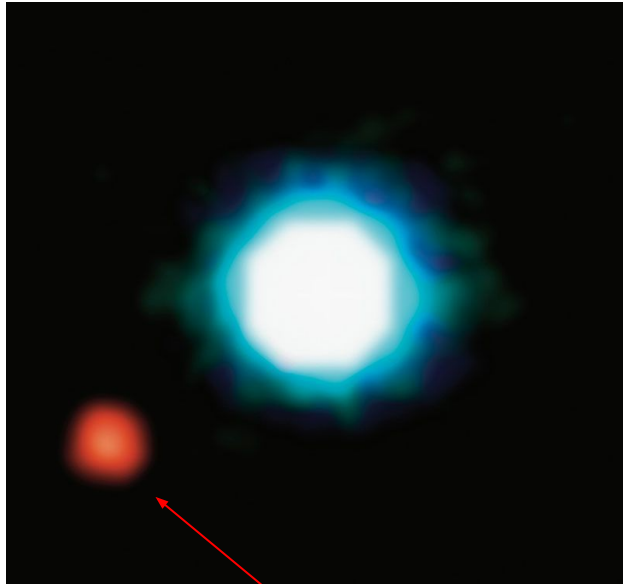


Simulation-based inference for exoplanet characterization

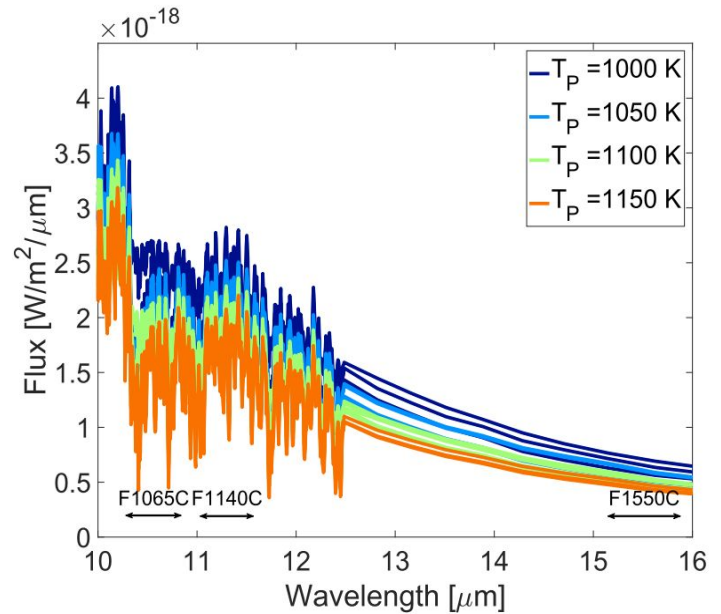
Malavika Vasist^a, Francois Rozet^b, Gilles Louppe^b, Olivier Absil^a

What's in an exoplanet?



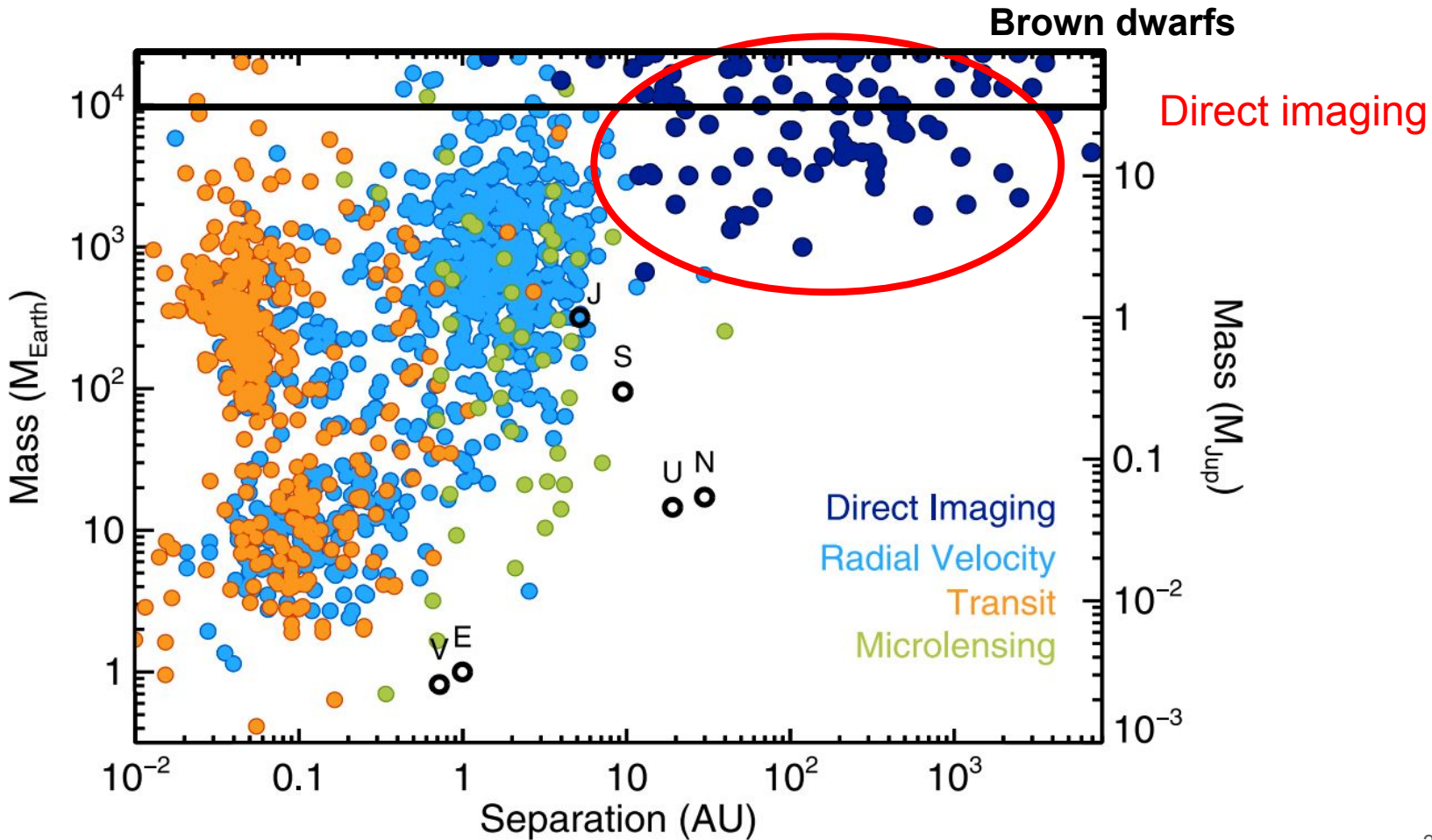
2M1207b

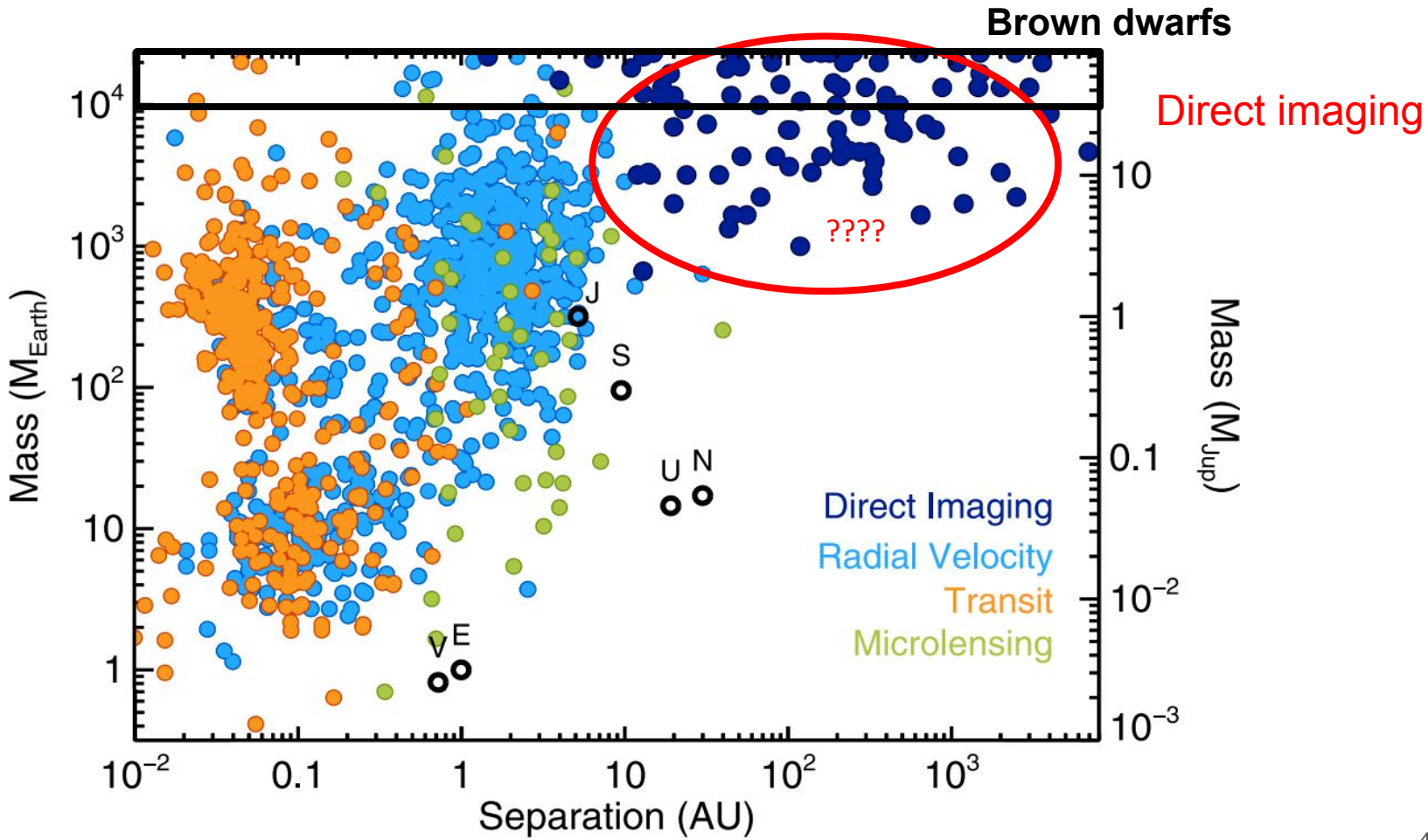
Direct imaging



Emission spectra

Danielski et al 2018





Motivation

Spectral retrieval, a best fit solution to the measured spectrum

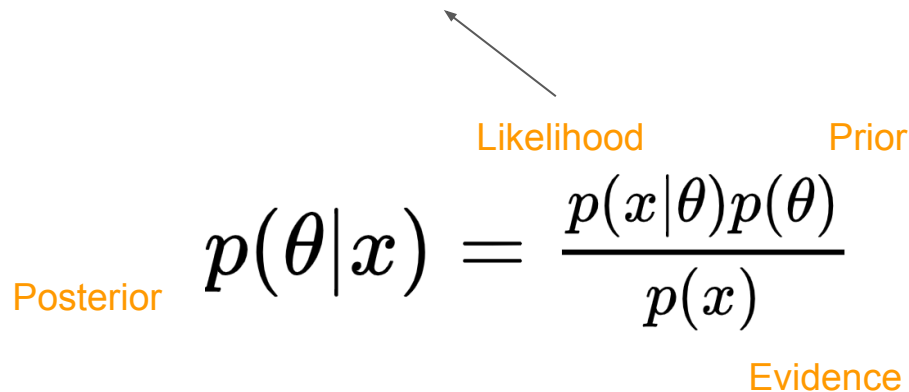
$$\text{Posterior } p(\theta|x) = \frac{\text{Likelihood } p(x|\theta) \text{ Prior } p(\theta)}{\text{Evidence } p(x)}$$

Bayesian inference

Motivation

Spectral retrieval, a best fit solution to the measured spectrum

Current forward models: **explicit and tractable** likelihood.
(e.g, Gaussian distance measure/correlation coefficient)



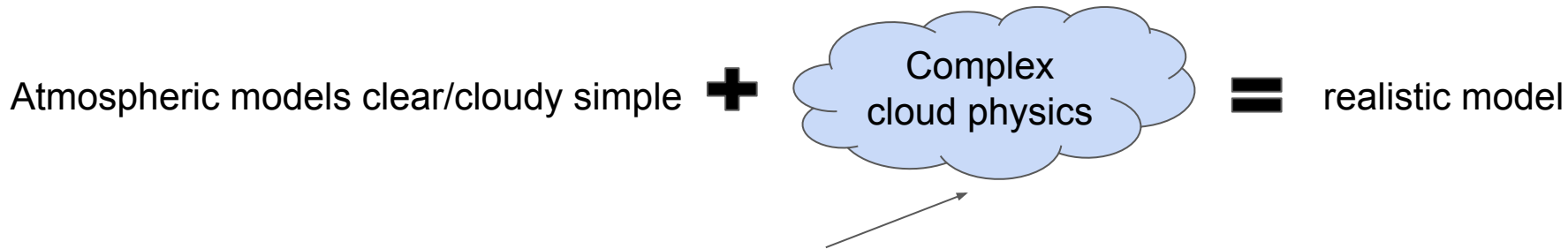
A diagram illustrating the Bayesian inference equation. The equation is $p(\theta|x) = \frac{p(x|\theta)p(\theta)}{p(x)}$. The terms are labeled as follows: 'Posterior' is written in orange to the left of $p(\theta|x)$; 'Likelihood' is written in orange above $p(x|\theta)$; 'Prior' is written in orange above $p(\theta)$; and 'Evidence' is written in orange below $p(x)$. A thin black arrow points from the 'Likelihood' label up and to the left towards the text 'Current forward models: explicit and tractable likelihood.' above.

$$\text{Posterior } p(\theta|x) = \frac{\text{Likelihood } p(x|\theta) \text{ Prior } p(\theta)}{\text{Evidence } p(x)}$$

Bayesian inference

Motivation

Spectral retrieval, a best fit solution to the measured spectrum

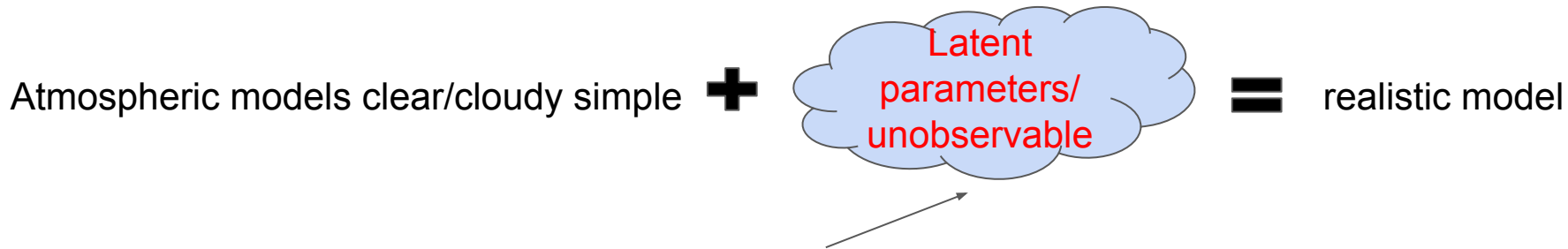


$$\text{Posterior } p(\theta|x) = \frac{\text{Likelihood } p(x|\theta) \text{ Prior } p(\theta)}{\text{Evidence } p(x)}$$

Bayesian inference

Motivation

Spectral retrieval, a best fit solution to the measured spectrum



$$\text{Posterior } p(\theta|x) = \frac{\text{Likelihood } p(x|\theta) \text{ Prior } p(\theta)}{\text{Evidence } p(x)}$$

We suggest **simulation-based inference** to **estimate** the **posterior** without explicitly calculating a likelihood.

Proof of concept setup

(simple case without latent parameters for comparison)



Simulator: *petitRADTRANS*^a for radiative transfer,

- line and collision opacities
- rayleigh scattering
- 2 clouds Fe and MgSiO₃
- 16 parameters- 3 cloud parameters,

a. <https://petitradtrans.readthedocs.io/>

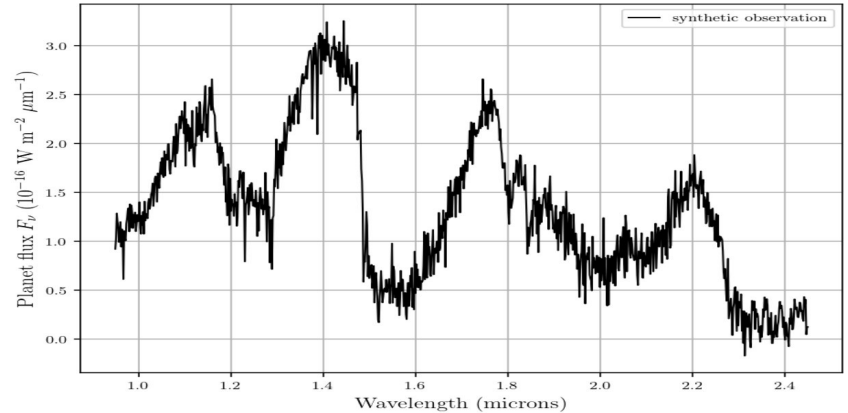
Proof of concept setup

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Synthetic **observation** spectra + $\mathcal{N}(0, \sigma^2)$
Mollière et al. (2020)

a. <https://petitradtrans.readthedocs.io/>

Proof of concept setup

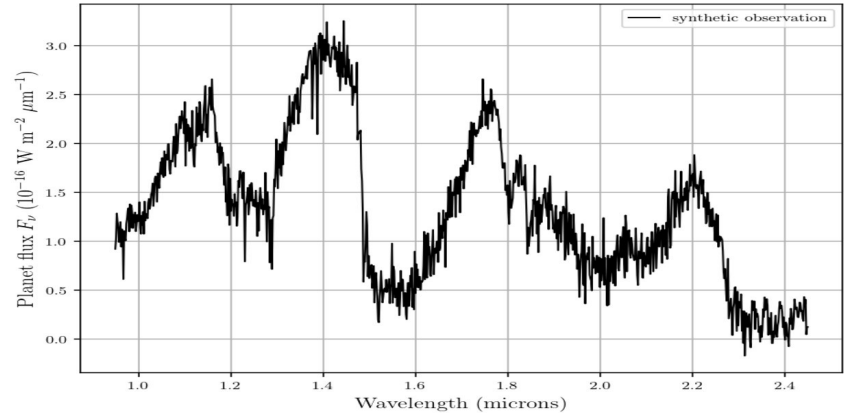
(simple case without latent parameters for comparison)



Simulator: *petitRADTRANS*^a for radiative transfer,

- line and collision opacities
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- 2 clouds Fe and MgSiO₃
- 16 parameters- 3 cloud parameters,

SBI package: *Lampe*^b

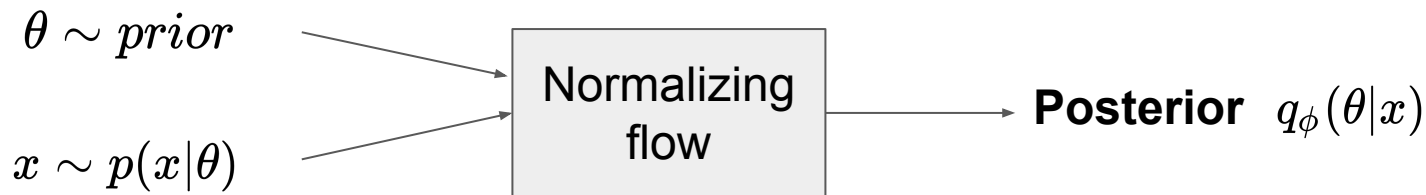


Synthetic **observation** spectra + $\mathcal{N}(0, \sigma^2)$
Mollière et al. (2020)

- <https://petitradtrans.readthedocs.io/>
- <https://github.com/francois-rozet/lampe>

Neural posterior estimation (NPE)

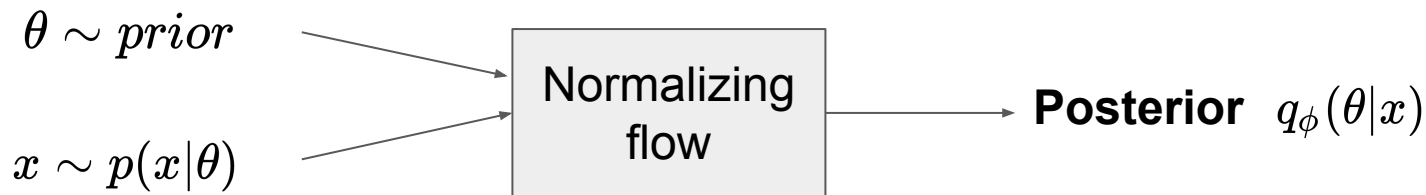
Embedding network : Res-MLP
NF: Masked autoregressive flow (MAF)



$$\phi^* = \operatorname{argmax}_\phi \mathbb{E}_{p(\theta,x)} [\log q_\phi(\theta|x)]$$

Neural posterior estimation (NPE)

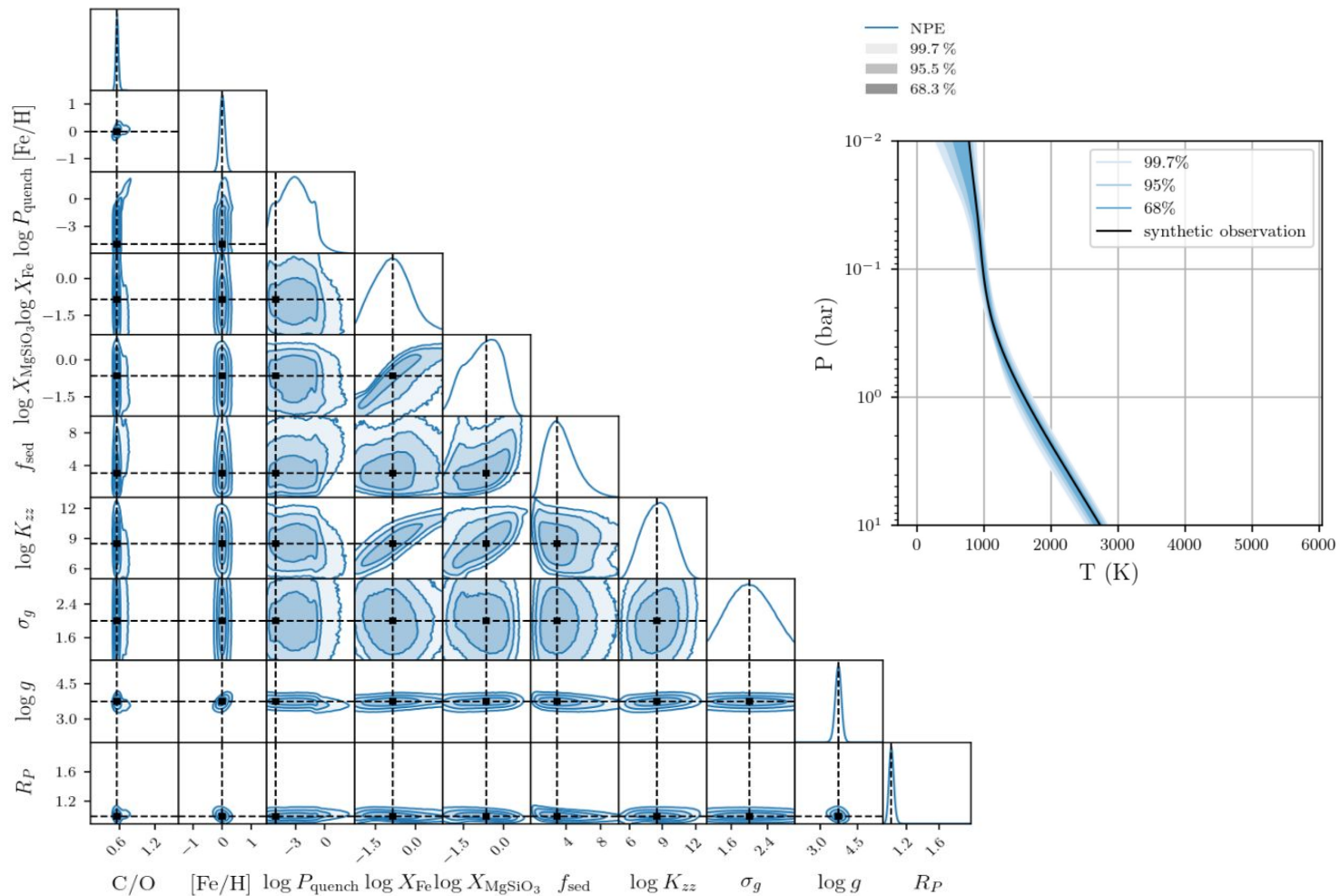
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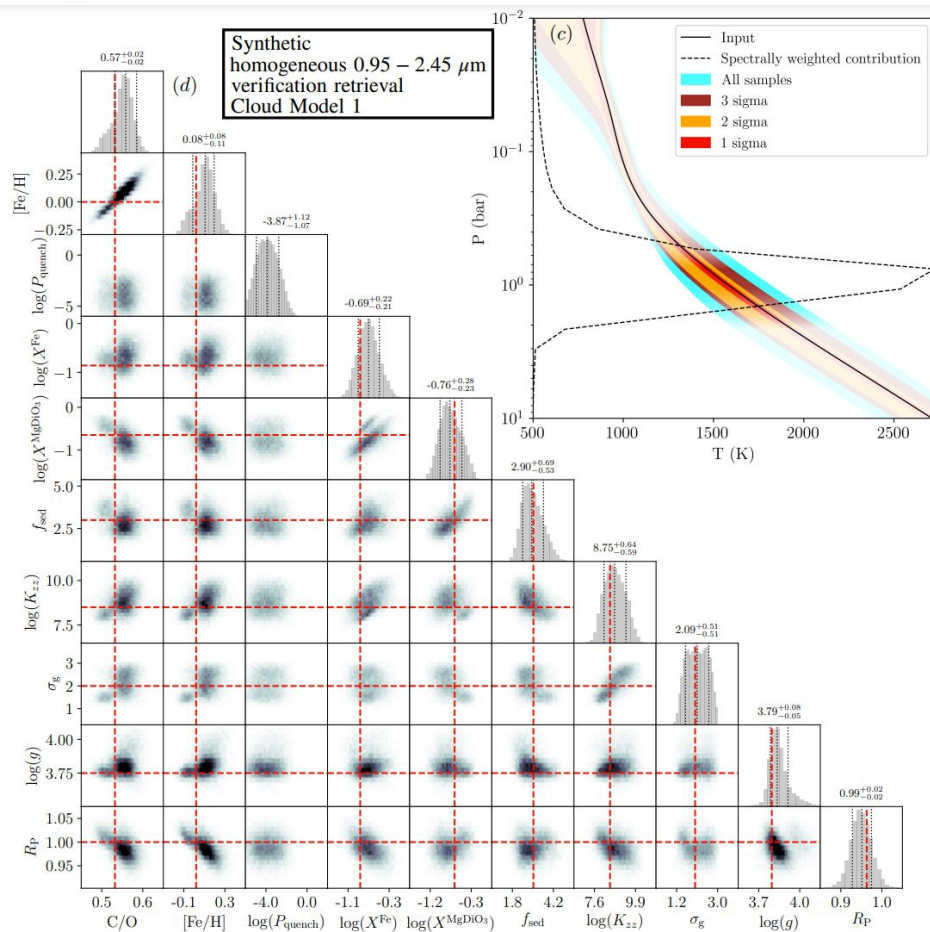
$$\phi^* = \operatorname{argmax}_\phi \mathbb{E}_{p(\theta,x)} [\log q_\phi(\theta|x)]$$

The estimator is amortized with respect to observations

Results

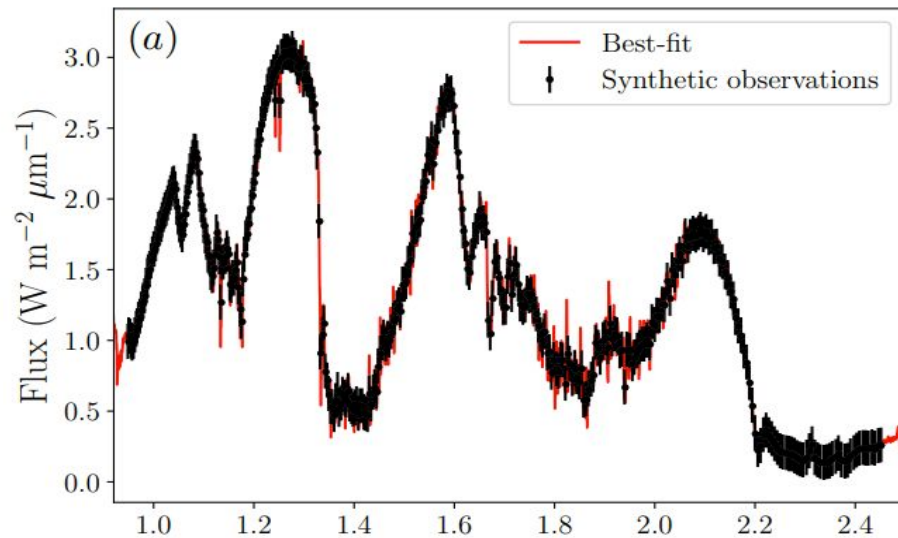
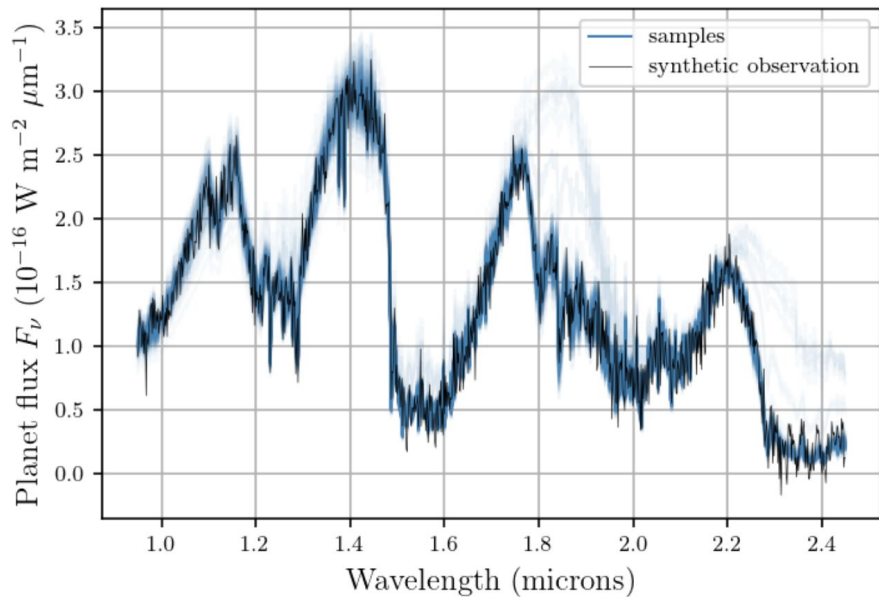


Results from Mollière et al 2020



Bayesian residuals

$$p(x'|x) = \int p(x'|\theta)q_\phi(\theta|x)d\theta$$

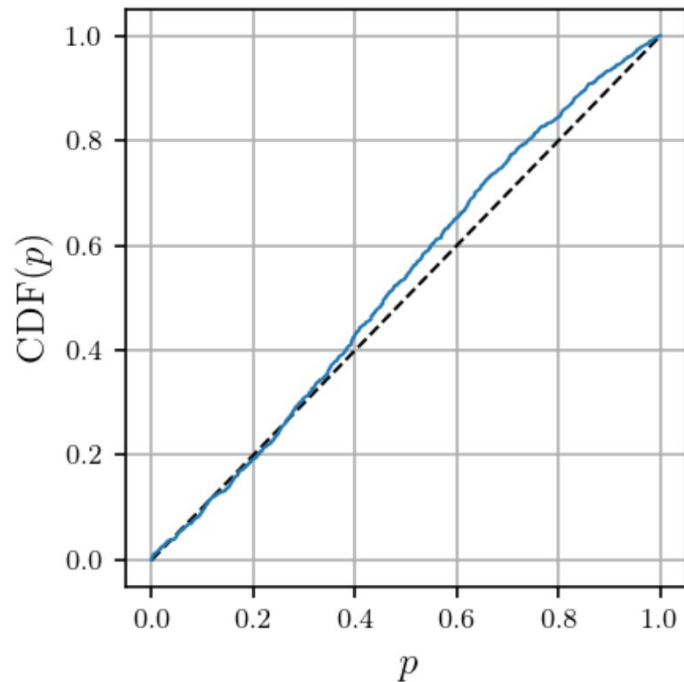


Consistent with synthetic observation

Coverage plot

Here we compare the **average of our estimated posterior** with the prior.

$$p(\theta) \approx \mathbb{E}_{p(x)} q_{\phi}(\theta|x)$$



Consistent with the prior

Conclusions

- The obtained results are **consistent with Nested Sampling** in Molliere et al 2020.
- SBI allows us to **characterize** exoplanet spectra **without** needing to explicitly **compute a likelihood**.
- It is **amortized** with respect to observations, hence faster and computationally less expensive.
- With this established proof of concept, this approach can be further used for **detailed atmospheric models** with complex cloud physics.

Thank You