



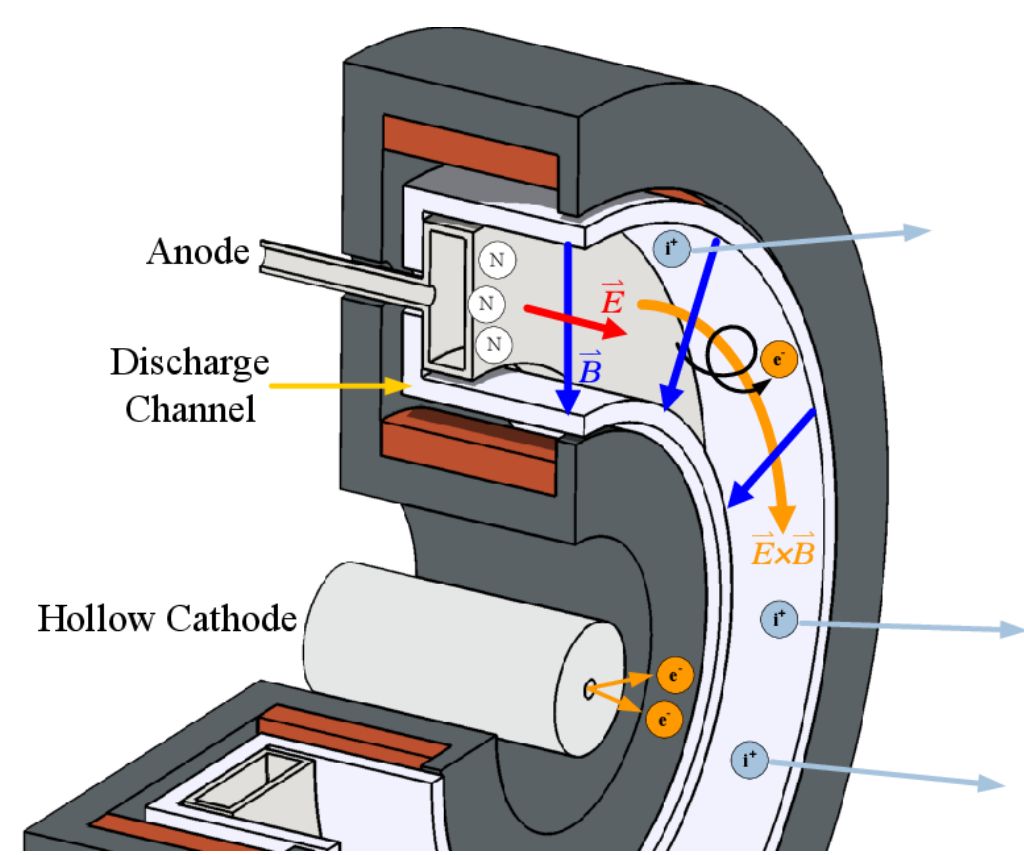
## Hall effect thrusters

**Very high specific impulse**  
**Flexible charge density**

- **Applications:** satellite positioning & long duration missions
- **Belgian industry:** power units Thales Alenia Space

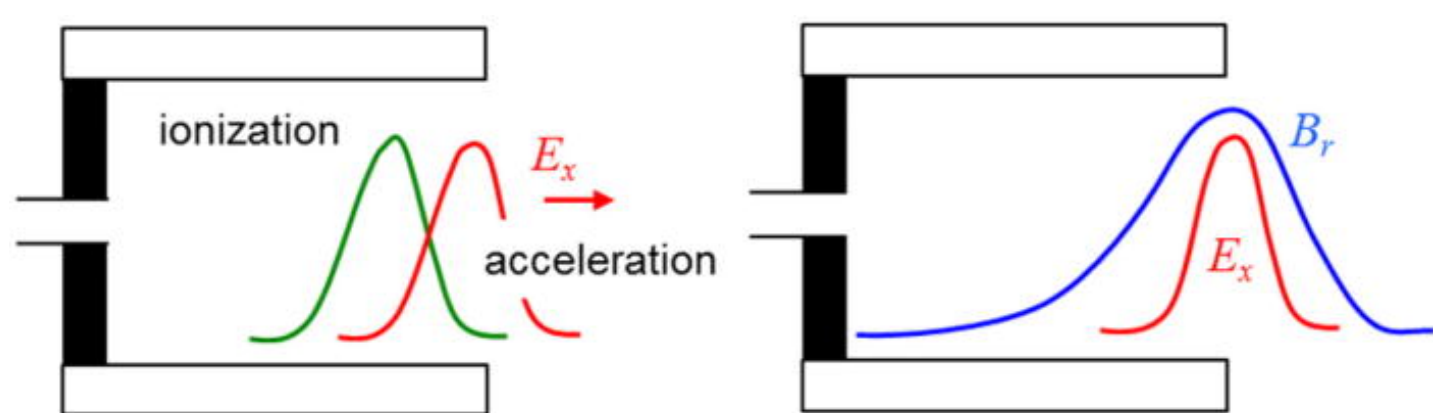
### Operating principle

Electron trapping and high speed  $\sim \mathbf{E} \times \mathbf{B}$  drift  
→ high electric potential  
→ no charge density limitation  
→ en situ ionization



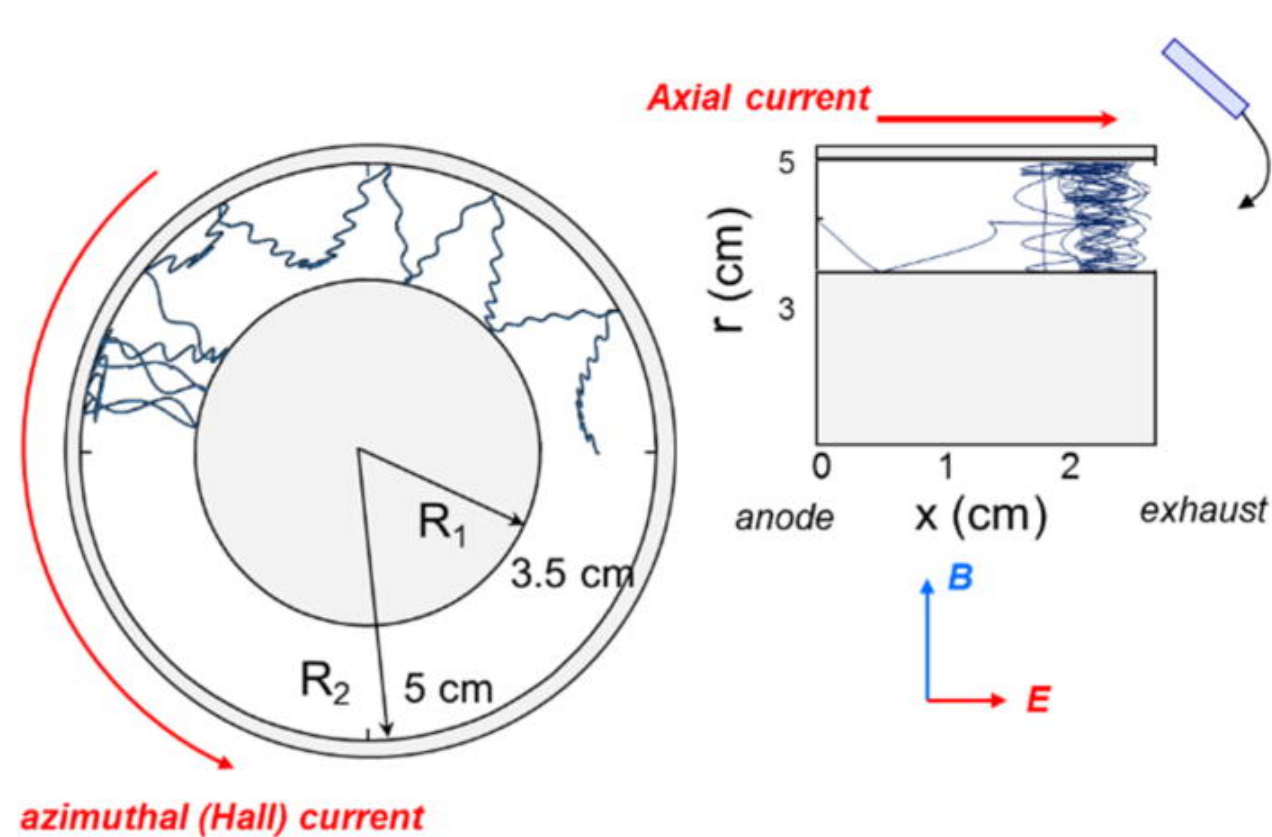
### Instabilities

**Breathing mode:** Periodic axial oscillation of particle densities → operating limit, variation of discharge current



Requirement : accurate collision model

**ECDI and MTSI:** Density waves in azimuthal and radial direction → operating limits, anomalous transport



Requirement: full 3D domain

## Thesis Objectives

### High Order Fluid Simulation of a HET

Lower computational cost than other methods  
Enables the study of small scale phenomena

### Towards: first principle simulation

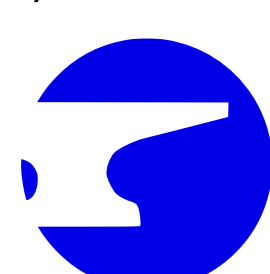
Objectives: investigate

- flowfield and estimate performance
- flow non-uniformity and instabilities
- anomalous transport of electrons

### Numerical challenges

- allow variety of complex constitutive laws
- stiff problem to solve - conditioning
- large range of scales - high accuracy

In-house code: ForDGe



## State of the Art

Simulation usually in 0d, 1D or 2D

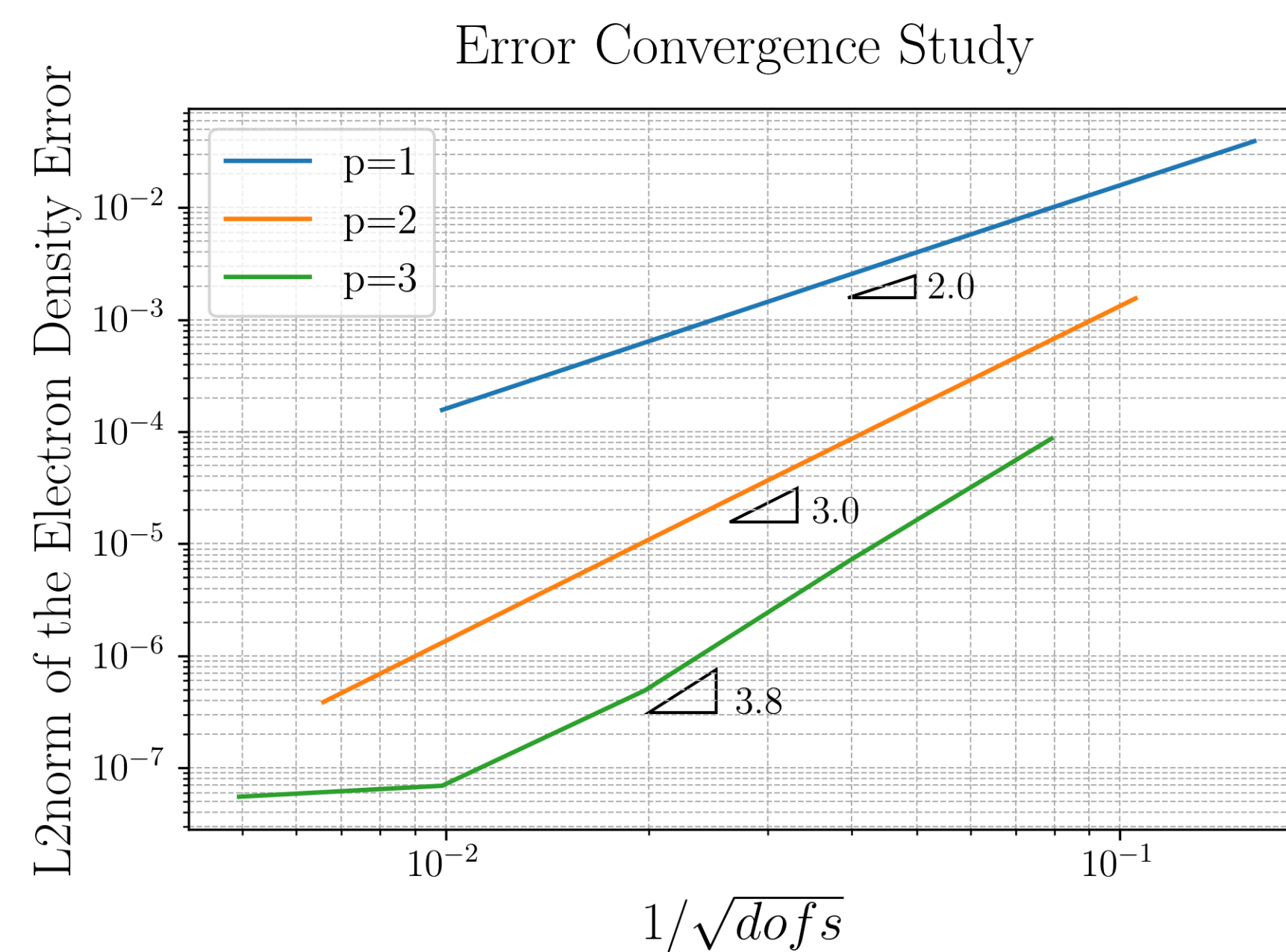
Particle in Cell (PIC) is the most popular Model (high cost)

Model	Name	Collisions	Heat Tr.	Neutrals	Ionization
2D PIC	Villafana	×	N/A	×	×
	Lafleur	✓	N/A	×	✓
2D Hybrid	Dominguez	✓	✓	✓	✓
2D Fluid	Joncquieres	✓	×	×	✓
3D PIC	Villafana	×	N/A	×	×

## Current State of ForDGe

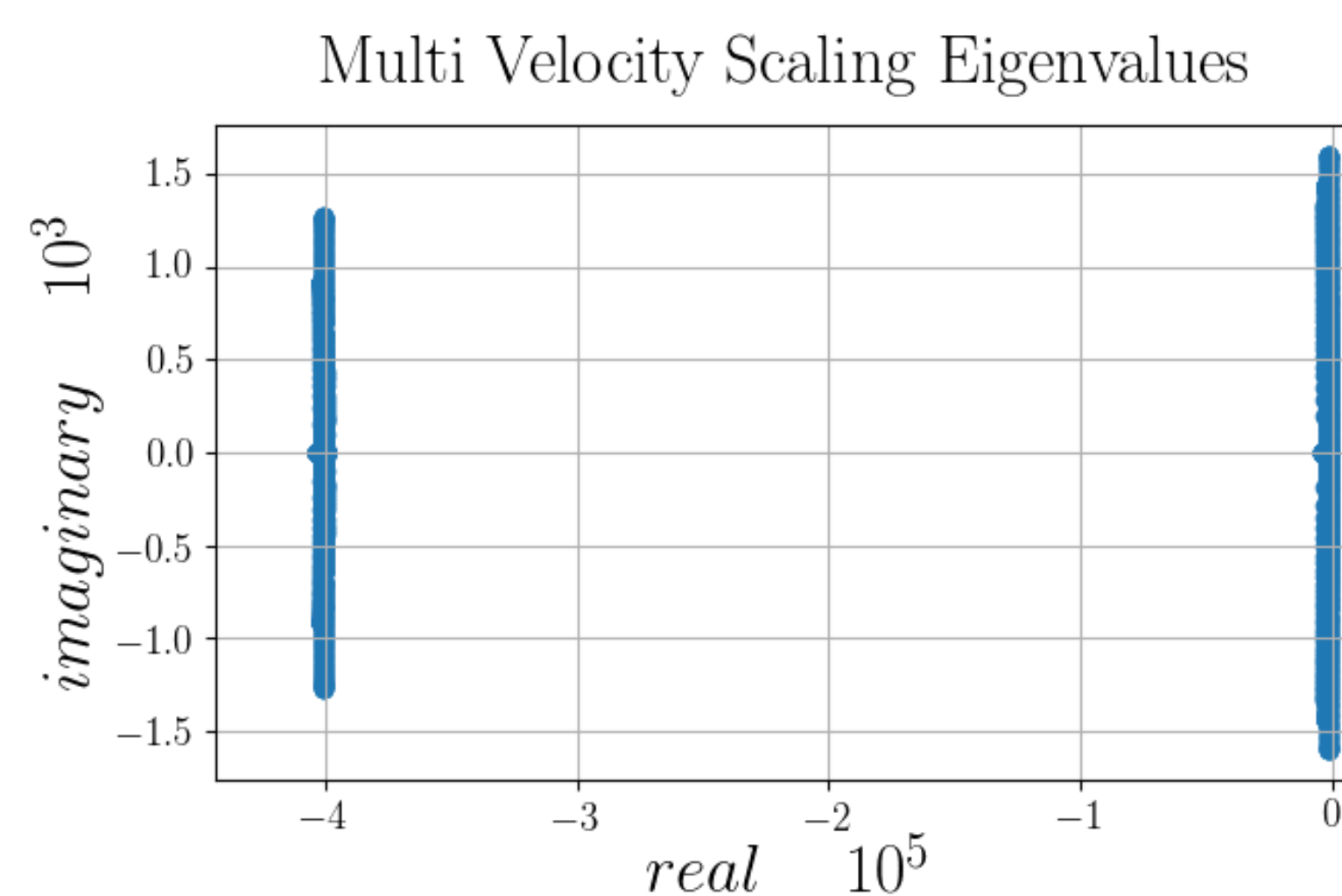
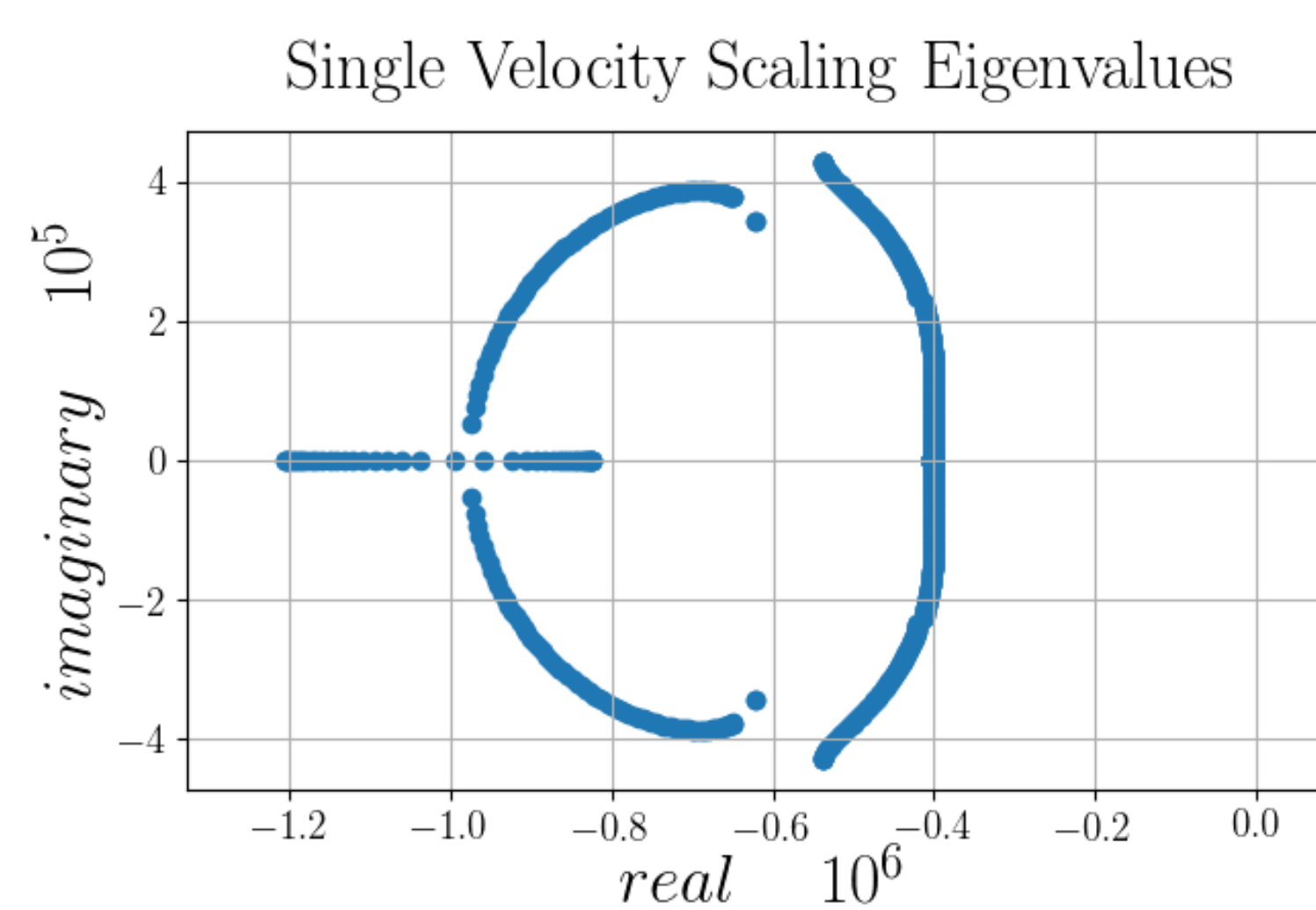
### High Order Accuracy

Required for small phenomena such as sheaths and instabilities



### Variable Dependent Scaling

Better conditioning through variable dependent velocity scaling  
Leads to variable dependent time scaling



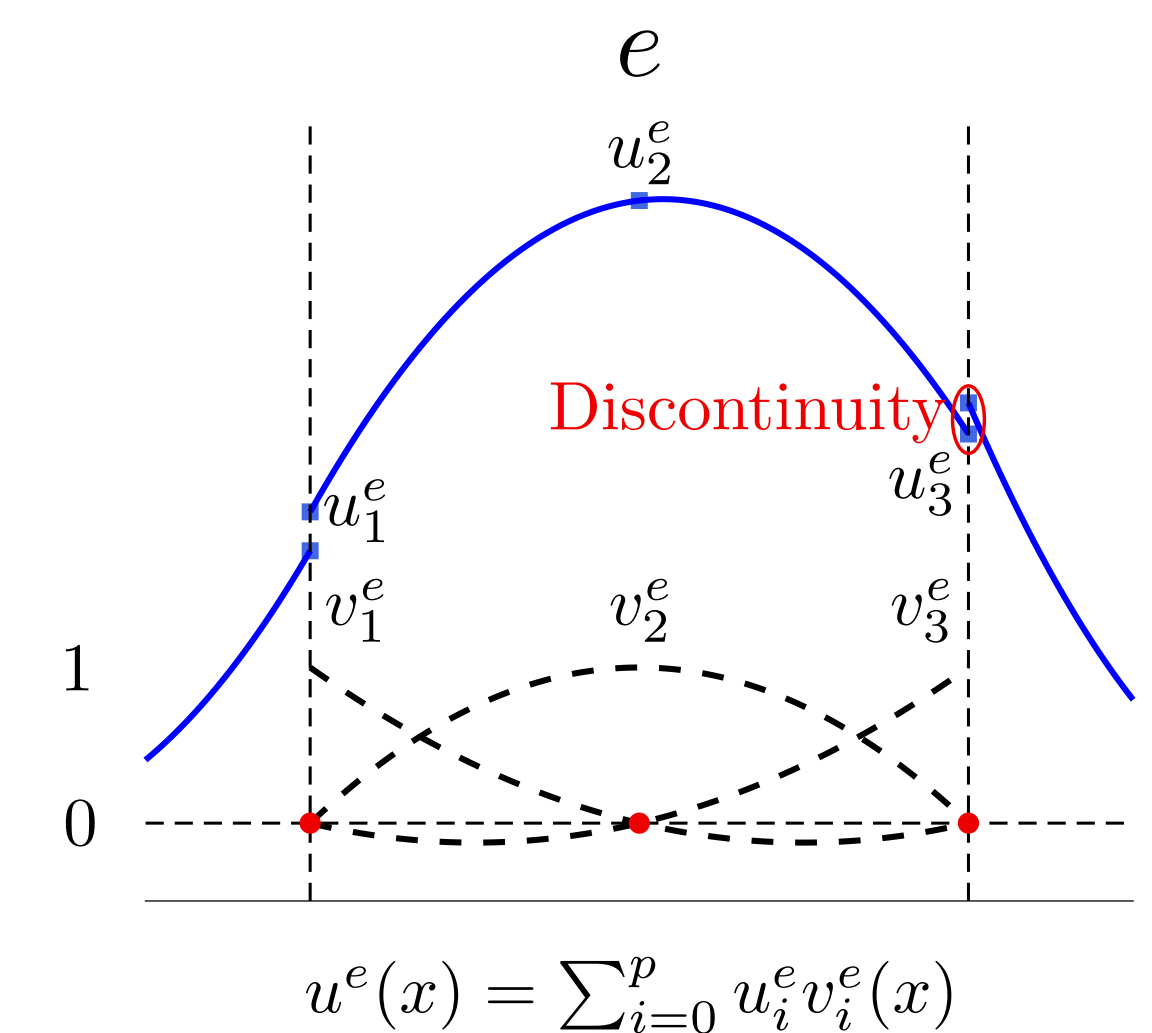
## Future Developments

Polar Coord Formulation	→	Circular Channel
Added Dimension in Model	→	Axisymmetric Simulation
Collision Modeling	→	Ionization
Combined	→	High Resolution 3D Sim

## ForDGe Software

### High order Discontinuous Galerkin method

- Stable for generic convection-diffusion-reaction
- Low dispersion/dissipation error on arbitrary meshes
- HP-adaptation



## Governing Equations

### Multi-Fluid Model

#### Boltzmann Equation

$$\partial_t f_\alpha + v \partial_x (f_\alpha) + \partial_v \left( \frac{F_\alpha}{m_\alpha} f_\alpha \right) = S_\alpha^{coll}$$

#### First 3 moments divided by particle mass

$$\partial_t n_\alpha + \partial_x (n_\alpha v_\alpha) = S_\alpha^{(n)}$$

$$\partial_t (n_\alpha v_\alpha) + \partial_x (n_\alpha v_\alpha^2 + \frac{p_\alpha}{m_\alpha}) = S_\alpha^{(m)}$$

$$\partial_t (n_\alpha e_\alpha) + \partial_x (n_\alpha v_\alpha h_\alpha) = -\frac{1}{m_\alpha} \partial_x q_\alpha + S_\alpha^{(e)}$$

### Choice

- Neutral, ion & electron frame
- Moments
- Particle and wall collisions

### Electro-Magnetic Model

#### Electric Potential

$$\partial_x (\partial_x V) = -\frac{(n_+ - n_-) Q_0}{\epsilon}$$

#### Magnetic Field

Prescribed and not computed

#### Lorentz Forces

$$\mathbf{F} = n_\alpha Q_0 (-\nabla V + \mathbf{v} \times \mathbf{B})$$

## First Year Objective

### 2.5D Axisymmetric Simulation of HET

Three species:  $e^-$ , Ar,  $Ar^+$   
Lorentz forces  
Cylindrical coordinates

