

The changing face of AU Mic b: stellar spots, spin-orbit commensurability, and transit timing variations as seen by CHEOPS and TESS

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ABSTRACT

AU Mic is a young planetary system with a resolved debris disc showing signs of planet formation and two transiting warm Neptunes near mean-motion resonances. Here we analyse three transits of AU Mic b observed with the *CHaracterising ExoPlanet Satellite* (*CHEOPS*), supplemented with sector 1 and 27 *Transiting Exoplanet Survey Satellite* (*TESS*) photometry, and the *All-Sky Automated Survey* (*ASAS*) from the ground. The refined orbital period of AU Mic b is 8.462995 ± 0.000003 d, whereas the stellar rotational period is $P_{\text{rot}} = 4.8367 \pm 0.0006$ d. The two periods indicate a 7:4 spin-orbit commensurability at a precision of 0.1%. Therefore, all transits are observed in front of one of the four possible stellar central longitudes. This is strongly supported by the observation that the same complex star-spot pattern is seen in the second and third *CHEOPS* visits that were separated by four orbits (and seven stellar rotations). Using a bootstrap analysis we find that flares and star spots reduce the accuracy of transit parameters by up to 10% in the planet-to-star radius ratio and the accuracy on transit time by 3-4 minutes. Nevertheless, occulted stellar spot features independently confirm the presence of transit timing variations (TTVs) with an amplitude of at least 4 minutes. We find that the outer companion, AU Mic c, may cause the observed TTVs.

1. Introduction

Very young planetary systems allow us to study planets that recently formed or are still in the process of formation. One of the youngest stars with a planetary system known to date is AU Mic, a ~ 22 Myr-old (Mamajek & Bell 2014) M1 star belonging to the β Pic moving group (Torres et al. 2006), which has a dynamical trace-back age of 18.5 ± 2 Myr (Miret-Roig et al. 2020). The debris disc of AU Mic (Kalas et al. 2004) was first detected thanks to IRAS 12, 25, and 60 μm infrared observations (Mathioudakis & Doyle 1991). The disc is seen edge-on and has a complex inner structure, with rich substructures at the scale of 1 AU, a central cavity in the inner 30 AU that lacks small grains, and a prominent loop that rises 2.3 AU above the disc mid-plane (see Wisniewski et al. 2019, for an extensive review). These structures have been interpreted as possible tracers of ongoing planet formation.

Combining light curves from NASA's Transiting Exoplanet Survey Satellite (*TESS*) with near-infrared radial velocity measurements, Plavchan et al. (2020) recently an-

nounced the discovery of an 8.5-day transiting planet (AU Mic b) that lies within the inner cavity of the disc. These authors also found evidence for the presence of an additional planet candidate at ~ 30 days. The second planet in the system (AU Mic c) with an orbital period of about 18 days was recently confirmed based on *TESS* data by Martioli et al. (2021).

Being a young M-type star, AU Mic is very active. The *TESS* light curve from Sector 1 shows frequent flares superimposed on a $0^{\text{m}}08$ (peak-to-peak) photometric variability associated with the presence of active regions carried around by stellar rotation (Plavchan et al. 2020). The distance to AU Mic is only 9.7141 ± 0.0022 pc (Gaia Collaboration et al. 2018), making it one of the closest planetary systems with a transiting planet known to date.

The sky-projected spin-orbit angle of AU Mic b has been measured by several authors: $\lambda = -2.96^{+10.44}_{-10.30}$ (Palle et al. 2020); $\lambda = 0^{+18}_{-15}$ (Martioli et al. 2020); $\lambda = -4.7^{+6.8}_{-6.4}$ (Hirano et al. 2020); $\lambda = +5^{+16}_{-15}$ (Addison et al. 2020).

These measurements are all consistent with an aligned orbit, suggesting that AU Mic b likely formed in the protoplanetary disc that evolved into the current debris disc, provided that the star–disc–planet components of the system share the same angular momentum orientation.

Planets transiting magnetically active stars offer a unique opportunity to directly map the distribution of surface features, such as spots and faculae, along the transit chord (Lagrange et al. 2010). The passage of the planets in front of active regions that are spatially located along the transit chord can induce transit timing variations (TTVs; see, e.g. Barros et al. 2013; Mazeh et al. 2015). Different methods have been proposed to estimate the spot-filling factor along the transit chord and correct for unocculted star spot effects (Boisse et al. 2012; Lanza et al. 2011; Dumusque et al. 2014; Rosich et al. 2020).

The CHaracterising ExOPlanet Satellite (CHEOPS) is the first ESA space mission primarily dedicated to the study of known extrasolar planets (Benz et al. 2021). Its 30 cm (effective) aperture telescope enables the collection of ultra-high precision time-series photometry of exoplanetary systems in a broad optical bandpass. CHEOPS is a pointed mission, optimised to obtain high-cadence photometric observations for a single star at a time, and started its scientific operations in March 2020 (Lendl et al. 2020).

Here we present high-precision photometric follow-up observations of AU Mic b carried out with the CHEOPS space telescope. We aim to independently confirm the recently announced transiting planet AU Mic b and to improve its transit parameters and radius. The paper is organised as follows. We describe the observations in Section 2 and present the data detrending and analysis in Sections 3 and 4. We discuss our results in Section 5 and conclude in Section 6.

2. Space- and ground-based photometry

In the present paper we used CHEOPS photometry (Sect. 2.1) complemented with TESS light curves (Sect. 2.2) and archival ground-based photometry from the *All-Sky Automated Survey* (ASAS, Sect. 2.3). The log of the observations is listed in Tables 1 and 2.

2.1. CHEOPS imagette photometry

We observed three transits of AU Mic b with CHEOPS in July, August, and September 2020. The efficiency of the observations varied between ~ 55 and 90% depending on the aspect and duration of the Earth occultation. The brightness of AU Mic ($V=8^m.6$ and GAIA $G=7^m.843$; Kiraga 2012; Gaia Collaboration et al. 2018) enabled short-cadence photometry. We scheduled continuous 15-second exposures for the first two visits. For the third visit we reduced the integration time to 3 s to better sample and mask out flares. Figure 1 shows a $200'' \times 200''$ CHEOPS sub-array image centred around AU Mic. The CHEOPS Data Reduction Pipeline (DRP; Hoyer et al. 2020) provides aperture photometry of these sub-array frames. Because of the satellite bandwidth limitation, individual short exposures are normally co-added before download. For observations of AU Mic, this resulted in a sub-array cadence of 30 s, even if the cadence of individual photometric exposures is as short as 3 s.

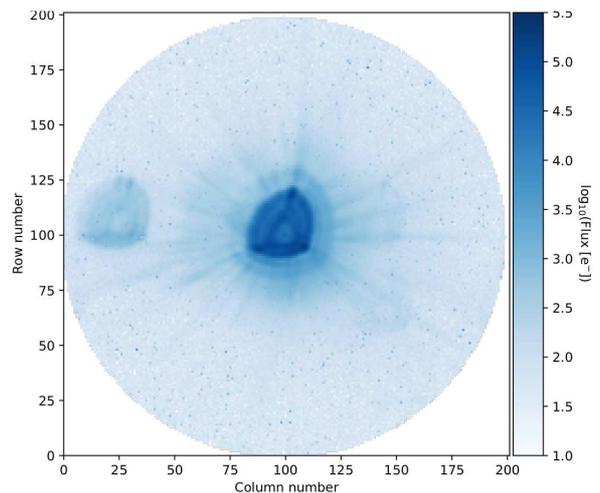


Fig. 1. CHEOPS $200'' \times 200''$ field of view. AU Mic is located at the center while the close-by faint field stars rotate during the observations.

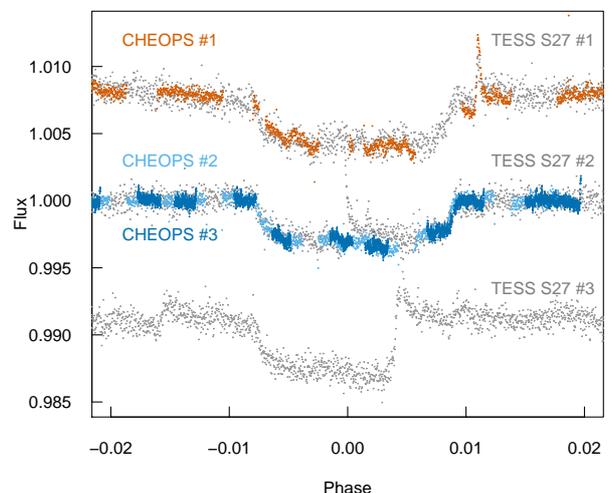


Fig. 2. CHEOPS and TESS S27 observations of AU Mic in 2020. CHEOPS#1 and TESS S27#1 were measured synchronously. CHEOPS#2 and #3 are overplotted with TESS S27#2, as they were observed at the same stellar longitude at different times. TESS S27#3 is plotted alone as there are no CHEOPS observations at this stellar longitude. This figure shows CHEOPS #3 data points binned to 15 s cadence.

In addition to the sub-arrays, there are images of 30 pixels in radius centred around the target, the so-called *imagettes*. These *imagettes* can be downloaded at a higher cadence, typically without the need to co-add them. In order to take advantage of the higher temporal cadence of the *imagettes* compared to the subarrays, we developed a custom *PSF imagette photometric extraction* (PIPE) tool that derives a point-spread function (PSF) from the data series, and fits it to each *imagette* to extract the photometry. The PIPE photometry is consistent with that derived from the DRP, with comparable performance. The higher cadence is particularly useful for resolving flares in active stars such as AU Mic.

In order to keep the cold plate radiators facing away from the Earth, the spacecraft rolls during its orbit, causing the field of view to rotate around the pointing direction. The target star remains stationary to within typi-

Table 1. CHEOPS observation logs. Time notation follows the ISO-8601 convention. The File Key supports the fast identification of the observations in the CHEOPS archive.

Visit #	Start date	End date	File key	CHEOPS product	Integ. time (s)	Co-added exposures	Num. of frames
1	2020-07-10 09:07:24	2020-07-11 00:45:29	PR100010_TG001701	Subarray <i>Imagettes</i>	30 15	15 s × 2 —	3597 7194
2	2020-08-21 19:07:06	2020-08-22 06:05:26	PR100010_TG001702	Subarray <i>Imagettes</i>	30 15	15 s × 2 —	4422 8844
3	2020-09-24 16:29:54	2020-09-25 10:16:00	PR100010_TG001801	Subarray <i>Imagettes</i>	42 3	3 s × 14 —	873 12222

Table 2. TESS and ASAS observation logs. Time notation follows the ISO-8601 convention.

Survey	Start date	End date	T _{exp} (s)	Num. points	Remarks
TESS S1	2018-07-25 19:12:03	2018-08-22 16:01:18	120	20066	Plavchan et al. (2020), 2 transits
TESS S27	2020-07-05 18:48:10	2020-07-30 03:33:42	20	97519	3 transits
ASAS	2001-08-21 03:09:30	2008-04-18 09:34:39	180	430	Stellar rotation

cally a pixel (Bonfanti et al. 2021). The irregular shape of the CHEOPS point-spread function (Fig. 1) along with the rotation of the field of view produces a variation of the flux contamination from nearby sources in phase with the roll angle of the spacecraft (Hoyer et al. 2020; Benz et al. 2021). We accounted for the roll angle systematics affecting the CHEOPS light curve of AU Mic using a fourth-order Fourier polynomial, with coefficients in the range of 0–400 ppm, as described in the Appendix. The raw CHEOPS light curves are shown in Fig. 2.

2.2. TESS data

TESS photometrically monitored AU Mic twice. Two transits were observed in Sector 1 (S1, July–August 2018) with a 120-s cadence and presented in Plavchan et al. (2020). Three additional transits were recently observed by TESS during its extended mission in Sector 27 (S27, July 2020) with a 20-s cadence. We retrieved the S1 and S27 TESS light curves from the Mikulski Archive for Space Telescopes (MAST) portal¹. For both sectors, we downloaded the simple aperture photometry (SAP) light curves detrended with the pre-search data conditioning (PDC) pipeline (Stumpe et al. 2012), that is, the so-called PDC-SAP fluxes.

The first transit observed by TESS in Sector 27 (hereafter transit S27#1) was also observed by CHEOPS during its first visit (hereafter CHEOPS#1). The different bandpasses of the two instruments allowed us to study the effects of stellar activity on the estimate of the planetary radius, as described in the following sections.

2.3. ASAS photometry

We also used archival ground-based photometry from the ASAS (ASAS, Pojmanski 1997). ASAS is currently monitoring $\sim 10^7$ stars brighter than $V < 14$ using two wide-field cameras in Chile (since 1997) and in Maui (since 2006). We retrieved the ASAS time-series photometry of AU Mic from

the web-page of the project². The data set consists of 423 data points covering a time-span of about 7.5 years, from August 2001 to April 2008. Following visual inspection of the light curve, we removed four obvious outliers. The average scatter of the remaining 419 data points is 0.023 mag, which hides the transits but contains the photometric variability induced by the presence of stellar spots appearing and disappearing as the star rotates about its axis.

3. Removal of systematics and flares

The TESS and CHEOPS light curves of AU Mic show numerous flares, with occasional peak amplitudes up to 0.1 mag superimposed on a periodic spot-induced variability of about 0.08 magnitudes (see Fig. 1 in Plavchan et al. 2020, and Fig. 3 in this work). Flares are among the most dominant sources of uncertainty for the parameter estimates extracted from the modelling of the transit light curves, and careful treatment of the observed transits is required. Prominent flares are observed during TESS S27#1 and S27#2 transits (see Fig. 2), with an energetic flare occurring at the mid-time of the S27#2 transit, severely biasing the second half of the transit light curve. During the S27#3 transit, a series of flares also burst, distorting the shape of the second half of the transit (Fig. 2).

Two flares are observed before and after the CHEOPS #1 transit, which are the same as in the TESS S27#1 transit. An energetic single flare is also observed shortly after the transit in CHEOPS#1 data with a top-to-bottom amplitude of 4700 ppm, while a weaker flare is present at the ingress, more visible (1500 ppm) in CHEOPS#1 data compared to TESS S27#1 photometry (1200 ppm). These flares can bias the level of the reference brightness before and after the transit. Nevertheless, one rotation farther from the transit, a ‘quieter’ light curve segment is observed out of transit. In this case, we used points from the two orbits that are one orbit apart from the transit to fit the out-of-transit level.

As AU Mic rotates about its axis, the out-of-transit level varies slowly with a peak-to-peak amplitude of 0.08 mag-

¹ <https://mast.stsci.edu/portal/Mashup/Clients/Mast/Portal.html>

² <http://www.astrouw.edu.pl/asas/>

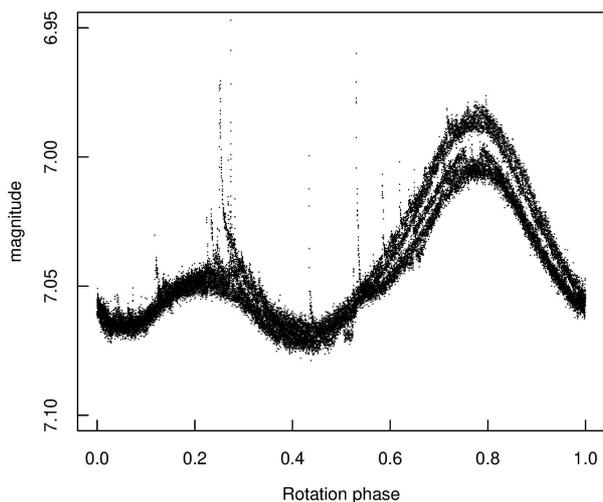


Fig. 3. TESS S27 light curve of AU Mic phase-folded at the stellar rotation period ($P_{\text{rot}}=4.8367$ d, $T_0 = 2459058.48$).

nitudes, as a result of the rotating spot complexes on the stellar surface. This is a slow systematic component from the point of view of the transit analysis, and as a part of the pipeline, we correct for it by (1) modelling the pattern of this contamination in synthetic images and subtracting it from the observations; and (2) involving a parametric fourth-order polynomial of the roll angle to the planet fitting procedure to make sure that the possible remnants of rolling systematics are removed from the pre-cleared signal (see the amplitude of these corrections in Table .2).

Major flares were identified as fast-increasing and exponentially decreasing light-curve features exceeding the local flux levels by at least 5σ . After removing flares and spot-induced photometric variation from the CHEOPS light curves, we inspected the residuals and found an additional variability with an amplitude of up to 20% the transit depth in CHEOPS data. The pattern is observed both in and out of transit and could be due to low-energy flares and granulation. During transits, we also expected features from occulted spots in the light curve. This variability, having a characteristic timescale of the ingress and egress duration of the transit, has a strong impact on the depth and timing measurements. Taking these systematics into account, we designed a bootstrap set of transit data and re-evaluated the precision of the planet parameter estimates, as described in the Appendix.

4. Data analysis

4.1. Stellar rotation

The magnetically active star AU Mic has a projected rotational velocity of $v \sin i_* = 7.5 \pm 0.9 \text{ km s}^{-1}$ (Martoli et al. 2020). A periodic pattern is observed in the TESS S1 data at a reported period of 4.86 d (Plavchan et al. 2020), which is ascribable to the presence of spots combined with stellar rotation. TESS S27 data show a rotation pattern similar to S1 data from 2018 (Plavchan et al. 2020), with cycle-to-cycle changes near the peak flux (Fig. 3). As in 2018, four stellar rotations are covered by the 2020 TESS S27 light curve.

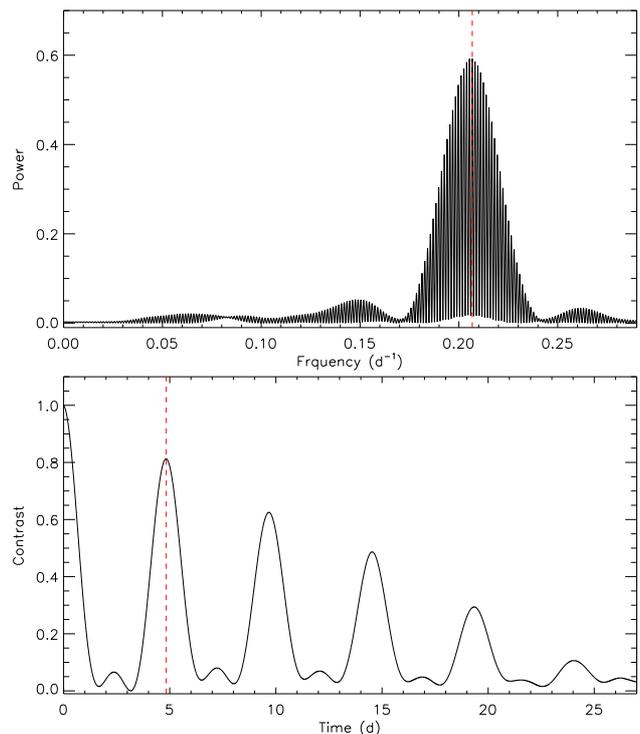


Fig. 4. *Upper panel.* Generalised Lomb-Scargle periodogram of the combined S1 and S27 TESS light curves. The red dashed line marks the rotation period of the star. The equally spaced peaks symmetrically distributed around the dominant frequency are due to the ~ 2 -year gap between the two TESS observations. *Lower panel:* Autocorrelation function of the combined TESS light curve. The red dashed line marks the rotation period of the star.

We masked out flares and transits of AU Mic and combined the S1 and S27 TESS light curves by separately median-normalising the two time-series. The generalised Lomb-Scargle (GLS) periodogram (Zechmeister & Kürster 2009) of the combined TESS light curve (Fig. 4) displays a significant peak at 4.8362 ± 0.0002 d with a false-alarm probability (FAP) well below 10^{-6} . We estimated the FAP using the bootstrap randomisation technique (Murdoch et al. 1993). Briefly, we computed the GLS periodogram of 10^6 mock data sets obtained by randomly shuffling the photometric measurements and their uncertainties, while keeping the time of observations fixed. We defined the FAP as the fraction randomised data sets whose highest GLS power exceeds that of the original data set in the frequency range $0.0 - 0.5 \text{ d}^{-1}$. We found no false alarms out of the 10^6 trials, implying a $\text{FAP} < 10^{-6}$. We note that the periodogram of the combined TESS light curves (Fig. 4) also displays a set of equally spaced aliases that are symmetrically distributed around the highest peak, with a frequency separation of $\sim 0.0014 \text{ d}^{-1}$ (~ 714 d). Those aliases are caused by the ~ 2 -year gap between the two TESS visits. We also performed a frequency analysis of each TESS time-series separately and obtained consistent results but with a larger uncertainty owing to the shorter baseline of each TESS sector (about 27 days).

We also used the autocorrelation function (ACF; McQuillan et al. 2013, 2014) method to measure the rotational period of AU Mic from the combined S1 and S27 TESS light curves. Briefly, the ACF technique measures the

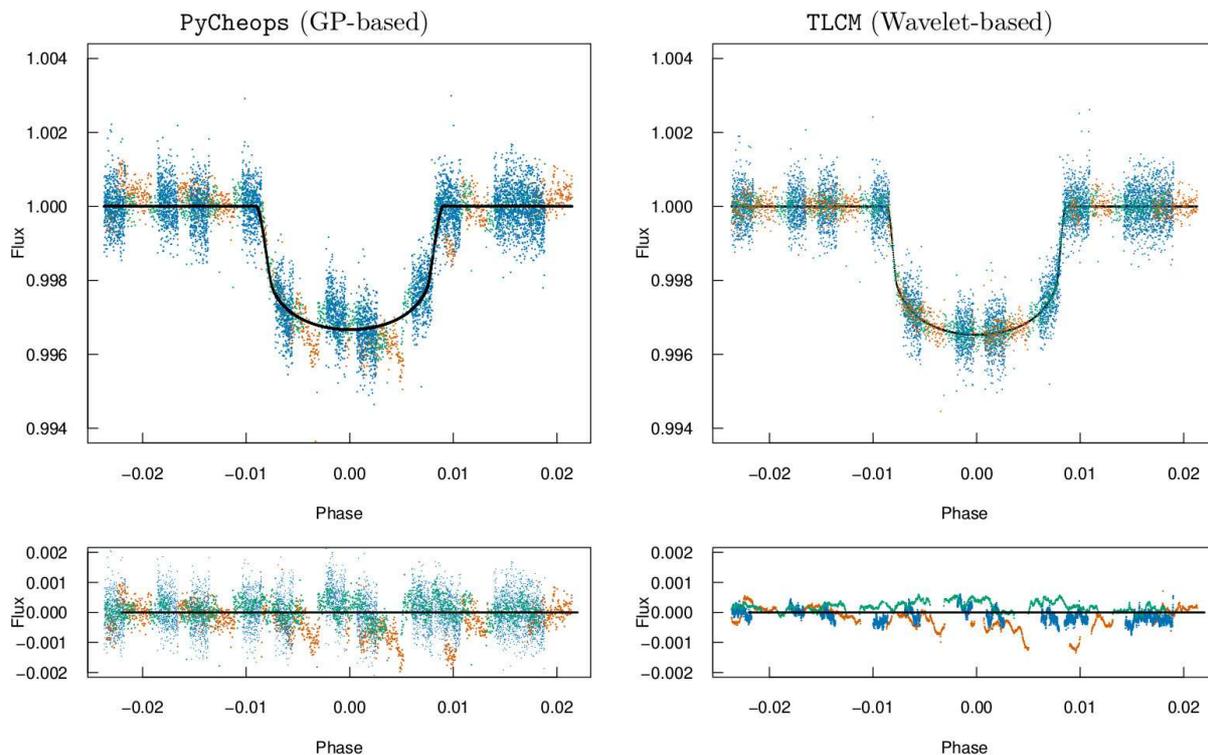


Fig. 5. Joint solution of the three CHEOPS transit observations, as derived following the two methods presented in Sect. 4.2. The colors code is the same as in Fig. 2. *Left upper panel.* Phase-folded CHEOPS data and best fitting transit model as obtained with `pycheops`. *Left lower panel.* Residuals to the `pycheops` solution. *Right upper panel.* Phase-folded CHEOPS data, TLCM1 best-fitting transit model, and white (uncorrelated) noise component separated by the TLCM. *Right lower panel.* Correlated part of the noise. The photometric variation is due to stellar activity and to the planet crossing active regions. All panels shows unbinned CHEOPS data from *imaggette* photometry.

degree of self-similarity of the light curve over a range of lags. In the case of rotational modulation, a peak in the ACF will occur at the number of lags corresponding to the period at which the spot-crossing signature repeats. The ACF of the TESS light curve displays its first two correlation peaks at $P_{\text{rot}}/2 \approx 2.4$ d and $P_{\text{rot}} \approx 4.8$ d (Fig. 4). The latter is the dominant peak at the rotational period of the star. We attributed the peak at 2.4 d to a partial correlation between active regions at opposite longitudes on the stellar photosphere. As the evolution timescale of active regions is longer than the rotation period of the star, the ACF shows secondary correlation peaks at $3/2 P_{\text{rot}}$, $5/2 P_{\text{rot}}$, and $7/2 P_{\text{rot}}$, as well as at $2 P_{\text{rot}}$, $3 P_{\text{rot}}$, $4 P_{\text{rot}}$, and $5 P_{\text{rot}}$. We fitted a Gaussian function to the correlation peak with the highest contrast and found a rotation period of $P_{\text{rot}} = 4.8367 \pm 0.0006$ d.

We finally performed a frequency analysis of the ASAS light curve of AU Mic (Sect. 2.3). The periodogram shows its highest peak at a frequency of 0.20648 ± 0.00013 d $^{-1}$, corresponding to a rotation period of $P_{\text{rot}} = 4.843 \pm 0.003$ d. Although the sampling of the ASAS photometry is sparse and the noise is much higher than in case of TESS and CHEOPS observations, results are in very good agreement, suggesting that there are likely some ‘preferred longitudes’ of starspots that give rise to a stable signal over a long time-span. Preferred longitudes have been observed to be present regularly in the case of several active stars (Strassmeier 2009; Berdyugina 2007), including planet-host stars (Lanza et al. 2009; Savanov 2011), and AU Mic fits well in this picture.

The three analyses provide consistent results well within their nominal uncertainties. For further analysis, we used the results with the highest nominal precision (ACF) and adopted a rotation period of $P_{\text{rot}} = 4.8367 \pm 0.0006$ d.

Our precise estimate of the rotational period reveals that there is a low-order commensurability between the stellar spin and the planet’s orbital period in the AU Mic system, in the form of:

$$7.0 \times P_{\text{rot}} = (4.0006 \pm 0.0005) \times P_{\text{orb}}. \quad (1)$$

This has important consequences for our interpretation of the measurements. As one orbit takes 1.75 stellar rotations, the stellar central longitude lags exactly $90 \pm 0.004^\circ$ in the retrograde direction from transit to transit. As a result, there are only four possible geometrical configurations for transits that are repeating continuously. Those transits that are separated by $4 \times n \times P_{\text{rot}}$ orbits are observed in front of the exact same stellar meridian, suffer very similar systematics from transited stellar features if the transit observations are taken close in time, and can be directly compared (n is an integer). This is why transits taken at different times are plotted over each other in Fig. 2.

Klein et al. (2021) used the brightness imaging technique on spectropolarimetric SPIROU data to reconstruct the differential rotation of AU Mic from spectral line profiles. They found that AU Mic has a solar-like differential rotation, with rotation periods of $P_{\text{eq}} = 4.84 \pm 0.01$ d at the equator and $P_{\text{pol}} = 5.10 \pm 0.15$ d at the poles. Klein et al.

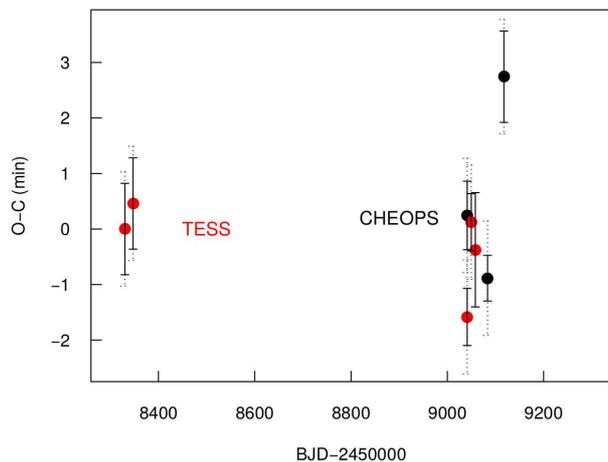


Fig. 6. $O - C$ diagram of the transit mid-times derived using an orbital period of 8.462995 days and an epoch of $T_0 = 2459041.28272$ BJD. TESS and CHEOPS transits are shown with red and black circles, respectively. The solid error bars mark the fitted uncertainties (precision), while the dotted error bars show the bootstrap errors (estimated accuracy), as derived using simulated *data sets*. (Sect. 4.3).

(2021) also found that active regions seem to be distributed on most of the stellar photosphere (see Figure 7 in their paper), with a higher concentration around the equator.

We measured a stellar rotation period of $P_{\text{rot}} = 4.8367 \pm 0.0006$ d, in very good agreement with the equatorial rotation period found by Klein et al. (2021). We note that our period estimate is also consistent with the expected value based on the stellar radius of $R_{\star} \approx 0.75 R_{\odot}$ (Plavchan et al. 2020), and the projected rotational velocity of $v \sin i \approx 7.5 \text{ km s}^{-1}$ (Martioli et al. 2020), assuming that the star is seen equator-on (Wisniewski et al. 2019). We are therefore confident that our estimate of the stellar rotation period refers to the stellar equator.

4.2. Transit light-curve modelling

We determined the transit parameters using the `pycheops` software module (Maxted et al., in prep.). `pycheops` uses the `qpower2` transit model and power-2 limb-darkening law (Maxted & Gill 2019). It uses a Gaussian process (GP) regression to account for the roll angle systematics, whose parameters are estimated using the out-of-transit data. Flares can severely bias the roll angle models of systematic error and also overestimate the level of correlated noise in the GP module. We therefore masked out the flares before modelling the data with `pycheops`.

The model parameters are the transit time (T_t), the transit depth parameter $D = (R_p/R_{\star})^2$, the transit duration parameter $W = (R_s/a) \sqrt{(1+k)^2 - b^2} / \pi$, and the impact parameter $b = a \cos(i) / R_s$. The priors are listed in Table 3. The stellar fundamental parameters were taken from SWEET-Cat (Sousa et al. 2018), which are the same as in Plavchan et al. (2020). The period was kept fixed and taken from the $O - C$ analysis (see paragraph below). The noise model was calculated with `celerite` using the white-noise term $JitterTerm(\log \sigma_w)$ plus, optionally, a GP with kernel $SHOTerm(\log \omega_0, \log S_0, \log Q)$. The same values of $\log \sigma_w$, $\log \omega_0$, $\log S_0$ and $\log Q$ are used for all the CHEOPS data sets in the combined fit. The priors for the GP noise

Table 3. Priors used with `pycheops`, TLMC1, and TLMC2.

Method	Parameter	Prior
<code>pycheops</code>	D	$N(0.003, 0.001)$
	W	$N(0.019, 0.005)$
	b	$N(0.01, 0.17)$
	T_t	$N(2459041.2747, 0.0022)$
TLMC1	T_{eff}	$U(3700, 100)$
	Z	$U(0.019, 0.02)$
TLMC2	R_{\star}	$N(0.75, 0.03)$
	T_{eff}	$U(3700, 100)$
	Z	$U(0.019, 0.02)$

parameters were S_0 between -30 and 0 , $\log \omega$ between $-2.3 \dots 8$, and $\log \sigma$ between -16 and -1 . The phase-folded CHEOPS transit light curves are shown in the left panel of Fig. 5 along with the best-fitting transit model derived with `pycheops`.

We found a significant variation of the orbital period well above the nominal uncertainties, and also on the nominal epoch of $T_0 = 2459041.28272$ BJD, depending on which transits are actually included in the joint analysis. This is a possible sign of TTVs, and/or severe stellar systematic errors that bias the parameter estimates, as discussed in the following sections. Therefore, we did not fit P_{orb} directly, but we fitted the transit time T_t of all transits individually, extending it to TESS data from 2018 and 2020. Subsequently, we determined the period with an observed-calculated ($O - C$) analysis (see, e.g. Sterken 2005). Briefly, the $O - C$ analysis compares the observed transit times to the calculated mono-periodic prediction, assuming an epoch T_0 and a trial period P_t , $C = T_0 + n \cdot P_t$, where n is an integer counting the number of transits from T_0 . If the period can be refined, the point distribution will have a linear component. This way, the problem of period determination is converted to a simple linear fit. As such, all CHEOPS and TESS transit light curves are used to determine period and T_0 . Applying the linear slope as a correction to the trial period, we obtained P_0 , the best-fitting period of the dataset. Also, the second order (a curvature) of the $O - C$ would show a period change. Consequently, the unexplained residuals to the $O - C$ have to be read in the same way as the classical TTV diagram. Another advantage is that this method separates the determination of the period and the other planet parameters, so after this analysis P can be kept fixed.

The three CHEOPS and five TESS transits led to the following mean period of $P_{\text{orb}} = 8.462995 \pm 0.000003$ d and $T_0 = 2459041.28272 \pm 0.00033$ (Table 4). We note that in comparison with the orbital period found by Martioli et al. (2021), this result seems to be less precise, because the error interval increased after introducing three new points to the previous distribution. This is a result of low number statistics. The errors on a quantity are themselves statistical variables too, and they suffer transient fluctuations before they start converging asymptotically. In the case of CHEOPS #1 and CHEOPS #2 observations, the transit times coincide well (within ~ 1 minute) with the linear fits to the TESS points, but CHEOPS #3 is very inaccurate (2.9 minutes from the linear fit to the other points). This measurement increased the empirical scatter and scaled

Table 4. Best-fitting parameters of AU Mic b, as derived from the joint analysis of the three CHEOPS transit light curves. Quantities marked with an asterisk are priors. The orbital period was derived using the three CHEOPS and five TESS transit times (see Sect. 4.2 for details). The parameters are compared to the results of Plavchan et al. (2020) (P2020) and Martioli et al. (2021) (M2021).

	pycheops		TLCM1		TLCM2		P2020	M2021
P [d]	8.462995	$\pm 3 \cdot 10^{-6}$	8.462995	(fixed)	8.462995	(fixed)	$8.46321 \pm 4 \cdot 10^{-5}$	$8.46300 \pm 2 \cdot 10^{-6}$
R_p/R_*	0.0531	± 0.0023	0.0534	± 0.0006	0.0534	± 0.0006	0.0514 ± 0.0013	$0.0526^{+0.0003}_{-0.0002}$
a/R_*	19.24	± 0.37	19.37	$^{+0.13}_{-0.18}$	19.10	$^{+0.13}_{-0.18}$	$19.1^{+1.8}_{-1.6}$	$19.1^{+0.2}_{-0.4}$
W [h]	3.48	± 0.19	3.51	± 0.10	3.51	± 0.10	$3.50^{+0.63}_{-0.59}$	3.50 ± 0.08
R_* [R_\odot]	0.75*	± 0.03	0.725	± 0.15	0.75*	± 0.03	0.75 (fixed)	0.75 (fixed)
M_* [M_\odot]	0.50*	± 0.03	0.53	± 0.27	0.56	± 0.06	0.50 ± 0.03	0.50 (fixed)
R_p [R_\oplus]	4.36	± 0.18	4.23	± 0.8	4.38	± 0.05	4.29 ± 0.20	4.07 ± 0.17
a [AU]	0.0678	± 0.0013	0.0692	± 0.0006	0.0704	± 0.0006	$0.066^{+0.007}_{-0.006}$	0.0645 ± 0.0013
b	0.09	± 0.05	0.00	± 0.13	0.00	± 0.13	$0.16^{+0.14}_{-0.11}$	0.18 ± 0.11

up the estimates on the error of the orbital period — in a way that is consistent with the statistical behaviour of quantities and their errors. The $O - C$ diagram is shown in Fig. 6 and is discussed further below in detail. For the interpretation of the $O - C$ diagram, and the proper comparison of our parameter estimates with those reported in the discovery paper (Plavchan et al. 2020), a critical assessment of the effects of the systematics and stellar activity is necessary.

We also modelled the CHEOPS transit light curves with the wavelet-based Transit and Light Curve Modeller (TLCM) (TLCM; Csizmadia 2020). TLCM uses the light curve model of Mandel & Agol (2002) along with the quadratic limb-darkening law. Instead of directly fitting the linear (u_a) and the quadratic (u_b) limb-darkening coefficients, we fitted their combinations $u_+ = u_a + u_b$ and $u_- = u_a - u_b$, as they are less degenerate with the other model parameters and with each other than u_a and u_b (Brown et al. 2001).

TLCM accounts for the red noise via a wavelet-based approach (Carter & Winn 2009). This confers the advantage that it requires only two additional parameters, namely σ_w (white noise level) and σ_r (red noise factor)³. We estimated the red noise from the out-of-transit photometry. We added a four-order truncated Fourier-series to account for the baseline-variation caused by the rotation of the field of view around the telescope line of sight (for details on the baseline fitting refer to Lendl et al. 2020), which causes the stellar images to fall on different pixels every ~ 98.7 minutes (i.e., the CHEOPS orbital period; Benz et al. 2021). The pixels can vary from visit to visit as the satellite is repositioned to a new target and then back to AU Mic. We therefore used different coefficients for every CHEOPS visit.

The model parameters are the scaled semi-major axis (a/R_*), the planet-to-star radius ratio (R_p/R_*), the impact parameter (b), epoch, the noise parameters σ_w and σ_r , and a zero-point flux level correction p_0 . In addition, we fitted four cosine and four sine terms (3 transits \times 8 free parameters) to model the baseline variation. TLCM also determines a stellar model based on T_{eff} and the fitted stellar density $\rho_* = 3\pi(a/R_*)^3 G^{-2} P_{\text{orb}}^{-2} (1 + q)$, where the mass ratio q can be approximated with zero in the case of a planet. The $T_{\text{eff}} - \rho$ isochrones are then fitted from Tognelli et al.

³ See Carter & Winn (2009) for an explanation of their meaning.

(2011), which finally gives the mass and radius of the star as a fitted parameter.

TLCM first searches for the initial best-fit values using a genetic algorithm (Harmony Search) and refines the parameter estimates by simulated annealing. The refined values are used to initialise the Markov chain Monte Carlo (MCMC) analysis. For the analysis of the CHEOPS transit light curves of AU Mic, we ran 500 MCMC chains with a thin factor of 100, until convergence was reached (this required 400 000 steps in each chain). The convergence was checked via monitoring the Gelman-Rubin statistic of the chains and via the estimated sample size. Table 4 lists the inferred transit parameters and their uncertainties, which are defined as the median and 68 % region of the credible interval of the posterior distributions for each fitted parameter. The nominal errors are lower in the case of TLCM models because of the separation of white and red noise, but the accuracy of the two models is supposed to be identical.

A strong flare occurred after CHEOPS transit #1, which significantly increased the out-of-transit flux after the event. In principle, the red noise treatment implemented in TLCM is able to correct for this flux change but not perfectly. To assess the impact of the flare on the planet-to-star radius, we modelled the transit twice, first including and then masking out the data points affected by the flare. We find that the planetary radius decreases by 1.8 % if the data points affected by the flare are removed from the light curve. As the 1σ relative uncertainty of the planetary radius is about 1.05 %, this flare introduces less than 2σ systematic uncertainty into the planet-to-star radius ratio. As for the remaining transit parameter, the differences are not significant, being less than 2σ . To account for the possible bias introduced by flares, we increased the $\sim 1\%$ relative uncertainty of the planet-to-star radius ratio to 2 %.

The parameter estimates obtained with `pycheops` and `TLCM1` are consistent within their 1σ uncertainties, and they are also consistent with those of Plavchan et al. (2020) and Martioli et al. (2021). Unbiasing the best-fitting planetary radius for systematic errors is a non-trivial task, but the compatibility of the results in this paper and the previous literature confirms both our solutions and the parameters in the previous papers. While the stellar mass and radius estimated by TLCM from the isochrones and the tran-

sit light curve are in good agreement with those given by White et al. (2019) and Plavchan et al. (2020), the former are less precise than the latter, leading to a larger uncertainty on the planet’s radius derived by TLMC. This is due to the fact that PMS stellar isochrones of M-type low-mass stars are very close to each other.

To account for the lack of precision on the stellar mass and radius inferred using the isochrones, we performed a second analysis with TLMC (see Table 4) using a Gaussian prior for R_\star of $N(0.75, 0.03)$. The stellar mass M_\star was derived via the $\log \rho_\star - T_{\text{eff}}$ –metallicity relationship based on the PMS isochrones of Tognelli et al. (2011). The results are reported in Table 4.

The parameter estimates derived using the three methods described in the previous paragraphs agree well within their nominal 1σ uncertainties. We adopted the results obtained with the second TLMC modelling for further analyses as they have the highest precision (TLMC2 in Table 4). This provided a planetary radius of $R_p = 4.38 \pm 0.05 R_\oplus$, in agreement with the value reported by Plavchan et al. (2020).

4.3. Accuracy of the planet parameters in the presence of systematics

It is known that systematics on timescales comparable to the transit duration can lead to biased parameter estimates with uncertainties that are underestimated in the formal precision produced by the analysis. To estimate a realistic accuracy in the fundamental parameters, we designed a parametric bootstrap and measured the stability of the reconstructed transit parameters.

The noise model, including stellar and instrumental systematics, was simultaneously synthesised by fitting third-order ARIMA models (Box & Jenkins 1976; Saleh Ahmar et al. 2018) to the out-of-transit data after removing the low-frequency variation due to the stellar rotation signal and masking out evident flares as described in Sect. 2.4. ARIMA models produce noise terms with partial correlation, simulating systematic patterns in a parametric auto-regressive process with a moving average. The model transit light curve for AU Mic b, with the same input parameters as those obtained in Sect. 4.2, was injected into 100 different realisations of the ARIMA noise model. Earth occultations were taken into account by omitting short segments of the light curve that are one CHEOPS orbit apart, with an efficiency of 85%.

The transit parameters were then determined from 100 such simulations, with each fit being solved for transit depth, duration, and transit time. The resulting parameters were compared with the input transit parameters. The transit time in the model fits has a standard deviation of 3 minutes, while the relative standard deviations were 5.5% in the nominal value of the relative radius and 2.0% or 4.2 minutes in transit duration, respectively.

We conclude that the transit time can be determined from observations with an accuracy of 3 minutes at best. This means that fitted transit times can be expected to vary on a timescale of ± 3 minutes simply due to the presence of correlated noise, without any specific physical variations in the AU Mic system.

Table 5. Transit times and planet-to-star radius ratios derived with TLMC1 from the individual CHEOPS transits.

Transit	T_t (BJD)	R_p/R_\star [TLMC]
CHEOPS #1	2459041.2828 ± 0.0006	0.0575 ± 0.0012
CHEOPS #2	2459083.5970 ± 0.0004	0.0532 ± 0.0010
CHEOPS #3	2459117.4515 ± 0.0008	0.0525 ± 0.0012

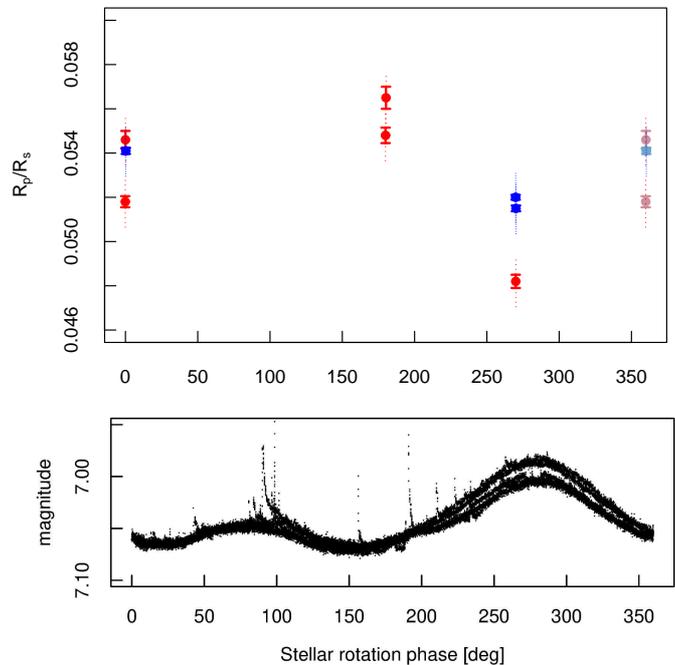


Fig. 7. Planet-to-star radius ratio versus stellar rotation phase. The red and blue circles mark the TESS and CHEOPS transits, respectively, as modelled with `pyaneti`. (We note that the data points at phase 0° are repeated at phase 360° for clarity.) The solid error bars are the nominal uncertainty (precision), while the dotted lines are the uncertainties after accounting for the lack of accuracy with the bootstrap method described in Sect. 4.3.

4.4. Transit depth variation

The presence of spots on the photosphere of AU Mic has a twofold effect on the transit depth, and therefore on the measurement of the planet-to-star radius retrieved from the modelling of the transit light curves.

1. Spots along the transit chord that are partially or completely occulted by the planet distort the shape of the transit light curve: While the planet is passing in front of a spot, the fractional loss of light is temporarily reduced and a positive ‘bump’ is observed in the transit light curve (see, e.g. Sanchis-Ojeda & Winn 2011).
2. Spots that are not spatially located along the transit chord by the time the planet passes in front of the star reduce the brightness of the unocculted part of the stellar hemisphere with respect to a spot-free surface, making the transit appear deeper (see, e.g. Pont et al. 2008). As the transit depth is proportional to the filling factor of the unocculted spots, transits are expected to be deeper when the star is closer to its photometric minimum.

Both effects depend on the spot temperature contrast with respect to the temperature of the quiet photosphere, with their magnitude increasing at shorter wavelengths. We measured the depth and the mid-time for each transit observed by CHEOPS and TESS using the code (`pyaneti`; Barragán et al. 2019). We fixed the period, scaled semi-major axis, impact parameter, and limb-darkening coefficients to the values derived from the joint analysis, while allowing for the mid-time and depth to vary (results are listed in Table .1). Figure 7 displays the planet-to-star radius ratio R_p/R_* as a function of the rotation phase of the star. The thick lines mark the nominal uncertainties (precision), while the dotted lines are the uncertainties as derived using the bootstrap method described in Sect. 4.3. We arbitrarily set the stellar rotation phase to zero at the mid-time of the first transit observed by TESS, which occurred around one of the two photometric minima of the star. Given the 7:4 commensurability between the rotation period of the star and the orbital period of AU Mic b, the transits can only be observed at four rotation phases.

We find significant transit depth variations of up to $\sim 20\%$, well above the nominal uncertainties (solid error bars). The deepest transits are observed around the photometric minima of the star (phase 0.75 in Fig. 7), when the spot filling factor is higher. We also detect a possible chromatic effect. The transits observed by CHEOPS tend to be deeper than those observed by TESS, in agreement with the hypothesis that if the star is heavily spotted, the transit appears deeper in the CHEOPS passband, which is bluer than that of TESS (Fig. 7).

4.5. Active regions along the transit chord

The modelling of the CHEOPS transit light curves revealed the presence of systematic patterns in the residuals (Fig. 5, lower panels). These are partly due to low-energy flares and granulation, but they can also be associated to the occultation of starspots and faculae spatially located along the transit chord.

Dark and bright spot-crossing events have already been observed in several transiting systems, such as CoRoT-2b (Silva-Valio et al. 2010), HAT-P-11 (Sasselov et al. 2010), WASP-4 (Sanchis-Ojeda et al. 2011), Qatar-2 (Močnik et al. 2017; Dai et al. 2017), and WASP-19 (Espinoza et al. 2019). These anomalies have been used to measure the spin-orbit misalignment, that is, the angle between the stellar rotation axis and the angular momentum vector of the planet. For instance, the observed patterns of these events in the light curves of CoRoT-2 (Nutzman et al. 2011), Kepler-17 (Désert et al. 2011), and WASP-85 (Močnik et al. 2016) revealed a spin-orbit alignment and a prograde orbital motion of their planets, while HAT-P-11b (Sanchis-Ojeda & Winn 2011) and WASP-107b (Dai & Winn 2017) have been found to have orbital planes that are misaligned with respect to the orbital axes of their host stars.

The AU Mic system is unique in that not only are the observed light curve features clearly separated, but the entire transit floor is continuously undulated. Whether these structures are caused by dark spots or correspond to bright faculae is unclear. As we always see the presence of active areas in the transit chord, the precise radius determination of AU Mic can only be expected from a parallel photometric (preferably both visual and infrared) and spectroscopic

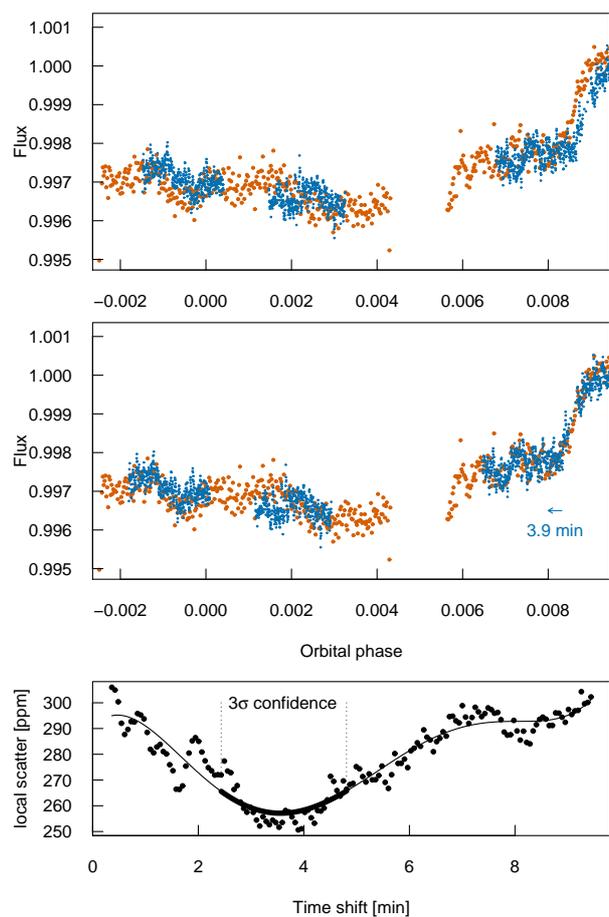


Fig. 8. *Top panel:* Zoom into the second half of CHEOPS#2 and CHEOPS#3 transits (orange and blue data points, respectively) plotted against each other, according to the phases derived from the best-fitting joint solution (Sect. 4.2). The colour code is the same as in Fig. 2. *Middle panel:* Same as in the upper panel, but with a leftward TTV correction of 3.9 minutes applied to the CHEOPS#3 transit (blue data points). We note that both the egress and the structures due to occulted active regions overlap, confirming the time shift. *Bottom panel:* Determination of the time-shift with a phase dispersion minimisation analysis (see text in Sect. 4.6).

measurement where the map of the surface can be modelled with Doppler tomography. This ambiguity explains the larger error in R_p/R_* from the present analysis (Table 4) than that in Plavchan et al. (2020).

4.6. Transit-timing variation revealed by occulted active regions

As occulted active regions systematically distort the light curves, they are candidate sources of apparent TTVs without a dynamical background (Barros et al. 2013). An especially active system such as AU Mic has to be handled with extraordinary care, avoiding over-interpretation when comparing transit times before different stellar surface structures.

Fortunately, we know that CHEOPS#2 and CHEOPS#3 transits occurred at the same stellar longitude, which allows us to compare the transit light curves directly. We note that by simple visual inspection, we see that the egresses of these two transits are shifted

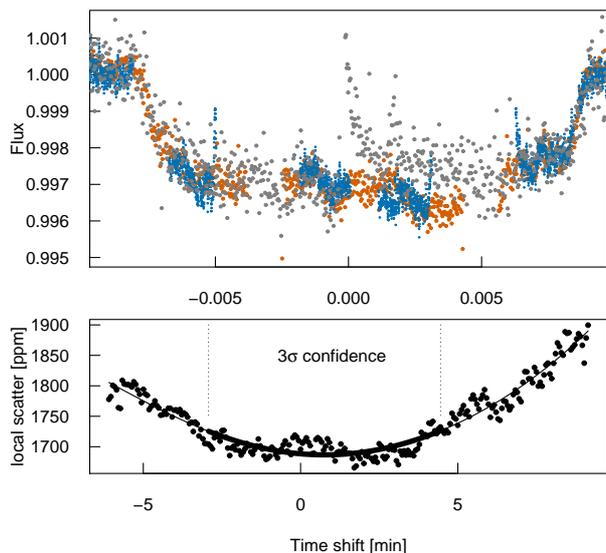


Fig. 9. *Upper panel:* Unified CHEOPS #2-#3 transit light curves (orange and blue data points respectively). CHEOPS #3 transit has been corrected for TTV to the time frame of CHEOPS #2, as in the middle panel of Fig. 8. TESS S27 #2 data not corrected for TTV are displayed with grey points. The colour code is the same as in Fig. 2. *Lower panel:* Corresponding cross-correlation analysis.

in time (see Fig. 8 for a zoom-in of the two CHEOPS measurements).

To test the time-shift between these light curves, we adopted a method that is very similar to the cross-correlation. CHEOPS#2 and CHEOPS#3 datasets were unified by shifting the CHEOPS#3 data by a shift parameter that was kept free during the analysis. The unified dataset was sorted by the orbital phase variable. The free parameter in this test is the time-lag between CHEOPS#2 and CHEOPS#3, in minutes. The σ mean local scatter was determined as:

$$\sigma = \sqrt{\langle (f_{i+1} - f_i)^2 \rangle}, \quad (2)$$

where the mean (denoted by $\langle \rangle$) was calculated in the transit bin only. Here, f is the scaled flux of the unified (original) CHEOPS#2 and (shifted) CHEOPS#3 dataset, and i is the rank with respect to phase.

The shape of the local scatter as a function of time-lag has then been fitted by a fifth-order polynomial (lowest panel in Fig. 8). The confidence level of the time shift that takes the residuals of CHEOPS#2 to CHEOPS#3 was determined by a threshold value of the minimum of the fitted model, plus three times the standard deviation between the model and the points. This interval (lowest panel in Fig. 8) corresponds to shifts of between 2.1 and 5.1 minutes, which are compatible with the TTV measured from the fitted models (Fig. 6).

The middle panel of Fig. 8 shows the phased transit light curves (second half of the transit floor and egress part magnified) after applying the time-lag correction of 3.9 minutes. We see that, not only do the egresses overlap, but the undulation from occulted stellar surface structures also perfectly match. This confirms that (1) the observed time-lag is really due to TTVs of the planet, and (2) the undulating features are due to the star.

We repeated the same analysis to compare the combined CHEOPS #2 (not TTV corrected) and CHEOPS #3 (TTV corrected to the phase frame of CHEOPS #2) datasets versus the TESS S27 #2 transit — which shows a transit at the same equatorial latitude but at a different time. In other words, the combined datasets in Fig. 8 (middle panel) and Fig. 2 (middle panel, grey dots) were compared. The result of this comparison is shown in Fig. 9. We see that the minimum of the correlation function is at ≈ 1 minute, showing that CHEOPS #2 should be shifted by 1 minute to get the best overlap of residuals with TESS S27 #2. However, the uncertainty is 7 minutes, which is on the order of the standard deviation of the TTV of AU Mic; and therefore this comparison is not conclusive. TESS has a different cadence, different passband (less sensitive to spots), and a different precision, and is less suited to studying the effect of occulted spots in this case.

We stress that there is also considerable out-of-transit red noise, which is characteristic of stellar activity, and has an amplitude comparable to the red noise component which is specific to the transits. Therefore, the separation of red noise from flicker and from occulted surface features is impossible based on monochromatic transit observations only, and will be investigated in a future study involving ground-based follow up observations. Although the stellar spot map of AU Mic is unknown, the reoccurring stellar surface together with the repeating light-curve features nevertheless confirm that the observed TTVs have a dynamical origin.

5. Discussion

5.1. A 7:4 period commensurability between the stellar spin and the planet orbit

Low-order spin-orbit commensurability is not unexpected in exoplanets, but there are few systems known to exhibit this feature. A reason for the low number of detections could be the difficulty in measuring the precise rotational periods from long and continuous photometry. Typically, exoplanets in the original Kepler field are the best-suited systems for this kind of study. Presently, there is no universal theoretical framework to explain any example of a low-order spin-orbit commensurability.

Regardless of the difficulties, similar systems have been known for almost a decade. Walkowicz & Basri (2013) determined the rotational period of a large sample of KOI stars, and noted an overdensity at the 1:1 resonance in the $P_{\text{rot}} - P_{\text{orb}}$ parameter space, and possibly another one at 2:1. They remarked that the distribution is valid only for large planets; while there does not appear to be a relationship between stellar rotation and planetary orbital periods for planetary candidates smaller than $R_p = 6 R_{\oplus}$, candidates with $R_p > 6 R_{\oplus}$ tend to appear closer to a low-order commensurability.

Concerning the 1:1 commensurability, the interaction of the planet's magnetic field was suggested to enhance the activity at the stellar surface toward the planet (Lanza 2012). These latter authors also debated whether the motion of the spots truly reflects the stellar rotation in this case, or rather that they move on the stellar surface by following the planet. The example of Kepler-17 revealed a system that is close to a perfect 8:1 spin-orbit commensurability (Désert et al. 2011). Another intriguing case is Kepler-13, which was found to be in a 3:5 commensurabil-

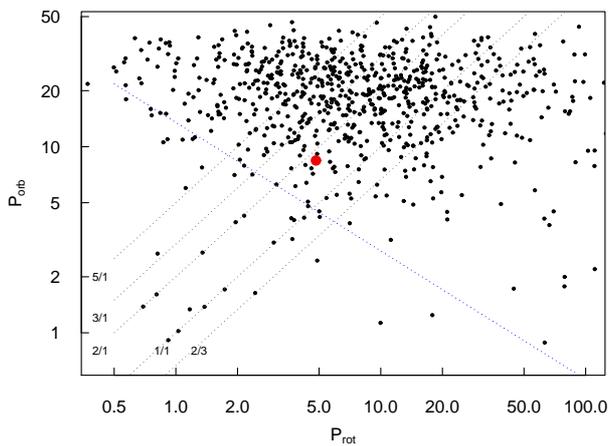


Fig. 10. Position of AU Mic (red dot) in the $P_{\text{rot}} - P_{\text{orb}}$ parameter space of Kepler exoplanets (small grey dots). The low-order spin-orbit commensurability ratios are shown by the black dotted lines. The lower envelope of the distribution (McQuillan et al. 2013) is plotted by the blue line.

ity (Szabó et al. 2012). In this system, the suspected reason was suggested to be a spin-orbit misalignment; at high latitudes of the orbit, the star and planet move together in a quasi-synchronous state for a considerable amount of time and, twice per rotation, the planet resides for 8 hours within 1 degree of one of the three distinguished longitudes. In the case of AU Mic, the explanation cannot be a spin-orbit misalignment, as we know that AU Mic b is aligned.

Another interesting feature is the dearth of close-in planets around rapid rotators, as recognised by McQuillan et al. (2013). These latter authors also determined the empirical boundary of the lower envelope of the allowed distribution. This is a purely empirical power law that confines the majority of exoplanets, with very few outliers being observed below it. In Fig. 10 we plot the sample of Kepler planets and the boundary according to McQuillan et al. (2013), and show the position of AU Mic b in this distribution. AU Mic b is near the edge of the densely populated area, but well within the identified boundary. Interestingly, AU Mic b is a small planet, smaller than the $6 R_{\oplus}$ limit (Walkowicz & Basri 2013), but the star is also smaller than most stars in the Kepler sample. Furthermore, there is an overdensity of planets in the lower left corner of Fig. 10 at low-order spin-orbit resonances. For clarity we show only some of them, noting that several other possible examples can be seen by eye.

The structure of exoplanets in the $P_{\text{rot}} - P_{\text{orb}}$ plane is completely unexplained. Here, AU Mic b occupies a key location that can help us to gain a better understanding of planet-star interactions in general. The extreme youth of AU Mic points to a speculative interpretation that the commensurability in this system was needed for the formation of the planet. Without a detailed theoretical explanation, we speculate that planet-star interactions may be more frequent than often recognised.

5.2. Transit timing variations explained by perturbations from the outer planet AU Mic c

Transit timing variations are commonly observed in multi-planet systems. The amplitude and period of TTVs is a complex question and a full solution can only be given if

the periods of both the perturbing and perturbed planets are known. In this section we show that the measured TTV amplitude of AU Mic b is compatible with the perturbations coming from the outer planet AU Mic c. Also, a rough estimate of its mass can be given from a TTV analysis.

Because of the scarce sampling of AU Mic transits, we have no exact information about the periodicity nor the full amplitude of the TTV. We can obtain a lower estimate of the fastest variation of TTV from the measured data. Certainly,

$$\max\left(\frac{dTTV}{dt}\right) = 2\pi \times \frac{A(TTV)}{P(TTV)}, \quad (3)$$

where $A(TTV)$ and $P(TTV)$ are the amplitude and the period of the TTV, and the formula makes use of simple basic properties of the sinusoid function.

The TTV signal is thoroughly determined by Lithwick et al. (2012); the general formulas for period and amplitude are provided in their Eqs. 7–8. The most important parameters are j , which measures the closest mean-motion resonance (in the form of $j : (j - 1)$), and Δ , the actual distance from the perfect resonance. Taking into account the period of AU Mic b and that of AU Mic c (18.858991 ± 0.000010 d, Martioli et al. (2021)), we get $j = 2$ and $\Delta = 0.114203$, which is precise to the last digit. Those together determine the superperiod, that is the period of the TTV. The ratio of the orbital period of the perturber and the superperiod is $j \times \Delta \approx 0.228$, and therefore the superperiod of a TTV signal from AU Mic c is expected to be 82.6 d.

The TTV amplitude is scaled by the f parameter which has an absolute value of around unity. In the case of $j = 2$, it can be calculated as $-1.190 + 2.20\Delta = -0.9387$ for AU Mic. During the gravitational interaction, the planets perturb each other's orbit predominantly through oscillations in eccentricity. This gives a correction to f which is summarised in the z_{free} parameter. This cannot be exactly determined unless all the orbital parameters of both planets are known. However, for the known Kepler planets, it is found that $z_{\text{free}} \ll \Delta$, and z_{free} usually means only a correction on the order of 10^{-4} to f . Assuming the same for AU Mic, the z_{free} correction can be neglected.

Substituting the exact value of f and $j = 2$ into Eq. 7 of Lithwick et al. (2012), and converting both sides to the form of Eq. 3 in the present paper, we get

$$2\pi \times \frac{A(TTV)}{P(TTV)} = 2\pi \frac{A(TTV)j\Delta}{P_c} = 2.36 \frac{P_b}{P_c} \mu_c, \quad (4)$$

where P and μ stand for orbital period and the planet-star mass ratio, and the b and c indices indicate the planets AU Mic b and c.

The left term of Eq. 4 is $\gtrsim 7.8 \times 10^{-5}$. Substituting the observed periods of AU Mic b and c into the right-hand side and the mass of AU Mic into the expression of μ , we finally get $M_c \approx 12 M_{\oplus}$. This value is only a rough estimate because we do not have information about the biases from the sparse sampling, but this result is numerically very compatible with the mass estimate for AU Mic c from its transit light curve, $2.2M_{\oplus} < M_c < 25.0M_{\oplus}$ (Martioli et al. 2021). This is evidence that the dominant factor in the TTV of AU Mic b is the perturbations from AU Mic c.

6. Summary

We present three transit observations of AU Mic b carried out with the CHEOPS space telescope, combined with the TESS light curves from Sectors 1 and 27. We analysed the transits with two different methods, which include a GP regression (`pycheops`) and a wavelet-based approach (TLCM). We summarise our results below.

- By combining the CHEOPS and TESS transit light curves, we measured an orbital period for AU Mic b of $P_{\text{orb}} = 8.462995 \pm 0.000003$ d, which confirms the previous estimate presented by Martioli et al. (2021). The modelling of the three CHEOPS transits using `pycheops` and TLCM provides a planetary radius of $R_{\text{p,pycheops}} = 4.36 \pm 0.18 R_{\oplus}$ and $R_{\text{p,TLCM}} = 4.38 \pm 0.05 R_{\oplus}$, respectively. These results agree within 3σ with the values found by Plavchan et al. (2020) and by Martioli et al. (2021). The result that we obtained using TLCM is two times more precise than previous estimates.
- Spot-crossing events and red noise arising from stellar activity affect the transit parameters. We derived bootstrap accuracy values of 5.5% for the transit depth, 3 minutes for the transit mid-time, and 4.2 minutes for the transit duration. The derived accuracy is consistent with the observed variation of the transit parameters retrieved from the three individual CHEOPS transits. We also find systematic variations in the transit depth that seem to correlate with the star’s brightness, with the deepest transits observed around the photometric minima of the star. These variations are very likely induced by spots that are not spatially located along the transit chord. This will be the subject of a forthcoming separate paper.
- We measured a photometric period of $P_{\text{rot}} = 4.8367 \pm 0.0006$ d, reflecting the stellar rotation and the brightness variation coming from spots close to the equator. This period is in a 7:4 commensurability with the orbital period of AU Mic b. As it takes 1.75 stellar rotations for AU Mic b to complete one orbit around its host star, the transits can only occur at four specific stellar longitudes. We have observations from three of the possible geometrical configurations.
- Because of the 7:4 commensurability between the rotation period of the star and the orbital period of the planet, during the second and third CHEOPS transits AU Mic b crossed the same stellar surface. We find that the two transits exhibit the same sequence of dark and bright spot-crossing events. We used these events to measure the TTV and found a variation of ~ 3.9 minutes on a baseline of 33 days. The presence of an outer perturber such as AU Mic c can account for the observed TTV.

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References

- Addison, B. C., Horner, J., Wittenmyer, R. A., et al. 2020, arXiv e-prints, arXiv:2006.13675
- Barragán, O., Gandolfi, D., & Antoniciello, G. 2019, *MNRAS*, 482, 1017
- Barros, S. C. C., Boué, G., Gibson, N. P., et al. 2013, *MNRAS*, 430, 3032
- Benz, W., Broeg, C., Fortier, A., et al. 2021, *Experimental Astronomy*, 51, 109
- Berdyugina, S. V. 2007, *Mem. Soc. Astron. Italiana*, 78, 242
- Boisse, I., Bonfils, X., & Santos, N. C. 2012, *A&A*, 545, A109
- Bonfanti, A., Delrez, L., Hooton, M. J., et al. 2021, arXiv e-prints, arXiv:2101.00663
- Box, G. P. E. & Jenkins, G. M. 1976, in *Holden-Day Series in Time Series Analysis*
- Brown, T. M., Charbonneau, D., Gilliland, R. L., Noyes, R. W., & Burrows, A. 2001, *ApJ*, 552, 699
- Carter, J. A. & Winn, J. N. 2009, *ApJ*, 704, 51
- Csizmádia, S. 2020, *MNRAS*, 496, 4442
- Dai, F. & Winn, J. N. 2017, *AJ*, 153, 205
- Dai, F., Winn, J. N., Yu, L., & Albrecht, S. 2017, *AJ*, 153, 40
- Désert, J.-M., Charbonneau, D., Demory, B.-O., et al. 2011, *ApJS*, 197, 14
- Dumusque, X., Boisse, I., & Santos, N. C. 2014, *ApJ*, 796, 132
- Espinoza, N., Rackham, B. V., Jordán, A., et al. 2019, *MNRAS*, 482, 2065
- Gaia Collaboration, Brown, A. G. A., Vallenari, A., et al. 2018, *A&A*, 616, A1
- Hirano, T., Krishnamurthy, V., Gaidos, E., et al. 2020, *ApJ*, 899, L13
- Hoyer, S., Guterman, P., Demangeon, O., et al. 2020, *A&A*, 635, A24
- Kalas, P., Liu, M. C., & Matthews, B. C. 2004, *Science*, 303, 1990
- Kiraga, M. 2012, *Acta Astron.*, 62, 67
- Klein, B., Donati, J.-F., Moutou, C., et al. 2021, *MNRAS*, 502, 188
- Lagrange, A. M., Desort, M., & Meunier, N. 2010, *A&A*, 512, A38
- Lanza, A. F. 2012, *A&A*, 544, A23
- Lanza, A. F., Boisse, I., Bouchy, F., Bonomo, A. S., & Moutou, C. 2011, *A&A*, 533, A44
- Lanza, A. F., Pagano, I., Leto, G., et al. 2009, *A&A*, 493, 193
- Lendl, M., Csizmádia, S., Deline, A., et al. 2020, *A&A*, 643, A94
- Lithwick, Y., Xie, J., & Wu, Y. 2012, *ApJ*, 761, 122
- Mamajek, E. E. & Bell, C. P. M. 2014, *MNRAS*, 445, 2169
- Mandel, K. & Agol, E. 2002, *ApJ*, 580, L171
- Martíoli, E., Hébrard, G., Correia, A. C. M., Laskar, J., & Lecavelier des Etangs, A. 2021, *A&A*, 649, A177
- Martíoli, E., Hébrard, G., Moutou, C., et al. 2020, *A&A*, 641, L1
- Mathioudakis, M. & Doyle, J. G. 1991, *A&A*, 244, 433
- Maxted, P. F. L. & Gill, S. 2019, *A&A*, 622, A33
- Mazeh, T., Holczer, T., & Shporer, A. 2015, *ApJ*, 800, 142
- McQuillan, A., Mazeh, T., & Aigrain, S. 2013, *ApJ*, 775, L11
- McQuillan, A., Mazeh, T., & Aigrain, S. 2014, *ApJS*, 211, 24
- Miret-Roig, N., Galli, P. A. B., Brandner, W., et al. 2020, *A&A*, 642, A179
- Močnik, T., Clark, B. J. M., Anderson, D. R., Hellier, C., & Brown, D. J. A. 2016, *AJ*, 151, 150
- Močnik, T., Southworth, J., & Hellier, C. 2017, *MNRAS*, 471, 394
- Murdoch, K. A., Hearnshaw, J. B., & Clark, M. 1993, *ApJ*, 413, 349
- Nutzman, P. A., Fabrycky, D. C., & Fortney, J. J. 2011, *ApJ*, 740, L10
- Palle, E., Oshagh, M., Casasayas-Barris, N., et al. 2020, *A&A*, 643, A25
- Plavchan, P., Barclay, T., Gagné, J., et al. 2020, *Nature*, 582, 497
- Pojmanski, G. 1997, *Acta Astron.*, 47, 467
- Pont, F., Knutson, H., Gilliland, R. L., Moutou, C., & Charbonneau, D. 2008, *MNRAS*, 385, 109
- Rosich, A., Herrero, E., Mallonn, M., et al. 2020, *A&A*, 641, A82
- Saleh Ahmar, A., Daengs GS, A., Listyorini, T., et al. 2018, in *Journal of Physics Conference Series*, Vol. 1028, *Journal of Physics Conference Series*, 012189
- Sanchis-Ojeda, R. & Winn, J. N. 2011, *ApJ*, 743, 61
- Sanchis-Ojeda, R., Winn, J. N., Holman, M. J., et al. 2011, *ApJ*, 733, 127
- Sasselov, D. D., Basri, G., Marcy, G., et al. 2010, in *American Astronomical Society Meeting Abstracts*, Vol. 215, *American Astronomical Society Meeting Abstracts #215*, 317.07
- Savanov, I. S. 2011, *Astronomy Reports*, 55, 341
- Silva-Valio, A., Lanza, A. F., Alonso, R., & Barge, P. 2010, *A&A*, 510, A25
- Sousa, S. G., Adibekyan, V., Delgado-Mena, E., et al. 2018, *A&A*, 620, A58
- Sterken, C. 2005, in *Astronomical Society of the Pacific Conference Series*, Vol. 335, *The Light-Time Effect in Astrophysics: Causes and cures of the O-C diagram*, ed. C. Sterken, 3
- Strassmeier, K. G. 2009, *A&A Rev.*, 17, 251
- Stumpe, M. C., Smith, J. C., Van Cleve, J. E., et al. 2012, *PASP*, 124, 985
- Szabó, G. M., Pál, A., Derekas, A., et al. 2012, *MNRAS*, 421, L122
- Tognelli, E., Prada Moroni, P. G., & Degl’Innocenti, S. 2011, *A&A*, 533, A109
- Torres, C. A. O., Quast, G. R., da Silva, L., et al. 2006, *A&A*, 460, 695
- Walkowicz, L. M. & Basri, G. S. 2013, *MNRAS*, 436, 1883
- White, R., Schaefer, G., Boyajian, T., et al. 2019, in *American Astronomical Society Meeting Abstracts*, Vol. 233, *American Astronomical Society Meeting Abstracts #233*, 259.41
- Wisniewski, J. P., Kowalski, A. F., Davenport, J. R. A., et al. 2019, *ApJ*, 883, L8
- Zechmeister, M. & Kürster, M. 2009, *A&A*, 496, 577

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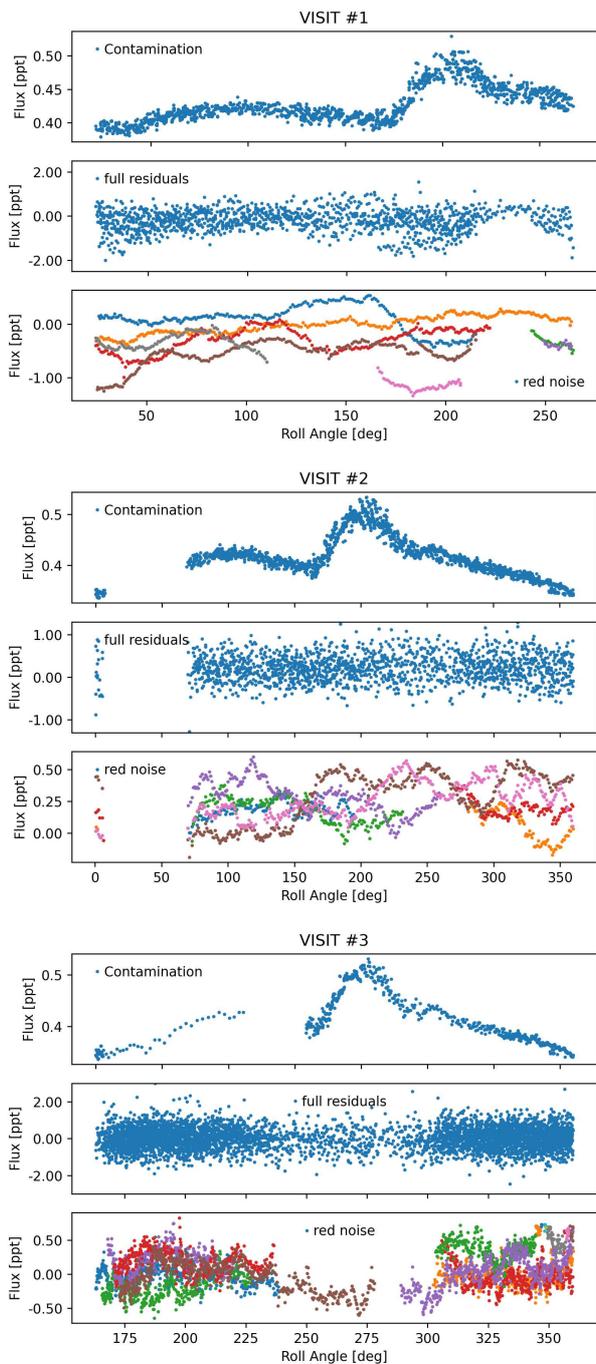


Fig. .1. The comparison of light contamination due to the rotation of the telescope (top panels), the local scatter (middle panels) and the shape (bottom panel) of red noise as a function of the roll angle. The different colours correspond to different orbits. The data are well calibrated for roll angle systematics which do not survive significantly in the red noise components of the fit residuals.

Appendix A: Transit depth and transit times for the individual transits with `pyaneti`

Table .1 shows the transit times, transit depths, and radius parameters fitted by `pyaneti` for individual transits involved in the analysis in this paper. We compare the derived minimum times to those of Martioli et al. (2020), and they are general within one error interval. We also have to

note that the errors in Table .1 are derived from massive bootstraps, as described in Section 4.1. and Section 4.3. Bootstrap errors estimate the non-linear biases from noise correlations, and hence, they can be significantly larger than errors from the MCMC statistical fits. In the case of MCMC, the statistical errors show how far our acceptable solutions spread out from the best fit—the best fit itself can be biased due to noise correlations, too—while the bootstrap tells us how far the best fit can be from the physical parameter set. Therefore, the two error definitions are very different, and cannot be compared directly.

Appendix B: Determination of roll-angle systematics and the accuracy in planet parameters

Table .2 shows the value of roll-angle systematics from the TLCM solutions. The coefficients belong to a fourth-order polynomial in the form of $\sum \sin_i(i \times \alpha) + \cos_i(i \times \alpha)$, where α is the roll angle.

Figure .1 shows the predicted photometry systematics from the rotation of the telescope (with a period of 97.8 minutes) and the varying scattered light inside the aperture (top panels) for the three CHEOPS visits. These values are the output of the field star modelling algorithm in the CHEOPS DRP, which takes into account the nearby stars and the rotation of the telescope (Hoyer et al. 2020). This pattern is compared to the scatter (middle panel) and the shape (bottom panel) of the red noise decomposed by the TLCM algorithm from the fit residuals. We can see that the red noise highly exceeds the pattern of scattered light, while the predicted pattern does not repeat in the residuals at all.

We also performed a correlation analysis using the plotted data. We compared the predicted contamination of scattered light with the measured and separated red noise component at the same time in the actual measurements. We found very low correlation coefficients of +0.02 (CHEOPS #1 and CHEOPS #2) and +0.03 (CHEOPS #3), while the value of exact 0.0 is in the 95% and 98% confidence intervals, respectively. This shows that the calibration and removal of rolling systematics has been done properly, and the red noise pattern we detect is not related to instrument systematics.

Table .1. Transit times, transit depth, and relative planet radius derived from individual CHEOPS and TESS measurements with `pyaneti`. For comparison, we show the derived transit times of Martioli et al. (2021) converted to BJD, with their published statistical MCMC errors. Our errors are precision values derived by parametric bootstraps, the errors in Martioli et al. are MCMC statistical errors describing the core 35% of the distribution.

Transit	T_t (BJD) [This paper]	R_p/R_* [<code>pyaneti</code>]	T_t (BJD) [Martioli et al. (2021)]
CHEOPS #1	2459041.2828±0.0006	0.0541±0.0002	—
CHEOPS #2	2459083.5970±0.0004	0.0520±0.0002	—
CHEOPS #3	2459117.4515±0.0008	0.0515±0.0002	—
TESS S1#1	2458330.3911±0.0008	0.0546±0.0004	2458330.39046±0.00016
TESS S1#2	2458347.3174±0.0008	0.0565±0.0005	2458347.31646±0.00016
TESS S27#1	2459041.2816±0.0008	0.0517±0.0003	2459041.28238±0.00026
TESS S27#2	2459049.7457±0.0008	0.0582±0.0003	2459049.74538±0.00026
TESS S27#3	2459058.20795±0.0008	0.0548±0.0004	2452058.20838±0.00026

Table .2. Value of roll angle systematics from the TLCM solutions. Values are given in ppm.

	CHEOPS #1	
cos ₁ , sin ₁	79 + 78/ - 78	208 + 132/ - 141
cos ₂ , sin ₂	312 + 104/ - 104	9 + 104/ - 104
cos ₃ , sin ₃	146 + 69/ - 75	-257 + 78/ - 75
cos ₄ , sin ₄	0 + 47/ - 46	-94 + 46/ - 46
	CHEOPS #2	
cos ₁ , sin ₁	-54 + 40/ - 30	30 + 53/ - 55
cos ₂ , sin ₂	47 + 40/ - 41	29 + 32/ - 33
cos ₃ , sin ₃	69 + 30/ - 29	41 + 33/ - 33
cos ₄ , sin ₄	-37 + 29/ - 29	47 + 29/ - 29
	CHEOPS #3	
cos ₁ , sin ₁	92 + 46/ - 49	-249 + 140/ - 151
cos ₂ , sin ₂	-400 + 109/ - 132	-3 + 63/ - 59
cos ₃ , sin ₃	-19 + 64/ - 59	112 + 84/ - 79
cos ₄ , sin ₄	215 + 46/ - 46	36 + 44/ - 48