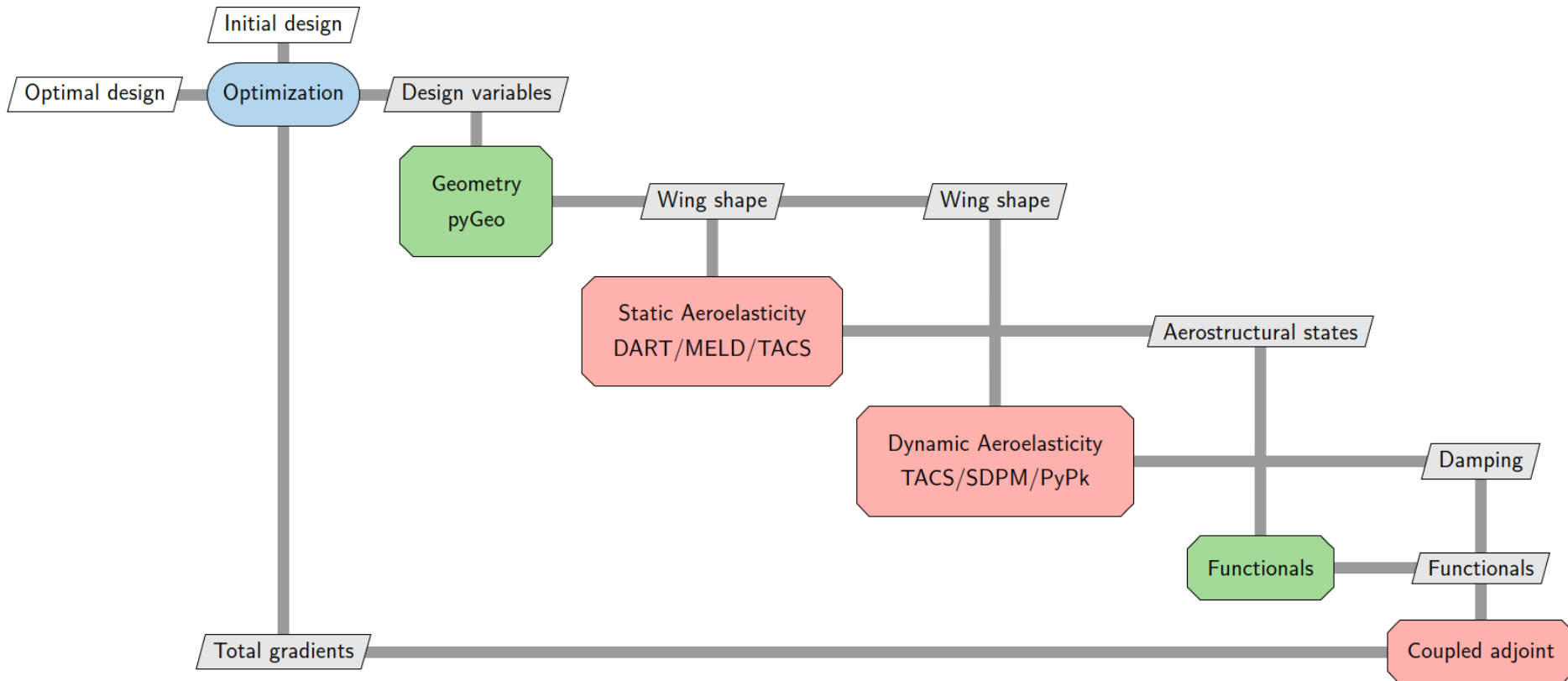
Dynamic aeroelasticity

- Unsteady aerodynamic and flutter modeling
- SDPM and PyPk

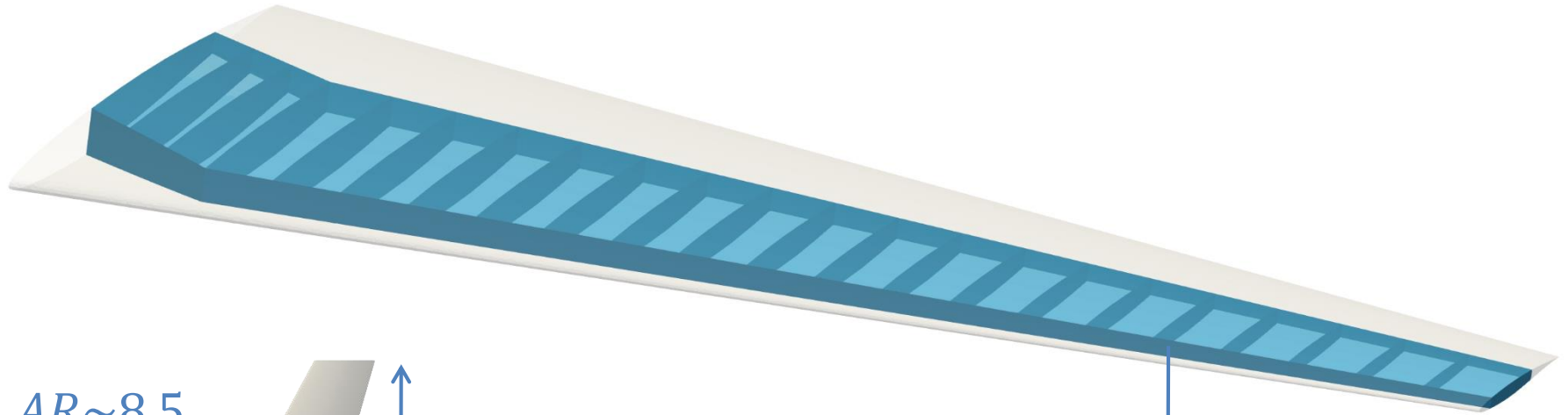
Benchmark case

- Problem description
- Optimization results

Optimization framework



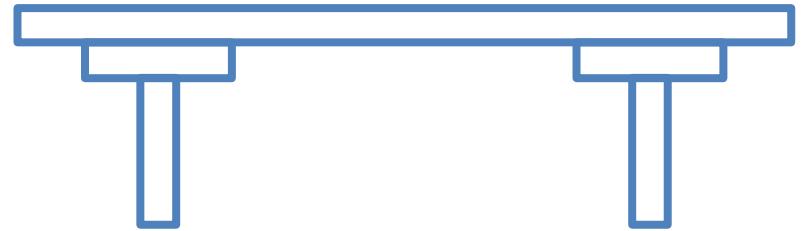
RAE wing



$AR \sim 8.5$
 $\lambda \sim 0.33$



$s = 14 \text{ m}$

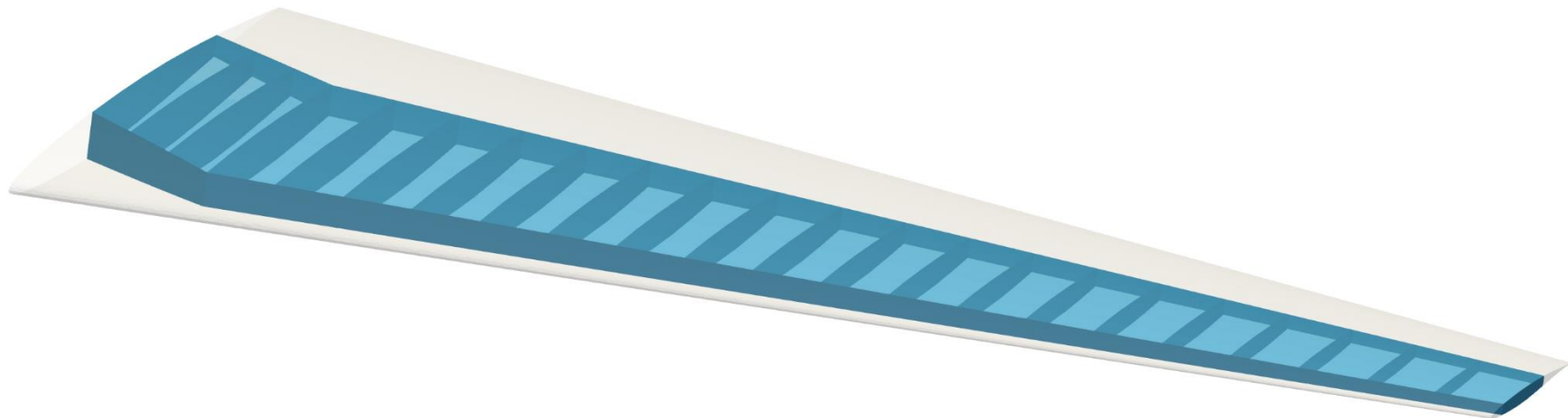


Skin/stiff: $[0_{0.45} / -45_{0.22} / +45_{0.22} / 90_{0.11}]$

Spar/rib: $[0_{0.10} / -45_{0.35} / +45_{0.35} / 90_{0.20}]$

RAE 2822 $\updownarrow t/c = 0.12$

Flight conditions



Cruise

$M_{\infty} = 0.82$ — FL 350

$n = 1.0$

Maneuver

$M_{\infty} = 0.78$ — FL 200

$n = 2.5$

Flutter (low-speed)

$M_{\infty} = 0.50$

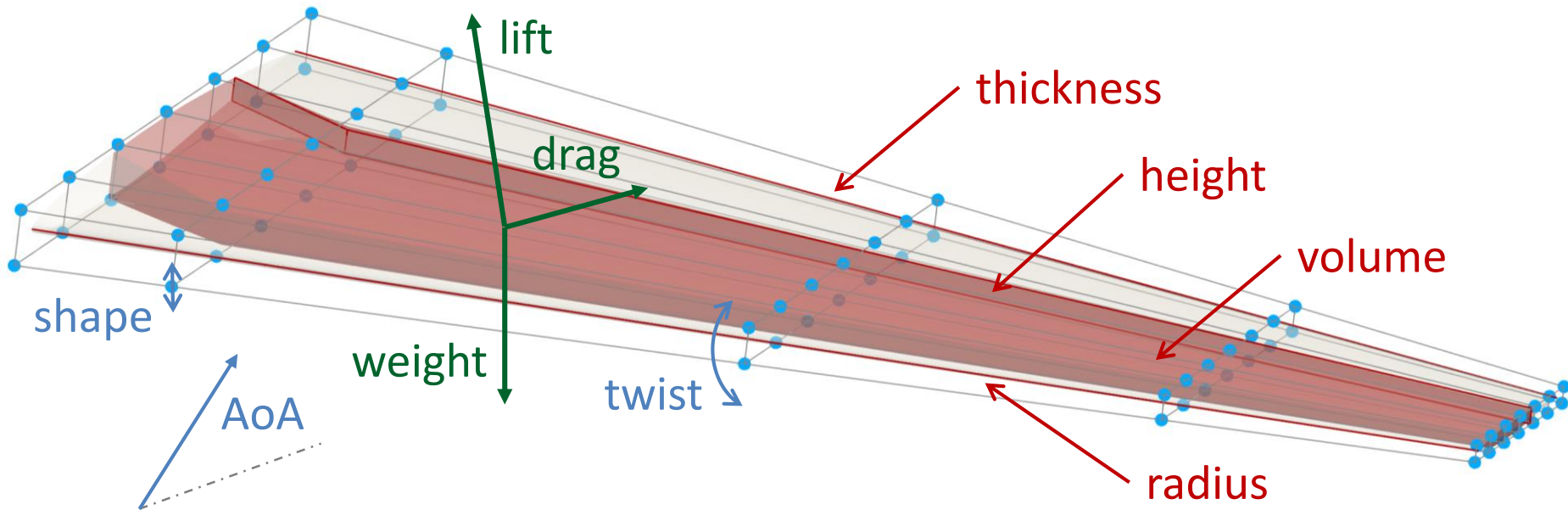
FL = $[-200, +400]$

Flutter (high-speed)

$M_{\infty} = 0.95$

FL = $[-200, +400]$

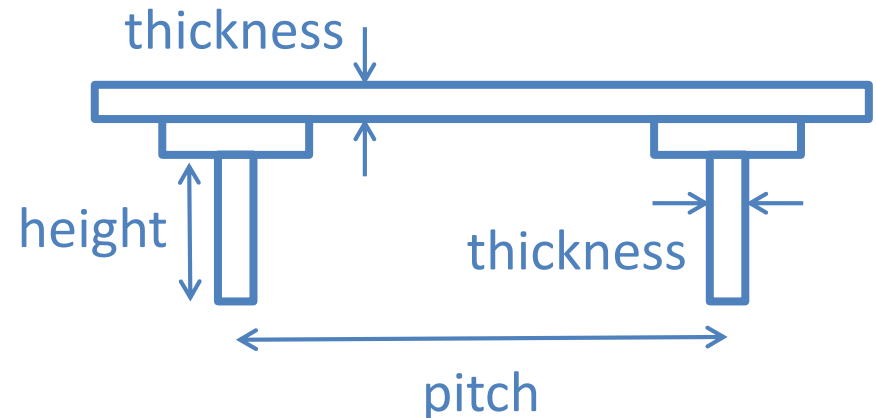
Optimization problem formulation



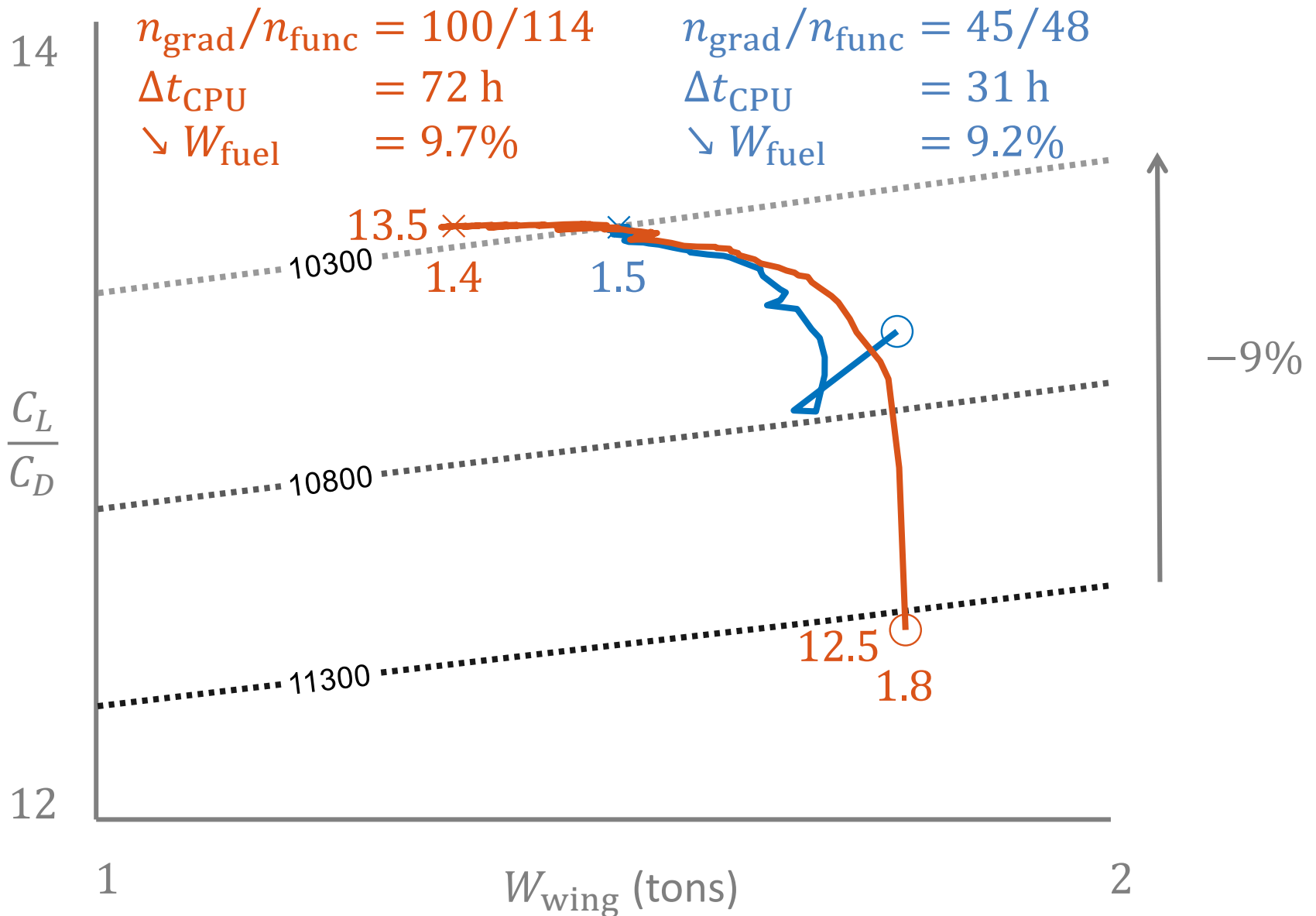
min fuel = Breguet(lift, drag, weight)

w. r. t. AoA, shape, twist, structure

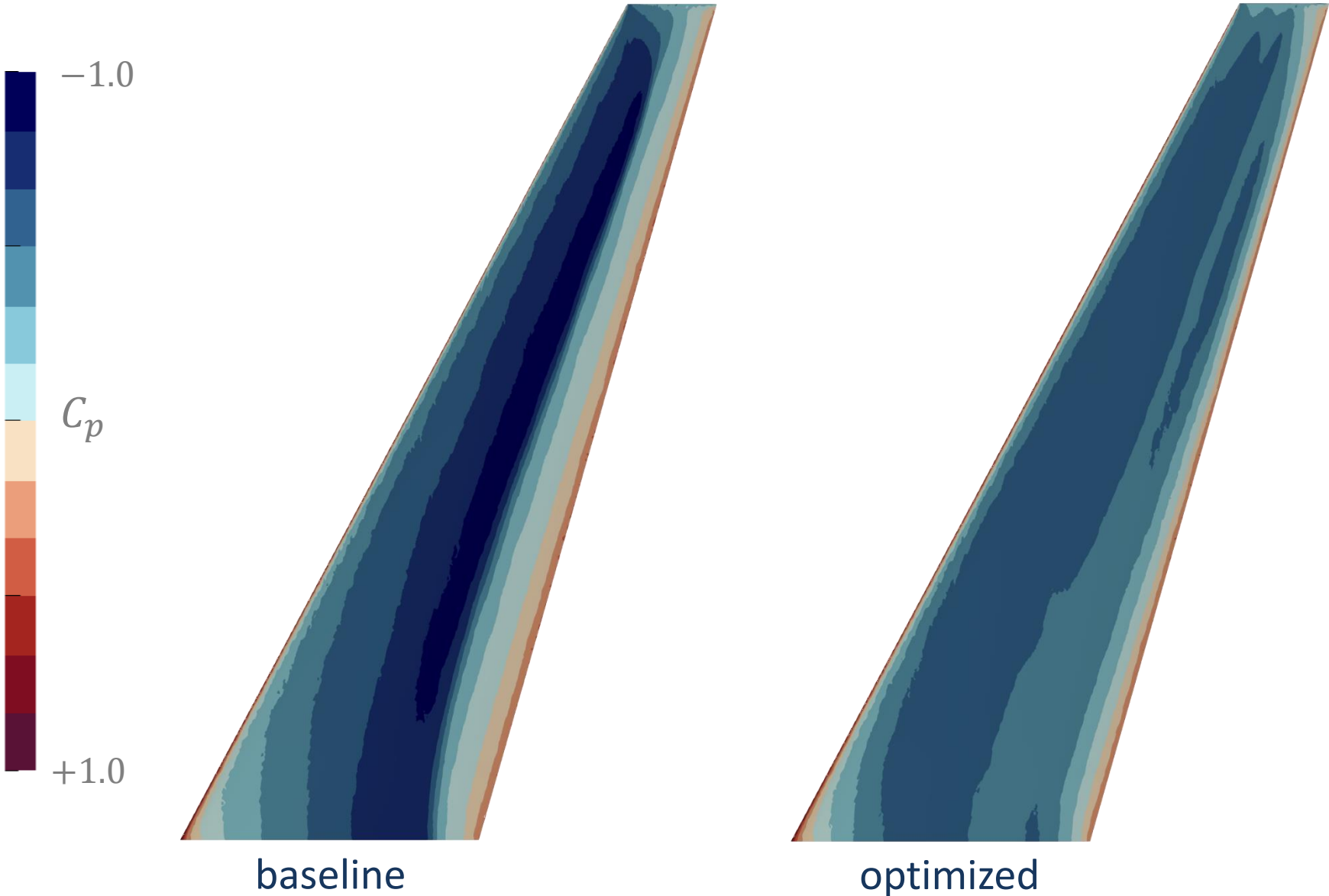
s. t. load factor
structural failure
~flutter
geometry



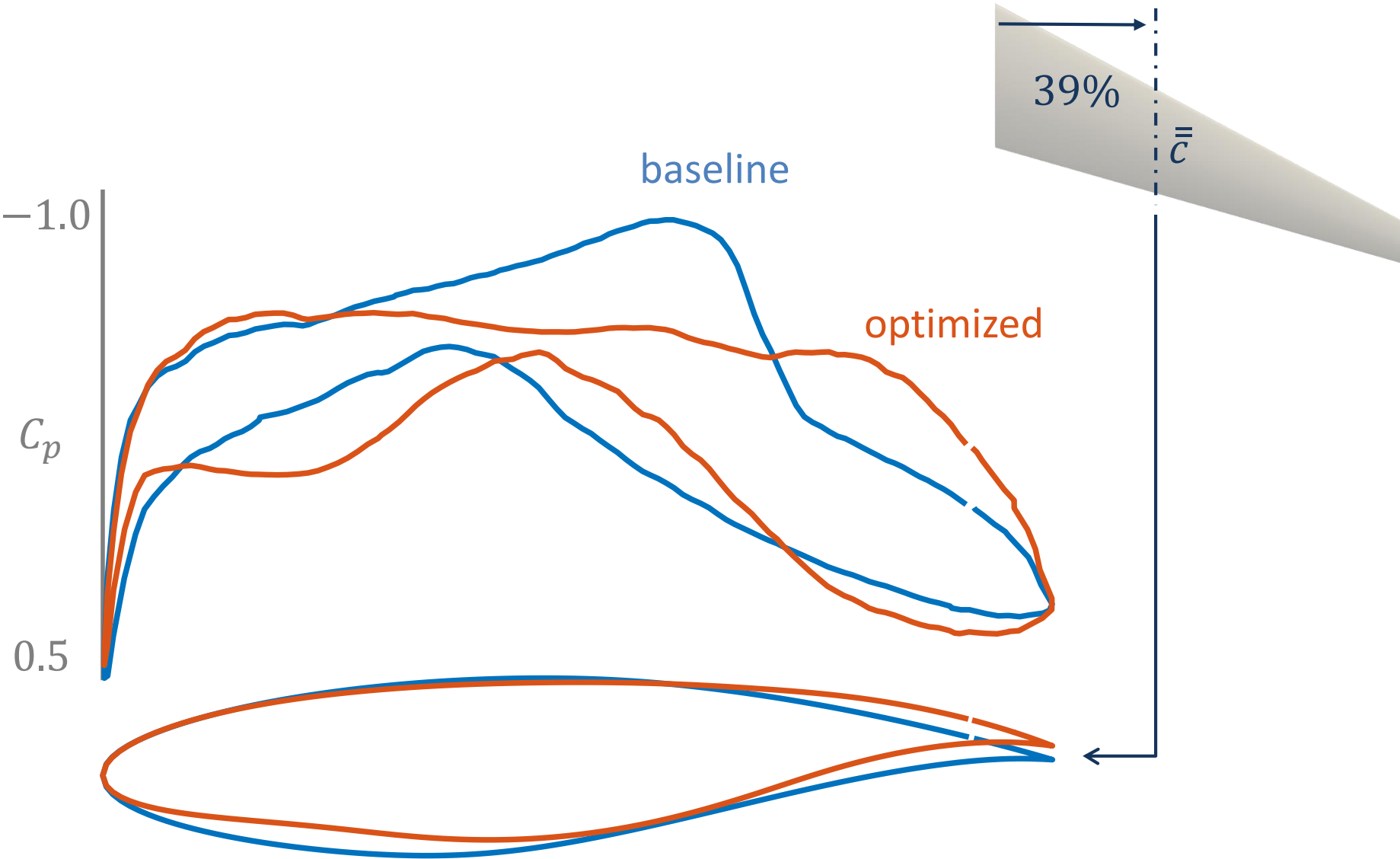
Fuel burn



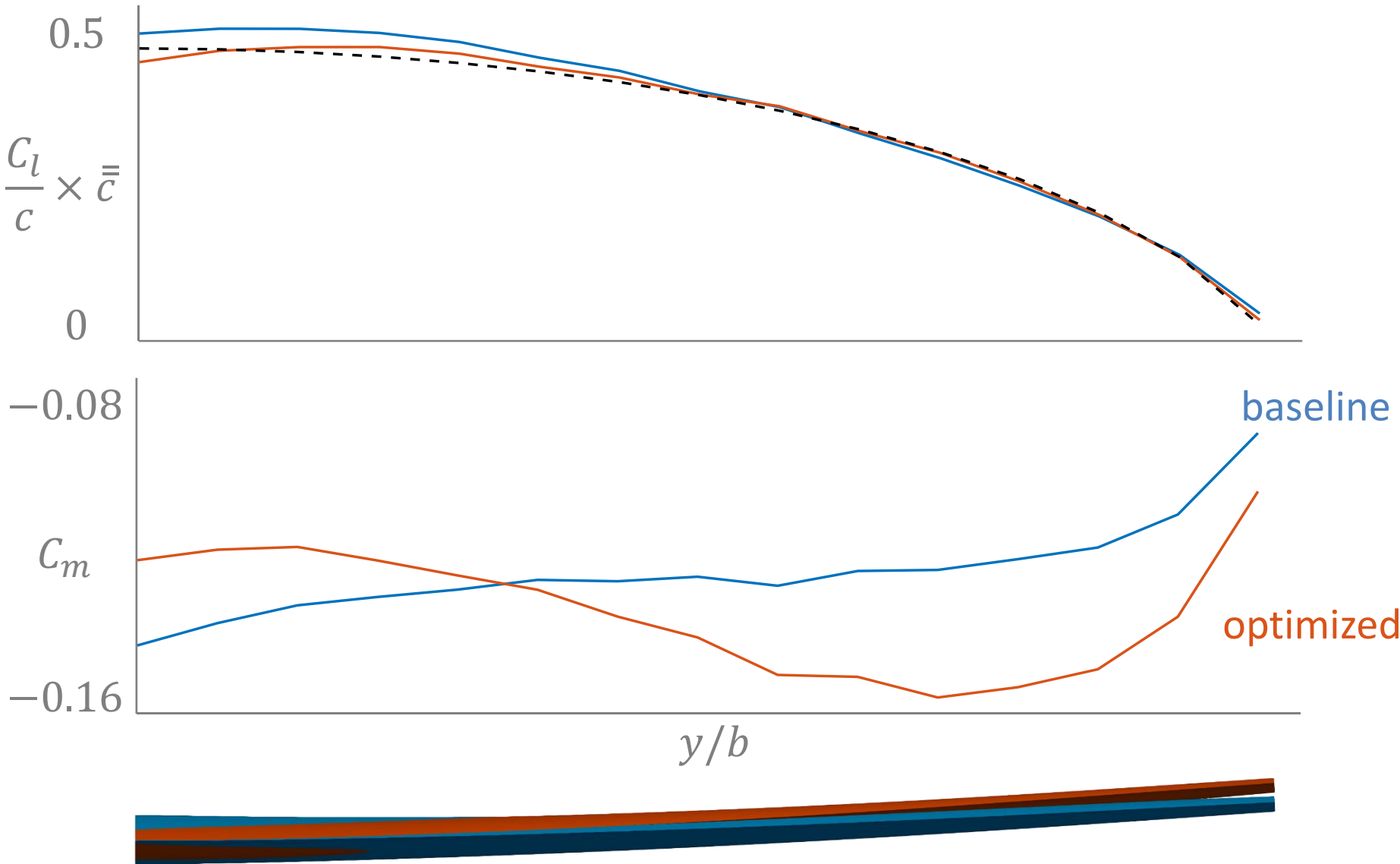
Pressure contour – cruise



Pressure distribution – cruise

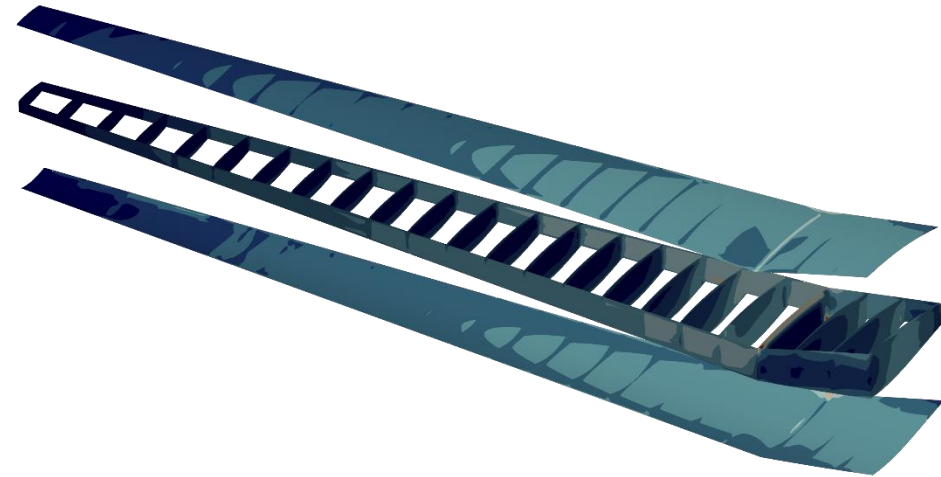


Loads distribution – cruise

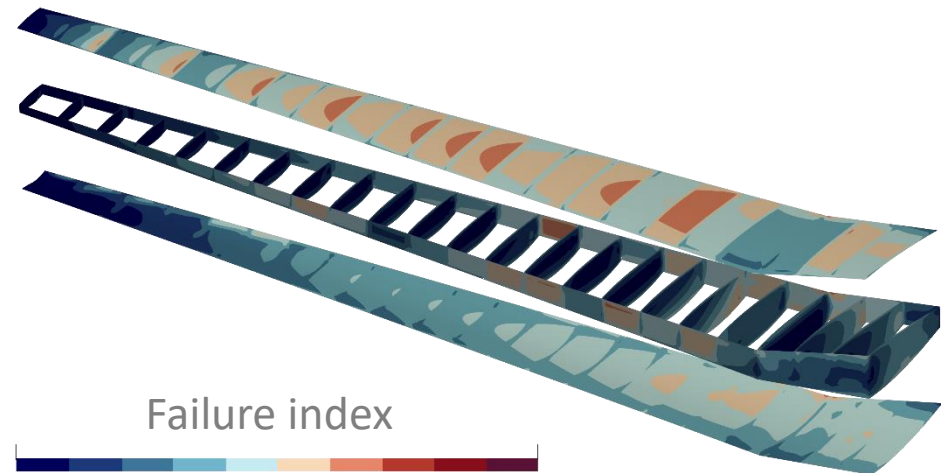


Thickness and failure index – maneuver

baseline



optimized



Equivalent thickness

Failure index

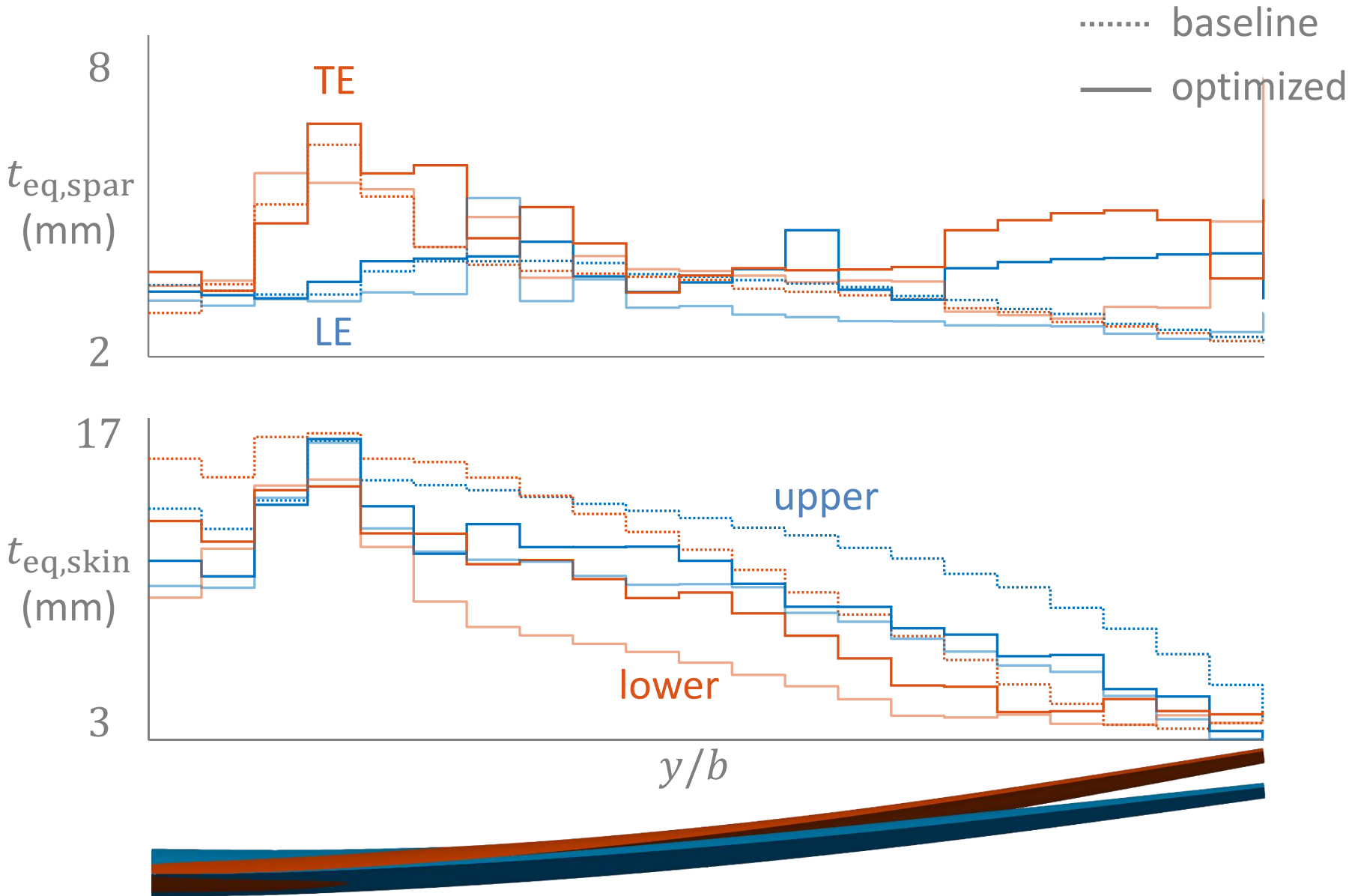
2 mm

16 mm

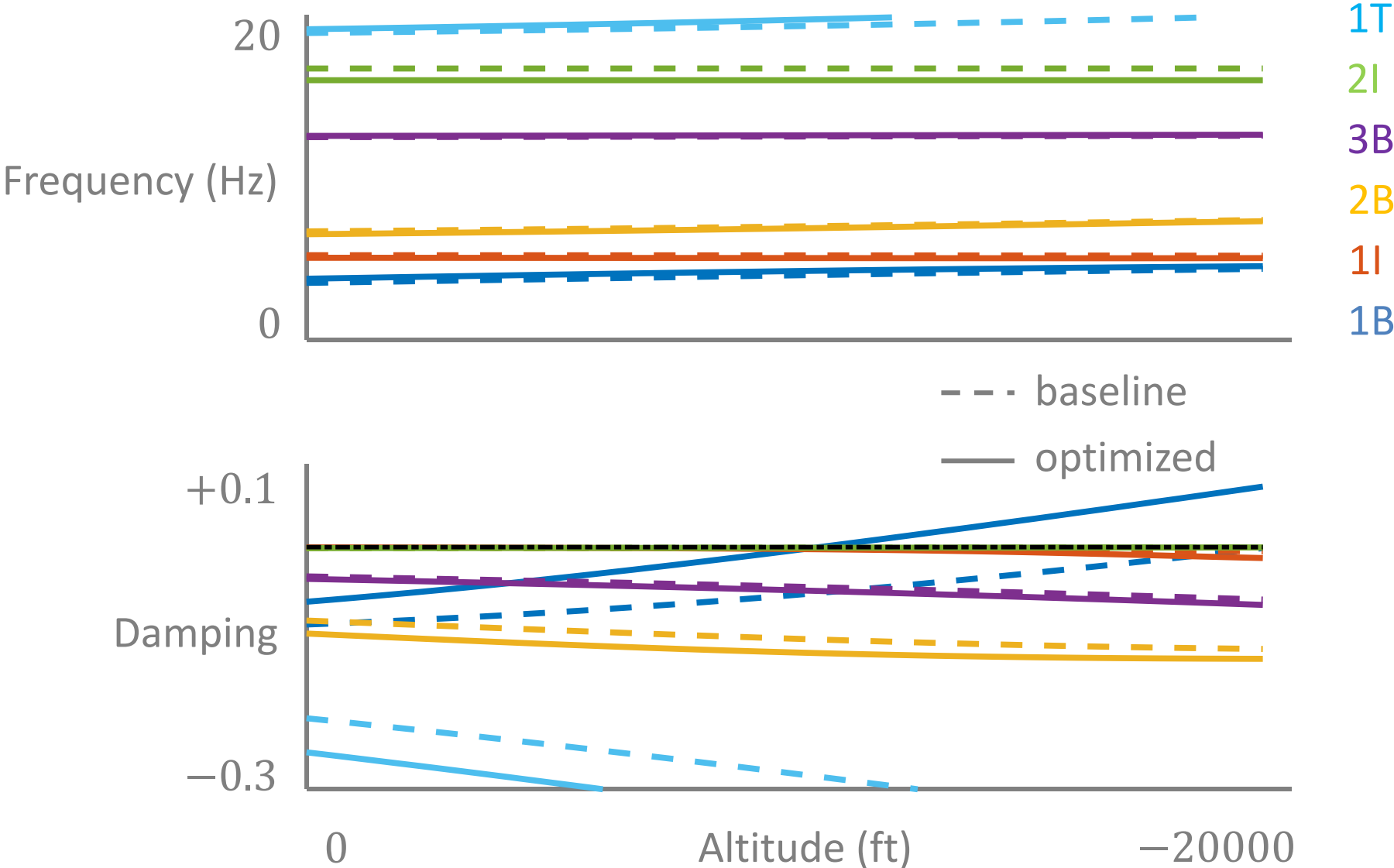
0.0

1.0

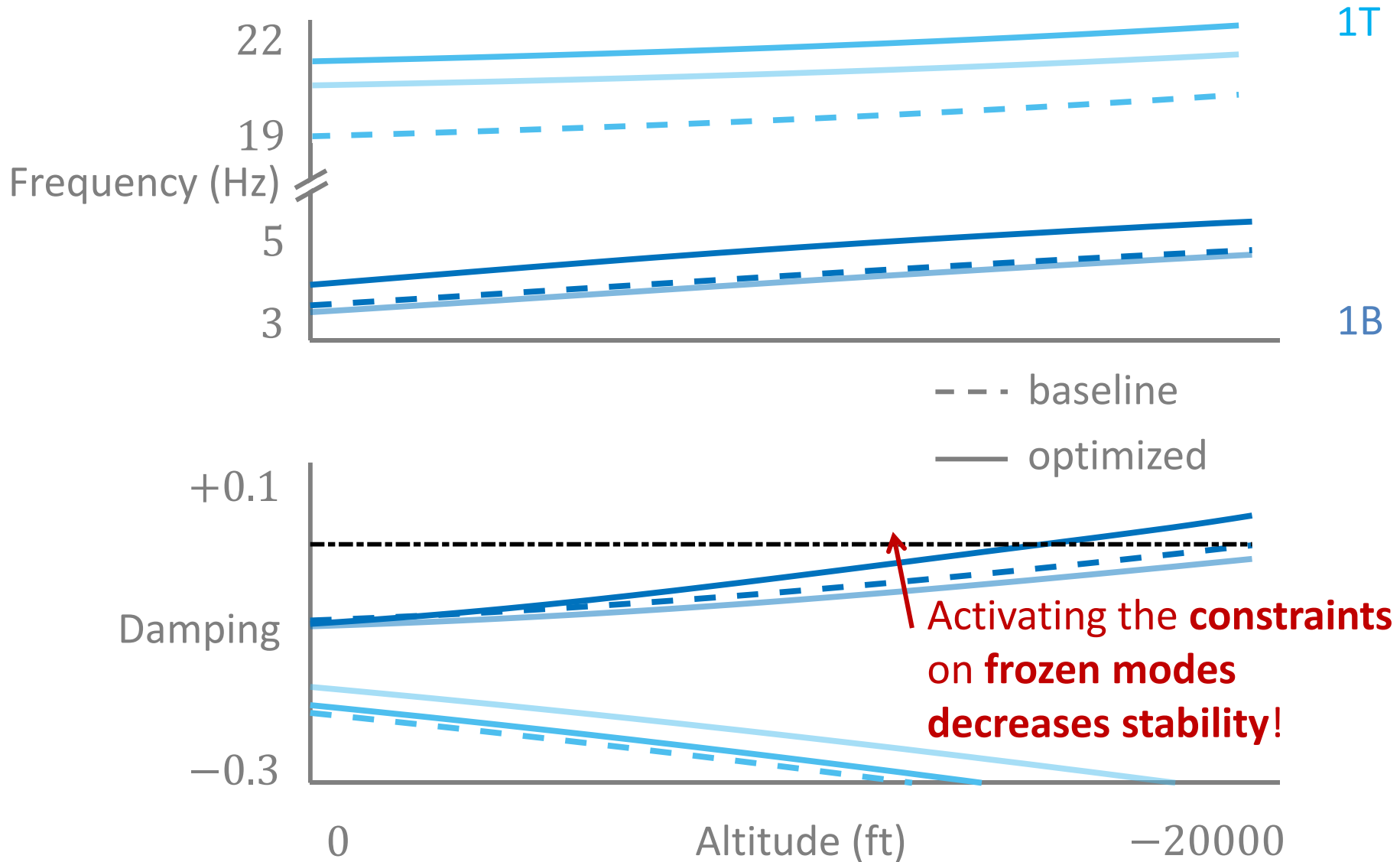
Equivalent thickness – maneuver



Modes migration – high-speed



Effect of flutter constraints – high-speed



Conclusion

Main points

- **Aerostructural optimization** is performed in **preliminary aircraft design**; choosing the **appropriate numerical models and methods** is of paramount importance
- **Developed DART** to **quickly** calculate **steady transonic** flows
- **Developed SDPM** to **quickly** calculate **unsteady** (transonic) flows
- **Implemented NIPK** with mode tracking to calculate **flutter**
- **Interfaced** all codes with **OpenMDAO**

Main results

- **Relevant** results for **static aerostructural** calculations can be obtained within a **few days**
- **Aeroelastic stability** can be **calculated** but **not constrained** yet

Conclusion

Challenges

- Some **structural and aerodynamic partial derivatives** required to calculate **total damping derivative** are **missing**; optimization **may not converge**
- **Flutter** modeling is **simplified**; **structural states** and **transonic aerodynamics** are **not taken into account**
- **Flutter** modeling is **costly**; accounts for **a third of computational time**

Next steps

- **Integrate viscous-inviscid interaction** in static optimization
- **Implement missing damping derivatives** for flutter constraint
- **Improve flutter** modeling and **reduce computational cost**
- **Improve benchmark** (optimize composite material, add push-down case, use full aircraft configuration, etc.)

ONERA seminar

Aerostructural modeling for preliminary aircraft design

Adrien Crovato – Châtillon, June 2024

