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Development of Machine Learning based wall shear stress models for LES in the presence of adverse pressure gradients and separation

JDD Safran, October 18th-19th 2023, Bordes, France

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## Separation phenomenon - Sketch



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## Separation phenomenon - Non-dimensional mean velocity profiles





## Analytic WSS model based on Reichardt's profile (a priori)





## Analytic WSS model based on Reichardt's profile (a priori)

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**Observation:** The analytical WSS model is too restrictive for the flow physics developing in the periodic hill. Nonetheless, the reverse flow is detected because the bubble is sufficiently thick.

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## Analytic WSS model based on Reichardt's profile (a posteriori)

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**Observation:** Misprediction of (1) separation and (2) reattachment location, and (3) underestimation of friction peak. There is room for improvement.

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## **Data-driven WSS model - Motivations**



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## Data-driven WSS model - Architecture

Gaussian Mixture Neural Networks (GMN) aim to predict the probability distribution  $p(\tau_w|\mathbf{x})$  of the wall shear stress component as a linear combination of Gaussian distribution :

$$p(\tau_w | \mathbf{x}) = \sum_{k=1}^{K} \pi_k p_k = \sum_{k=1}^{K} \pi_k \mathcal{N}(\mu_k, \sigma_k)$$



## Data-driven WSS model - Data extraction

The input stencil size<sup>1</sup> is represented as follows,



**Remark:** Proper training requires a high correlation between input and output. Causality has nothing to do with it. Due to the large input size, **NN** is replaced by a Convolutional Neural Network (combined with residual blocks).

<sup>&</sup>lt;sup>1</sup>based upon analysis of space-time correlations [1].

## **Data-driven WSS model - Preprocessing**



where  $\boldsymbol{u}_{p} = \operatorname{sign}\left(\nabla p\right) \left( rac{
u}{\rho} | \nabla p | \right)^{1/3}$  is a velocity based on the pressure gradient.



## Data-driven WSS model - Complete procedure

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The wall shear stress  $\tau_w$  is **sampled** from the predicted distribution,



The predicted  $\tau_w$  is implemented as a **boundary condition** in Argo-DG [2].



Image by pikisuperstar on Freepik

#### A priori prediction on the lower wall of the two-dimensional periodic hill,



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#### A priori prediction on the upper wall of the two-dimensional periodic hill,



#### A priori prediction on the upper wall of the two-dimensional periodic hill,



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## A priori prediction observed in a $(y^+, u^+)$ graph,



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#### Friction coefficient on the lower wall obtained after the accumulation of statistics over about $35t_c$ ,



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#### **Friction coefficient** on the lower wall obtained after the accumulation of statistics over about $35t_c$ .



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#### **Mean velocity profile** obtained after the accumulation of statistics over about $35t_{c_1}$



#### **Mean Reynolds stress profile** obtained after the accumulation of statistics over about $35t_{c}$ .



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**Friction coefficient** on the upper wall obtained after the accumulation of statistics over about  $35t_{c}$ .



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# **Non-dimensional velocity profiles** on the upper wall obtained after the accumulation of statistics over about $35t_c$ ,



**Remark:** The data-driven wmLES is always closer to the DNS profiles.



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## **Data-driven WSS model - Conclusion**

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- **Objective.** Development of a novel WSS model for the separation/reattachment phenomenon.
- Scientific contribution. Generate a data-driven WSS model to predict a distribution that better captures the instantaneous behaviour of wall shear stress.
- **Positive impact.** A great improvement in the WSS curve is observed on both the upper and lower walls of the two-dimensional periodic hill.
- **Points to be improved.** The reattachment location is underestimated and this affects the physics in the whole domain. Dupuy *et al.* [3, 4] have also observed this underestimation on other test cases featuring separation. The volume data may be more influenced by the direction of the wall shear stress (which is currently randomly generated) than its amplitude.



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