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Non-linear behaviour of concrete beams reinforced with GFRP and CFRP bars grouted in sleeves

Mostafa Kazemi¹, Jie Li², Salar Lahouti Harehdasht³, Negin Yousefieh⁴, Soheil Jahandari⁵,
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Abstract

The low-quality bond between fibre reinforced polymer (FRP) bars and surrounding concrete has drawn the attention of many researchers. The use of high-strength materials such as the grout in the intersection of FRP bars and surrounding concrete can effectively prevent any slippage once they are in contact and subsequently increase the bond quality. Therefore, this study was numerically focused on the flexural behaviour of concrete beams reinforced with glass fibre reinforced polymer (GFRP) and carbon fibre reinforced polymer (CFRP) bars, grouted only in the pure bending zone and along the whole beam length. The numerical outputs revealed that the grouted GFRP bars propagated the maximum principal stress in high-strength concrete beams, but not as much as that in normal-strength concrete specimens. In addition, the stress distribution in the grout, created only in the pure bending zone, was nearly constant at the ultimate moment. For the grout, developed along the whole beam length, this stress increased by approaching the mid-span of the concrete beam. Furthermore, at the ultimate moment, the tensile stress of 12-mm diameter CFRP bars was about 3.5 times more than that of the 16-mm diameter CFRP bars, leading to the generation of difference between failure modes of concrete specimens reinforced with various diameters of CFRP bars.

Keywords: Flexural behaviour; pure bending zone; grouted FRP bars; FE analysis.

1. Introduction

Corrosion of steel reinforcement bars is known as one of the major causes of structural deterioration, and it is estimated that about 4% of the gross domestic product of industrialized countries is accounted for the cost of corrosion [1, 2]. One of the innovative solutions to reduce the effect of corrosion in the tension region of concrete components is to replace the flexural steel bars with fibre reinforced polymer (FRP) bars which can be considered as a viable substitute to the other options in the construction sector [3-7]. Different types of FRP bars including carbon fibre reinforced polymer (CFRP), glass fibre reinforced polymer (GFRP), and aramid fibre reinforced polymer (AFRP) bars have been proposed by researchers due to some advantages including low density, corrosion resistance, and high tensile strength [8-11].

Of all FRP composite materials, the GFRP flexural bar [12] has drawn the attention of researchers owing to its corrosion resistance feature. Regarding this, the behaviour of concrete specimens strengthened with steel transverse reinforcement and GFRP flexural reinforcement was assessed with Khorasani et al. [13, 14]. They showed that the ultimate load of GFRP strengthened concrete increased by increasing the level of concrete strength and the GFRP reinforcement ratio. Meanwhile, the failure mode of the aforementioned composite components with and without transverse reinforcement was found to be rupture and shear, respectively. A similar study by Ashour [15] showed that the major diagonal crack was generated in the GFRP reinforced concrete components with no stirrup at failure load and the type of failure mode was shear. Another study by Ospina and Bakis [16] demonstrated that higher amount of the GFRP flexural reinforcement ratio in concrete beams led to narrower crack widths. In addition, a decrease in the bar diameter led to a lower tensile strength of GFRP bars [17].

The CFRP bar is proposed by researchers as another reinforcing material, having higher chemical resistance and suitable tensile properties. Concerning this, Brozda et al. [18] demonstrated that the tensile strength of CFRP bars, embedded in concrete elements, was found to be very high and a linear elastic characteristic was observed for CFRP bars until rupture. El-Hacha and Gaafar [19] assessed the performance of concrete beams strengthened with a 9-mm diameter CFRP bar. According to the outputs, the use of CFRP bar effectively led to an increase in the load-bearing capacity and delaying the opening new cracks in the concrete beams until ultimate load. A study by Rafi et al. [20] showed that a negligible difference appeared between the cracking pattern of concrete beams strengthened with CFRP and steel bars. Meanwhile,

concrete specimen strengthened with 9.5-mm diameter CFRP bar had high deformability factors, demonstrating its ductile nature of failure. Recently, Mustafa and Hassan [21] evaluated the influence of various diameters of CFRP flexural reinforcement on the failure mode of concrete beams. The results showed that these components strengthened with CFRP bars with the diameters of 16, 18, 20 and 22 mm were failed by concrete crushing rather than by rupture FRP reinforcement.

Apart from some advantages of FRP bars, the bond quality at the interface between concrete materials and FRP reinforcement is not as much as that of the concrete materials and conventional steel bars. So, the substitution of steel bar with FRP bars in concrete members causes to generate larger deflections, leading to wider cracks in the tension zone owing to the low elastic modulus of FRP materials [22, 23]. This bond quality at the interface between FRP bars and concrete members can be somewhat improved by partial replacement of normal-strength concrete materials with the high-strength cement grout, surrounding the FRP bars [23-25]. Dong et al. [26] assessed the bendability of concrete components strengthened with CFRP and GFRP bars embedded in the grout. They showed that the utilization of high-strength cement grout, holding GFRP and CFRP bars, decreased crack widths and improved the serviceability behaviour of concrete beams. It can be stated that previous studies have mainly focused on experimentally evaluating the flexural behaviour of concrete components strengthened with FRP bars grouted in sleeves. To get a better understanding of the non-linear behaviour of FRP-strengthened concrete specimens, the participation of transverse and flexural reinforcement, grout and concrete components in carrying different amounts of loading is required to be assessed numerically in details. Meanwhile, the level of concrete strength can affect the stress distribution in these specimens. Therefore, for further investigation, the flexural performance of concrete beams reinforced with GFRP and CFRP bars grouted in sleeves was numerically analyzed at nominal and ultimate moments in this study, where the contour plots of the stress distribution showed how different components of FRP-reinforced concrete beams participated in carrying the generated stress intensity. In addition, the non-linear behaviour of the grout, surrounding the FRP bars within the pure bending zone and along the whole beam length was effectively analyzed at nominal and ultimate moments using the contour plots of damage variable and stress distribution, which played a key role in the bending behaviour of FRP-reinforced concrete beams. Furthermore, the results also provided a comparison between the CFRP and GFRP bars' abilities

to participate in the distribution of maximum tensile stress along the beam length, where the effect of GFRP and CFRP reinforcement ratio on the failure mode was analyzed. Meanwhile, the influence of normal- and high-strength concrete on the stress distribution and load-bearing capacity of FRP reinforced concrete beams was assessed. Generally, the interaction between different components of FRP-reinforced concrete beams within the pure bending zone and along the whole beam length was numerically evaluated and the results were compared to each other.

2. FE modeling

2.1. Material properties and numerical models

To model the concrete components strengthened by steel flexural bar and GFRP and CFRP composite bars, the ABAQUS software was employed in this study. The mechanical properties of conventional steel and GFRP and CFRP bars are presented in Table 1. The Poisson's ratio for all of the flexural bars was considered to be equal to 0.3, as suggested by other researchers [27, 28]. The experimental outputs, given by Dong et al. [26], were used to verify the numerical models. As shown in Fig. 1, three cases were considered by Dong et al. [26]. In some cases, FRP composite bars were employed to strengthen concrete components in the absence of high-strength grout in the tension region (Fig. 1(a)). FRP composite bars only in the pure bending zone of some other concrete components were surrounded by the grout (Fig. 1(b)). Meanwhile, the whole length of FRP composite bars in the last specimen was grouted in sleeves (Fig. 1(c)). It is noteworthy that the diameter of flexural steel bar was equal to 12 mm. To assess the effect of various sizes of FRP composite bars on the bending behaviour of concrete components, two diameters of 12 and 16 mm were considered for GFRP, CFRP bars. According to the experimental considerations, for top and middle longitudinal reinforcements of concrete beams 10-mm diameter plain steel bars were numerically employed.

The internal and external diameters of the sleeve component were equal to 33 mm and 36 mm, respectively, and the thickness of this component was 0.3 mm thickness. As reported by Dong et al. [26], the sleeve was made the helically wrapping corrugated galvanized strip. Therefore, the yield and ultimate stresses of this component were assumed to be 250 MPa, and 350 MPa, respectively, as recommended by Sarycheva et al. [28].

Generally, 12 concrete beams were modeled and reinforced with different diameters of steel, GFRP, and CFRP bars (Table 2). Among these concrete components, 10 normal-strength concrete beams (30 MPa) were verified with experimental data given by Dong et al. [26]. After verifying the numerical models of G12-P and G12-W, the mechanical properties of normal-strength concrete were replaced with those of high-strength concrete to assess the influence of high-strength concrete (60 MPa) on the non-linear behaviour of beam strengthened with grouted GFRP bars (G12-P-H and G12-W-H). It is noteworthy that GFRP flexural bars in the G12-P-H specimen were grouted in sleeves only in the pure bending zone, while GFRP flexural bars in the G12-W-H specimen were grouted along the whole length of the beam.

In all numerical models, the compressive strength of grout was assumed to be 60 MPa, similarly to what was obtained from 40×40×160mm prisms as reported by Dong et al. [26]. Meanwhile, the corresponding strength for the normal- and high-strength concrete was equal to 30 MPa and 60 MPa, respectively. The elastic modulus of concrete materials was calculated using the Eq. 1 as suggested by Hognestad [29].

$$E_c = 4700\sqrt{f_c} \quad (1)$$

Where E_c and f_c were the elastic modulus and compressive strength of concrete materials in MPa, respectively. Therefore, the elastic modulus of the grout was assumed to be 36400 MPa. Meanwhile, this value for the normal- and high-strength concrete was 25700 MPa and 36400 MPa, respectively. On the other hand, the peak strain of concrete and grout in this study was assumed to be 0.0035 at the most as recommended by Hognestad [29].

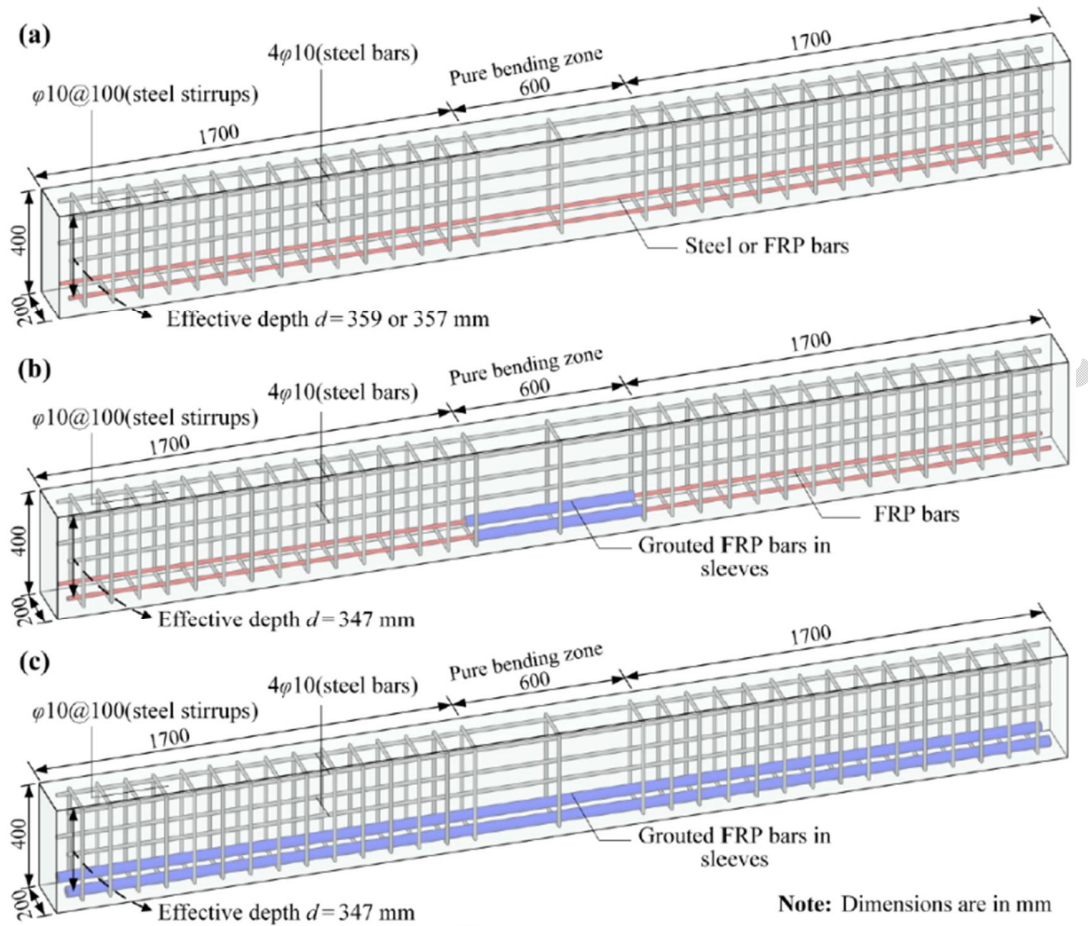


Fig. 1. Reinforcing bars details of concrete components strengthened with conventional steel or FRP composite bars (a); the grouted FRP composite bars only in the pure bending region (b); and wholly grouted FRP composite bars [26].

Table 1. Mechanical properties of steel, GFRP, and CFRP bars.

Type of the bar	Dimeter of bar (d_b) (mm)	Area of flexural bar (A_f) (mm ²)	Yield Stress (f_y) (MPa)	Ultimate stress (f_{tu}) (MPa)	Modulus of Elasticity (E_f) (GPa)	Poisson Ratio
Steel	10	78.5	350	-	195	0.3
	16	201.1	449	-	197	0.3
GFRP	12	113.1	-	947	45.4	0.3
	16	201.1	-	889	46.4	0.3
CFRP	12	113.1	-	1890	136.4	0.3
	16	201.1	-	1600	127.6	0.3

^e Modulus of Elasticity

Table 2. Details of reinforced concrete beams.

Specimens	Flexural reinforcement		$A_f E_f$ (MN)	d^a (mm)	Transverse reinforcement
	Type	Amount			
S ^b 16	Steel	2Ø16	39.6	357	Ø10@100
G ^c 12-N ^d		2Ø12	5.1	359	Ø10@100
G12-P ^c		2Ø12	5.1	347	Ø10@100
G12-W ^f		2Ø12	5.1	347	Ø10@100
G12-P-H ^g	GFRP	2Ø12	5.1	347	Ø10@100
G12-W-H		2Ø12	5.1	347	Ø10@100
G16-N		2Ø16	9.3	357	Ø10@100
G16-P		2Ø16	9.3	347	Ø10@100
C ^h 12-N		2Ø12	15.4	359	Ø10@100
C12-P		2Ø12	15.4	347	Ø10@100
C16-N	CFRP	2Ø16	25.7	357	Ø10@100
C16-P		2Ø16	25.7	347	Ø10@100

^a Distance from extreme compression fibre to centroid of tension reinforcement

^b Steel bar

^c GFRP bar

^d Specimen with FRP bars

^e Specimen strengthened with grouted FRP composite bars only in the pure bending region

^f Specimen strengthened with wholly grouted FRP composite bars

^g High-strength concrete specimen

^h CFRP bar

2.2. Concrete Damaged Plasticity Model

In ABAQUS software, the crack model of concrete damaged plasticity (CDP) was used to analyze both non-linear compressive and tensile behaviours of concrete beams [30, 31] (Fig. 2). Eqs. (1) and (2) show the relationships between the stress and strain of concrete to develop the CDP model at tension and compression.

$$\sigma_t = (1 - d_t) E_c (\varepsilon_t - \varepsilon_t^{pl}) \quad (1)$$

$$\sigma_c = (1 - d_c) E_c (\varepsilon_c - \varepsilon_c^{pl}) \quad (2)$$

Where E_0 is the Young's modulus of concrete, d_c and d_t are compressive damage variable (DAMAGEC) and tensile damage variable (DAMAGET), respectively, and ε_c^{pl} and ε_t^{pl} are equivalent plastic strains at compression and tension, respectively [32].

Some parameters were considered in ABAQUS software to develop the CDP model. One of these parameters was the viscosity parameter (μ). This parameter permits to moderately exceed the plastic potential surface area in certain sufficiently small problem steps. Thus, it needs to arrange the value of viscosity parameter a few times to specify its effects on the problem solution result in ABAQUS and to suitably select a minimum value of μ . By considering this, a very small number was assumed for μ as suggested by other researchers [31, 33, 34]. The behavior of concrete under compound stress can be determined using the parameter of dilation angle (ψ). This parameter was considered to be 31 degrees as recommended by Szczecina and Winnicki [35]. Another parameter is the modification coefficient of the deviatoric plane (K_c), which can be controlled by the utilization of the Drucker-Prager yield criterion to assume the yielding pattern for stress-strain curves of concrete [36]. According to Fig. 3, the failure surface in the deviatoric cross section can be controlled using K_c and it is not required to be considered a perfect circle as shown in Fig. 3. As suggested by other researchers [37], K_c can be in the range of 0.5-1. Therefore, the value of 0.667 was assumed for this parameter in the CDP model. σ_{b0}/σ_{c0} is the ratio of initial biaxial compressive yield stress to initial uniaxial compressive yield stress. As recommended in the ABAQUS user's manual [31], the amount of 1.16 was considered for this ratio. The ratio of tensile to compressive strength is introduced as the parameter of flow potential eccentricity (ε) in the CDP model. As suggested by other researchers [33, 34], the value of 0.1 was introduced to the software for this parameter.

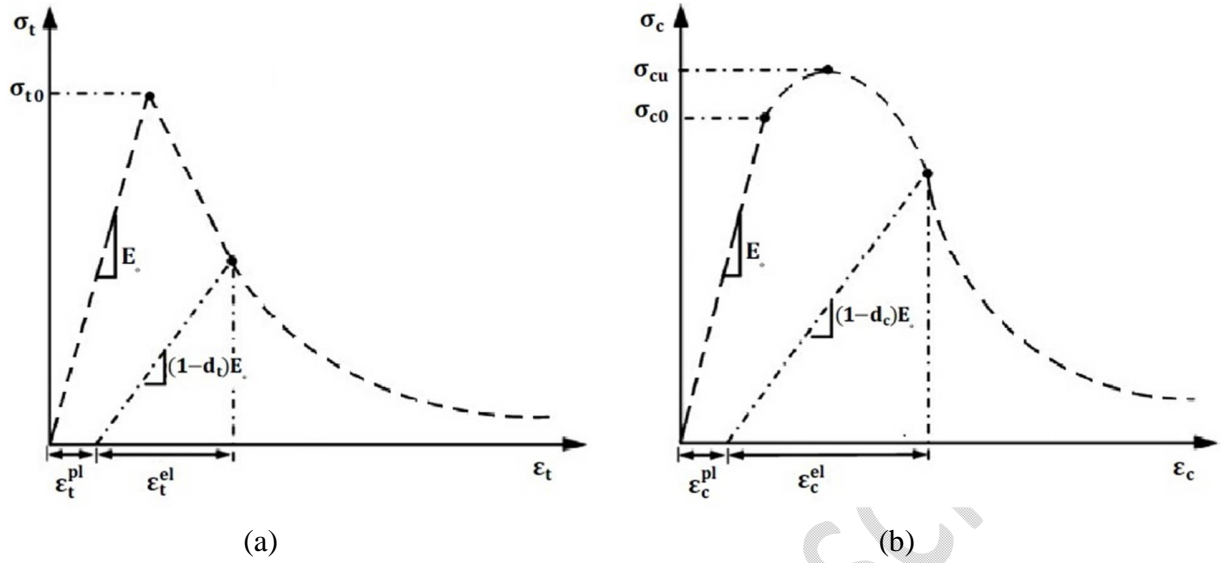


Fig. 2. Proposed non-linear tensile (a) and compressive (b) behaviours of concrete component, employed in ABAQUS.

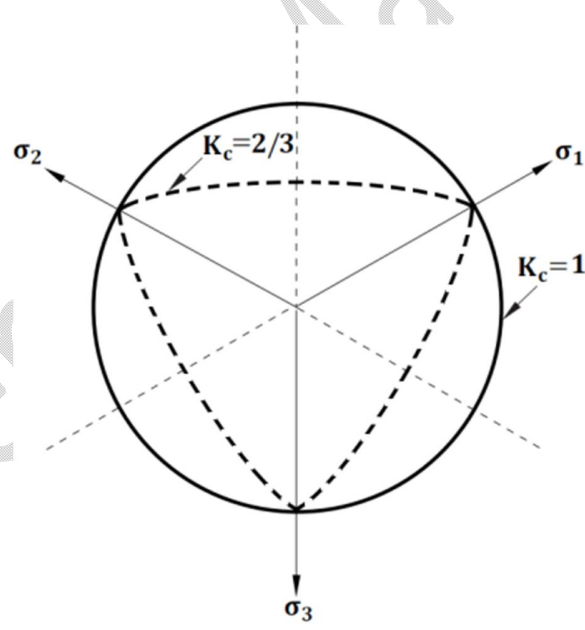


Fig. 3. Yield patterns obtained by utilizing Drucker-Prager yield criterion to control K_c values.

2.3. Components of numerical models and features of element type

Figs. 4 and 5 show the components of numerical models including two rigid sections as supports, two other rigid sections as load cells, a concrete beam, grout, sleeve, stirrups, steel, and GFRP and CFRP bars. To model stirrups, steel, and GFRP and CFRP bars, the element type of 3D deformable wire (truss element) was employed. In addition, as recommended by other researchers [33, 38, 39, 40, 41, 42], the element type of three-dimensional (3D) hexahedral element, with 8 nodes and reduced integration (C3D8R) was used to simulate the concrete beam, grout, sleeve, and rigid sections.

Suitable mesh sizes were introduced to each reinforced concrete beam. For S16, G12-N, G12-P, G12-W, G12-P-H, G12-W-H, G16-N, G16-P, C12-N, C12-P, C16-N and C16-P, the approximate element sizes of 90, 110, 110, 100, 100, 110, 110, 90, 110, 110, 90 and 110 mm, respectively, were introduced to longitudinal steel and FRP bars. The same element sizes were considered for the pure bending zone of concrete beams in the longitudinal direction. The approximate element size of 120 mm was considered for other parts of concrete beams in the aforementioned direction. The mesh size of transverse reinforcement was assumed to be 40 mm for all concrete beams.

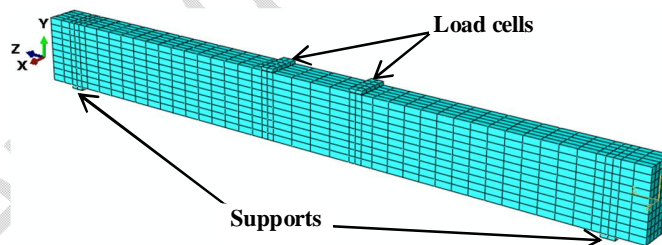


Fig. 4. FE mesh of the reinforced concrete beam.

2.3. Loading pattern, surface interaction and boundary condition

The constraint of tie was introduced to the intersection of sleeves and grout. The same constraint was used in the intersection between the load cells and concrete beam. When surrounded by the grout, FRP bars can be considered to be embedded in the grout. Thereafter, all bars, stirrups, sleeves, and grout were embedded in the concrete beam. The surface to surface contact was utilized to define the intersection between supports and concrete component in which no slip happened once points were in contact. Fig. 5 shows the surfaces for applying load.

To realistically model the reinforced concrete beams, the rotations and displacements of rigid supports were effectively restricted.

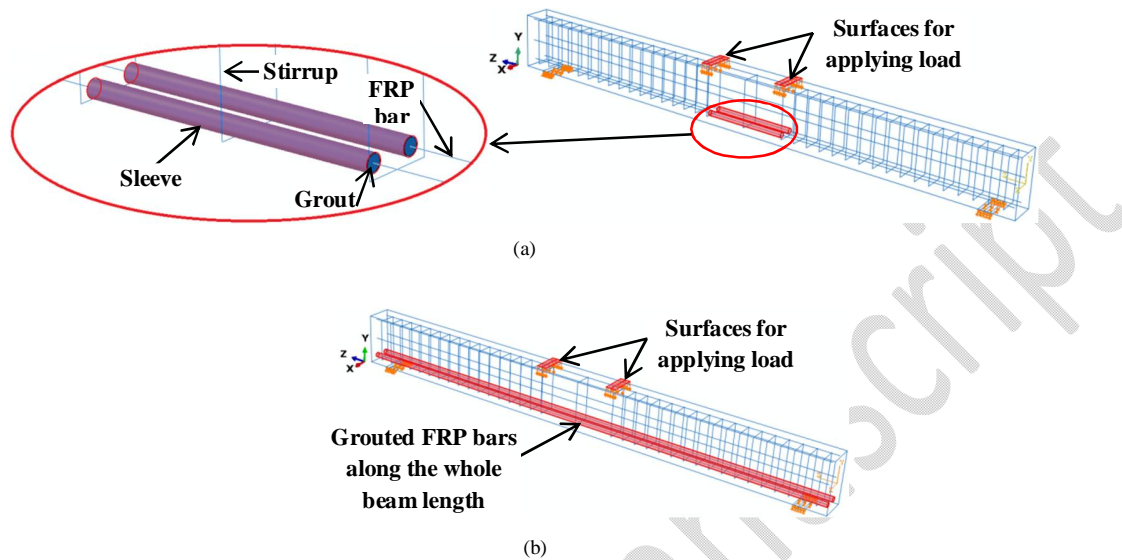


Fig. 5. Configuration of the developed concrete specimens with wholly grouted FRP composite bars: in the pure bending zone (a); and along the whole beam length (b).

3. Verification of FE model

A comparison between the experimental data given by Dong et al. [26] and the numerical outputs from this study was performed. As shown in Fig. 6, the curves of load against mid-span deflection for numerical models were observed to be moderately higher than those of the experimental specimens at the beginning of loading, owing to the initial stiffness of the numerical models. This minor difference was negligible and the curve slopes of numerical and experimental outputs were nearly the same. On the other hand, as shown in the tensile damage variable (DAMAGET) (Figs. 7 and 8) and compressive damage variable (DAMAGEC) (Fig. 9), the numerical models were nearly failed in the pure bending zone, similar to what was observed in the experimental specimens.

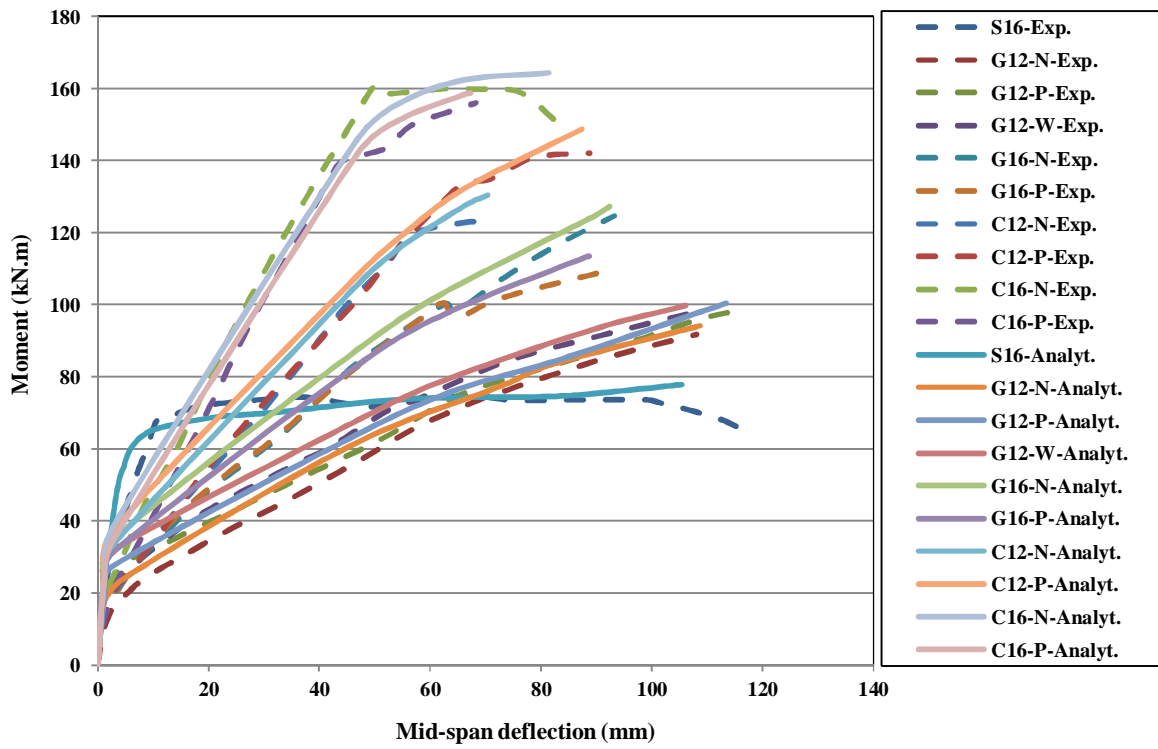


Fig. 6. Load vs. mid-span deflection plot for FRP reinforced concrete beams.

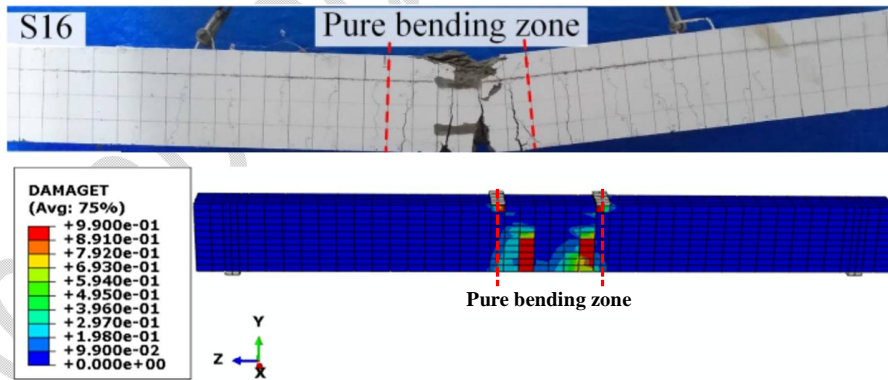
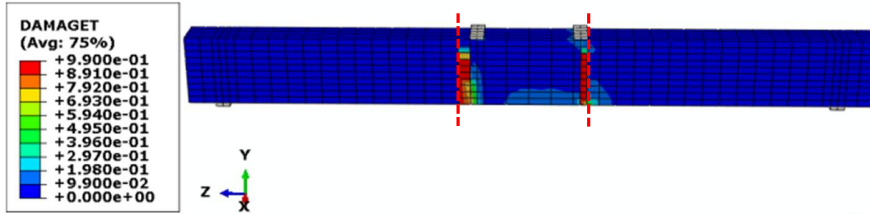
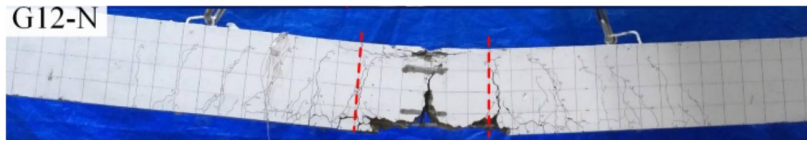
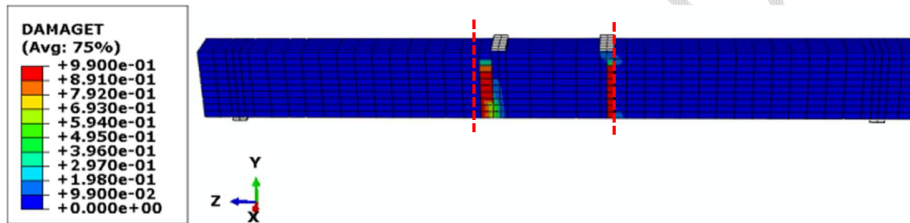
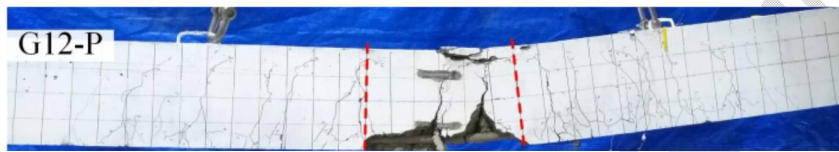


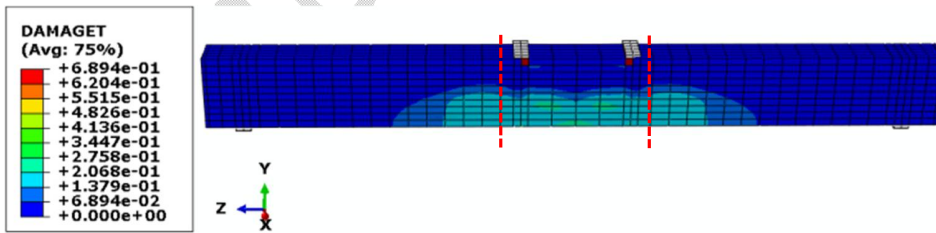
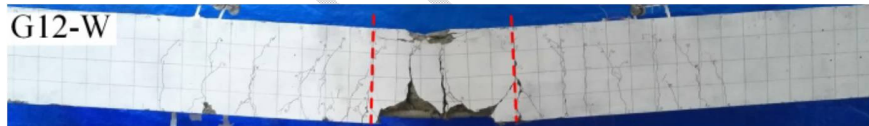
Fig. 7. Failure mode of steel yielding followed by concrete crushing in the pure bending zone for S16.



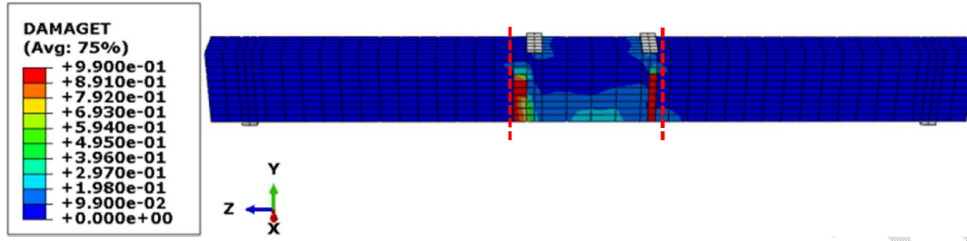
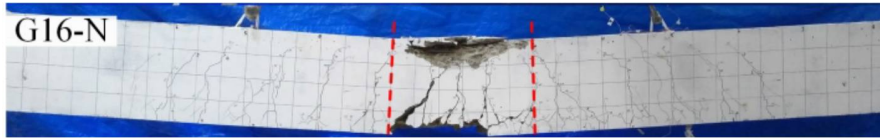
(a)



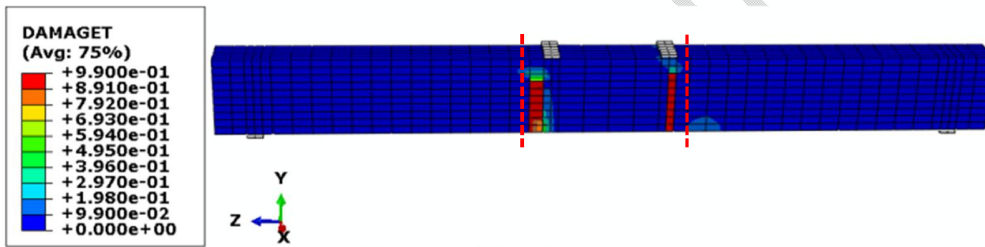
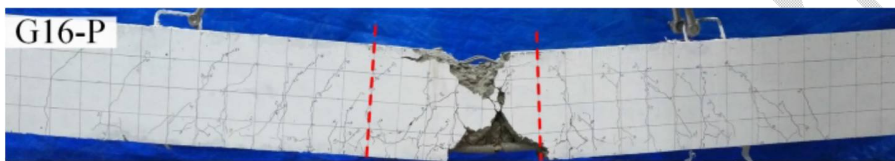
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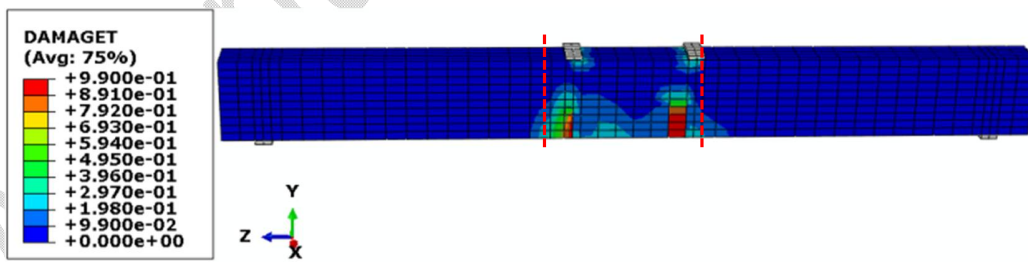
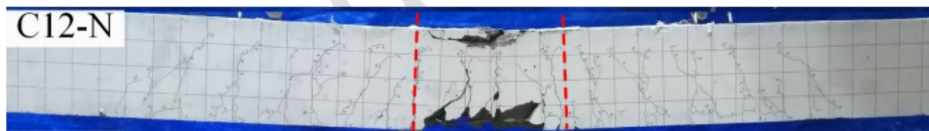
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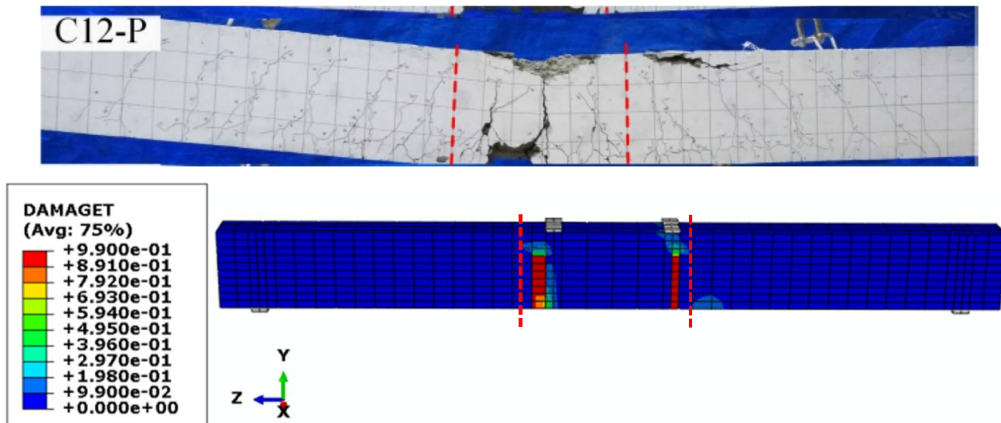
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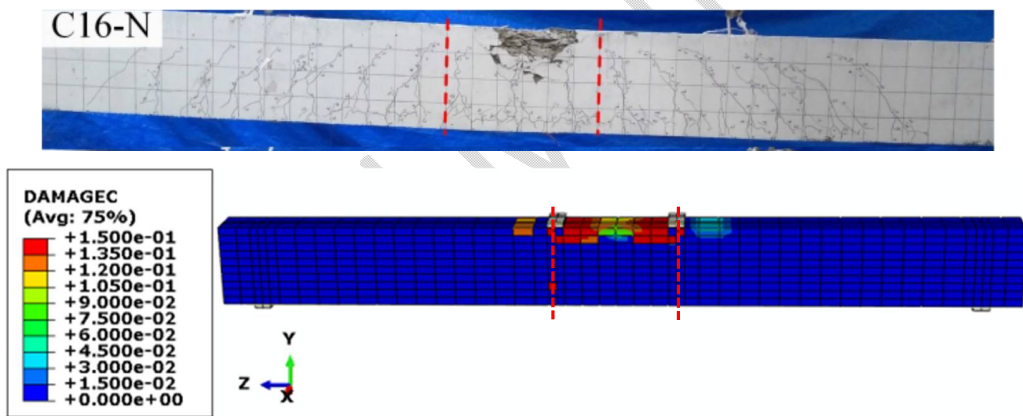


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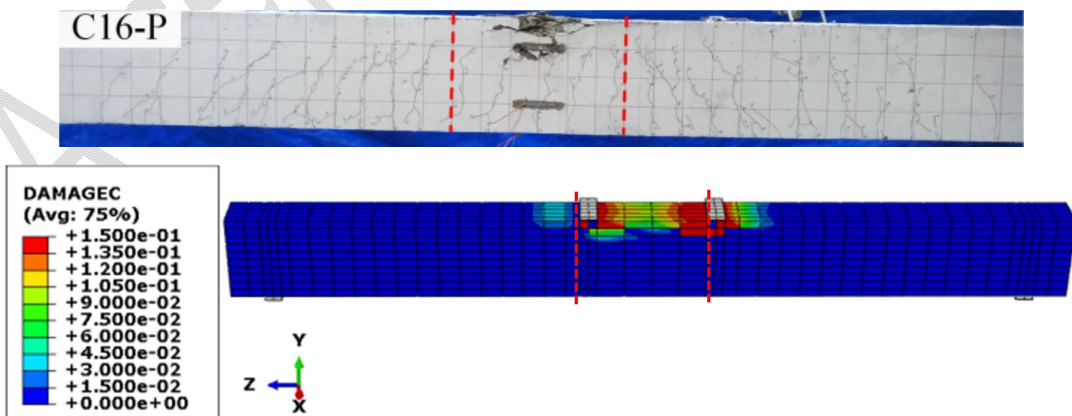


(g)

Fig. 8. Failure mode of concrete crushing followed by rupture of FRP bars in the pure bending zone for G12-N (a); G12-P (b); G12-W (c); G16-N (d); G16-P (e); C12-N (f); C12-P (g).



(a)



(b)

Fig. 9. Failure mode of concrete crushing without rupture of CFRP bars in the pure bending zone for C16-N (a); C16-P (b).

4. Results and discussions on FE analysis

According to the results, the difference between the ultimate mid-span deflection of experimental and numerical models was negligible as shown in Fig. 6. In Table 3, the values of moments, obtained by Dong et al. [26], are presented for different experimental specimens. The ultimate moments of S16, G12-N, G12-P, G12-W, G16-N, G16-P, C12-N, C12-P, C16-N and C16-P in this numerical study were respectively obtained by 2.1%, 2.6%, 2.1%, 1.3%, 2.1%, 4.2%, 5.5%, 4.7%, 8.7% and 1.7% more than those in the experimental results given by Dong et al. [26].

Table 3. Nominal and ultimate moments of reinforced concrete beams given by Dong et al. [26].

Specimens	M_n^a (kN.m)	M_u^b (kN.m)	M_u/M_n
S16	74.7	-	-
G12-N	72.8	91.7	1.26
G12-P	74.6	98.3	1.32
G12-W	74.2	98.4	1.33
G16-N	100.2	124.6	1.24
G16-P	101.5	108.8	1.07
C12-N	118.6	123.6	1.04
C12-P	119.8	142	1.19
C16-N	146.2	158.9	1.09
C16-P	140.9	156	1.11

^a Nominal moment

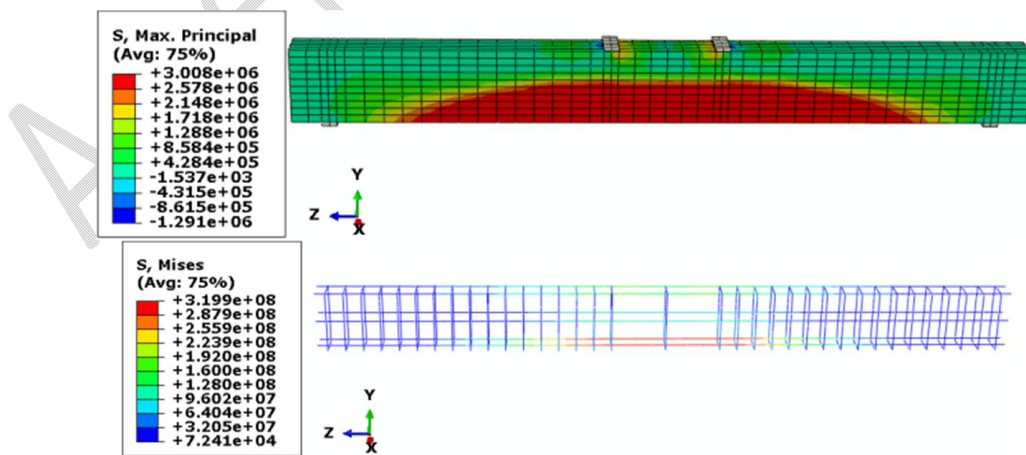
^b Ultimate moment

The numerical results provided more descriptions about the failure mechanism, load-bearing capacity and stress distribution of developed models. Meanwhile, the plots of tensile damage

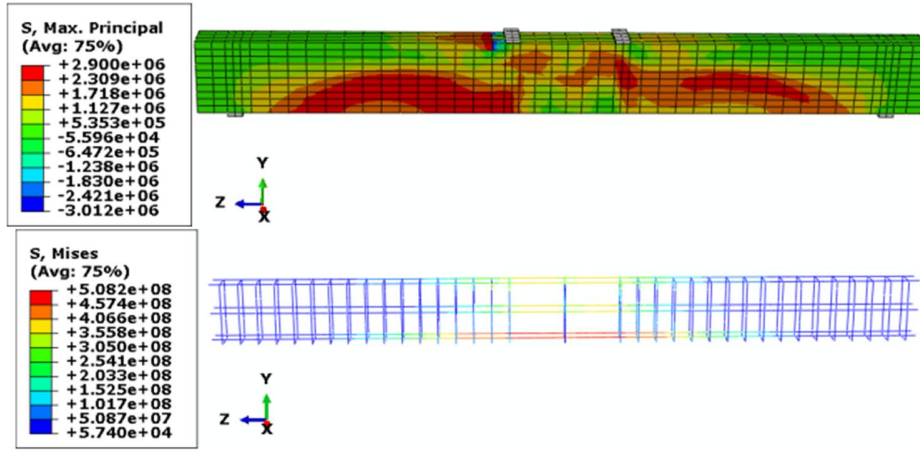
variable (DAMAGET) (Figs. 7 and 8) and compressive damage variable (DAMAGEC) (Fig. 9) were employed to analyze the failure mechanisms of numerical models. In addition, the stress distribution of reinforced concrete models was assessed at nominal and ultimate moments. To realistically predict the non-linear behaviour of ductile and brittle materials, the von Mises stress and the maximum principal stress were used in ABAQUS software as proposed by other researchers [42, 43]. Therefore, the contour plots of S, Mises and maximum principal stress were utilized to analyze the stress distribution in reinforcement and concrete element, respectively.

4.1. Failure mode and stress distribution of control beam (S16)

According to the numerical outputs for S16 model (Fig. 7), the damage was generated in the tension region within the pure bending zone. The stress distribution in the control model (S16) at nominal and ultimate moments is shown in Fig. 10. As indicated in Fig. 10(a), at nominal moment, the maximum tensile stress appeared in the tension zone near to the mid-span and it was equal to 3 MPa. Concerning the stress distribution in the steel bars, the maximum tensile stress was found to be 319.9 MPa at nominal moment. By increasing the load, the stress of flexural steel bars increased up to 508.2 MPa, which was more than the value of yield stress (449 MPa). This procedure caused to dissipate the maximum principal stress to the sides of concrete beam as depicted in Fig. 10 (b). Therefore, it can be inferred that the steel yielding was followed by concrete crushing within the pure bending zone, similarly to what was observed by Dong et al. [26] in the experimental specimen.



(a)

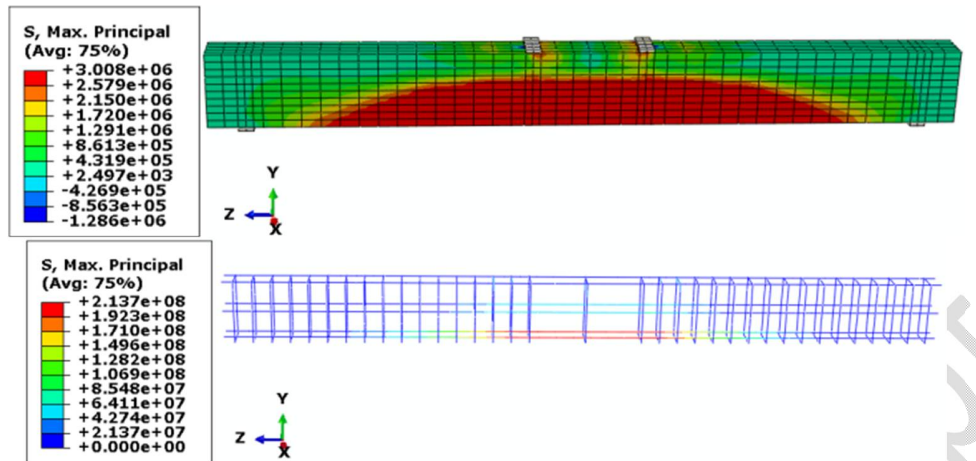


(b)

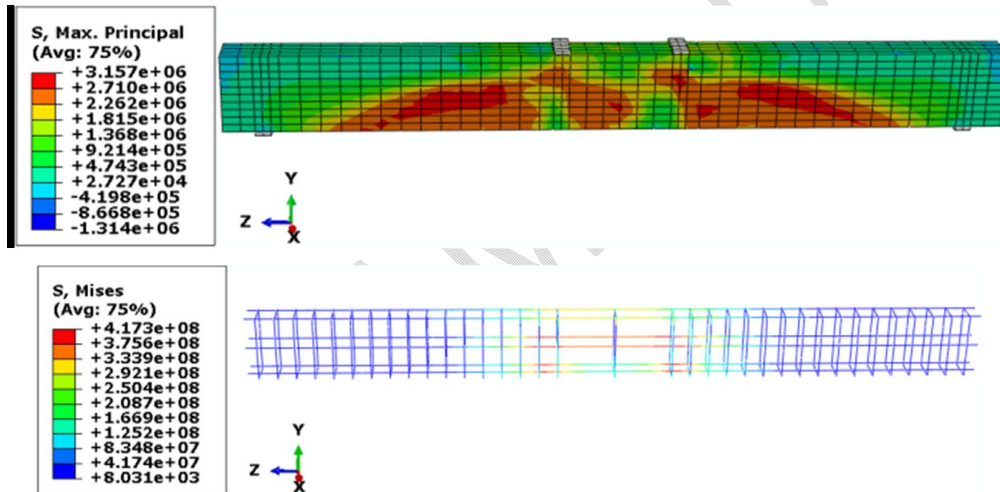
Fig. 10. Stress distribution in S-16 at nominal moment (a); and ultimate moment (b); the unit in the legends is MPa.

4.2. Failure mode and stress distribution of FRP reinforced concrete specimens

The tensile damage evolution in G12-N, G12-P, G12-W, G16-N, G16-P, C12-N, and C12-P models appeared within the pure bending zone as depicted in Fig. 8. In most cases, the maximum stress of reinforcement occurred in the GFRP and CFRP bars as shown in Figs. 11-13. Therefore, by considering the fact that concrete can be classified as a brittle material with low flexural strength [44-53], the concrete crushing was followed by the effective participation of GFRP bars in carrying the generated stress intensity, particularly in the pure bending zone. For instance, at the nominal moment, the maximum tensile stress in G12-N was depicted in the tension zone near to the mid-span, where the maximum tensile stress in GFRP bars was found to be 213.7 MPa as indicated in Fig. 11 (a). The maximum stress in GFRP bars increased up to 417.3 MPa at ultimate moment, about twice that at the nominal moment. Meanwhile, by increasing the load, the maximum principal stress in concrete component was dissipated to the sides of concrete beam as shown in Fig. 11 (b). Therefore, GFRP flexural bars effectively participated in the distribution of the highest stress intensity up to the ultimate load.



(a)



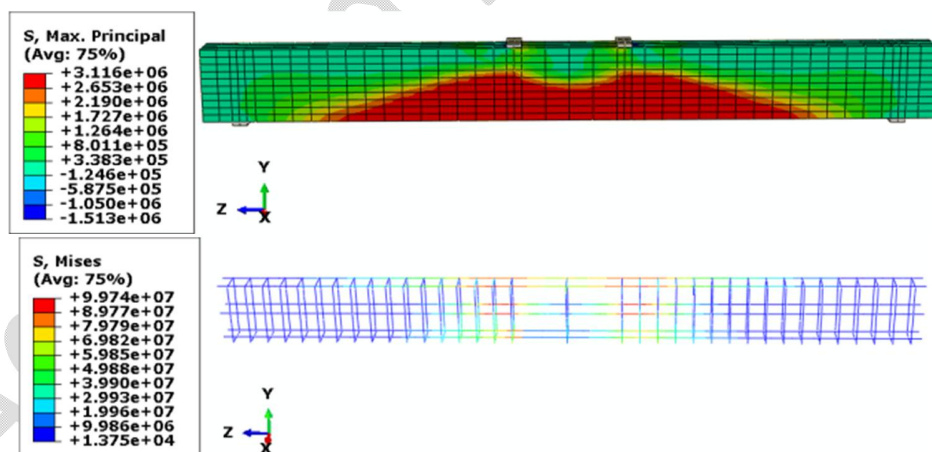
(b)

Fig. 11. Stress distribution in G12-N at nominal moment (a); and ultimate moment (b); the unit in the legends is MPa.

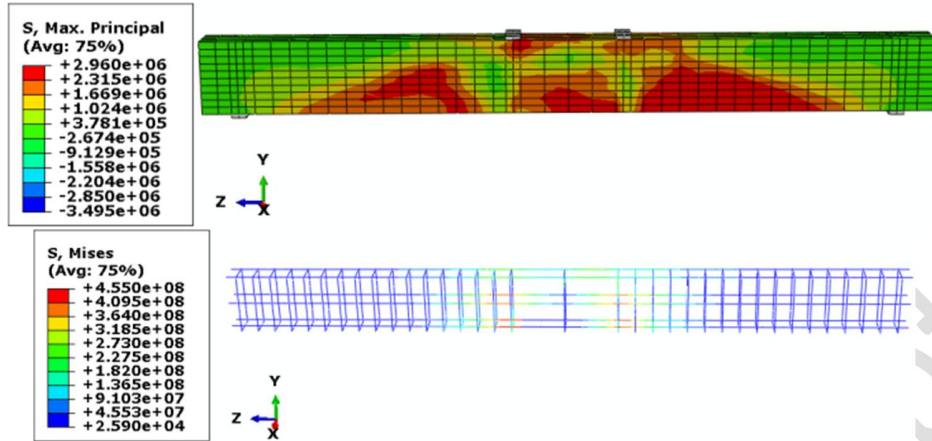
4.2.1. A comparison between the FRP composite bars in the pure bending region and along the whole beam length

There was no significant difference between the failure mode of concrete member strengthened with FRP bars grouted in the pure bending zone and along the whole beam length (G12-P and G12-W) as indicated in Fig. 8. However, a comparison between the stress

distributions in these two models showed that the FRP bars grouted along the whole beam length led to dissipating the maximum principal stress in concrete component more as shown in Figs. 12 and 13. In addition, the maximum tensile stress of GFRP bars in the G12-P model concentrated on the pure bending zone and it was equal to 455 MPa at ultimate moment, while the tensile stress of GFRP bars in the G12-W model was dissipated along the beam length and it was found to be 258.1 MPa. Therefore, a suitable bond quality appeared between the GFRP composite bars and high-strength grout in sleeves, leading to the reduction of crack widths at the tension zone of the reinforced concrete beam. Concerning this, a study by El-Nemr et al. [54] on the flexural performance of GFRP-reinforced concrete beams showed that an increase in the level of concrete strength resulted in increasing the bond quality between the GFRP bars and high-strength concrete and subsequently decreasing the mid-span deflection of GFRP-reinforced concrete beams. This manner led to the generation of smaller crack widths in the flexural zone of GFRP-reinforced concrete beams. Generally, it can be stated that the flexural performance of GFRP composite bars in contact with high-strength concrete materials such as high-strength grout can be considered as a viable solution to control the crack widths of GFRP-reinforced concrete beams, similarly to what was observed in the present study.

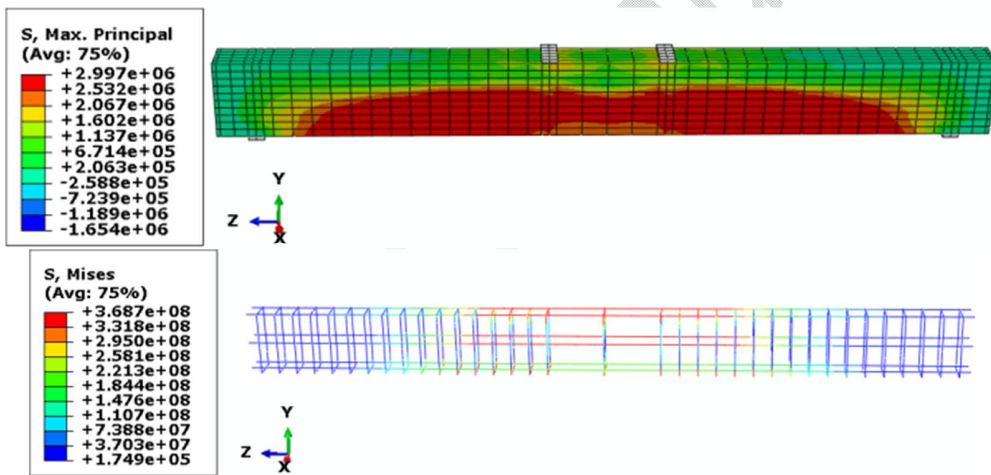


(a)

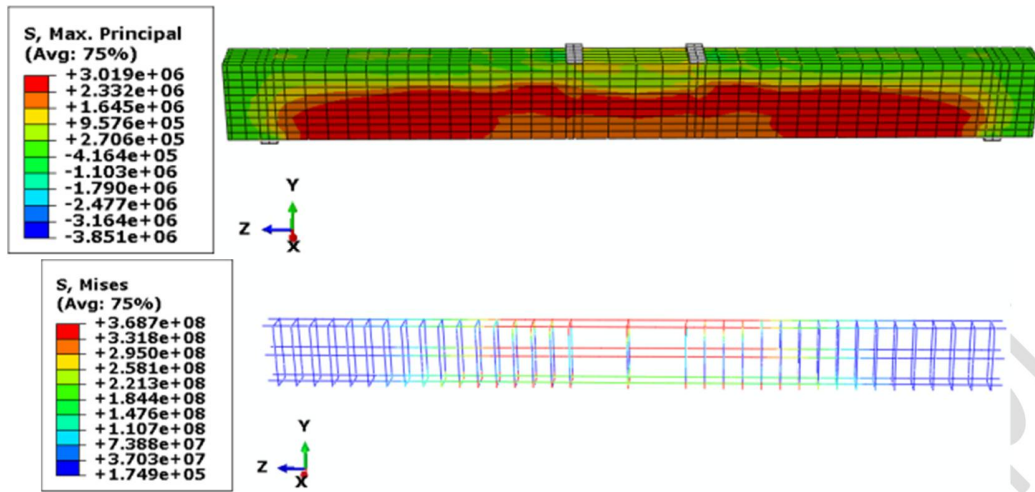


(b)

Fig. 12. Stress distribution in G12-P at nominal moment (a); and ultimate moment (b); the unit in the legends is MPa.



(a)



(b)

Fig. 13. Stress distribution in G12-W at nominal moment (a); and ultimate moment (b); the unit in the legends is MPa.

4.2.2. Effects of FRP bars' diameter on the stress distribution and failure mode of concrete components

According to the numerical outputs, by increasing the diameter of GFRP composite bars from 12 to 16 mm, no change was appeared in the failure mode of concrete models with the normal-strength, while the reverse occurred for the concrete components strengthened with the CFRP composite bars. For instance, the plots of tensile damage variable for the normal-strength concrete models strengthened with the GFRP composite bars showed that the tensile damages were generated within the pure bending zone, and then these damages continued to appear near to the compression zone as shown in Fig. 8. Similar results were reported by Khorasani et al. [13]. They showed that there was no significant change in the failure mode of concrete components with the normal-strength by increasing the amount of GFRP bars in the tension region. As seen in Fig. 8, the failure modes of concrete models strengthened with the 12-mm diameter CFRP bars was nearly the same as those strengthened with the GFRP composite bars. Similar results were also reported by Hacha and Gaafar [19] for the concrete beams reinforced with a 9-mm diameter CFRP bar. However, the compressive damage in the C16-N and C16-P models appeared in the compression zone of normal-strength concrete near to the mid-span (Fig.

9). Concerning this, Mustafa and Hassan [21] showed that the concrete components strengthened with the CFRP composite bars with the diameters of 16, 18, 20 and 22 mm were failed by concrete crushing rather than by rupture FRP reinforcement. According to the mechanical properties of CFRP bars presented in Table 1, the axial stiffness ($E_f A_f$) of 16-mm diameter CFRP bars was found to be 10.3 MN more than that of the 12-mm diameter CFRP bars. Therefore, an increase in the reinforcement ratio of the CFRP bars led to a reduction in the mid-span deflection and a subsequent generation of concrete crushing in the compression zone of normal-strength concrete without rupture of the CFRP bars. Similar results were also observed in the plots of stress distribution. As shown in Fig. 14, for the C12-P model, the maximum principal stress occurred in the tension zone, where the tensile stress of 12-mm diameter CFRP bars was found to be high (851.1 MPa) at ultimate moment. However, for the C16-P model, the approximate location of the maximum principal stress appeared in the compression zone of normal-strength concrete near to the mid-span, while low tensile stress was obtained for the 16-mm diameter CFRP bars (237 MPa) at the ultimate moment as shown in Fig. 15. Therefore, the CFRP flexural bars with a diameter of 16 mm slightly participated in carrying some of the generated stress intensity.

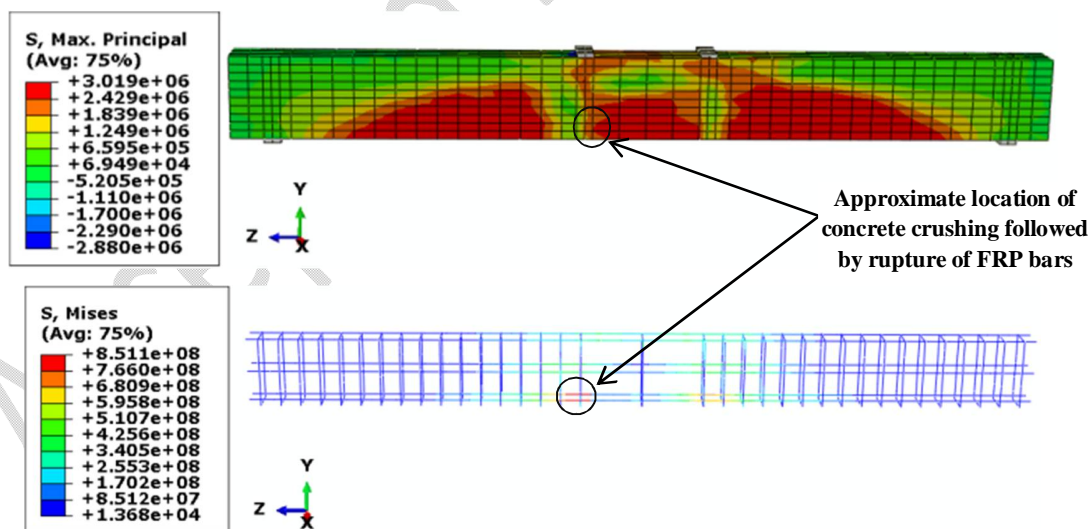


Fig. 14. Stress distribution in the C12-P at ultimate moment; the unit in the legends is MPa.

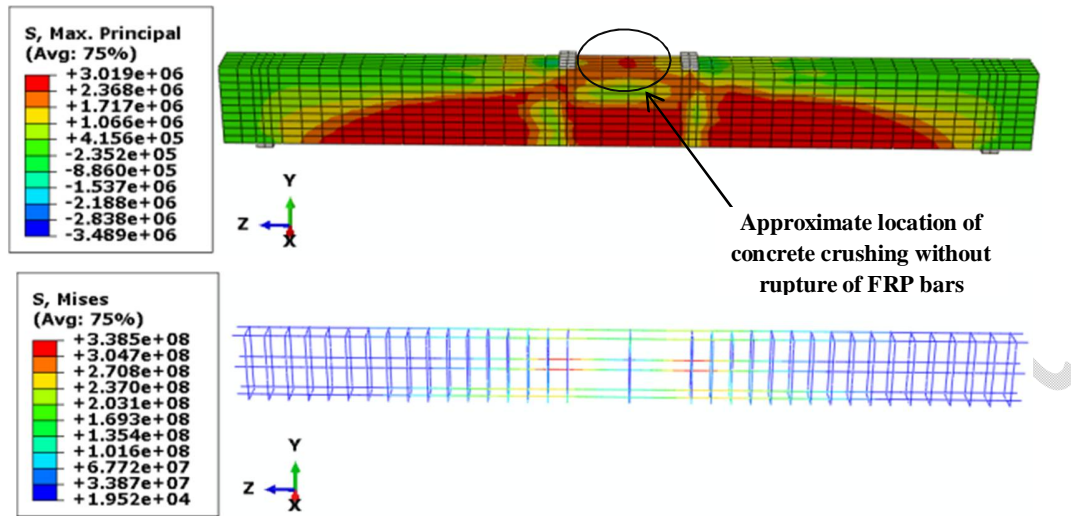


Fig. 15. Stress distribution in the C16-P at ultimate moment; the unit in the legends is MPa.

4.3. A comparison between the FRP reinforced normal- and high-strength concrete beams

The results of GFRP strengthened normal-strength concrete components were numerically compared with those of the GFRP strengthened high-strength concrete components. Fig. 16 indicates the ultimate moment of GFRP strengthened high-strength concrete beams was on average about 26.1% more than that of the GFRP strengthened normal-strength concrete specimens. The corresponding difference for the mid-span deflection was 14.2%. Therefore, it can be stated that by increasing the concrete strength, the load-bearing capacity and mid-span deflection increased, similarly to what was reported by El-Nemr et al. [54]. Another study by Khorasani and Esfahani [14] on the behaviour of normal- and high-strength concrete beams strengthened with GFRP bars showed that the ultimate load of GFRP reinforced high-strength concrete beams was about 27.9-38.4% more than that of the GFRP reinforced normal-strength concrete beams. The corresponding difference for the mid-span deflection was in the range of 12.3-28.8%. Therefore, the results of this study were nearly within the range of the results given by Khorasani and Esfahani [14].

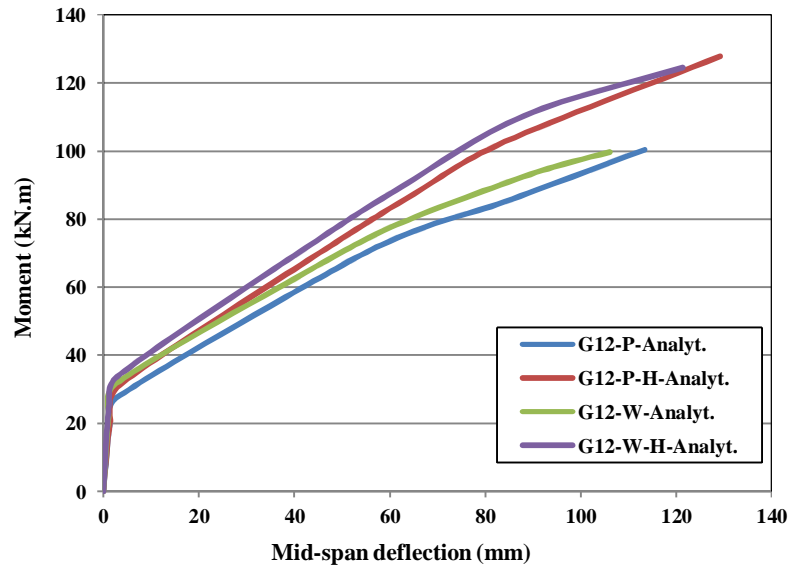
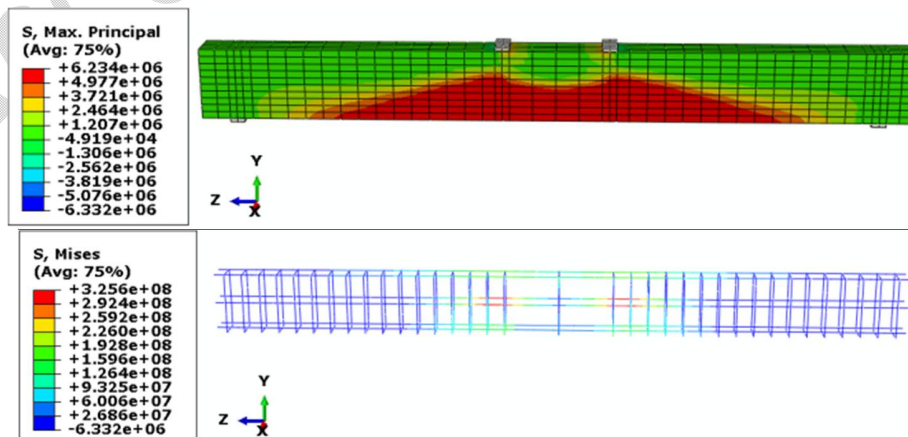
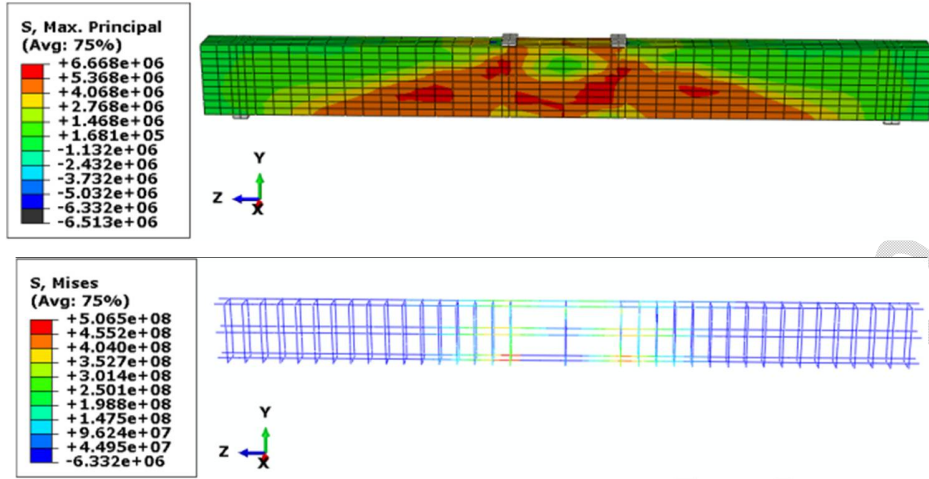


Fig. 16. Load against mid-span deflection of normal- and high-strength concrete models.

Figs. 17 and 18 show that the maximum tensile stress in the concrete component was in the range of 6-6.6 MPa. This stress appeared near the tension zone of high-strength concrete beams (Figs. 17 and 18), and the general trend of stress distribution was nearly the same observed in the normal-strength concrete beams (Figs. 12 and 13). In addition, it seems that the GFRP bars grouted in the pure bending zone and along the whole beam length dissipated the maximum principal stress in the high-strength concrete beams at nominal and ultimate moments (Figs. 17 and 18), but not as much as that in the normal-strength concrete beams (Figs. 12 and 13).

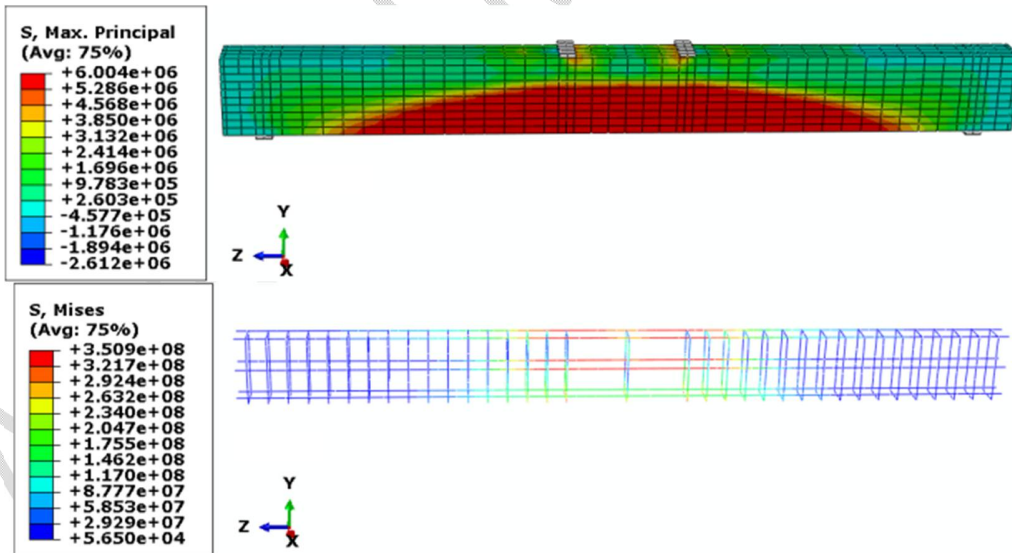


(a)

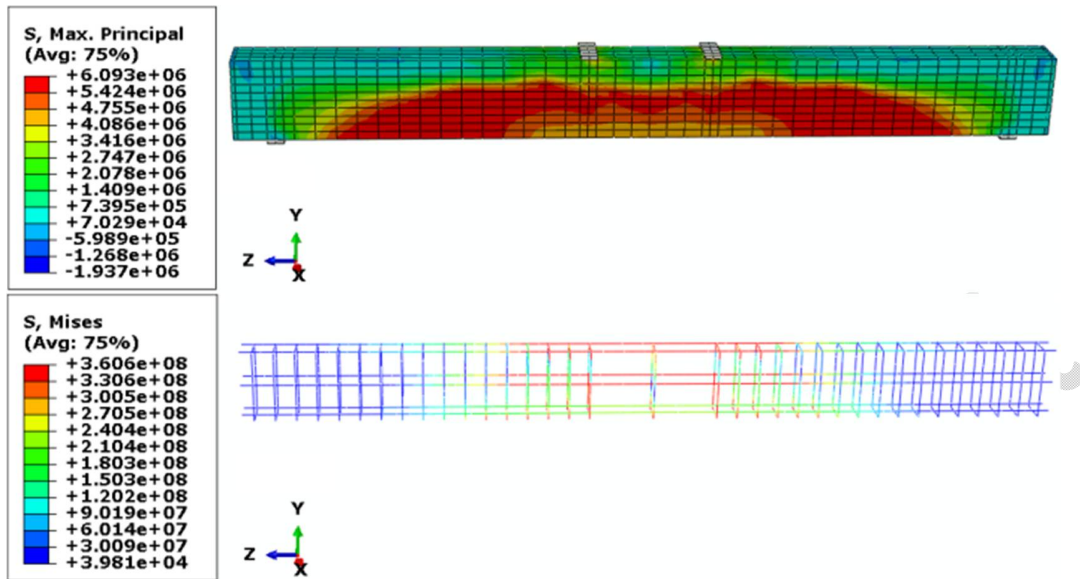


(b)

Fig. 17. Stress distribution in the G12-P-H at nominal moment (a); and ultimate moment (b); the unit in the legends is MPa.



(a)



(b)

Fig. 18. Stress distribution in the G-12W-H at nominal moment (a); and ultimate moment (b); the unit in the legends is MPa.

4.4. Stress distribution in the grout component

The evolution of tensile damage in the grout within the pure bending zone at ultimate moment is shown in Fig. 19. The approximate location of generated cracks in the grout was near to the mid-span. In addition, the maximum tensile stress in the grout was found to be 5.95 MPa and 6.56 MPa at nominal and ultimate moments as shown in Fig. 20. This stress was first generated in the mid-span of grout at nominal moment, and then it was propagated along the whole grout length by increasing the load. Therefore, it can be stated that the grout component effectively participated in carrying the nominal and ultimate moments and transferring the maximum tensile stress to the FRP bars.

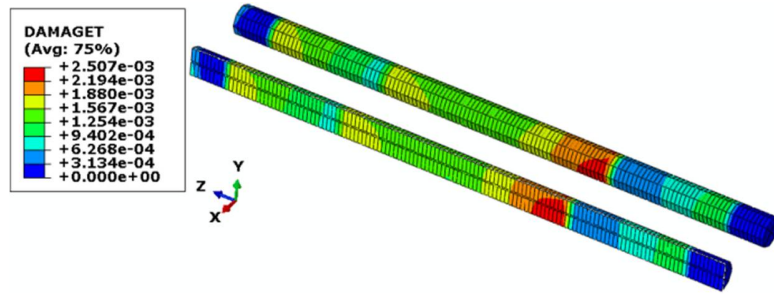
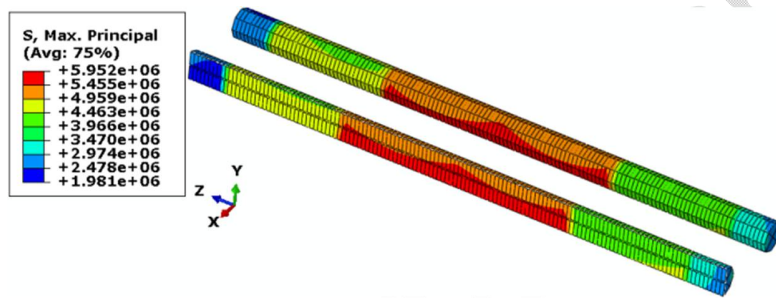
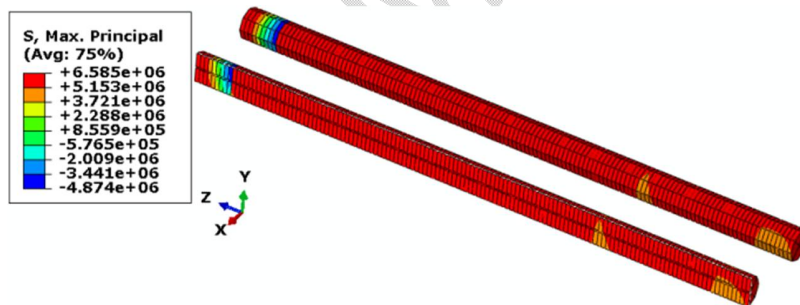


Fig. 19. Evolution of the tensile damage in the grout within the pure bending zone at ultimate moment; the unit in the legend is MPa.



(a)



(b)

Fig. 20. Stress distribution in the grout within the pure bending zone at nominal moment (a); and ultimate moment (b); the unit in the legends is MPa.

Fig. 21 shows the evolution of tensile damage in the grout, developed along the whole beam length at ultimate moment. The results showed that the tensile damage increased by approaching the mid-span of the grout, while this damage disappeared at the two ends of the grout as expected. According to Fig. 22, the maximum principal stress at nominal and ultimate moments was equal to 5.67 MPa and 6.6 MPa, respectively. This stress was propagated near to the two ends of the grout by increasing the moment from nominal to ultimate.

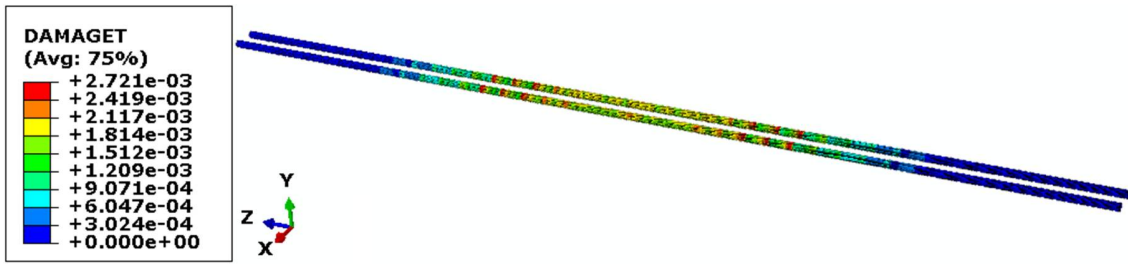
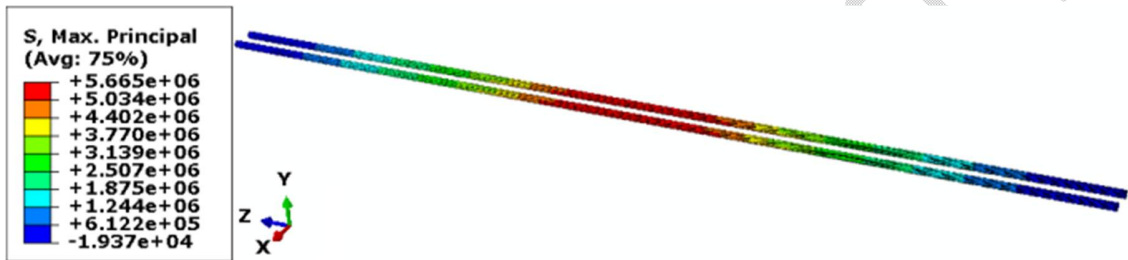


Fig. 21. Evolution of the tensile damage in the grout developed along the whole beam length at ultimate moment; the unit in the legend is MPa.



(a)



(b)

Fig. 22. Stress distribution in grout in the grout developed along the whole beam length at nominal moment (a); and ultimate moment (b); the unit in the legends is MPa.

According to the results, the maximum principal stress of grout within the pure bending region was found to be nearly the same as that of the grout, developed along the whole beam length. However, at ultimate moment, the maximum principal stress was constantly dissipated in the grout, created within the pure bending zone (Fig. 20 (b)), while there was no stress at the two ends of the grout, developed along the whole beam length and this stress increased by approaching the mid-span as shown in Fig. 22 (b).

5. Conclusions

The present study was performed to numerically assess the non-linear behaviour of the concrete component strengthened with grouted CFRP and GFRP composite bars. According to the numerical results, the following conclusions can be drawn:

- The contour plots of damage variable showed that there was good compatibility between the results of FRP reinforced concrete models and experimental specimens. Meanwhile, the approximate paths of damage in FRP concrete beams were approximately observed in the numerical models. The failure modes of C16-N and C16-P models revealed that the compressive damage was propagated near to the mid-span in the compression zone, while for other models, the tensile damage appeared in the tension zone.
- In the S16 model, by increasing the moment from nominal to ultimate, the maximum tensile stress of steel rebar increased from 319.9 MPa to 508.2 MPa, leading to the dissipation of maximum principal stress from the mid-span to the sides of the concrete beam.
- In the G12-N model, the maximum stress in the GFRP flexural bars was obtained 417.3 MPa at ultimate load, about twice that at the nominal moment. Therefore, it can be stated that the GFRP flexural bars effectively participated in the distribution of highest stress intensity, thereby the concrete crushing being followed by the effective participation of GFRP bars in carrying the generated stress intensity, particularly in the pure bending zone.
- The maximum tensile stress of GFRP bars in the G12-P model concentrated on the pure bending zone at ultimate moment, while the tensile stress of GFRP bars in the G12-W model was dissipated along the beam length, leading to a decrease of crack widths at the tension zone of reinforced concrete specimen.
- According to the numerical results, the GFRP bars either with the diameter of 12mm or 16mm effectively participated in carrying the ultimate moment and there was no significant difference among the failure modes of concrete specimens strengthened with different diameters of GFRP bars. However, a comparison between C12-P and C16-P models made with the normal-strength concrete showed that, at ultimate load, the tensile stress of 12-mm diameter CFRP bars was 851.1 MPa, about 3.5 times more than that of

the 16-mm diameter CFRP bars. Therefore, the failure modes of C12-P and C16-P models were different, and it seems that the 12-mm diameter CFRP flexural bars effectively participated with the normal-strength concrete in carrying the ultimate moment, while the 16-mm diameter CFRP flexural bars, embedded in the normal-strength concrete, moderately participated with the normal-strength concrete beam in which the concrete crushed by reaching the ultimate compressive strain of concrete in the compression zone without the rupture of the 16-mm diameter CFRP bars in the pure bending zone.

- The ultimate moment and mid-span deflection of high-strength concrete models strengthened with the GFRP bars were respectively on average about 26.1% and 14.2% more than those of the normal-strength concrete models strengthened with GFRP bars.
- The GFRP bars, surrounded by the grout, propagated the maximum principal stress in the high-strength concrete models at nominal and ultimate moments, but not as much as that in the normal-strength concrete beams.
- The approximate locations of tensile damage in the grouts, created either within the pure bending zone or along the whole beam length, were appeared to be near to the mid-span. Meanwhile, there was no significant difference between the maximum principal stress of these two types of grouts, and it was in the range of 5.67-6.56 MPa.
- The distribution of maximum principal stress in the grout embedded in the pure bending region of the concrete component was found to be nearly constant, and it completely participated in carrying the ultimate load and transferring the maximum tensile stress to the FRP composite bars. However, there was no stress at the two ends of the grout, developed along the whole beam length and this stress increased by approaching the mid-span.

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