



## **Rôle de la zone endommagée sur la convergence des galeries de stockage, modélisation numérique d'expériences dans le laboratoire souterrain de Bure**

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## Long-term management of radioactive wastes



Intermediate  
(long-lived)  
&  
high activity  
wastes

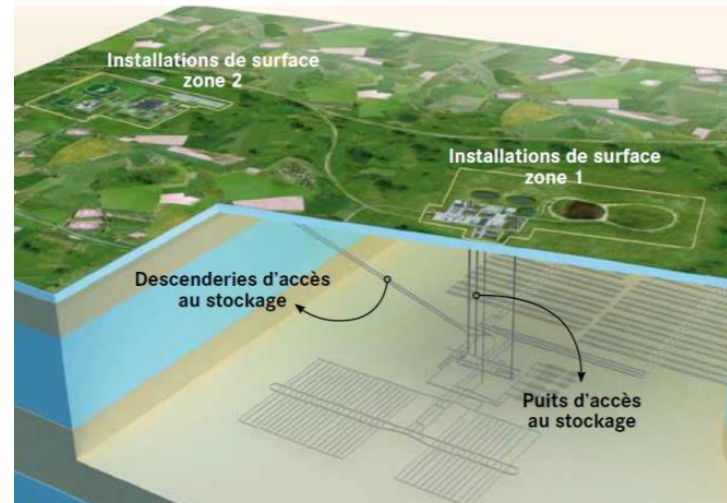


### Deep geological disposal

Repository in deep geological media with good confining properties

(Low permeability  
 $K < 10^{-12}$  m/s)

Underground structures  
= network of galleries

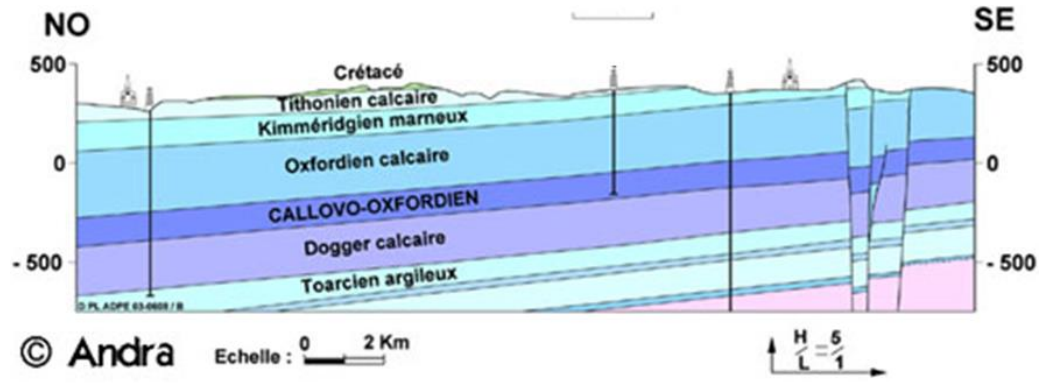


Disposal facility of Cigéo project in France  
(Labalette et al., 2013)

# 1. Context

## Callovo-Oxfordian claystone (COx)

Sedimentary clay rock (France).



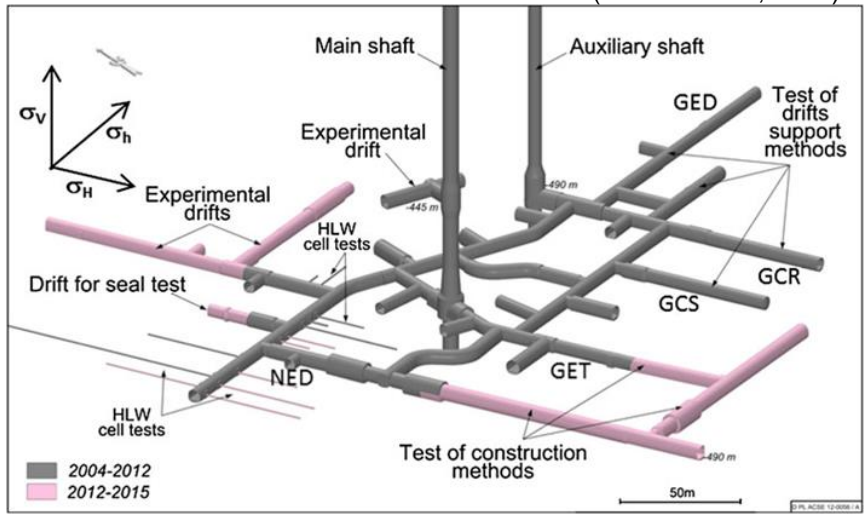
Borehole core samples (Andra, 2005)

- Underground research laboratory

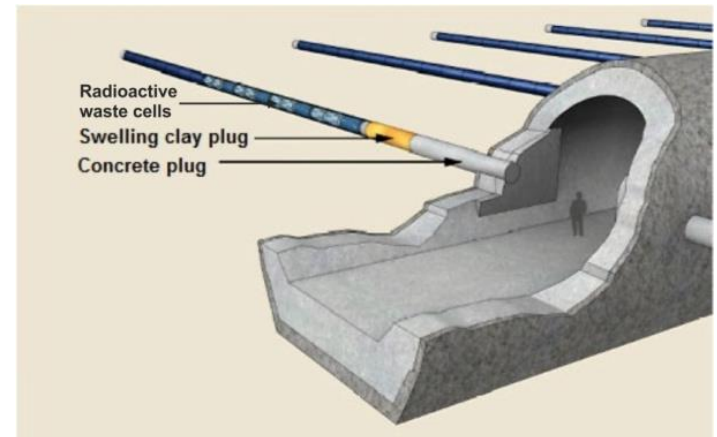
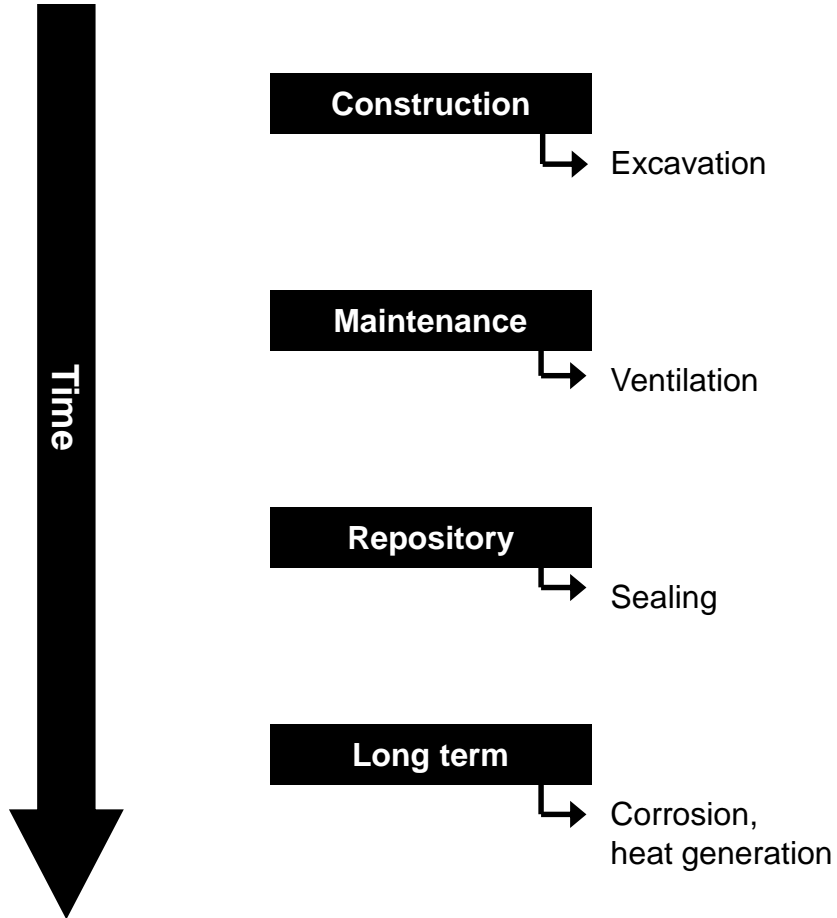
Feasibility of a safe repository

France (Meuse / Haute-Marne, Bure)

(Armand et al., 2014)



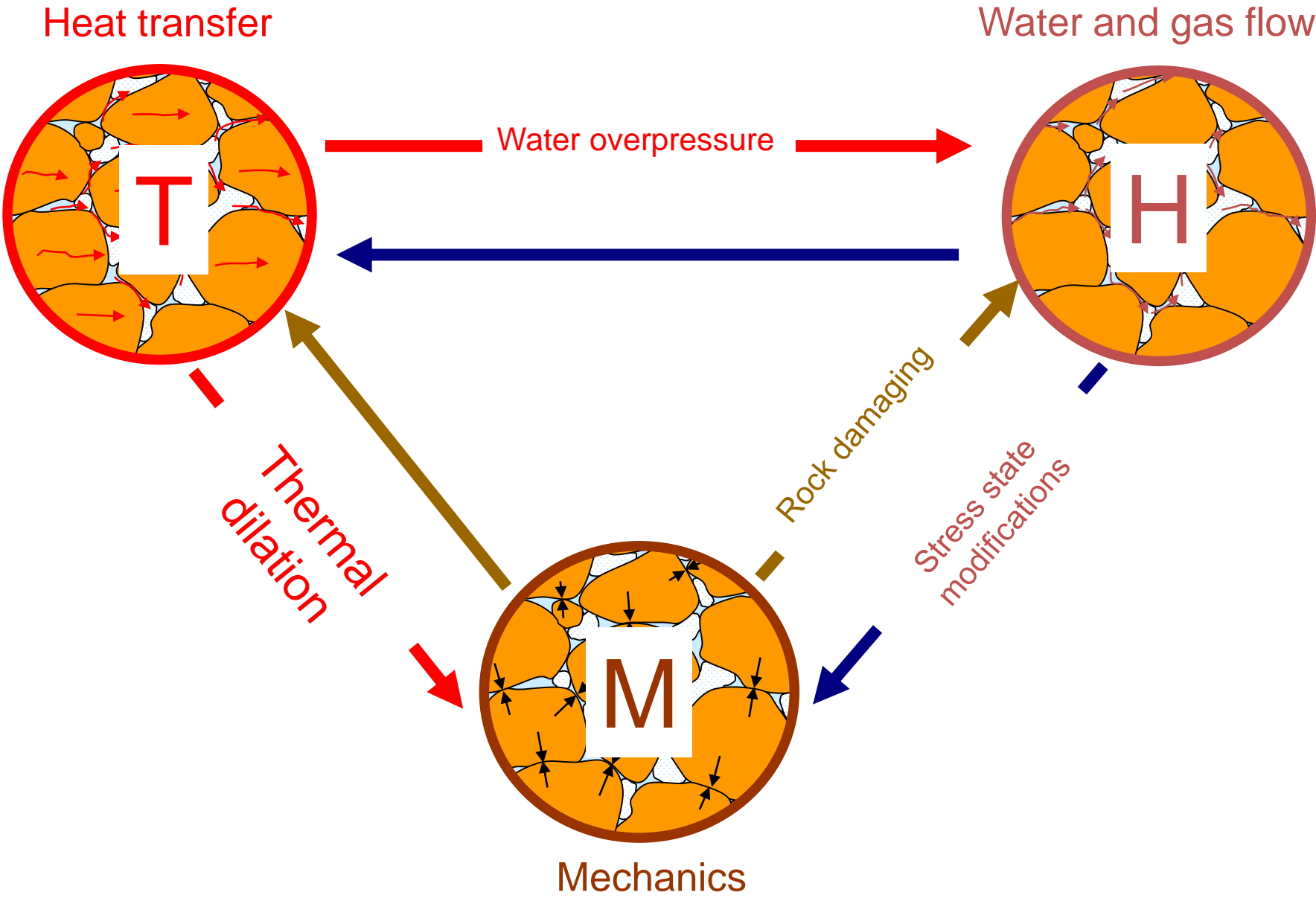
## Repository phases



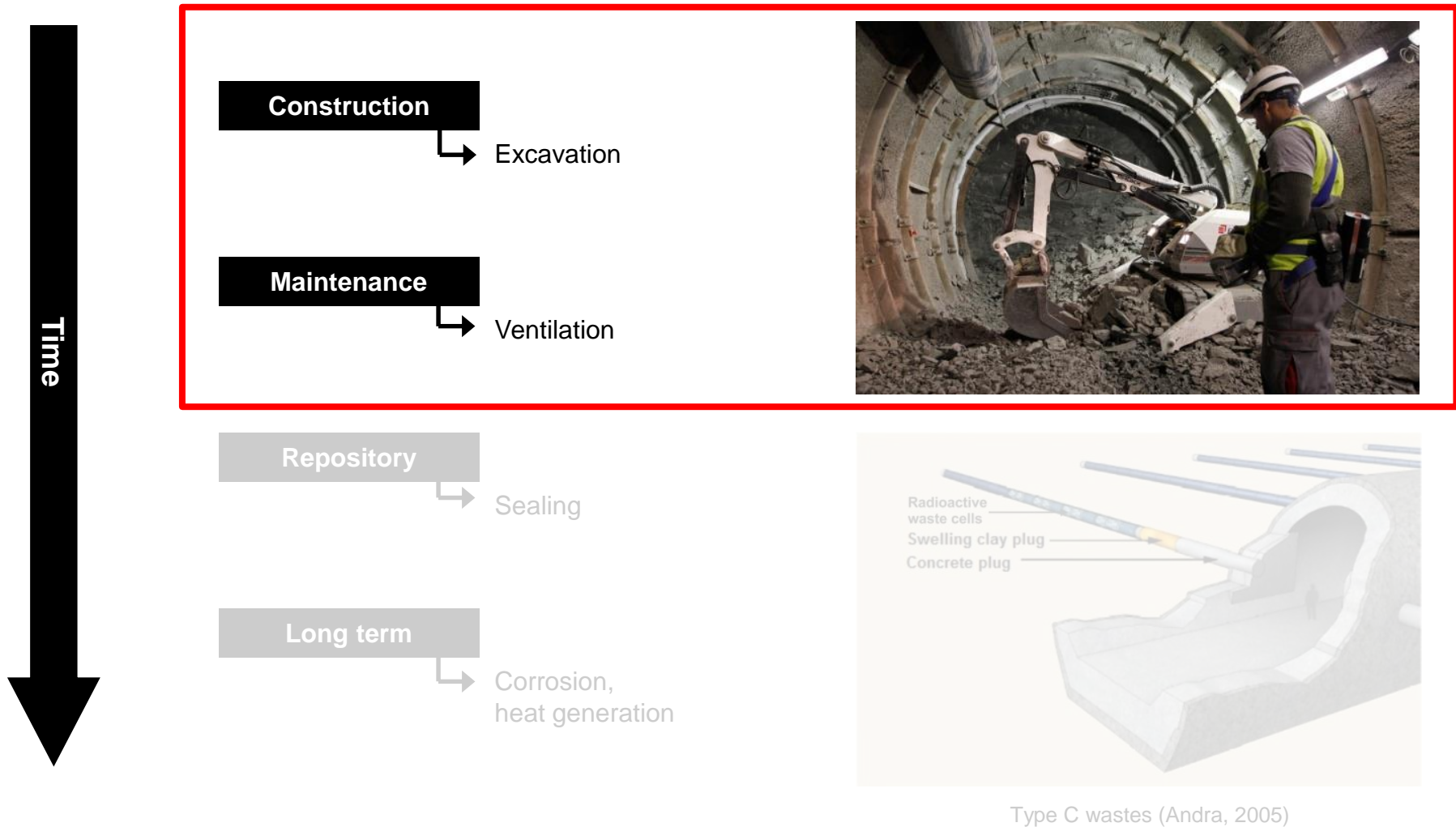
Type C wastes (Andra, 2005)



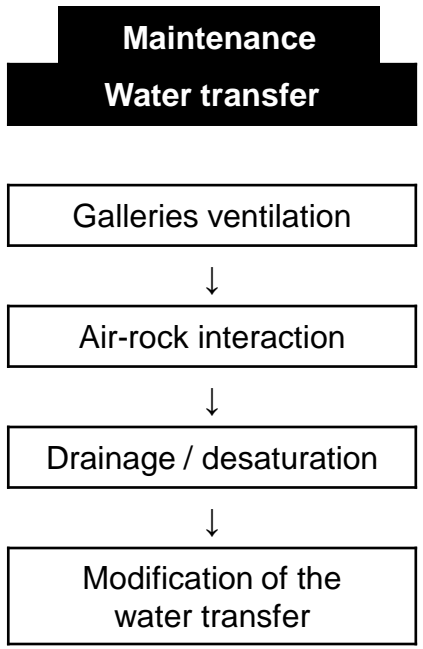
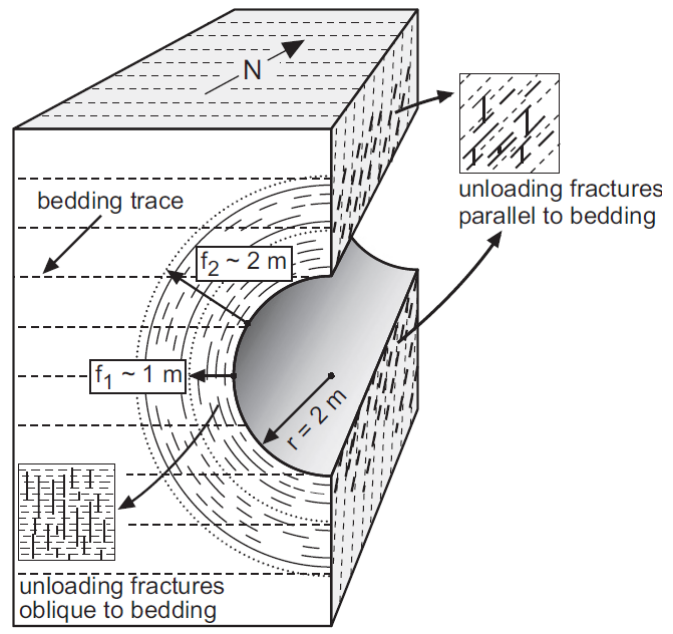
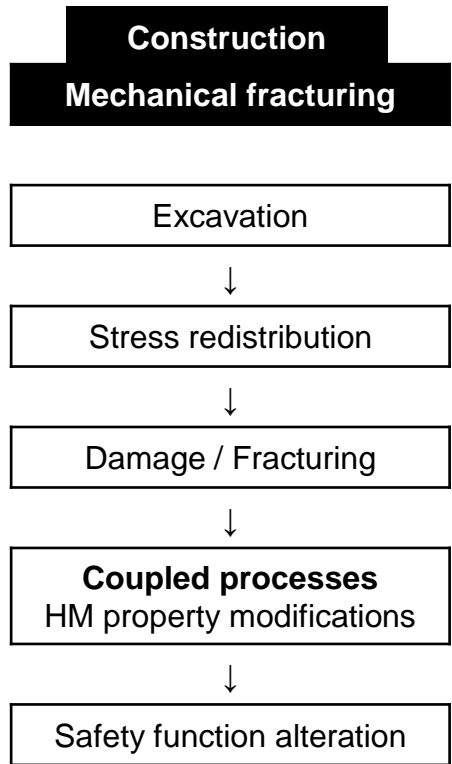
# 1. Context



## Repository phases



## Excavation Damaged Zone (EDZ)



Fracturing & permeability increase  
(several orders of magnitude)

Opalinus clay in Switzerland  
(Bossart et al., 2002)

# 1. Context

## - Fracturing

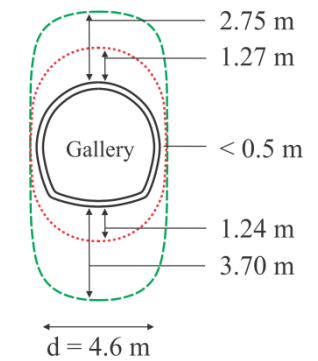
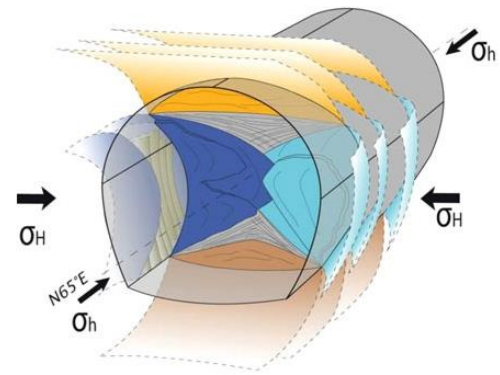
Anisotropies: - stress :  $\sigma_H > \sigma_h \sim \sigma_v$

- material : HM cross-anisotropy.

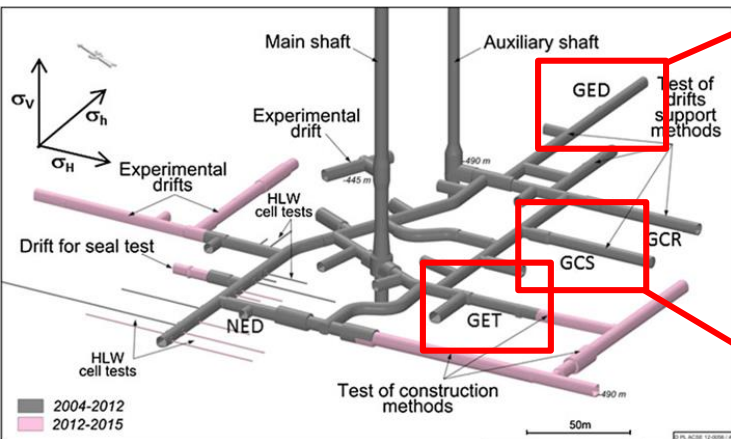
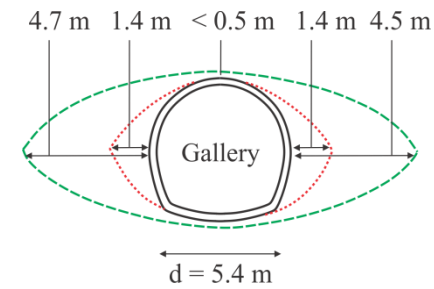
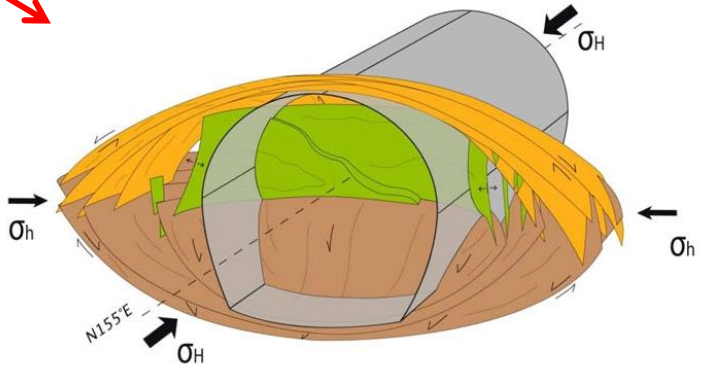
(Armand et al., 2014)

--- Shear fractures  
 - - - Mixed fractures

Galery // to  $\sigma_h$



Galery // to  $\sigma_H$



Issues: Prediction of the fracturing.  
 Effect of anisotropies ?  
 Permeability evolution & relation to fractures ?

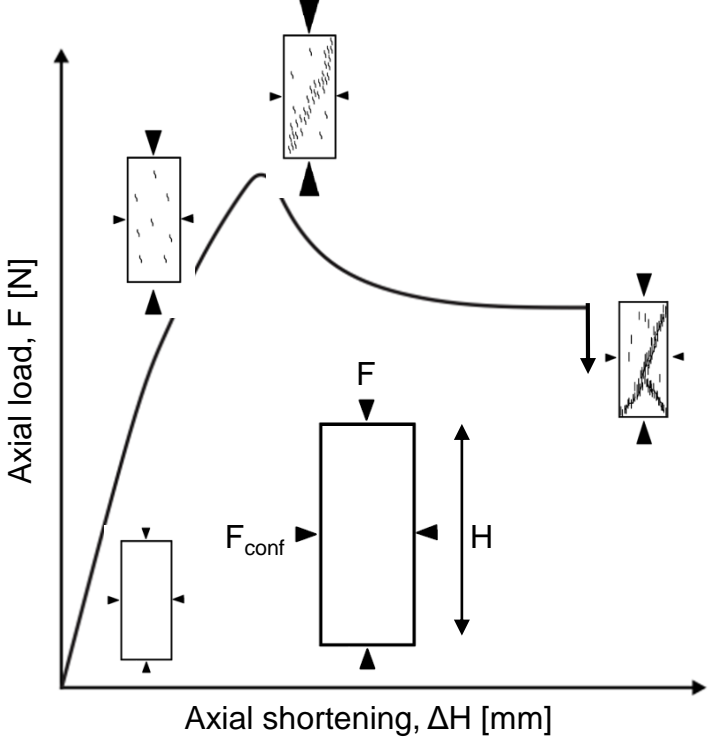
1. Context
2. **Fracture modelling with shear bands**
3. Influence of mechanical anisotropy
4. Permeability evolution and water transfer
5. Conclusions and perspectives



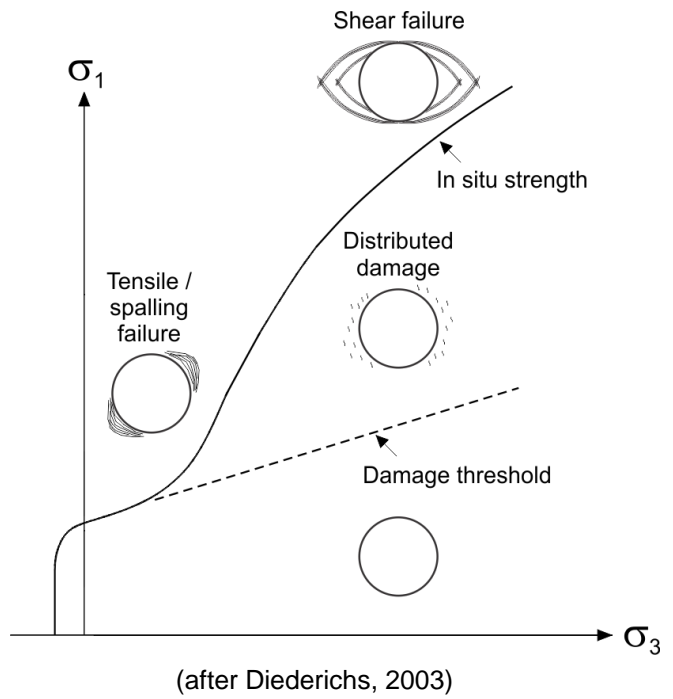
# 2. Fracture modelling with shear bands

## 2.1. Material rupture

- Compression test on small sample



- Mechanisms of rock mass failure around gallery



- Fracture modelling

Shear bands are observed in many geomaterials.

COx : 75% of fractures in mode II (shear).



Shear strain localisation (continuous approach)

## 2. Fracture modelling with shear bands

### 2.2. Constitutive models for COx

- Mechanical law - 1st gradient model

Isotropic elasto-plastic internal friction model

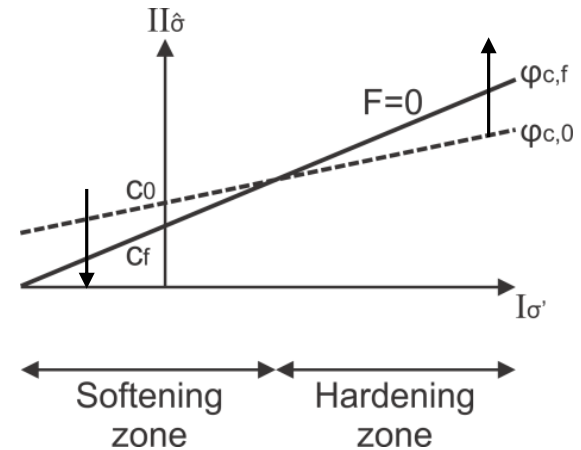
Non-associated plasticity, Van Eeckelen yield surface :

$$F \equiv II_{\hat{\sigma}} - m \left( I_{\sigma'} + \frac{3c}{\tan \varphi_c} \right) = 0$$

$\varphi$  hardening /  $c$  softening

$$c = c_0 + \frac{(c_f - c_0) \hat{\epsilon}_{eq}^p}{B_c + \hat{\epsilon}_{eq}^p}$$

→ Strain localisation



- Hydraulic law

Fluid mass flow (advection, Darcy) :

$$f_{w,i} = -\rho_w \frac{k_{w,ij} k_{r,w}}{\mu_w} \left( \frac{\partial p_w}{\partial x_j} + \rho_w g_j \right)$$

Water retention and permeability curves (Mualem - Van Genuchten's model)

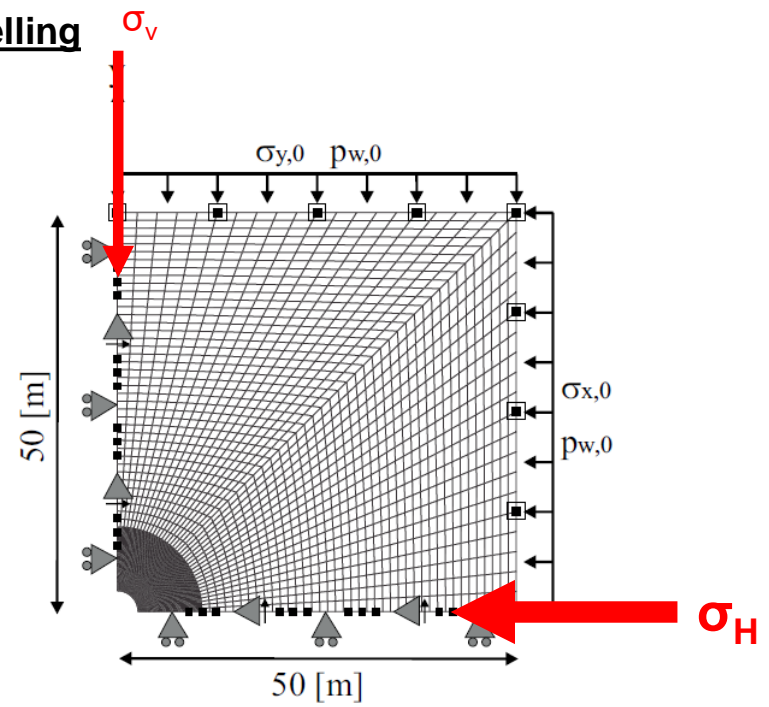
# 2. Fracture modelling with shear bands

## 2.3. Gallery excavation modelling

- Numerical model

HM modelling in 2D  
plane strain state

Gallery radius = 2.3 m



- ▣ Drained boundary
- ▣ Impervious boundary
- ← Constant total stress
- ⊕ Constrained displacement
- ⊕ Constrained normal derivative of the radial displacement

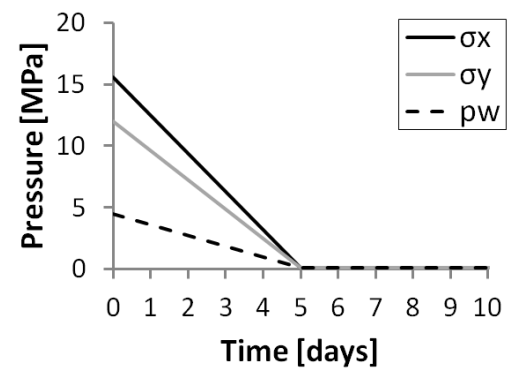
- Gallery in COx //  $\sigma_h$

**Effect of stress anisotropy**

Anisotropic stress state

$p_{w,0} = 4.5$  [MPa]  
 $\sigma_{x,0} = \sigma_H = 1.3 \sigma_v = 15.6$  [MPa]  
 $\sigma_{y,0} = \sigma_v = 12$  [MPa]  
 $\sigma_{z,0} = \sigma_h = 12$  [MPa]

- Excavation



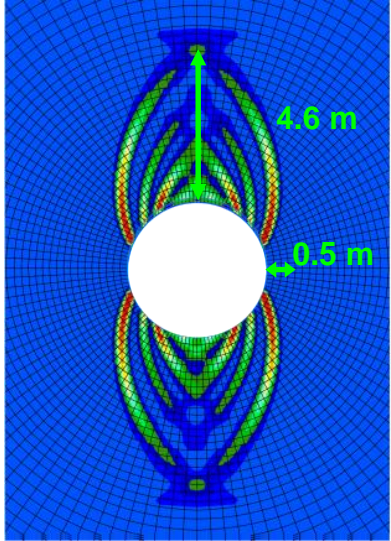
# 2. Fracture modelling with shear bands

- Localisation zone

Incompressible solid grains,  $b=1$

1000 days  
End of excavation

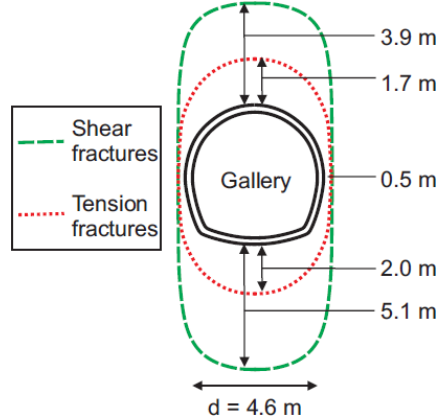
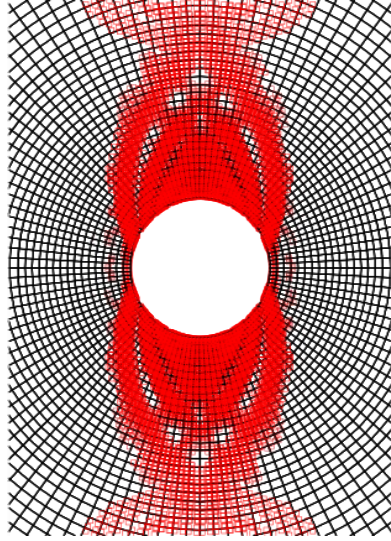
Total deviatoric strain



$$\hat{\epsilon}_{eq} = \sqrt{\frac{2}{3} \hat{\epsilon}_{ij} \hat{\epsilon}_{ij}}$$

0 0.06

Plasticity



→ For an isotropic mechanical behaviour, the appearance and shape of the strain localisation are mainly due to mechanical effects linked to the anisotropic stress state.

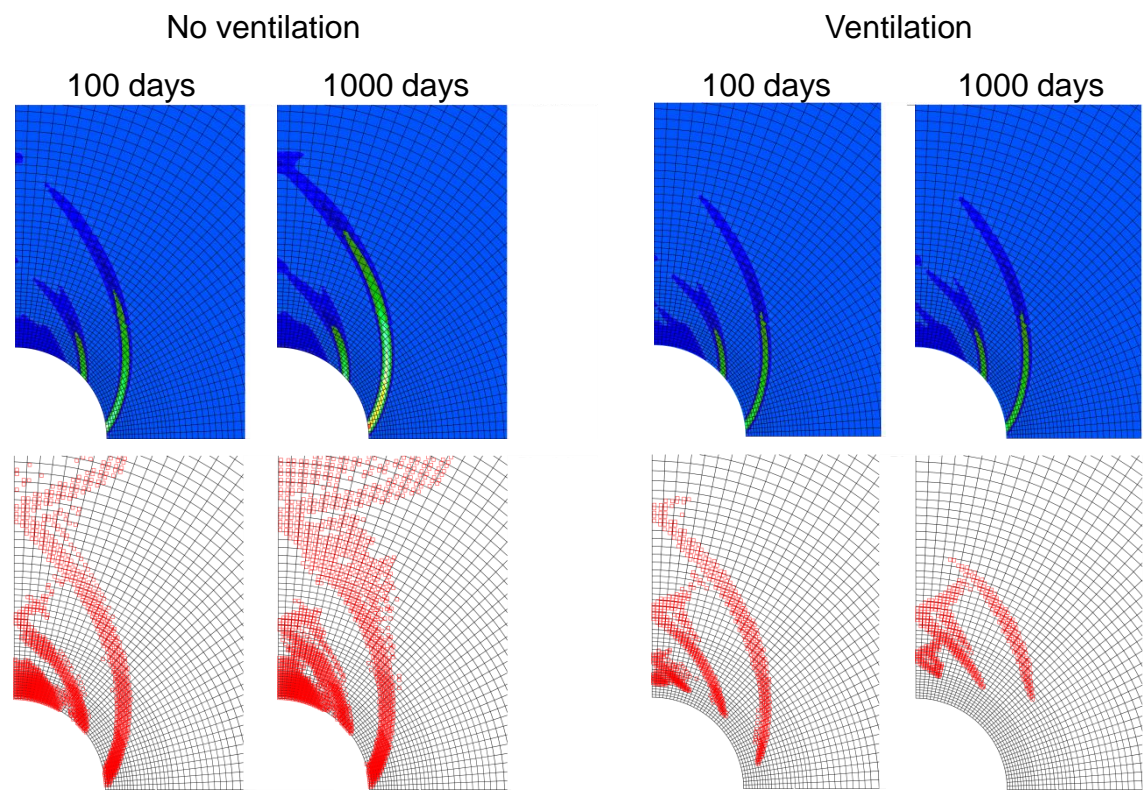
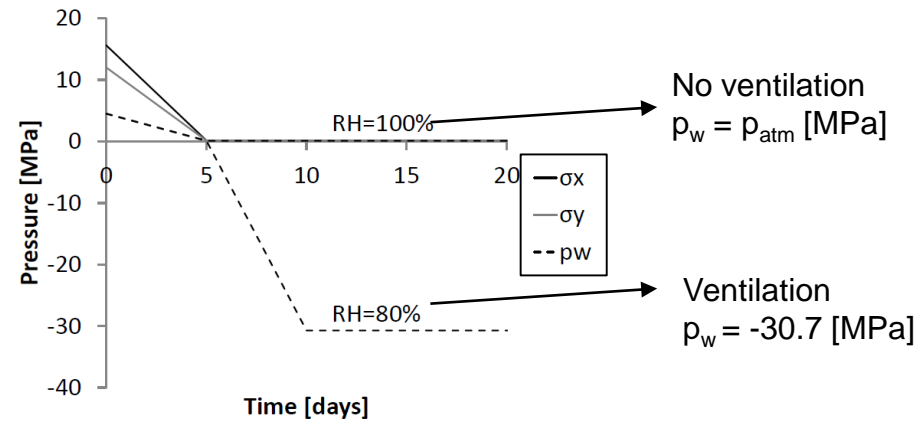
# 2. Fracture modelling with shear bands

- Gallery air ventilation :

Water phases equilibrium at gallery wall (Kelvin's law)

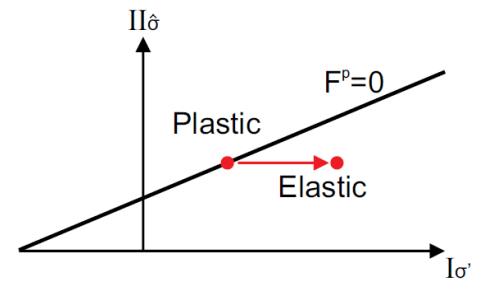
$$RH = \frac{p_v}{p_{v,0}} = \exp\left(\frac{-p_c M_v}{RT \rho_w}\right)$$

Compressibility of the solid grains:  $b=0.6$



$$\sigma_{ij} = \sigma'_{ij} + b S_{r,w} p_w \delta_{ij}$$

- suction ↑
- $\sigma' \uparrow$
- Elastic unloading
- Inhibition of localisation
- Restrain  $\epsilon$

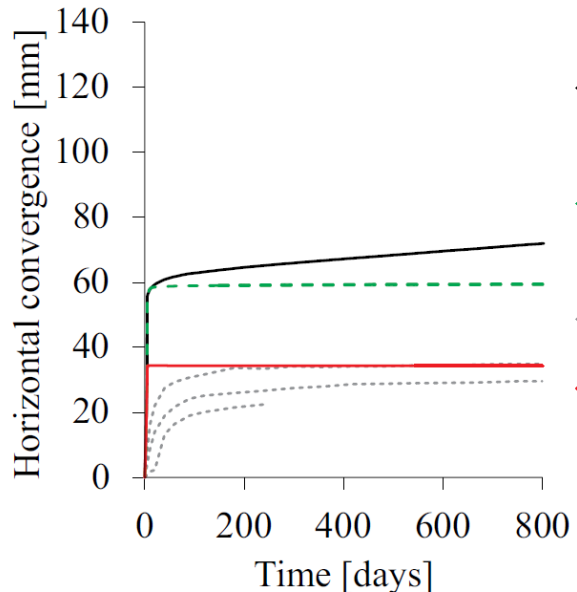
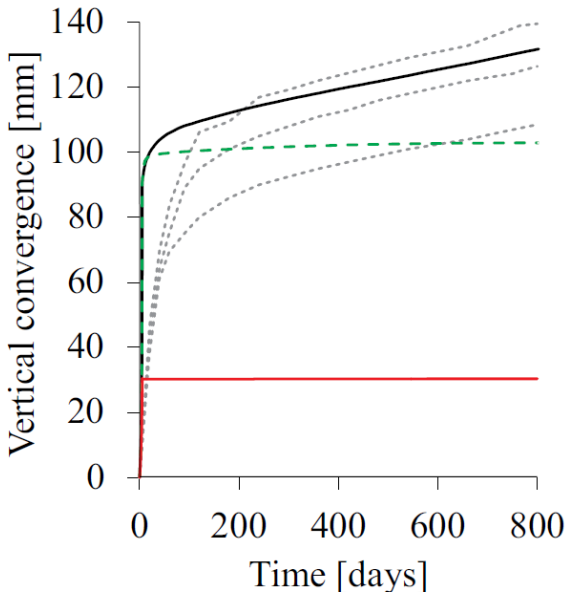
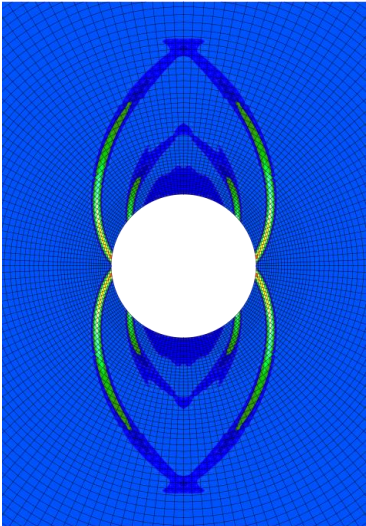




# 2. Fracture modelling with shear bands

## - Convergence:

- Important during the excavation
- Anisotropic convergence
- Influence of the ventilation
- Experimental results (GED - Andra's URL)
- No strain localisation



- Numerical, RH=100%, no ventilation
- - Numerical, RH=80%, ventilation
- ... Experimental, GED
- Numerical, no strain localisation, RH=80%, ventilation

## 2. Fracture modelling with shear bands

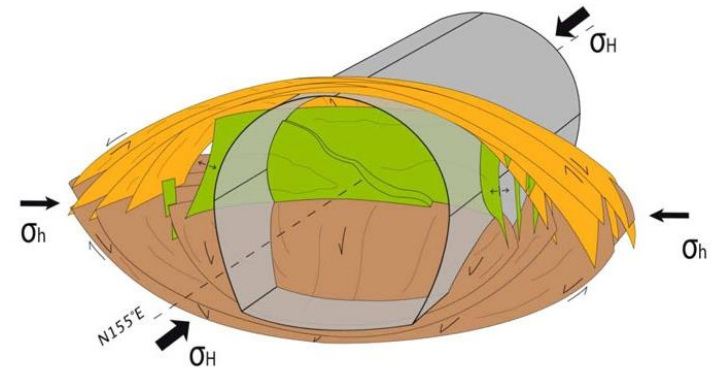
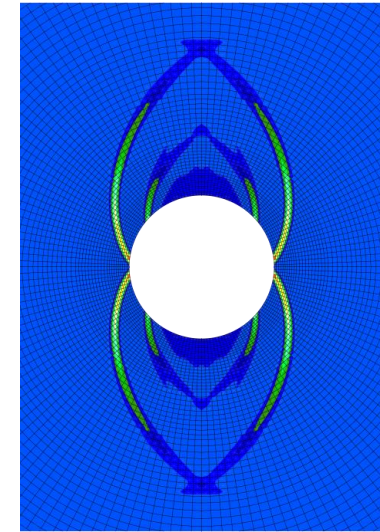
### 2.5. Conclusions and outlooks

#### - Conclusions

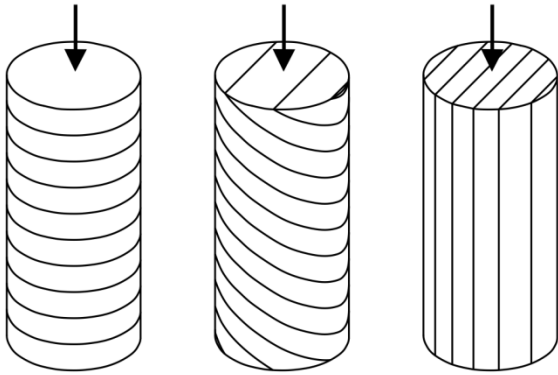
- ✓ Reproduction of EDZ with shear bands.
- ✓ Shape and extent of EDZ **governed by anisotropic stress state.**

#### - Next steps ...

- X Mechanical rock behaviour.  
→ Material anisotropy, gallery //  $\sigma_H$ .
- X HM coupling in EDZ.  
→ Influence of fracturing on hydraulic properties.
- X Gallery air ventilation and water transfer (drainage / desaturation).



### 3. Influence of mechanical anisotropy



- Linear elasticity :

Cross-anisotropic (5 param.) + Biot's coefficients

$$E_{//}, E_{\perp}, \nu_{//}, \nu_{//\perp}, G_{//\perp} \quad b_{//}, b_{\perp}$$

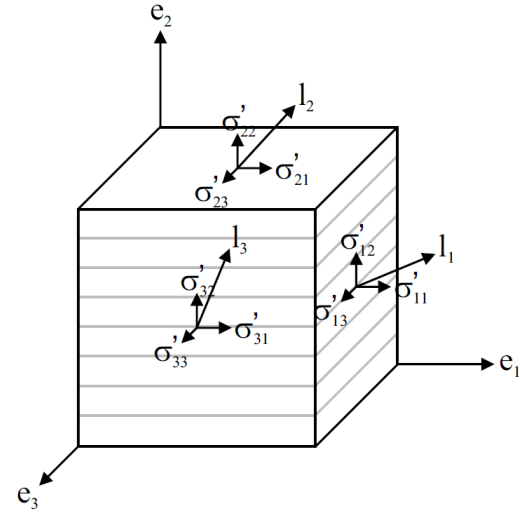
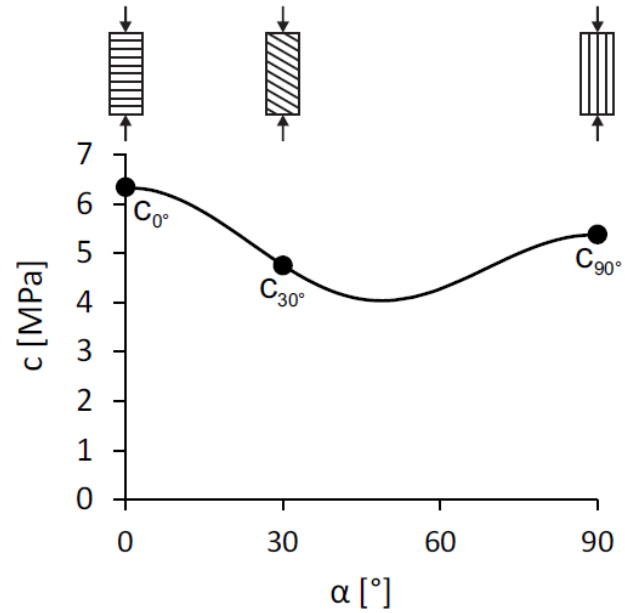
- Plasticity :

Cohesion anisotropy with fabric tensor

$$c_0 = a_{ij} l_i l_j \quad l_i = \sqrt{\frac{\sigma_{i1}'^2 + \sigma_{i2}'^2 + \sigma_{i3}'^2}{\sigma_{ij}' \sigma_{ij}'}}$$

Cross-anisotropy

$$c_0 = \bar{c} \left( 1 + A_{//} (1 - 3l_2^2) + b_1 A_{//}^2 (1 - 3l_2^2)^2 + \dots \right)$$



# 3. Influence of mechanical anisotropy

## 3.3. Gallery excavation modelling for anisotropic initial stress state

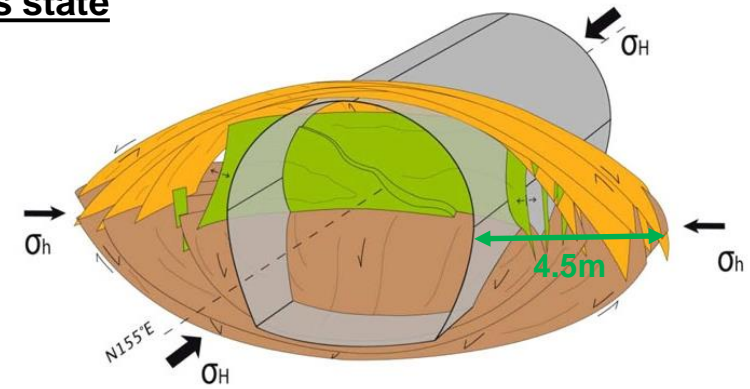
### - Stress state

Major stress in the axial direction  
 Gallery // to  $\sigma_H$

$$\sigma_{x,0} = \sigma_h = 12.40 \text{ MPa}$$

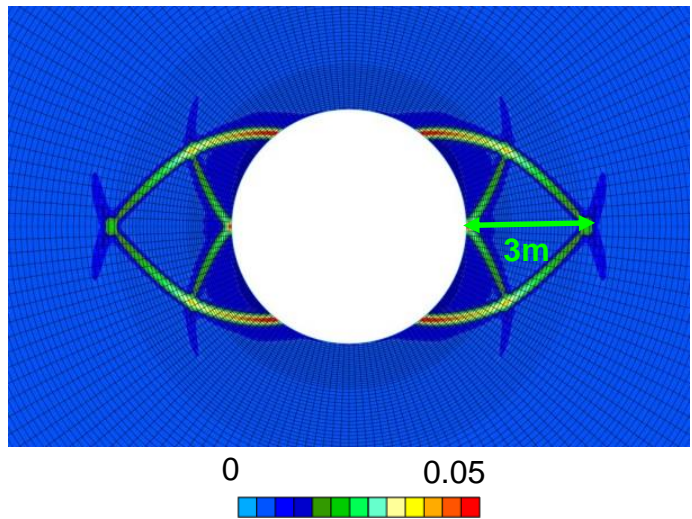
$$\sigma_{y,0} = \sigma_v = 12.70 \text{ MPa}$$

$$\sigma_{z,0} = \sigma_H = 1.3 \times \sigma_h = 16.12 \text{ MPa}$$



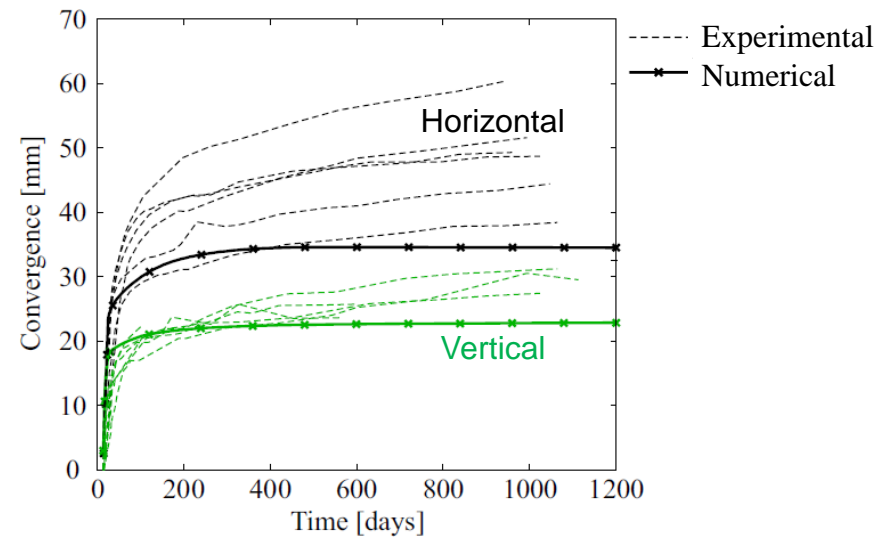
### - Shear banding

Total deviatoric strain



→ Shape modification due to  $\sigma_H$

### - Convergence

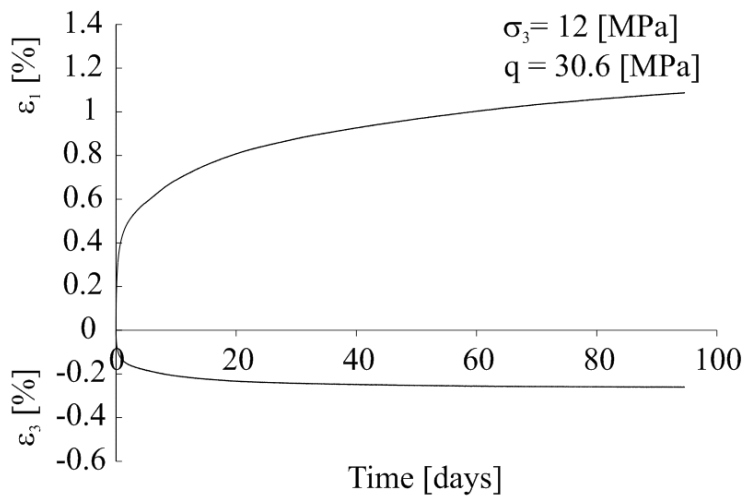
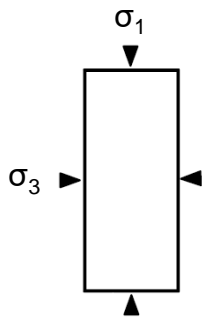


→ Long-term deformation → Creep deformation

# 3. Influence of mechanical anisotropy

## - Creep deformation

Permanent strain  
 In the long term  
 Under constant stress  
 below the yield strength



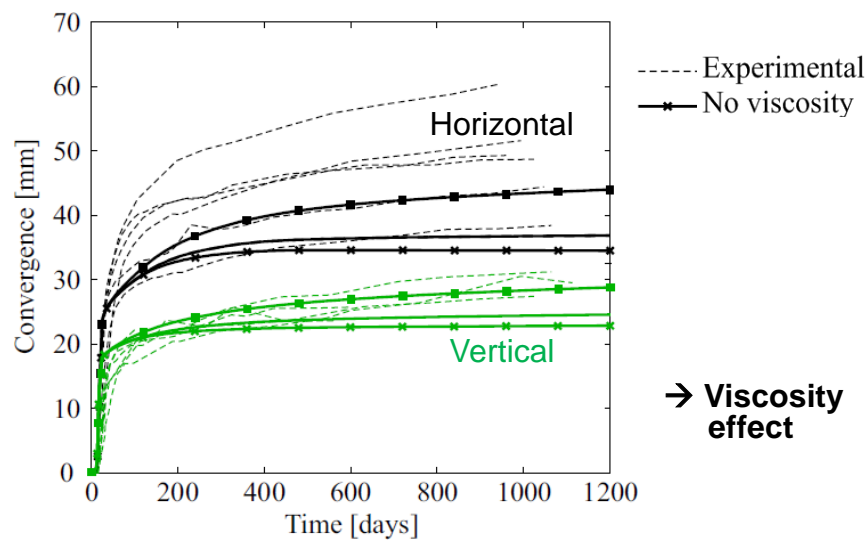
## - Viscosity

Time-dependent plastic strain  
 (Jia et al., 2008; Zhou et al. 2008)

$$\dot{\epsilon}_{ij} = \dot{\epsilon}_{ij}^e + \dot{\epsilon}_{ij}^p + \dot{\epsilon}_{ij}^{vp}$$

$$F^{vp} \equiv \sqrt{3} II_{\dot{\sigma}} - \alpha^{vp} g(\beta) R_c \sqrt{A^{vp} \left( C^{vp} + \frac{I_{\sigma'}}{3R_c} \right)} = 0$$

## - Convergence





# 3. Influence of mechanical anisotropy

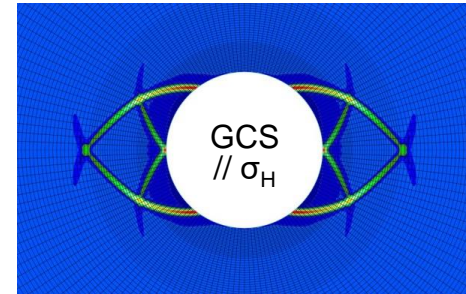
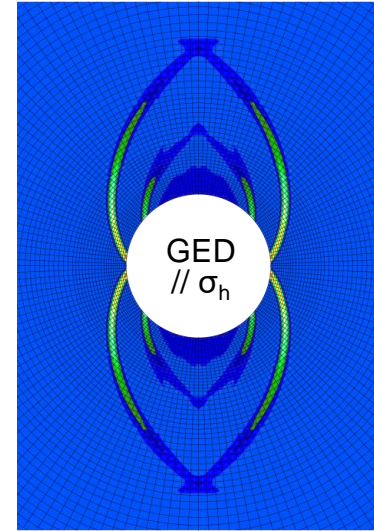
## 3.4. Conclusions and outlooks

### - Conclusions

- ✓ Reproduction of EDZ in both directions.
- ✓ Shape and extent of EDZ governed by:
  - **anisotropic stress state.**
  - **anisotropic mechanical behaviour.**
- ✓ Long-term convergence with viscosity.

### - Next steps ...

- X HM coupling in EDZ.
  - Influence of fracturing on hydraulic properties.
- X Gallery air ventilation and water transfer.

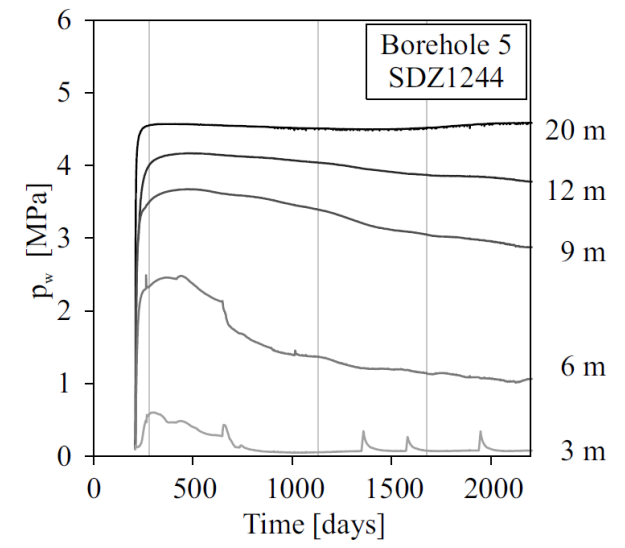
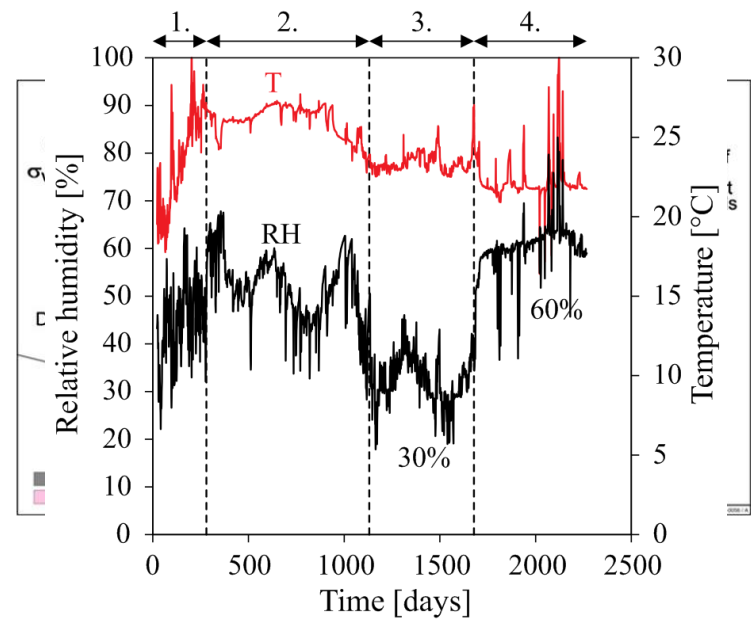
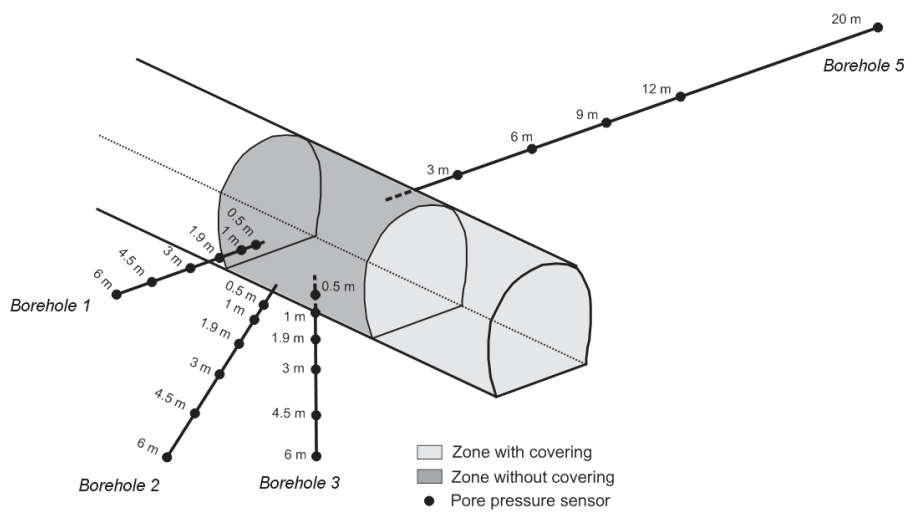
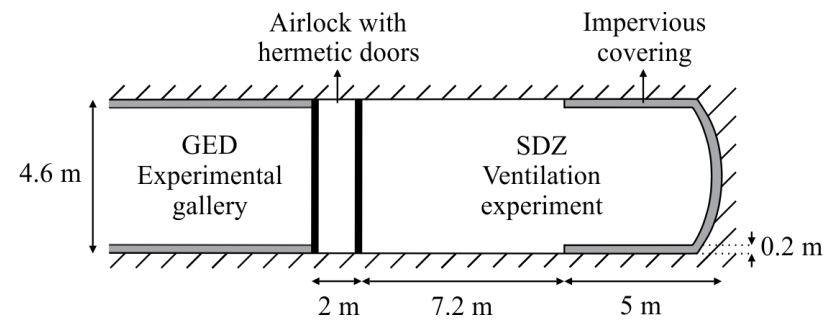


# 4. Permeability evolution and water transfer

## 4.1. Large-scale experiment of gallery ventilation (SDZ)

Characterise the effect of gallery ventilation on the hydraulic transfer around it.

- drainage / desaturation
- exchange at gallery wall

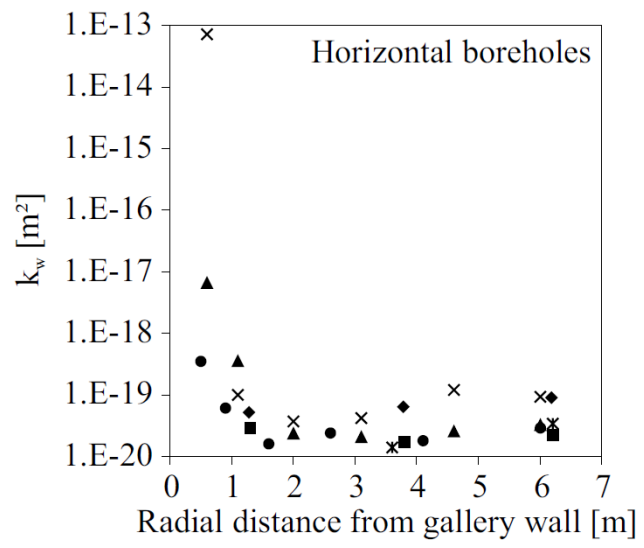
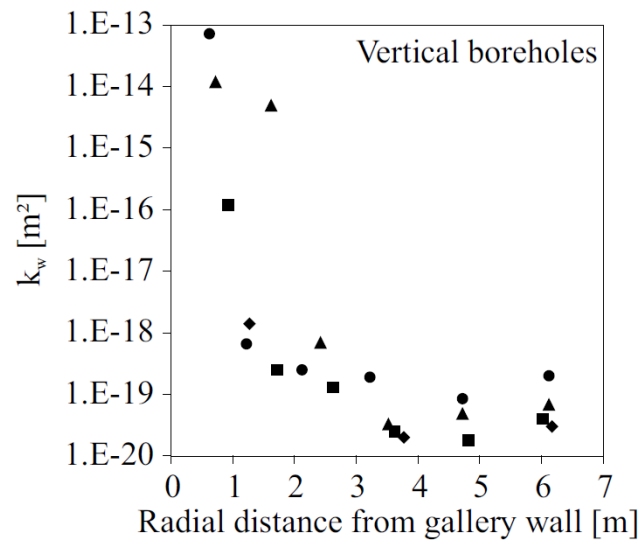
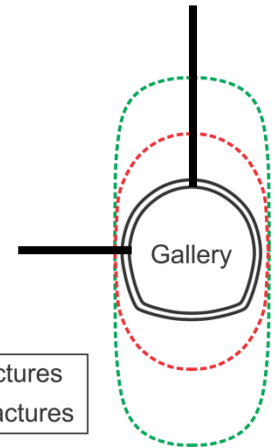


# 4. Permeability evolution and water transfer

## 4.2. Permeability variation in fractured zone

HM coupling in the EDZ.

### 4.2.1. Saturated permeability in boreholes



Fracture and rock matrix permeabilities

- Capture  $k_w$  evolution
- Relation to fractures

# 4. Permeability evolution and water transfer

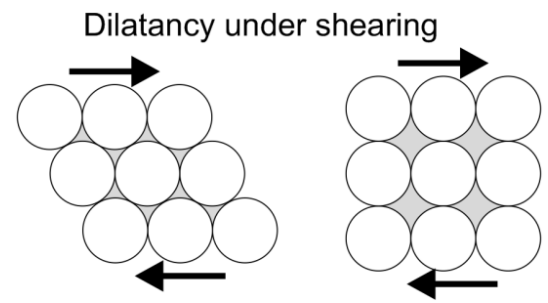
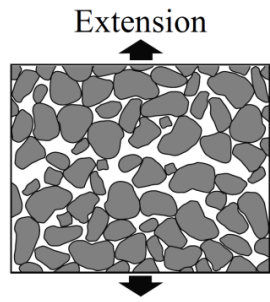
## 4.2.2. Evolution of intrinsic water permeability

Various approaches: deformation, damage, cracks...

### - Relation to deformation

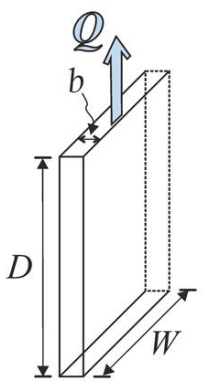
Volumetric effects = increase of porous space  
(Kozeny-Carman)

$$k_w = k_{w,0} \frac{(1-\phi_0)^{\xi_1}}{\phi_0^{\xi_2}} \frac{\phi^{\xi_2}}{(1-\phi)^{\xi_1}} \quad \varepsilon_v = \frac{\varepsilon_{ii}}{3}$$

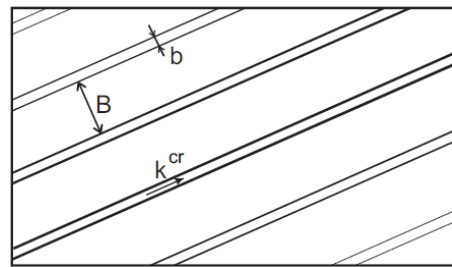


### - Fracture permeability

Cubic law for parallel-plate approach  
(Witherspoon 1980; Snow 1969, Olivella and Alonso 2008)



$$k_w^{cr} = \frac{b^2}{12}$$



$$k_w = \frac{b^3}{12B}$$

$$b = b_0 + B \langle \varepsilon^n - \varepsilon_0^n \rangle$$

$$k_w = k_{w,0} \left( 1 + A \langle \varepsilon^n - \varepsilon_0^n \rangle \right)^3$$

Localised deformation  
Fracture initiation

### - Empirical law

Related to strain localisation effect  
Permeability variation threshold

$$k_{w,ij} = k_{w,ij,0} \left( 1 + \beta_{per} \langle YI - YI^{thr} \rangle \hat{\varepsilon}_{eq}^3 \right)$$

$$YI = \frac{II_{\hat{\sigma}}}{II_{\hat{\sigma}}^p}$$

# 4. Permeability evolution and water transfer

## 4.4. Modelling of excavation and SDZ experiment

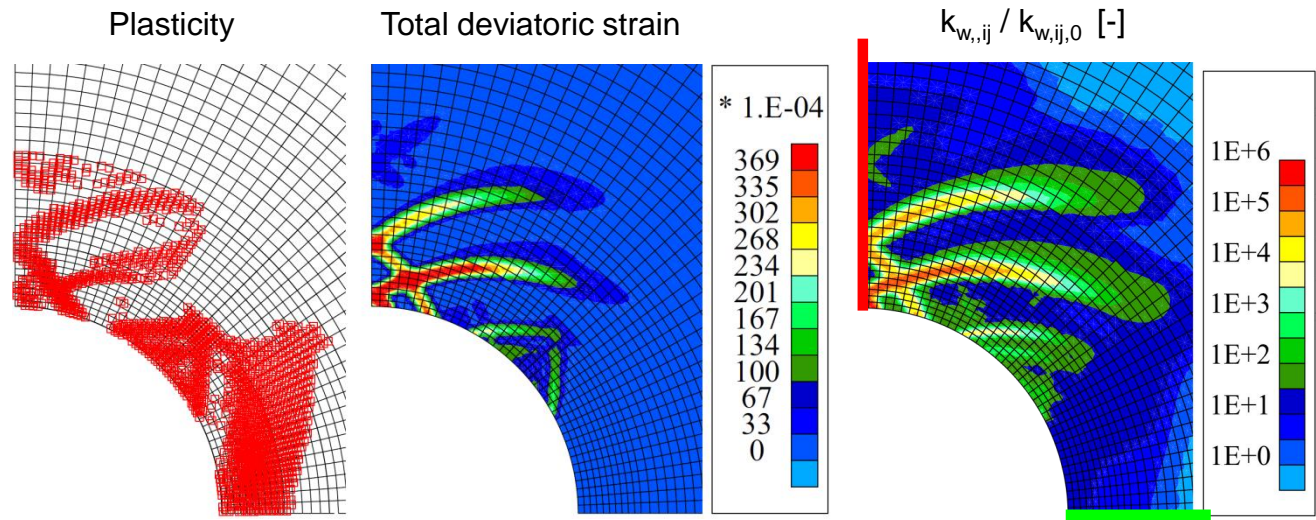
### 4.4.1. HM coupling in EDZ

- Gallery excavation

SDZ → GED gallery //  $\sigma_h$

Anisotropic  $\sigma_{ij,0}$  and material

→ Localisation zone dominated by stress anisotropy

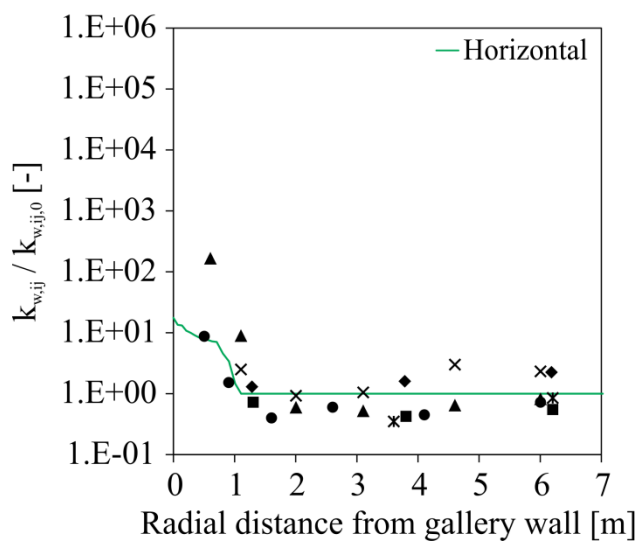
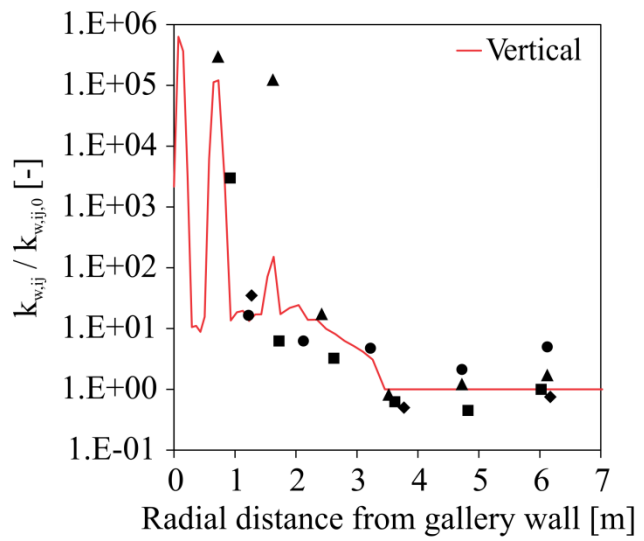


- Intrinsic permeability evolution

$$\frac{k_{w,ij}}{k_{w,ij,0}} = \left(1 + \beta \langle YI - YI^{thr} \rangle \hat{\varepsilon}_{eq}^3\right)$$

$$YI^{thr} = 0.95$$

Cross-sections

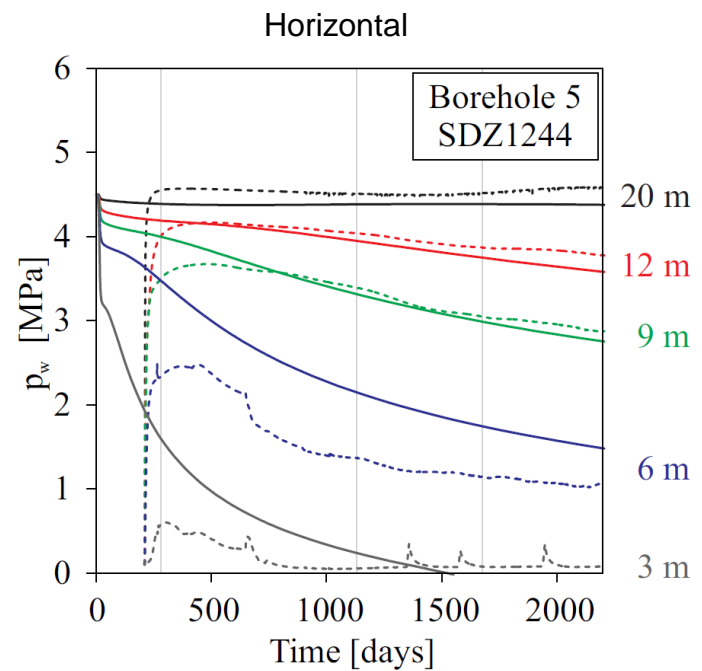
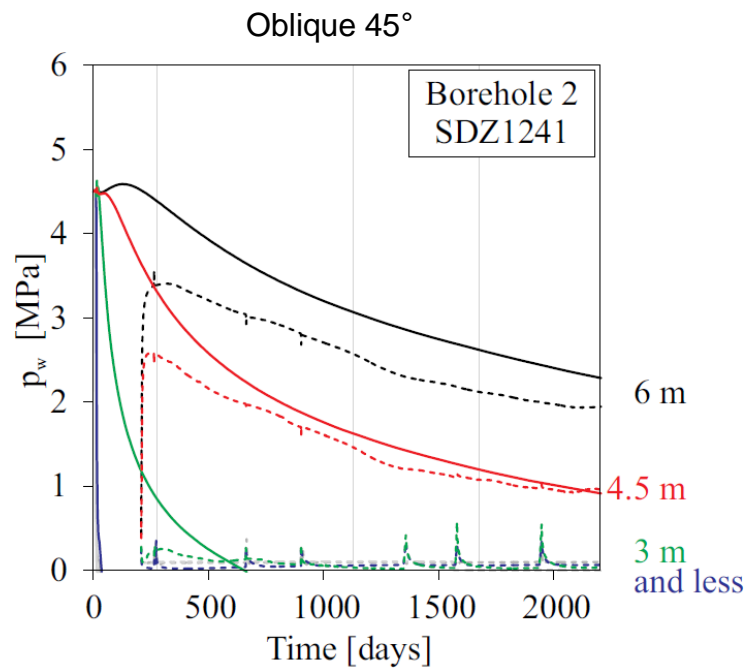
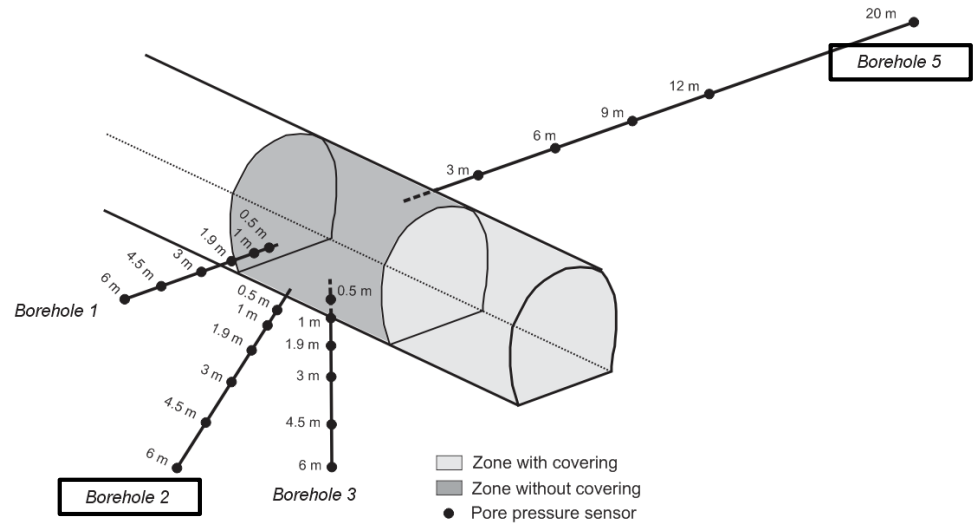


Plastic strain and a part of the elastic one → EDZ extension +  $k_w$  increase



# 4. Permeability evolution and water transfer

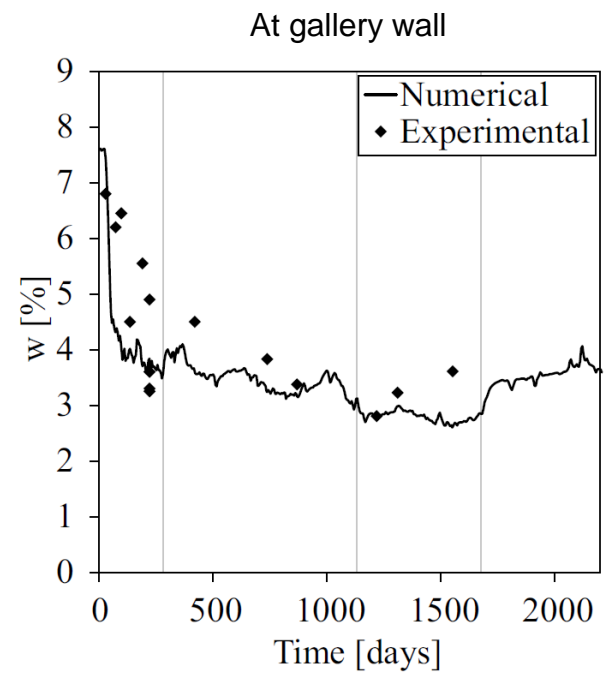
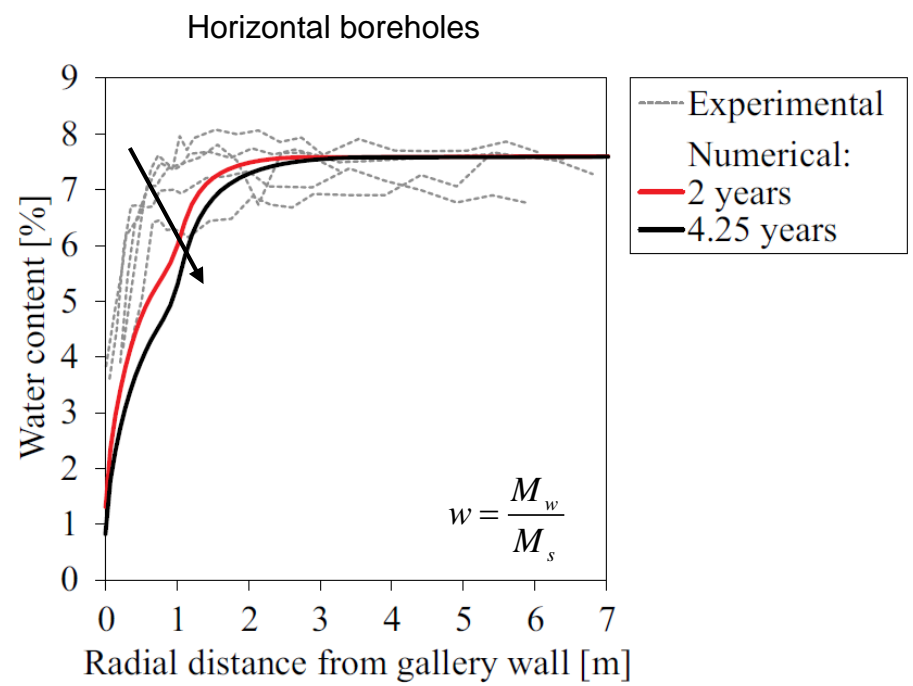
- Drainage /  $p_w$  reproduction



--- Experimental  
 — Numerical  
 $\alpha_v = 10^{-3}$  m/s

# 4. Permeability evolution and water transfer

- Desaturation EDZ / w reproduction



→ Desaturation: overestimation in long term

→ Vapour transfer ( $\alpha_v = 10^{-3}$  m/s)

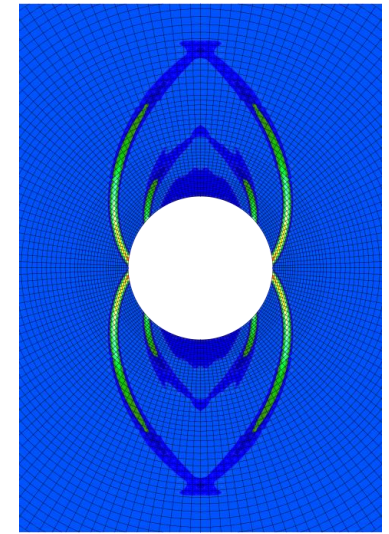
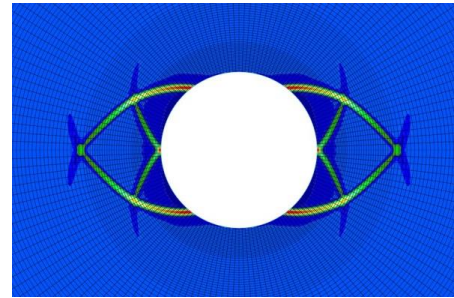
→ Good reproduction at gallery wall

1. Context
2. Fracture modelling with shear bands
3. Influence of mechanical anisotropy
4. Permeability evolution and water transfer
- 5. Conclusions and perspectives**

## 5. Conclusions and perspectives

### Conclusions

Better understand, predict, and model the behaviour of the EDZ in partially saturated clay rock, at large scale.



#### Fracture description

EDZ with strain localisation.

#### Constitutive models

Mechanics: anisotropy, viscosity.

Coupled: fracture influence on permeability.

#### Numerical modelling

Shape, extent.

Influence of fracturing, permeability variation, anisotropy.

Water transfer.

Contribution : Provide new elements for the prediction and understanding of the HM behaviour of the EDZ.

Innovations : Fracturing process is predicted on a **large scale** with **shear bands**.  
Strain localisation effects are taken into account in **coupled processes** (water flow).

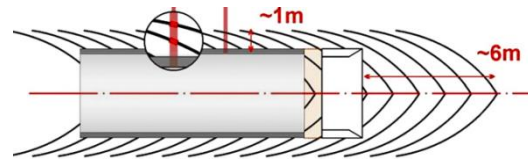


# APPENDICES



# I. Gallery excavation in 3D

- Fracturation = 3D problem

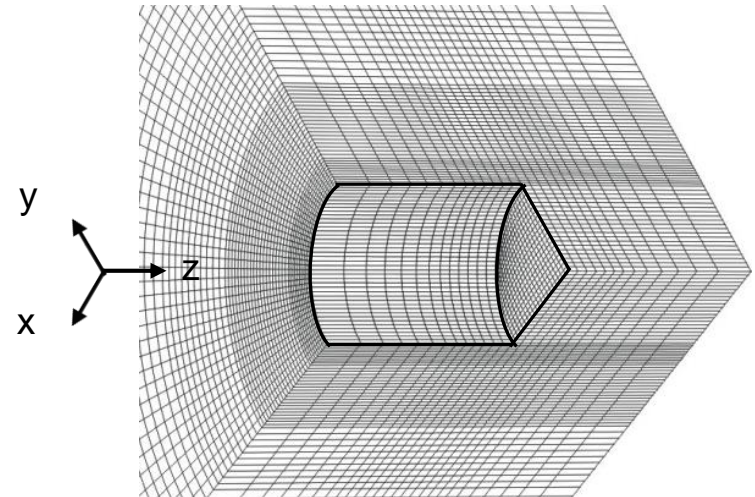
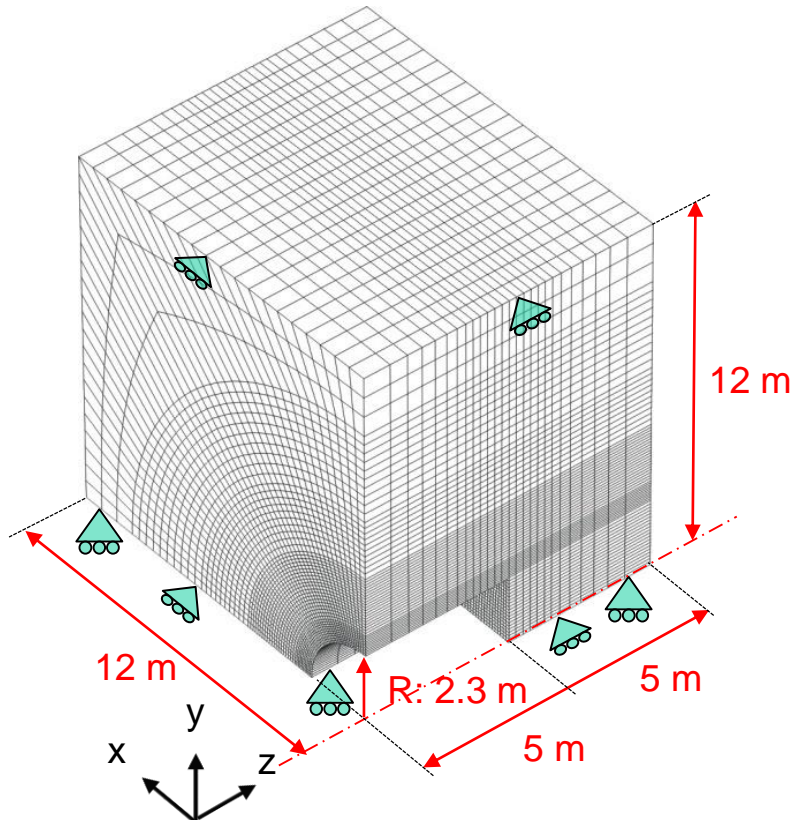


Fractures pattern around a gallery in Boom clay

- Mesh:

Mechanical modelling in 3D state.

Classical FE, no regularisation method.



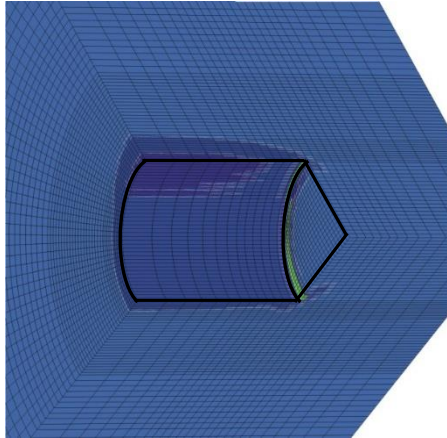
# I. Gallery excavation in 3D

- Localisation zone:

Equivalent deformation  $\varepsilon_{eq}$  during boring.  $\hat{\varepsilon}_{eq} = \sqrt{\frac{2}{3} \hat{\varepsilon}_{ij} \hat{\varepsilon}_{ij}}$

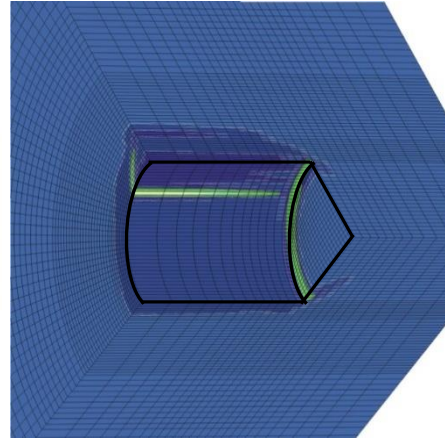
3 days

$\sigma/\sigma_0 = 0.40$



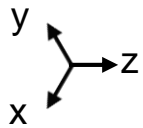
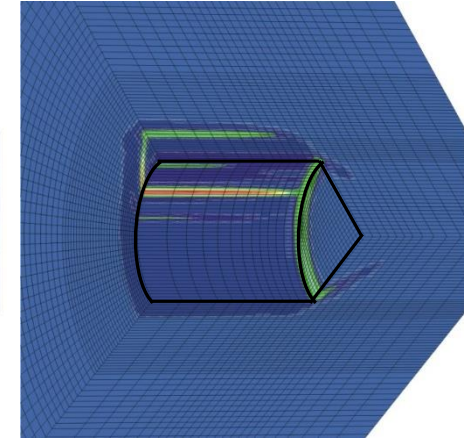
3.25 days

$\sigma/\sigma_0 = 0.35$



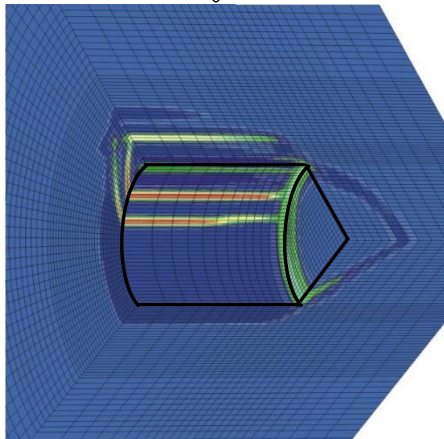
3.5 days

$\sigma/\sigma_0 = 0.30$



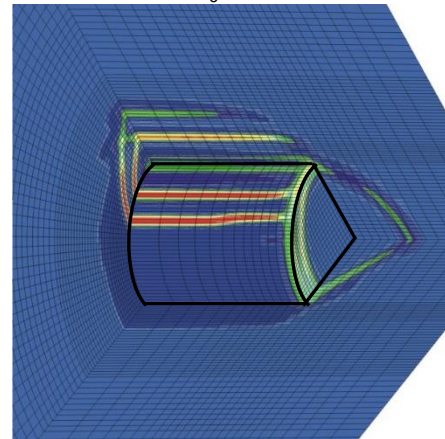
3.75 days

$\sigma/\sigma_0 = 0.25$



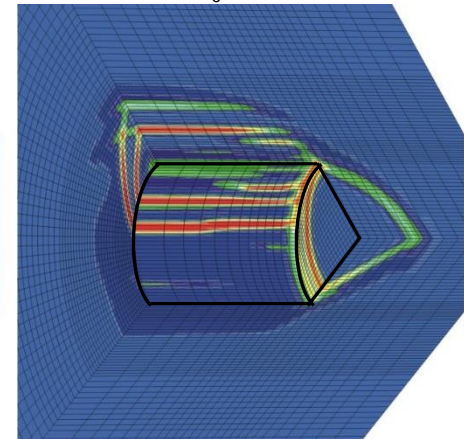
4 days

$\sigma/\sigma_0 = 0.20$



4.25 days

$\sigma/\sigma_0 = 0.15$



# I. Gallery excavation in 3D

- Localisation zone:

Equivalent deformation  $\varepsilon_{eq}$  during boring.  $\hat{\varepsilon}_{eq} = \sqrt{\frac{2}{3} \hat{\varepsilon}_{ij} \hat{\varepsilon}_{ij}}$

3 days

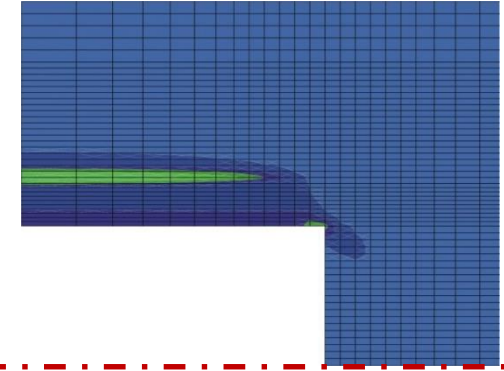
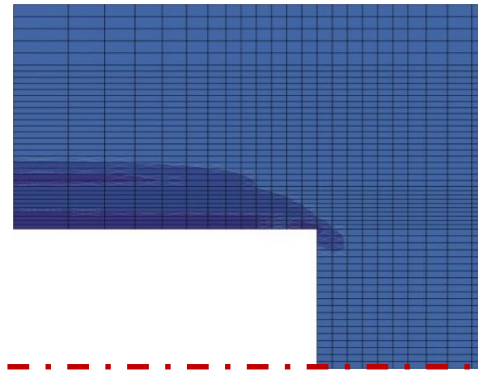
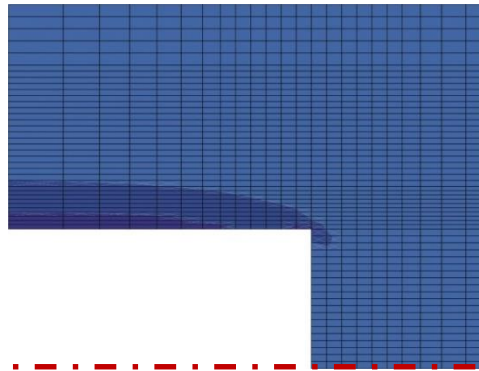
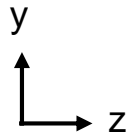
$\sigma/\sigma_0 = 0.40$

3.25 days

$\sigma/\sigma_0 = 0.35$

3.5 days

$\sigma/\sigma_0 = 0.30$



3.75 days

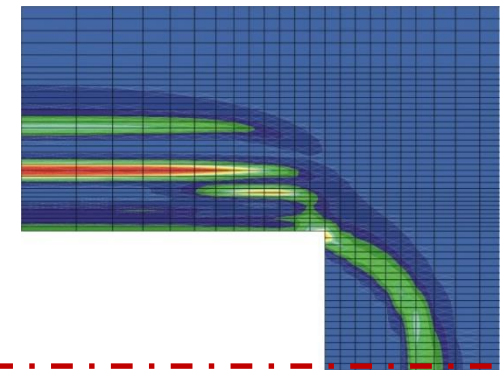
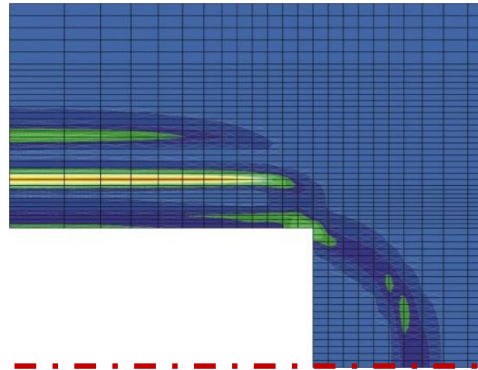
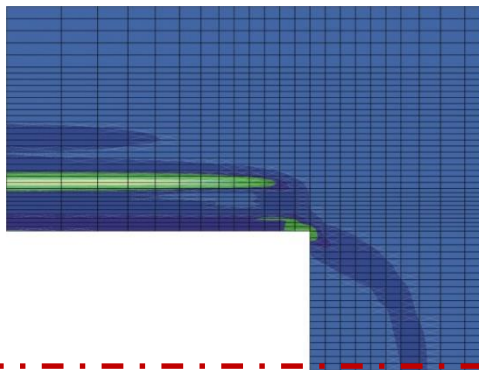
$\sigma/\sigma_0 = 0.25$

4 days

$\sigma/\sigma_0 = 0.20$

4.25 days

$\sigma/\sigma_0 = 0.15$





# I. Gallery excavation in 3D

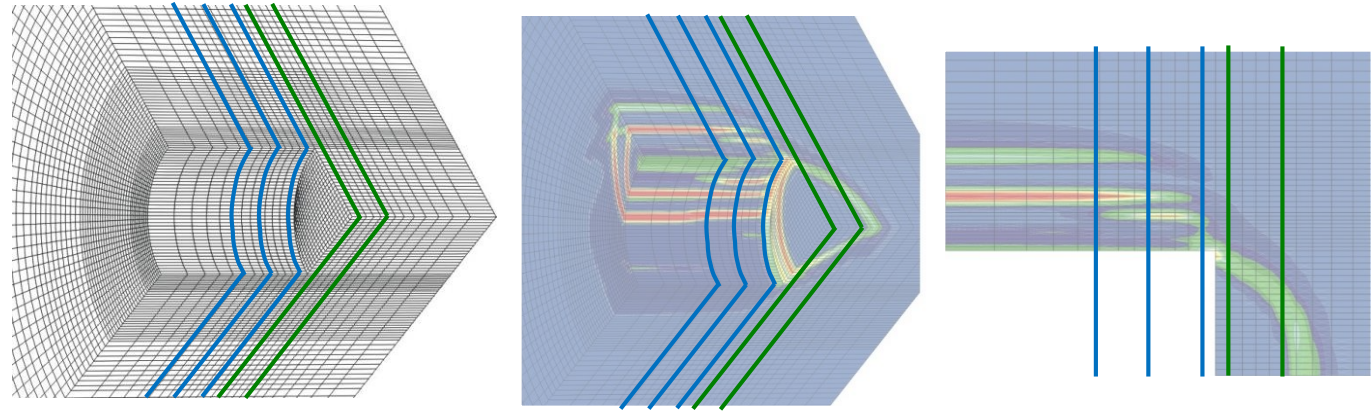
## - Localisation zone

Equivalent deformation  $\epsilon_{eq}$  - for 4.25 days of excavation ( $\sigma/\sigma_0 = 0.15$ ) :

$z < 0$  : excavation zone

$z = 0$  : gallery front

$z > 0$  : rock mass



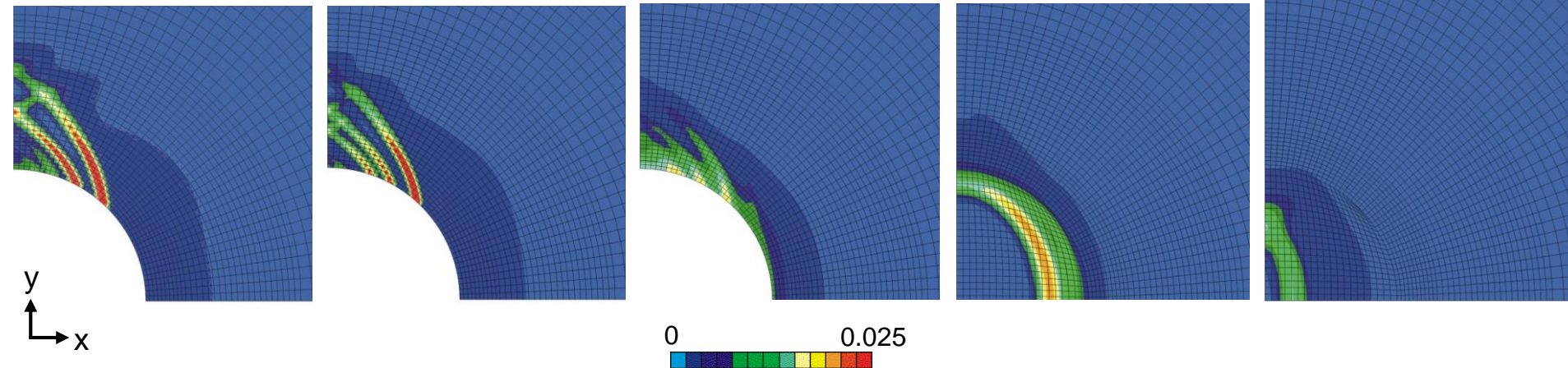
$z = -2.25\text{m}$

$z = -1.25\text{m}$

$z = -0.25\text{m}$

$z = +0.25\text{m}$

$z = +1.25\text{m}$

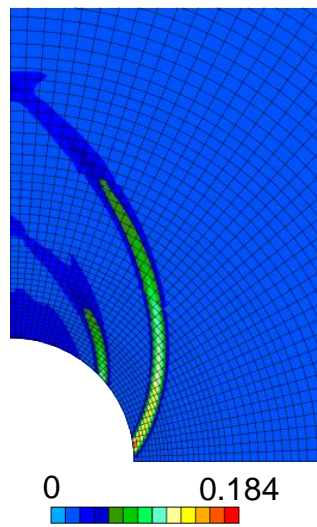


# Compressibility influence on shear banding

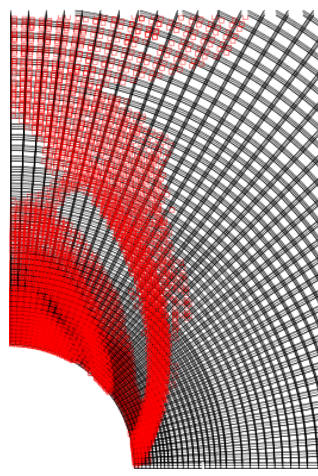
Biot's coefficient:  $b=0.6$

1000 days  
End of excavation

Total deviatoric strain



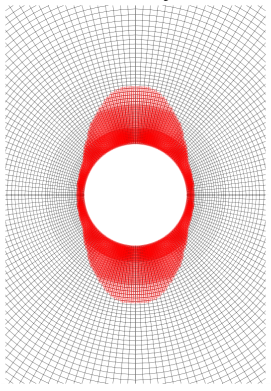
Plasticity



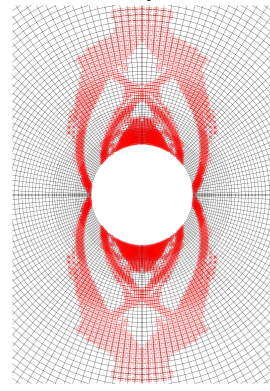
Plasticity

$b=0.6$

4 days

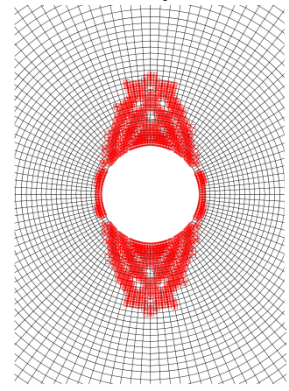


5 days

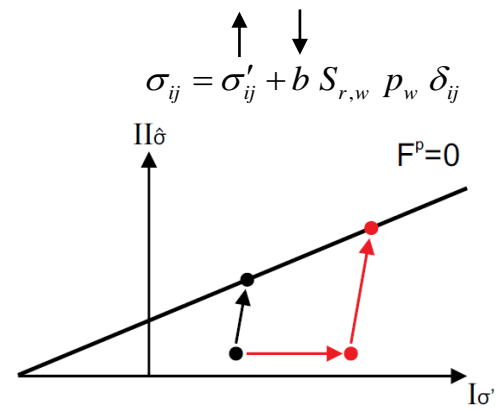
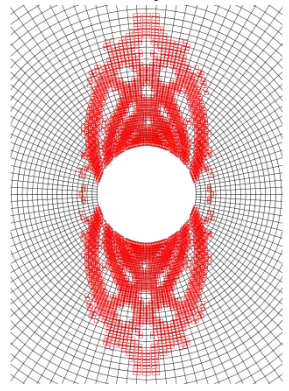


$b=1$

4 days

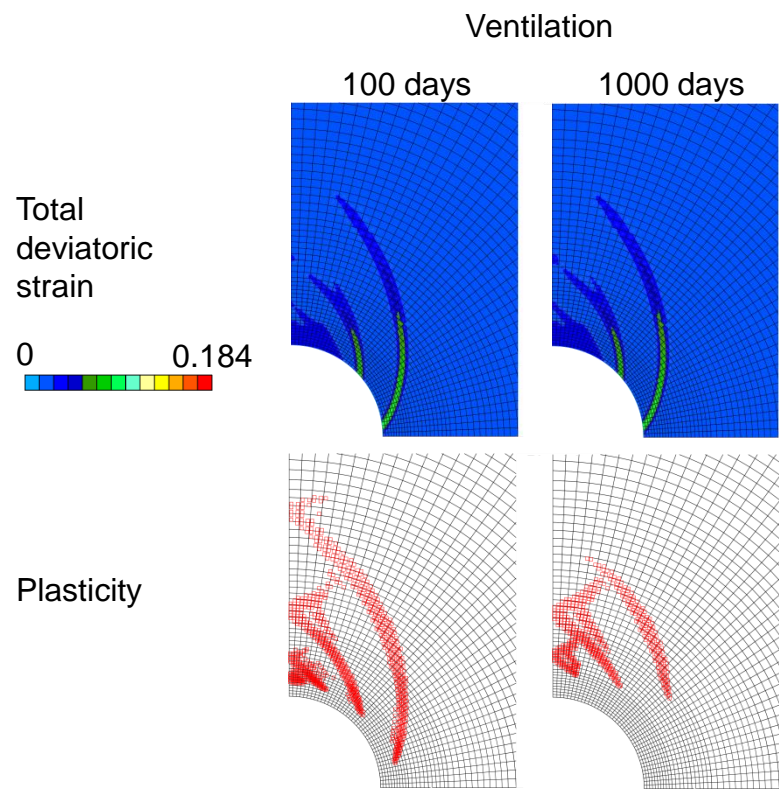


5 days



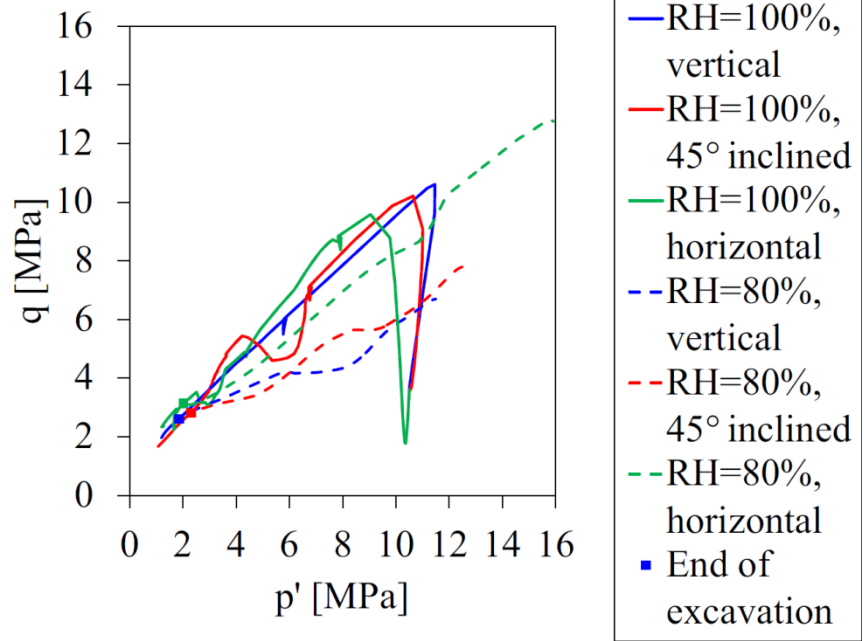
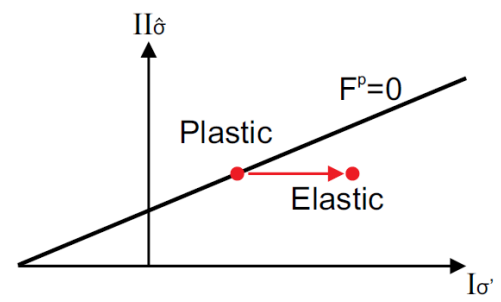
# Air ventilation influence on shear banding

- Gallery air ventilation :



$$\sigma_{ij} = \sigma'_{ij} + b S_{r,w} p_w \delta_{ij}$$

- suction ↑
- $\sigma'$  ↑
- Elastic unloading
- Inhibition of localisation
- Restrain  $\epsilon$





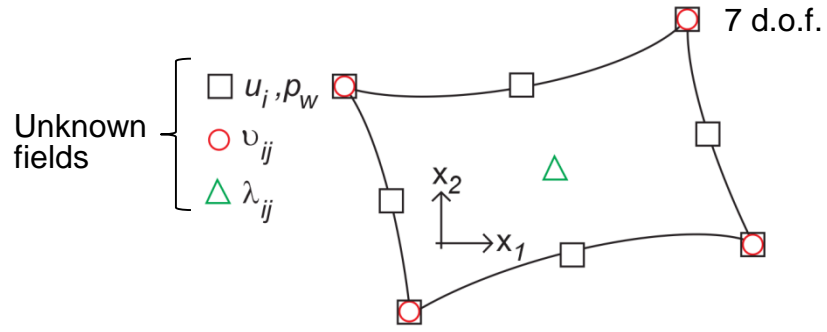
# Finite element formulation – 2d gradient model

- Spatial discretisation

Matricial form of balance equations:

$$\int_{\Omega^{\tau 1}} [U_{(x_1, x_2)}^{*, \tau 1}]^T [E^{\tau 1}] [dU_{(x_1, x_2)}^{\tau 1}] d\Omega^{\tau 1} = -\Delta_1^{\tau 1} - \Delta_2^{\tau 1} - \Delta_3^{\tau 1}$$

$[dU_{(x_1, x_2)}^{\tau 1}]$  vector of the unknown increments of nodal variables



- Element stiffness matrix

Unsaturated condition,  $S_{r,w}$

Soild phase compressibility,  $b$

Permeability anisotropy and evolution,  $k_{w,ij}$

$$[E^{\tau 1}]_{25 \times 25} = \begin{bmatrix} E_{14 \times 4}^{\tau 1} & 0_{4 \times 2} & K_{WM}^{\tau 1} & 0_{4 \times 8} & 0_{4 \times 4} & -I_{4 \times 4} \\ G_{12 \times 4}^{\tau 1} & 0_{2 \times 2} & G_{22 \times 3}^{\tau 1} & 0_{2 \times 8} & 0_{2 \times 4} & 0_{2 \times 4} \\ K_{MW}^{\tau 1} & 0_{3 \times 2} & K_{WW}^{\tau 1} & 0_{3 \times 8} & 0_{3 \times 4} & 0_{3 \times 4} \\ E_{28 \times 4}^{\tau 1} & 0_{8 \times 2} & 0_{8 \times 3} & D_{8 \times 8}^{\tau 1} & 0_{8 \times 4} & 0_{8 \times 4} \\ E_{34 \times 4}^{\tau 1} & 0_{4 \times 2} & 0_{4 \times 3} & 0_{4 \times 8} & 0_{4 \times 4} & I_{4 \times 4} \\ E_{44 \times 4}^{\tau 1} & 0_{4 \times 2} & 0_{4 \times 3} & 0_{4 \times 8} & -I_{4 \times 4} & 0_{4 \times 4} \end{bmatrix}$$

# Second gradient mechanical law – Influence of the elastic modulus

- Second gradient mechanical law

Linear elastic law function

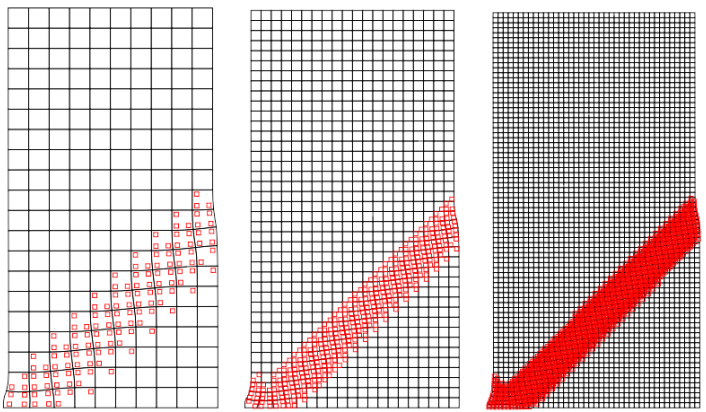
Independent of  $p_w$

$$\tilde{\Sigma}_{ijk} = [D] \frac{\partial \dot{v}_{ij}}{\partial x_k}$$

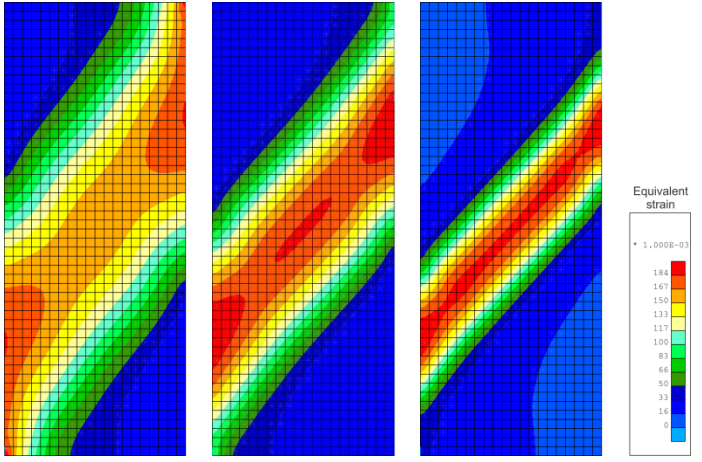
Internal length scale  
D represents the physical microstructure

$$\begin{bmatrix} \tilde{\Sigma}_{111} \\ \tilde{\Sigma}_{112} \\ \tilde{\Sigma}_{121} \\ \tilde{\Sigma}_{122} \\ \tilde{\Sigma}_{211} \\ \tilde{\Sigma}_{212} \\ \tilde{\Sigma}_{221} \\ \tilde{\Sigma}_{222} \end{bmatrix} = D \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & \frac{1}{2} & \frac{1}{2} & 0 \\ 0 & \frac{1}{2} & \frac{1}{2} & 0 & -\frac{1}{2} & 0 & 0 & \frac{1}{2} \\ 0 & \frac{1}{2} & \frac{1}{2} & 0 & -\frac{1}{2} & 0 & 0 & \frac{1}{2} \\ 0 & 0 & 0 & 1 & 0 & -\frac{1}{2} & -\frac{1}{2} & 0 \\ 0 & -\frac{1}{2} & -\frac{1}{2} & 0 & 1 & 0 & 0 & 0 \\ \frac{1}{2} & 0 & 0 & -\frac{1}{2} & 0 & \frac{1}{2} & \frac{1}{2} & 0 \\ \frac{1}{2} & 0 & 0 & -\frac{1}{2} & 0 & \frac{1}{2} & \frac{1}{2} & 0 \\ 0 & \frac{1}{2} & \frac{1}{2} & 0 & 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \frac{\partial \dot{v}_{11}}{\partial x_1} \\ \frac{\partial \dot{v}_{11}}{\partial x_2} \\ \frac{\partial \dot{v}_{12}}{\partial x_1} \\ \frac{\partial \dot{v}_{12}}{\partial x_2} \\ \frac{\partial \dot{v}_{21}}{\partial x_1} \\ \frac{\partial \dot{v}_{21}}{\partial x_2} \\ \frac{\partial \dot{v}_{22}}{\partial x_1} \\ \frac{\partial \dot{v}_{22}}{\partial x_2} \end{bmatrix}$$

Plasticity



Total deviatoric strain  $\hat{\epsilon}_{eq} = \sqrt{\frac{2}{3} \hat{\epsilon}_{ij} \hat{\epsilon}_{ij}}$



D = 80 N

D = 20 N

D = 5 N

- D should be evaluated based on experimental measurements
- Better numerical precision if a few elements compose the shear band width
- Large scale ...

## Cross-anisotropic elasticity

Linear elasticity (5 param.)

$$d\varepsilon_{ij}^e = D_{ijkl}^e d\sigma_{kl} \quad E_{//}, E_{\perp}, \nu_{////}, \nu_{//\perp}, G_{//\perp}$$

$$\frac{\nu_{//\perp}}{E_{//}} = \frac{\nu_{\perp//}}{E_{\perp}} \quad G_{////} = \frac{E_{//}}{2(1+\nu_{////})}$$

$$D_{ijkl}^e = \begin{bmatrix} \frac{1}{E_{//}} & -\frac{\nu_{\perp//}}{E_{\perp}} & -\frac{\nu_{////}}{E_{//}} & 0 & 0 & 0 \\ -\frac{\nu_{//\perp}}{E_{//}} & \frac{1}{E_{\perp}} & \frac{\nu_{//\perp}}{E_{//}} & 0 & 0 & 0 \\ -\frac{\nu_{////}}{E_{//}} & -\frac{\nu_{\perp//}}{E_{\perp}} & \frac{1}{E_{//}} & 0 & 0 & 0 \\ 0 & 0 & 0 & \frac{1}{2G_{//\perp}} & 0 & 0 \\ 0 & 0 & 0 & 0 & \frac{1}{2G_{////}} & 0 \\ 0 & 0 & 0 & 0 & 0 & \frac{1}{2G_{\perp//}} \end{bmatrix}$$

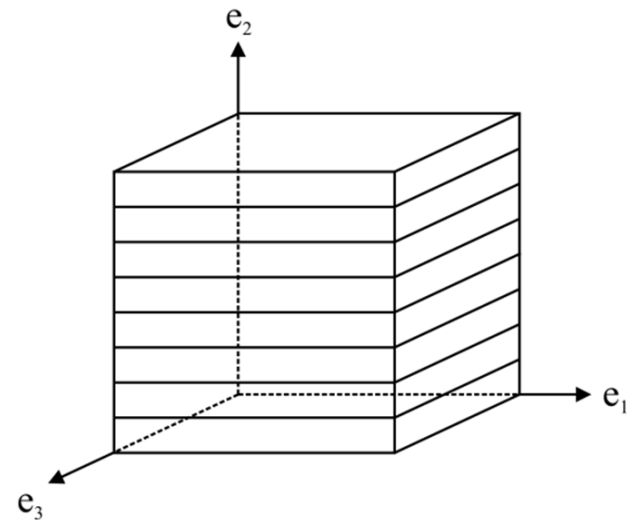
Biot's coefficients

$$b_{ij} = \delta_{ij} - \frac{C_{ijkk}^e}{3K_s} \quad b_{ij} = \begin{bmatrix} b_{//} & & & \\ & b_{\perp} & & \\ & & b_{//} & \\ & & & b_{\perp} \end{bmatrix}$$

$$b_{//} = 1 - \frac{1 + \nu_{////} + \nu_{////}\nu_{\perp//} + \nu_{\perp//}}{3E_{//}E_{\perp}\Upsilon K_s}$$

$$b_{\perp} = 1 - \frac{1 - \nu_{////}^2 + 2\nu_{//\perp} + 2\nu_{//\perp}\nu_{////}}{3E_{//}E_{//}\Upsilon K_s}$$

Micro-homogeneity and micro-isotropy assumptions (Cheng, 1997) for which  $K_s$  is homogeneous and isotropic at grains scale.



# Influence of mechanical anisotropy

## Anisotropic plasticity with fabric tensor

Cohesion anisotropy with fabric tensor.

$c_0$  is the projection of the tensor on a generalised unit loading vector :

$$c_0 = a_{ij} l_i l_j \quad l_i = \sqrt{\frac{\sigma_{i1}'^2 + \sigma_{i2}'^2 + \sigma_{i3}'^2}{\sigma_{ij}' \sigma_{ij}'}} \quad \|l_i\| = 1$$

Deviatoric part:

$$\hat{a}_{ij} = a_{ij} - \bar{c} \delta_{ij} \quad , \quad \bar{c} = \frac{a_{ii}}{3} \Rightarrow c_0 = \bar{c} (1 + A_{ij} l_i l_j)$$

$$A_{ij} = \frac{\hat{a}_{ij}}{\bar{c}} \quad , \quad A_{ii} = \hat{a}_{ii} = 0$$

Generalisation with higher order tensor:

$$c_0 = \bar{c} \left( 1 + A_{ij} l_i l_j + b_1 (A_{ij} l_i l_j)^2 + b_2 (A_{ij} l_i l_j)^3 + \dots \right)$$

Orthotropy:

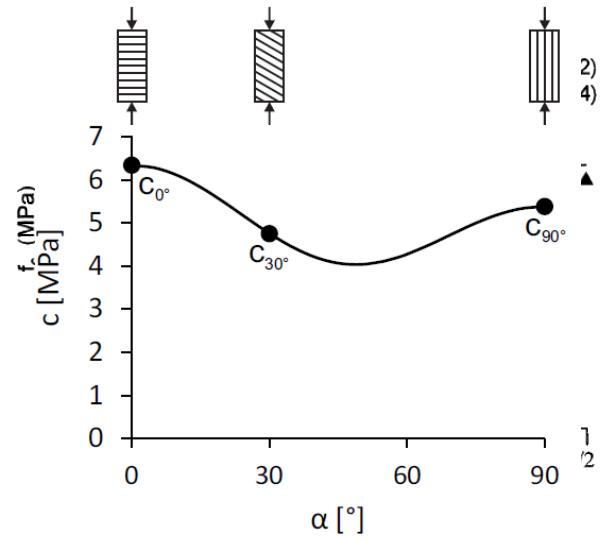
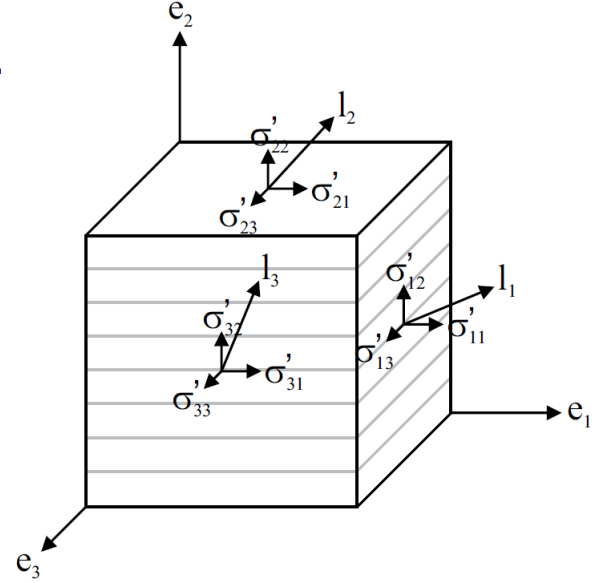
$$A_{ij} = \begin{bmatrix} A_{11} & 0 & 0 \\ 0 & A_{22} & 0 \\ 0 & 0 & A_{33} \end{bmatrix} \Rightarrow A_{ij} l_i l_j = A_{11} l_1^2 + A_{22} l_2^2 + A_{33} l_3^2$$

Cross-anisotropy:

$$A_{ij} = \begin{bmatrix} A_{//} & 0 & 0 \\ 0 & A_{\perp\perp} & 0 \\ 0 & 0 & A_{//} \end{bmatrix} \Rightarrow A_{ij} l_i l_j = A_{//} (1 - 3l_2^2)$$

$$c_0 = \bar{c} \left( 1 + A_{//} (1 - 3l_2^2) + b_1 A_{//}^2 (1 - 3l_2^2)^2 + b_2 A_{//}^3 (1 - 3l_2^2)^3 + \dots \right)$$

$$A_{\perp\perp} = -2A_{//} \quad , \quad \|l_i\| = 1$$



## Viscosity

Time-dependent plastic strain, delayed plastic deformation

Progressive evolution of the material microstructure or to mechanical properties degradation (damage)

$$\dot{\varepsilon}_{ij} = \dot{\varepsilon}_{ij}^e + \dot{\varepsilon}_{ij}^p + \dot{\varepsilon}_{ij}^{vp}$$

Viscoplastic loading surface and potential surface:

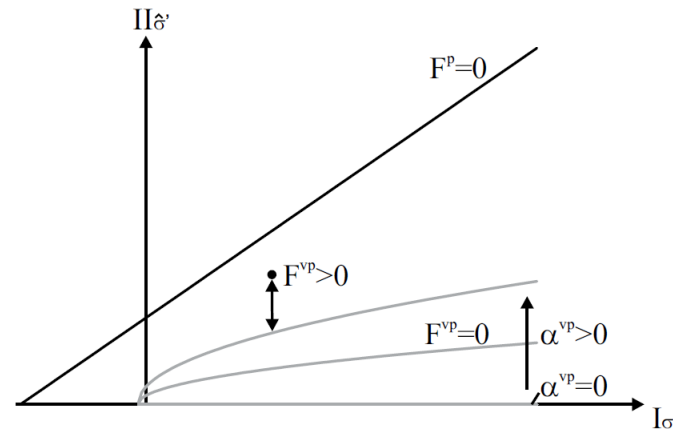
$$F^{vp} \equiv \sqrt{3} \Pi_{\hat{\sigma}} - \alpha^{vp} g(\beta) R_c \sqrt{A^{vp} \left( C^{vp} + \frac{I_{\sigma'}}{3R_c} \right)} = 0$$

$$G^{vp} \equiv \sqrt{3} \Pi_{\hat{\sigma}} - (\alpha^{vp} - \beta^{vp}) g(\beta) R_c \left( C^{vp} + \frac{I_{\sigma'}}{3R_c} \right) = 0$$

$$\dot{\varepsilon}_{ij}^{vp} = \gamma \left\langle \frac{F^{vp}}{R_c} \right\rangle^N \frac{\partial G^{vp}}{\partial \sigma'_{ij}}$$

Delayed viscoplastic hardening function:

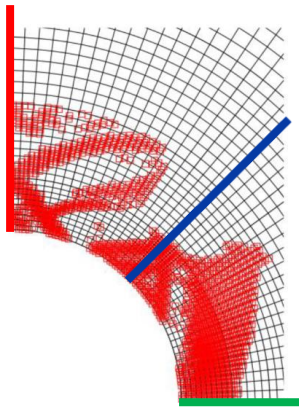
$$\alpha^{vp} = \alpha_0^{vp} + (1 - \alpha_0^{vp}) \frac{\varepsilon_{eq}^{vp}}{B^{vp} + \varepsilon_{eq}^{vp}}$$



- Current stress state
- Plastic loading surface
- Viscoplastic loading surface with hardening ( $\alpha^{vp} \geq 0$ )

# Permeability evolution and water transfer

- Reproduction at the end of excavation



$$k_{w,ij} = k_{w,ij,0} (1 + \beta \langle \gamma \rangle^3)$$

(a) Volumetric strain

$$\gamma = \varepsilon_v = \varepsilon_{ii} / 3$$

(b) Equivalent deviatoric total strain

$$\gamma = \hat{\varepsilon}_{eq} = \sqrt{\frac{2}{3} \hat{\varepsilon}_{ij} \hat{\varepsilon}_{ij}}$$

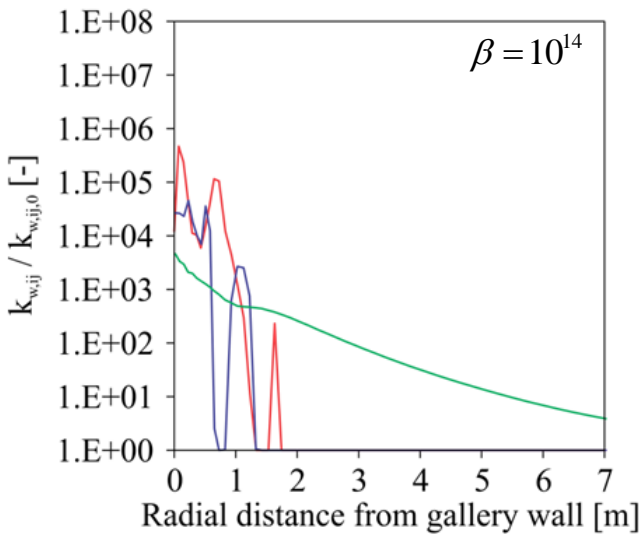
(c) Equivalent deviatoric plastic strain

$$\gamma = \hat{\varepsilon}_{eq}^p = \sqrt{\frac{2}{3} \hat{\varepsilon}_{ij}^p \hat{\varepsilon}_{ij}^p}$$

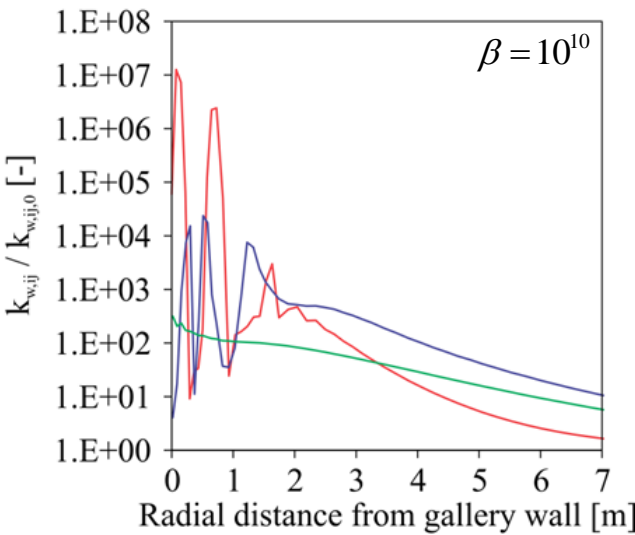
(d) Plastic strain and a part of the elastic one

$$k_{w,ij} = k_{w,ij,0} (1 + \beta \langle YI - YI^{thr} \rangle \hat{\varepsilon}_{eq}^3)$$

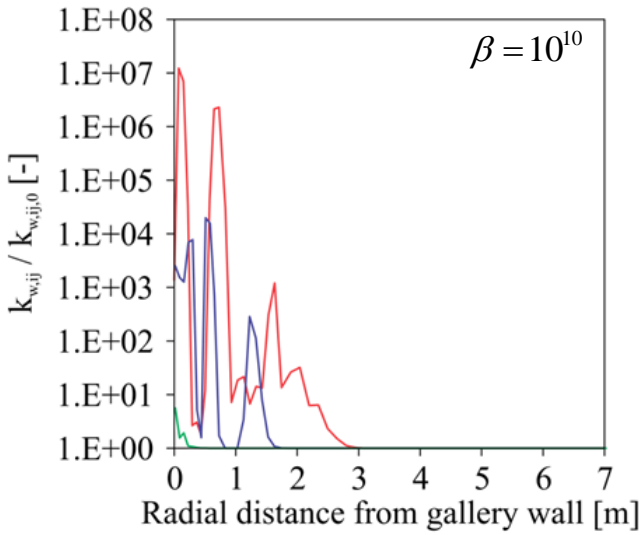
— Vertical — Oblique — Horizontal



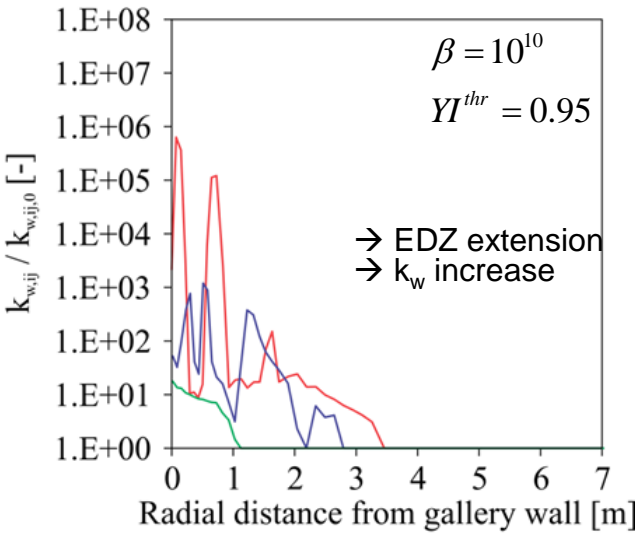
(a)



(b)



(c)



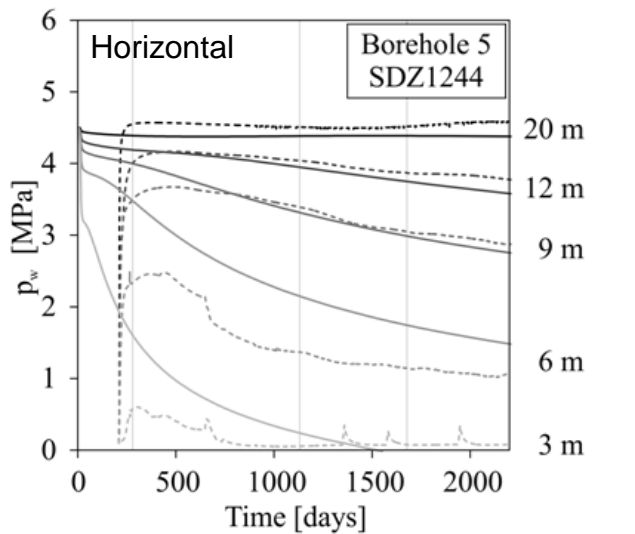
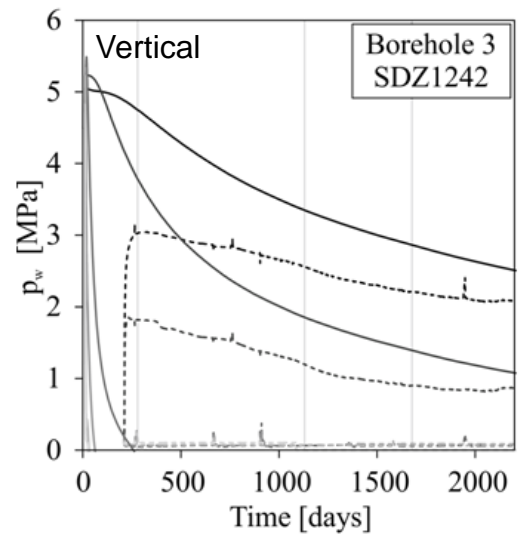
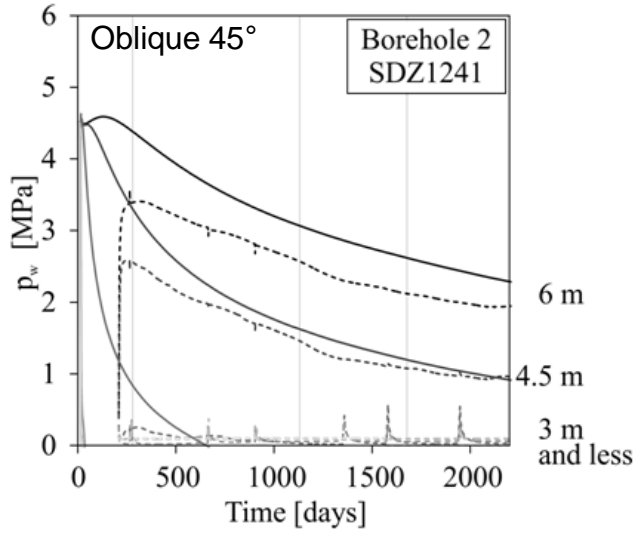
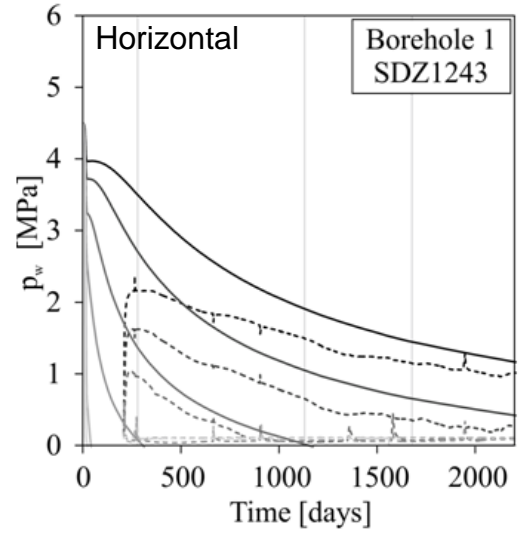
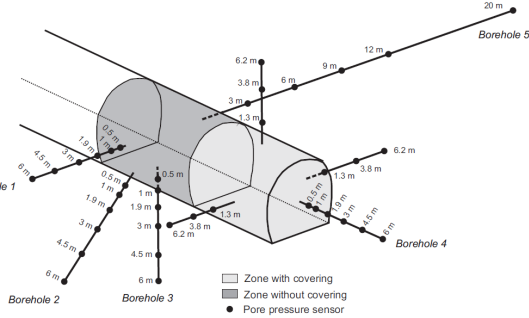
(d)



# Permeability evolution and water transfer

- Drainage /  $p_w$  reproduction

— Numerical - - Experimental



$\alpha_v = 10^{-3} \text{ m/s}$   
 → Good matching  
 → HM effect -  $k_{w,h} > k_{w,v}$

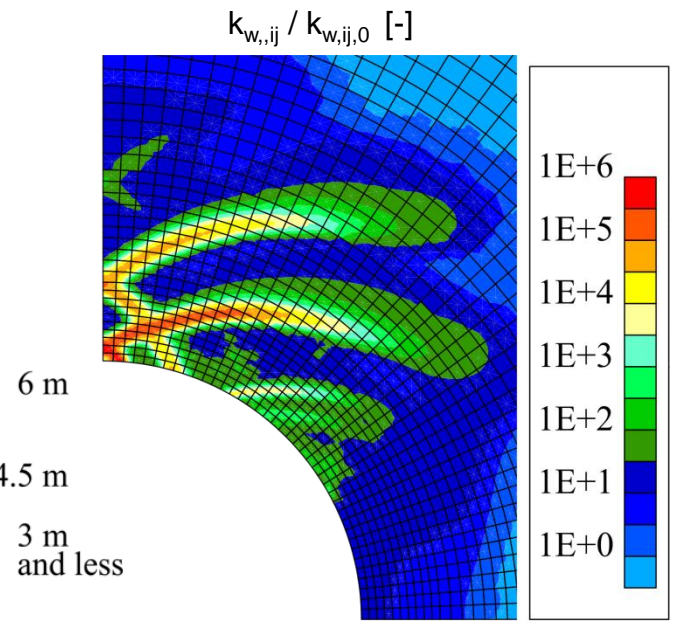
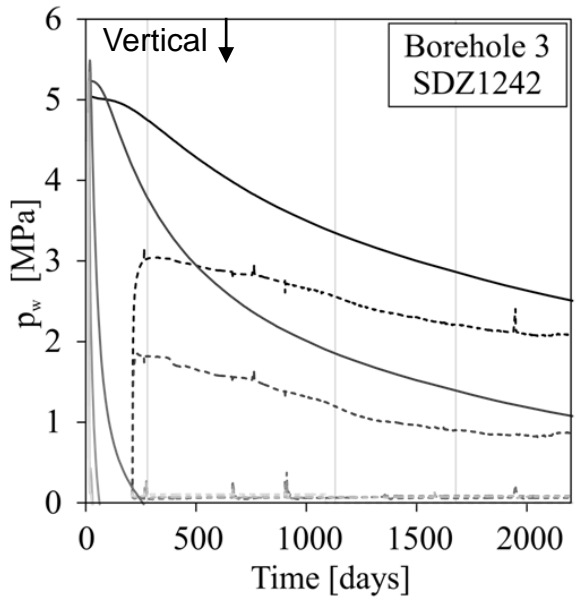
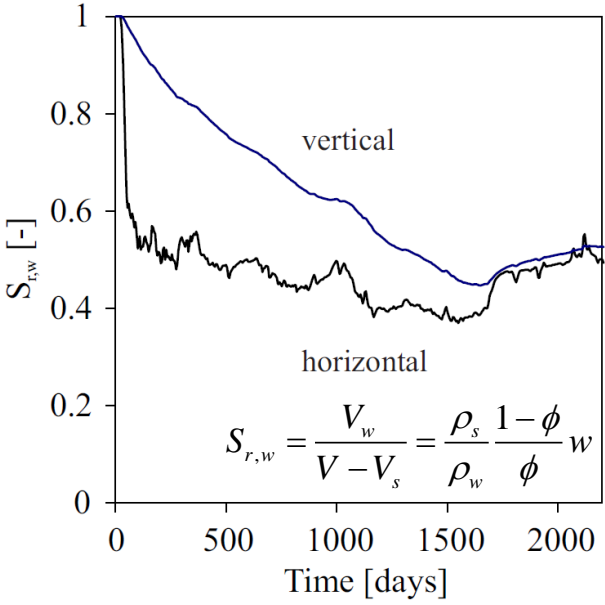
# Permeability evolution and water transfer

- Desaturation EDZ / w reproduction

At gallery wall

→ Low vertical drainage

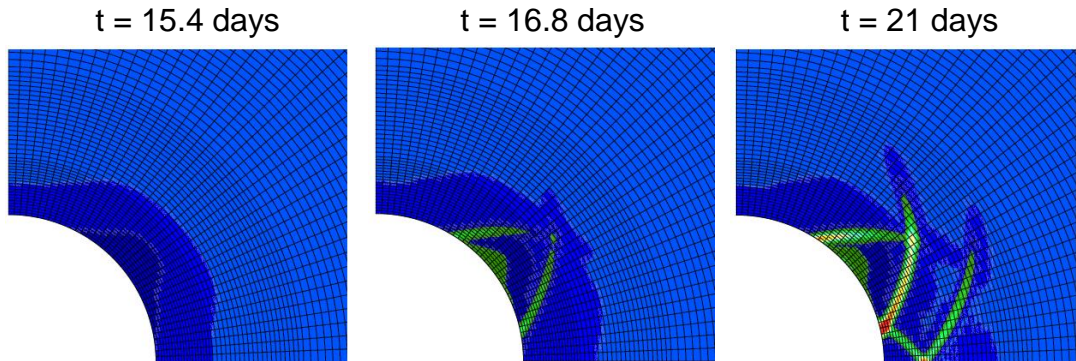
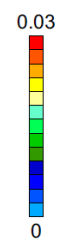
→  $k_{w,h} > k_{w,v}$  :  $k_{w,h/v} = 4 \cdot 10^{-20} / 1.33 \cdot 10^{-20} [m^2]$



# Mechanical anisotropy

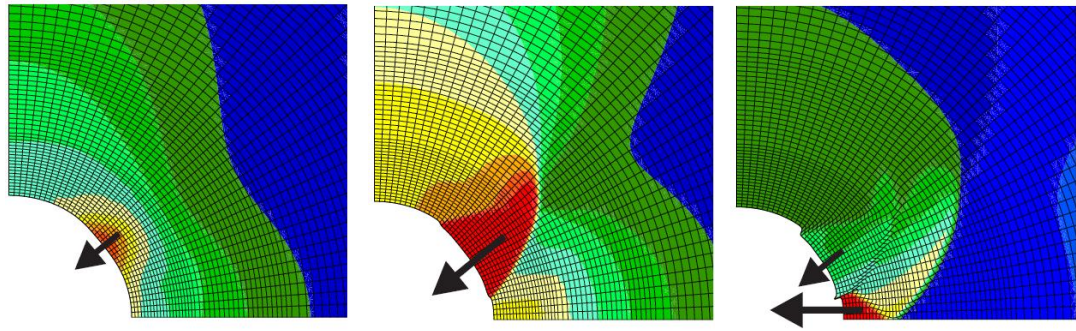
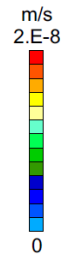
- Convergence

Total deviatoric strain

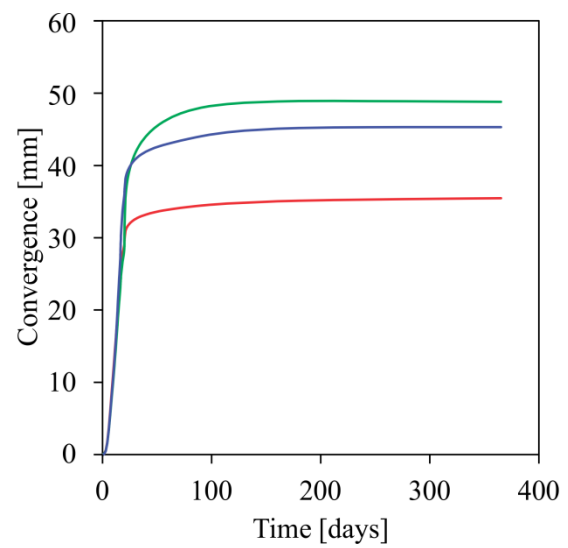
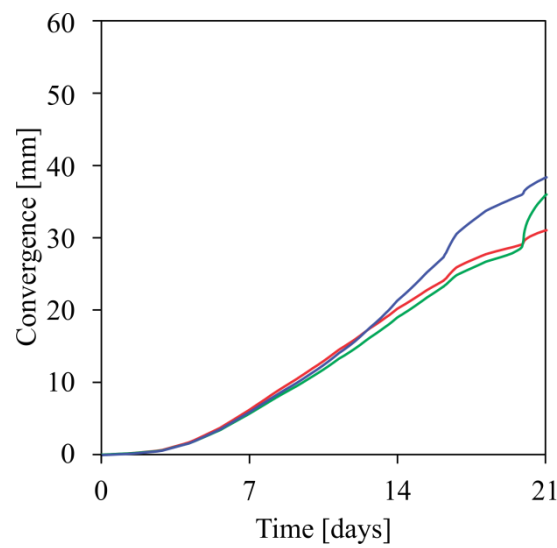


Velocity norm

$$\|v\| = \sqrt{v_x^2 + v_y^2}$$



Diametrical convergence



Numerical localised:  
 - Horizontal (green line)  
 - Inclined 45° (blue line with asterisk)  
 - Vertical (red line)

# Kinetics of drying process – Mixed boundary condition

## - Non-classical mixed boundary condition

Progressive thermodynamic equilibrium by vapour transfer.

Vapour transfer in a boundary layer.

## - Non-classical mixed boundary condition

Liquid water + water vapour

$$\bar{q}_w = \bar{S} + \bar{E}$$

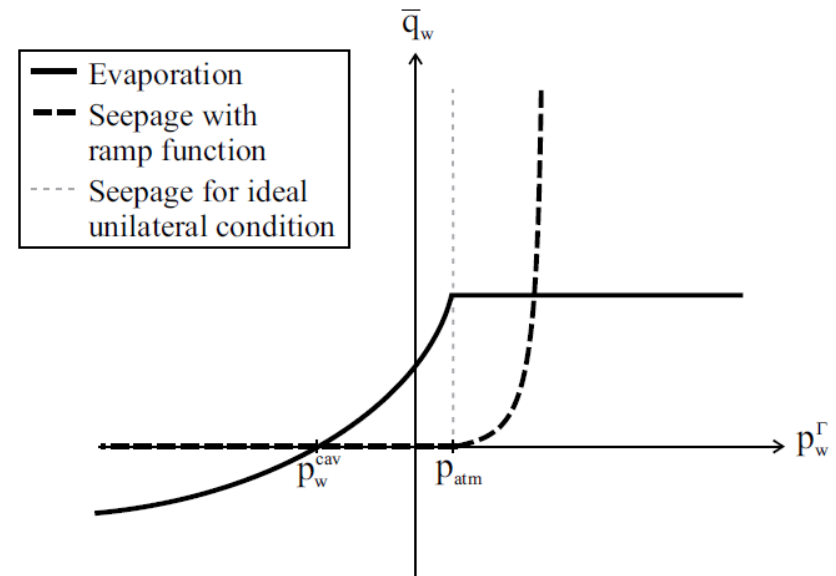
## - Seepage flow :

$$\begin{cases} \bar{S} = K^{pen} (p_w^\Gamma - p_{atm})^2 & \text{if } p_w^\Gamma \geq p_w^{air} \text{ and } p_w^\Gamma \geq p_{atm} \\ \bar{S} = 0 & \text{otherwise} \end{cases}$$

## - Evaporation flow :

(Nasrallah and Perre, 1988)

$$\bar{E} = \underline{\alpha}_v (\rho_v^\Gamma - \rho_v^{air})$$



Evaporation and seepage flows at gallery wall for a constant air ventilation (Gerard et al., 2008).

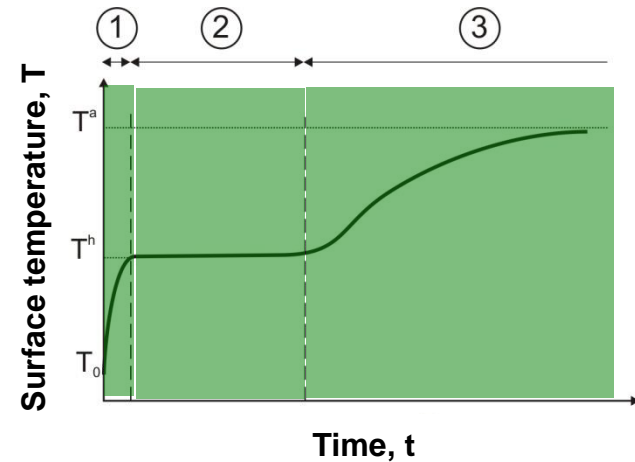
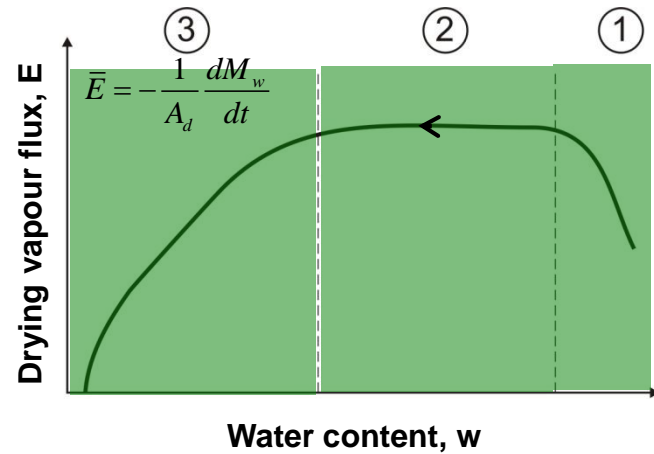
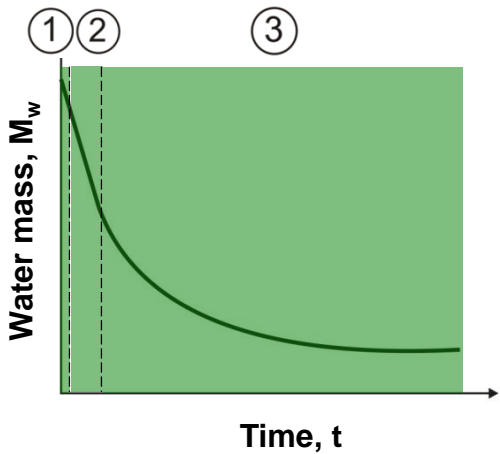
# Kinetics of drying process – Water vapour transfer

Drying test : saline solutions (control vapour phase & RH), or convective drying tests

Drying flux curve:

Thermo-hydraulic process and exchanges in a boundary layer.

1. Preheating
2. Constant flux : heat totally used for water evaporation, saturated boundary layer, external conditions (RH, T, v).
3. Decrease of the flow : internal resistances restrict the water outflow, desaturation of the boundary layer

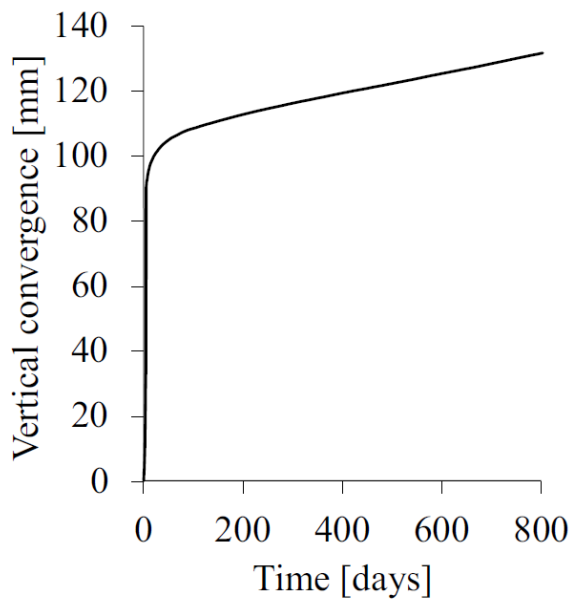
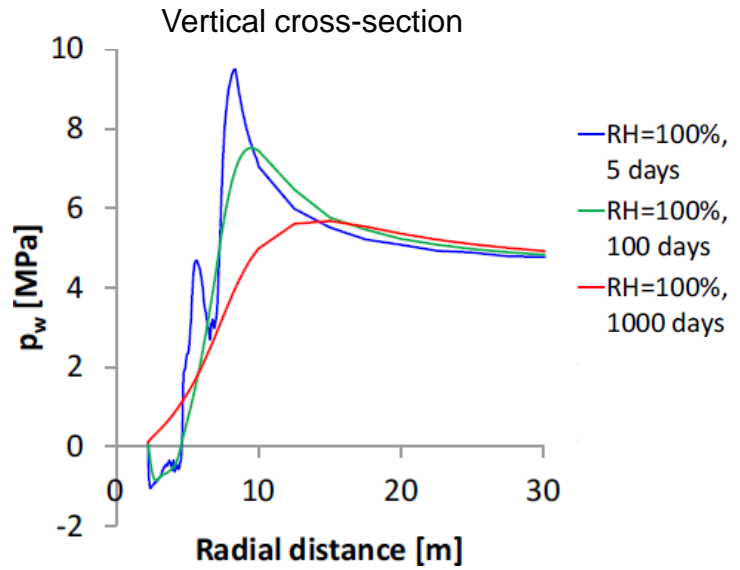
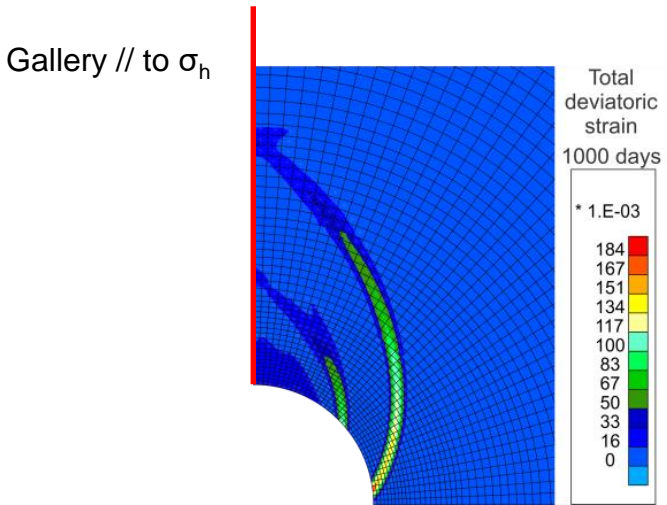


$$\bar{E} = \alpha_v (\rho_v^\Gamma - \rho_v^{air})$$

$$\alpha_v = \frac{\bar{E}_{max}}{\rho_v^\Gamma - \rho_v^{air}} = \frac{\max\left(-\frac{1}{A_d} \frac{dM_w}{dt}\right)}{\rho_v^{0,\Gamma}(T^h) - RH \rho_v^{0,air}(T^a)}$$

→  $\alpha_v$  depends on external drying conditions (RH, T, v)

## Gallery excavation modelling for anisotropic initial stress state



Close to gallery wall:  
 Strong effect of the localisation bands  
 $\sigma^r = \text{cst}$ ,  $p_w \uparrow$ ,  $\sigma^t \downarrow$ ,  $\epsilon^p \uparrow$  (on the yield surface)  
 Convergence keep increasing

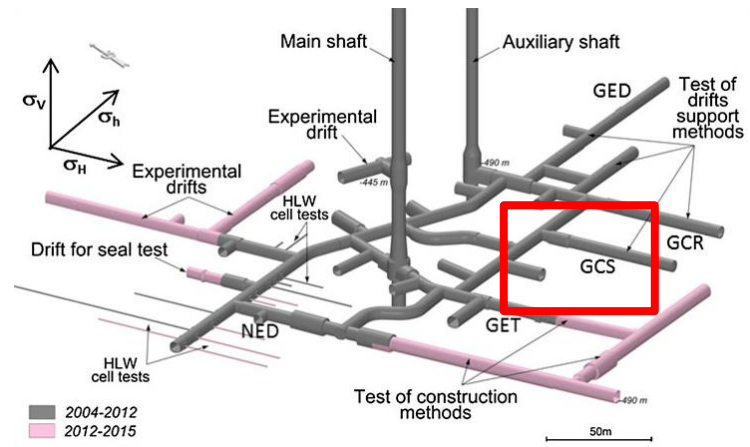
In the vertical: similar



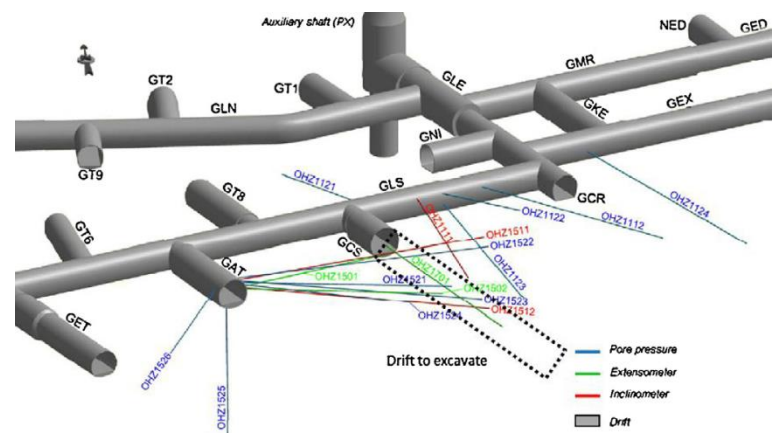
# Mine-by experiment

## - Displacements

Andra's URL

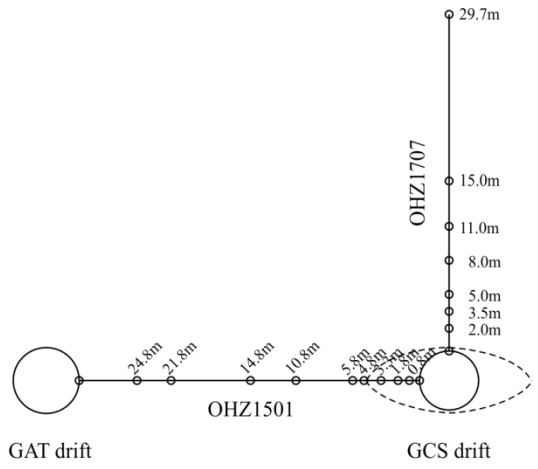
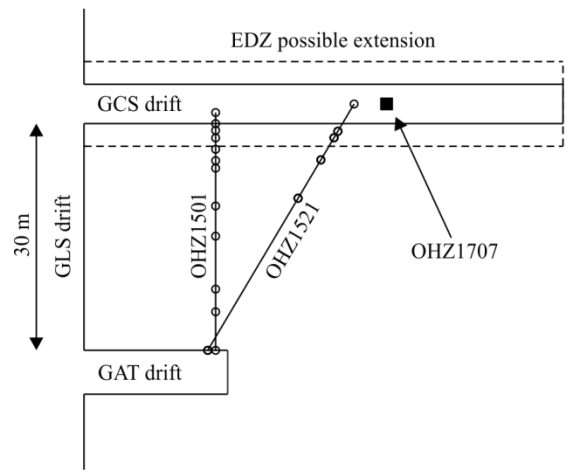


Mine-by experiment



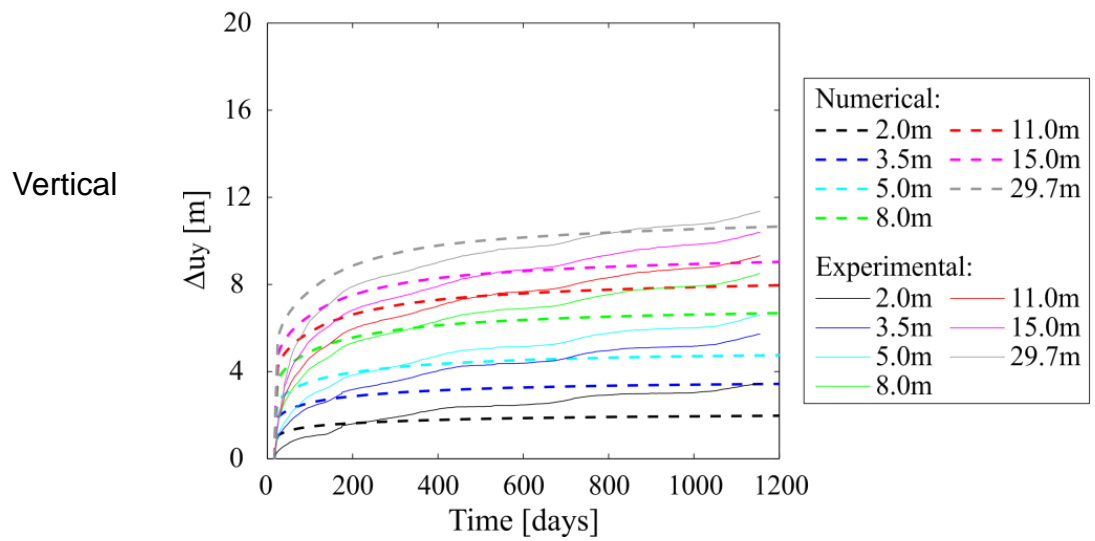
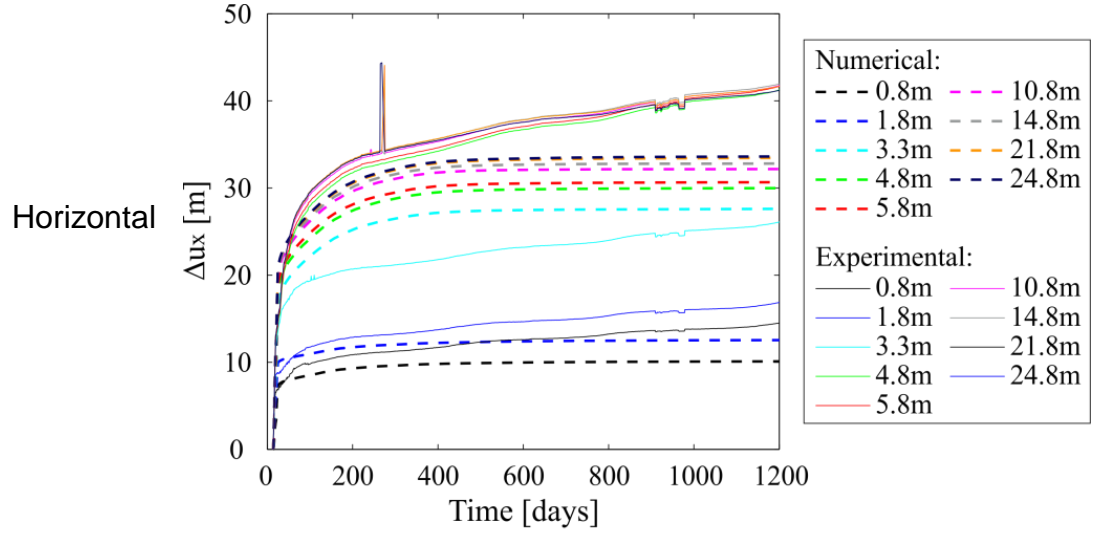
## Borehole – extensometers and pore pressure

→ Characterise the displacements in the rock mass

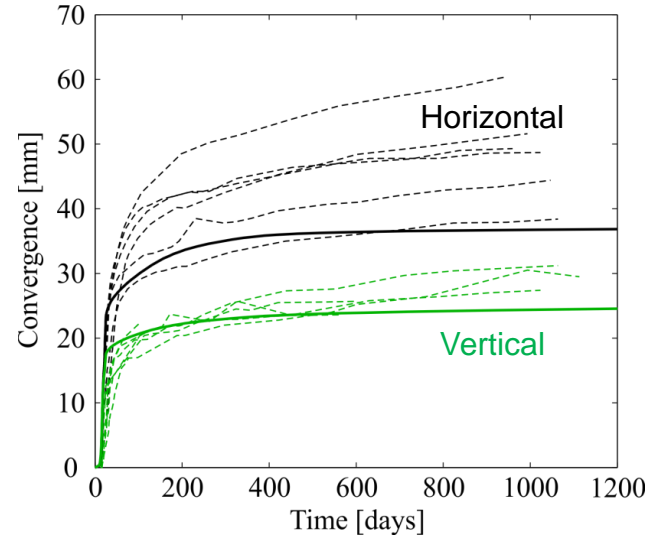


## - Displacements

Viscosity based on **creep tests**

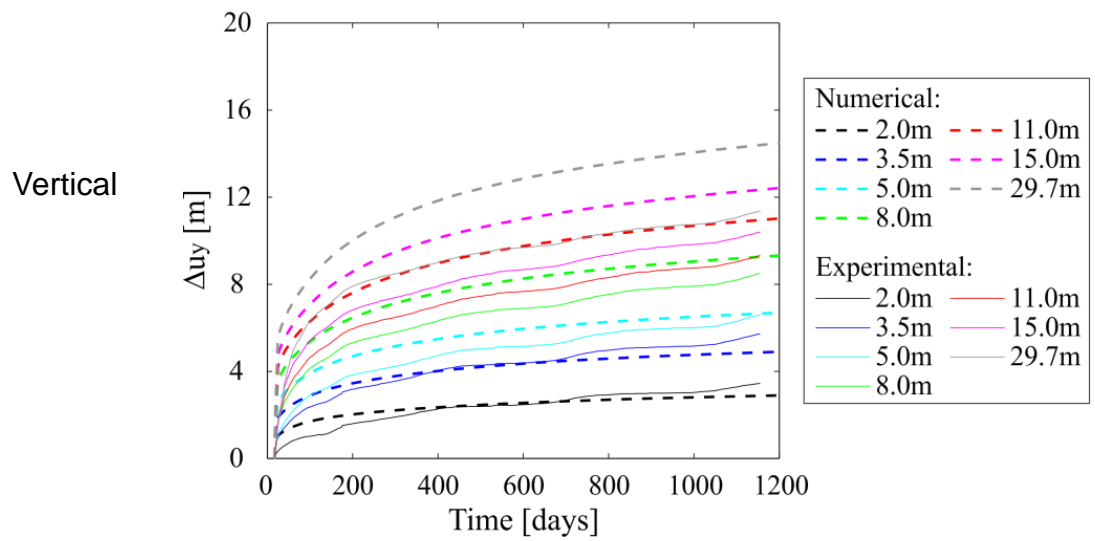
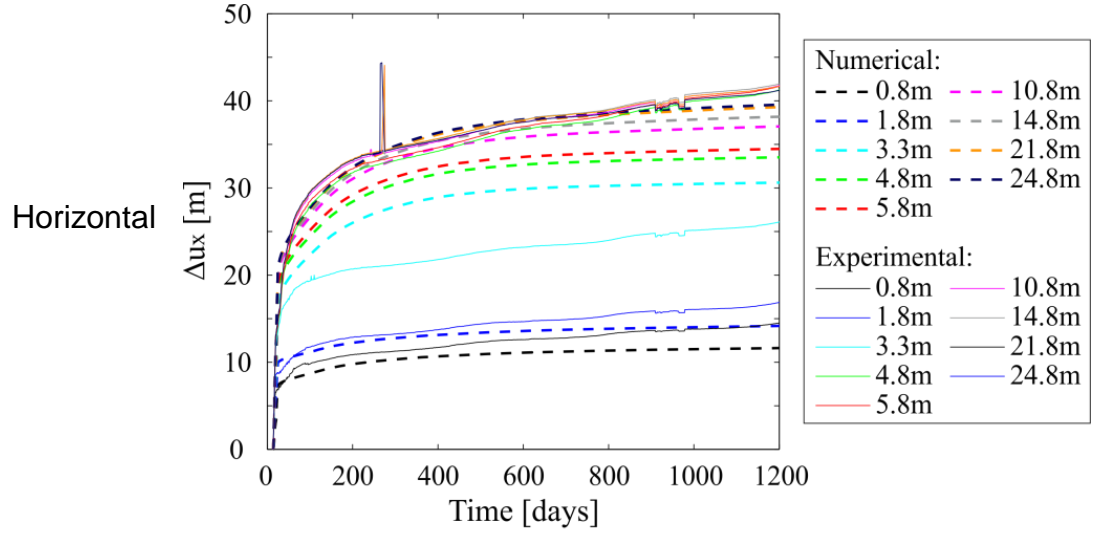


## - Convergence

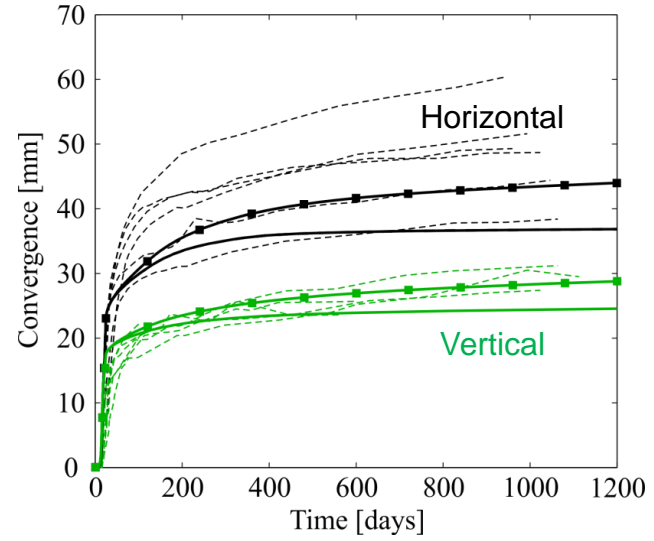


## - Displacements

Viscosity based on **in situ measurements** → Viscosity influence



## - Convergence

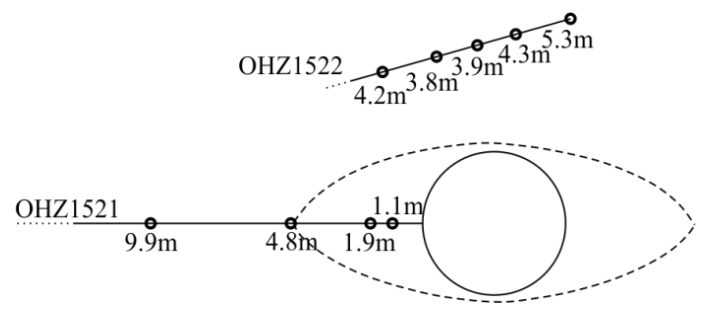


Viscosity allows to reproduce the increase of convergence in the long term.

# Mine-by experiment

- Pore water pressure

Mine-by test



After excavation: RH=100% ,  $p_w = 0$  MPa in the gallery

Horizontal:

