

# Acquiring the successor function of symbolic numbers: longitudinal comparison of verbal number words and cardinal number gestures

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## Introduction

Children would achieve a complete understanding of the cardinal principle through the discovery of, a conceptual rule, the successor function, which is that every number word  $n$  in the verbal number sequence has a strict predecessor/successor with a cardinal meaning of  $n-1/n+1$ , respectively (Carey, 2004, 2009; Sarnecka & Carey, 2008). It has been suggested that counting would implement the successor function in two stages. Children would first work out the direction of the numerical change the child before the unit of the change. These conceptual progress were found to be accessible only to cardinal principle knowers (Give-a-number task).

Counting activities and basic "+1" small calculation were found to be important sources of knowledge for the acquisition of the successor function (Schneider et al., 2020, 2021ab) but they might not be the only ones. Converging lines of evidence suggest that children's ability to use their fingers in numerical contexts contributes to their understanding of numerical concepts (Roesch & Moeller, 2015) but there is no consensus at present on the role of fingers in cardinal knowledge development. Some authors found no advantage of cardinal number gestures compared to number words in 2- to 5-year-olds (Nicoladis et al., 2010) while others showed that children who do not master the cardinal principle were more accurate at estimating numbers with cardinal finger gestures than with number words (Gunderson et al., 2015).

## Aims

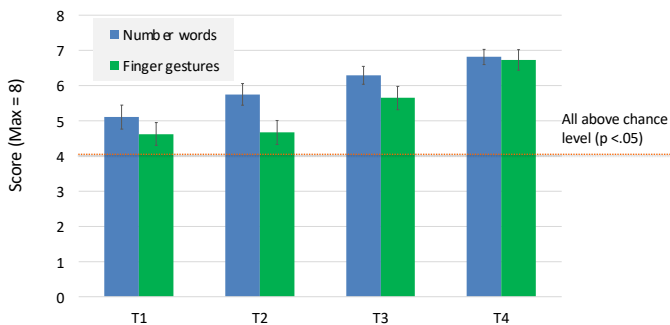
- Tracking the two stages of development the successor function in a longitudinal study using the Direction and the Unit task
- Examining how finger might contribute to the discovery of the successor function
- Exploring the relationship with cardinal knowledge development (Give-a-number task)

## Results

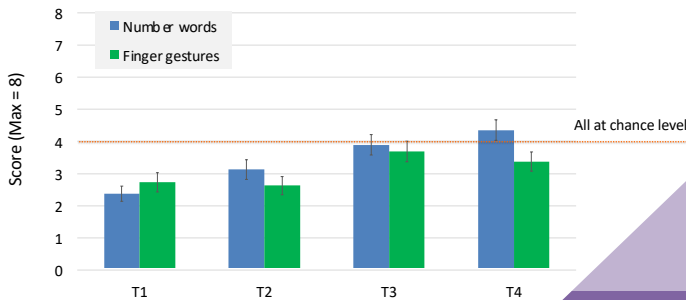
Repeated Measures ANOVA :

- Task :  $F(1, 47) = 220.9, p < .001$
- Modality :  $F(1, 47) = 7.8, p < .01$
- Time :  $F(3, 141) = 22.3, p < .001$
- No significant interaction

### Direction Task



### Unit Task



References:

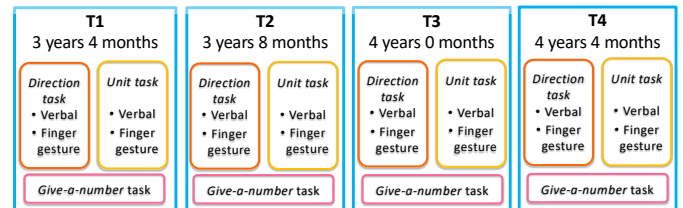
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## Methodology



48 preschoolers tested 4 times every 4 months from the age of 40 months

### TIME LINE



**Direction task**  
Verbal number words

Step 1. I put [three] tokens in the box. There is [three]  
Step 2. Now I'm closing the box...  
Step 3. ... and I'm putting this in (+1) / taking this out (-1)  
Is there [two] or [four] ?

**Unit task**  
Verbal number words

Step 1. I put [three] tokens in the box. There is [three]  
Step 2. Now I'm closing the box...  
Step 3. ... and I'm putting this in (+1) / this and this in (+2)  
Is there [four] or [five] ?

**Materials and Procedure**

Step 1. Putting tokens all at once in the box and communicating how many (number words or gestures)

Step 2. Closing the box

Step 3. adding or removing tokens

Size (starting points)

- Small numerosities : [2, 3]
- Large numerosities : [6, 7]
- > 2 items x 2 size x 2 numerosities = 8 items

Step 1. I put this [three] tokens in the box. There is this [three]  
Step 2. Now I'm closing the box...  
Step 3. ... and I'm putting this in (+1) / taking this out (-1)  
Is there [two] or [four] ?

**Direction task**  
Cardinal finger gestures

Step 1. I put this [three] tokens in the box. There is this [three]  
Step 2. Now I'm closing the box...  
Step 3. ... and I'm putting this in (+1) / this and this in (+2)  
Is there [four] or [five] ?

**Unit task**  
Cardinal finger gestures

### Give-a-number task

- The child received 10 tokens : Can you give me [three] tokens? »
- Cardinal development level = the largest numerosity accurately identified by the child two out of three times

### Distribution of children as a function for their verbal cardinal knowledge level across time

	Give-N	T1		T2		T3		T4	
		Frequency	%	Frequency	%	Frequency	%	Frequency	%
Pre-numeral knowers	0	2	4.2	3	6.3	0	0	0	0
One-knowers	1	5	10.4	4	8.3	0	0	0	0
Two-knowers	2	26	54.2	10	20.8	14	29.2	6	12.5
Three-knowers	3	11	22.9	14	29.2	8	16.7	8	16.7
Four-knowers	4	3	6.3	5	10.4	11	22.9	3	6.3
Five-knowers	5	0	0	5	10.4	1	2.1	6	12.5
Six-knowers	6	0	0	0	0	2	4.2	3	6.3
Seven-knowers (max)	7	1	2.1	7	14.6	11	22.9	21	43.8
Total		48	100	48	100	48	100	48	100

### Mean performance in each task in subset- and CP-knowers (Give-N task)

Task	N	Subset-knowers				CP-knowers			
		T1	T2	T3	T4	T1	T2	T3	T4
Direction	Number words	5.05*	5.42*	5.65*	5.8*	/	6.35*	6.88*	7.27*
	Finger gestures	4.57	4.23	5.39*	5.47*	/	5.47*	5.88*	7.3*
Unit	Number words	2.27	2.74	3.22	3	/	3.82	4.52	4.97
	Finger gestures	2.7	2.45	3.91	2.13	/	2.94	3.48	3.94

\* above chance level (p < .05)

The development of the successor function is a long-lasting process which extend over a protracted period beyond the age of 4 years and 4 months.

Children first figure out the direction of the numerical change the child before the unit of the change.

Cardinal finger gestures provided no advantage in the discovery of the successor function

Subset-knowers performed above chance level in the Direction task, suggesting that they are able to understand the direction of the numerical changes. This result contradicts the idea that this important conceptual progress would only be accessible to cardinal principle-knowers

## Conclusion

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