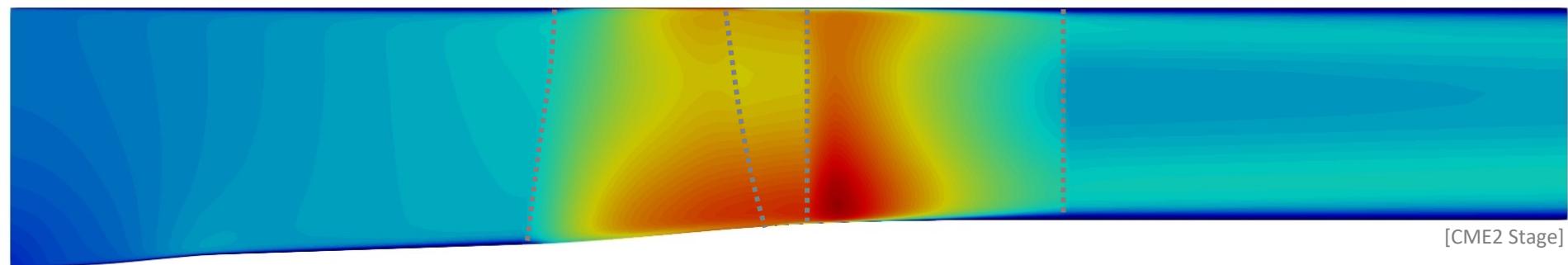


Quantification of geometric variability effects through a viscous through-flow model: sensitivity analysis of the manufacturing tolerance effects on performance of modern axial-flow compressor blades



Arnaud Budo⁽¹⁾

Thibault Le Men⁽²⁾, Koen Hillewaert⁽¹⁾,
Maarten Arnst⁽¹⁾, Vincent E. Terrapon⁽¹⁾

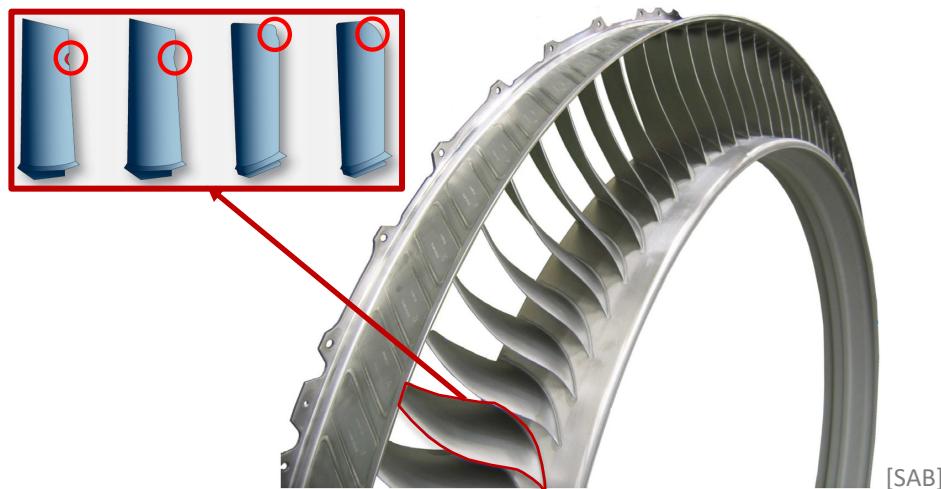


ASME Turbo Expo 2023

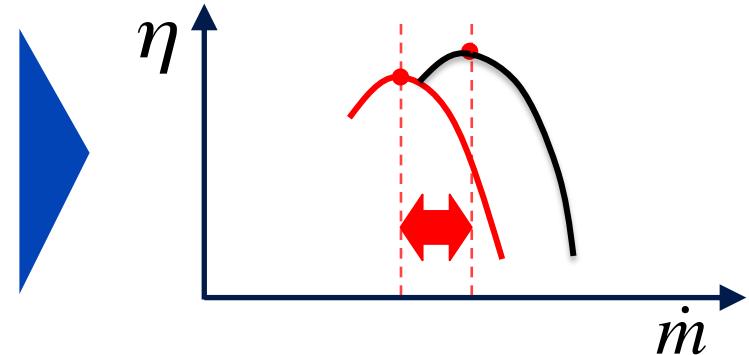


Context

Geometric variability of low-pressure compressor blades



Performance variation



Manufacturing tolerances?

- Need of rigorous/robust definition
- Linked to manufacturing process
- Simplify the treatment of poorly made parts

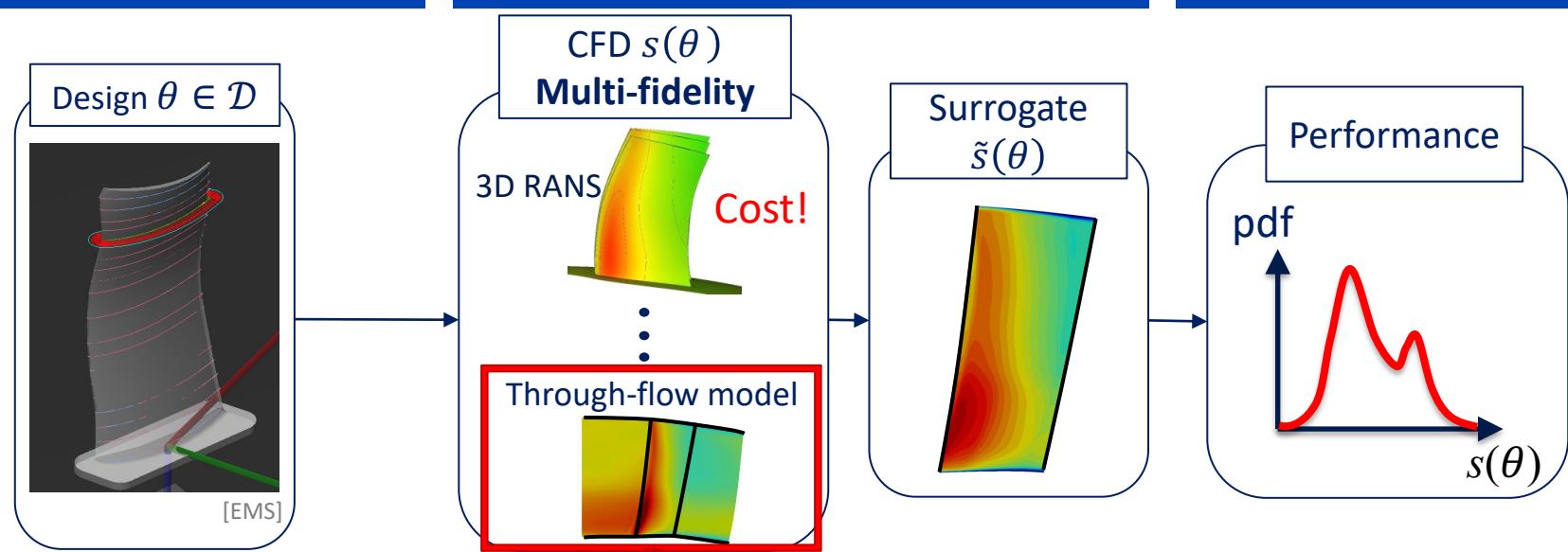
Trade-off
Cost \Leftrightarrow performance

Methodology & objectives

Characterization

Propagation

Qualification



Able to predict performance?

Through-flow model validation

- Consistency
- Choice of model correlations

Able to capture variability effects?

Geometrical variability

- Sensitivity analysis
- (Uncertainty quantification)

Outline

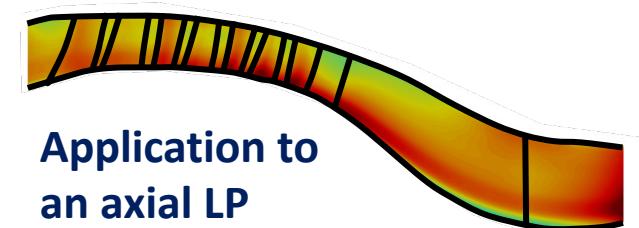
1

Viscous through-flow model

$$\frac{\partial U}{\partial t} + \frac{\partial (F - F_v)}{\partial x} + \frac{\partial (G - G_v)}{\partial r} = S$$

2

Model Assessment



3

Geometric variability



[SAB]

Outline

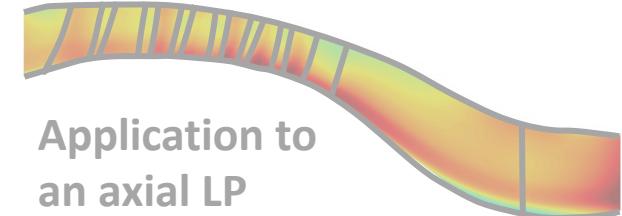
1

Viscous through-flow model

$$\frac{\partial \mathbf{U}}{\partial t} + \frac{\partial (\mathbf{F} - \mathbf{F}_v)}{\partial x} + \frac{\partial (\mathbf{G} - \mathbf{G}_v)}{\partial r} = \mathbf{S}$$

2

Model Assessment



3

Geometric variability

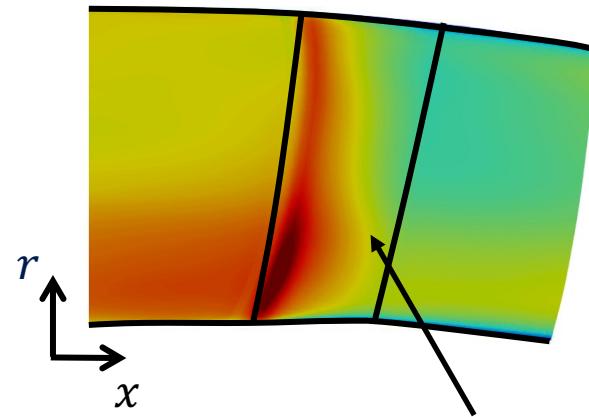
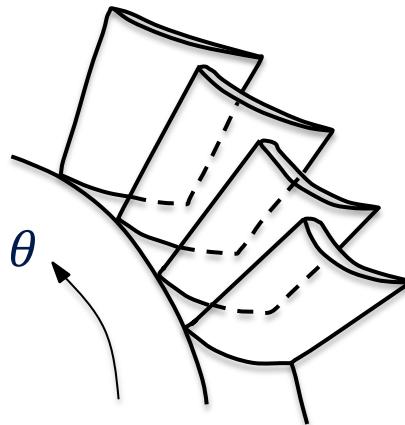


[SAB]

Through-flow model

$$D_t U(r, \theta, x, t) = \mathbf{G}(U, r, \theta, x, t) \xrightarrow{\theta\text{-averaging}} D_t \bar{U}(r, x) = \bar{\mathbf{G}}(U, r, x)$$

Unclosed!



Implicit presence of the blades

- Azimuthal/pitchwise averaging approach
- Axisymmetric steady flow (meridional plane)
- Empirical correlations
- Low computational cost $\mathcal{O}(\min)$

Through-flow formulation

$$D_t \bar{U}(r, x) = \bar{G}(U, r, x)$$

Governing equations

- Underlying assumptions
(NSE, Euler, SLC, ...)?
- Consistency?

Closure models

- Exhaustive?
- Assumptions?
- Correlations?

Choices influence **level of empiricism** and determine **error sources**

→ characterize error in a **rigorous and exhaustive way**

Adamczyk's cascade

$$D_t \bar{U}(r, x) = \bar{G}(U, r, x)$$

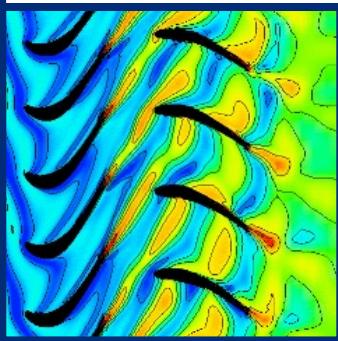
- Exact mathematical formulation of source terms
- NSE-based equations

3D DNS $\mathcal{O}(\text{months})$



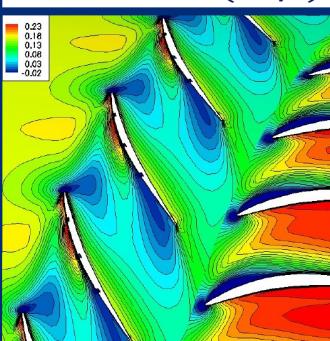
High cost

3D URANS $\mathcal{O}(\text{weeks})$



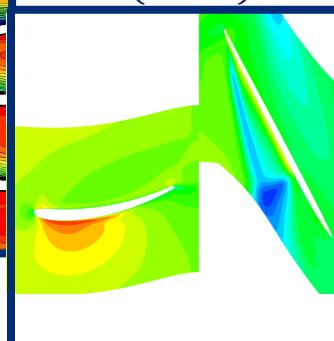
[Cenaero]

3D RANS $\mathcal{O}(\text{days})$



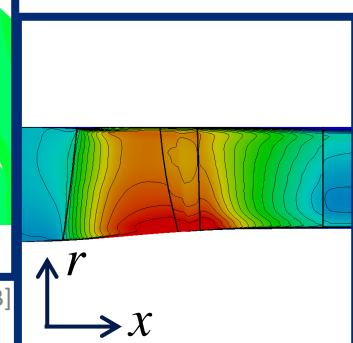
[Schauberger]

3D steady periodic RANS
 $\mathcal{O}(\text{hours})$



[SAB]

2D axisymmetric Through-flow
 $\mathcal{O}(\text{minutes})$



Low cost

Ensemble average

Time average

Passage-to-passage average

Circumferential average

[Simon 2007]

Adamczyk's cascade: unclosed terms

$$D_t \bar{U}(r, x) = \bar{\mathbf{G}}(U, r, x)$$

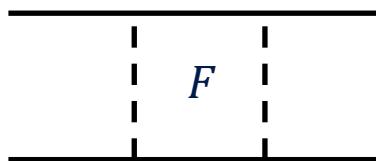
Unclosed terms:

$$\overline{\rho V'_i V'_i}$$

Non-linear
equations

- $\tau_{reys} \succ$ Reynolds
- $\tau_{uns} \succ$ Unsteady
- $\tau_{ape} \succ$ Aperiodic
- $\tau_{circ} \succ$ Circumferential

Stresses



- $B_i \succ$ inviscid
- $B_v \succ$ Viscous

Forces

Empiricism/approximation through model

Relative importance of source terms

$$D_t \bar{U}(r, x) = \bar{G}(U, r, x)$$

Included

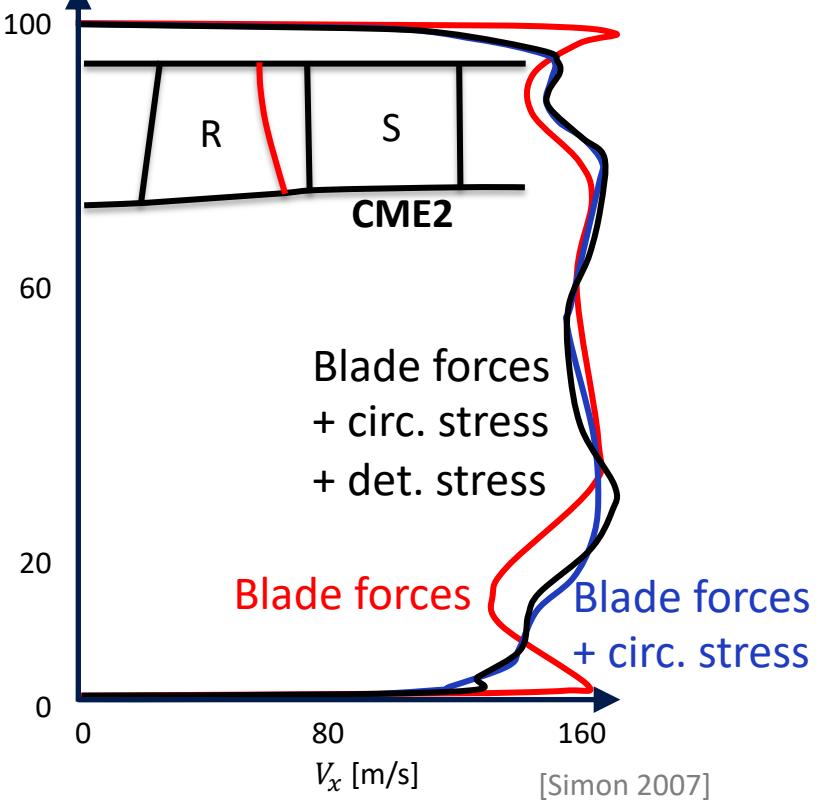
- Reynolds stress
- Inviscid blade force
- Viscous blade force
- Axisymmetric source terms

- Reynolds stress
- Inviscid blade force
- Viscous blade force
- Circumferential stress
- Unsteady stress
- Aperiodic stress
→ Generally neglected

Major terms

Lower importance

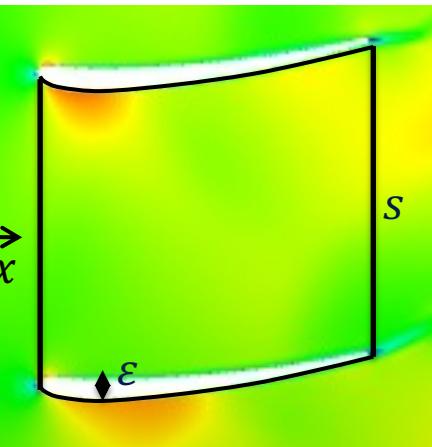
Normalized radius



[Simon 2007]

ASTEC: a viscous through-flow model

Circumferential averaged Navier-Stokes equations:


$$\frac{\partial \mathbf{U}}{\partial t} + \frac{1}{b} \overbrace{\frac{\partial b(\mathbf{F} - \mathbf{F}_v)}{\partial x}}^{x\text{-fluxes}} + \frac{1}{b} \overbrace{\frac{\partial b(\mathbf{G} - \mathbf{G}_v)}{\partial r}}^{r\text{-fluxes}} = \mathbf{S}$$

Blockage factor

$$b = 1 - \frac{\varepsilon(x)}{s}$$

- Reynolds stress
- Inviscid blade force
- Viscous blade force
- Axisymmetric source terms

Non-intrusive formulation for CFD solver:

$$\frac{\partial \mathbf{U}}{\partial t} + \frac{\partial(\mathbf{F} - \mathbf{F}_v)}{\partial x} + \frac{\partial(\mathbf{G} - \mathbf{G}_v)}{\partial r} = \mathbf{S} + \frac{(\mathbf{F}_v - \mathbf{F})}{b} \frac{\partial b}{\partial x} + \frac{(\mathbf{G}_v - \mathbf{G})}{b} \frac{\partial b}{\partial r}$$

Blockage factor terms (known)

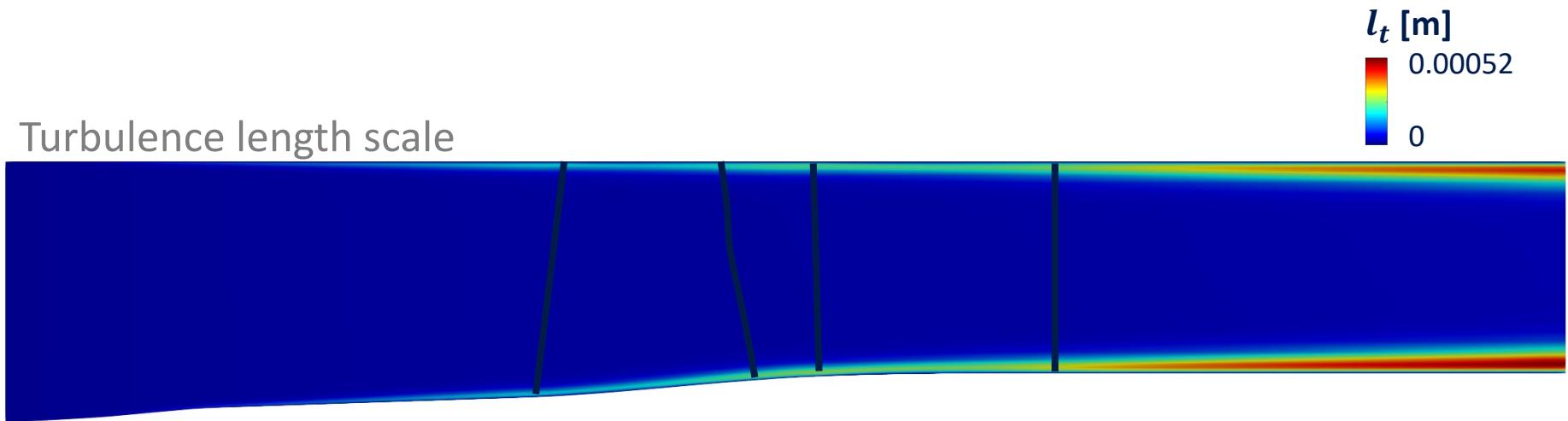
Viscous TF model: closure models

Circumferential averaged Navier-Stokes equations:

$$\frac{\partial \mathbf{U}}{\partial t} + \frac{\partial (\mathbf{F} - \mathbf{F}_v)}{\partial x} + \frac{\partial (\mathbf{G} - \mathbf{G}_v)}{\partial r} = \boxed{\mathbf{S}}$$

- Reynolds stress
- Inviscid blade force
- Viscous blade force
- Axisymmetric source terms

Reynolds stress τ_{reys} : standard turbulence model ($k - l$ Smith)



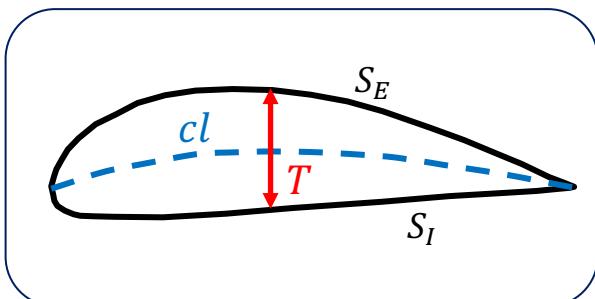
Viscous TF model: closure models

Circumferential averaged Navier-Stokes equations:

$$\frac{\partial \mathbf{U}}{\partial t} + \frac{\partial(\mathbf{F} - \mathbf{F}_v)}{\partial x} + \frac{\partial(\mathbf{G} - \mathbf{G}_v)}{\partial r} = \mathbf{S}$$

- Reynolds stress
- **Inviscid blade force**
- Viscous blade force
- Axisymmetric source terms

Inviscid blade force decomposition B_i :



$$B_i \rightarrow$$

Blade blockage contribution: $B_{i1} = f\left(\frac{P_{SE} + P_{SI}}{2}\right)$

Deflection force: $B_{i2} = f(P_{SE}, P_{SI})$

Unknown!

Closure models: blade forces

$$\frac{\partial \mathbf{U}}{\partial t} + \frac{\partial(\mathbf{F} - \mathbf{F}_v)}{\partial x} + \frac{\partial(\mathbf{G} - \mathbf{G}_v)}{\partial r} = \mathbf{S}$$

- Reynolds stress
- Inviscid blade force
- Viscous blade force
- Axisymmetric source terms

Blade blockage B_{i1}

$$B_{i1} = B_{i1} \left(\frac{P_{SE} + P_{SI}}{2} \right)$$



Averaged pressure

$$\mathbf{s}_{bi1} = \begin{bmatrix} 0 \\ p \frac{\partial b}{\partial x} \\ b \frac{\partial b}{\partial x} \\ p \frac{\partial b}{\partial r} \\ b \frac{\partial b}{\partial r} \\ 0 \\ 0 \end{bmatrix}$$

Blockage factor: b

Deflection B_{i2} and viscous force B_v

$$B_{i2} = B_{i2}(P_{SE}, P_{SI})$$

$$B_v = B_v(\tau_{SE}, \tau_{SI})$$

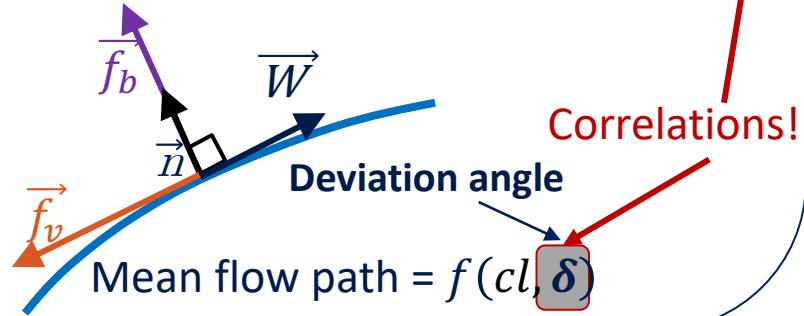


Distributed forces:

$$\frac{\partial f_b}{\partial \tau} = -C (\vec{W} \cdot \vec{n})$$

$$f_v = \rho T \frac{W_m \frac{\partial_m s}{W}}{W} = f(\omega)$$

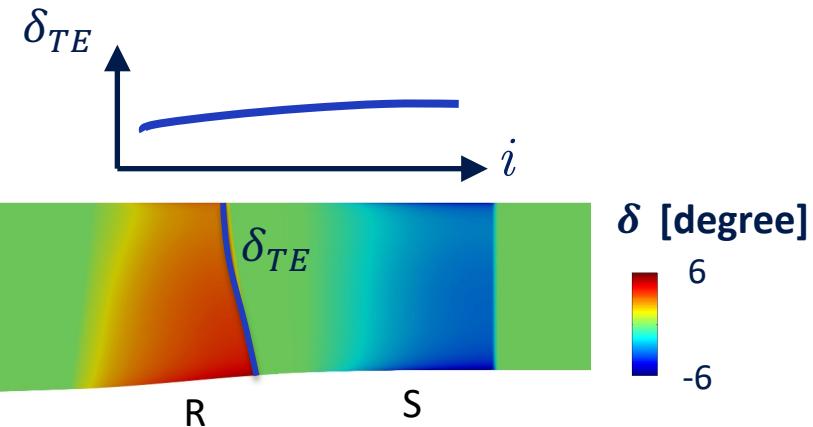
Loss coefficient



Correlations for δ and ω

Deviation angle $\delta \rightarrow$ inviscid blade force

- δ_{TE} from cascade experiments (Lieblein)
- Linear variation with incidence around design conditions
- $\delta = \delta_{TE} \frac{\kappa_{LE} - \kappa}{\kappa_{LE} - \kappa_{TE}}$ ← Blade angle

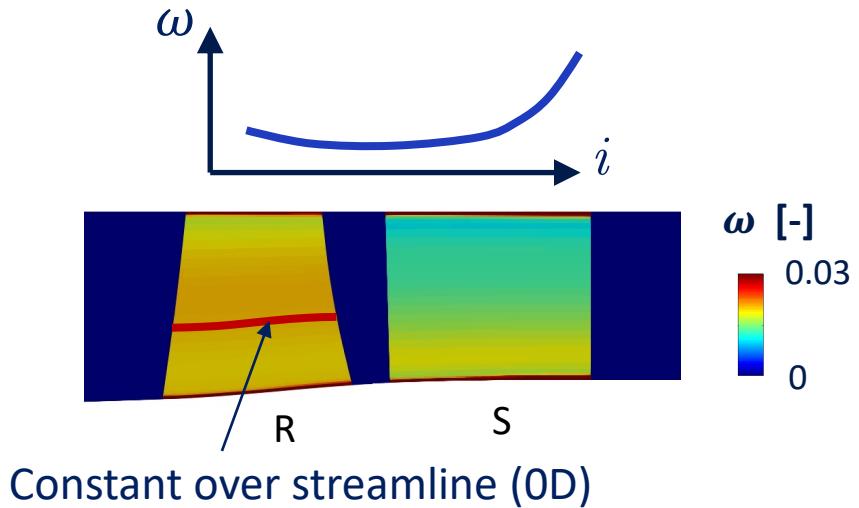


Loss coefficient $\omega \rightarrow$ viscous blade force

- From cascade experiments (Lieblein)



Profile loss only



Constant over streamline (0D)

Outline

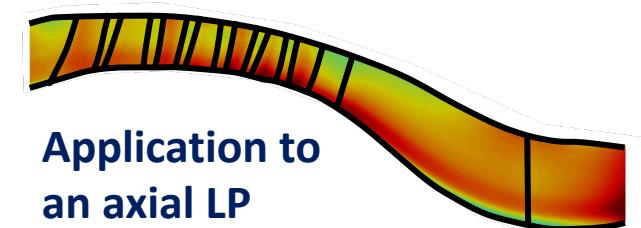
1

Viscous
through-flow model

$$\frac{\partial U}{\partial t} + \frac{\partial (F - F_v)}{\partial x} + \frac{\partial (G - G_v)}{\partial r} = S$$

2

Model Assessment



Application to
an axial LP
compressor

3

Geometric variability

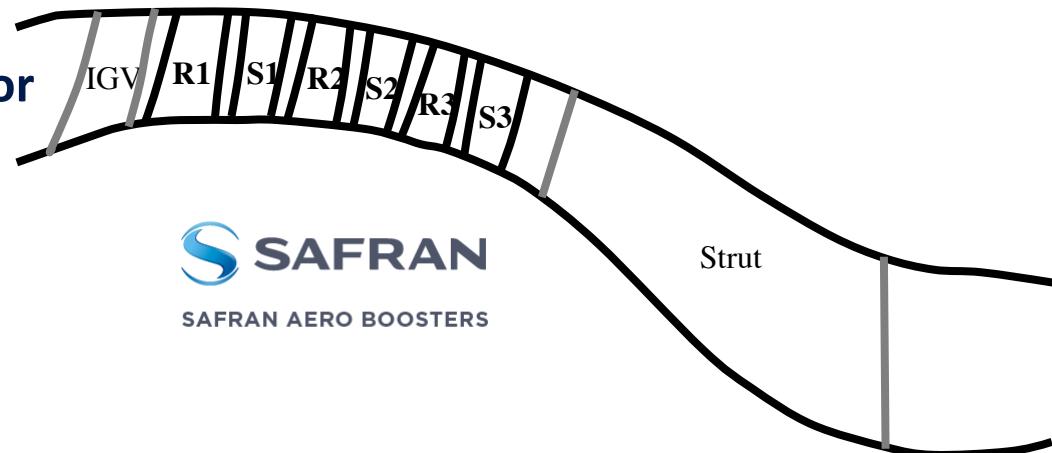


[SAB]

Closure model assessment

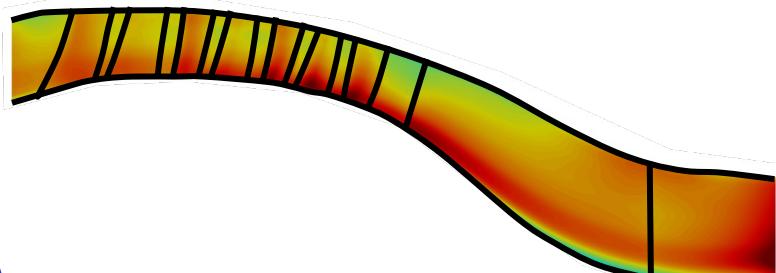
- Quantify closure **model errors**
- Simulations fed with **exact** averaged distribution of δ_{TE} , ω

Test-case : low-pressure compressor

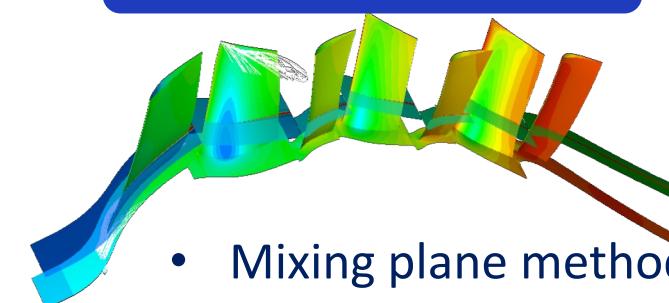


- Highly loaded
- High subsonic Mach number
- 3D modern blades

Through-flow (TF)
simulations



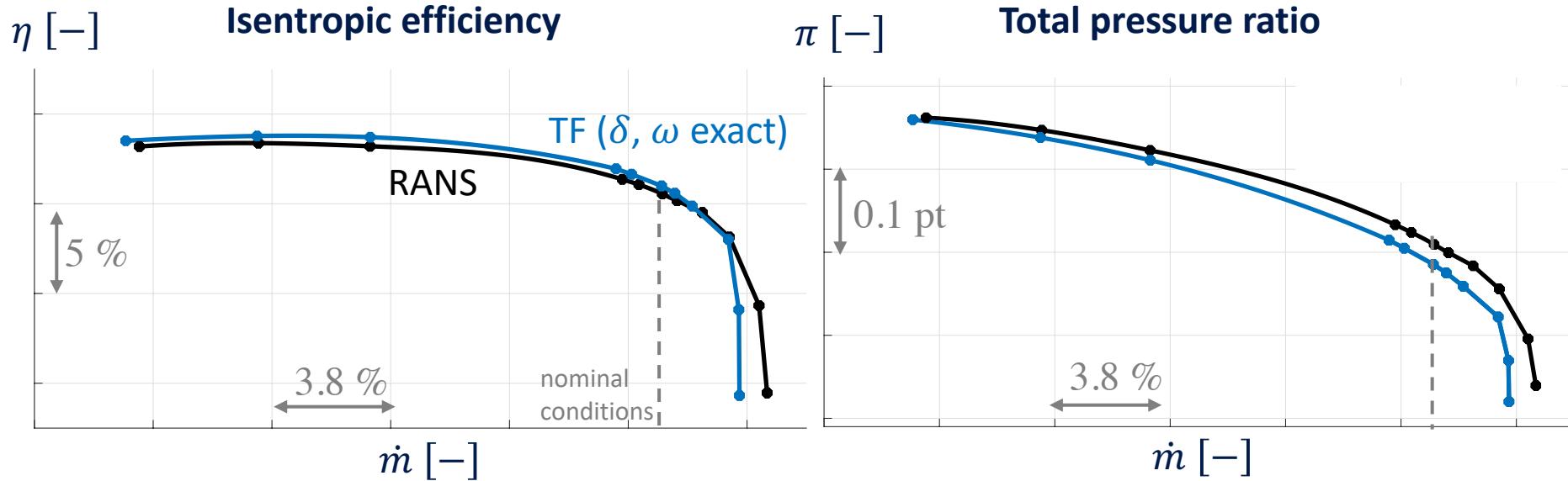
3D RANS simulations



- Mixing plane method
- Steady, periodic flow

δ_{TE} , ω
distributions

Closure model assessment



- Good prediction (low margin)
- 600 times faster
- Sources of errors: τ_{circ} , closure model form, δ_{TE} distribution, blockage assumption, turbulence model...

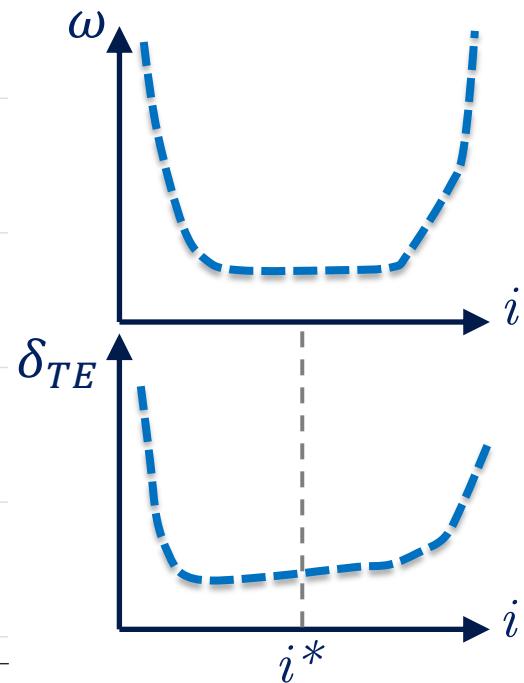
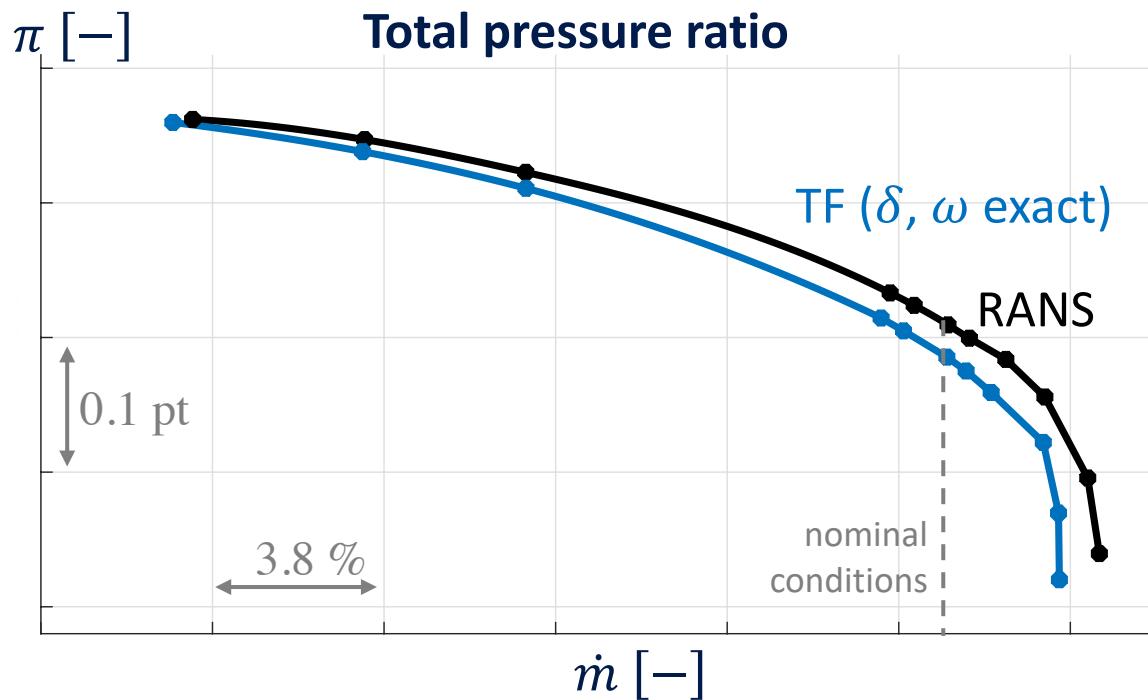


Model able to predict performance

But exact δ, ω unknown in practice...

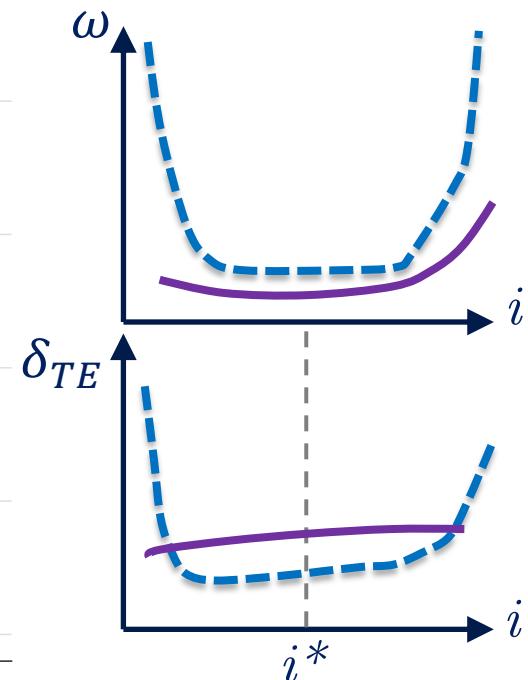
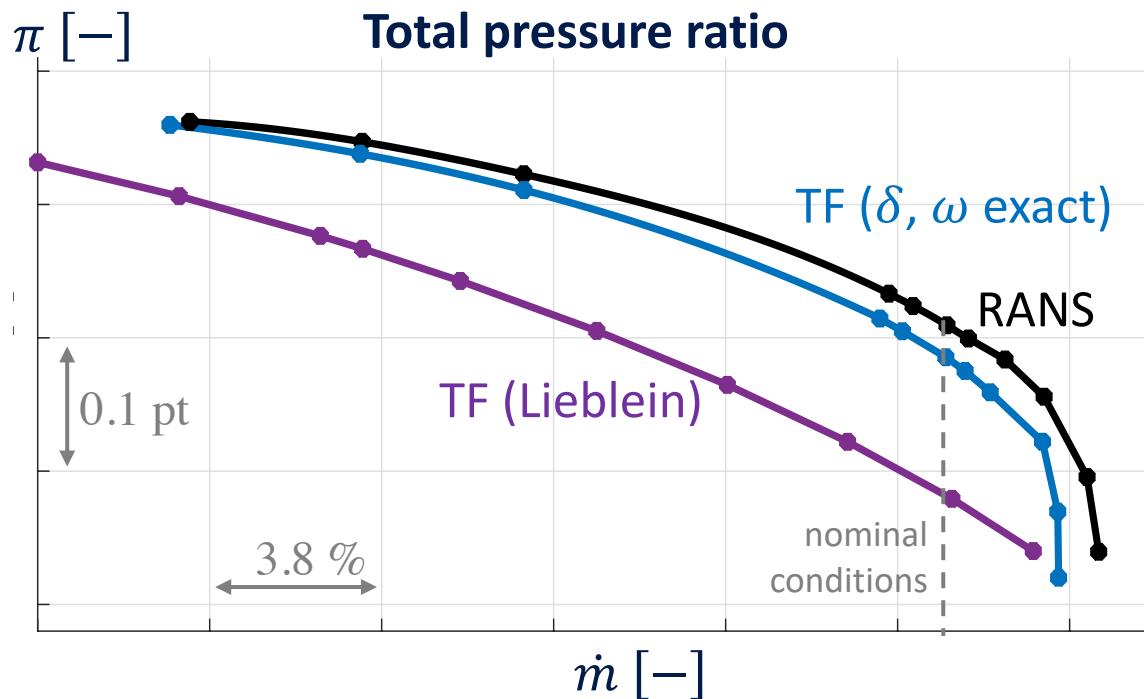
Correlations assessment

- Error quantification of correlations for δ, ω



Correlations assessment

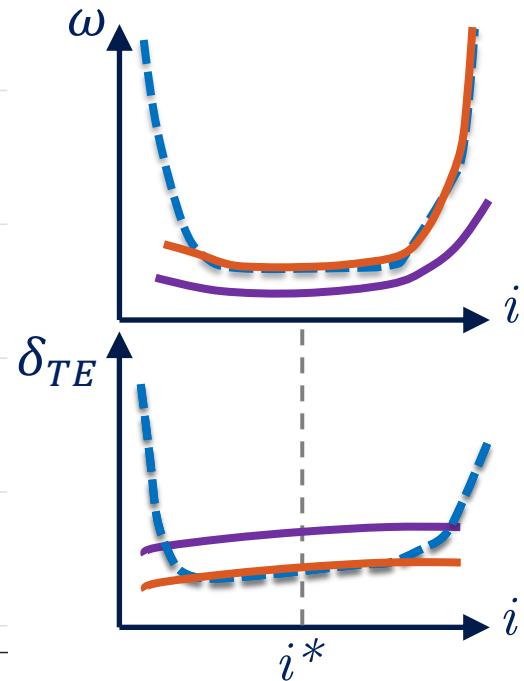
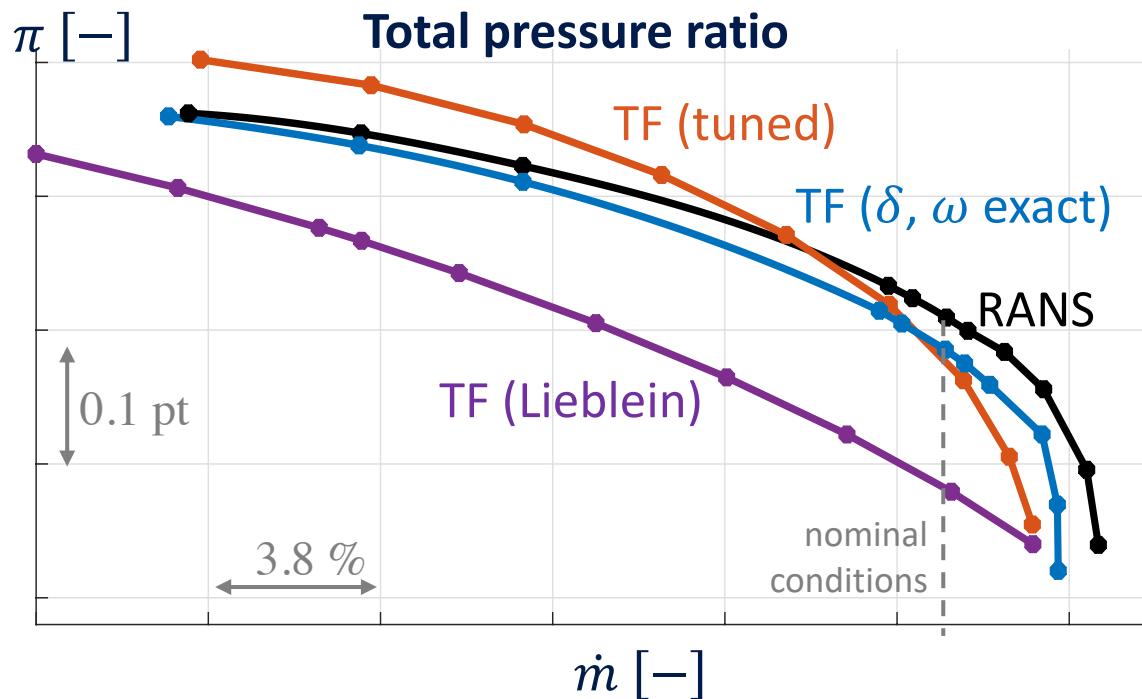
- Error quantification of correlations for δ, ω



- Inaccurate when applied to the modern compressor

Correlations assessment

- Error quantification of correlations for δ , ω



- Rotor deviation angle **correction** → total pressure ratio improvement
- Mach number effect added to loss coefficient

Strong dependence of model prediction with respect to correlation accuracy

Outline

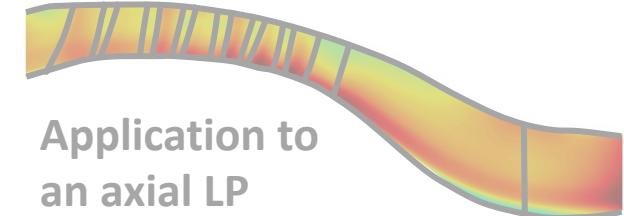
1

Viscous
through-flow model

$$\frac{\partial U}{\partial t} + \frac{\partial (F - F_v)}{\partial x} + \frac{\partial (G - G_v)}{\partial r} = S$$

2

Model Assessment



3

Geometric variability

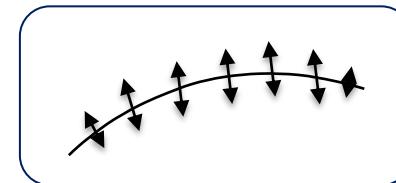
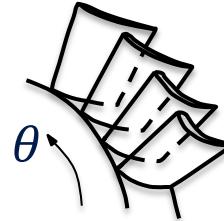
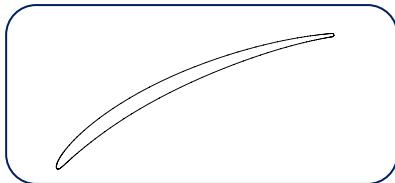


Geometry in through-flow model

$$D_t U(r, \theta, x, t) = \mathbf{G}(U, r, \theta, x, t)$$

θ -averaging

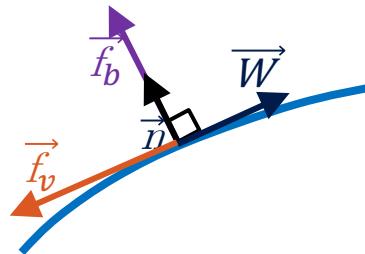
$$D_t \bar{U}(r, \theta, x) = \bar{\mathbf{G}}(U, r, \theta, x)$$



Camber line coordinates
&
Thickness distribution

Blade forces

$$b = 1 - \frac{\varepsilon}{s}$$



$$\delta_{TE}, \omega, i^* = f \left(\begin{array}{l} \text{geometry,} \\ \text{flow quantities} \end{array} \right)$$



Direct impact

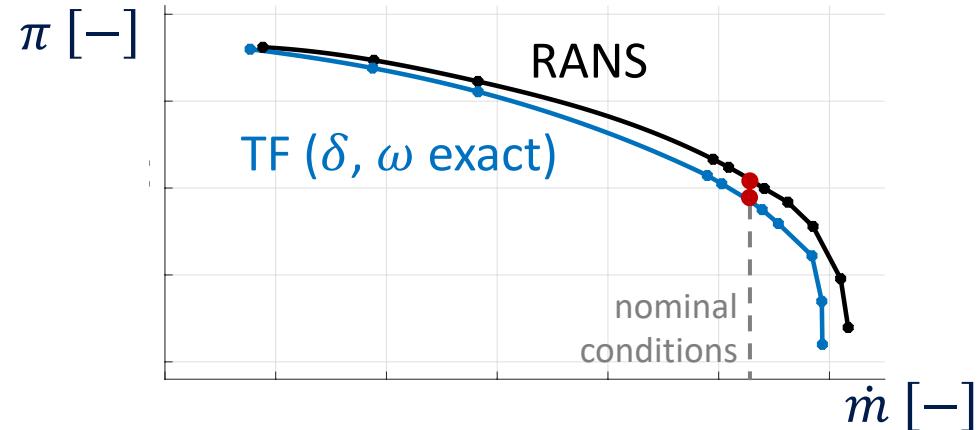
Indirect impact

Geometric variabilities

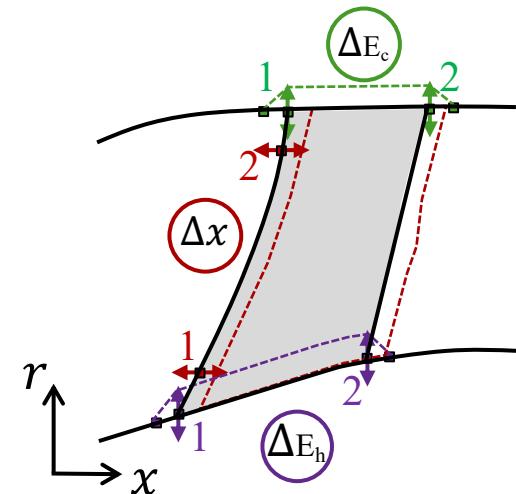
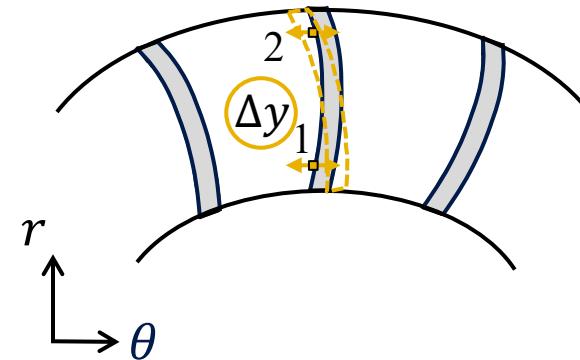
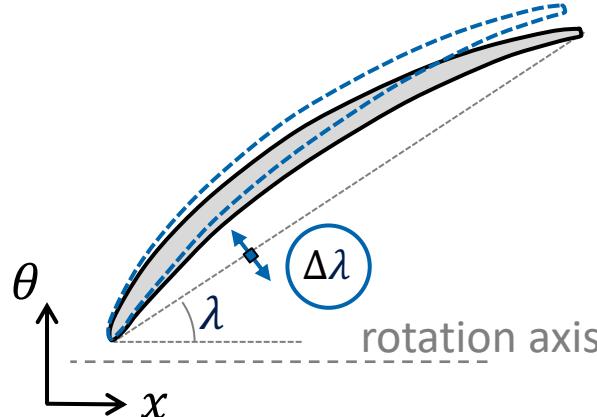
- Assess adequacy to predict performance variation due to **geometric variabilities**

Preliminary analysis

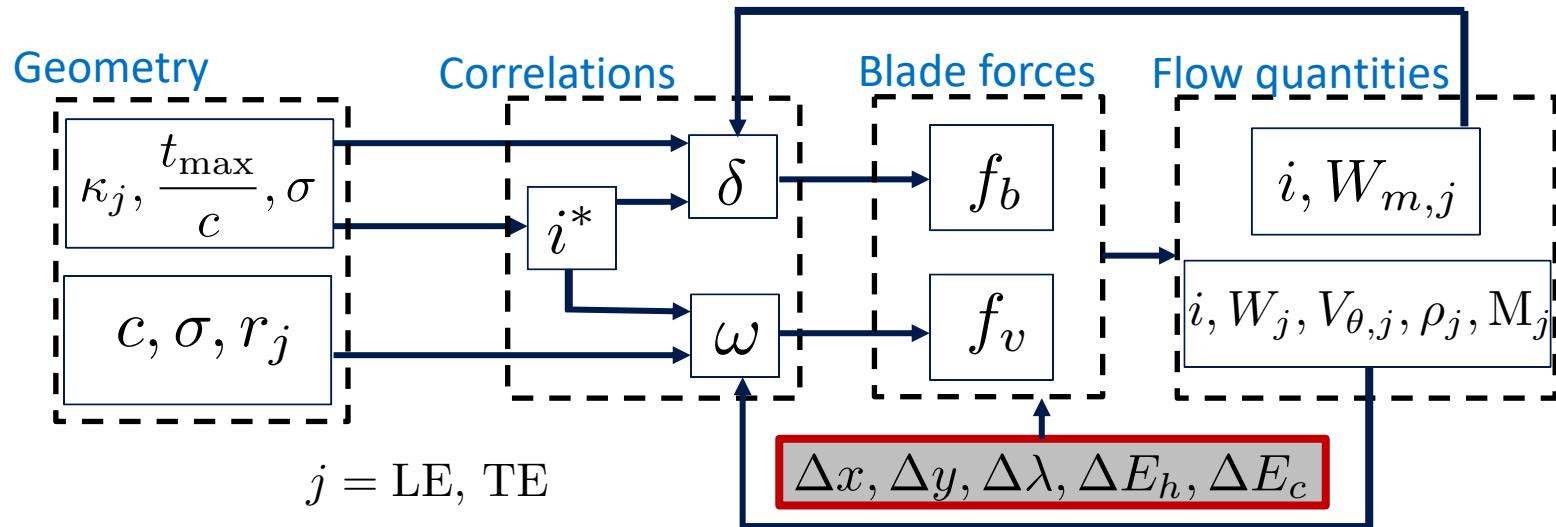
- @ nominal conditions
- Relative variations
- Stator blades



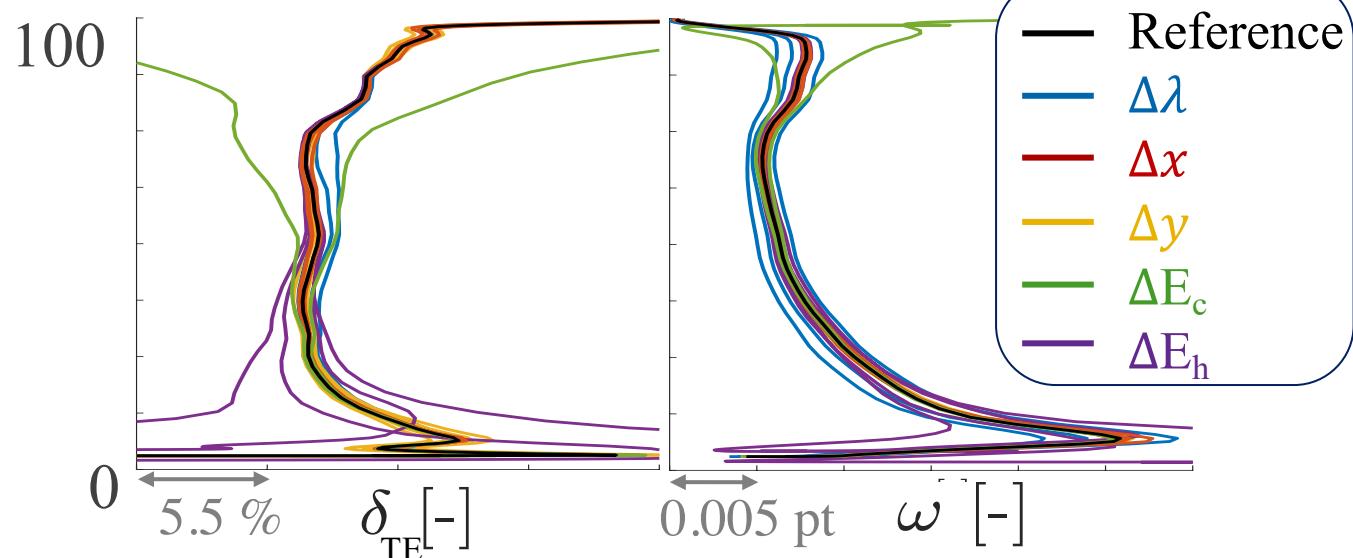
- 3D position of undeformed & endwalls deformation



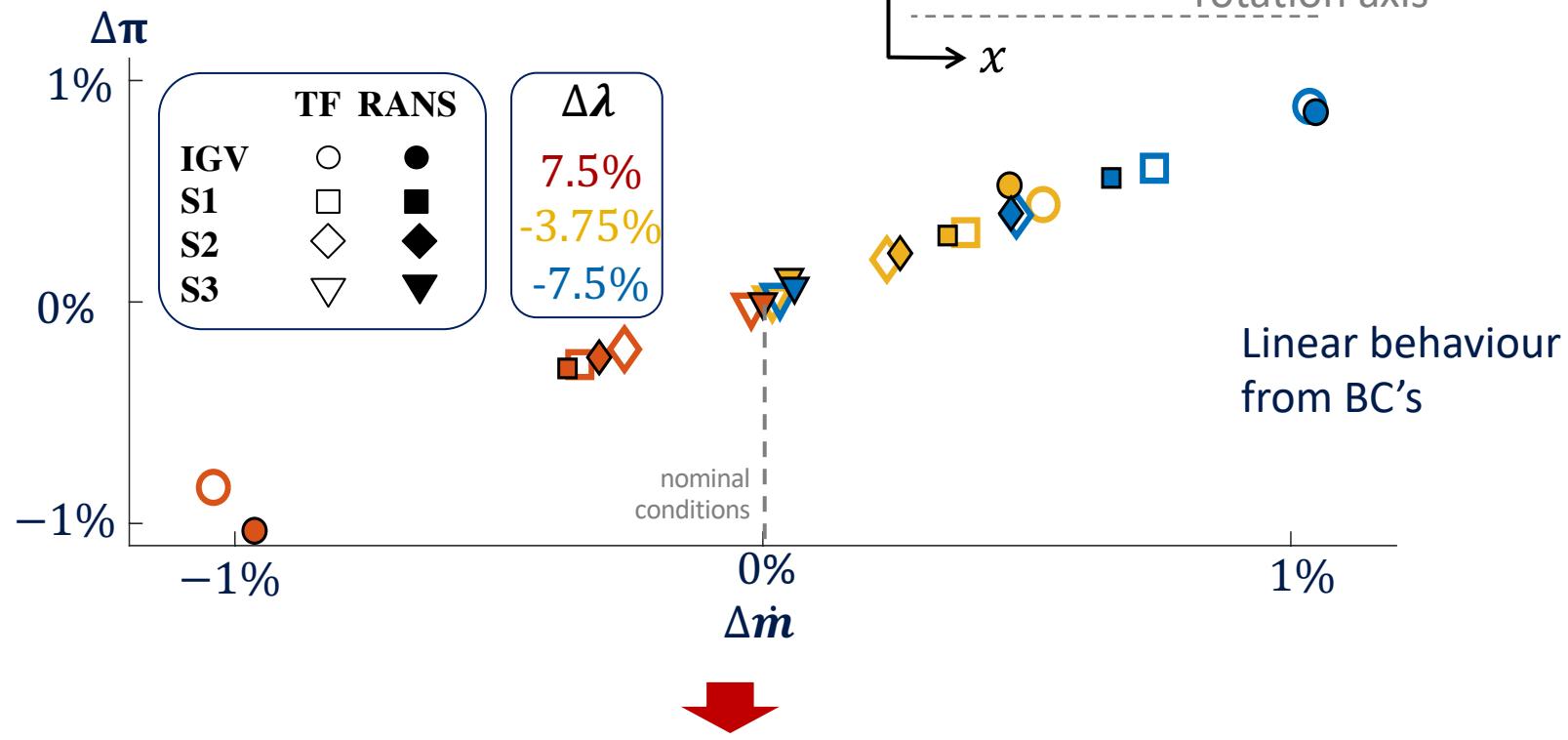
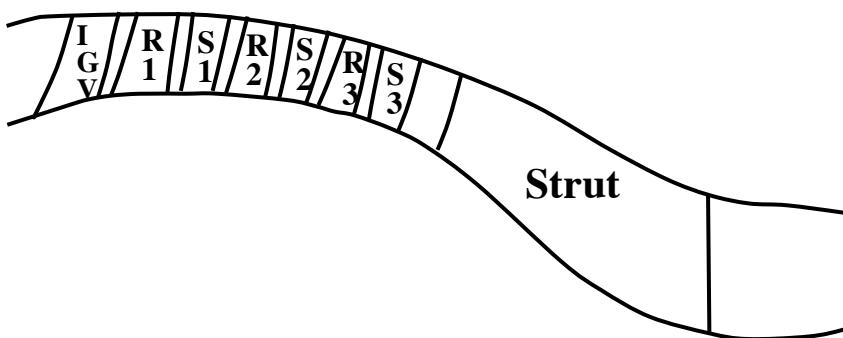
Geometry in through-flow model



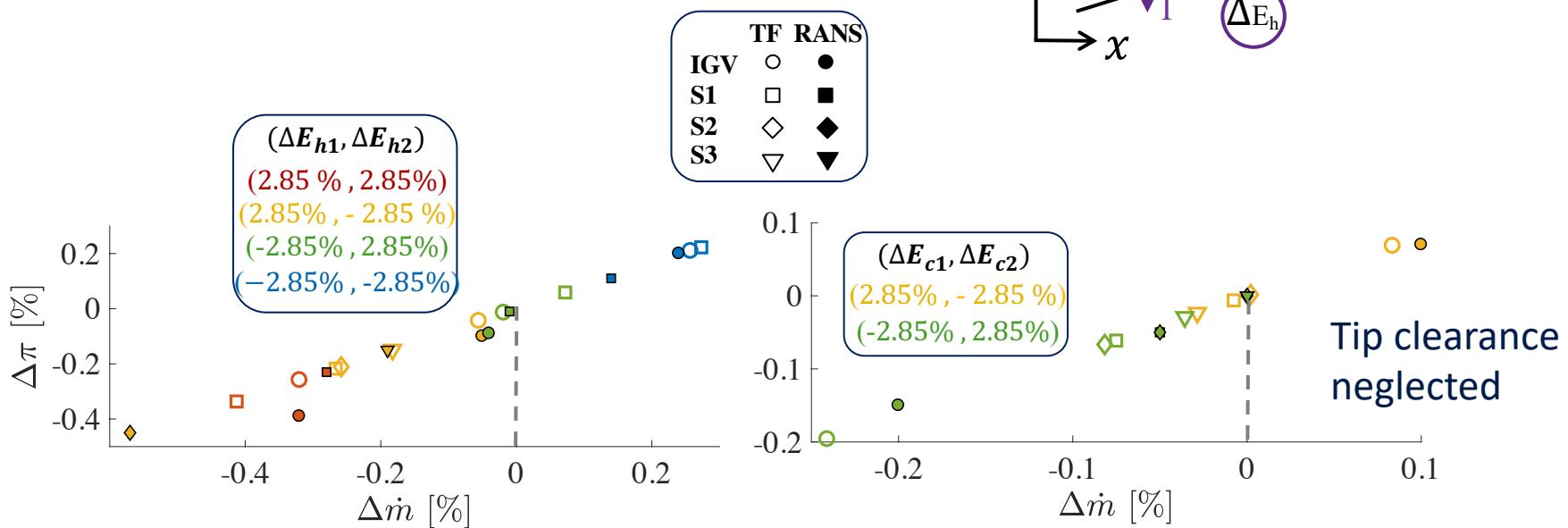
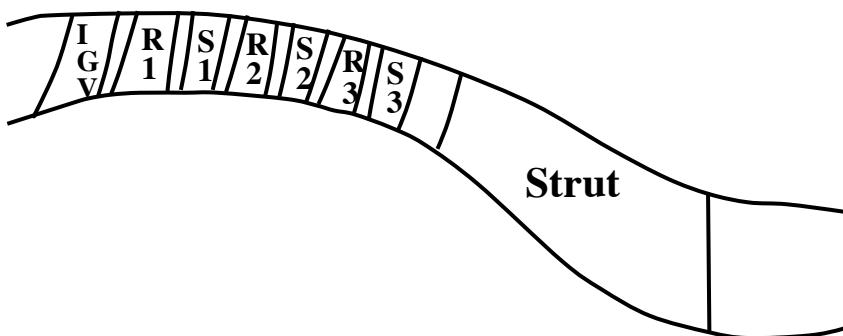
- Indirect impact on correlations by flow quantities



Geometric variabilities: stagger angle

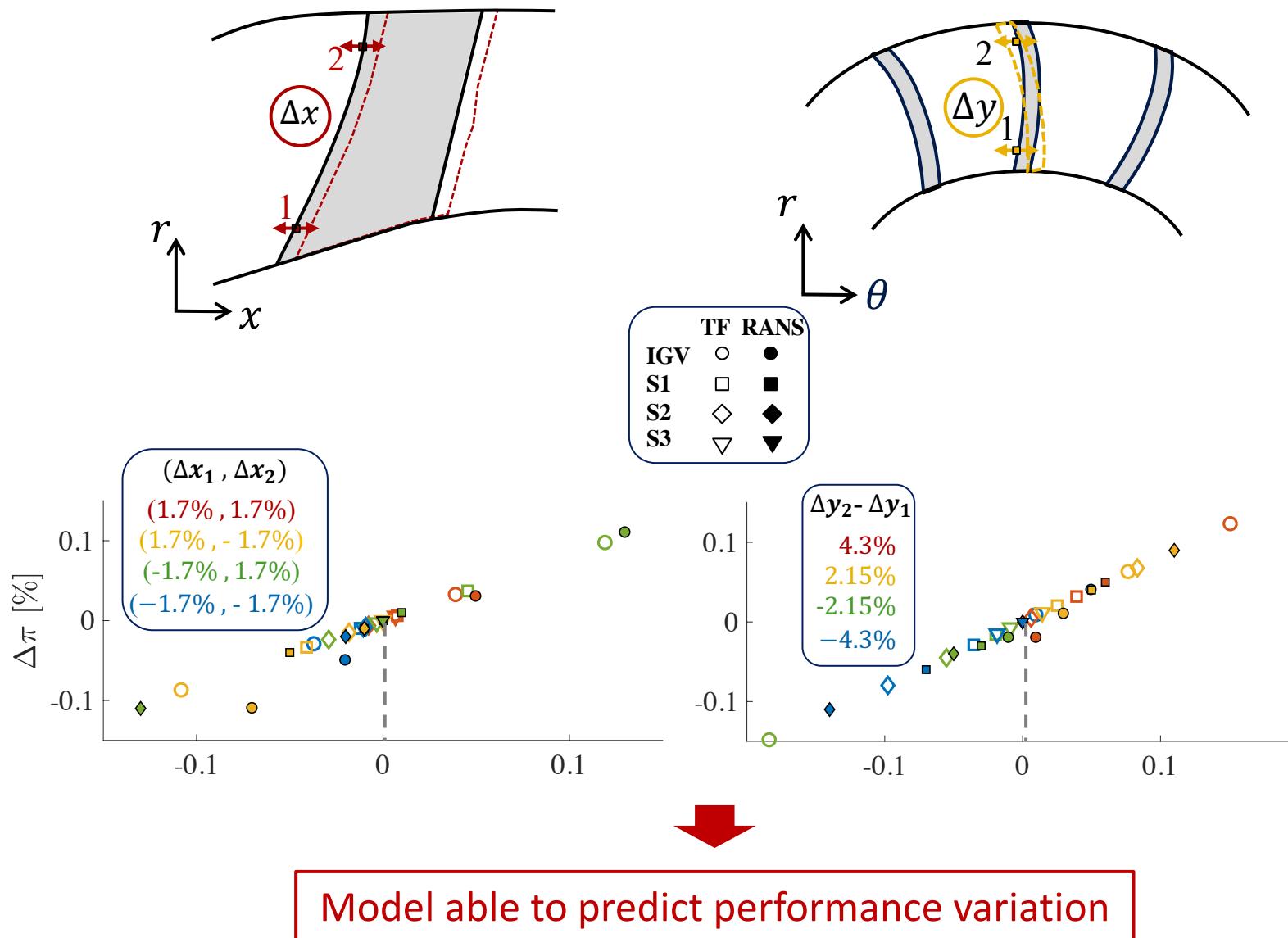


Geometric variabilities: endwalls



Model able to predict performance variation

Geometric variabilities: blade position



Conclusion

Through-flow model

- Reliable low-fidelity method
- Good prediction of performance
- Strong dependence between performance prediction and correlation accuracy
- Promising approach to drastically reduce CPU cost compared to 3D RANS for multi-fidelity approach and UQ

Geometrical variability

- Global good agreement for performance variation
- Promising first step towards the use of TF modeling for geometric uncertainty quantification

Future work

- Correlation improvement @ high incidence
- Thorough analysis of geometric variability propagation
- Strength and weakness of the model

Acknowledgement

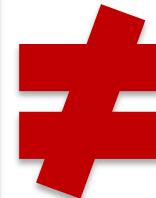
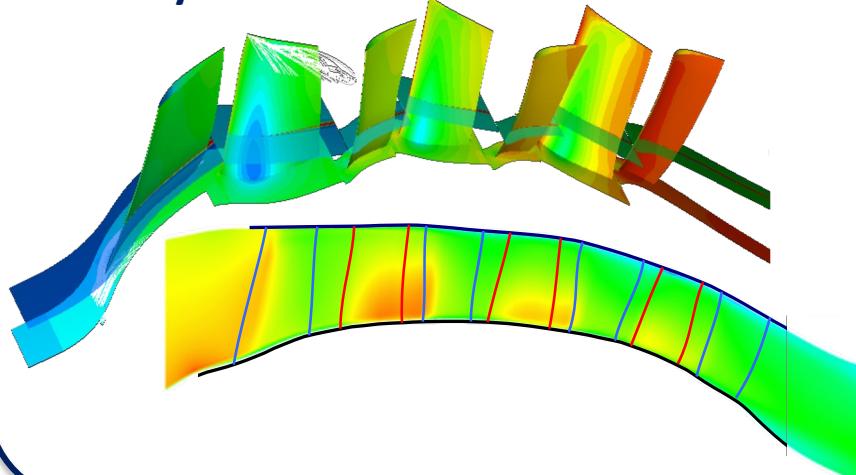
Funding for this research is provided by the Walloon region, under grant no. 7900 in the frame of the project MARIETTA



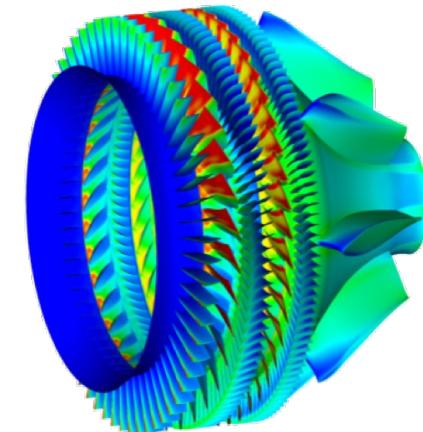
BACK-UP

Relevance

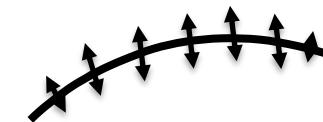
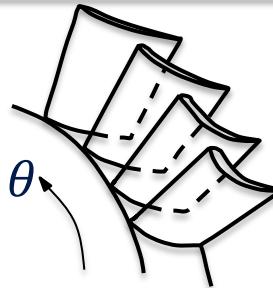
Axisymmetric TF simulation or 3D RANS



Mistuning

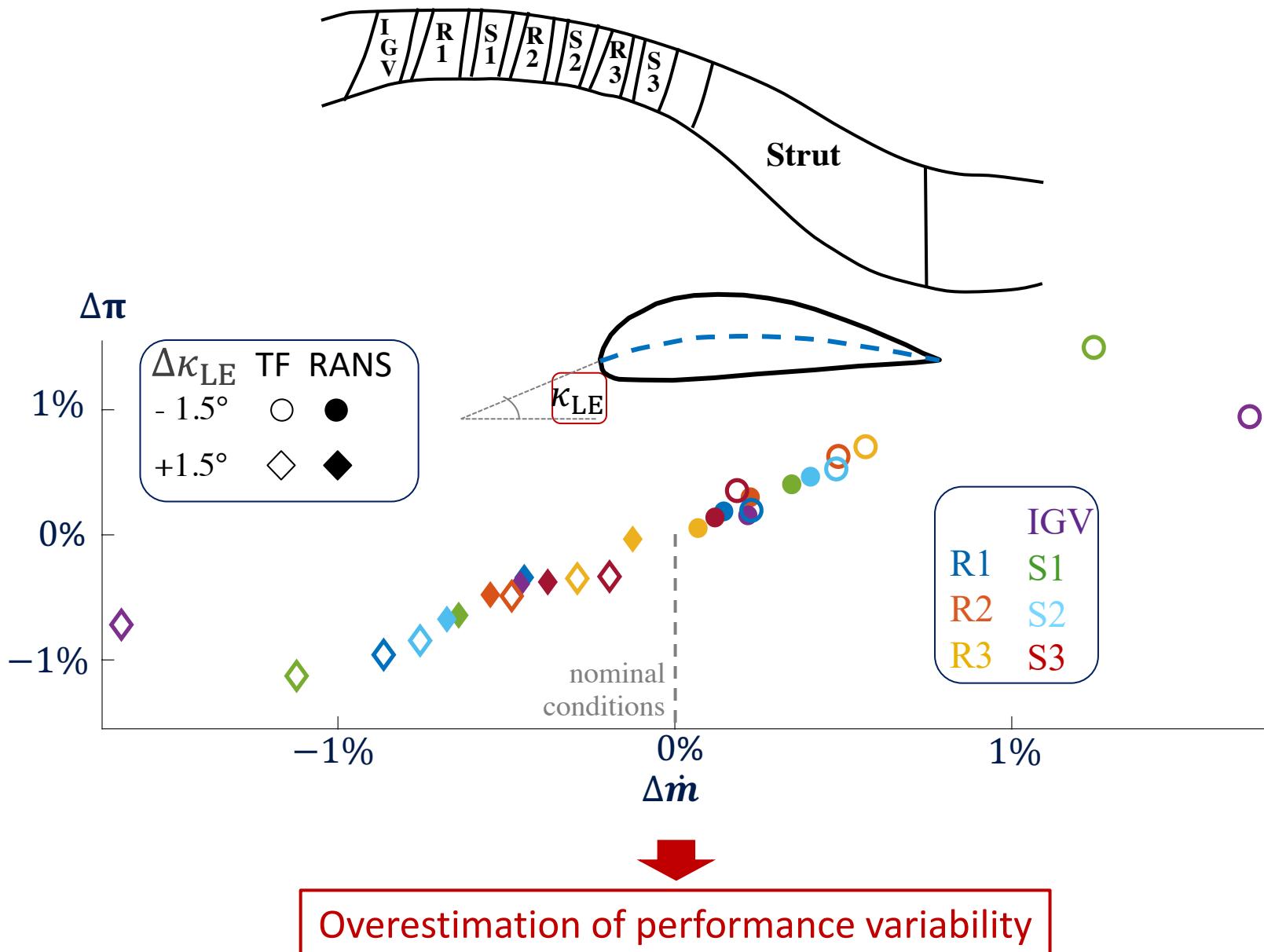


But



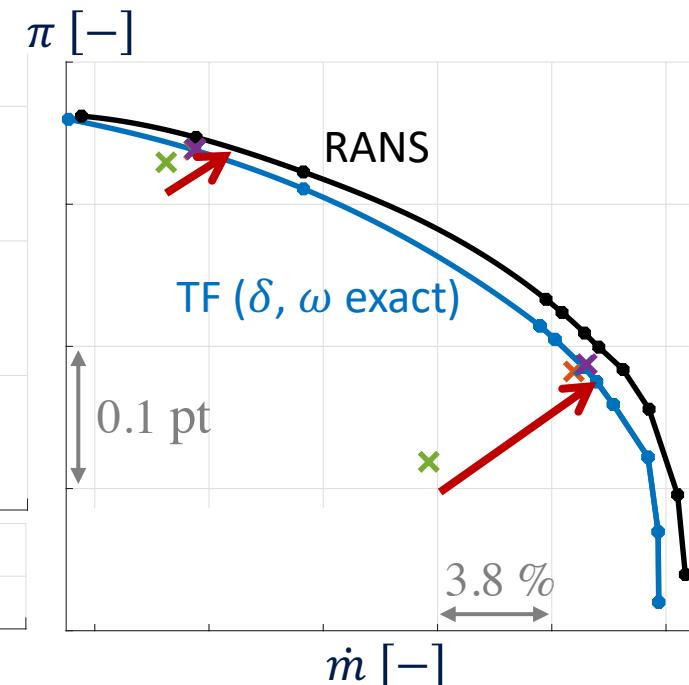
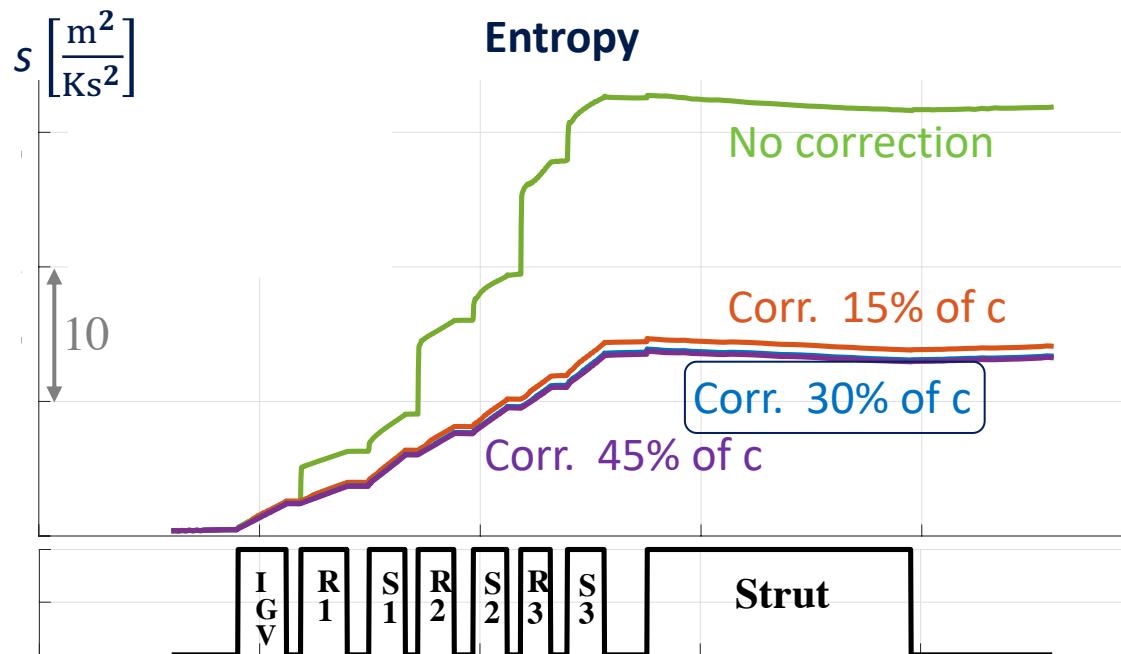
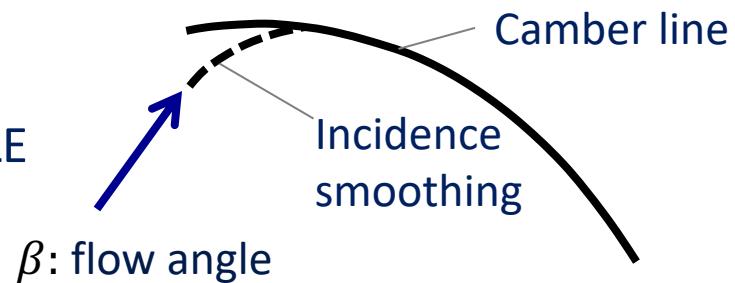
- Recurring patterns (tolerances, blade production, ...)
- Low deformation distribution

Applications: blade angle variability



Incidence correction

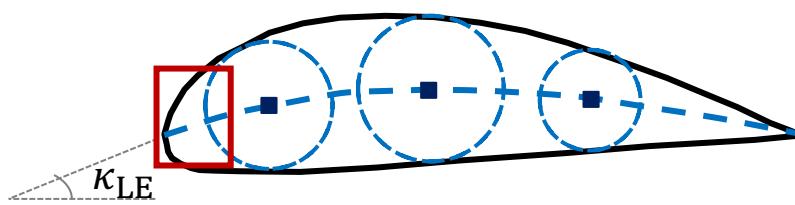
- Avoid flow angle discontinuity
- Modification of blade skeleton @ LE
- Unchanged correlation input



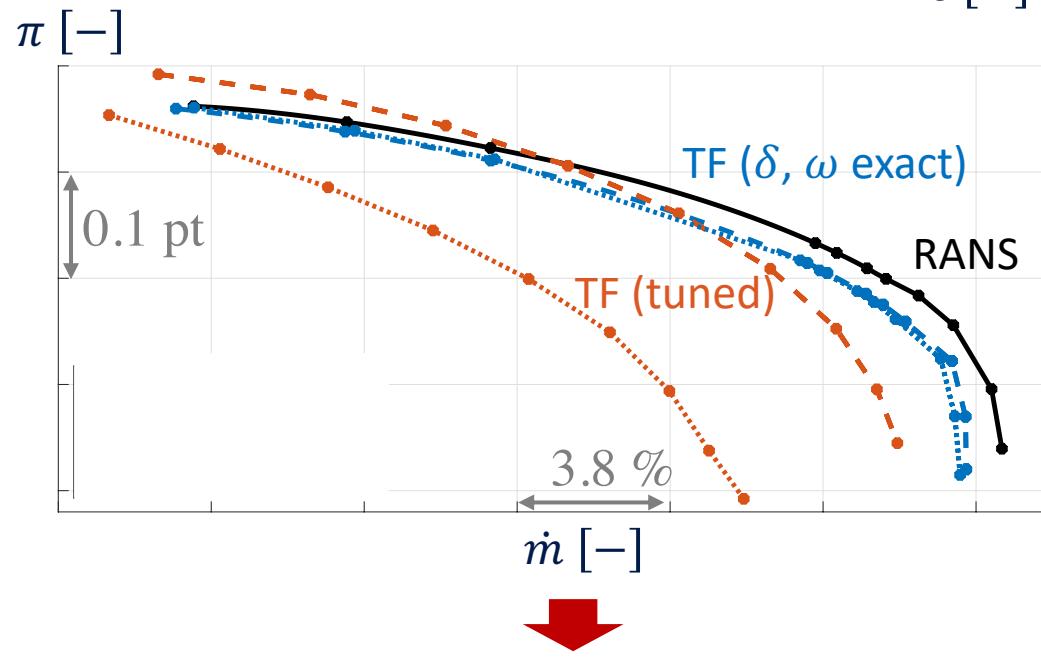
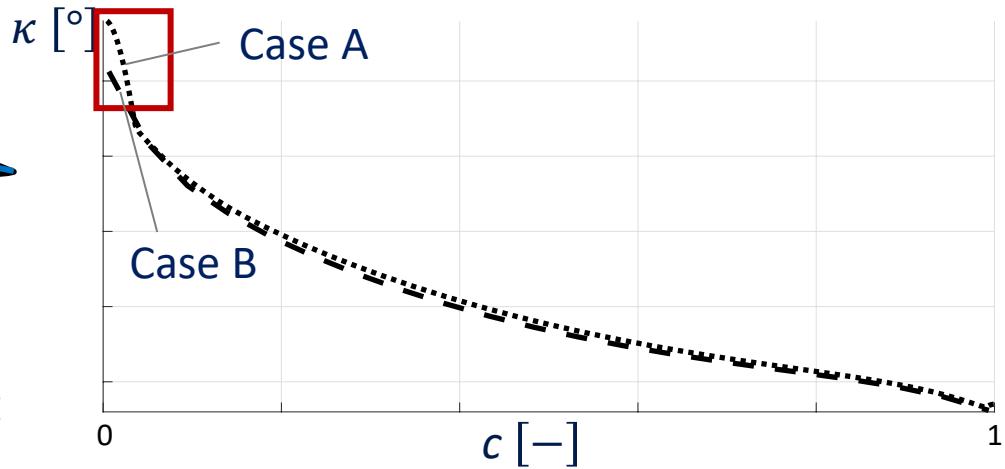
Incidence correction can smooth variability @ LE



Camber line definition



Definition not unique close to LE
→ Large impact on correlation input

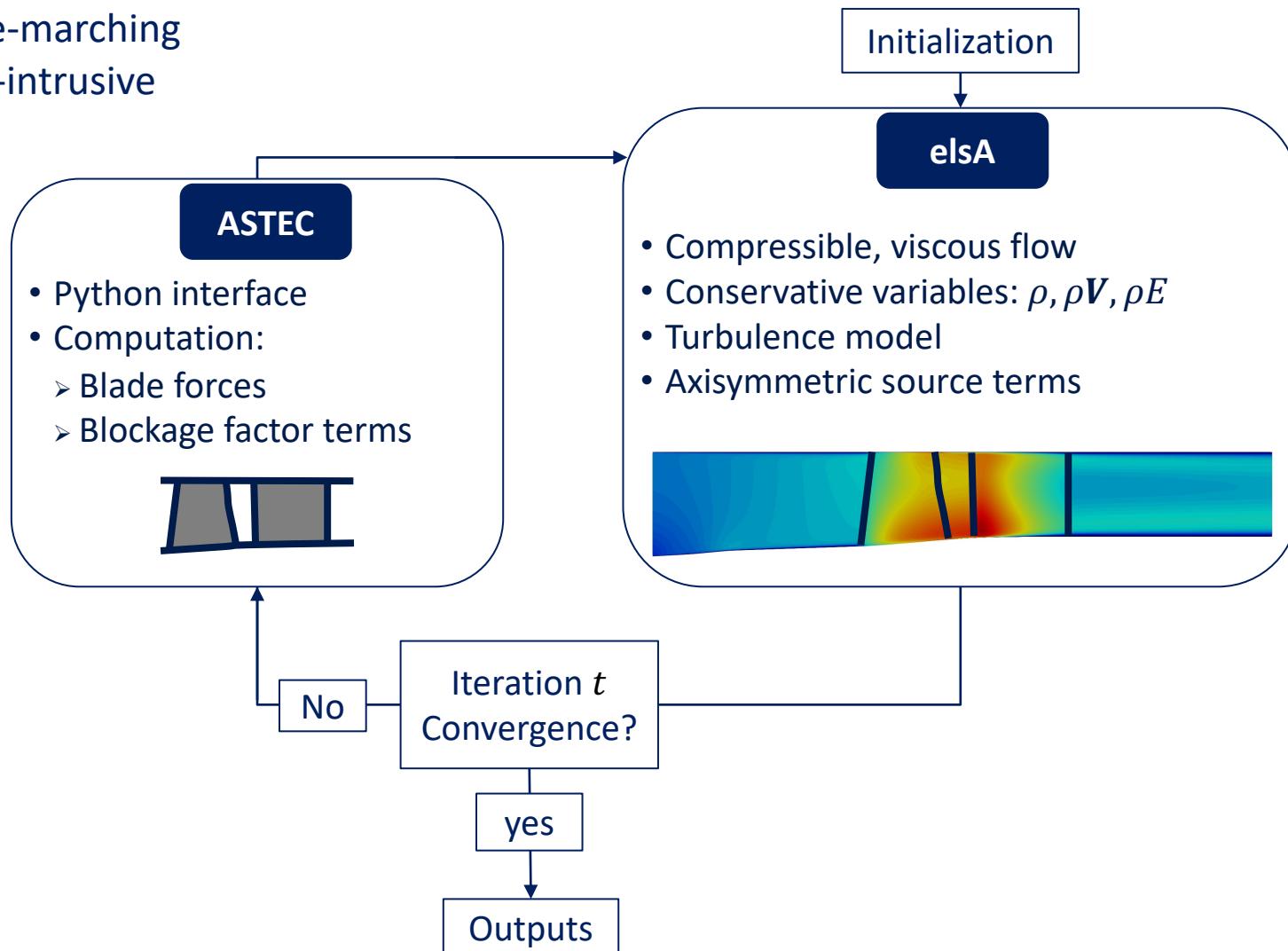


Strong dependence of model prediction with respect to LE blade angle

Viscous through-flow model: ASTEC

Methodology:

- Time-marching
- Non-intrusive



Modern compressor: comparison to RANS

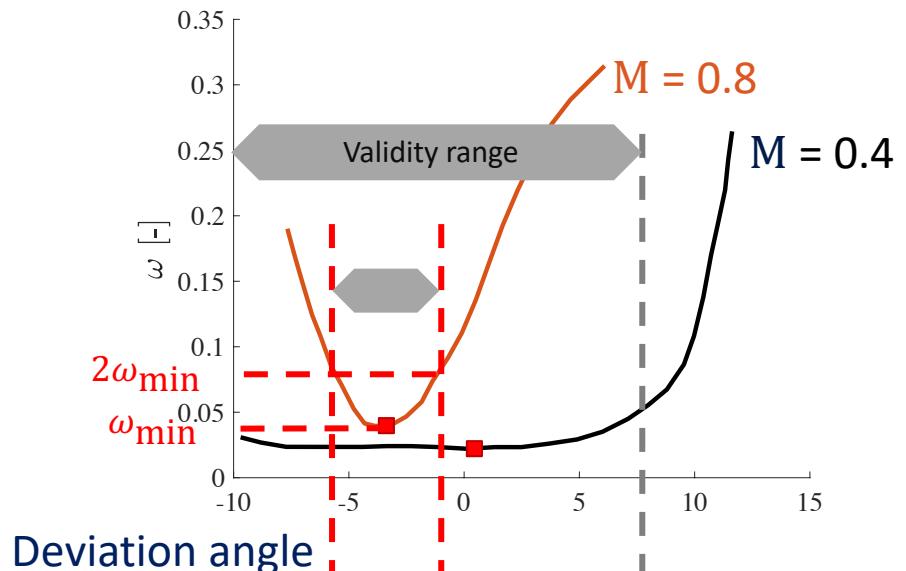
Impact of Mach number

- Minimum-loss incidence angle shifted
- Increase of ω_{\min}
- Narrow range of validity
- Inconsistency between loss validity range and deviation linear range

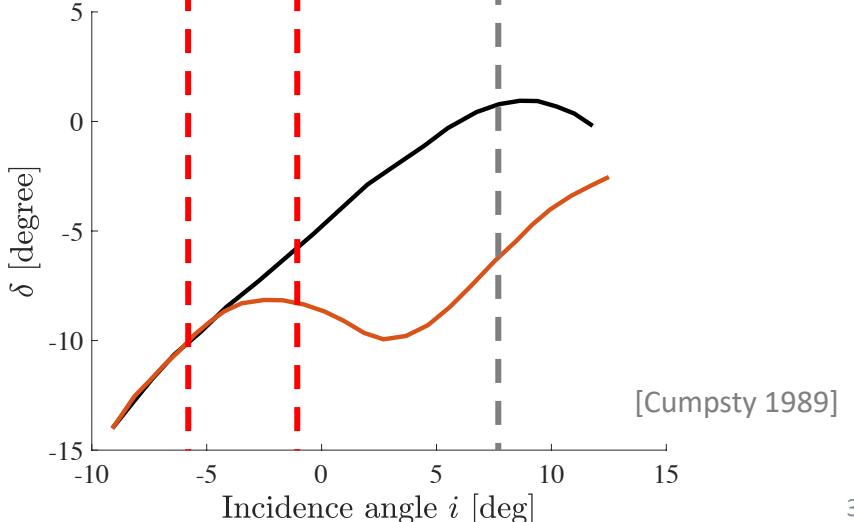
Correlations **not calibrated** for these flow conditions

Measurements of C4-series cascade

Loss coefficient



Deviation angle



[Cumpsty 1989]