

Abstract

Ferromagnetic lamination stacks are ubiquitous in electrical engineering applications. An accurate knowledge of iron losses in such stacks is highly valuable in a design phase, but their explicit modelling is computationally prohibitive. Hence, iron losses are usually neglected in R&D and lossless material laws are used. Here, a lossy homogenized parametric law $\tilde{\mathbf{H}}(\mathbf{B}, \dot{\mathbf{B}}, p_k)$ is used as material law. The parameters p_k are identified elementwise, thanks to a neural network, on basis of the local knowledge of the magnetic field. This approach provides designers with a fast and robust model to account for iron losses, with a controlled accuracy and only little overhead compared to a conventional formulation.

New irreversible parametric material law: the p_k law

$$\tilde{\mathbf{H}}(\mathbf{B}, \dot{\mathbf{B}}, p_k) = \left(p_0 + (p_1 \|\mathbf{B}\|^2)^{p_2} \right) \mathbf{B} + \left(\frac{p_3}{\sqrt{p_3^2 + \|\mathbf{B}\|^2}} + \frac{p_4}{\sqrt{p_3^2 + \|\mathbf{B}\|^2}} \right) \dot{\mathbf{B}}$$

$\tilde{\mathbf{H}}_{an}$ → Reversible (anhysteretic) saturation curve

$\tilde{\mathbf{H}}_{eddy}$ → Irreversible dynamic eddy current (viscosity-like) term

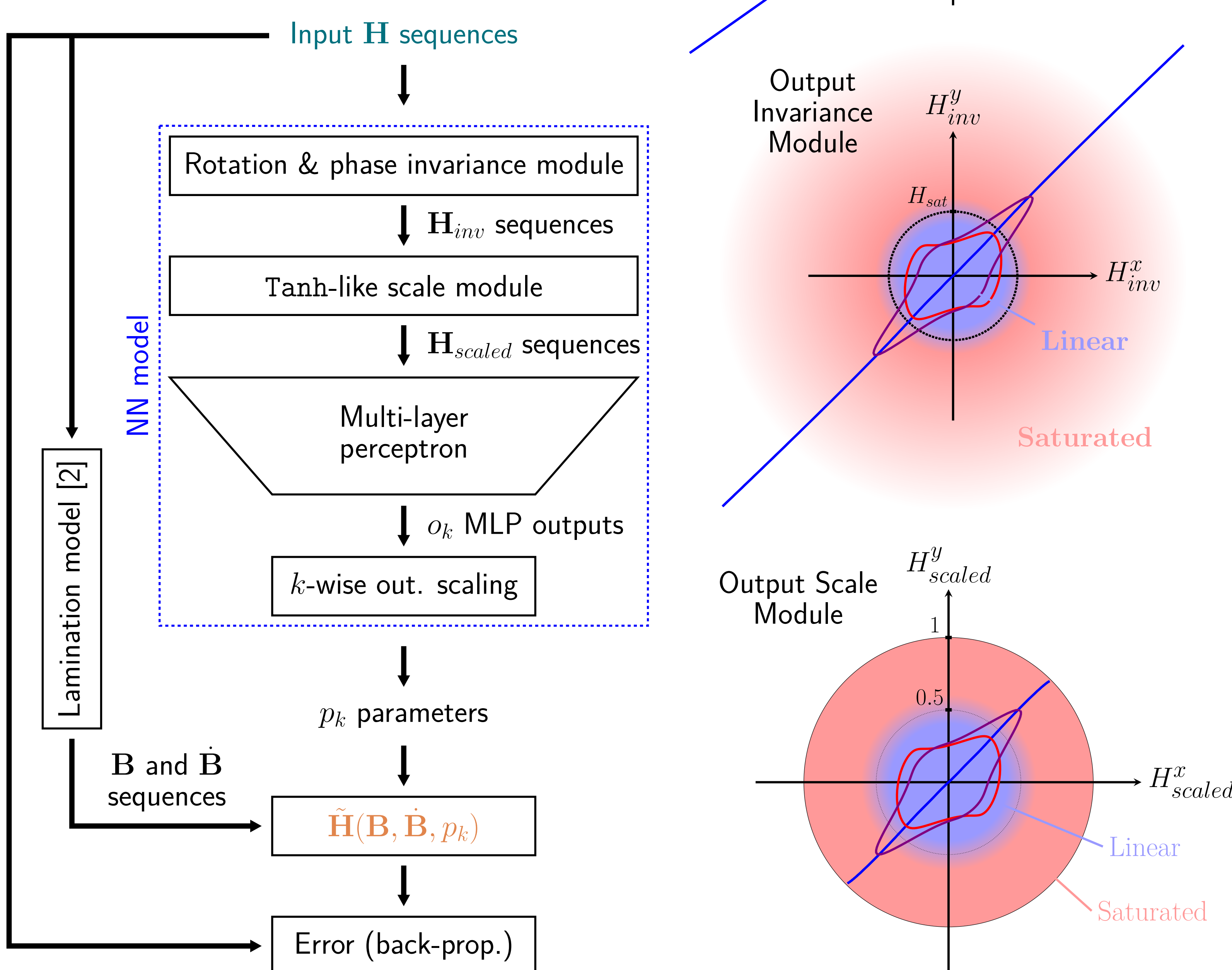
$\tilde{\mathbf{H}}_{hyst.}$ → Irreversible hysteresis (dry friction-like) term

p_k Identification with a Neural Network: Architecture and Learning

Assuming periodicity, the parameters p_k can be determined using a neural network:

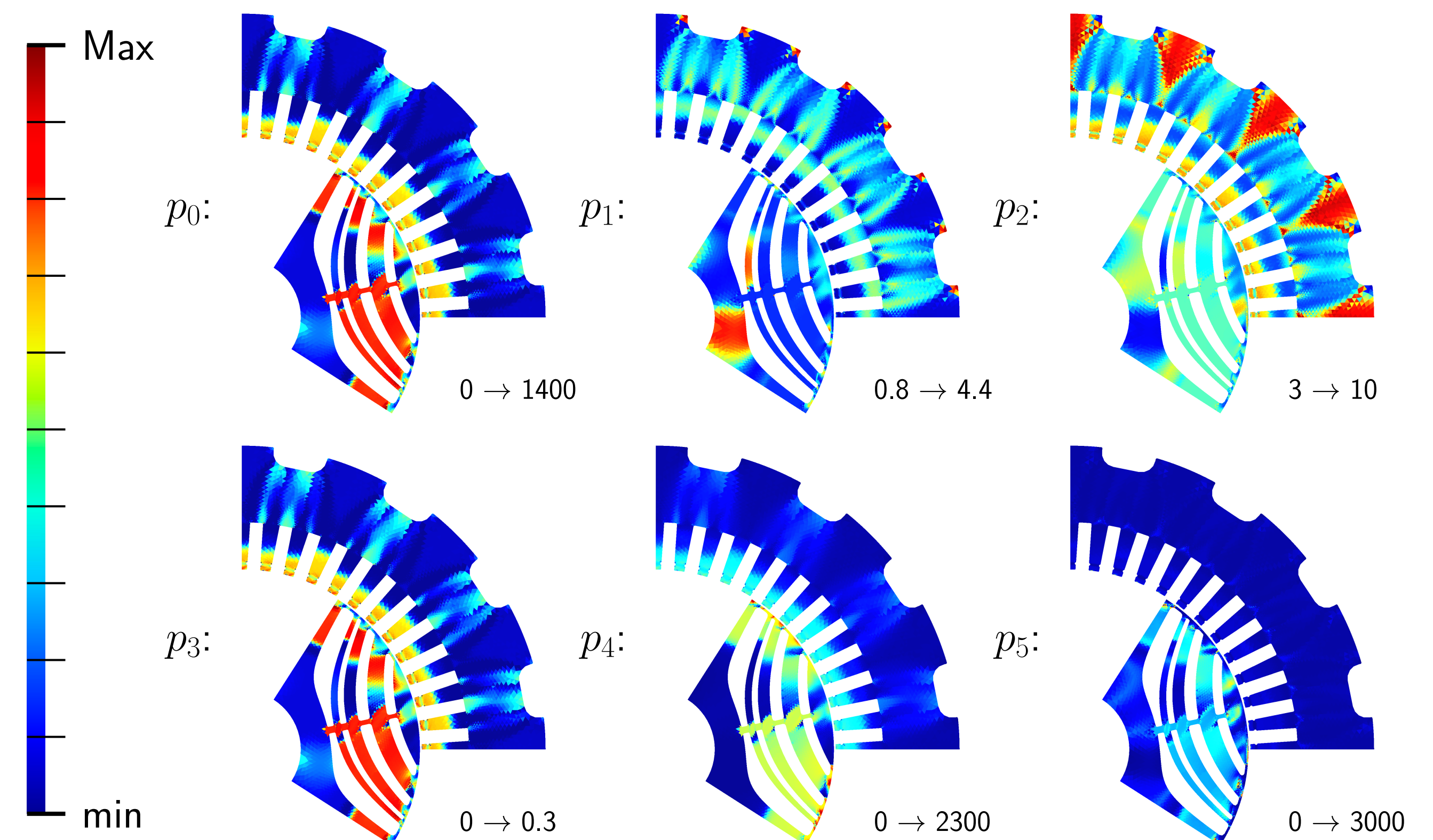
- Auto-encoder-like learning [1], the p_k law is the decoder

- Sequences image of each other by a phase shift and/or a rotation are equivalent → **Rotation & phase invariance module**
- Material exhibits saturation → **Saturation-like input scaling**
- Parameters vary on different scales → **k-wise output scaling**

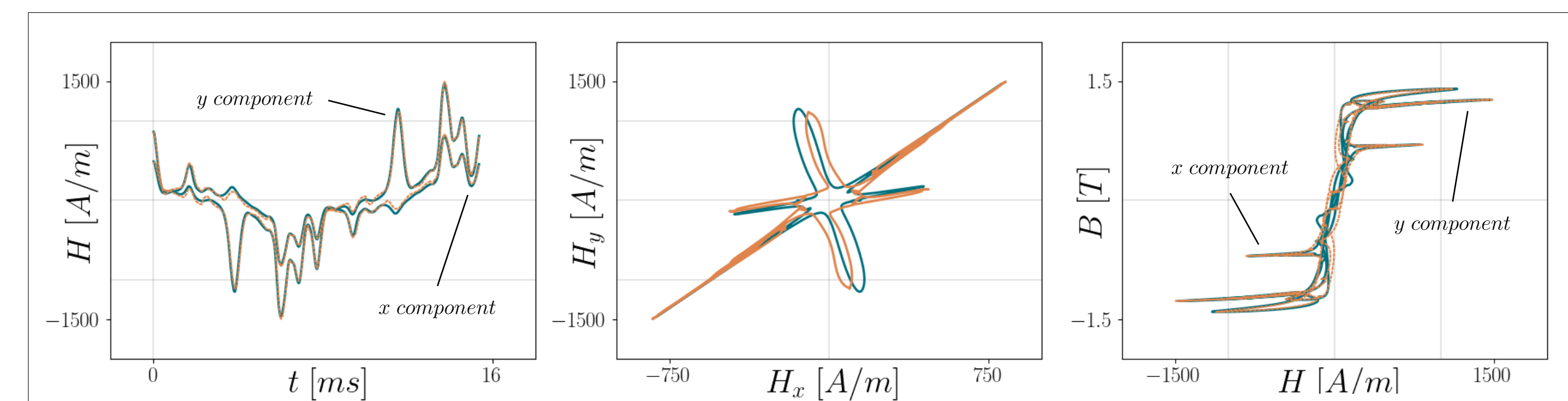


Results

NN computed distribution of the p_k parameters in a switched reluctance motor:



Error distribution and Input \mathbf{H} Sequences vs. $\tilde{\mathbf{H}}(\mathbf{B}, \dot{\mathbf{B}}, p_k)$ curves:

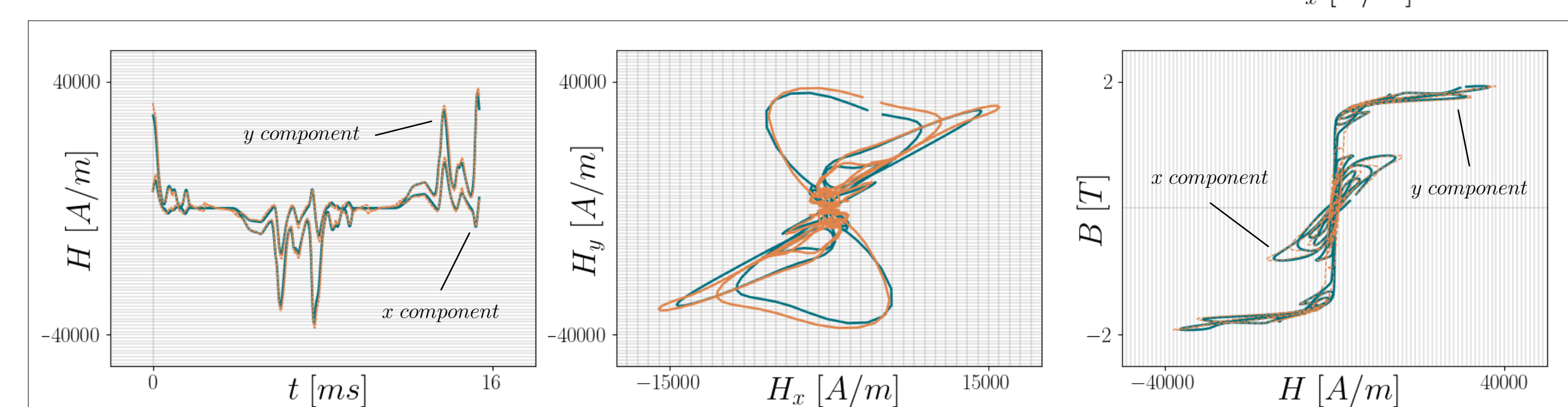


Legend:
 Input \mathbf{H} seq.
 $\tilde{\mathbf{H}}(\mathbf{B}, \dot{\mathbf{B}}, p_k)$

For the above distribution of p_k 's, the distribution of the error

$$\sqrt{\frac{\int_T (H_x - \tilde{H}_x)^2 + (H_y - \tilde{H}_y)^2}{\int_T H_x^2 + H_y^2}}$$

is plotted in the range 0 → 1. The mean error is about 8.3%.



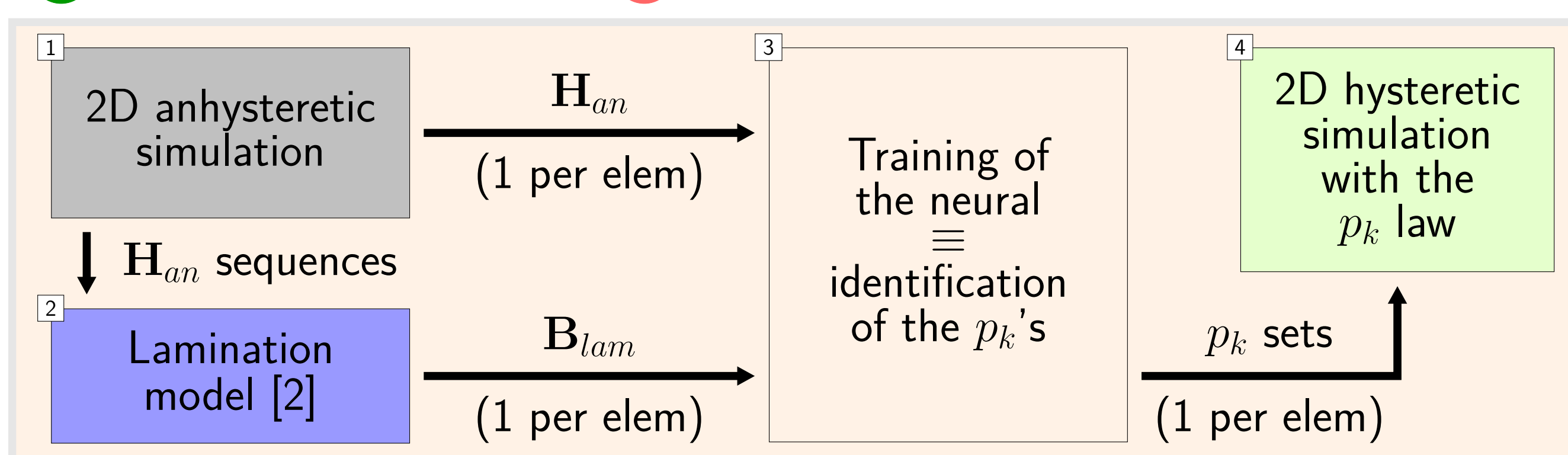
A NN trained in an auto-encoder fashion, with appropriate pre-and-post processing modules, is a fast and accurate way to evaluate the parameters of the p_k law. The obtained p_k law is a realistic lossy material law for steel lamination stacks.

p_k Identification on a 2D Model: Synthetic vs. Specific Approaches

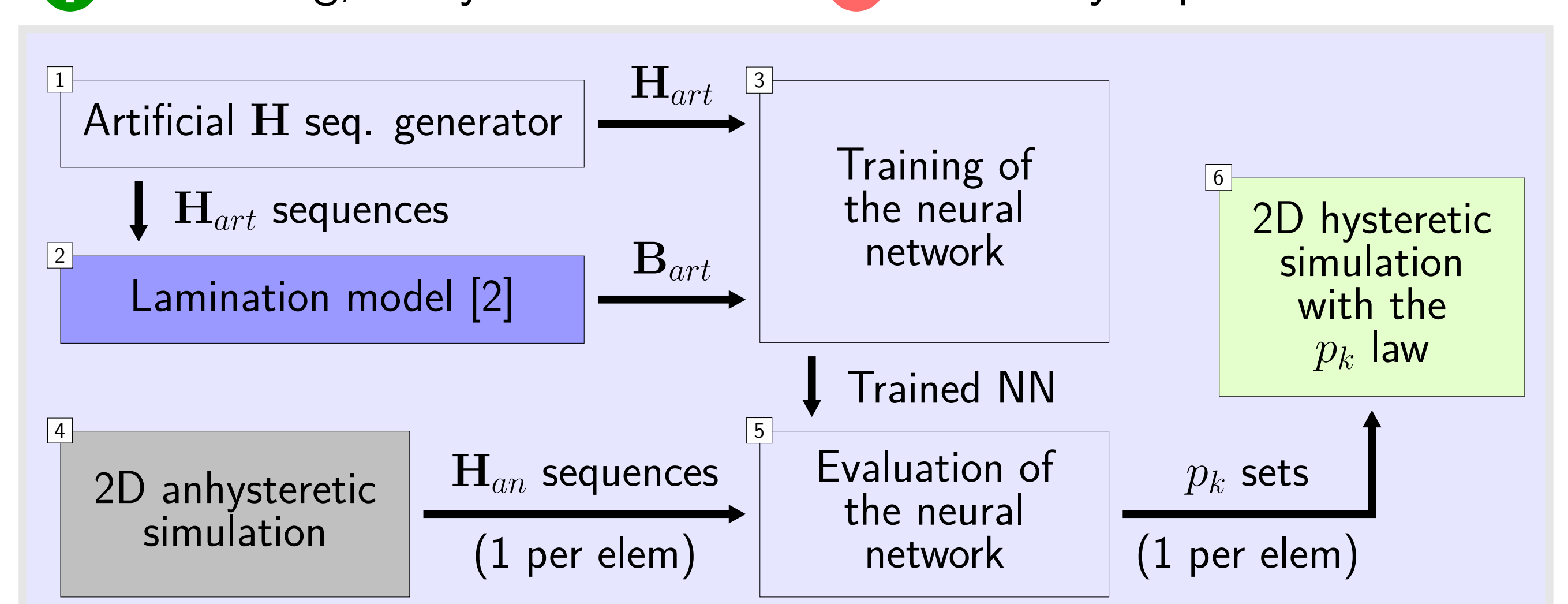
Synthetic approach: Training on a dataset of artificially created \mathbf{H} sequences. NN used for machines with simple harmonic content

Specific approach: Training on the sequences of a specific machine. NN used for that specific machine only

⊕ Measurable accuracy ⊖ Slower p_k identification process



⊕ 1 training, many identifications ⊖ Accuracy depends on dataset



[1] Purnode, F., Henrotte, F., Caire, F., Da Silva, J., Louppe, G., & Geuzaine, C. (2022). A Material Law Based on Neural Networks and Homogenization for the Accurate Finite Element Simulation of Laminated Ferromagnetic Cores in the Periodic Regime. IEEE Transactions on Magnetics. doi:10.1109/TMAG.2022.3160651

[2] Henrotte, F., Steentjes, S., Hameyer, K., & Geuzaine, C. (2015). Pragmatic two-step homogenisation technique for ferromagnetic laminated cores. IET Science, Measurement and Technology, 9 (2), 152-159. doi:10.1049/iet-smt.2014.0201