



UNIVERSIDAD  
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# Efficient thermo-mechanical modelling of cyclic loading with Chaboche type constitutive law coupled with damage

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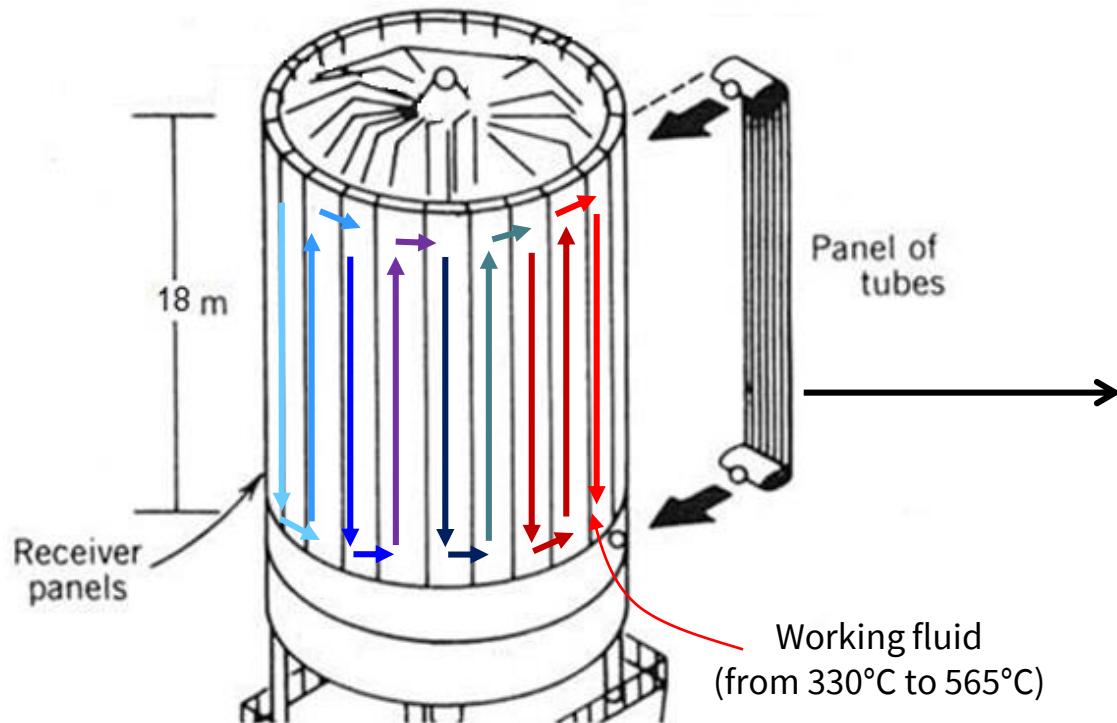
# Context: Solar power plant

Solar receivers: extreme thermo-mechanical conditions



Khi Solar One power plant (South Africa)

# Context: Solar receiver



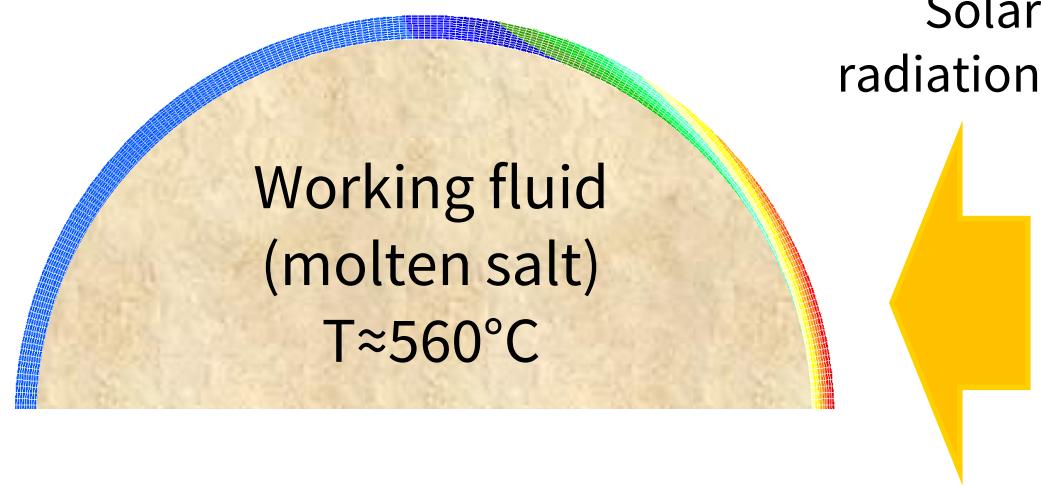
**Solar receiver**  
*(source : W.B.Stine, R.W.Harrigan,  
 Solar Energy Systems Design)*



**Panel of tubes manufactured from  
 nickel alloy sheet (Haynes 230)**  
*(source : CMI Solar)*

# Context: The tubes

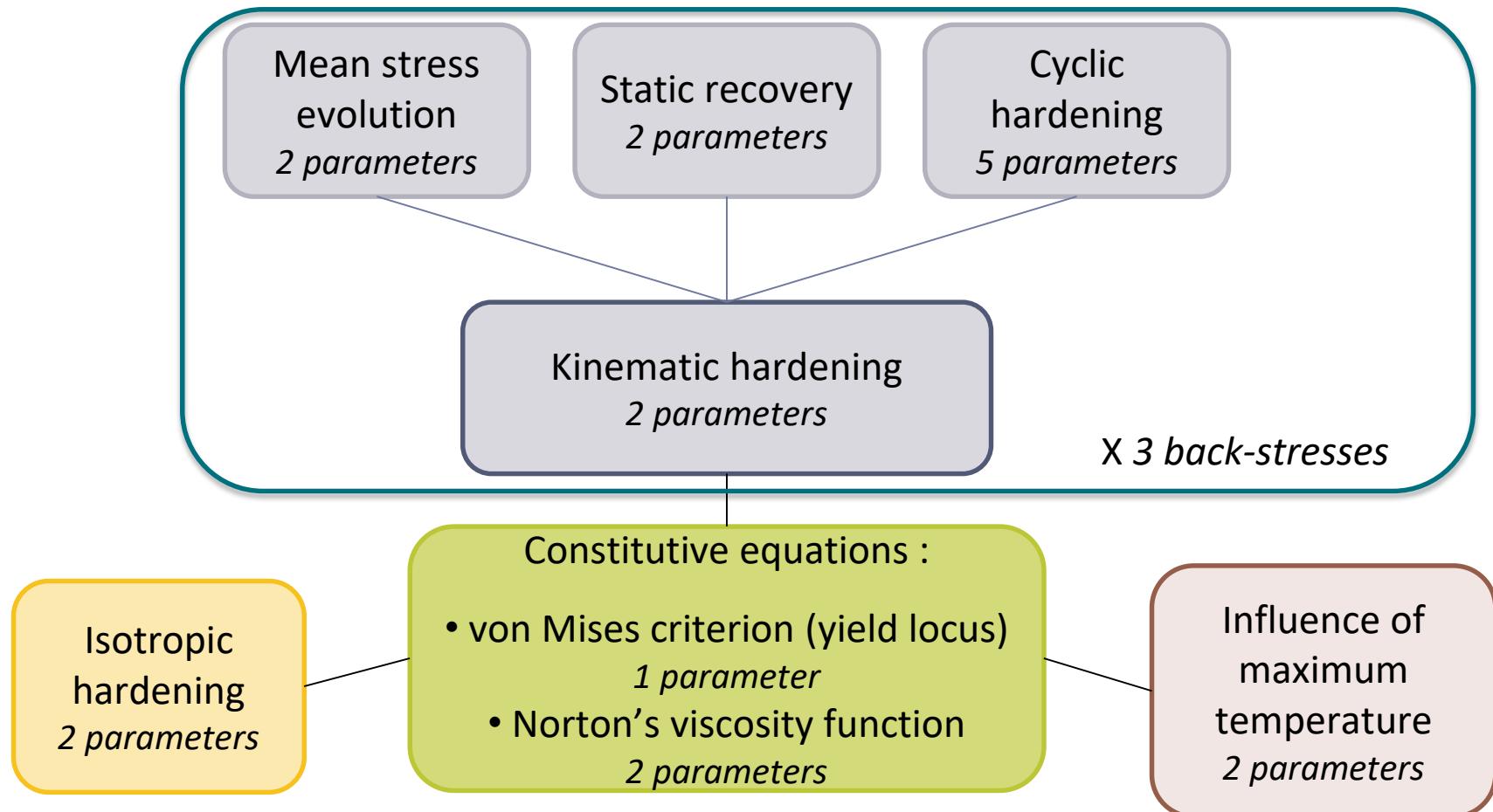
Temperature distribution in a tube  
(Lagamine FE code)



- ▶ **Fatigue + creep + corrosion**
- ▶ **Extreme Thermo-mechanical loading**  
(Haynes 230)
- ▶ **Advanced constitutive model + Damage**

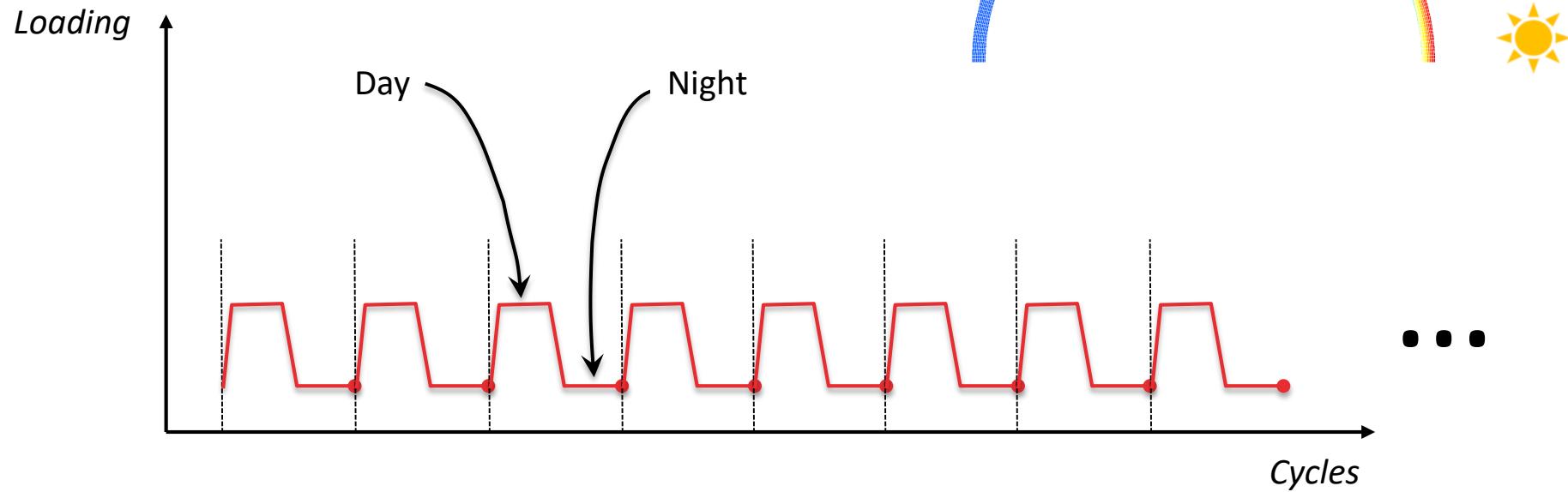


# Advanced Chaboche model



+ Lemaitre Damage (creep + fatigue + corrosion)

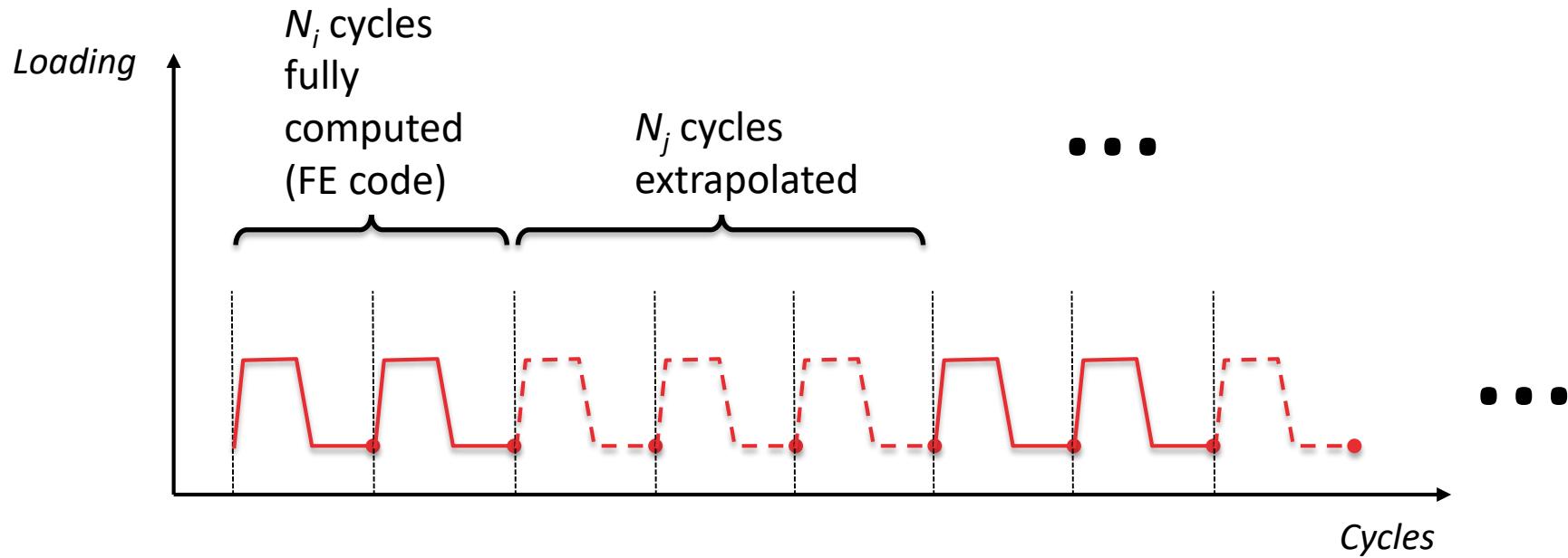
# Cycle jump approach



Target:

- ▶ 10 000 cycles  
(~25 years)
- ▶ 18m long tube  
(~200 000 FE,  $10^6$  DOFs)

# Cycle jump approach



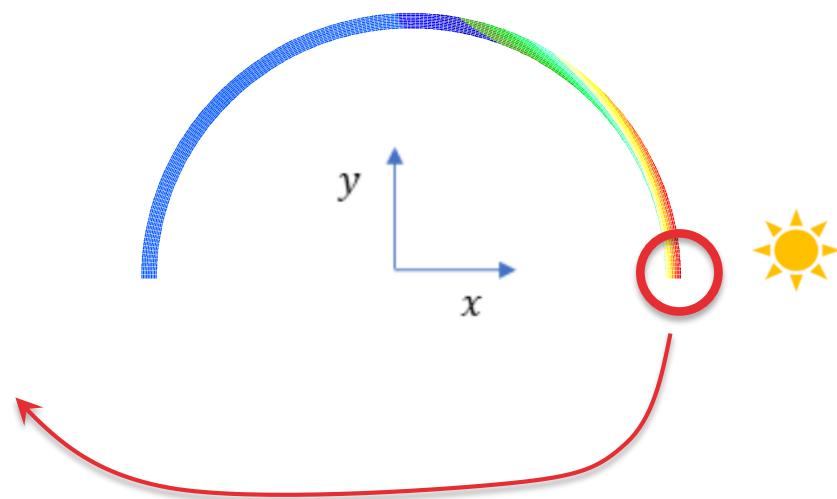
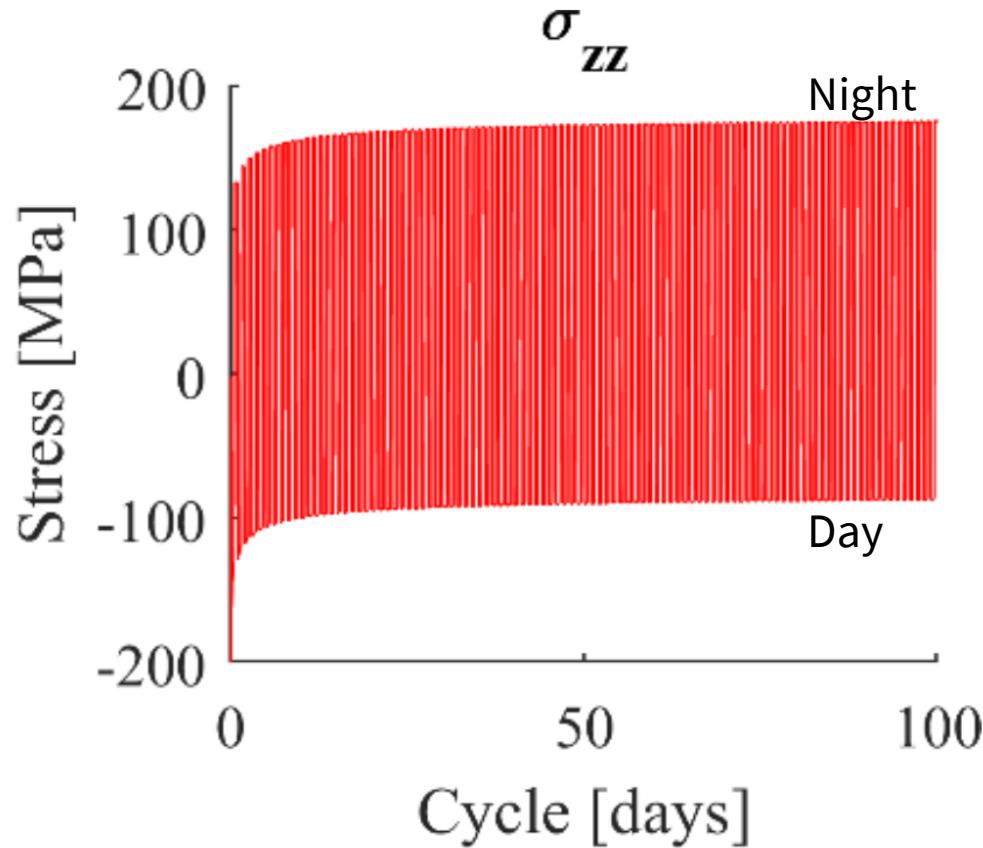
Target:

- ▶ 10 000 cycles  
(~25 years)
- ▶ 18m long tube  
(~200 000 FE,  $10^6$  DOFs)

This study:

- ▶ 5 000 cycles
- ▶ 1 slice of the tube  
(300 FE, ~3000 DOFs)

# Cycle jump: near-steady-state



→ Full FE computation for the first 100 cycles



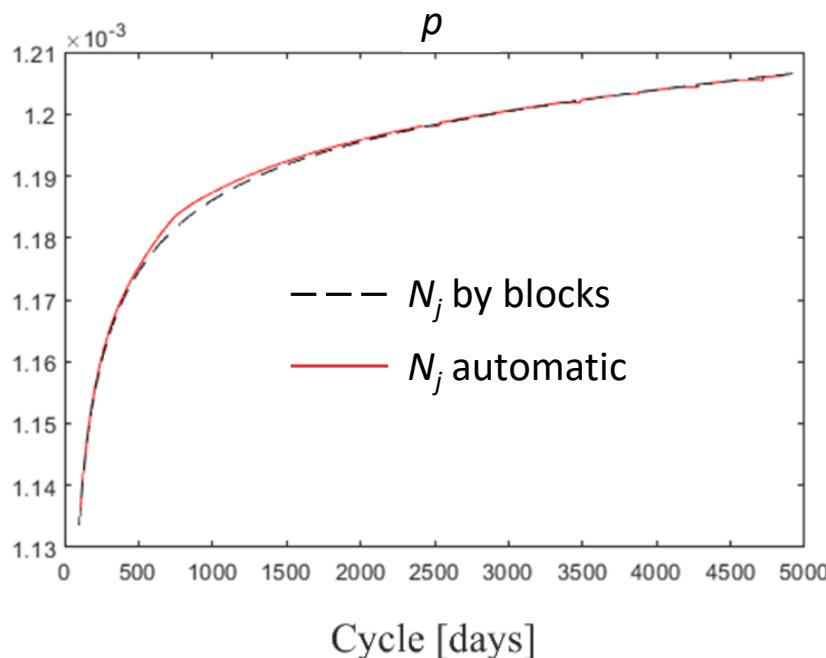
# Cycle jump: effects of $N_j$

3 solutions implemented:

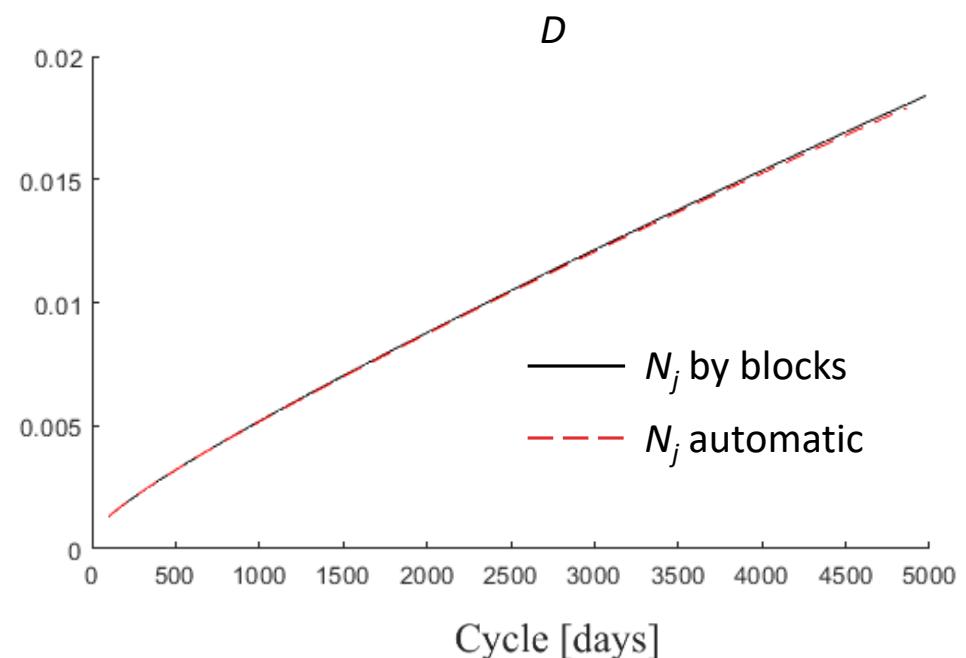
- Constant: user-defined value
- Constant by blocks: idem with predefined evolution (16...26...36)
- Automatic: adjusted by the code to limit  $\Delta D$  over the jumped cycles for all elements ( $\Delta D^{\max} = 5.10^{-4}$ )

# Cycle jump: effects of $N_j$

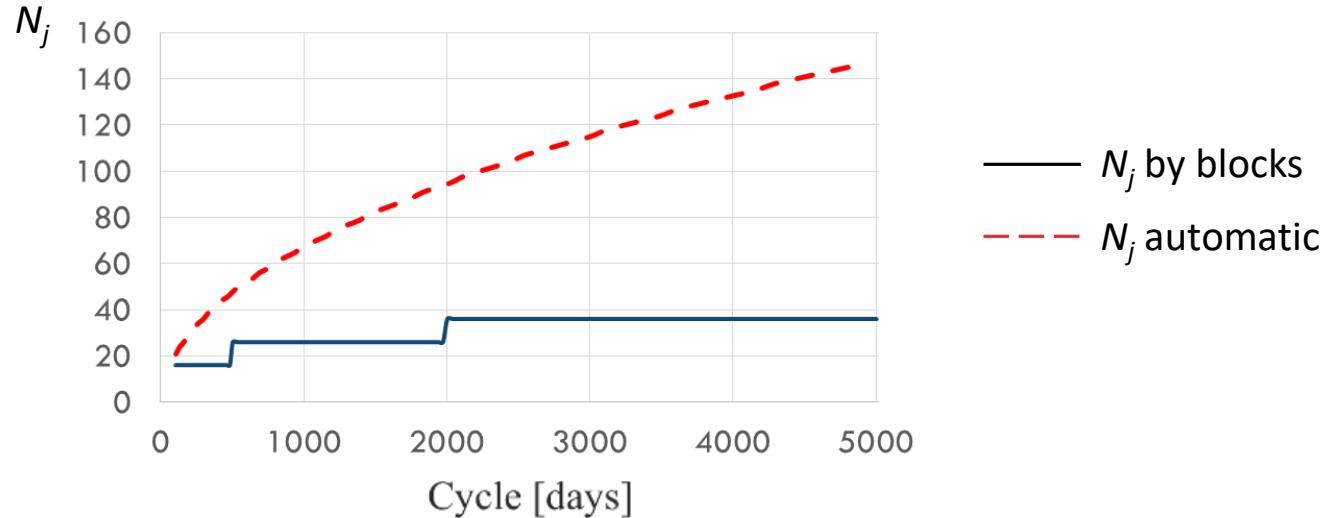
Total plastic strain



Total Damage

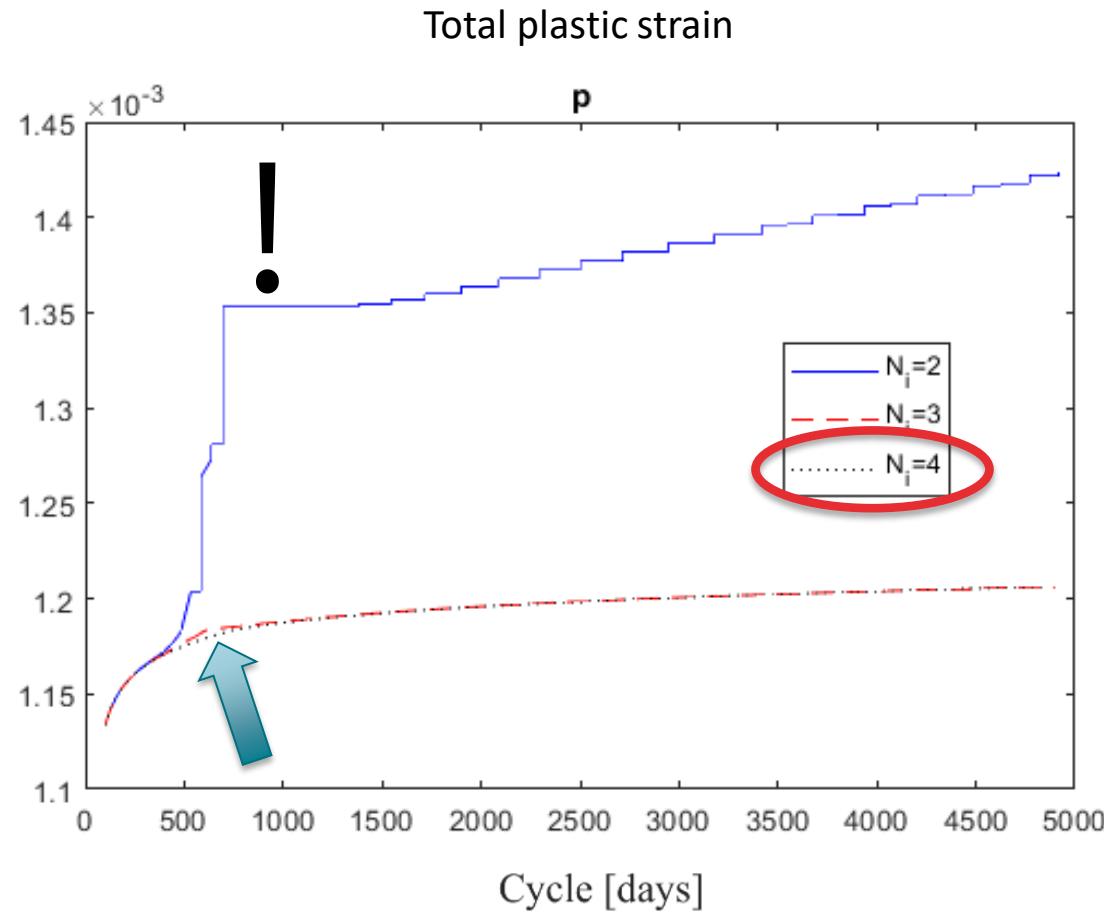


# Cycle jump: effects of $N_j$



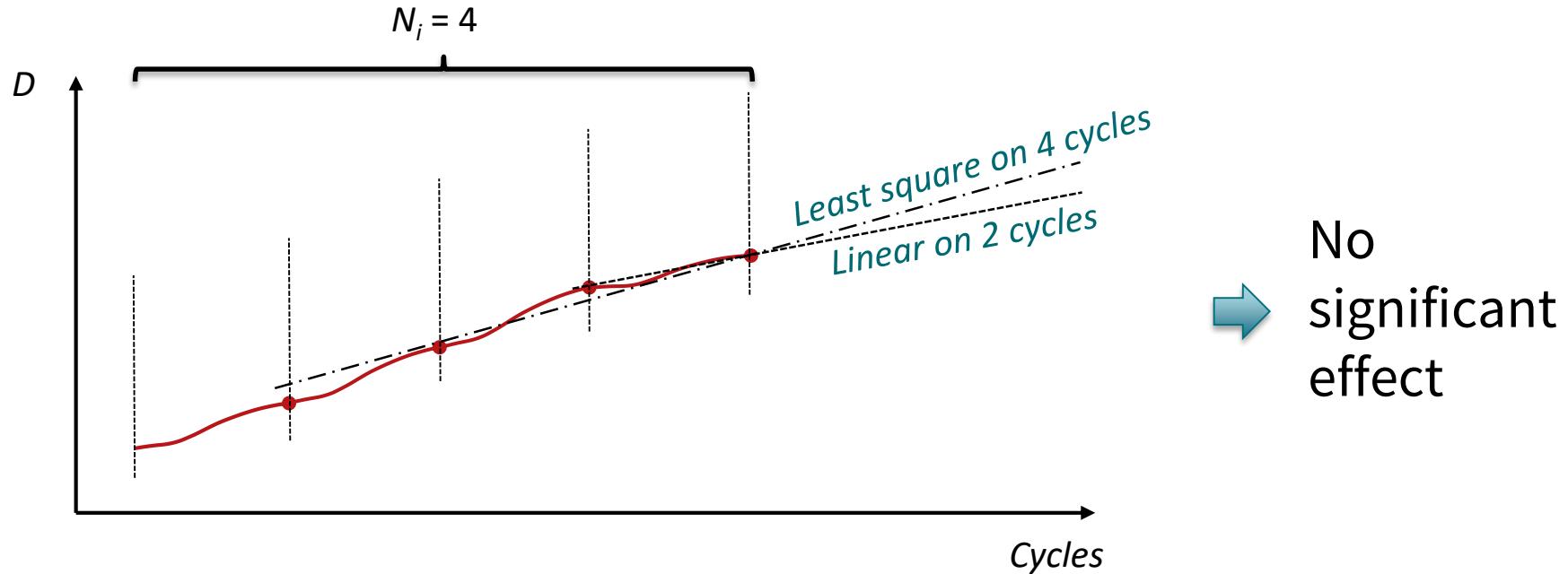
	<b>FE cycles</b>	<b>Jumped cycles</b>	<b>Total</b>	<b>Number of jumps</b>	<b>Mean <math>N_j</math></b>
$N_j$ by blocks	580	4420	5000	145	30
$N_j$ automatic	220	4780	5000	55	87

# Cycle jump: effects of $N_i$



# Cycle jump: extrapolation strategy

- Extrapolation scheme



- Variables to extrapolate

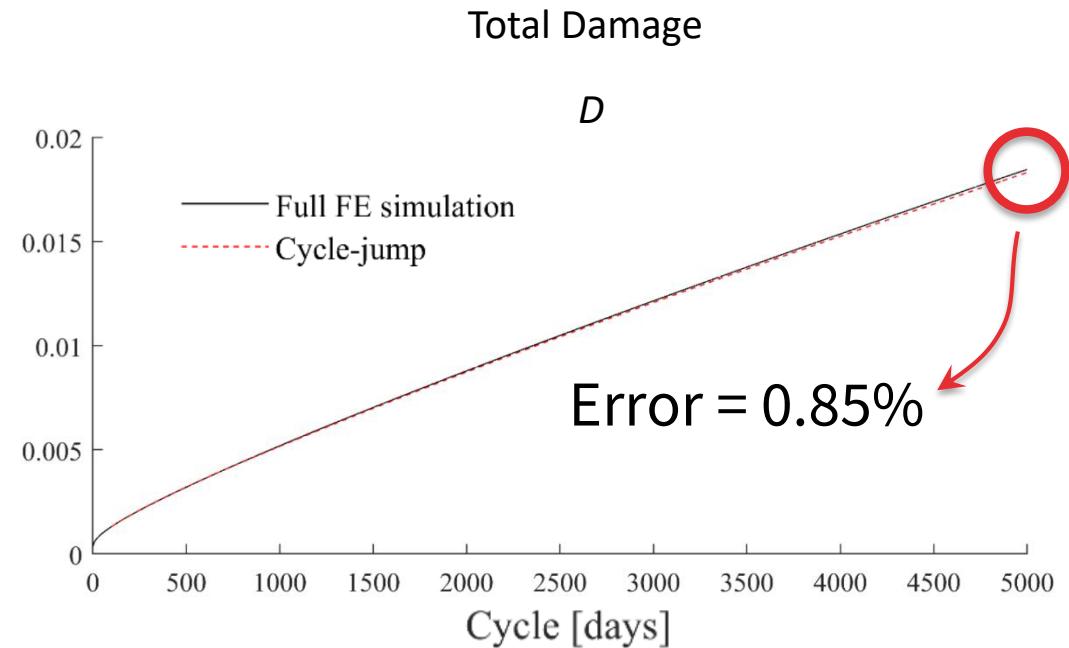
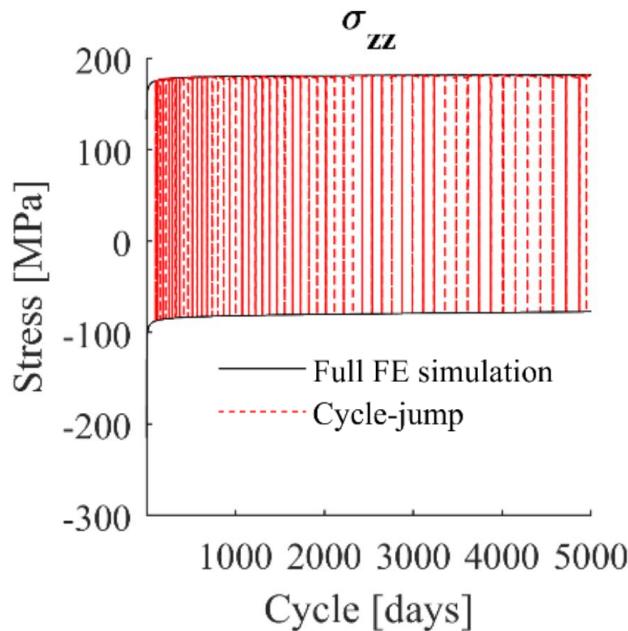
All FE variables, only  $D$ ... No significant effect



# Cycle jump: optimum parameters

- First 100 cycles → full FE computation
- $N_i = 4$
- $N_j$  automatic ( $\Delta D^{\max} = 5 \cdot 10^{-4}$ )
- Extrapolation scheme: linear on 2 cycles
- All FE variables extrapolated

# Cycle jump: optimum parameters



	CPU time (hours)
Full FE computation	104
Optimum Cycle jump	11

- ▶ 5 000 cycles
- ▶ 1 slice of the tube  
(300 FE, ~3000 DOFs)



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## Modèle de base

$$\underline{\varepsilon} = \underline{\varepsilon}^{\text{el}} + \underline{\varepsilon}^{\text{vp}} + \underline{\varepsilon}^{\text{th}}$$

$$\underline{\sigma} = \underline{\underline{E}} : \underline{\varepsilon}^{\text{el}}$$

$$\dot{\underline{\sigma}} = \underline{\underline{E}} : \dot{\underline{\varepsilon}}^{\text{el}} + \underline{\underline{E}} : \underline{\varepsilon}^{\text{el}}$$

## Surface de plasticité

$$f = \|\underline{\sigma} - \underline{X}\| - \sigma_0 - R \leq 0$$

Contrainte visqueuse

$$\sigma_v = f > 0$$

Loi de viscosité

$$\dot{P} = \left\langle \frac{\sigma_v}{K} \right\rangle^n$$

$$\text{Avec : } \dot{p} = \sqrt{\frac{2}{3} \underline{\varepsilon}^{\text{vp}} : \underline{\varepsilon}^{\text{vp}}}$$

## Ecrouissage cinématique

$$\hat{\underline{X}} = \sum_{i=1}^{nAF} \hat{\underline{X}}_i$$

$$\dot{\hat{\underline{X}}}_i = \frac{2}{3} C_i \dot{\underline{\varepsilon}}^{\text{vp}} - \gamma_i (\hat{\underline{X}}_i - Y_i) \dot{p}$$

## Ecrouissage isotrope

$$\dot{R} = b(Q - R)\dot{p}$$

Restauration statique

$$\hat{\underline{X}}_i = \dots - b_i \|\underline{X}_i\|^{r_i-1} \hat{\underline{X}}_i$$

Variations de température

$$\hat{\underline{X}}_i = \dots + \frac{1}{C_i} \frac{\partial C_i}{\partial T} \dot{T} \hat{\underline{X}}_i$$

Evolution de la contrainte moyenne

$$\dot{\underline{Y}}_i = -\alpha_{b,i} \left( \frac{3}{2} Y_{st,i} \frac{\hat{\underline{X}}_i}{\|\underline{X}_i\|} + \underline{Y}_i \right) \|\underline{X}_i\|^r$$

Ecrouissage cyclique

$$\dot{\gamma}_i = D_{\gamma i} (\gamma_i^0 - \gamma_i) \dot{p}$$

$$\gamma_i^0 = a_{\gamma i} + b_{\gamma i} e^{-c_{\gamma i} q}$$

Influence sur l'écrouissage cyclique

$$\dot{D}_{\gamma i} = b_{D\gamma} (D_{\gamma i}^{T_{\max}} - D_{\gamma i}) \dot{p}$$

## Influence de la température maximale

Evolution du module d'Young

$$E = f_E E + (1 - f_E) E_{T_{\max}}$$

$$\dot{f}_E = b_E (f_E^S - f_E) \dot{p}$$