Public defence of doctoral thesis

ARTIFICIAL INTELLIGENCE TECHNIQUES FOR DECISION-MAKING IN MARKET ENVIRONMENTS

by Thibaut Théate

11th September 2023





Graphical abstract

Artificial Intelligence Techniques for Decision-making in Market Environments





Source: Midjourney v4.

The AI revolution is upon us!







will survive th revolution?

Smart machines are meant to work for us, but there are already signs that we will end up working for them. What will the workplace of the future look like, and will your role still exist?

David Runciman

(Elena Lacey/Washington Post Illi Sat 19 Aug 2023 09.00 BST

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between technology invention and adoption across industries and

Robot and young woman face to face. GETTY author

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Artificial Intelligence – Warning

66 With great risk comes great reward.

-- Thomas Jefferson

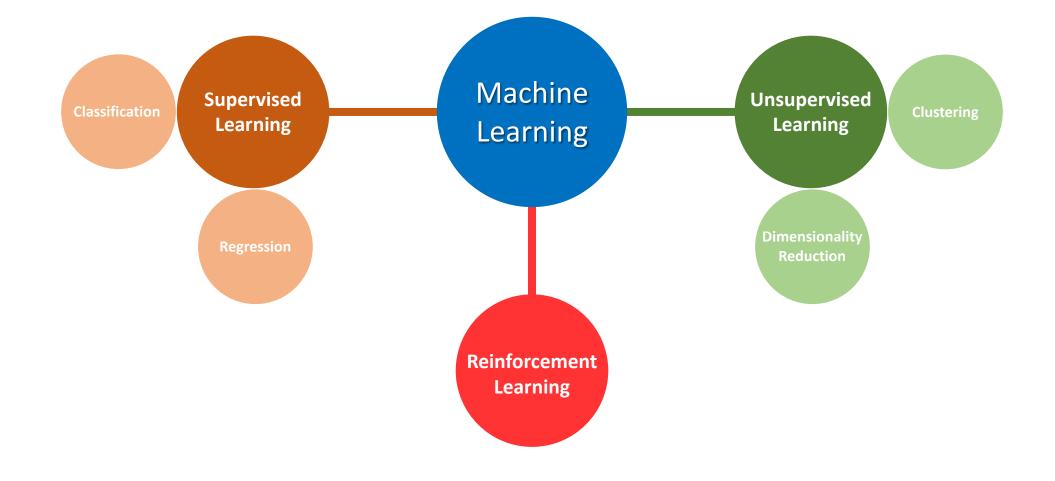


Primary risks related to Artificial Intelligence:

- Major security concerns (use by malicious actors);
- Reinforced economic inequalities (job displacement);
- Important concentration of power (e.g. OpenAI with ChatGPT);
- Manipulation and misinformation (AI-generated content);
- Discrimination and bias (societal and data biases).

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Machine Learning – Overview

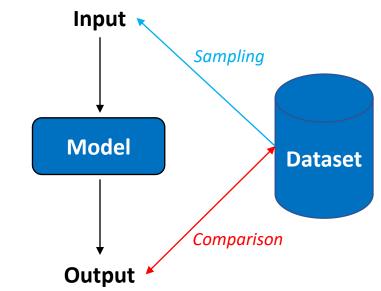


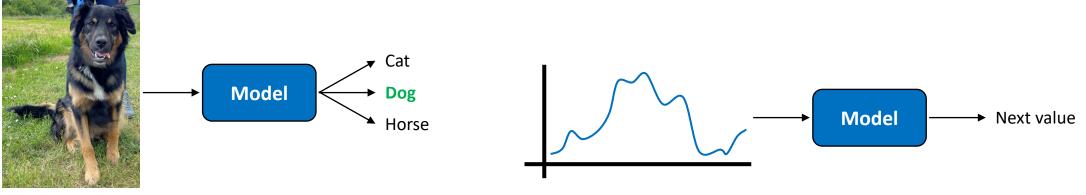
Supervised Learning

Core idea: *Supervised Learning* (SL) is concerned with the learning process of a function mapping an input to an output, based on a labelled dataset of input-output pairs.

Classification: The output is a categorical label.

Regression: The output is a continuous value.



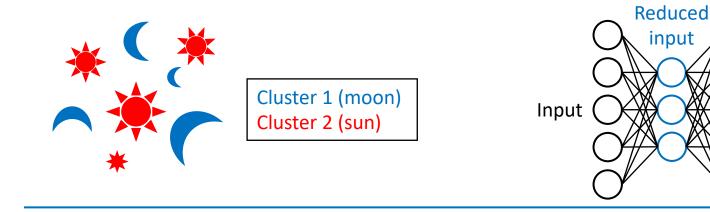


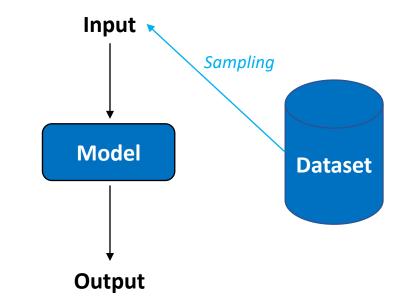
Unsupervised Learning

Core idea: Unsupervised Learning (UL) is concerned with the identification of patterns and structures within the input data from an unlabelled dataset.

Clustering: Grouping similar data points together into clusters.

Dimensionality reduction: Transforming high-dimensional data into a lower-dimensional space.





Input

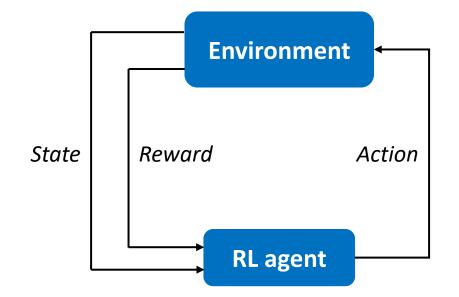
Reinforcement Learning

Core idea: *Reinforcement Learning* (RL) is concerned with the training of an agent by interacting with its environment through trial-and-error in order to achieve a specific goal.

Training loop:

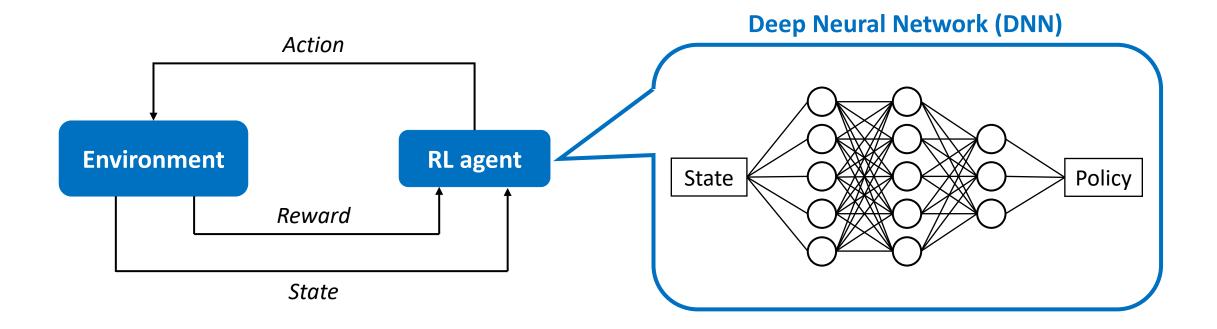
- 1. Observation of the environment;
- 2. Decision-making about the next action;
- 3. Reception of a reward as feedback;
- 4. Update of the decision-making policy.

Objective: Learning an optimal decision-making policy that maximises the cumulative reward over time.



Deep Reinforcement Learning (DRL)

Core idea: Combining *Deep Learning* (DL) and *Reinforcement Learning* (RL) in order to significantly improve the scalability of the RL approach (high-dimensional state and action spaces).



Markets everywhere!

Economic liberalisation => proliferation of markets.

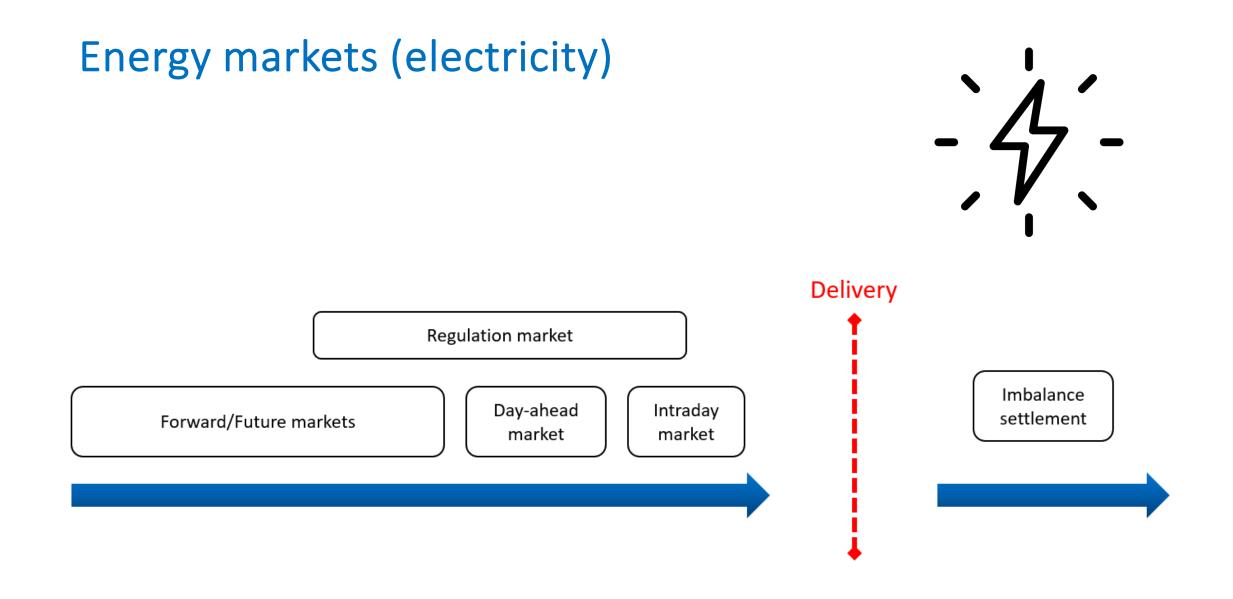
Interesting direction? Beyond the scope of this doctoral thesis...

Various markets for exchanging a diverse range of goods and services.

Numerous challenging (sequential) decision-making problems.

Tremendous impact on the population => huge potential.





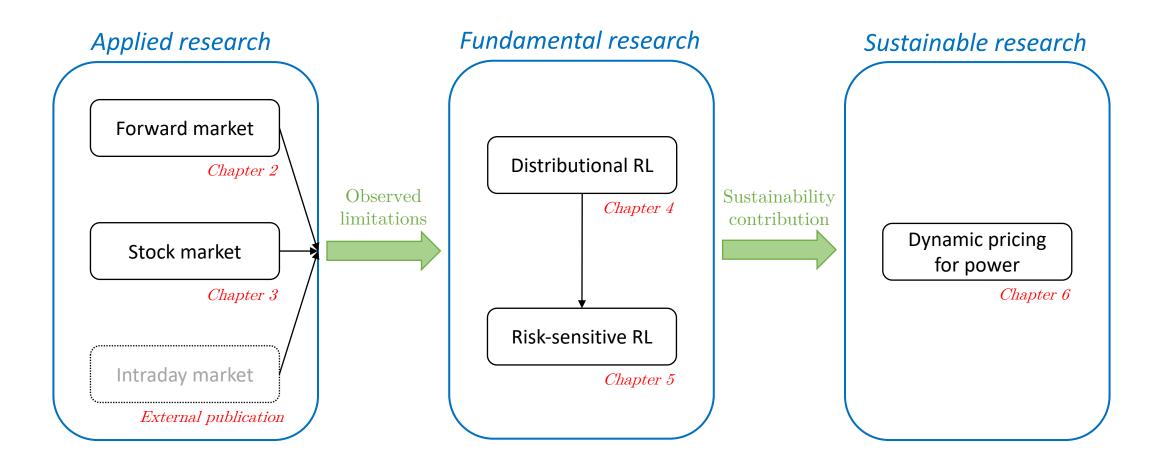
Scope of the doctoral thesis

The study of complex sequential decision-making problems related to markets, and the development along with analysis of novel algorithmic solutions on the basis of innovative AI techniques.



Source: Midjourney v4.

Outline of the doctoral thesis



List of publications



Six publications in peer-reviewed scientific journals (five as main author and one as co-author):

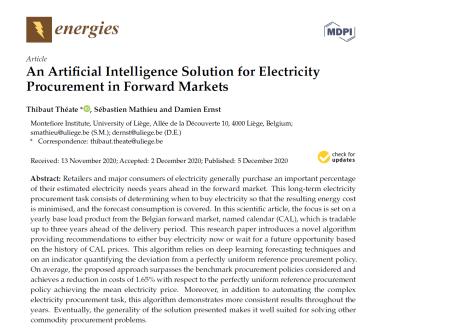
- Thibaut Théate, Sébastien Mathieu, and Damien Ernst. An Artificial Intelligence Solution for Electricity Procurement in Forward Markets. *Energies*, 13(23), 2020.
- Thibaut Théate and Damien Ernst. An Application of Deep Reinforcement Learning to Algorithmic Trading. *Expert Systems with Applications*, 173:114632, 2021.
- Thibaut Théate, Antoine Wehenkel, Adrien Bolland, Gilles Louppe, and Damien Ernst. Distributional Reinforcement Learning with Unconstrained Monotonic Neural Networks. *Neurocomputing*, 534:199–219, 2023.
- Thibaut Théate and Damien Ernst. Risk-Sensitive Policy with Distributional Reinforcement Learning. Algorithms, 16(7):325, 2023.
- Thibaut Théate, Antonio Sutera, and Damien Ernst. Matching of Everyday Power Supply and Demand with Dynamic Pricing: Problem Formalisation and Conceptual Analysis. *Energy Reports*, 9:2453–2462, 2023.
- Ioannis Boukas, Damien Ernst, Thibaut Théate, Adrien Bolland, Alexandre Huynen, Martin Buchwald, Christelle Wynants, and Bertrand Cornélusse. A Deep Reinforcement Learning Framework for Continuous Intraday Market Bidding. Machine Learning, 110(9):2335–2387, 2021.

Doctoral Thesis – Open Access

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Trading in the forward electricity markets

Publication: Thibaut Théate, Sébastien Mathieu, and Damien Ernst. An Artificial Intelligence Solution for Electricity Procurement in Forward Markets. *Energies*, 13(23), 2020.



Keywords: artificial intelligence; deep learning; electricity procurement; forward/future market



Source: Midjourney v4.

16

Problem statement

Context: Hedging for both retailers and large consumers of energy.

Objective: Determining when to purchase power over a certain trading horizon so that the resulting energy costs are minimised, while covering the predicted consumption.

Research question: How can innovative Artificial Intelligence (AI) techniques contribute to solve the decision-making problem behind the long-term electricity procurement task?

Thibaut Théate - Doctoral thesis public defence

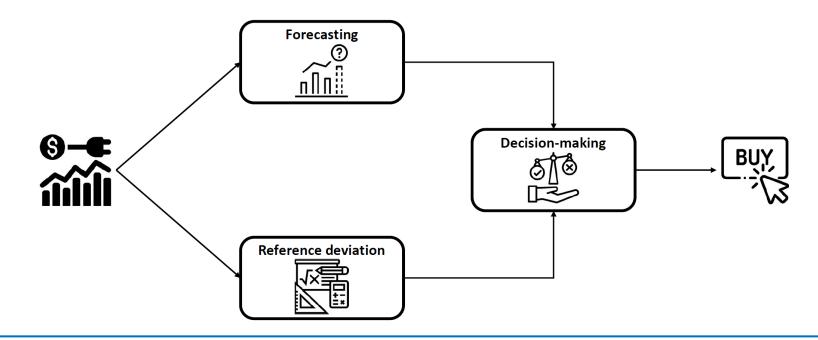






Contributions

- Mathematical formalisation of the sequential decision-making problem.
- Novel algorithmic solution on the basis of DL techniques, providing recommendations to either buy electricity now or wait for a future opportunity based on the history of forward prices.





Problem formalisation

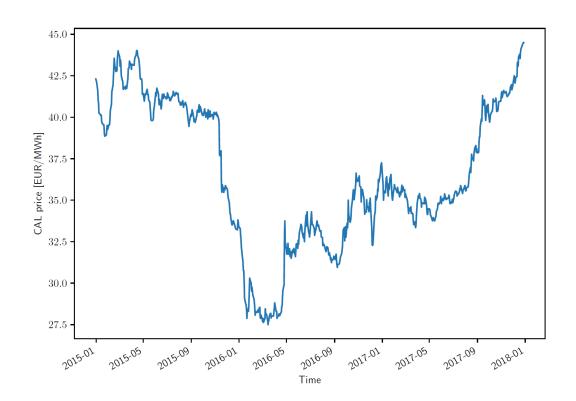
Supply source: Calendar (CAL) product from the Belgian forward market (*Ice Endex*).

Trading frequency: Daily.

Input: Price history and state information.

Output: Wait or purchase (a fixed quantity).

Objective: Minimisation of the costs.



Algorithmic solution – Overview

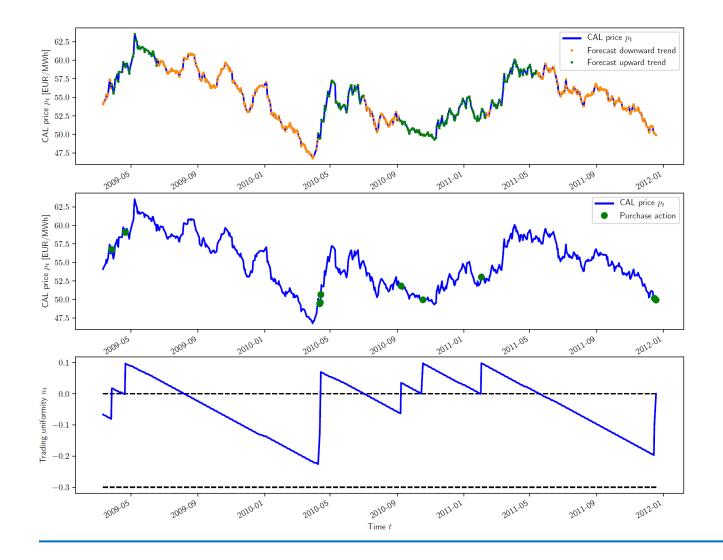


Core idea: To split purchase decisions over the procurement horizon to spread the trading risk, with nominal anticipation or delay depending on the expected market direction.

Three main parts:

- A forecasting mechanism for predicting the future dominant market trend;
- A mathematical indicator quantifying the deviation from a reference policy;
- An interpretable decision-making process taking as input this information.

Results – Analysis



DL forecaster:

- Accuracy of approximately 80%;
- Convenient predictions.

Decision-making:

- Valuable interpretability;
- Ability to delay purchase operations when price is expected to decrease in the future, so that they are executed close to local minima.

Results – Overall

Strengths:

- Improved raw performance (1.7% lower than average price);
- Low variance, with consistent results throughout the years;
- Valuable robustness to exceptional events (built-in risk mitigation);
- Key interpretability of the decision-making process as a whole.

Weaknesses:

- Strong dependence of the performance on the quality of the forecasts;
- Poor interpretability of the DL forecasting model (black-box);
- Potential limitation of the performance by the built-in risk mitigation.

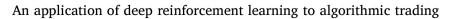


Trading in the stock market

Publication: Thibaut Théate and Damien Ernst. An Application of Deep Reinforcement Learning to Algorithmic Trading. Expert Systems with Applications, 173:114632, 2021.

Expert Systems With Applications 173 (2021) 114632



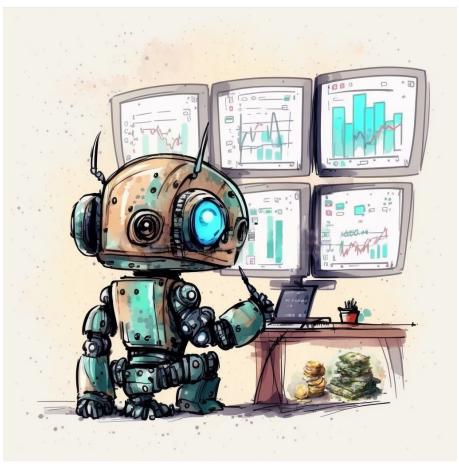


Check for updates Thibaut Théate^{*}, Damien Ernst

Montefiore Institute, University of Liège, Allée de la découverte 10, 4000 Liège, Belgium

ARTICLE INFO	ABSTRACT
Keywords: Artificial intelligence Deep reinforcement learning Algorithmic trading Trading policy	This scientific rese solve the algorithm trading activity in t ratio performance gorithm (TDQN), t to the specific algo

This scientific research paper presents an innovative approach based on deep reinforcement learning (DRL) to solve the algorithmic trading problem of determining the optimal trading position at any point in time during a trading activity in the stock market. It proposes a novel DRL trading policy so as to maximise the resulting Sharpe ratio performance indicator on a broad range of stock markets. Denominated the Trading Deep Q-Network algorithm (TDQN), this new DRL approach is inspired from the popular DQN algorithm and significantly adapted to the specific algorithmic trading problem at hand. The training of the resulting reinforcement learning (RL) agent is entirely based on the generation of artificial trajectories from a limited set of stock market historical data. In order to objectively assess the performance of trading strategies, the research paper also proposes a novel, more rigorous performance assessment methodology. Following this new performance assessment approach, promising results are reported for the TDQN algorithm.



Source: Midjourney v4.

Problem statement

Context: Financial Technology (FinTech) => Algorithmic trading.

Objective: Determining the optimal position, either long or short, at any point in time during the trading activity of a given stock.

Research question: Could innovative Artificial Intelligence (AI) techniques, especially Deep Reinforcement Learning (DRL), effectively solve this sequential decision-making problem?









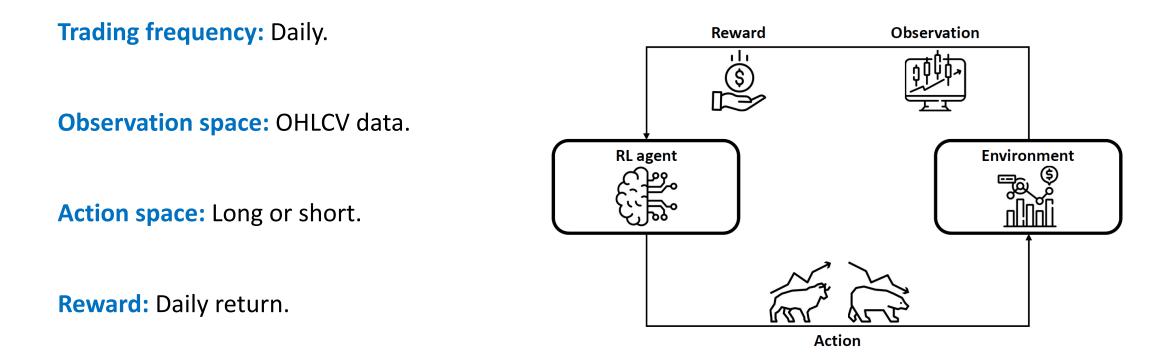
Contributions

24

- Mathematical formalisation (RL) of the sequential decision-making problem.
- Design of a novel algorithmic trading solution on the basis of DRL techniques.
- Design of a new performance assessment methodology to rigorously evaluate algorithmic trading policies, which was lacking in scientific literature.
- Analysis of the strengths and weaknesses of the RL approach in market environments.



Problem formalisation



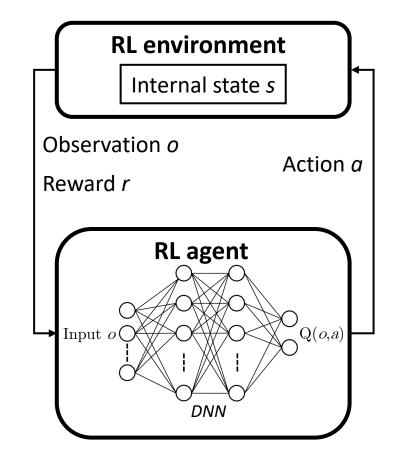
Objective: Sharpe ratio maximisation.

Solution designed

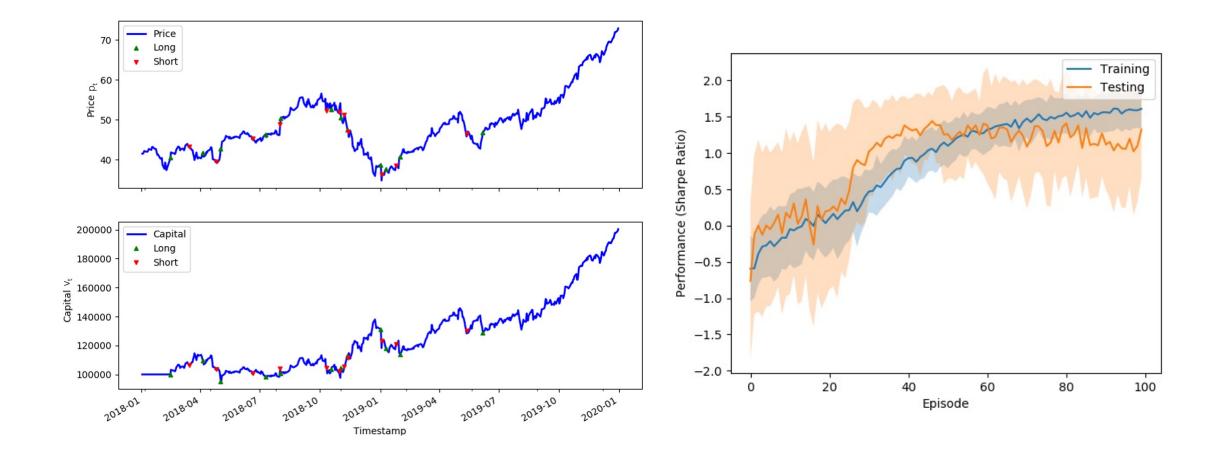
Starting point: Deep Q-Network (DQN) algorithm.

Various improvements (selected empirically):

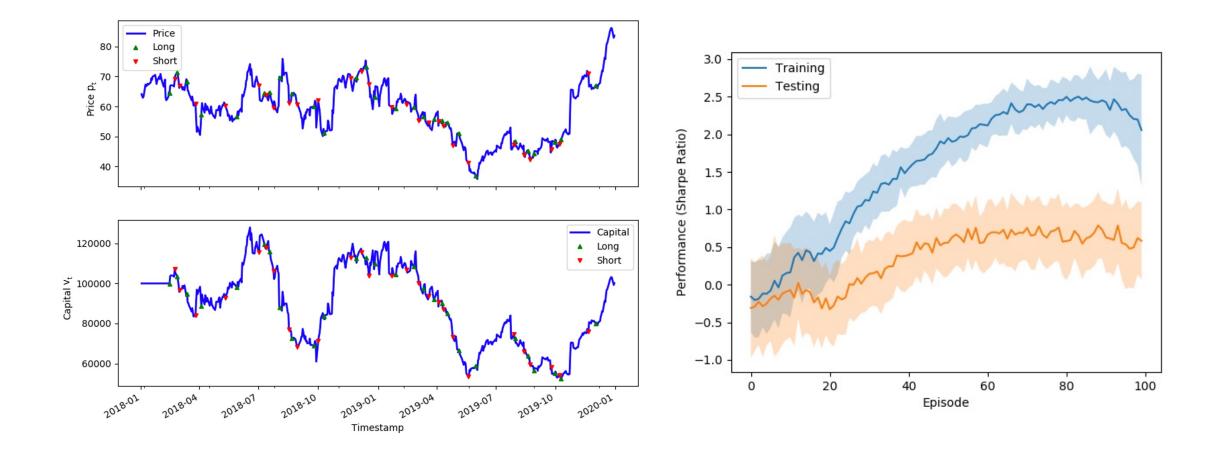
- DNN architecture (FFN + Leaky ReLU);
- Xavier initialisation (improved convergence);
- Double DQN (to combat overestimations);
- ADAM optimiser (improved stability and convergence);
- Gradient clipping (improved stability);
- Huber loss (improved stability);
- Batch normalisation layers (improved generalisation);
- Regularisation techniques (to combat overfitting);
- Data augmentation (signal processing);
- Preprocessing and normalisation.



Results – Positive (Apple stock)



Results – Concerning (Tesla stock)



Results – Overall

Promising results:

- Apparent potential, with significant room for improvements;
- A single trading strategy to effectively fit various market patterns;
- Valuable versatility (passive trading, trend following, mean reversion);
- Learning of a sound decision-making policy according to the trading costs.

Yet mixed results:

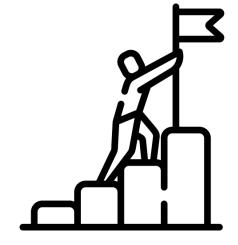
- Prone to overfitting;
- Important variance in the results;
- Dependence on the relevance of the training set;
- Black-box model with poor explainability of the decision-making process.



Limitation of RL in market environments

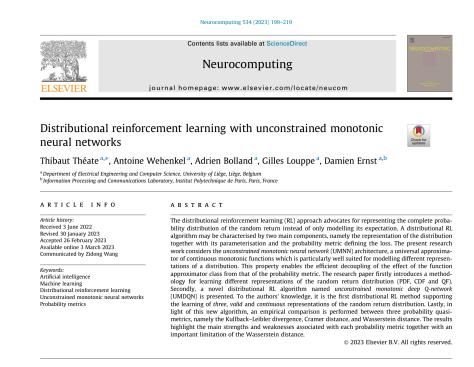
Key challenges:

- The substantial stochasticity of market environments.
- The extremely poor observability of market environments.
- The important non-stationarity of market environments.
- The proper mitigation of the risk associated with decision-making.
- The poor explainability of the decision-making process.
- The tendency of RL towards overfitting.
- The serious variance of RL algorithms.



Improving distributional reinforcement learning

Publication: Thibaut Théate, Antoine Wehenkel, Adrien Bolland, Gilles Louppe, and Damien Ernst. Distributional Reinforcement Learning with Unconstrained Monotonic Neural Networks. Neurocomputing, 534:199–219, 2023.





Source: Midjourney v4.

Distributional RL – Overview

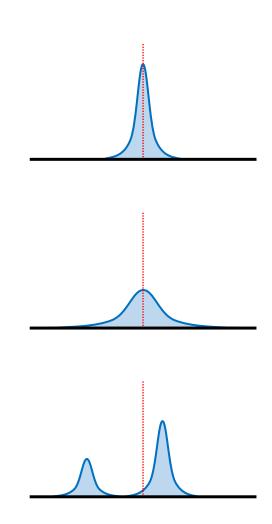
Core idea: Representing the complete probability distribution of the random return instead of solely modelling its expectation.

Main benefits:

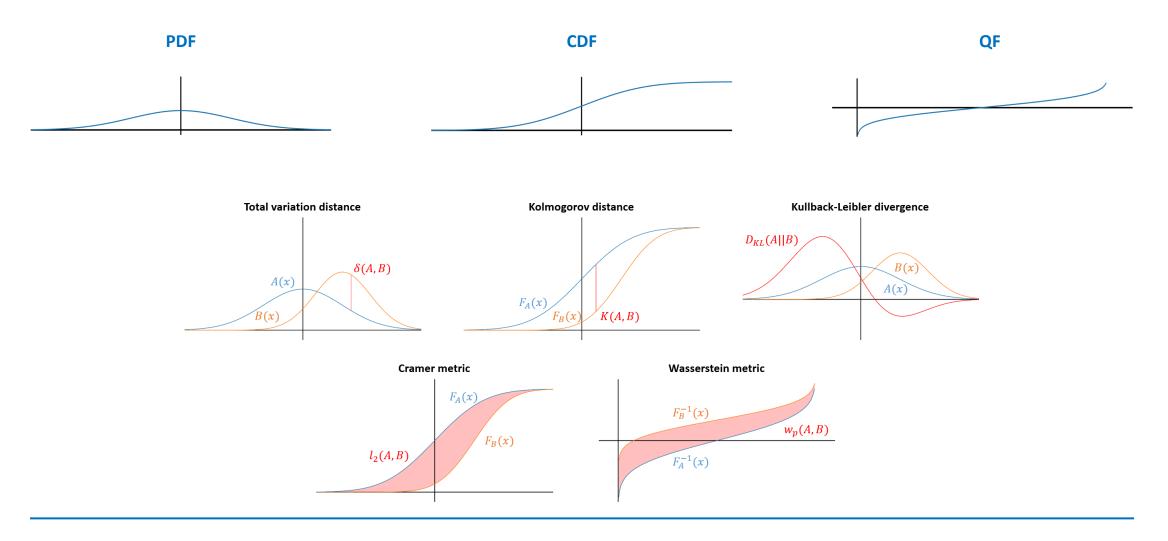
- Learning a richer representation of the random return, which leads to more efficient and stable learning;
- Enabling risk-sensitive control and exploration policies;
- Improving the interpretability of decision-making.

Features characterising a distributional RL algorithm:

- Representation and parameterisation of the distribution;
- Probability metric defining the loss.

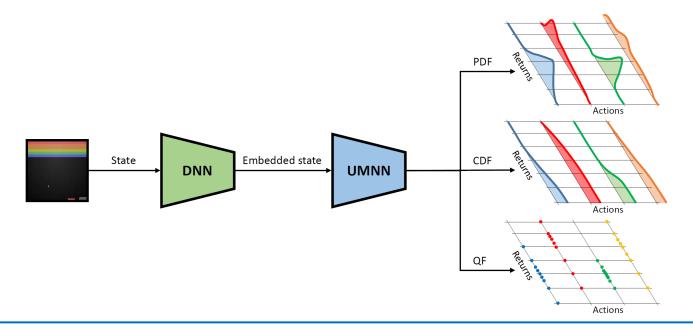


Distributional RL – Main features

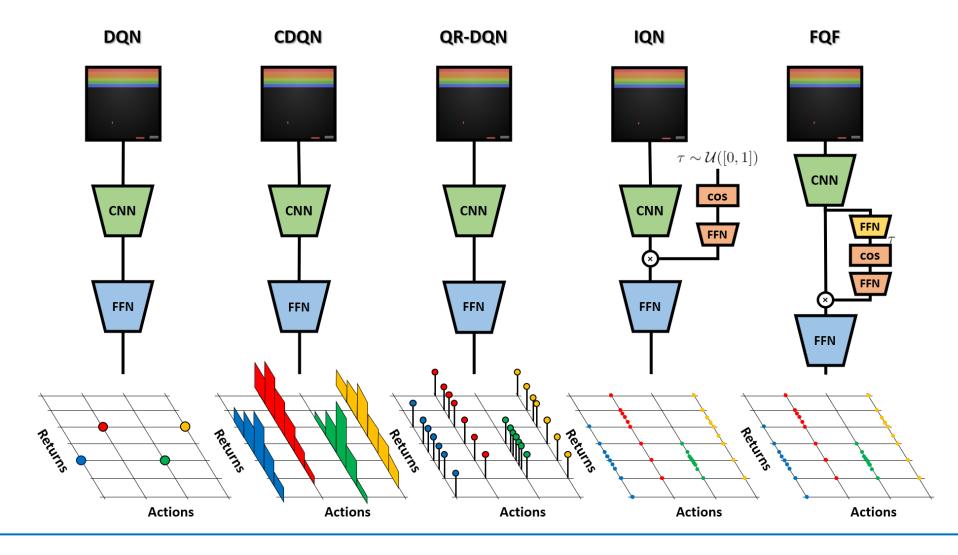


Contributions

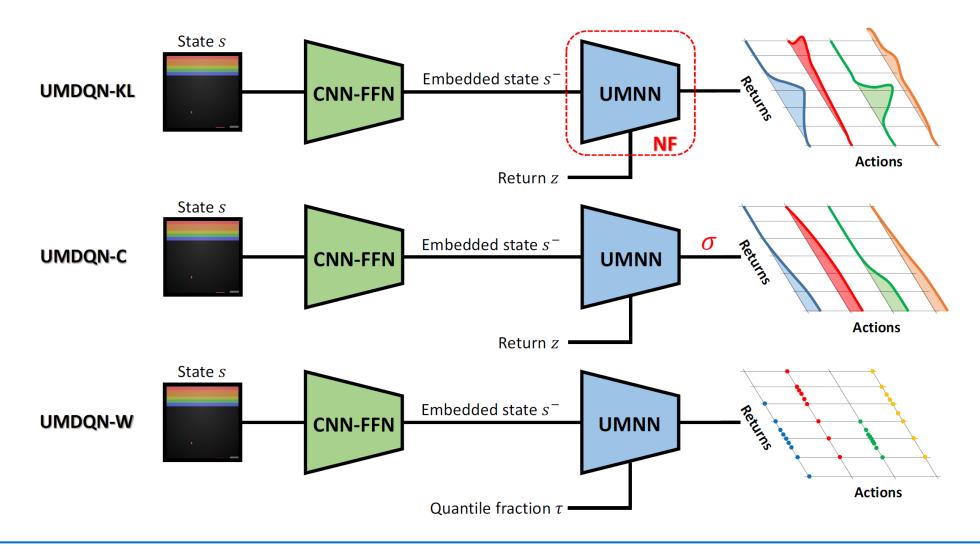
- Methodology for learning three representations of the random return probability distribution (PDF, CDF, QF).
- Novel distributional RL algorithm named Unconstrained Monotonic Deep Q-Network (UMDQN), supporting the learning of three (PDF, CDF, QF), valid (by ensuring monotonicity) continuous (as opposed to discrete) representations of the random return distribution.
- Empirical comparison of three probability metrics: KL divergence, Cramer distance and Wasserstein distance.



State of the art (SOTA)



Solution designed



Results – Probability distribution analysis (1)

Ground truth:

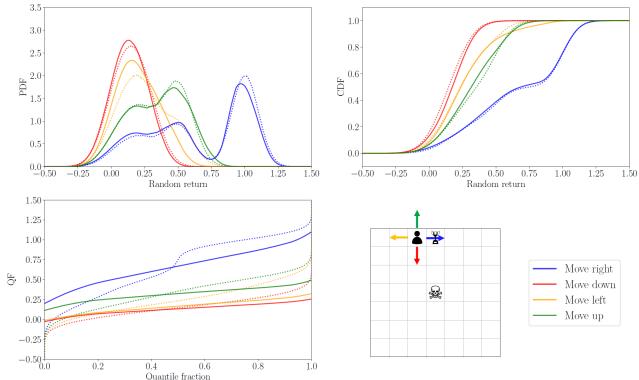
- 1. Optimal policy manually derived;
- 2. Monte Carlo methodology.

PDF and CDF:

- Not 100% accurate, but quite close;
- Preserved multimodality.

QF:

- Unacceptable error;
- Accurate expectation, but incorrect higher-order moments of the distribution;
- Multimodality no longer preserved.



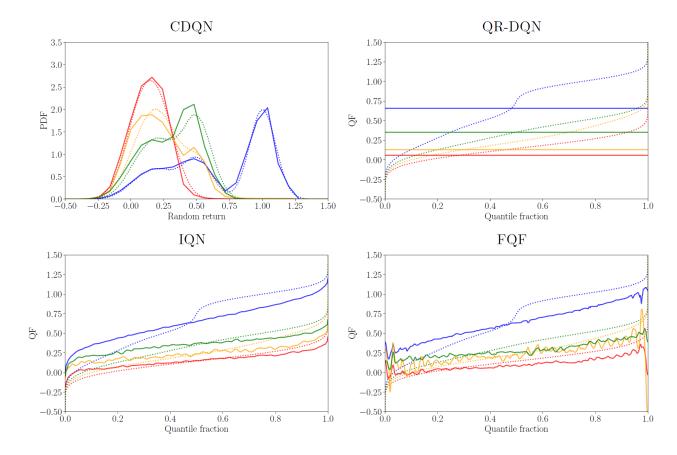
Results – Probability distribution analysis (2)

What about the SOTA algorithms?

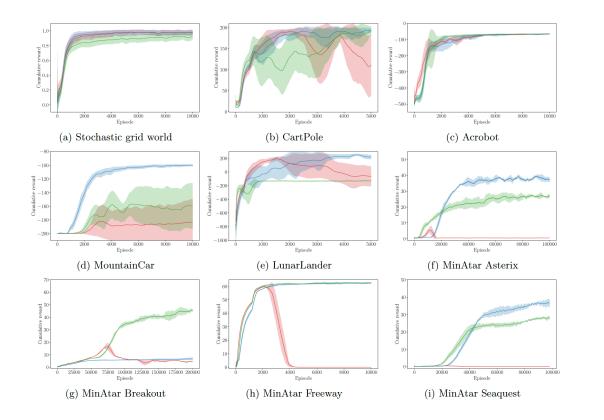
- Similar observations.
- CDQN => <mark>OK</mark>.
- QR-DQN, IQN, FQF => Warning.

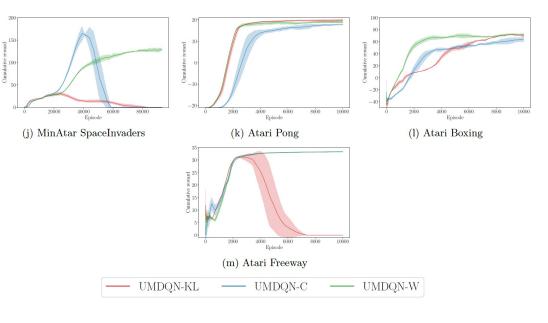
Conclusion about quantile regression:

- Effective solution if the objective is to solely learn a decision-making policy maximising the expected return.
- Poor solution if the higher-order moments of the random return probability distribution are used.



Results – Policy performance (1)





Results – Policy performance (2)

UMDQN-KL:

- No contraction mapping with the KL divergence, but it can still work;
- Lack of stability in the learning process, with collapses in performance;
- Phenomenon strongly tied to the x-axis range specified for the returns.

UMDQN-C:

- Requirement to appropriately set the range of returns;
- If accurate, stable learning process and great performance.

UMDQN-W:

- No requirement to estimate the range of returns beforehand;
- Stable learning process and great performance (versatility);
- Poor accuracy of the random return probability distributions learnt.



Taking risk into consideration

Publication: Thibaut Théate and Damien Ernst. Risk-Sensitive Policy with Distributional Reinforcement Learning. Algorithms, 16(7):325, 2023.



Article Risk-Sensitive Policy with Distributional Reinforcement Learning

Thibaut Théate ^{1,*} and Damien Ernst ^{1,2}

- Department of Electrical Engineering and Computer Science, University of Liège, 4031 Liège, Belgium
 Information Processing and Communications Laboratory, Institut Polytechnique de Paris, 91120 Paris, France; demst®uliègebe
- * Correspondence: thibaut.theate@uliege.be

Abstract: Classical reinforcement learning (RL) techniques are generally concerned with the design of decision-making policies driven by the maximisation of the expected outcome. Nevertheless, this approach does not take into consideration the potential risk associated with the actions taken, which may be critical in certain applications. To address that issue, the present research work introduces a novel methodology based on distributional RL to derive sequential decision-making policies that are sensitive to the risk, the latter being modelled by the tail of the return probability distribution. The core idea is to replace the Q function generally standing at the core of learning schemes in RL by another function, taking into account both the expected return and the risk. Named the *risk-based utility function* U, it can be extracted from the random return distribution? Laturally learnt by any distributional RL algorithm. This enables the spanning of the complete potential trade-off between risk minimisation and expected return maximisation, in contrast to fully risk-averse methodologies. Fundamentally, this research yields a truly practical and accessible solution for learning risk-sensitive policies with minimal modification to the distributional RL algorithm, with an emphasis on the interpretability of the resulting decision-making process.

Keywords: distributional reinforcement learning; sequential decision-making; risk-sensitive policy; risk management; deep neural network

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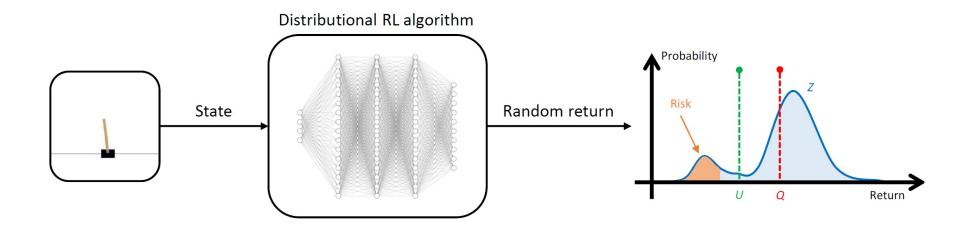


Source: Midjourney v4.

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Contributions

- A truly practical and accessible solution for learning risk-sensitive policies with minimal modification to the original distributional RL algorithm, and with an emphasis on the interpretability of the resulting decision-making process.
- A novel performance assessment methodology with new benchmark environments for effectively analysing the proficiency of RL algorithms when it comes to risk-sensitive decision-making.



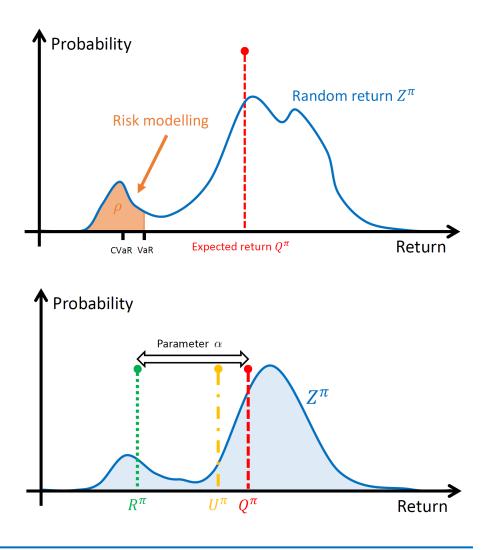
Solution designed

Risk modelling:

- Tail of the random return probability distribution;
- Value at Risk (VaR) or Conditional Value at Risk (CVaR).

Risk-based utility function:

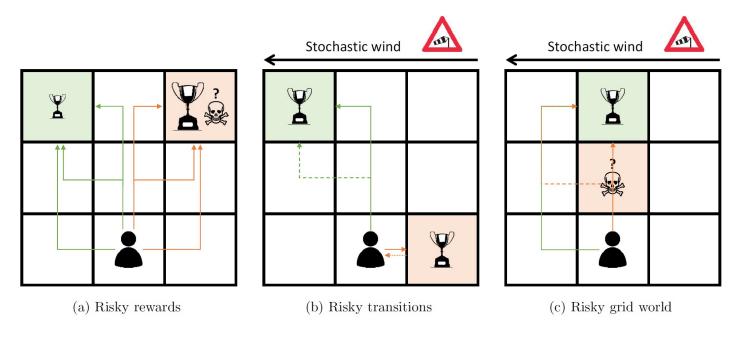
- Extension of the popular Q^{π} function (expected return);
- Definition of the *state-action risk function* R^{π} , derived from the *value distribution* Z^{π} ;
- Linear combination between functions Q^{π} and R^{π} ;
- Hyperparameter *α* between 0 and 1, to be tuned according to the relative importance of risk;
- Maximisation of the *risk-based utility function* U^{π} instead of Q^{π} for action selection in any distributional RL algorithm.



Benchmark environments

Design philosophy:

- Optimal policy differs depending on whether the objective is to solely maximise the expected performance or to also mitigate the risk.
- Including relevant stochasticity into both the reward and state transition functions.



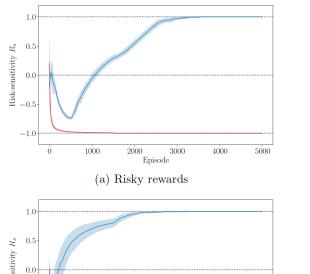


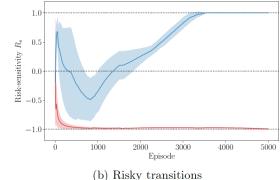
Results – Policy performance

DQN algorithm:

- Rapid convergence towards the optimal policy in terms of expected return;
- No consideration for the risk.

Benchmark environment	DQN			RS-UMDQN-C		
Denominary environment	$\mathbb{E}\left[S^{\pi}\right]$	$\mathcal{R}_{\rho}\left[S^{\pi}\right]$	$U\left[S^{\pi}\right]$	$\mathbb{E}\left[S^{\pi}\right]$	$\mathcal{R}_{\rho}[S^{\pi}]$	$U\left[S^{\pi}\right]$
Risky rewards	0.3	-1.246	-0.474	0.1	-0.126	-0.013
Risky transitions	0.703	0.118	0.411	0.625	0.346	0.485
Risky grid world	0.347	-1.03	-0.342	0.333	0.018	0.175





RS-UMDQN-C algorithm:

- Convergence towards the optimal policy in terms of risk mitigation;
- Quite stable learning process despite having to maximise a much more complex function.



ISIN -0.5

-1.0

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Episode (c) Risky grid world

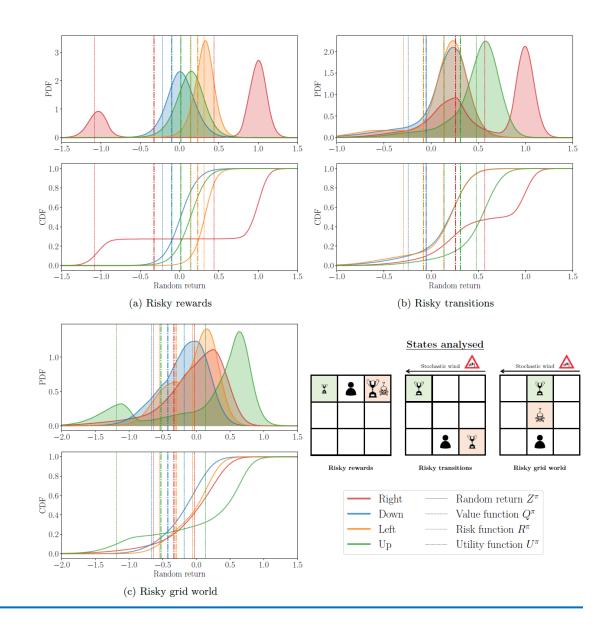
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Results – Visualisation

- Preserving the accurate learning of the random return probability distributions.
- Greatly enhancing the interpretability of the decision-making process.
- Significantly easing the understanding of the trade-off between raw performance and risk mitigation for a given problem.



Contributing to a more sustainable society

Publication: Thibaut Théate, Antonio Sutera, and Damien Ernst. Matching of Everyday Power Supply and Demand with Dynamic Pricing: Problem Formalisation and Conceptual Analysis. Energy Reports, 9:2453–2462, 2023.

Energy Reports 9 (2023) 2453-2462

	Contents lists available at ScienceDirect	ENERGY REPORTS
5-2-69	Energy Reports	
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Research paper

Matching of everyday power supply and demand with dynamic pricing: Problem formalisation and conceptual analysis

9	
updates	

Thibaut Théate^{a,*}, Antonio Sutera^b, Damien Ernst^{a,c}

^a Department of Electrical Engineering and Computer Science, University of Liège, Liège, Belgium ^b Haulagy, Intelligent Systems Solutions, Braine-le-Conne, Belgium ci Information Processing and Communications Laboratory, Institut Polytechnique de Paris, Paris, France

ARTICLE INFO

ABSTRACT

Article history: Received 2 November 2022 Received in revised form 19 December 2022 Accepted 8 January 2023 Available online 25 January 2023

Keywords: Matching of supply and demand Dynamic pricing Demand response Power producer/retailer The energy transition is expected to significantly increase the share of renewable energy sources whose production is intermittent in the electricity mix. Apart from key benefits, this development has the major drawback of generating a mismatch between power supply and demand. The innovative dynamic pricing approach may significantly contribute to mitigating that critical problem by taking advantage of the flexibility offered by the demand side. At its core, this idea consists in providing the consumer with a price signal which is evolving over time, in order to influence its consumption. This novel approach involves a challenging decision-making problem that can be summarised as follows: how to determine a price signal maximising the synchronisation between power supply and demand under the constraints of maintaining the producer/retailer's profitability and benefiting the final consumer at the same time? As a contribution, this research work presents a detailed formalisation of this particular decision-making problem. Moreover, the paper discusses the diverse algorithmic components necessary to efficiently design a dynamic pricing policy: different forecasting models together with an accurate statistical modelling of the demand response to dynamic prices. © 2023 The Author(s). Published by Elsevier Ltd. This is an open access article under the CCBVI(license (http://creativecommons.org/licenses/by/40.)/





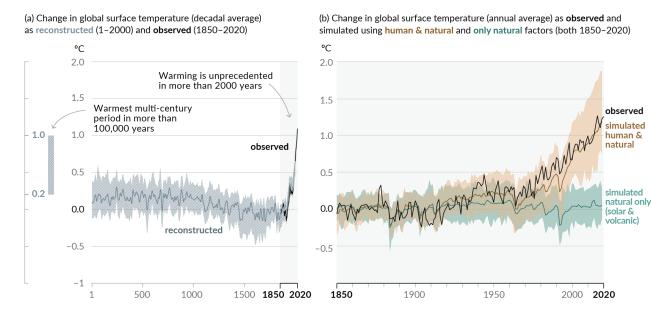


- Human activities, principally through emissions of greenhouse gases, have unequivocally caused global warming, with global surface temperature reaching 1.1°C above 1850–1900 in 2011–2020.
- Climate change is a threat to human well-being and planetary health. The choices and actions implemented in this decade will have impacts now and for thousands of years.
- The likelihood of abrupt and irreversible changes increases with higher global warming levels.
- There is a rapidly closing window of opportunity to secure a liveable and sustainable future for all.

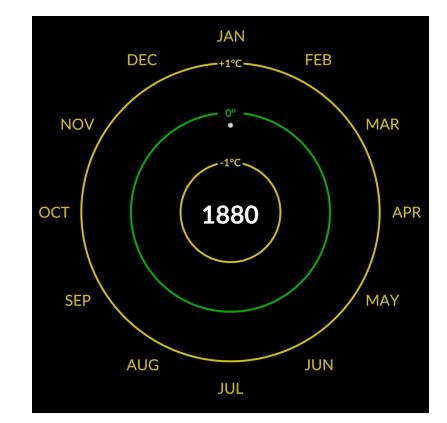
Climate change – IPCC report (2)

Human influence has warmed the climate at a rate that is unprecedented in at least the last 2000 years

Changes in global surface temperature relative to 1850–1900



Source: Figure SPM.1 in IPCC, 2021: Summary for Policymakers.



Source: NASA's Scientific Visualization Studio.

Problem statement

Context: Energy transition => intermittent renewable energy sources.

Objective: Determining a price signal maximising the synchronisation between power supply and demand under the complex constraints of maintaining the producer/retailer's profitability while also benefiting the final consumer at the same time.

Research question: What are the major challenges in solving this *dynamic pricing* problem from the perspective of the supply side and how can Artificial Intelligence (AI) contribute to its resolution?







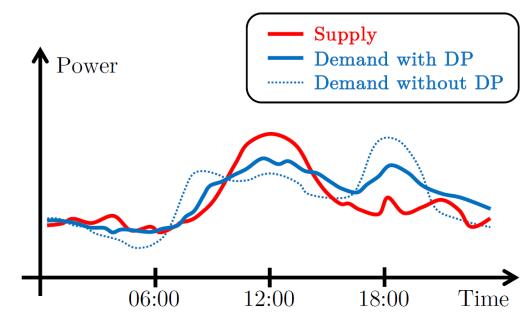
Dynamic pricing – Overview

Targeted actor: power producer/retailer whose generation portfolio is composed of an important share of intermittent renewable energy sources (supply side).

Core idea: continuously adapting the power price in order to influence the electricity consumption curve by taking advantage of the flexibility offered by the demand side.

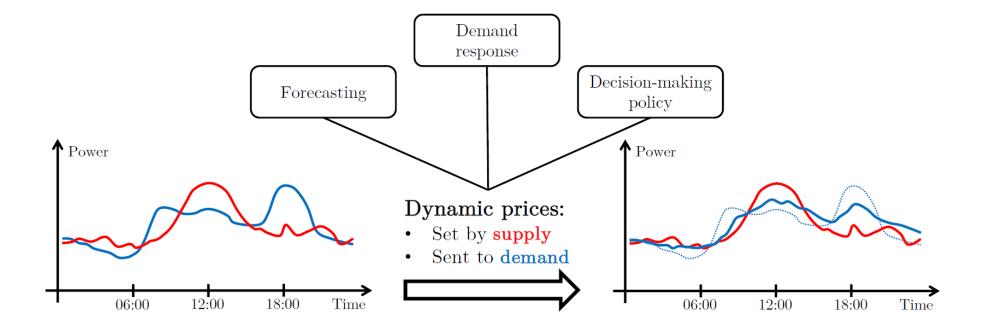
Motivations: potential benefits for both supply and demand sides, in terms of:

- Ecology;
- Economy;
- Autonomy.

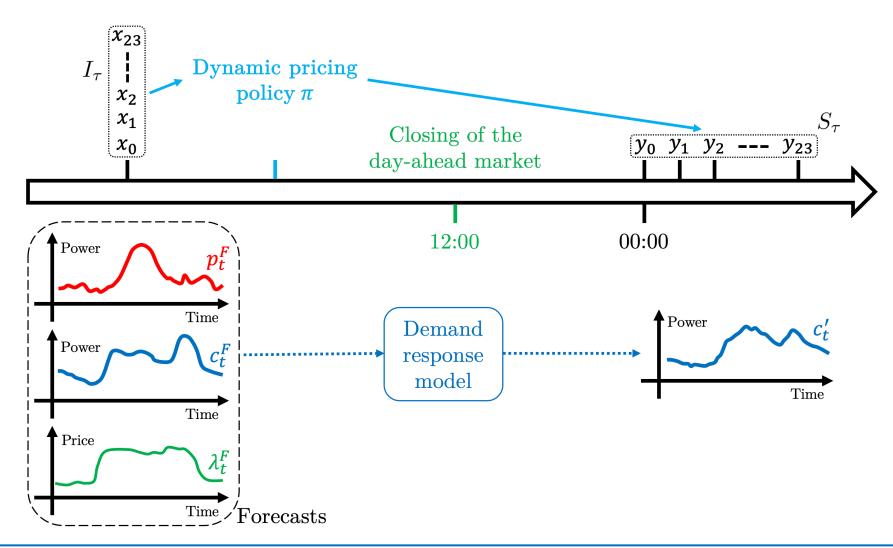


Contributions

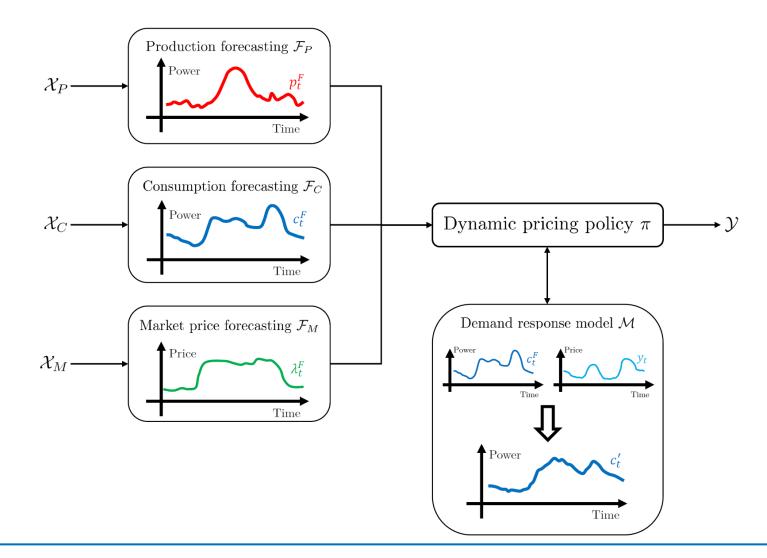
- Detailed mathematical formalisation of the (sequential) decision-making problem behind the *dynamic pricing* approach from the perspective of the supply side.
- Discussion of the algorithmic components necessary to the design of a dynamic pricing policy.



Problem formalisation – Overview



Necessary algorithmic components



Future work

Data collection, design, implementation and experimentation:

- Forecasting => DL techniques (RNN, CNN and transformers).
- Demand response => Supervised Learning approach.
- Decision-making => DRL techniques (risk-sensitive distributional RL).

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Conclusion and future work





Source: Midjourney v4.

Main contributions

Applied research:

- Stock and energy markets (forward and intraday);
- Rigorous formalisation of the sequential decision-making problems;
- Design of new AI-based algorithmic solutions (DL and RL);
- Highlight of the main limitations of RL in market environments.

Fundamental research:

- Novel distributional RL algorithm leveraging an advanced DL architecture;
- Empirical comparison of probability metrics in distributional RL;
- New intuitive methodology for risk-sensitive distributional RL.

Sustainable research:

- Dynamic pricing from the perspective of the supply side;
- Meticulous formalisation of the decision-making problem and discussion.

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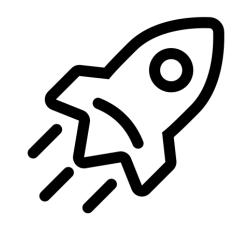
Primary future work

- Completing the research loop initiated by this doctoral thesis.
- Extending the information available as input (observability).
- Improving the adaptability of DRL approaches.
- Enhancing the interpretability of decision-making based on RL.

- Experimenting with more advanced DL architectures and RL techniques.
- Developing the theoretical foundations underlying risk-sensitive and distributional RL.

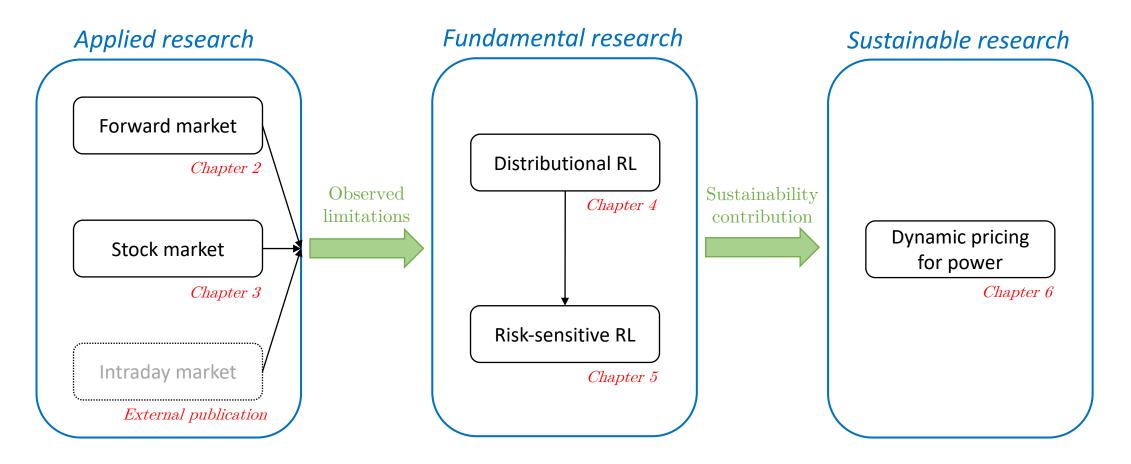


- My doctoral thesis => extraordinarily fulfilling experience!
- My next challenge: the energy transition.
- I am thankful for your interest and attention.



Questions





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- My former colleagues from Blacklight Analytics;
- The F.R.S.-FNRS (funding);
- My wonderful family.



Sources

Images:

- Coloured images: https://www.midjourney.com
- Icons: https://www.flaticon.com



Doctoral thesis: https://orbi.uliege.be/handle/2268/304075

IPCC report: IPCC, 2021: Climate Change 2021: The Physical Science Basis. Contribution of Working Group I to the Sixth Assessment Report of the Intergovernmental Panel on Climate Change. Cambridge University Press, Cambridge, United Kingdom and New York, NY, USA, In press, doi:10.1017/9781009157896.