RESEARCH

Open Access

Individual-specific networks for prediction modelling – A scoping review of methods



Mariella Gregorich^{1,2}, Federico Melograna³, Martina Sunqvist⁴, Stefan Michiels⁴, Kristel Van Steen^{3,5} and Georg Heinze^{1*}

Abstract

Background: Recent advances in biotechnology enable the acquisition of high-dimensional data on individuals, posing challenges for prediction models which traditionally use covariates such as clinical patient characteristics. Alternative forms of covariate representations for the features derived from these modern data modalities should be considered that can utilize their intrinsic interconnection. The connectivity information between these features can be represented as an individual-specific network defined by a set of nodes and edges, the strength of which can vary from individual to individual. Global or local graph-theoretical features describing the network may constitute potential prognostic biomarkers instead of or in addition to traditional covariates and may replace the often unsuccessful search for individual biomarkers in a high-dimensional predictor space.

Methods: We conducted a scoping review to identify, collate and critically appraise the state-of-art in the use of individual-specific networks for prediction modelling in medicine and applied health research, published during 2000–2020 in the electronic databases PubMed, Scopus and Embase.

Results: Our scoping review revealed the main application areas namely neurology and pathopsychology, followed by cancer research, cardiology and pathology (N = 148). Network construction was mainly based on Pearson correlation coefficients of repeated measurements, but also alternative approaches (e.g. partial correlation, visibility graphs) were found. For covariates measured only once per individual, network construction was mostly based on quantifying an individual's contribution to the overall group-level structure. Despite the multitude of identified methodological approaches for individual-specific network inference, the number of studies that were intended to enable the prediction of clinical outcomes for future individuals was quite limited, and most of the models served as proof of concept that network characteristics can in principle be useful for prediction.

Conclusion: The current body of research clearly demonstrates the value of individual-specific network analysis for prediction modelling, but it has not yet been considered as a general tool outside the current areas of application. More methodological research is still needed on well-founded strategies for network inference, especially on adequate network sparsification and outcome-guided graph-theoretical feature extraction and selection, and on how networks can be exploited efficiently for prediction modelling.

Keywords: Individual-specific network, Prediction, Personalized medicine, Graph theory, Methodological review, Network analysis, Genomics, Neurology, Pathopsychology, Biomarker

*Correspondence: georg.heinze@meduniwien.ac.at ¹ Section for Clinical Biometrics, Center for Medical Statistics, Informatics and Intelligent Systems, Medical University of Vienna, Vienna, Austria Full list of author information is available at the end of the article



Introduction

Prediction modelling is essential to an individualized approach to risk assessment, diagnosis, prognosis, and medical decision-making. While the conventional

© The Author(s) 2022. **Open Access** This article is licensed under a Creative Commons Attribution 4.0 International License, which permits use, sharing, adaptation, distribution and reproduction in any medium or format, as long as you give appropriate credit to the original author(s) and the source, provide a link to the Creative Commons licence, and indicate if changes were made. The images or other third party material in this article are included in the article's Creative Commons licence, unless indicated otherwise in a credit line to the material. If material is not included in the article's Creative Commons licence and your intended use is not permitted by statutory regulation or exceeds the permitted use, you will need to obtain permission directly from the copyright holder. To view a copy of this licence, visit http://creativecommons.org/licenses/by/4.0/. The Creative Commons Public Domain Dedication waiver (http://creativecommons.org/publicdomain/zero/1.0/) applies to the data made available in this article, unless otherwise stated in a credit line to the data.

approach of model development is mainly based on a small set of patient characteristics, recent developments in biotechnology (e.g. high-resolution imaging modalities and high-throughput sequencing methods) have accelerated the generation of individual-specific data at an unprecedented level generally characterized by a high-dimensional variable space for each individual and complex correlation structures between the variables. Common methods of prediction modelling are not well suited to deal with such complex data structures in particular in small to moderately sized studies [1–3]. Hence the question arises how the abundance of biological information available per individual can be used most efficiently to provide accurate predictions of health outcomes.

Increasingly, it becomes possible to represent individual patient data as individual-specific networks that, apart from individual-specific node measurements, allow to capture connectivity information between variables (nodes) via their edges. Individual-specific networks are exemplified in Fig. 1 for a hypothetical small study cohort. The absence/presence of an edge, or its weight (strength of the connectivity) can be the same for all individuals in the sample (e.g. based on a reference or on sample estimates of a statistical measure of connectivity), or can vary from individual to individual. For example, the individuals depicted in Fig. 1 share the same network structure but are heterogeneous with respect to the edge weights. The network representation is further motivated by subject matter, since complex diseases of the human body are rarely caused by the malfunction of individual molecules but rather by the disruption or dysfunction of the underlying system behaviour or a specific set of biological units [4]. Graph-theoretical features can then capture the heterogeneous variability of system patterns across individuals by describing individualspecific structural and topological network patterns or identify biological modules, a set of nodes acting as key drivers of disease manifestation. For the sake of clarity, variables that originate from individual-specific networks will be referred to as graph-theoretical features throughout this work in order to distinguish them from classic clinical variables. Graph-theoretical features condense a high-dimensional predictor space into few quantitative and interpretable descriptors that can be used in prediction models instead of or in addition to classical clinical predictors in order to improve such models. Such an approach may lead to new insights into disease development or progression and may even replace the often unsuccessful search for individual prognostic biomarkers in the high-dimensional space.

In the past decades, the call for a complex systembased understanding of human disease mechanisms has led to a general theory and various application frameworks of group-level networks, i.e. network inference based on the aggregated study cohort. For example, see Barabási et al. [4] for an extensive review on 'network medicine' and Li et al. [5] for an overview of graph representation learning in biology and medicine. However, a "one size fits all" approach for network inference may wash out the individual-specific systems behaviour. Linking individual-specific patterns of connections rather than group-level system behaviour across biological components to disease manifestation can not only capture the



heterogeneity of biological system behaviour across individuals but also pave the way for the detection of novel biomarkers for more individualized prediction.

To our knowledge, the potential of using graph-theoretical features of individual-specific networks as predictors in clinical prediction models has not yet been systematically explored and hence the state-of-the-art in this relatively new field of predictive research remains unknown. Therefore, we conducted a scoping review [6, 7] to systematically examine the scientific literature to identify, collate and critically appraise methodological approaches incorporating individual-specific networks to improve and advance prediction modelling of clinical outcomes in applied health research. We did not consider studies exclusively employing group-level networks and those which do not aim at individual outcome prediction.

The remainder of this paper is organized as follows. In Section 2, we discuss the methodology of the scoping review. The general study characteristics and findings of the search strategy are presented in Section 3. Further, we present and collate the identified approaches to individual-specific network inference, graph-theoretical feature extraction and their usage for prediction in Section 4 and conclude with current challenges and future aspects of the identified methodology in Section 5.

Methods

Search strategy

We conducted a scoping literature search in the three electronic databases PubMed, Embase and Scopus to extract peer-reviewed articles published between January 1st, 2000 and August 31st, 2020. The search strategy consisted of three sets of terms to cover the research intersection of network analysis and prediction modelling adequately but also to reduce false positive hits by the broad meaning of the term 'network'. The three sets of terms were: 1) terms associated with network analysis, 2) terms associated with predictive research and 3) exclusion terms (see the Supplementary Material for a detailed overview).

Studies met the inclusion criteria if graph-theoretical features derived from an individual-specific network were considered as candidate predictors in prediction modelling in the medical field. Studies were excluded if they did not focus on prediction modelling of health outcomes and did not consider networks constructed for single individuals. Therefore, we excluded studies that concentrated solely on the descriptive analysis of individual-specific networks without examining their potential association with a clinical outcome or studies considering group-level networks computed from aggregated data. Studies that essentially aimed at predicting network behaviour, link prediction or changes in network topology or structure were also discarded.

Selection of studies

All studies identified by the search strategy were initially screened based on the title and then, after inclusion, based on the abstract to determine eligibility. Letters, commentaries and conference abstracts were excluded. Selected articles were then subjected to a full-text analysis. The first author was responsible for the initial search, application of the exclusion criteria, screening of all the identified articles and the quality evaluation of the included papers. A random subset of studies (consisting of 250, 50 and 25 studies in the title, abstract and fulltext screening phases, respectively) was independently assessed by three additional reviewers (GH, FM, MS) to ensure general validity and reliability of the screening process and data extraction of the first reviewer. Any inconsistencies in selection among the reviewers were discussed and resolved to reach a general consensus., We refer the reader to the Supplementary Material for a more detailed summary of the search strategy and the extraction process. Reporting adhered to the PRISMA-ScR guidelines [7] to ensure methodological transparency.

Results

Search results and study characteristics

A total of 4988 studies was initially retrieved from the electronic database search together with the manual selection from other sources. After the screening of the titles, 488 articles remained and after reviewing the abstracts, only 227 articles met the eligibility criteria for full-text analysis of which 79 were excluded due to the following reasons: (1) construction of non-individual-specific networks (N=36), (2) the term "network" was used in a different context (N=17), (3) no association with an outcome of interest was considered (N=17) or (4) graph-theoretical features were used as dependent variables (N=9). This left 148 studies (3.0%) out of the initial 4988 studies meeting the eligibility criteria of the review (see Fig. 2).

Through a synthesis of the sources of evidence, four medical domains of application were identified. The majority of the eligible studies (N = 129, 87.2%) covered neurological research, followed by the fields of psychopathology (N = 9, 6.1%), genomics (N = 7, 4.7%), cardiology (N = 2, 1.4%) and pathology (N = 1, 0.7%). The oldest study meeting our inclusion criteria was published in 2009, with the number of studies published annually increasing steadily thereafter (see Supplementary Fig. S1). Most of the studies (N = 100, 67.6%) were published after 2015. Out of the 148 included studies, 135 (91.2%) were identified as quantitative studies and 13 (8.8%) as



qualitative studies (e.g. reviews). Besides the process of data acquisition and preparation in applied health research, three main topics emerged in the included articles covering the intersection of network analysis and prediction and were addressed separately in the following subsections: Section 3.2 focuses on data-driven network inference consisting of the individual-specific network construction and network sparsification, Section 3.3 on the extraction of graph-theoretical features and Section 3.4 on predictive analytics using graph-theoretical features. Main modules in a general workflow of considering individual-specific networks in prediction modelling and some aspects of their implementation are illustrated in Fig. 3. However, a detailed presentation of each of the identified analytics for network analysis and prediction modelling as well as their theoretical



properties is beyond the scope of this article. Instead, the reader will find useful references throughout this work.

Network construction and sparsification *Notation and concepts*

In general, an undirected network (or graph) consists of a pair G = (V, E) where V denotes a finite, non-empty set of *p* nodes and *E* is a subset of $V \times V$ containing pairs of connected nodes $e_{ii} \coloneqq (v_i, v_i)$ referred to as edges. In directed graphs (digraph), each edge has a direction such that $e_{ii} \neq e_{ii}$. In weighted networks, each edge e_{ii} is associated with a weight $w_{ij} \coloneqq w(v_i, v_j) \in R$. A subnetwork G' = (V, E') is a network such that $V \subseteq V$ and $E' \subseteq E$. The data structure defining a network is the adjacency matrix $A = [a_{ij}]$ in which $a_{ij} = 1$ indicates the presence of an edge between v_i and v_i , while $a_{ii} = 0$ indicates its absence. For weighted networks $a_{ii} = w_{ii}$, and again $a_{ii} = 0$ indicates the absence of the respective edge. For individual-specific networks, we assume that for each individual s (s = 1, ...,N) a unique network $G_{s} = (V_{s}, E_{s})$ exists, where N is the number of individuals within the study cohort.

Global graph-theoretical features characterize properties of the entire network, while local features only take the information of a smaller substructure of the network (e.g. node, module) into account. For example, edge density is a global graph-theoretical feature defined as the ratio of the number of actual connections to the number of all possible connections in the network

$$d = \frac{2 |E|}{|V|(|V|-1)}$$
(1)

See Table 1 for an overview of some global and local graph-theoretical features identified in the reviewed studies.

Construction of individual-specific networks

Repeated measurements per variable per individual Depending on the field of research, the nodes mainly represented regions of interest (ROIs) in the brain, genes or psychotic symptoms (e.g. stress, insomnia). In two individual proof-of-concept studies, the nodes corresponded to 5-min heart rate variability (HRV) segments [8] or ROI in muscle biopsy images [9]. A variety of methods were identified for defining connectivity between pairs of nodes based on data-driven structural learning, i.e., estimating the graphical structure from the data (see Fig. 4 for a schematic illustration).

The majority of identified studies conducted correlationbased approaches (see Fig. 4A) using repeatedly measured continuous data (e.g. sequential data, time series) to define edges between the prespecified nodes [10-27]. In neurological applications, adjacency matrices most frequently consisted of correlation coefficients (N=69, P=48.9%) (e.g., Pearson product moment correlation coefficient) of time series of brain activity (e.g. blood oxygenation level dependent (BOLD) signal) or longitudinal cortical thickness between pairs of ROIs [16]. Fisher's r-to-z transformation was applied to Pearson correlation coefficients to achieve approximate normality [14, 21, 26, 28, 29]. However, correlation-based inference of the network structure can be subject to interfering effects (e.g. outliers, noise) and can only capture pairwise information. Thus, variations of the Pearson correlation such as spatial smoothing have been proposed in which the time series corresponding to a region is obtained by a linear mixture of neighbouring time series or segmentation of the BOLD time series into subdivisions (e.g. snapshot graphs, sliding-window approach) [10, 30-32]. The sliding window or snapshot

Table 1 Explanation of the graph-theoretical features used in \geq 10 prediction modelling studies. Local features can be averaged over all nodes to obtain the global-scale counterpart

Graph-theoretical feature	Abbrev.	N	Scale	Explanation	
Clustering coefficient	СС	82	Both	Ratio of the connected triangles to the maximum possible number of triangles	
Characteristic path length	CPL	60	Both	Average of all shortest paths over all pairs of nodes	
Global efficiency	GE	55	Global	Average of the reciprocals of the shortest path lengths	
Local efficiency	LE	45	Local	Global efficiency applied to the neighbourhood of a node	
Small-world index	SWI	42	Global	Ratio of the CC normalized by that expected in a random graph and the CPL normalized by that expected in a random graph	
Degree	Dg	38	Local	Number of links of a node	
Betweenness centrality	BC	36	Local	Ratio of all shortest paths with and without the node	
Edge weight	EW	34	Local	Strength of the connection between two nodes	
Modularity	М	21	Global	Degree to which nodes tend to form relatively independent modules	
Density	Ds	18	Global	Percentage of observed connections from the maximum number of possible connections	
Assortativity	А	10	Global	Pearson correlation coefficient of degree between pairs of connected nodes	



graph approach only consider small time windows of the full time series yielding a set of graphs $G_s = \{G_{s1}, ..., G_{st}\}$ for individual *s* and *t* time windows. Then, a presumably more robust final version of the individual-specific network can be obtained by assessing the frequency of appearance of each edge in each G_{sj} for j=1, ..., t because only a few of these snapshot graphs G_{sj} are influenced by disruptions of the time series by noise artefacts [10]. Some studies also employed several modifications of the standard Pearson correlation coefficient to define connectivity [33–37].

An extension to the bivariate determination of connectivity were partial correlation-based networks [38, 39]. Partial correlation coefficients describe the correlation between two variables that cannot be explained by associations of the variable pair with other variables. In the case of nonnormality of the data, a transformation can be applied prior. Another approach to control for covariates while accounting for temporal information is vector autoregressive (VAR) modelling that regresses the dependent variable measured at time point t on the lagged dependent variable and the predictors evaluated at time point t-1. VAR was only employed in psychological studies [40, 41]. This way directed individual-specific networks were obtained such that an edge weight w_{ii} associated with a directed link from node v_i to node v_i corresponds to the respective VAR coefficient in the model. The VAR model and resulting directed networks implied that in general $w_{ii} \neq w_{ii}$. Only 2 out of the 135 quantitative studies considered directed networks estimated using VAR models [40, 41].

A recently introduced network-based representation referred to as a visibility graph allows to derive individual-specific networks from time series data if available per patient in the cohort [42]. A time series with *n* sequentially ordered data points, $\{x_t\}_{t=1, \dots, n}$ is transformed into a network in which each time point *t* represents a node connected to time point *s* if the visibility criterion

$$x_u < x_s + (x_t - x_s) \frac{s - u}{s - t}$$

holds true for an additional data point x_u placed between them. Applications of visibility graphs were mostly found in context of EEG data [43–45] but also in a cardiologic study dealing with human heart rate variability time series to differentiate between wake/sleep stages [46] and patients of spinal cord injury [47]. A more thorough overview of concepts and algorithms to map time series data into networks can be found in Silva et al. [48].

Alternatively, various distributional similarity approaches were used to evaluate the similarity between two distributions corresponding to a pair of nodes (Jensen-Shannon divergence [49], Kullback-Leibler divergence [50], dynamic time warping [8], generalized measure of association [51]). Zhang et al. [49] employed a kernel-based on the Jensen-Shannon divergence to measure the similarity of multivariate time series, whereas Dong et al. [8] assessed similarity between pairs of time series based on dynamic time warping.

Single measurement per variable per individual The approaches presented so far are only applicable if repeated data points of all variables per individual are available. In the identified studies in which all independent variables were measured only once for an individual, individual-specific network inference was mainly based on quantifying each individual's contribution to the overall group-level structure either by leave-one-out network construction (LOONC) [52, 53] or by a differential perturbation approach [54–59]. Strictly speaking, these two approaches do not involve individual-level parameter inference per se but aim to derive individualspecific networks from group-level networks regardless of the group-level network inference procedure. More precisely, LOONC removes a single individual from group-level network construction and measures the degree of change in all edge weights caused by the removal against the full group-level network. Kuijjer et al. [52] proposed to reversely engineer individualspecific networks by linear interpolation between each edge weight $w_{ij}^{(C_{int})}$ of the group-level network (using all $N_{C_{int}}$ observations in the study cohort of interest C_{int}) and the corresponding edge weight $w_{ij}^{(C_{int} \setminus q)}$ in the network using all observations except an individual of interest q to obtain the edge weight estimate $w_{ii}^{(q)}$ for a single individual by

$$w_{ij}^{(q)} = N\left(w_{ij}^{(C_{int})} - w_{ij}^{(C_{int}\setminus q)}\right) + w_{ij}^{(C_{int}\setminus q)}$$
(2)

where N can be a generic or individual-specific weight but is usually set to $N_{C_{int}}$. In contrast, differential perturbation analysis quantifies the extent to which an edge weight is perturbed by the addition of an individual compared to a reference network constructed independently from the cohort of interest. Edge weights of the individual-specific network G_q for individual q are determined by computing the absolute difference in edge weights between the network computed from the reference population augmented by that individual (augmented network) and the reference network as

$$w_{ij}^{(q)} = w_{ij}^{(C_{ref} \cup q)} - w_{ij}^{(C_{ref})}$$
(3)

where $w_{ij}^{C_{ref}}$ denotes the edge weights in the reference network and $w_{ij}^{(C_{ref} \cup q)}$ in the augmented network.

Neither of the two presented approaches to individualspecific network construction for single measurements of each variable per individual relies on a particular inference method for the group-level networks. Equation (2) and (3) require the edge weights of the estimated grouplevel networks but do not specify how these networks have to be inferred. Perturbation analysis in contrast to LOONC, however, depends on an additional reference network to obtain individual-specific edge weights.

In the study by Zhu et al. [54], a group-level reference network for the differential perturbation analysis was inferred using Pearson correlation coefficients of gene co-expression data of $N_{C_{ref}}$ cancer-free individuals of a reference cohort C_{ref} . An augmented network for an individual with cancer q was constructed by including the expression data of that individual in the reference cohort $(C_{ref} \cup q)$. The approach was also found with networks constructed using partial correlation [57]. In Kuijjer et al. [52], LOONC was implemented using group-level networks derived from Pearson correlation and mutual information, a non-linear measure of association, while Lopes-Ramos et al. [53] used biologically motivated regulatory networks. Note that since both equations quantify the inferred difference in edge weighting, the obtained individual-specific weights can also assume values outside the boundaries of the underlying statistic of the group-level networks. For example, edge weights in the individual-specific networks derived from LOONC or differential perturbation using Pearson correlation can yield values $\langle -1 \text{ and } \rangle 1$ (see Eq. (2–3)). Both approaches were only found in cancer research [57, 59].

Only one of the identified studies using single measurements per variable did not conduct LOONC or perturbation analysis. Xie et al. [39] proposed conditional Gaussian graphical modelling with mean and covariance matrix depending on an individual's covariates while assuming homogeneous network structure across individuals in order to infer individual-specific networks. Hence, differences in edge weights between individuals are covariate-dependent.

Domain-specific techniques In neurological application, certain high-resolution imaging methods for data acquisition generate domain-specific data structures that require a specifically designed methodology of network inference. For instance, tractography detects fibre pathways linking different anatomical brain regions [60–68]. Electroencephalographic (EEG)-based connectivity was predominantly assessed by metrics such as phase lag index, coherence-based similarity, or synchronization likelihood index [69–72]. The interested reader is referred to the references for more details on these applications.

Techniques for network sparsification

Network sparsification removes edges from a network with the intent to optimise the inference of the 'true' system by the omission of "spurious" edges, improve interpretability and enable computational feasibility in construction and further processing of the network. In addition, the structural and topological properties of the network might be improved by removing seemingly spurious connections i.e. edges that are erroneously generated during network inference. Given an undirected network G = (V, E), sparsification yields a subnetwork G' = (V, E') of G with fewer edges such that |E| > |E'|.

More than half of the quantitative studies employed network sparsification (N=74, 54.8%), followed by studies analysing non-sparsified networks (N=58, 43.0%) and 3 studies that considered both approaches (2.2%). As illustrated in Fig. 4B, the most popular strategy was proportional thresholding (N=37) in which a common sparsity threshold (e.g. in terms of density) is defined for all individual-specific networks, and edges are removed sequentially in each network in ascending order of their edge weights until the prespecified sparsity threshold is reached [10, 21, 23-25, 29, 58, 73]. The second most common approach constituted weight-based thresholding (N=31) in which one common weight threshold is defined for all individual-specific networks such that all edge weights within an individual-specific network falling below (or above) the threshold are removed (Fig. 5) [8, 11, 67, 68, 74, 75]. The majority of the weight-based approaches employed binarization of all individual-specific networks (N=21) according to the selected weight threshold τ such that $w'_{ii} = 1$ if $w_{ii} > \tau$ and 0 otherwise [23, 27, 29, 75, 76]. Edges with negative weights were often removed due to their questionable interpretability or the inability to compute some graph-theoretical features from them (e.g. clustering coefficient or characteristic path length), omitting potentially meaningful inverse relation between nodes. In N=6 studies, a sparse representation of a partial correlation-based network was achieved individually by including an L_q -norm ($q \in \{1, 2\}$) regularization penalty to the network inference process in order to reinforce strong connections across individuals and drive weak connections towards zero [36, 37, 39, 77, 78]. Due to the individually imposed regularization, inter-subject variability might then be inherently induced according to Wee et al. [36]. Hence, they imposed an additional group constraint to encourage a common network topology across the study cohort. Other studies selected a fixed penalty term for all individual networks which is why this approach can also be seen as a special case of weight-based thresholding [34, 37]. Group-level edge elimination for each individual-specific network was carried out by univariate testing of the edge weights (N=17), either by permutation testing to control the probability of including spurious connections at 0.05 or by only including edges with weights significantly different from zero [13, 15–19, 79–81]. Then all those edges that were characterized as spurious at the group level were removed from all individual-specific networks.

The implemented strategy of network sparsification across studies varied substantially in terms of: the sparsification method, the number or combination of investigated methods, the selected sparsification threshold(s) and the reasoning behind the chosen strategy. It was not uncommon for studies to combine several sparsification strategies [12, 21, 22, 24] or to examine several strategies separately [33, 34, 37]. Further, all of the identified approaches to network sparsification were dependent on the careful selection of a thresholding parameter by the researcher. To circumvent the arbitrariness associated with the selection of a single threshold, the majority of studies employed multiple thresholding, meaning that a range of cut-off values with small incremental steps was examined such that a series of networks $\mathcal{G}_s := \{G_{s,\tau_k}\}_{k=1,\dots,T}$ for each individual s ($s = 1, \dots, N$) was obtained with T thresholds τ_k where k = 1, ..., T [65, 73, 76, 82]. For an illustrated example of multiple thresholding, see Fig. 6. Only one study performed weight-based thresholding with a single, arbitrary threshold [83].

In general, there was considerable heterogeneity in the selection of the optimal threshold value for sparsification in the studies evaluated:(1) a threshold yielding a small-world index (see Table 1 for definition) above 1 of the networks was chosen [65, 84], (2) an arbitrary fixed





threshold was chosen [39], (3) the differently sparsified networks corresponding to a single individual G_s were fused into an average individual-specific network [25], (4) the numerical integral or average of the graph-theoretical feature over the range of network G_s was computed [25, 56, 64, 65, 76], (5) a threshold generating the best results in terms of classification accuracy or association with the outcome was selected [8, 29, 34, 51], and (6) further processing was done including varying network sparsity levels [24, 75, 85].

According to the identified studies conducting network sparsification, the choice of the threshold is crucial to balance between noise removal (spurious edges) and preservation of 'true' edges. For instance, proportional thresholding may leave edges with very low edge weights assumed spurious, whereas weight-based thresholding yields different densities across the individual-specific networks which then may affect other graph-theoretical features and in turn, hinder comparability across networks. While the evaluated studies often adequately addressed the selection of the threshold parameter weight-based and proportional thresholding, 'hidden' threshold parameters in regularized network inference (i.e. penalty strength) or univariate testing (i.e. significance level) were rarely further investigated.

Graph-theoretical feature extraction

Appropriate features describing the network after its construction reduce the dimensionality of the network, capture aspects of the graph structure and may constitute valuable biomarkers for clinical outcomes in applied health research. The connectivity information within a network can be characterized on different scales: globally or locally. While global features capture properties of the whole network, local features describe their characteristics in defined subareas such as nodes, edges or modules (i.e. clusters of nodes).

The majority of quantitative studies extracted both, local and global graph-theoretical features (N=56, 41.5%), followed by studies only focusing on local features (N=44, 32.6%) and studies interested only in global graph-theoretical features (N=35, 26.0%). The average number of computed global graph-theoretical features describing different aspects of the network across all studies was 3.19 with a standard deviation (SD) of 4.69 and a range of 0 to 44, while the average number of local features was comparatively small with a mean of 1.62 and a SD of 1.72 and a range of 0 to 10. The most frequently examined graphtheoretical features were the clustering coefficient (CC) (N=84, 62.2%) [86] quantifying the tendency of clustering within the network and the characteristic path length

(CPL) (N=61, 45.2%) defined as the *average* of all shortest paths over all pairs of nodes in a network. A total of 57 different graph-theoretical features were identified. The most commonly used metrics (examined in more than 10 studies) are briefly explained in Table 1. More detailed descriptions are available elsewhere [87]. In some studies, graph-theoretical features were normalized by dividing them by the same metric computed from a randomly generated network of identical size, density and/or degree distribution to account for differences in network size and density, introducing additional computational complexity. Largely, studies (N=31, 23.8%) examined the normalized clustering coefficient and characteristic path length obtained by dividing the CC and CPL by the CC and CPL of multiple randomly generated networks [18, 20, 79, 81, 84, 88]. For instance, Imms et al. [89] highlighted the use of normalized CC and CPL as diagnostic biomarkers to differentiate between controls and patients with traumatic brain injury.

Feature selection and prediction modelling

Around a third of the 135 quantitative studies (N=46, 34.1%) conducted implicit techniques for prediction i.e. elementary statistical analytics (e.g. hypothesis testing, correlation analysis) to identify potential biomarkers associated with the outcome [8, 59, 84, 90] while the remaining studies (N=89, 65.9%) conducted prediction modelling using explicit techniques i.e. methods with the possibility of predicting for an unseen individual. Among the latter, about two thirds aimed at the supervised identification of disease subgroups using graph-theoretical features as independent variables (N = 57, 64.0%) and one third prognosticated a clinical outcome (N=32, 36.0%). Despite the similarity of the methodological frameworks, the evaluated studies turned out to be very heterogeneous regarding feature selection, sample size, outcome types, the outcome modelling technique and the validation analytics employed.

Feature selection Feature selection approaches identified in the studies used to define an optimal subset of features can be classified into filter methods (e.g. univariable testing, Pearson correlation) and wrapper methods (iterative optimization of a classification algorithm) but hybrid approaches were also proposed [83]. The majority of studies used filter methods to remove features before training a classifier or a regression model [20, 21, 91]. Wrapper methods (e.g. support vector machine (SVM) with recursive feature elimination (RFE), repeated selection across leave-one-out cross-validation (LOOCV) runs) either iteratively reduced the features based on a ranking score (e.g. feature importance) of the feature in the prediction algorithm to optimize classification accuracy [25, 63] or selected features with the most discriminative ability out of the full set of features based on repeated least absolute shrinkage and selection operator (LASSO) feature selection across LOOCV runs [77].

Prediction modelling The median sample size in neurology was 68 (interquartile range (IQR) 41 to 127), in genomics 445 (IQR: 333-761), and in pathopsychology 62 (IQR: 41-97) as illustrated in Fig. 7A. In pathology, only one study with a sample size of 70 was identified and two studies in cardiology with a sample size of 55 and 389 individuals, respectively. The most commonly investigated types of dependent variables across all 135 guantitative studies were binary (N = 86, 63.7%), followed by continuous (N = 37, 27.4%), categorical (N = 14, 10.4%) and lastly, time-to-event (N = 4, 3.0%) with some studies assessing multiple outcome types (N=6, 4.4%). The considered statistical modelling techniques employed for the task of prediction varied accordingly. Hence, for the sake of clarity, we will distinguish between data modelling and algorithmic modelling approaches according to Breiman [92] (Table 2). The former group contains modelling techniques that connect covariates to the outcome variable by a stochastic model (e.g. linear or logistic regression), while approaches belonging to the latter group use an algorithm to predict the outcome from the covariates (e.g. SVM, random forest). For a complete list of the grouping of the identified methods, we refer to the supplementary material. In general, SVMs were the most popular approach (N=40, 45.0%) [27], followed by linear regression (N=25, 28.0%) [19, 22, 28, 64, 67, 81, 93, 94], random forests (N=12, 13.5%) [15, 41, 58, 72, 95, 96] and logistic regression (*N*=9, 10.1%) [41, 61, 65, 97, 98].

The majority of quantitative studies built discriminative classifiers for discrete outcome labels mainly using only local graph-theoretical features (see Table 2 and Fig. 7B). The most common approach extracted local graph-theoretical features with filter-based feature selection and then trained a linear SVM for outcome classification [16, 30, 37, 62, 77, 83]. A popular choice for feature selection before SVM training and classification was univariable feature screening of statistical significance [10, 13, 14, 34, 36, 74, 78]. However, this method is known to suffer from conceptual shortcomings [99]. In the case of multiple thresholding [74], the use of multiple data modalities [14] or the extraction of multiple local features [32, 100] for classification, a supervised multiple-kernel learning approach was adopted to fuse layers of features to predict disease subgroups. A subset of studies even trained multiple classifiers for the binary classification of the presence of disease (e.g. SVM, k-nearest neighbour, decision tree, random forests, Naïve Bayes, Adaptive Boosting)



Table 2 Types of prediction modelling approach identified inthe 89 studies conducting advanced statistical procedures basedon graph-theoretical features

	Algorithmic modelling	Data modelling
Total	56	46
Sample size	137.75 (171.46)	168.54 (232.62)
Graph-theoretical scale		
Global	9	23
Local	45	20
Both	2	4
Outcome		
Continuous	5	21
Binary	46	20
Categorical	5	3
Time-to-event	0	2

*Continuous variables stated as mean (standard deviation, SD). Categorical variables represent the number of approaches identified in the studies

[11, 26, 35, 69, 96, 101]. For instance, [26] stated to have built 67 classifiers to differentiate between children with autism spectrum disorder and age-matched controls and 23 advanced regression models for phenotypic prediction.

In terms of model validation, nearly all diagnostic studies reported model discrimination and performance of the classifier in terms of cross-validated accuracy, sensitivity, specificity and the area under the receiver operating characteristic curve (AUC) [12, 23, 25, 27, 70, 77]. Some studies reported estimated predictive accuracy solely utilizing correlation between the predicted and the true values [93, 96]. In a few studies, performance was claimed to exceed previous approaches, but such a claim was often unsubstantiated and solely based on the comparison between their overall accuracy or AUC and that of the existing studies without consideration of other study factors (study design, set of variables, sample size, heterogeneity between study cohorts) [26, 102, 103]. Imbalanced distribution of class labels was stated as an issue for training accurate classifiers but was accounted for in some studies by assessing the balanced accuracy (i.e. the arithmetic mean of sensitivity and specificity) [58, 70, 74, 100]. Further, calibration analysis as a reliability assessment of the predicted probability of the event actually occurring with the observed relative frequency by the means of a calibration curve was rarely reported in any of the evaluated studies.

Regression-based modelling was mainly performed by linear regression (N=28, 60.7%), followed by logistic regression (N=8, 17.4%), Cox proportional hazards regression (N=2, 4.3%) and mixed-effects modelling (N=2, 4.3%). In case global graph-theoretical features were extracted from each individual-specific network or a continuous outcome type was of interest, regressionbased analytics were the preferred course of action (see Table 2). The majority of the studies used only graphtheoretical features as independent variables and rarely adjusted for clinical characteristics (e.g. in [15, 18, 21, 22, 67, 73, 80, 97]). Even fewer studies adjusted for network size and density within the regression model to account for their inter-subject differences affecting the extracted graph-theoretical features [79, 81]. Model adjustment by clinical information was more common in studies

investigating the association of global graph-theoretical features with an outcome of interest rather than studies interested in local features. Batalle et al. [61] stated that the graph-theoretical features included in addition to the clinical-epidemiological covariates even proved to yield a higher contribution in terms of statistical significance after separate (blockwise) stepwise backward elimination of variables. However, clinical variables were not only used to adjust the model. For example, Xie et al. [39] proposed a two-stage approach consisting of first, deriving individual-specific network models from conditional Gaussian graphical models dependent on an individual's clinical features and second, the clinical outcome model to estimate the graph-theoretical parameters' effects on an outcome of interest adjusted by the same clinical features.

The sample size of studies conducting regression-based methods was slightly higher and showed a significantly greater variance in comparison with the sample size studies employing classification-based methods (Table 2). Furthermore, possible overfitting of predictive data modelling was rarely directly addressed as in the study by Batalle et al. [61] who reduced preselected graph-theoretical features into a single summary index or in Anderson et al. [98] who restricted the variables which entered the model to 4 to have at least 5 events per variables [104].

Only three of the 130 quantitative studies conducted Cox proportional hazards model to model a time-to-event outcome [66, 77, 79]. Tuladhar et al. [66] identified global efficiency instead of conventional MRI biomarkers as a predictor of all-cause dementia with lower global efficiency associated with a higher risk of dementia onset while adjusting for a set of clinical features. Similarly, Liu et al. [77] stated that none of the traditional clinical features was consistently selected in the majority of the LOOCV runs for overall survival time of high-grade glioma patients and out of the three most important selected features, two were graph-theoretical features.

Discussion

In this scoping review, we identified the state-of-theart statistical methodology currently employed when using individual-specific networks for prediction in medicine and applied health research. We found a wide range of applications and methodological concepts in our review. We collated the key concepts identified across the 148 included studies considering three main aspects of modelling with individual-specific networks: (1) individual-specific network inference, (2) extraction of graph-theoretical features, and (3) prediction modelling. Within each of these aspects, there is considerable methodological heterogeneity in the implementation, use, areas of application, and reporting. However, all approaches outlined in this work are in principle generalizable to any field of research and may be suitable to answer various prognostic or diagnostic research questions in medicine.

Individual-specific networks were frequently constructed by evaluating correlations between repeated measurements of pairs of variables (e.g. time-series data of two brain regions). Here we identified two main approaches based on bivariate and partial correlation analysis, some variants thereof, and some further approaches that were often tied to the process of data acquisition itself. Furthermore, the recently proposed visibility graphs offer a flexible approach to individualspecific network inference in relation to time series data. However, sometimes several time series are available per individual so that the individual-specific network is ambiguous, which leads to a further layer of complexity. In the absence of repeated measurements per variable, two novel and promising approaches were LOONC and differential perturbation. Despite their flexibility and ease of application to continuous independent variables, a big challenge in the latter two approaches remains the considerable computational burden, in particular in high-dimensional data settings, due to the repeated computation of the augmented network for each individual [57].

In the pursuit to separate 'real' from 'spurious' connections, in addition to the need for a reduced computational burden, network sparsification has become an important aspect of network analysis. However, sparsification not only depends on the selected technique but, more importantly, also on the chosen threshold, and hence, often multiple thresholds were employed to reduce the impact of a possibly flawed choice, yielding a sequence of networks per individual with varying edge weights. Various approaches were then applied to deal with the sequence of networks; numerical integration or averaging were the most popular approaches together with a threshold selection yielding the best AUROC. Although the majority of studies refrained from using a single, arbitrary threshold value, multiple edge weighting schemes and sparsification strategies were seldom guided by model fit. In addition, sensitivity analyses evaluating the impact of threshold choice on predictive performance were expected but hardly found.

For the extraction of graph-theoretical features, we found a set of global and local features (e.g. see Table 2) that were used in many studies across research fields. For the most part, the clustering coefficient, the characteristic path length and the edge weights were examined in the search for potential biomarkers of the outcome of interest. Furthermore, the extraction of graph-theoretical features did not follow a deliberate process but often consisted of a greedy collection of network characteristics i.e. the computation and outcome-associated investigation of as many graph-theoretical variables as possible.

Despite the multiplicity of identified methodological approaches for individual-specific network inference across fields of application, the number of studies that proposed models actually intended to provide clinical outcome prediction for future individuals was quite limited, and most models were estimated to provide a proof-of-concept that graph-theoretical features may in principle be useful for outcome prediction. The lack of deployable clinical prediction models could be either a consequence of the fundamental challenges in network inference methods shared by all areas of application, in particular concerning the lack of a gold standard for network construction and sparsification, or of the general unawareness in how individual-specific networks can be exploited for prediction.

Through the systematic collation of the identified analytical approaches, we found some areas interesting for future research and which may help to reduce some of the arbitrariness of some analytical choices.

First, more research is needed to reduce the computational burden related to the construction and analysis of relatively large and dense networks and the inherent computational complexity of graph metric computation. Large omics studies generate substantial amounts of data which can lead to major computational difficulties in network inference and further analysis, if each node in the network represents a single variable. In particular, LOONC and differential perturbation approaches would suffer in such a data setting due to the computational burden caused by the repeated network computation for each individual in the study cohort. One possible strategy for reducing network complexity and facilitating network analysis and feature extraction could be node aggregation over groups of connected, non-independent nodes (modules). In this sense, variables could be combined as modules either through unsupervised clustering algorithms or through biological background knowledge, so that each node represents a group of independent variables and no longer a single variable.

Second, network sparsification and multivariable model estimation could be linked more closely by guiding the search for a suitable threshold or the integration over several thresholds by the model fit. Multiple thresholding yields a set of sequential graph-theoretical estimates of the networks that are computed over a fine grid on a continuous domain using incremental steps between threshold values (e.g. grid searching). Ideas from functional data analysis could be transferred to the area of modelling with individual-specific networks. Briefly, instead of choosing a threshold that provides univariably optimal prediction performance, or integration over multiple pre-specified thresholds with equal weights of each threshold, one could interpret the individual-specific sequence of graph-theoretical features corresponding to the set of sparsified networks $\mathcal{G}_s := \left\{ G_{s, au_k}
ight\}_{k=1, ..., \mathrm{T}}$ as a functional data predictor. Then, one may define a flexible weighting function of τ_k , $f(\tau_k)$, through outcome-guided calibration to optimize clinical prediction. Consequently, such an analysis would also yield an estimate of the relative importance of different thresholds for network sparsification. Alternatively, carefully conducted sensitivity analyses would allow evaluating to what extent the reported results depended on the choice of the selected threshold value in particular for studies continuing the search for the optimal threshold parameter by univariate analysis.

Further, the comparison of networks of varying sizes and edge densities can impose issues for prediction modelling since some graph-theoretical features are confounded by them [80]. The inclusion of these two features regardless of 'significance' may reduce the magnitude of bias, and improve prediction performance and explainability of such models [105]. Omission of these confounding variables could mask the actual effects of interest in model explanation. Generally, graph-theoretic features are inherently associated with each other, and more research is needed to better understand these associations.

In contrast, a reoccurring problem of multivariable model building was found in the evaluated studies: "univariable prefiltering" of variables in which only variables with a statistically significant association with the outcome are included in the model [106, 107]. However, a *p*-value above the statistical significance threshold of 5% is not sufficient evidence for the lack of an effect of the independent variable [108]. The popularity of prefiltering across the evaluated studies can presumably be traced back to the greedy collection of graph-theoretical features or to a disproportional number of local graph features that were obtained relative to sample size. Since the actual goal of univariable preselection was often a considerable reduction of the number of independent variables proportional to the sample size to seemingly avoid overfit, defining a minimum basic set of features (MBSF) to investigate may be beneficial when network analysis is employed for prediction. The identification of such an MBSF, however, is not an easy task and may require investigations across a range of applications embedded in the respective research fields.

Lastly, future studies should investigate the added benefit of graph-theoretical features in addition to clinical variables so as not to examine their clinical utility separately from traditional variables and hence, improve existing clinical prediction models. We have seen that graph-theoretical variables were mostly examined independently, which was partly due to the relatively low samples across the evaluated studies but also due to the dominant preference of algorithmic classification approaches with local graph-theoretical features, where clinical information was largely ignored. In some studies, in which graph-theoretical features were examined together with clinical variables, these even turned out to be stronger predictors than the traditional set of clinical variables. It remains elusive if this could be explained by publication bias or demonstrates the clinical relevance of graph-theoretical features.

Research on the aforementioned points is essential to establish a state-of-the-art and to provide more evidence-based guidance in using individual-specific networks for the prediction of clinical outcomes to applied researchers. Despite the identified aspects for future research, our scoping review is subject to some limitations. First, we may have missed some relevant applications due to the lack of standardized terminology to describe the intersection of network analysis (in particular approaches to construct individual-specific networks) and prediction modelling but also because of the ambiguity of the term 'network'. Secondly, by limiting our study to applications in medicine and health research, we may not have captured studies that employed individual-specific networks in which the individuals do not represent patients but other individual entities. Thirdly, since the screening of 4988 studies and extracting data for the 148 articles included in this review was laborious, some time passed between identification of studies and completion of data extraction. Nevertheless, we decided not to update our search to include more recent articles (i.e. published from August 2020 onwards) because we do not believe that there were substantial changes in practice in the intervening time. Last but not least, this review focused on the use of individual-specific network analysis for prediction which is why existing refinements of the presented methods for network construction and extraction of graph-theoretic ones might not have passed the inclusion criteria of our search strategy.

At this juncture, it is important to emphasize that we have not assessed the quality of included studies and did not perform a risk of bias assessment. This was done in agreement with the general guidelines on conducting a scoping review. Consequently, our review is unable to make definitive recommendations for practice but rather describes the current methodological practice and possible areas of future research [7, 109].

Conclusion

Network analysis offers a flexible tool for personalized medicine, hence prediction with individual-specific networks is an emerging field full of potential for future research. The application in clinical research is still in its infancy but our findings can strengthen the methodological conduct to incorporate individual-specific network analysis in predictive tasks. The framework still requires further refinement, and research must cover statistical, computational and application-specific aspects. In addition to methodologies are needed to understand how methods compare and which method works best in a specific setting. This may eventually lead to establishing a state-of-the-art in this novel and fascinating scientific arena located at the cross-section of statistics, computer science and medicine.

Abbreviations

AUC: Area under the curve; A: Assortativity; BC: Betweenness centrality; BOLD: Blood oxygenation level-dependent; CC: Clustering coefficient; CPL: Characteristic path length; DAG: Directed acyclic graph;; Dg: Degree; Ds: Density; EEG: Electroencephalography; EW: Edge weight; GE: Global efficiency; HRV: Heart rate variability; IQR: Interquartile range; LASSO: Least absolute shrinkage and selection operator; LE: Local efficiency; LOONC: Leave-one-out network construction; LOOCV: Leave-one-out cross-validation; M: Modularity; MBSF: Minimum basic set of features; RFE: Recursive feature elimination; SD: Standard deviation; SVM: Support vector machine; SWI: Small world index; ROI: Region of interest; VAR: Vector autoregressive.

Supplementary Information

The online version contains supplementary material available at https://doi. org/10.1186/s12874-022-01544-6.

Additional file 1. Preferred Reporting Items for Systematic reviews and Meta-Analyses extension for Scoping Reviews (PRISMA-ScR) Checklist

Additional file 2: Supplementary Material S1. Detailed Methods. Table S1. Keyword sets used in the search strategy across the databases for article extraction. Figure S1. Year of publication of the identified studies. Table S2. Scale of the graph-theoretical features used as candidate predictors stratified by the area of application.

Additional file 3. Supplementary Material S2. Questionnaire for fulltext screening

Acknowledgements

KVS and FM acknowledge the European Union's Horizon 2020 research and innovation programme under grant agreement No 860895 (TranSYS-h2020transys.eu). KVS also acknowledges the European Union's Horizon 2020 research and innovation programme under the Marie Sklodowska-Curie grant agreement No 813533 (MLFPM-mlfpm.eu).

Authors' contributions

MG was responsible for the conception, design of the study, search, screening, inclusion of relevant articles, data extraction of eligible studies and wrote the initial draft of the manuscript. GH was responsible for the conception, design and carried out the screening and data extraction of a fraction of articles. FM and MS conducted screening and data extraction of a fraction of articles. GH, KVS and SM revised the draft critically for important intellectual content. All authors agreed to the final submission.

Funding

This project has received funding from the European Union's Horizon 2020 research and innovation programme under the Marie Skłodowska-Curie grant agreement No 860895 (FM, KVS).

Availability of data and materials

Not applicable.

Declarations

Ethics approval and consent to participate Not applicable.

Consent for publication

Not applicable.

Competing interests

All authors declare that they have no competing interests.

Author details

¹Section for Clinical Biometrics, Center for Medical Statistics, Informatics and Intelligent Systems, Medical University of Vienna, Vienna, Austria. ²Division of Nephrology and Dialysis, Department of Internal Medicine III, Medical University of Vienna, Vienna, Austria. ³BIO3 Laboratory for Systems Medicine, Department of Human Genetics, KU Leuven, Leuven, Belgium. ⁴Service de Biostatistique et d'Epidémiologie, Gustave Roussy, Oncostat U1018, Inserm, University Paris-Saclay, labeled Ligue Contre le Cancer, Villejuif, France. ⁵BIO3 Laboratory for Systems Genetics, GIGA-R Medical Genomics, University of Liège, Liège, Belgium.

Received: 27 July 2021 Accepted: 11 February 2022 Published online: 06 March 2022

References

- 1. Hastie T, Tibshirani R, Friedman J. The elements of statistical learning. New York: Springer Series in Statistics; 2001.
- Van Calster B, van Smeden M, De Cock B, Steyerberg EW. Regression shrinkage methods for clinical prediction models do not guarantee improved performance: simulation study. Stat Methods Med Res. 2020;29(11):3166–78.
- Šinkovec H, Heinze G, Blagus R, Geroldinger A. To tune or not to tune, a case study of ridge logistic regression in small or sparse datasets. BMC Med Res Methodol. 2021;21(1):199.
- Barabási A-L, Gulbahce N, Loscalzo J. Network medicine: a networkbased approach to human disease. Nat Rev Genet. 2011;12(1):56–68.
- Li MM, Huang K, Zitnik M. Graph Representation Learning in Biomedicine. arXiv. 2021;210404883.v2. https://arxiv.org/abs/2104.04883. Accessed 10 Nov 2021.
- Peters MD, Marnie C, Tricco AC, Pollock D, Munn Z, Alexander L, et al. Updated methodological guidance for the conduct of scoping reviews. JBI Evid Synth. 2020;18(10):2119–26.
- Tricco AC, Lillie E, Zarin W, O'Brien KK, Colquhoun H, Levac D, et al. PRISMA extension for scoping reviews (PRISMA-ScR): checklist and explanation. Ann Intern Med. 2018;169(7):467–73.
- Dong Z, Li X, Chen W. Frequency network analysis of heart rate variability for obstructive apnea patient detection. IEEE J Biomed Health Inform. 2017;22(6):1895–905.
- Sáez A, Rivas E, Montero-Sánchez A, Paradas C, Acha B, Pascual A, et al. Quantifiable diagnosis of muscular dystrophies and neurogenic atrophies through network analysis. BMC Med. 2013;11(1):1–11.
- Bian J, Xie M, Topaloglu U, Cisler JM. A Probabilistic Model of Functional Brain Connectivity Network for Discovering Novel Biomarkers. AMIA Summ Transl Sci Proc. 2013;2013:21.
- Saghayi M, Greenberg J, O'Grady C, Varno F, Hashmi MA, Bracken B, et al. Brain network topology predicts participant adherence to mental training programs. Netw Neurosci. 2020;4(3):528–55.
- 12. Xu X, Li W, Mei J, Tao M, Wang X, Zhao Q, et al. Feature selection and combination of information in the functional brain connectome for

discrimination of mild cognitive impairment and analyses of altered brain patterns. Front Aging Neurosci. 2020;12:28.

- Khazaee A, Ebrahimzadeh A, Babajani-Feremi A. Identifying patients with Alzheimer's disease using resting-state fMRI and graph theory. Clin Neurophysiol. 2015;126(11):2132–41.
- Wee C-Y, Yap P-T, Zhang D, Denny K, Browndyke JN, Potter GG, et al. Identification of MCI individuals using structural and functional connectivity networks. NeuroImage. 2012;59(3):2045–56.
- Paldino MJ, Zhang W, Chu ZD, Golriz F. Metrics of brain network architecture capture the impact of disease in children with epilepsy. NeuroImage: Clin. 2017;13:201–8.
- Li Y, Wang Y, Wu G, Shi F, Zhou L, Lin W, et al. Discriminant analysis of longitudinal cortical thickness changes in Alzheimer's disease using dynamic and network features. Neurobiol Aging. 2012;33(2):427 e15-. e30.
- 17. Paldino MJ, Golriz F, Zhang W, Chu ZD. Normalization enhances brain network features that predict individual intelligence in children with epilepsy. PLoS One. 2019;14(3):e0212901.
- Rimkus CM, Schoonheim MM, Steenwijk MD, Vrenken H, Eijlers AJ, Killestein J, et al. Gray matter networks and cognitive impairment in multiple sclerosis. Mult Scler J. 2019;25(3):382–91.
- Finn ES, Shen X, Scheinost D, Rosenberg MD, Huang J, Chun MM, et al. Functional connectome fingerprinting: identifying individuals using patterns of brain connectivity. Nat Neurosci. 2015;18(11):1664–71.
- van Duinkerken E, Ijzerman RG, Klein M, Moll AC, Snoek FJ, Scheltens P, et al. Disrupted subject-specific gray matter network properties and cognitive dysfunction in type 1 diabetes patients with and without proliferative retinopathy. Hum Brain Mapp. 2016;37(3):1194–208.
- De Baene W, Rutten GJM, Sitskoorn MM. Cognitive functioning in glioma patients is related to functional connectivity measures of the non-tumoural hemisphere. Eur J Neurosci. 2019;50(12):3921–33.
- 22. Wang Z, Zhang D, Liang B, Chang S, Pan J, Huang R, et al. Prediction of biological motion perception performance from intrinsic brain network regional efficiency. Front Hum Neurosci. 2016;10:552.
- Sen B, Bernstein GA, Mueller BA, Cullen KR, Parhi KK. Sub-graph entropy based network approaches for classifying adolescent obsessive-compulsive disorder from resting-state functional MRI. NeuroImage: Clin. 2020;26:102208.
- 24. Cheng H, Newman S, Goñi J, Kent JS, Howell J, Bolbecker A, et al. Nodal centrality of functional network in the differentiation of schizophrenia. Schizophr Res. 2015;168(1–2):345–52.
- Wen H, Liu Y, Rekik I, Wang S, Chen Z, Zhang J, et al. Combining disrupted and discriminative topological properties of functional connectivity networks as neuroimaging biomarkers for accurate diagnosis of early tourette syndrome children. Mol Neurobiol. 2018;55(4):3251–69.
- Zhou Y, Yu F, Duong T. Multiparametric MRI characterization and prediction in autism spectrum disorder using graph theory and machine learning. PLoS One. 2014;9(6):e90405.
- Hojjati SH, Ebrahimzadeh A, Babajani-Feremi A. Identification of the early stage of Alzheimer's disease using structural MRI and resting-state fMRI. Front Neurol. 2019;10:904.
- Yamashita M, Kawato M, Imamizu H. Predicting learning plateau of working memory from whole-brain intrinsic network connectivity patterns. Sci Rep. 2015;5(1):1–8.
- 29. Zhang T, Zhao Z, Zhang C, Zhang J, Jin Z, Li L. Classification of early and late mild cognitive impairment using functional brain network of resting-state fMRI. Front Psych. 2019;10:572.
- Zhou L, Wang Y, Li Y, Yap P-T, Shen D. Initiative AsDN. Hierarchical anatomical brain networks for MCI prediction: revisiting volumetric measures. PLoS One. 2011;6(7):e21935.
- Richiardi J, Achard S, Bunke H, Van De Ville D. Machine learning with brain graphs: predictive modeling approaches for functional imaging in systems neuroscience. IEEE Signal Process Mag. 2013;30(3):58–70.
- Zhang Y, Zhang H, Chen X, Lee S-W, Shen D. Hybrid high-order functional connectivity networks using resting-state functional MRI for mild cognitive impairment diagnosis. Sci Rep. 2017;7(1):1–15.
- Damaraju E, Allen EA, Belger A, Ford JM, McEwen S, Mathalon D, et al. Dynamic functional connectivity analysis reveals transient states of dysconnectivity in schizophrenia. NeuroImage: Clin. 2014;5:298–308.

- Qiao L, Zhang H, Kim M, Teng S, Zhang L, Shen D. Estimating functional brain networks by incorporating a modularity prior. NeuroImage. 2016;141:399–407.
- 35. Cecchi GA, Rish I, Thyreau B, Thirion B, Plaze M, Paillere-Martinot M-L, et al. Discriminative Network Models of SchizophreniaNIPS; 2009.
- Wee C-Y, Yap P-T, Zhang D, Wang L, Shen D. Group-constrained sparse fMRI connectivity modeling for mild cognitive impairment identification. Brain Struct Funct. 2014;219(2):641–56.
- Bohland JW, Saperstein S, Pereira F, Rapin J, Grady L. Network, anatomical, and non-imaging measures for the prediction of ADHD diagnosis in individual subjects. Front Syst Neurosci. 2012;6:78.
- Lord L-D, Allen P, Expert P, Howes O, Broome M, Lambiotte R, et al. Functional brain networks before the onset of psychosis: a prospective fMRI study with graph theoretical analysis. NeuroImage: Clin. 2012;1(1):91–8.
- Xie S, Li X, McColgan P, Scahill RI, Zeng D, Wang Y. Identifying diseaseassociated biomarker network features through conditional graphical model. Biometrics. 2020;76(3):995–1006.
- Booij SH, Wichers M, De Jonge P, Sytema S, Van Os J, Wunderink L, et al. Study protocol for a prospective cohort study examining the predictive potential of dynamic symptom networks for the onset and progression of psychosis: the Mapping Individual Routes of Risk and Resilience (Mirorr) study. BMJ Open. 2018;8(1):e019059.
- Lutz W, Schwartz B, Hofmann SG, Fisher AJ, Husen K, Rubel JA. Using network analysis for the prediction of treatment dropout in patients with mood and anxiety disorders: A methodological proof-of-concept study. Sci Rep. 2018;8(1):1–9.
- Lacasa L, Luque B, Ballesteros F, Luque J, Nuno JC. From time series to complex networks: The visibility graph. Proc Natl Acad Sci. 2008;105(13):4972–5.
- Ahmadlou M, Adeli H, Adeli A. New diagnostic EEG markers of the Alzheimer's disease using visibility graph. J Neural Transm. 2010;117(9):1099–109.
- Bajestani GS, Behrooz M, Khani AG, Nouri-Baygi M, Mollaei A. Diagnosis of autism spectrum disorder based on complex network features. Comput Methods Prog Biomed. 2019;177:277–83.
- Grobelny BT, London D, Hill TC, North E, Dugan P, Doyle WK. Betweenness centrality of intracranial electroencephalography networks and surgical epilepsy outcome. Clin Neurophysiol. 2018;129(9):1804–12.
- Hou F, Li F, Wang J, Yan F. Visibility graph analysis of very shortterm heart rate variability during sleep. Phys A Stat Mech Appl. 2016;458:140–5.
- Chen S, Gallagher MJ, Hogg F, Papadopoulos MC, Saadoun S. Visibility graph analysis of intraspinal pressure signal predicts functional outcome in spinal cord injured patients. J Neurotrauma. 2018;35(24):2947–56.
- Silva VF, Silva ME, Ribeiro P, Silva F. Time series analysis via network science: Concepts and algorithms. Wiley Interdiscip Rev Data Min Knowl Discov. 2021;11(3):e1404.
- Zhang Z, Ding J, Xu J, Tang J, Guo F. Multi-scale Time-series Kernelbased Learning Method for Brain Disease Diagnosis. IEEE J Biomed Health Inform. 2021;25(1):209–17.
- Homan P, Argyelan M, DeRosse P, Szeszko PR, Gallego JA, Hanna L, et al. Structural similarity networks predict clinical outcome in early-phase psychosis. Neuropsychopharmacology. 2019;44(5):915–22.
- Philips GR, Daly JJ, Príncipe JC. Topographical measures of functional connectivity as biomarkers for post-stroke motor recovery. J Neuroeng Rehabil. 2017;14(1):1–16.
- 52. Kuijjer ML, Tung MG, Yuan G, Quackenbush J, Glass K. Estimating sample-specific regulatory networks. lscience. 2019;14:226–40.
- Lopes-Ramos CM, Kuijjer ML, Ogino S, Fuchs CS, DeMeo DL, Glass K, et al. Gene regulatory network analysis identifies sex-linked differences in colon cancer drug metabolism. Cancer Res. 2018;78(19):5538–47.
- 54. Zhu K, Pian C, Xiang Q, Liu X, Chen Y. Personalized analysis of breast cancer using sample-specific networks. PeerJ. 2020;8:e9161.
- Liu X, Wang Y, Ji H, Aihara K, Chen L. Personalized characterization of diseases using sample-specific networks. Nucleic Acids Res. 2016;44(22):e164-e.
- Audrain S, Barnett AJ, McAndrews MP. Language network measures at rest indicate individual differences in naming decline after anterior temporal lobe resection. Hum Brain Mapp. 2018;39(11):4404–19.

- Huang Y, Chang X, Zhang Y, Chen L, Liu X. Disease characterization using a partial correlation-based sample-specific network. Brief Bioinform. 2021;22(3):bbaa062.
- Das T, Borgwardt S, Hauke DJ, Harrisberger F, Lang UE, Riecher-Rössler A, et al. Disorganized gyrification network properties during the transition to psychosis. JAMA Psychiatry. 2018;75(6):613–22.
- 59. Park B, Lee W, Park I, Han K. Finding prognostic gene pairs for cancer from patient-specific gene networks. BMC Med Genet. 2019;12(8):1–14.
- Boot EM, van Leijsen EM, Bergkamp MI, Kessels RP, Norris DG, de Leeuw F-E, et al. Structural network efficiency predicts cognitive decline in cerebral small vessel disease. NeuroImage: Clin. 2020;27:102325.
- Batalle D, Eixarch E, Figueras F, Muñoz-Moreno E, Bargallo N, Illa M, et al. Altered small-world topology of structural brain networks in infants with intrauterine growth restriction and its association with later neurodevelopmental outcome. NeuroImage. 2012;60(2):1352–66.
- 62. Sun Y, Bi Q, Wang X, Hu X, Li H, Li X, et al. Prediction of conversion from amnestic mild cognitive impairment to Alzheimer's disease based on the brain structural connectome. Front Neurol. 2019;9:1178.
- 63. Wee C-Y, Yap P-T, Li W, Denny K, Browndyke JN, Potter GG, et al. Enriched white matter connectivity networks for accurate identification of MCI patients. NeuroImage. 2011;54(3):1812–22.
- Welton T, Constantinescu CS, Auer DP, Dineen RA. Graph theoretic analysis of brain Connectomics in multiple sclerosis: Reliability and relationship with cognition. Brain Connectivity. 2020;10(2):95–104.
- 65. Du J, Wang Y, Zhi N, Geng J, Cao W, Yu L, et al. Structural brain network measures are superior to vascular burden scores in predicting early cognitive impairment in post stroke patients with small vessel disease. NeuroImage: Clin. 2019;22:101712.
- Tuladhar AM, van Uden IW, Rutten-Jacobs LC, Lawrence A, van der Holst H, van Norden A, et al. Structural network efficiency predicts conversion to dementia. Neurology. 2016;86(12):1112–9.
- 67. Yeo RA, Ryman SG, Van Den Heuvel MP, De Reus MA, Jung RE, Pommy J, et al. Graph metrics of structural brain networks in individuals with schizophrenia and healthy controls: group differences, relationships with intelligence, and genetics. J Int Neuropsychol Soc. 2016;22(2):240.
- Gou L, Zhang W, Li C, Shi X, Zhou Z, Zhong W, et al. Structural brain network alteration and its correlation with structural impairments in patients with depression in de novo and drug-naive Parkinson's disease. Front Neurol. 2018;9:608.
- Liu W, Zhang C, Wang X, Xu J, Chang Y, Ristaniemi T, et al. Functional connectivity of major depression disorder using ongoing EEG during music perception. Clin Neurophysiol. 2020;131(10):2413–22.
- Babajani-Feremi A, Noorizadeh N, Mudigoudar B, Wheless JW. Predicting seizure outcome of vagus nerve stimulation using MEG-based network topology. NeuroImage: Clin. 2018;19:990–9.
- Gomez-Pilar J, de Luis-García R, Lubeiro A, de la Red H, Poza J, Núñez P, et al. Relations between structural and EEG-based graph metrics in healthy controls and schizophrenia patients. Hum Brain Mapp. 2018;39(8):3152–65.
- Van Diessen E, Otte WM, Braun KP, Stam CJ, Jansen FE. Improved diagnosis in children with partial epilepsy using a multivariable prediction model based on EEG network characteristics. PLoS One. 2013;8(4):e59764.
- Wen W, Zhu W, He Y, Kochan NA, Reppermund S, Slavin MJ, et al. Discrete neuroanatomical networks are associated with specific cognitive abilities in old age. J Neurosci. 2011;31(4):1204–12.
- Jie B, Zhang D, Wee CY, Shen D. Topological graph kernel on multiple thresholded functional connectivity networks for mild cognitive impairment classification. Hum Brain Mapp. 2014;35(7):2876–97.
- dos Santos SA, Biazoli Junior CE, Comfort WE, Rohde LA, Sato JR. Abnormal functional resting-state networks in ADHD: graph theory and pattern recognition analysis of fMRI data. Biomed Res Int. 2014;2014:380531.
- Hou Z, Wang Z, Jiang W, Yin Y, Yue Y, Zhang Y, et al. Divergent topological architecture of the default mode network as a pretreatment predictor of early antidepressant response in major depressive disorder. Sci Rep. 2016;6(1):1–9.
- Liu L, Zhang H, Wu J, Yu Z, Chen X, Rekik I, et al. Overall survival time prediction for high-grade glioma patients based on large-scale brain functional networks. Brain Imaging Behaviour. 2019;13(5):1333–51.

- Yu R, Zhang H, An L, Chen X, Wei Z, Shen D. Connectivity strengthweighted sparse group representation-based brain network construction for M CI classification. Hum Brain Mapp. 2017;38(5):2370–83.
- Tijms BM, Ten Kate M, Gouw AA, Borta A, Verfaillie S, Teunissen CE, et al. Gray matter networks and clinical progression in subjects with predementia Alzheimer's disease. Neurobiol Aging. 2018;61:75–81.
- Tijms BM, Yeung HM, Sikkes SA, Möller C, Smits LL, Stam CJ, et al. Single-subject gray matter graph properties and their relationship with cognitive impairment in early-and late-onset Alzheimer's disease. Brain Connectivity. 2014;4(5):337–46.
- Hawkins R, Shatil A, Lee L, Sengupta A, Zhang L, Morrow S, et al. Reduced global efficiency and random network features in patients with relapsing-remitting multiple sclerosis with cognitive impairment. Am J Neuroradiol. 2020;41(3):449–55.
- Jie B, Liu M, Zhang D, Shen D. Sub-network kernels for measuring similarity of brain connectivity networks in disease diagnosis. IEEE Trans Image Process. 2018;27(5):2340–53.
- Dai D, He H, Vogelstein JT, Hou Z. Accurate prediction of AD patients using cortical thickness networks. Mach Vis Appl. 2013;24(7):1445–57.
- Langer N, Pedroni A, Gianotti LR, Hänggi J, Knoch D, Jäncke L. Functional brain network efficiency predicts intelligence. Hum Brain Mapp. 2012;33(6):1393–406.
- Hashmi JA, Kong J, Spaeth R, Khan S, Kaptchuk TJ, Gollub RL. Functional network architecture predicts psychologically mediated analgesia related to treatment in chronic knee pain patients. J Neurosci. 2014;34(11):3924–36.
- Watts DJ, Strogatz SH. Collective dynamics of 'small-world' networks. nature. 1998;393(6684):440–2.
- 87. Rubinov M, Sporns O. Complex network measures of brain connectivity: uses and interpretations. NeuroImage. 2010;52(3):1059–69.
- Tijms BM, Möller C, Vrenken H, Wink AM, de Haan W, van der Flier WM, et al. Single-subject grey matter graphs in Alzheimer's disease. PLoS One. 2013;8(3):e58921.
- Imms P, Clemente A, Cook M, D'Souza W, Wilson PH, Jones DK, et al. The structural connectome in traumatic brain injury: A meta-analysis of graph metrics. Neurosci Biobehav Rev. 2019;99:128–37.
- Lee J, Lee M, Kim D-S, Kim Y-H. Functional reorganization and prediction of motor recovery after a stroke: a graph theoretical analysis of functional networks. Restor Neurol Neurosci. 2015;33(6):785–93.
- Raamana PR, Weiner MW, Wang L, Beg MF. Initiative AsDN. Thickness network features for prognostic applications in dementia. Neurobiol Aging. 2015;36:S91–S102.
- Breiman L. Statistical modeling: The two cultures (with comments and a rejoinder by the author). Stat Sci. 2001;16(3):199–231.
- Christov-Moore L, Reggente N, Douglas PK, Feusner JD, Iacoboni M. Predicting empathy from resting state brain connectivity: A multivariate approach. Front Integr Neurosci. 2020;14:3.
- Doucet GE, Rider R, Taylor N, Skidmore C, Sharan A, Sperling M, et al. Presurgery resting-state local graph-theory measures predict neurocognitive outcomes after brain surgery in temporal lobe epilepsy. Epilepsia. 2015;56(4):517–26.
- Corps J, Rekik I. Morphological brain age prediction using multi-view brain networks derived from cortical morphology in healthy and disordered participants. Sci Rep. 2019;9(1):1–10.
- Gheiratmand M, Rish I, Cecchi GA, Brown MR, Greiner R, Polosecki PI, et al. Learning stable and predictive network-based patterns of schizophrenia and its clinical symptoms. NPJ Schizophr. 2017;3(1):1–12.
- Dicks E, Tijms BM, Ten Kate M, Gouw AA, Benedictus MR, Teunissen CE, et al. Gray matter network measures are associated with cognitive decline in mild cognitive impairment. Neurobiol Aging. 2018;61:198–206.
- Anderson ED, Giudice JS, Wu T, Panzer MB, Meaney DF. Predicting concussion outcome by integrating finite element modeling and network analysis. Front Bioeng Biotechnol. 2020;8:309.
- Sun G-W, Shook TL, Kay GL. Inappropriate use of bivariable analysis to screen risk factors for use in multivariable analysis. J Clin Epidemiol. 1996;49(8):907–16.
- Jie B, Wee C-Y, Shen D, Zhang D. Hyper-connectivity of functional networks for brain disease diagnosis. Med Image Anal. 2016;32:84–100.

- Xu M, Sanz DL, Garces P, Maestu F, Li Q, Pantazis D. A Graph Gaussian Embedding Method for Predicting Alzheimer's Disease Progression with MEG Brain Networks. IEEE Trans Biomed Eng. 2021;68(5):1579–88.
- 102. Rashid B, Calhoun V. Towards a brain-based predictome of mental illness. Hum Brain Mapp. 2020;41(12):3468–535.
- Wei R, Li C, Fogelson N, Li L. Prediction of conversion from mild cognitive impairment to Alzheimer's Disease using MRI and structural network features. Front Aging Neurosci. 2016;8:76.
- Vittinghoff E, McCulloch CE. Relaxing the rule of ten events per variable in logistic and Cox regression. Am J Epidemiol. 2007;165(6):710–8.
- Shrier I, Platt RW. Reducing bias through directed acyclic graphs. BMC Med Res Methodol. 2008;8(1):1–15.
- Heinze G, Wallisch C, Dunkler D. Variable selection–a review and recommendations for the practicing statistician. Biom J. 2018;60(3):431–49.
- 107. Heinze G, Dunkler D. Five myths about variable selection. Transpl Int. 2017;30(1):6–10.
- 108. Steyerberg EW. Clinical prediction models: a practical approach to development, validation, and updating. New York: Springer; 2019.
- Khalil H, Peters M, Tricco A, Pollock D, Alexander L, McInerney P, et al. Conducting high quality scoping reviews-challenges and solutions. J Clin Epidemiol. 2021;130:156–60.

Publisher's Note

Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.

Ready to submit your research? Choose BMC and benefit from:

- fast, convenient online submission
- thorough peer review by experienced researchers in your field
- rapid publication on acceptance
- support for research data, including large and complex data types
- gold Open Access which fosters wider collaboration and increased citations
- maximum visibility for your research: over 100M website views per year

At BMC, research is always in progress.

Learn more biomedcentral.com/submissions

