

WR 63: a multiple system (O+O) + WR?

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ABSTRACT

The spectrum of the Wolf–Rayet (WR) star WR 63 contains spectral lines of two different O stars that show regular radial velocity (RV) variations with amplitudes of ~ 160 and ~ 225 km s⁻¹ on a ~ 4.03 d period. The light curve shows two narrow eclipses that are 0.2 mag deep on the same period as the RV changes. On the other hand, our data show no significant RV variations for the WR spectral lines. Those findings are compatible with WR 63 being a triple system composed of two non-interacting late-O stars orbiting a WR star on a period longer than 1000 d. The amplitude of the WR spectral line-profile variability reaches 7–8 per cent of the line intensity and seems related to a 0.04 mag periodic photometric variation. Large wind density structures are a possible origin for this variability, but our data are not sufficient to verify this. Our analysis shows that, should the three stars be bound, they would be coeval with an age of about 5.9 ± 1.4 Myr. The distance to the O stars is estimated to be 3.4 ± 0.5 kpc. Their dynamical masses are 14.3 ± 0.1 and 10.3 ± 0.1 M_⊙. Using rotating single-star evolutionary tracks, we estimate their initial masses to be 18 ± 2 and 16 ± 2 M_⊙ for the primary and the secondary, respectively. Regular spectral monitoring is required in the future to detect RV variations of the WR star that would prove that it is gravitationally bound to the close O+OB system and to determine its mass.

Key words: binaries: eclipsing – binaries: spectroscopic – stars: individual: WR 63 – stars: winds, outflows – stars: Wolf–Rayet.

1 INTRODUCTION

Massive stars are one of the most important cosmic engines in the galaxies. During their evolution, they radiatively and mechanically influence their surroundings with their stellar winds, strong UV ionizing fluxes, and their deaths as supernovae. The Wolf–Rayet (WR) stage represents one of the most advanced phases in massive star evolution. In this phase, massive stars are characterized by strong emission feature spectra from highly ionized species (see Crowther 2007 for a detailed review). They are classified in three different categories depending on their degree of stripping starting from the nitrogen-rich WR stars (WN), the carbon-rich WR stars (WC), and finally, the oxygen-rich WR stars (WO). These objects might be formed through single-star evolution (classified as main-sequence WR stars, or classical WRs that have evolved off the main sequence through self-stripping; Conti 1975; Smith 2014) or through binary interaction (through mass transfer or merging in binary or multiple systems; Paczynski 1967; Shenar et al. 2020).

There are currently more than 660 WR stars known in our Galaxy (van der Hucht 2001; Rosslowe & Crowther 2015),¹ but only a few of them have been revealed to be truly core-eclipsing binaries, i.e. systems where the eclipses occur when the projected stellar discs on the sky occult one another. These are WR 20a (Rauw et al. 2004; Bonanos et al. 2004), WR 22 (Balona, Egan & Marang 1989; Gosset et al. 1991; Rauw et al. 1996), WR43a (also known as NGC 3606-A1; Moffat et al. 2004; Schnurr et al. 2008), WR 139 (Gaposchkin 1941; Marchenko, Moffat & Koenigsberger 1994), WR 151 (Hiltner 1948; Lewis et al. 1993; Hutton, Henden & Terrell 2009), and WR 155 (Gaposchkin 1944; Marchenko et al. 1995). In addition, in the Large Magellanic Cloud, there is R144 (Shenar et al. 2021). For all these systems, the basic stellar parameters can be determined with high accuracy, and the orbit well defined. Their double eclipsing nature (except for WR 22, which shows only one eclipse because of the high eccentricity of its orbit) offers the opportunity to directly measure the masses of their components by a simple least-model-dependent Keplerian orbit.

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¹<http://pacrowther.staff.shef.ac.uk/WRcat/index.php>

WR 20a and 43a are WN+WN systems and the two components are hydrogen-rich WR stars with masses over $80 M_{\odot}$. WR 22 is a WR+O system, and the WR component is also a hydrogen-rich star with a mass in the range $56\text{--}72 M_{\odot}$ (Rauw et al. 1996; Schweickhardt et al. 1999). The other three systems are WR+O systems, and the WR component is a classical evolved WR star with a mass around $15\text{--}20 M_{\odot}$. Such reliable determinations of WR star masses are of very high value for constraining and validating evolutionary models. Indeed, binary evolution (Vanbeveren et al. 1998; Sana et al. 2012; Moe & Di Stefano 2017), (rotational) mixing (Meynet & Maeder 2003), and mass-loss (Smith 2014; Vink 2022) are key ingredients that still suffer from a lack of good knowledge to understand massive star evolution. Therefore, while the Bonn and Geneva models (Brott et al. 2011; Ekström et al. 2012, respectively) for single-star evolution as well as the Binary Population and Spectral Synthesis (BPASS) models (Stanway & Eldridge 2018) for binary evolution are commonly used, they are still limited by many simplifying assumptions (see Martins & Palacios 2013 for further details). These can be better put to test with well constrained systems. Another utility of core-eclipsing binaries is that they allow for stellar parameters derived from atmospheric models to be accurately associated with stellar masses.

The present paper focuses on WR 63, a WN7o star that has been suspected of having an O5 V or B0 III companion based on its diluted emission lines (van der Hucht 2001, and related catalogues). Also, Rate & Crowther (2020) were unable to determine the *Gaia* distance to the star because it is absent from the catalogue, probably due to the presence of that putative companion. Here, we present the discovery of two O-star spectra blended with the WR spectrum, indicating the possible multiple nature of WR 63. It is not analogous to the binaries presented above, as the WR star is not eclipsing, but the two O stars are. In this work, we present the data as if the three stars were bound as a starting hypothesis. From the data in hand, we can analyse the photometric variations and radial velocity (RV) changes caused by the O stars and determine some of their fundamental parameters. We also present our analysis of the WR star line-profile variability and RV changes, and how future observations could lead to the determination of its mass.

In Section 2, we present our new photometric and spectroscopic data. In Section 3, we describe our methods to search for periods, measure RV, and determine line-profile variations (LPVs). In Sections 4 and 5 we present the details of the O+O inner binary and the evolution of the system, respectively. Finally, we present our conclusions in Section 6.

2 OBSERVATIONS

2.1 Photometric observations

As part of an intensive multiband photometric monitoring campaign of WR stars with the Swope 1.0 m telescope (Las Campanas), we observed WR 63 between 2012 May 12 and 31. Only three nights were lost due to bad weather over the entire run. Series of 10 CCD frames were obtained in each *B*, *V*, and *I* band two to three times per night, using the 1200^2 pix SITe#3 detector. Each series was separated in time by at least 2.5 h. We used the IDL functions *find* to detect the sources in the field and *aper* to perform the photometric measurements. The aperture was selected to be 3.5 times the full width at half-maximum (FWHM) of the mean point-spread function (PSF) of the sources (and hence is dependent on the seeing conditions), and the sky annulus was taken from 3.5–7 times the FWHM of the mean PSF of the sources. In the 8.7 arcsec^2 field of

view of the SITe#3 detector, we detected 125 stars in *B*, 256 stars in *V*, and 806 stars in *I*. To perform relative photometry and correct for the effects of variable weather conditions, we select the frame taken under the best conditions (greatest number of sources detected, and a small value of the average PSF FWHM) and compare the magnitude measured in that frame with the magnitudes measured in all the frames. The difference measured is assumed to be equal to the shift of the zero-point in magnitude that we must apply to bring all the frames to the same level.

The *Transiting Exoplanet Survey Satellite* (TESS, Ricker et al. 2014) light curve was taken in short cadence mode in Sector 38. We retrieved the light curves from the Mikulski Archive for Space Telescopes (MAST3) archive in their pre-conditioned form (PDC-SAP, Pre-search Data Conditioning Simple Aperture Photometry). We detrended them using a linear fit to remove any long-term trends. The light curve covers heliocentric Julian dates (HJD) from HJD = 2459334 to HJD = 2459361. The pseudo-Nyquist frequency is $\nu_{\text{Ny}} = 357.143 \text{ d}^{-1}$ (leading to a step of 241.92 s). The prefix ‘pseudo-’ is used to point out the fact that the aliasing is not pure.

2.2 Spectroscopic observations

We collected high-resolution spectra with the Fibre-fed Extended Range Optical Spectrograph (FEROS, Kaufer et al. 1997, 1999) mounted on the MPG/ESO 2.2 m telescope at La Silla (Chile). FEROS provides a resolving power of $R = 48\,000$ and covers the entire optical range from 3800 to 9200 Å. The data (Program ID: 089.D-0730, PI: Mahy) were obtained from 2012 May 1–7. Their reduction was done following the procedure described in Mahy et al. (2010, 2017).

We collected three spectra with the UV and Visible Echelle Spectrograph (UVES, Dekker et al. 2000) mounted on the ESO/VLT UT2 (Paranal, Chile). These three spectra were collected on 2017 April 22 (Program ID: 099.D-0314, PI: Mahy), 2018 May 29 (Program ID: 0101.D-0273, PI: Mahy), and 2019 May 22 (Program ID: 0103.D-0414, PI: Mahy), with CD#3-520nm, CD#3-520nm, and CD#3-564nm setups, respectively. These setups cover the 4143–6214 Å, and 4583–6686 Å wavelength ranges. The resolution of UVES is $R \sim 85\,000$. The UVES data were reduced using the ESO pipeline.

Optical spectroscopic time series were also obtained using the High Resolution Spectrograph (HRS) on SALT (Bramall, Sharples & Tyas 2010; Bramall et al. 2012; Crause et al. 2014) under program ID 2021-1-SCI-013 (PI: Manick). The data were taken in low-resolution mode ($R \sim 16\,000$) and cover the 3735–8779 Å wavelength domain. The data were reduced with the MIDAS pipeline (Kniazev, Gvaramadze & Berdnikov 2016) based on the *échelle* (Ballester 1992) and *feros* (Stahl, Kaufer & Tubbesing 1999) packages. We applied heliocentric corrections to the data.

Finally, lower-resolution spectra were obtained at Gemini using the GMOS-South spectrograph (Hook et al. 2004) under programs GS-2015A-Q-88, GS-2014A-Q-94, GS-2019B-Q-404, and GS-2020A-Q-410 (PI: Chené). The majority of the spectra were obtained with the B600 grating, offering a resolution power of $R \sim 1700$ over a spectral range of 3855–6980 Å, while four spectra were obtained with the R831 grating covering 3880–5050 Å with $R \sim 3800$. The data were reduced using the Gemini package in IRAF.²

²IRAF was distributed by the National Optical Astronomy Observatory, which was managed by the Association of Universities for Research in

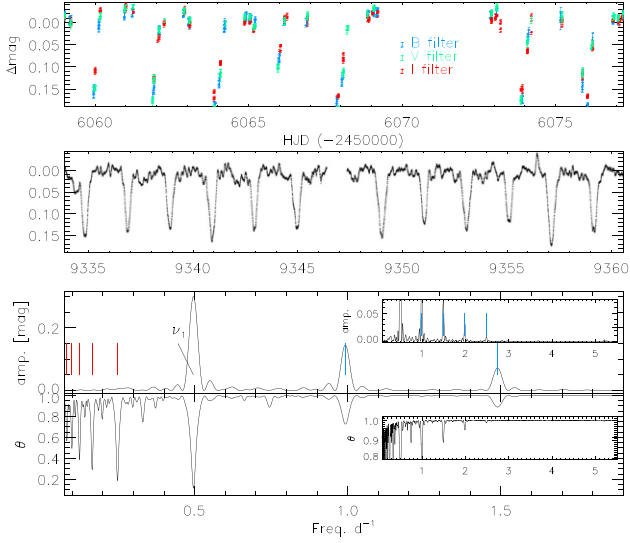


Figure 1. Swope (top panel) and *TESS* (middle panel) light curves of WR 63. Bottom: The semi-amplitude Fourier periodogram of the *TESS* light curve and the θ spectrum from the PDM method. The highest peak is marked as ν_1 . The associated harmonics are marked with blue lines (for $N \times \nu_1$) and the PDM subharmonics with red lines (for ν_1/M).

3 ANALYSIS

A first inspection of the Swope light curve revealed strong eclipses. The spectroscopic monitoring uncovered absorption lines related not just to one, but to two O stars. The following describes in detail our determination of the orbital motions.

3.1 Search for photometric periods

We ran a Fourier analysis based on the Heck–Manfroid–Mersch technique (Heck, Manfroid & Mersch 1985, revised by Gosset et al. 2001) on the Swope and *TESS* light curves. We selected the highest peaks based on the criterion presented by Mahy et al. (2011, their equation 2). The results from the Swope light curve are similar, but of course much noisier than the results from the *TESS* light curve. This iterative criterion provides us with about 60 formally significant frequencies. This large number is due to the large content of deterministic variability in the light curve. The semi-amplitude spectrum is dominated by a set of frequencies distributed according to a regular pattern including the fundamental frequency at about $0.498(1) \text{ d}^{-1}$ (denoted as ν_1 in Fig. 1) and its harmonics at $N \times \nu_1$ with $N = 2, 3, 4,$ and 5 . The presence of the harmonics is easily explained by the rather narrow shape of the eclipses. We also detect a significant frequency at $0.251(1) \text{ d}^{-1}$ but it is unclear whether that frequency is connected to the fundamental frequency mentioned above or to an independent signal since the span of time of the *TESS* data is too short. The presence of this frequency most probably indicates that the eclipses present different depths in alternation.

We also performed a period search using a phase-dispersion minimization (PDM) algorithm (Stellingwerf 1978), which is well suited to cases in which the signal is highly non-sinusoidal, such as core eclipses. The method consists in folding the data points in phase using different trial periods and dividing the resulting curves into a

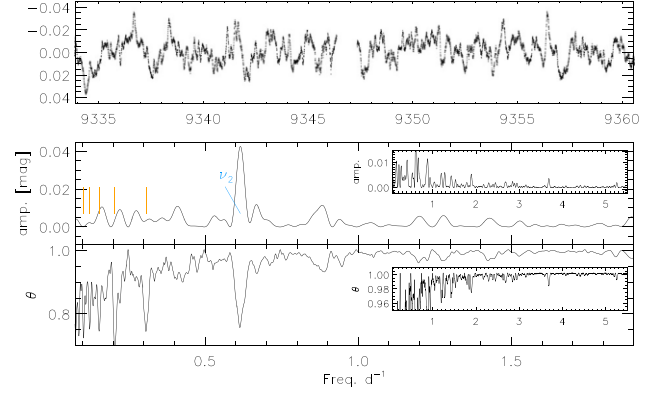


Figure 2. Same as Fig. 1, but for the *TESS* light curve after the eclipses have been subtracted.

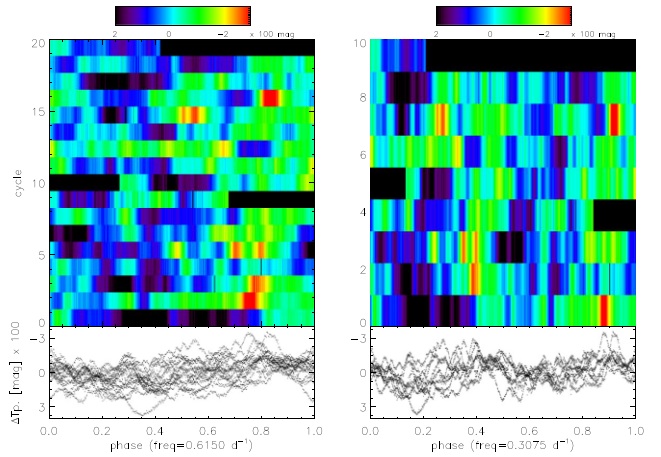


Figure 3. Left: The top panel shows the *TESS* light curve after subtraction of the eclipses, folded into the frequency 0.6150 d^{-1} . Each cycle is shown in succession and the residuals are coded by colour. The bottom panel shows the same thing, but all the cycles overlaid. Right: Same, but for the frequency 0.3075 d^{-1} .

predetermined number of phase bins. For each trial period, we can define S_j^2 , the sample variance around the mean for bin j ; S^2 , the cumulated variance over all S_j^2 ; and finally $\theta = S^2/\sigma^2$, where σ^2 is the variance of all data points. In addition to the main period ν_1 and its harmonics, it also displays more peaks at ν_1/M with $M = 2, 3, 4,$ and 5 (see Fig. 1). These additional peaks are subharmonics and are a well known artefact of the phase-folding minimization methods. These artefacts can be easily recognized thanks to the widths of the peaks that are narrower (width behaving as $1/M$).

The fundamental period is $P_{\text{orb}} = 4.0275 \pm 0.0008 \text{ d}$, and it corresponds to $\nu_1/2$. It also agrees with the RV motion of the He I lines in absorption, which will be discussed shortly in Section 3.2.

After removing the signal of the eclipses from the *TESS* light curve, we found a new peak at $0.615(1) \text{ d}^{-1}$ (denoted as ν_2 in Fig. 2) and related peaks at ν_2/M with $M = 2, 3, 4,$ and 5 . In Fig. 3, we present the light curve folded with the frequencies ν_2 and $\nu_2/2$. It is very subjective to determine if there are any coherent features that repeat at every cycle and exploring more harmonics would leave a very small number of cycles to work with. Possible origins for these variations will be covered in Section 3.3.

Once the frequencies ν_1 and ν_2 are removed, we are left with a barely significant peak at $5.26(2) \text{ d}^{-1}$, corresponding to a period of

0.192 d. This corresponds to the time span of a single smaller cusp, such as those pervading the entire *TESS* light curve.

3.2 Radial velocity measurements

The spectrum of the WR 63 system is dominated by the WR star. Only a few absorption lines from the O companions can be found on top of strong emission lines. Also, large-amplitude LPVs (see Section 3.3) hinder the detection and monitoring of the strong photospheric lines expected in O stars, such as the lines of the Balmer and Pickering series. Nevertheless, He I lines such as 4388, 4922, and 5016 Å could be isolated fairly easily and were used to determine the RVs of the O stars.

First, to increase the signal-to-noise ratio (S/N), which tends to be lower in the blue end of the spectra compared to redder wavelengths, we combined the three He I lines listed above into a mean profile. The average was weighted by the S/N measured in the continuum near the respective lines and was performed in velocity space. Secondly, we selected the spectra with the largest separation between the lines of both O stars, in order to fit their profiles using Gaussian functions. These were then used as a reference profile for each of the O stars. Finally, for each spectrum, we fitted the two components simultaneously by a simple minimization of χ^2 . The uncertainties are determined by the interval in velocity that provides a χ^2 near the minimum and within a range corresponding to the S/N of the spectrum.

In Fig. 4, the combined He I line profiles are organized based on the photometric period presented in Section 3.1. The RV curves of the two O stars are shown to guide the reader's eye to the centroids of the absorption lines. The two O-star RV semi-amplitudes are 160 ± 15 and $225 \pm 15 \text{ km s}^{-1}$. The sinusoidal shape of the RV curve, combined with the light curve showing eclipses being of identical widths and separated by exactly half the orbit period, suggests that the orbit of the O+O system is circular.

Determining the RV of the WR star requires another strategy. There are no true atmospheric lines in the WR spectrum and the majority of the emission lines are affected by the strong LPV (see Section 3.3). Nevertheless, it is possible to minimize the effect of the LPV by selecting a spectral line of high ionization level. Indeed, since those lines are formed in a region closer to the surface of the star, it is expected that the impact of wind density structures at the origin of the LPV is significantly smaller than for lines formed further out in the wind. We therefore selected the N IV 4058 Å line for this purpose, as it is usually formed twice as close to the base of the WR wind than any other optical lines presented here (Hillier 1988). We used a cross-correlation method, bisector measurement, and a simple fit of a Gaussian function to the line to determine the RVs. The cross-correlation was done through three iterations, the first one using the mean profile of all the spectra and the next two using the mean again, but after each individual spectrum was corrected by the previous measurement of the velocity shift.

All the methods give the same RV curve for the WR star, within the uncertainties. Unfortunately, the GMOS-South spectra using the B600 grating have an RV precision that is of the same order of magnitude as the RV variations of the WR star, and were therefore removed from the series.

Basically, through all of our spectroscopic campaigns, the WR star was static at an average RV near $-106 \pm 23 \text{ km s}^{-1}$ (see Fig. 5). This is consistent with a triple system formed of two close O stars orbiting the WR star with a high eccentricity and/or a long period. Further spectra would therefore be necessary to hunt for a potential periastron passage. Interestingly, the RV values of the centre of mass

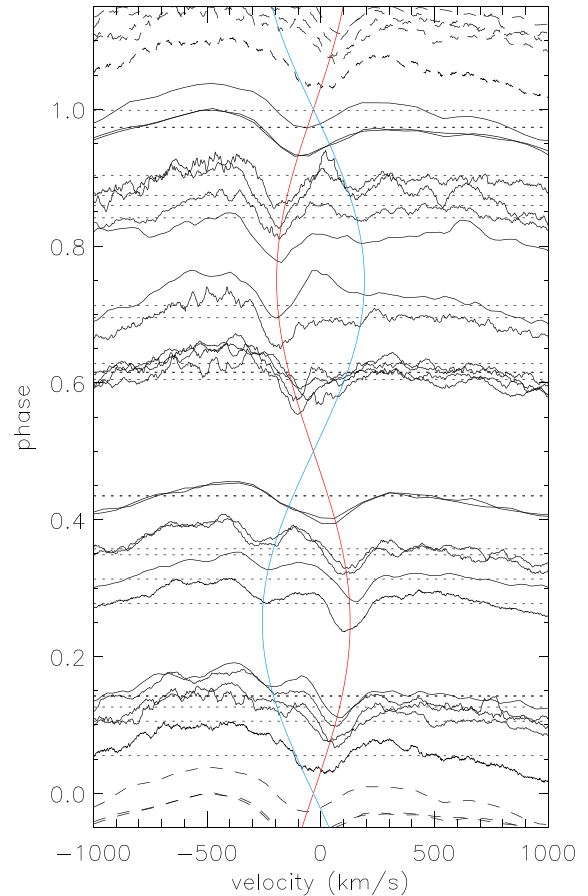


Figure 4. Mean profile of the He I 4388, 4922, and 5016 Å lines. Their position on the y-axis is determined by the orbital phase, based on the period determined in Section 3.1. The orbital solution of Section 4 is plotted.

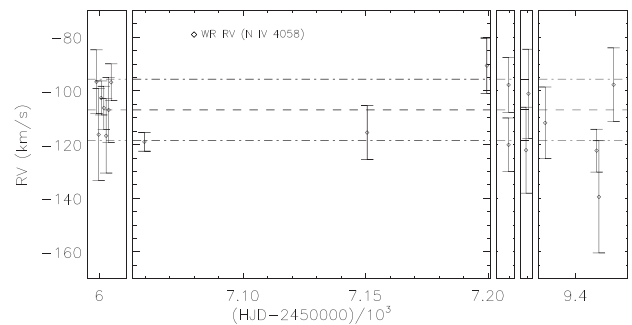


Figure 5. RV of the WR star (black) as a function of time. The average RV of the WR and its uncertainties are drawn with dashed and dash-dotted lines, respectively.

of the two O stars do not follow exactly the WR RV values. This will be discussed later in this publication.

3.3 WR wind variability

The wind of the WR star in the WR 63 system is known to be highly variable. Indeed, Chené & St-Louis (2011) have shown that its LPV can reach an amplitude as high as 10 per cent of the spectral line intensity. These variations are expected to be caused by density wind structures at small and/or large scale. Small-scale wind structures are

expected in virtually all WR stars due to wind clumping (Moffat et al. 1988). On the other hand, periodic large-amplitude LPVs have been found in some WR stars such as WR 134, 6, 1, and 110 (McCandliss et al. 1994; Morel, St-Louis & Marchenko 1997; Chené & St-Louis 2010; Chené et al. 2011, respectively). These are often thought to be due to the presence of corotating interaction regions (CIRs) in their winds, and that possibility is going to be our working assumption in this study.

We analysed our spectra to highlight LPVs in WR 63. Since we know that the emission lines are diluted by the continuum of the O stars, we adjusted the spectra to take into account the variable continuum due to the eclipses (presented in Section 4). In Fig. 6, we present the residuals of each spectrum obtained by subtracting the mean profile (top) from the individual spectra (bottom). In the middle panels we display the temporal variance spectrum (TVS) as defined by Fullerton, Gies & Bolton (1996) and expressed as $\Sigma(99 \text{ per cent}) (= \sqrt{\text{TVS}/[\sigma_0^2 \chi_{N-1}^2(99 \text{ per cent})]}$, where σ_0 is the reciprocal of the rms of the noise level in the continuum in a time series of N spectra) and σ , i.e. a modified TVS divided by the line flux ($\bar{S} - 1$), where \bar{S} is the weighted mean, as defined by St-Louis et al. (2009). These are presented for the N IV 4058 Å, N III 4637 Å, He II 4686 Å, He II 4861 Å, He II 5411 Å, He I 5876 Å, He II 6562 Å, and N V 6677 Å lines.

The value of Σ quantifies the level of variability, such that a spectrum that reaches a value of n varies with an amplitude n times higher than the variability measured in the continuum (which is assumed to be pure noise). Fig. 6 shows that all the spectral lines are significantly variable (i.e. $\Sigma(99 \text{ per cent}) > 1$), except for the line N IV 4058 Å. As said above, since this line is closer to the base of the wind than other lines, it is very likely that it is less affected by variations due to CIRs. Also, if there is any LPV in that line, it would be lost in the noise that tends to be bigger at that wavelength than in the rest of the spectrum, as spectrographs tend to be less efficient at blue wavelengths than at red ones.

For all spectral lines but N IV 4058 Å, we can determine a σ value, which gives the amplitude of variability relative to the line intensity. By averaging out the σ spectrum over the wavelength range corresponding to the emission line, we obtain an average LPV amplitude for the line. Different lines may give different results. We find $\sigma = 5.4 \pm 1.2$ per cent (N III 4637 Å), 6.1 ± 1.2 per cent (He II 4686 Å), 16.5 ± 3.1 per cent (He II 4861 Å), 8.5 ± 2.0 per cent (He II 5411 Å), 14.8 ± 7.5 per cent (He I 5876 Å), 7.6 ± 2.4 per cent (He II 6562 Å), and 7.7 ± 2.4 per cent (N V 6677 Å). The uncertainties are determined by the standard deviation of the σ spectrum. We conclude that most lines show comparable σ values between 6 per cent and 8 per cent, except for He II 4861 Å and He I 5876 Å, which have much higher values.

The He II 4861 Å line is more variable because, in addition to the CIR-like LPVs that can be seen in isolated lines such as He II 5411 Å, the H β lines from the two O companions are also moving following the orbit that we will describe later in this paper. Of course, the He II 6562 Å line is itself affected by the H α lines of the O companions, but because this emission line is much stronger than the He II 4861 Å line, the effect is much smaller. The He I 5876 Å line is potentially also affected by the same line in absorption from the O companions.

We can suspect that the LPVs have the same origin as the photometric variations with the frequency $\nu_2 = 0.615(1) \text{ d}^{-1}$ determined in Section 3.1. Unfortunately, the time sampling of the LPVs prevents any robust determination of a period to compare with. Indeed, CIR-like LPVs are known to be epoch-dependent, and observations that

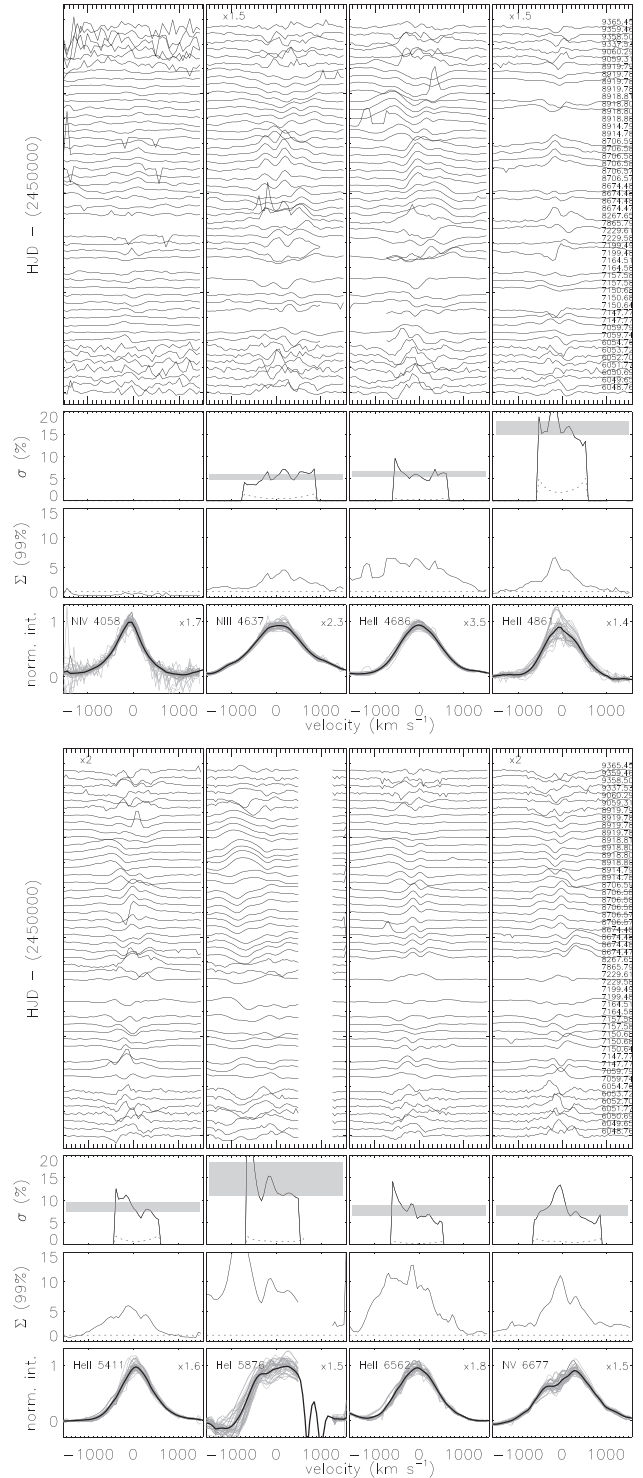


Figure 6. Variability in eight emission lines from the WR wind. The bottom section shows the average profile of the lines with every individual profile of all the observing runs superposed in pale grey. The top section shows the residuals of each individual spectra with the average profile. The HJD is indicated for each residual on the right of the plot. In the middle two sections the $\Sigma(99 \text{ per cent})$ and the σ (per cent) spectra are presented; see text for more details.

are obtained with a time difference longer than a few weeks cannot be combined, as the configuration of the CIRs at the origin of the LPVs has changed completely (St-Louis et al. 2020). The typical structures found in the residuals are a few 100 km s⁻¹ wide, but are wider in the absorption component of P Cygni profiles. Indeed, discrete absorption components (DACs) can be observed in P Cygni profiles and they vary with the same period as the bumps on top of emission lines (Aldoretta et al. 2016). The LPVs in well isolated lines, such as He II 4686 Å and He II 5411 Å, are very similar, while LPVs in double lines and multiplexes can be interpreted as the same variations repeated as many times as there are contributing lines.

Finally, the LPVs associated with DACs in the absorption component of the He I 5876 Å line seem to appear in most of the other lines as well, indicating that all lines have a component equivalent to a P Cygni profile, even when it is filled in by the emission component and is not clearly visible. This is interesting considering that atmospheric modelling often struggles to reproduce the extended blue absorption profile of strong emission lines where the P Cygni absorption feature seems overestimated (e.g. Herald, Hillier & Schulte-Ladbeck 2001; Sander et al. 2014; Aadland et al. 2022, or even in this study). From our observations, we suggest the possibility that it is the emission feature that is underestimated; however, we cannot at this point offer any physical explanation in support of this statement.

4 THE INNER O+O ECLIPSING BINARY

We use the PHOEBE (PHysics Of Eclipsing BinariEs, version 2.3, Prša & Zwitter 2005; Prša et al. 2016; Horvat 2018; Conroy et al. 2020) code to simultaneously model the *TESS* light and the RV curves (see Fig. 7). We adopt 1.0 for the bolometric albedos A (coefficients of reprocessing of the emission of a companion by ‘reflection’) and for the gravity darkening coefficients g (the orbital parameters are presented in Table 1). For the limb darkening, we use the square-root law, better suited for hotter stars (Diaz-Cordoves, Claret & Gimenez 1995). We also account for reflection effects and adopt two reflections. The orbital period was fixed to twice that derived from the *TESS* light curve since the eclipses are separated by half the orbital period. As mentioned above, the orbit was adopted to be circular.

The problem with WR 63’s light curve is the high level of variability of the WR wind that confuses the signal from the real eclipses. To prevent the PHOEBE algorithm from getting confused, especially in the interval between the eclipses, we use the median light curve folded in the orbital period as the input. The uncertainties on the derived parameters are estimated using the Markov chain Monte Carlo (MCMC) method implemented via EMCEE (Foreman-Mackey et al. 2013). Two models have been run to derive the properties of the system: first, a model without including a third light source that would come from the WR star, and a second with it.

Without the third star, the solution yields a system seen under an inclination of $73.8_{-0.1}^{+0.1}$. The O-star primary in the inner system has a radius equal to $7.7_{-0.2}^{+0.1} R_{\odot}$ and a mass of $15.8_{-0.1}^{+0.1} M_{\odot}$. The O-star secondary has a radius of $6.6_{-0.1}^{+0.1} R_{\odot}$ and a mass of $11.4_{-0.1}^{+0.1} M_{\odot}$. The surface gravities are equal to $3.87_{-0.01}^{+0.01}$ [cgs] for the primary and $3.86_{-0.01}^{+0.01}$ [cgs] for the secondary. We derive luminosities of $\log(L/L_{\odot}) = 4.45 \pm 0.07$ for the primary and $\log(L/L_{\odot}) = 4.32 \pm 0.07$ for the secondary. From the observed composite spectra, we also computed the projected rotational velocities of the two stars to be equal to 90_{-10}^{+10} and 80_{-10}^{+10} km s⁻¹, respectively. Using the inclination of the system (and assuming that the stars have a

Table 1. Orbital parameters for the 4.03 d inner binary, obtained from the orbital analysis using PHOEBE. Error bars correspond to 1σ .

Parameter	Value	
P_{orb}	4.0275 ± 0.0008	
HJD ₀	$2459000.48169 \pm 0.02083$	
e	0.0 (fixed)	
ω [°]	270.0 (fixed)	
$q(M_2/M_1)$	$0.72_{-0.02}^{+0.08}$	
K_1 [km s ⁻¹]	161.62 ± 6.50	
K_2 [km s ⁻¹]	224.47 ± 11.20	
γ [km s ⁻¹]	-33.13 ± 3.98	
$M \sin^3 i$ [M_{\odot}]	13.59 ± 1.36	9.92 ± 0.84
$a \sin i$ [R_{\odot}]	12.87 ± 0.47	17.63 ± 0.78

rotational axis perpendicular to the orbital plane), we find the two stars to be in synchronous corotation with the orbit.

In the second model (i.e. including a third light source), the WR star is expected to be responsible for 64 ± 2 per cent of the total flux of the system. As a consequence of the inclusion of the third light source the system is now seen under an inclination of $82.9_{-0.6}^{+1.0}$. The radius of the primary is equal to $7.4_{-0.1}^{+0.1} R_{\odot}$, and that of the secondary $7.0_{-0.1}^{+0.1} R_{\odot}$. These values are thus similar in the two models. The masses are equal to $14.3_{-0.1}^{+0.1} M_{\odot}$ for the O-star primary and $10.3_{-0.1}^{+0.1} M_{\odot}$ for the O-star secondary. The inferred surface gravities are $3.85_{-0.01}^{+0.01}$ [cgs] and $3.82_{-0.02}^{+0.02}$ [cgs] for the primary and secondary, respectively. Assuming effective temperatures of 31.0 ± 1.5 and $30.0_{-4.0}^{+0.8}$ K for the primary and secondary, respectively, the computed luminosities are $\log(L/L_{\odot}) = 4.66 \pm 0.08$ and $4.55_{-0.23}^{+0.05}$. The two models yield very similar parameters, even though, when the third light source is not considered, the masses of the two inner components are higher. While both models are acceptable, the sections between the eclipses are better modelled if we include the third light. A summary of the different parameters is given in Table 2.

5 EVOLUTIONARY STATUS

The analysis of the light curve provides us with good estimates of the stellar parameters of the two O stars in WR 63. We adopted synthetic spectra for the O stars, using effective temperatures, surface gravities, and projected rotational velocities, as given in Table 2. The models have been successively convolved with a rotation profile to mimic their rotational velocities ($v \sin i = 90$ and 80 km s⁻¹ for the O primary and O secondary, respectively) and a radial-tangential profile to reproduce their macroturbulent velocity ($v_{\text{mac}} = 30$ km s⁻¹ for both O stars). The wind parameters were adopted as follows: the mass-loss rates from Vink, de Koter & Lamers (2001) for Galactic metallicity, the terminal wind velocities are estimated to be 2.6 times the effective escape velocity from the photosphere (v_{esc} , Lamers, Snow & Lindholm 1995), and the exponent of the velocity law (β) to be 1 (Repolust, Puls & Herrero 2004). The models were computed by including the following elements: H, He, C, N, O, Ne, Mg, Al, Si, S, Ar, Ca, Fe, and Ni and the abundances were adopted to be solar (Grevesse et al. 2010).

To derive the fundamental properties of the WR star, we used the atmosphere code CMFGEN (Hillier & Miller 1998). CMFGEN is a non-LTE radiative transfer code, developed to model the atmospheres of stars with stellar winds. The luminosity, the radius, the mass-loss rate, the terminal wind speed, and the CNO surface abundances were considered as free parameters.

We fitted the spectral energy distribution (SED) of the whole system combining the three SEDs of individual objects. We obtained

Table 2. Stellar parameters of the three components in WR 63. Error bars correspond to 1σ .

Parameter	Primary ^a no third light source	Secondary ^a	Primary ^a with third light source	Secondary ^a	WR star ^b
Spectral type	O9 V	O8 V	O9 V	O8 V	WN7
i [°]	73.8 ^{+0.1} _{-0.1}		82.9 ^{+1.0} _{-0.6}		–
T_{eff} [kK]	31.0 ± 1.5	26.5 ± 3.0	31.0 ± 1.5	30.0 ^{+0.8} _{-4.0}	42.7 ± 1.5 ^c
$\log(L/L_{\odot})$	4.45 ± 0.07	4.32 ± 0.07	4.66 ± 0.08	4.55 ^{+0.05} _{-0.23}	5.33 ± 0.14
$\log g$ [cgs]	3.87 ^{+0.01} _{-0.01}	3.86 ^{+0.01} _{-0.01}	3.85 ^{+0.01} _{-0.01}	3.82 ^{+0.02} _{-0.02}	–
R [R_{\odot}]	7.7 ^{+0.1} _{-0.2}	6.6 ^{+0.1} _{-0.1}	7.4 ^{+0.1} _{-0.1}	7.0 ^{+0.1} _{-0.1}	8.5 ^{+1.7c} _{-1.5}
M [M_{\odot}]	15.8 ^{+0.1} _{-0.1}	11.4 ^{+0.1} _{-0.1}	14.3 ^{+0.1} _{-0.1}	10.3 ^{+0.1} _{-0.1}	–
$v \sin i$ [km s^{-1}]	90 ± 10	80 ± 10	90 ± 10	80 ± 10	–

Notes. ^aObtained from PHOEBE modelling.

^bObtained from CMFGEN modelling. ^cCorresponding to $T_{*} = 44.1 \pm 1.5$ kK and $R_{*} = 7.9^{+1.7}_{-1.5} R_{\odot}$.

an extinction of $A_V = 5.31 \pm 0.08$ using the reddening law of Fitzpatrick & Massa (2007). Given that *Gaia* does not provide a distance for WR 63, we used the luminosities of the two O stars, the bolometric corrections (computed from Martins, Schaerer & Hillier 2005 using their effective temperatures), and the dilution factors of $f_{\text{WR}} = 0.65 \pm 0.05$, $f_{\text{O}_1} = 0.21 \pm 0.03$, and $f_{\text{O}_2} = 0.14 \pm 0.02$ for the WR, the O primary, and the O secondary, respectively, to compute a distance of 3.4 ± 0.5 kpc. Adopting that distance, we compute a stellar luminosity of $\log(L/L_{\odot}) \sim 5.33 \pm 0.14$ for the WR star. All parameters are given in Table 2.

The modelling was carried out directly by comparing the combined synthetic spectra to the composite spectra. Given the heterogeneity of our observations (different resolutions, wavelength ranges, etc), we decided not to apply spectral disentangling at this point, but to wait for higher-resolution higher S/N spectra that will be better sampled over the orbital cycle of the O+O (inner) binary. We present in Fig. 8 a comparison between one of our observed spectra and the combined synthetic models. Given that the spectra contain three objects, we use the dilution factors listed above to scale the synthetic spectra to the different profiles in the composite spectra.

Assuming the usual β law ($v = v_{\infty} (1 - R/r)^{\beta}$) with $\beta = 1$, we derive for the WR star an effective temperature of 42.7 ± 1.5 kK and a radius of $12.2^{+1.7}_{-1.5} R_{\odot}$ at $\tau_{\text{ross}} = 2/3$. We use a mass-loss rate of $\dot{M} = 10^{-4.80} M_{\odot} \text{yr}^{-1}$ and a terminal wind speed of $v_{\infty} = 1350 \text{ km s}^{-1}$. The synthetic models have been computed by including wind clumping ($f_{\text{cl}} = 0.1$). We also compute the surface abundances of carbon, nitrogen, and oxygen to be $\epsilon_{\text{C}} = 7.78$ (mass fraction: $X(\text{C}) = 1.77 \times 10^{-4}$), $\epsilon_{\text{N}} = 9.58$ (mass fraction: $X(\text{N}) = 1.31 \times 10^{-2}$), and $\epsilon_{\text{O}} = 8.18$ (mass fraction: $X(\text{O}) = 5.90 \times 10^{-4}$), respectively, for the WR star. We stress that no indication of the presence of hydrogen is detected in the spectrum of this WR star, as mentioned by Hamann, Gräfener & Liermann (2006). This suggests that it has already reached the classical WR phase and has left the main sequence. The parameters that we derived for the WR star are in agreement with those provided by Hamann et al. (2006, 2019) within the error bars. These authors did, however, not account for the multiplicity of the system, which led to a larger luminosity for the WR star. Given the absence of UV spectra, the terminal wind speed was derived by Hamann et al. (2006, 2019) through a careful inspection of the lines, without, however, specifying which lines were considered. For our analysis, we mainly focus on the P Cygni profiles visible in the optical, mainly He I 5876 Å (see Fig. 8). The error bars on the terminal wind speed ($\sim 250 \text{ km s}^{-1}$) are therefore larger than when one derives it from the UV P Cygni profiles.

The evolutionary status of the three stars is interpreted using the single-star tracks from Ekström et al. (2012), with an initial rotational velocity of $\sim 300 \text{ km s}^{-1}$, as they predict the stellar evolution until the helium core-burning phase, unlike tracks from Bonn (Brott et al. 2011). We use the derived parameters for the O stars using the model with the third light source (see Table 2), and those of the WR star

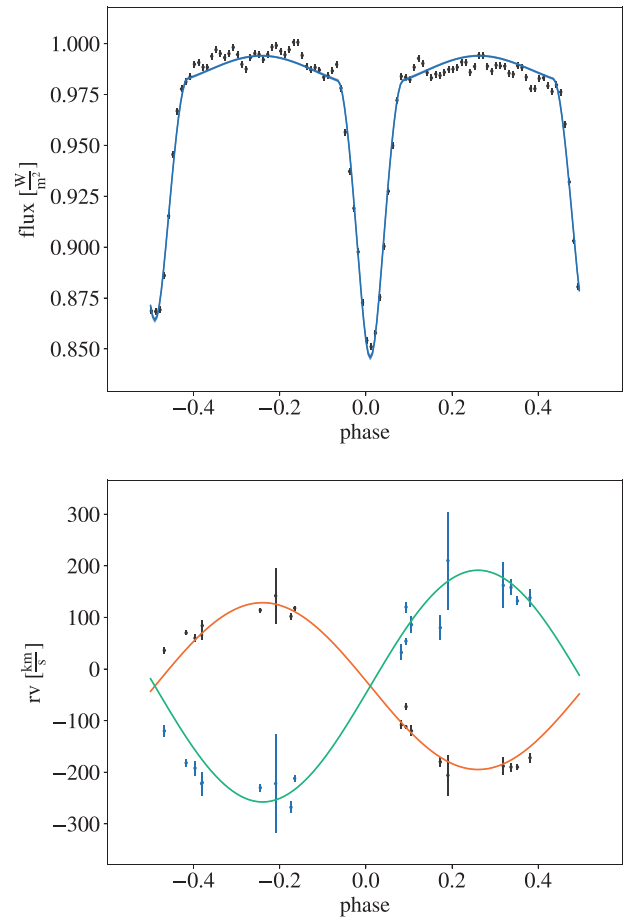


Figure 7. Top: Mean *TESS* light curve of WR 63 phase-folded with the 4.03 d period (black dots) and the fit (blue line) obtained from the orbital fitting using PHOEBE. Bottom: Radial velocity measurements and best-fitting RV curves of the O+O binary according to the solution listed in Table 2. The primary (secondary) is shown by black dots/orange line (blue dots/green line). Phase 0 corresponds to the primary eclipse.

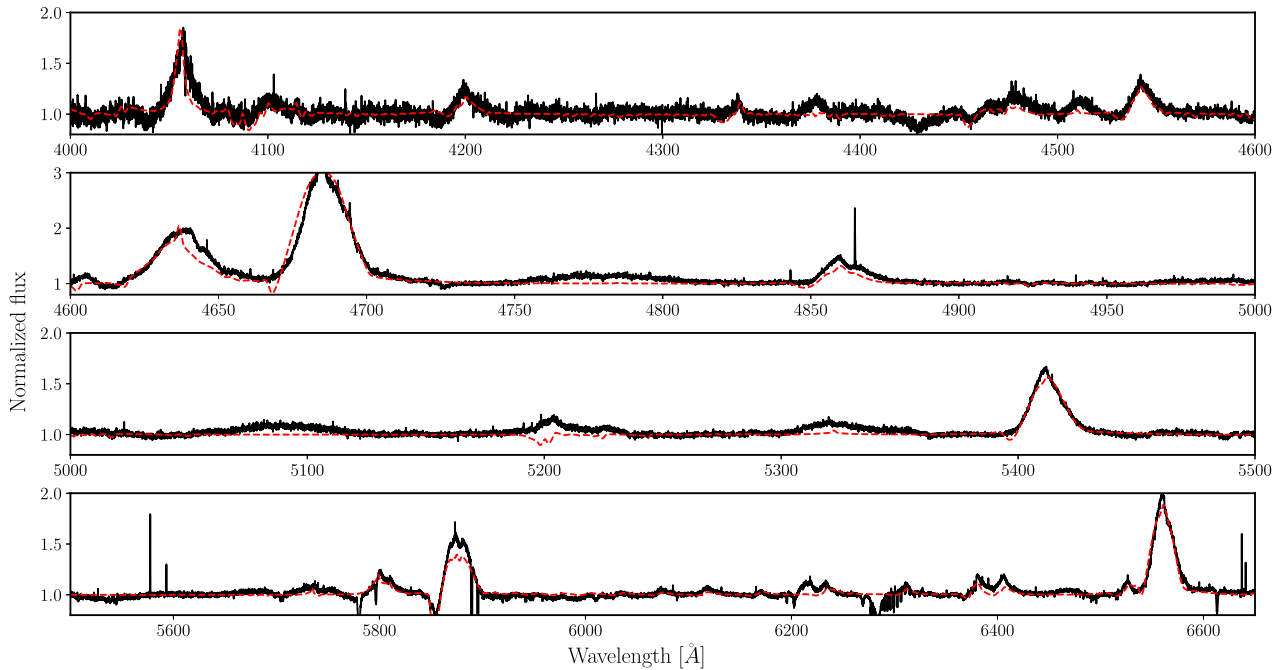


Figure 8. Best-fitting CMFGEN model (red) of WR 63 compared to the spectrum acquired on 2012 May 1. The synthetic spectra of the three stars have been combined with dilution factors of 0.65, 0.21, and 0.14 for the WR, the O primary, and the OB secondary, respectively.

as input to estimate the ages of the three stars. We display in Fig. 9 a Hertzsprung–Russell diagram, showing the positions of the three stars. We interpolated the stellar parameters through the Geneva tracks to estimate the predicted ages of the three stars. Within the error bars, it appears that the three stars are coeval (i.e. they are the same age). That indicates that the three objects have evolved as single stars. According to the Geneva tracks, the WR star is expected to have an initial mass of $35 \pm 5 M_{\odot}$ while the primary O star and the secondary O star are expected to have initial masses of 18 ± 2 and $16 \pm 2 M_{\odot}$, respectively. The Geneva tracks indicate an age of 5.9 ± 1.4 Myr for the WR star, 6.0 ± 1.1 Myr for the O primary, and 8.2 ± 2.5 Myr for the O secondary. One should note that the effective temperature of the secondary O star has a large uncertainty, and more spectroscopic data are needed to confirm our results.

Our spectroscopic data cover 3317 d, divided into five periods. Over that time span, we were not able to detect any motions of the WR star or the combined inner O+O binary system. Assuming that the three stars have evolved as single stars in a hierarchical system, the WR star should have gone through a red supergiant or luminous blue variable phase. During this phase, the radius of the star is assumed to reach hundreds of solar radii. The outer orbit (that hosting the WR star) must have a semimajor axis as large as that value, which implies the need for a long orbital period. That could indeed explain why, from our data, we are unable to detect the motion of the WR star. This is also true if the outer orbit is highly eccentric. Therefore, more observations are needed to constrain the real nature of the system, but, if WR 63 is really a hierarchical system, it could serve as a Rosetta stone for testing single-star evolutionary tracks.

6 SUMMARY AND CONCLUSIONS

Using high-resolution spectra and high-cadence photometry, we have identified three components in the composite spectra of WR 63: an

O9 V primary and an O9.5 V secondary that are paired in a 4.03 d orbit, and a WR star classified as WN7. Our analysis does not allow us to show that the WR star is gravitationally bound to the O+O system. Even though a spurious alignment between the WR star and the O+O system is possible, the likelihood of having a hierarchical triple system seems more plausible.

We have shown that the two O stars form a detached binary system, and that there is no sign that these components have already interacted with each other. Assuming that the WR star is bound to the inner system, the age of the system can be inferred by the WR star. Using the Geneva tracks (Ekström et al. 2012), the mean age of WR 63 is estimated to be about 5.9 ± 1.4 Myr. Combining the estimated age with the masses and luminosities of the O stars, we showed that the three objects are coeval.

Longer-term observations are therefore required to shed more light on the exact structure of this complex system, specifically elucidating the remaining hierarchical configuration of the WR star with respect to the O+O system. Knowing the orbital and physical properties of such a system could serve as a cornerstone to study the Kozai–Lidov mechanism that occurs in hierarchical triple systems.

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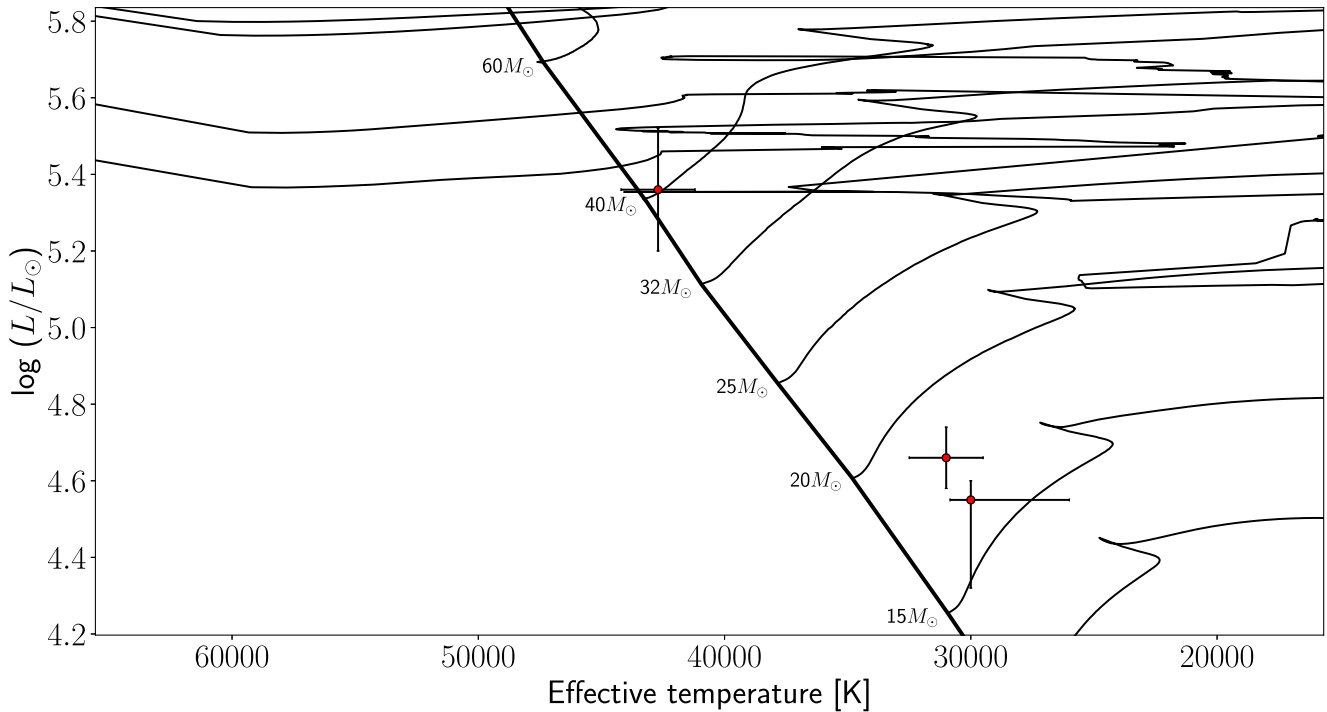


Figure 9. Hertzsprung–Russell diagram. The tracks are from Ekström et al. (2012), computed with an initial rotational velocity of 300 km s^{-1} . The locations of the three objects are based on the PHOEBE model including a third light source.

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DATA AVAILABILITY

Most spectroscopic observations underlying this article will have past the proprietary period by the time this publication will be published,

and raw data can be downloaded from the ESO, SALT and Gemini archives. The reduced spectra and the light-curves will be shared on reasonable request to the corresponding author.

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