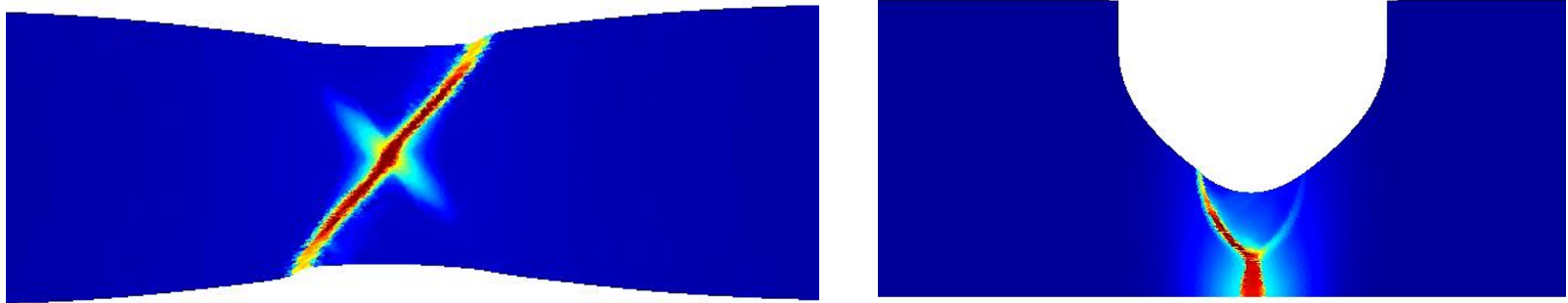

A multi-mechanism non-local porosity model for highly-ductile materials; application to high entropy alloys



Van Dung Nguyen⁽¹⁾, Philippe Harik⁽¹⁾, Antoine Hilhorst⁽²⁾, Pascal Jacques⁽²⁾, Thomas Pardoen⁽²⁾, Ludovic Noels⁽¹⁾

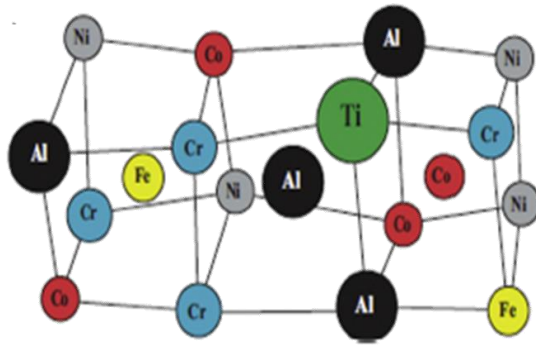
¹University of Liège, Belgium, ²University of Louvain, Belgium

The research has been funded by the Walloon Region under the agreement no. 1610154-EntroTough in the context of the 2016 WallInnov call.



Introduction

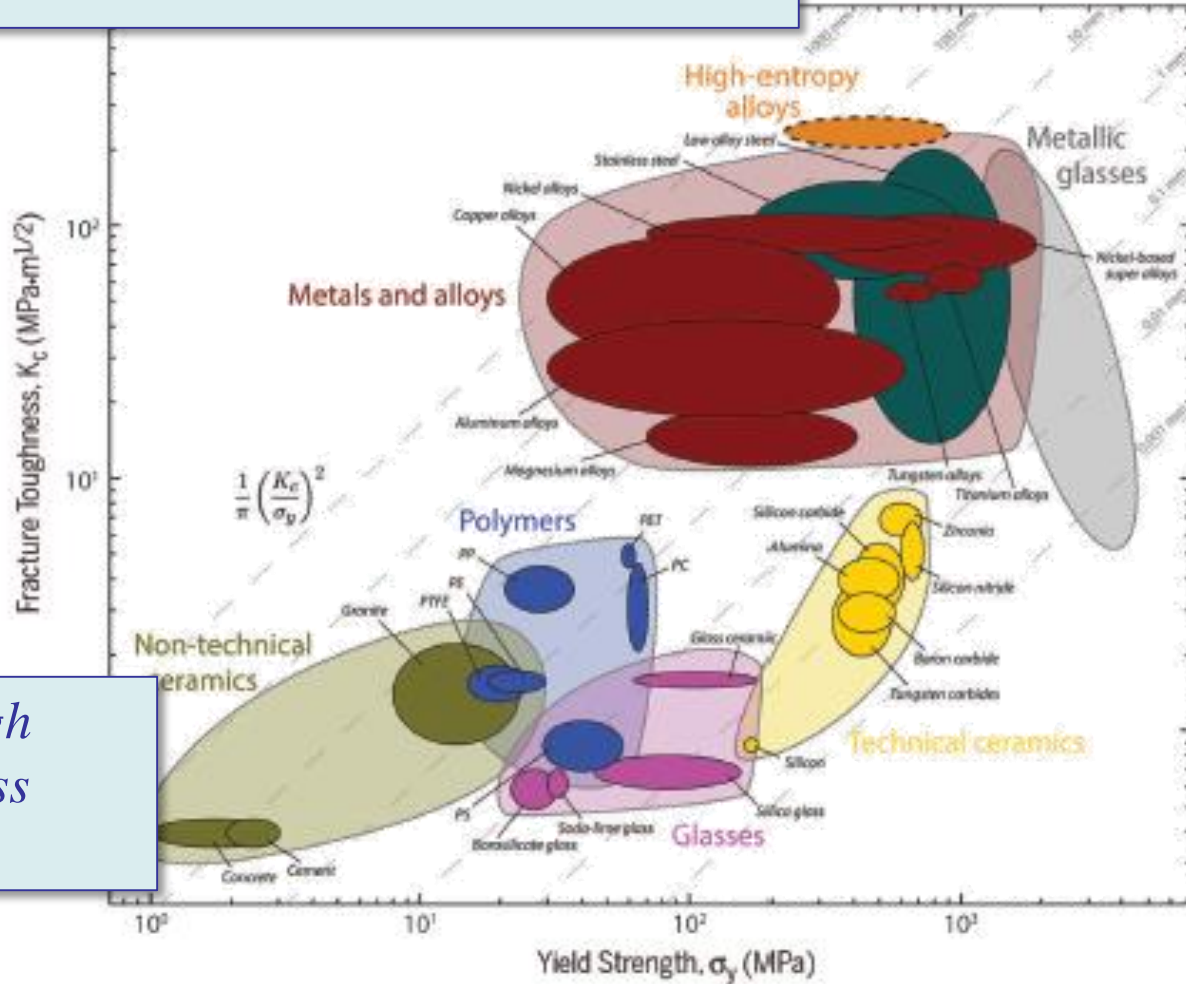
- High Entropy Alloy



Distorted lattice of several elements in equivalent proportions

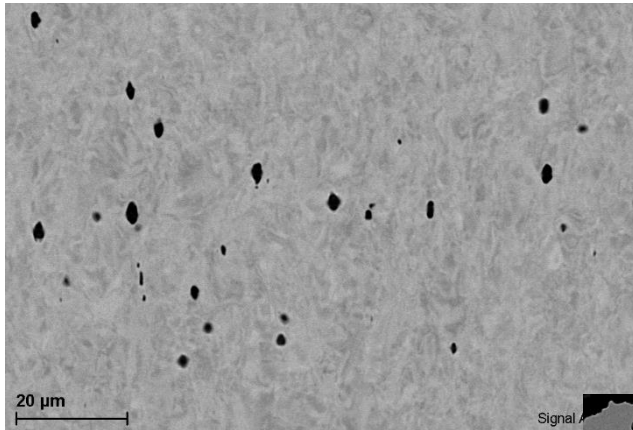
Zhang et al. 2014

Unexpectedly high fracture toughness

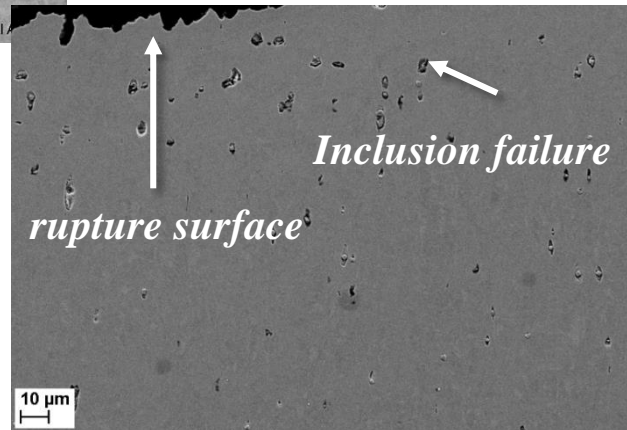


Introduction

- HEAs follow a ductile failure mechanism



*Porosity free
Initial inclusions*



*Nucleation from
inclusion failure*



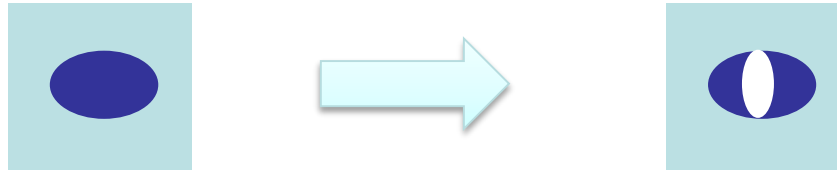
Tests performed at UCL by Antoine Hilhorst



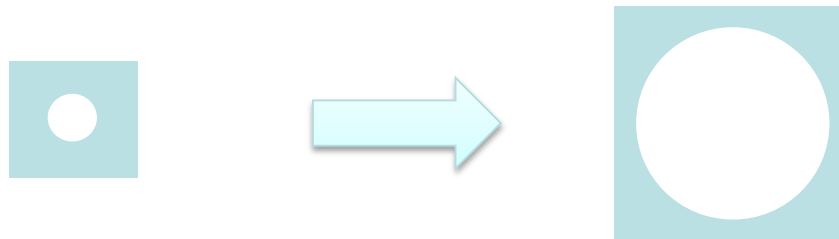
Introduction

- Ductile failure: failure mechanism

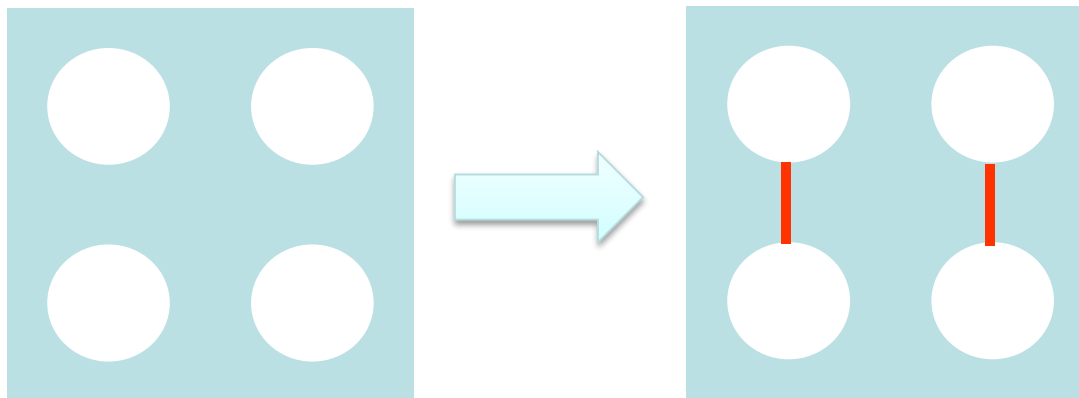
- Void nucleation (dislocation motion, particle/matrix decohesion, particle cracking, ...)



- Void growth of existing voids (because of plastic incompressibility)



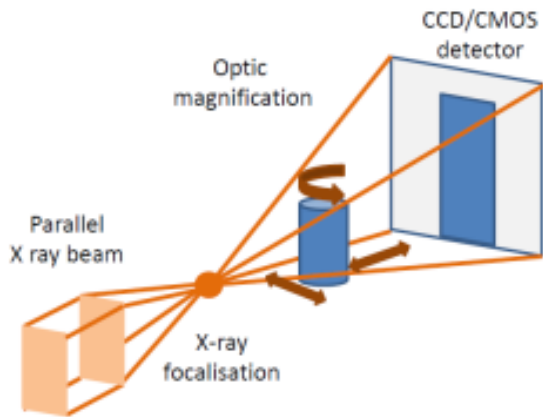
- Void coalescence (crack growth by shrinking of ligaments between voids)



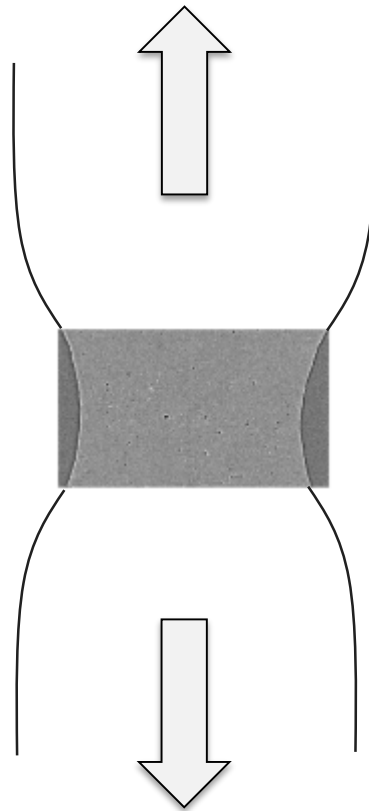
Introduction

- Ductile failure: complex coalescence scenarios
 - What does happen inside a « ductile » material under large strain ?

*X-ray tomography of in-situ tensile tests
= scanner for materials*



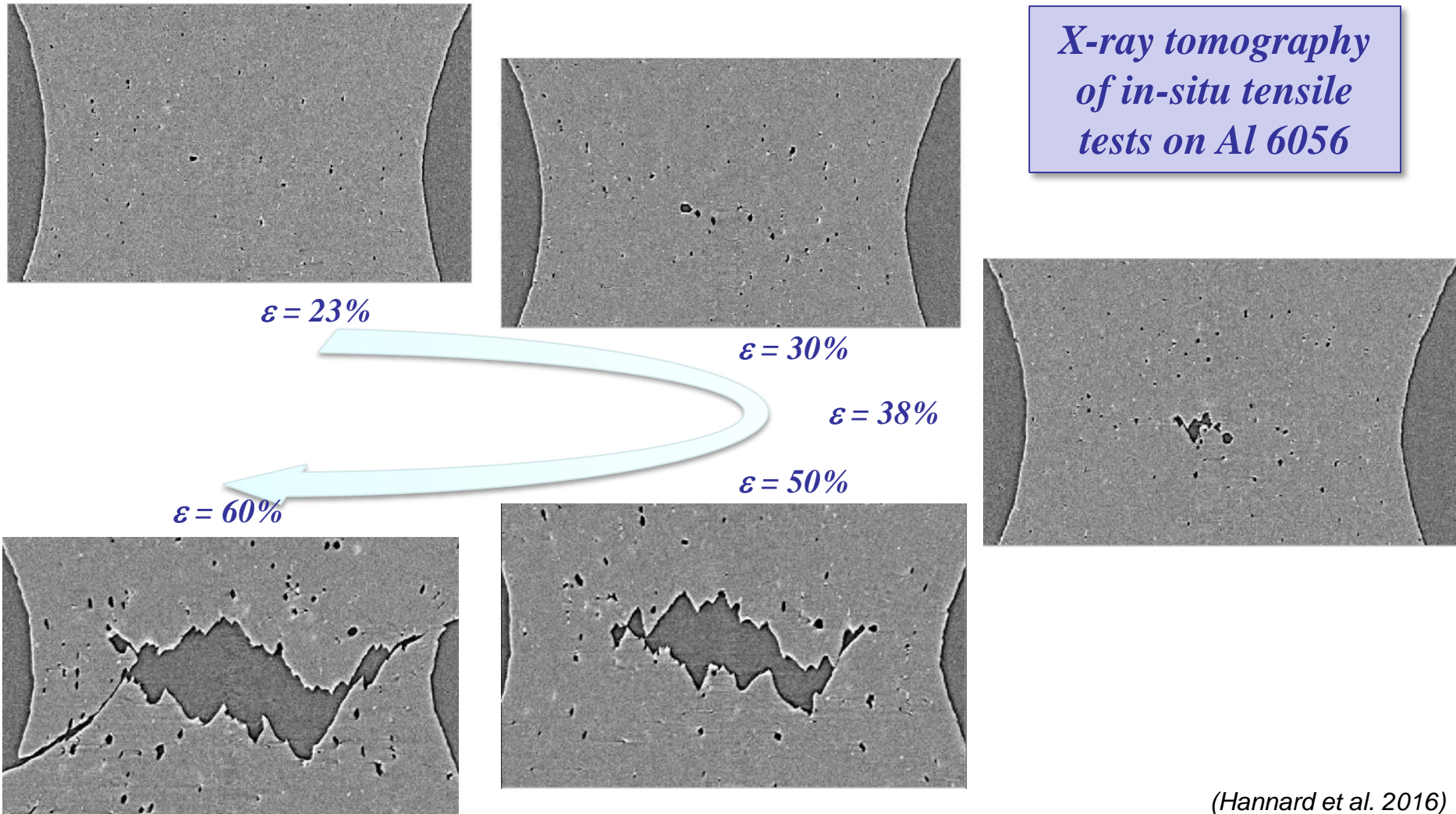
Tests performed at the ESRF synchrotron in Grenoble by F. Hannard (Ph. D. UCL) collaboration with Dr. E. maire INSA Lyon



(Hannard et al. 2016)

Introduction

- Ductile failure: complex coalescence scenarios
 - What does happen inside a « ductile » material under large strain ?

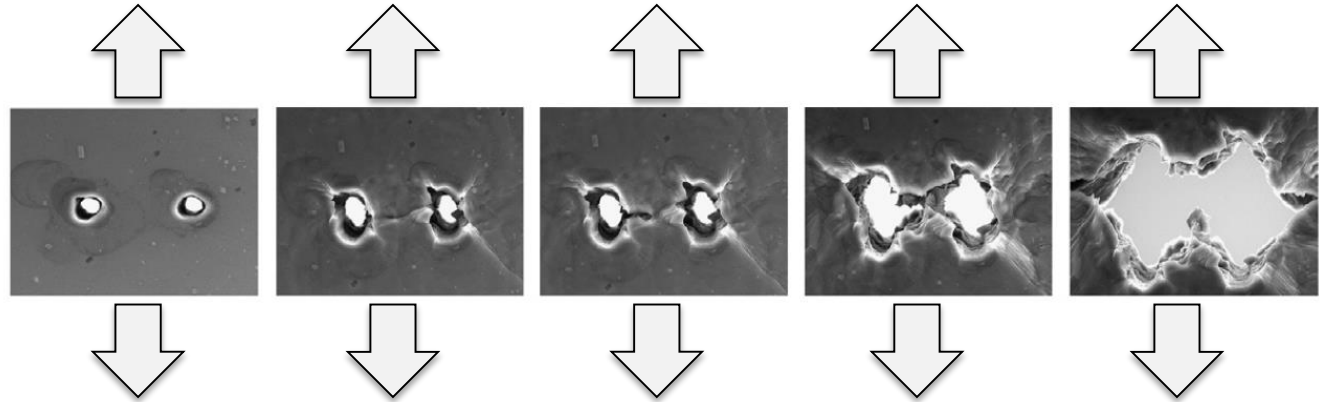


(Hannard et al. 2016)

Introduction

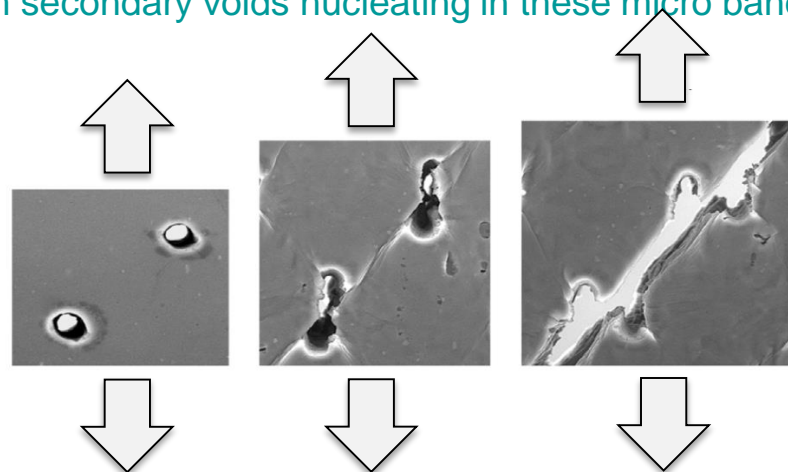
- Ductile failure: complex coalescence scenarios
 - Localization band perpendicular to the main loading direction
 - Shrinking of ligaments between voids

Internal necking coalescence



- Micro shear bands inclined to the main loading direction
 - Joining primary voids
 - Possibly with secondary voids nucleating in these micro bands

Shear driven coalescence



(Weck & Wilkinson 2008)

Introduction

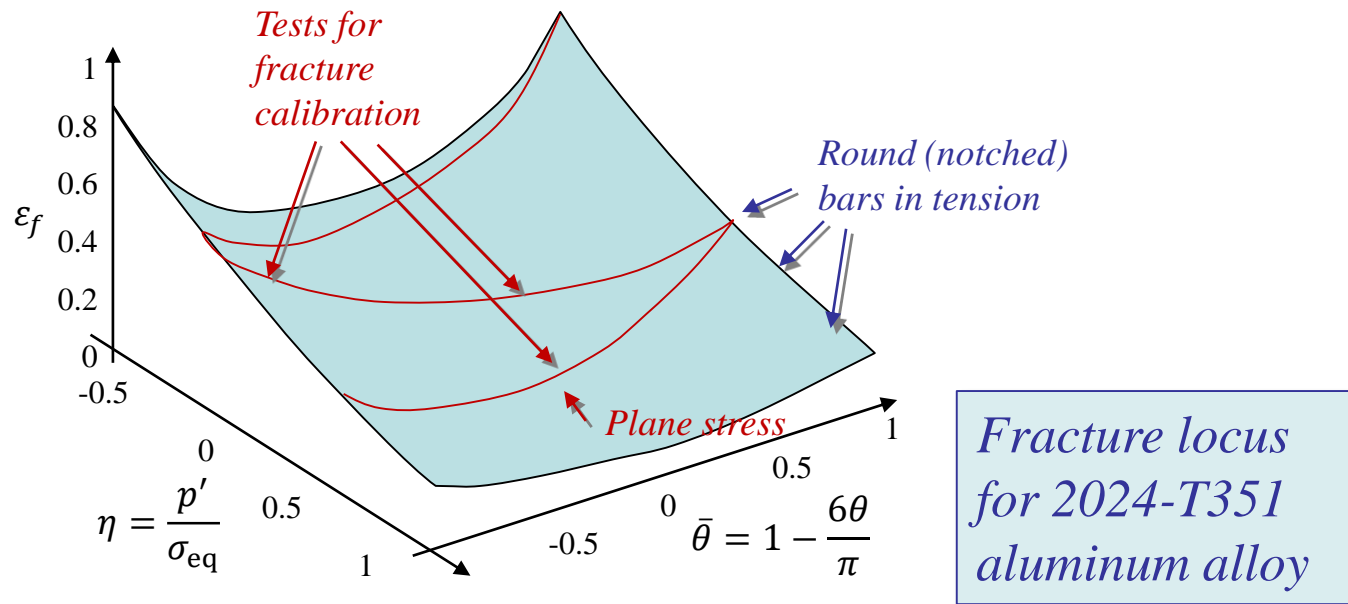
- Ductile failure: stress-state dependent fracture strain

- Stress triaxiality dependent

$$\eta = \frac{p'}{\sigma_{\text{eq}}} \in [-\infty \infty] \quad p' = \frac{\text{tr}(\boldsymbol{\sigma})}{3} \quad \sigma_{\text{eq}} = \sqrt{\frac{3}{2} \text{dev}(\boldsymbol{\sigma}) : \text{dev}(\boldsymbol{\sigma})}$$

- Lode dependent

$$\theta = \frac{1}{3} \arccos\left(\frac{27J_3}{2\sigma_{\text{eq}}^3}\right) \quad J_3 = \det(\text{dev}(\boldsymbol{\sigma}))$$



(Bai & Wierzbicki 2010)

• Objective & Methodology

– Develop a multi-surface model incorporating

- Void growth phase
- Internal necking coalescence phase
 - Driven by maximum principal stress
- Shear driven coalescence phase
 - Driven by maximum shear stress

The maximum principal stress & maximum shear stress are Lode-dependent!

– In a nonlocal formalism

• Why?

– Local forms suffer from mesh-dependency

• Implicit formulation

(Peerlings et al. 1998)

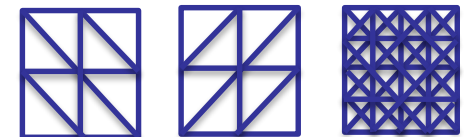
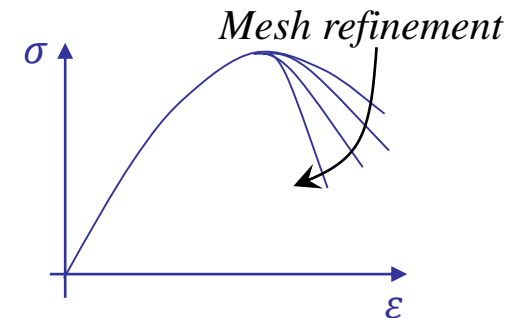
- Introduction of a characteristic length l_c
- New non-local degrees of freedom \bar{Z}_k
- New Helmholtz-type equation to be solved

$$\bar{Z}_k - Z_k - l_{ck}^2 \Delta_0 \bar{Z}_k = 0, \text{ with } k = 1, \dots, N$$

– Damage indicators depend on the nonlocal variable

• Multiple nonlocal variables can be considered

– Damage indicators depend on N different sources



The numerical results change without convergence

Multi-surface nonlocal porous model

- Porous plasticity corotational approach

- Yield condition

$$\Phi_{nl} = \Phi_{nl}(\boldsymbol{\sigma}; \sigma_Y, \mathbf{Y}) = 0$$

- Plastic flow

$$\mathbf{D}^P = \dot{\mathbf{F}}^P \cdot \mathbf{F}^{P-1} = \dot{\mu} \frac{\partial \Phi_{nl}}{\partial \boldsymbol{\sigma}}$$

- Evolution laws

- Equivalent matrix plastic strain rate:

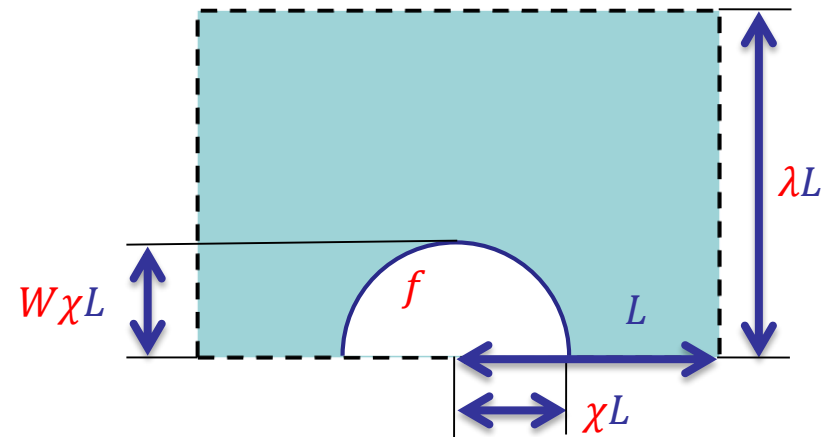
$$\dot{\varepsilon}_m = \frac{\boldsymbol{\sigma} : \mathbf{D}^P}{(1-f)\sigma_Y}$$

- Isotropic hardening law:

$$\sigma_Y = \sigma_Y^0 + R(\varepsilon_m)$$

- Evolution laws for void characteristics

$$\mathbf{Y} = [f \quad \chi \quad W \quad \lambda]^T$$



Void characteristics \mathbf{Y} :

Porosity : f

Void ligament ratio: χ

Void aspect ratio: W

Void spacing ratio: λ

Yield surface Φ_{nl} and evolution laws for \mathbf{Y} depend on the void expansion solution:

- *Void growth;*
- *Internal necking coalescence; or*
- *Shear driven coalescence*



- Void growth phase – GTN model

- Yield condition

$$\left\{ \begin{array}{l} \Phi_{nl} = \Phi_G = \frac{\hat{\sigma}_G}{\sigma_Y} - 1 = 0 \\ \hat{\sigma}_G(\sigma_{eq}, p', \sigma_Y, f) = \frac{\sqrt{\sigma_{eq}^2 + 2\sigma_Y^2 f q_1 \left[\cosh\left(\frac{3}{2} q_2 \frac{p'}{\sigma_Y}\right) - 1 \right]}}{1 - q_1 f} \end{array} \right.$$

$$p' = \frac{\text{tr}(\boldsymbol{\sigma})}{3}$$

$$\sigma_{eq} = \sqrt{\frac{3}{2} \text{dev}(\boldsymbol{\sigma}) : \text{dev}(\boldsymbol{\sigma})}$$

- Parameters:

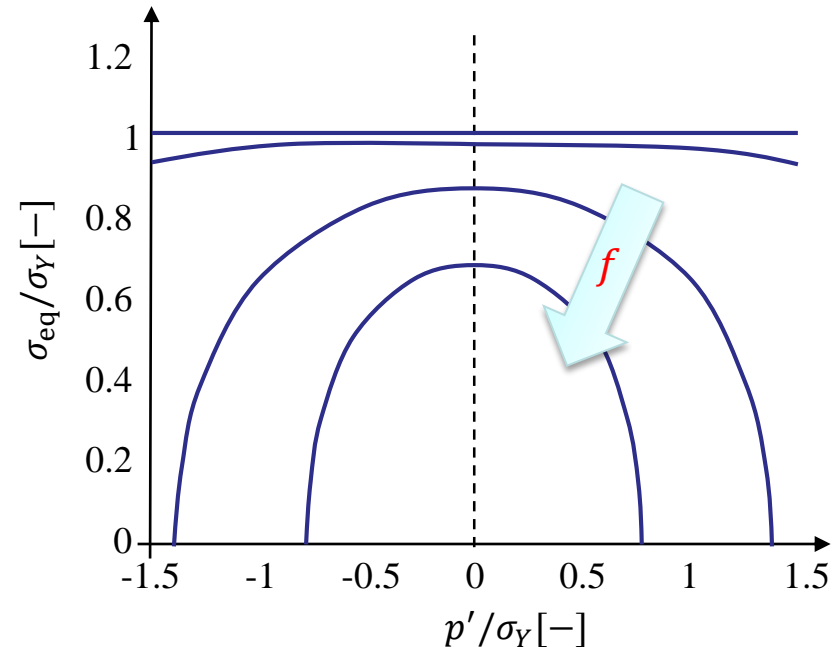
- q_1 and q_2

- Hardening law

- $\sigma_Y(\varepsilon_m)$
- Matrix plastic deformation ε_m

- Nonlocal evolution laws for void characteristics

$$\mathbf{Y}_{nl} = \mathbf{Y}_G(\varepsilon_m, \varepsilon_v, \varepsilon_d, \bar{\varepsilon}_m, \bar{\varepsilon}_v, \bar{\varepsilon}_d, \boldsymbol{\sigma})$$



Multi-surface nonlocal porous model

- Void growth phase - $\mathbf{Y}_{nl} = \mathbf{Y}_G(\varepsilon_m, \varepsilon_v, \varepsilon_d, \bar{\varepsilon}_m, \bar{\varepsilon}_v, \bar{\varepsilon}_d, \boldsymbol{\sigma})$

- Nonlocal porosity evolution

$$\dot{f} = \dot{f}_{gr} + \dot{f}_{nu} + \dot{f}_{sh}$$

- Growth part

$$\dot{f}_{gr} = (1 - f) \operatorname{tr}(\mathbf{D}^P) \Rightarrow \dot{f}_{gr} = (1 - f) \dot{\varepsilon}_v$$

- Nucleation part

$$\dot{f}_{nu} = A_n(\varepsilon_m) \dot{\varepsilon}_m \Rightarrow \dot{f}_{nu} = A_n(\bar{\varepsilon}_m) \dot{\varepsilon}_m$$

- Shear part

$$\dot{f}_{sh} = k_w \phi_\eta \phi_\omega f \frac{\operatorname{dev}(\boldsymbol{\sigma}) : \mathbf{D}^P}{\sigma_{eq}} \Rightarrow \dot{f}_{sh} = k_w \phi_\eta \phi_\omega f \dot{\varepsilon}_d$$

(Nahshon and Hutchinson 2008)

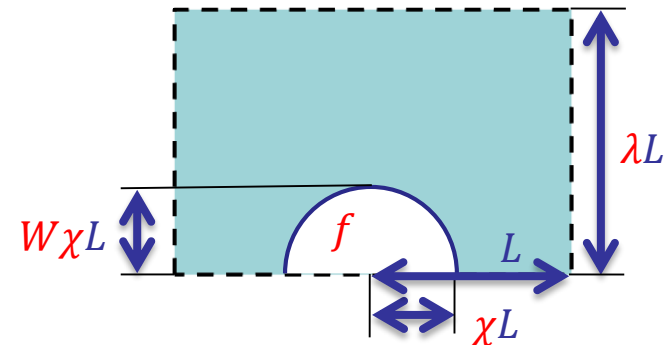
- Parameter: η_s, k_w

$$\phi_\eta = \exp\left(-\frac{1}{2} \left(\frac{\eta}{\eta_s}\right)^2\right) \quad \& \quad \phi_\omega = 1 - \omega^2$$

- Voids shape evolution

$$\left\{ \begin{array}{l} \dot{\lambda} = \kappa \lambda \dot{\varepsilon}_d \\ \chi = \left(\frac{3f\lambda}{2W}\right)^{\frac{1}{3}} \\ \dot{W} = 0 \end{array} \right.$$

Periodic distribution $\kappa = 1.5$,
 Random distribution $\kappa = 0$,
 Clustered distribution $0 < \kappa < 1.5$
 (Benzerga et al. 2016)



Multi-surface nonlocal porous model

• Internal necking – Coalescence

– Thomason coalescence onset

- Localized plastic flow in ligament (Thomason 1985)
- Limit load factor for uniaxial tension

$$C_{Tf}(\mathbf{Y}) = \frac{\sigma_{zz}}{\sigma_Y} = (1 - \chi^2) \left[h \left(\frac{1 - \chi}{W\chi} \right)^2 + g \sqrt{\frac{1}{\chi}} \right]$$

• Parameters:

– $g = 0.1$, $h = 1.24$ are generally adopted

– New yield surface accounting for general loading

- Driven by maximum principal stress (MPS)

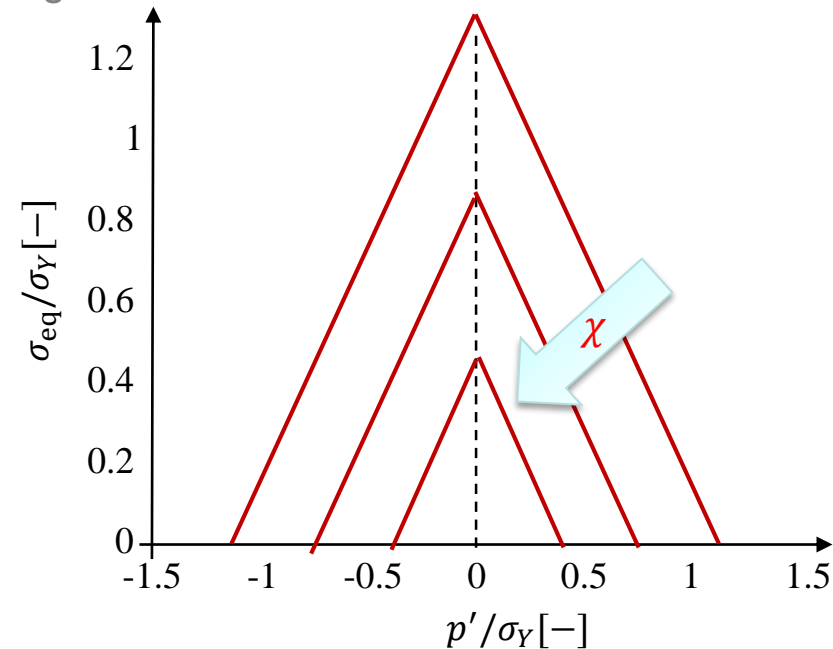
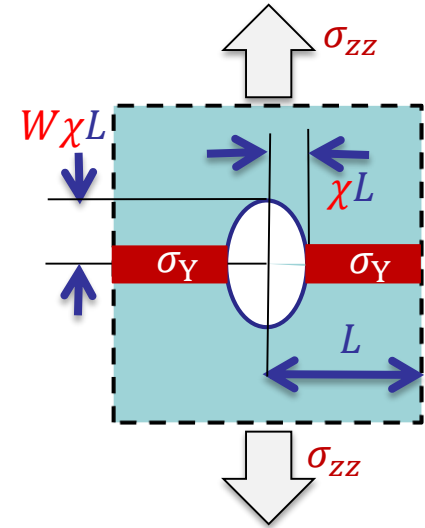
$$\left\{ \begin{array}{l} \Phi_{nl} = \Phi_T = \frac{\hat{\sigma}_T}{\sigma_Y} - 1 = 0 \\ \hat{\sigma}_T = \frac{1}{C_{Tf}} \left(\frac{2}{3} \sigma_{eq} \cos \theta + |p'| \right) \end{array} \right.$$

MPS

$$\theta(\sigma_{eq}, J_3) = \frac{1}{3} \arccos \frac{27J_3}{2\sigma_{eq}^3} \quad p' = \frac{\text{tr}(\boldsymbol{\sigma})}{3}$$

– Evolution laws for void characteristics

$$\mathbf{Y}_{nl} = \mathbf{Y}_T(\varepsilon_m, \varepsilon_v, \varepsilon_d, \bar{\varepsilon}_m, \bar{\varepsilon}_v, \bar{\varepsilon}_d, \boldsymbol{\sigma})$$



Multi-surface nonlocal porous model

- Shear driven – Coalescence

- Thomason-like coalescence onset

- Limit load factor

$$C_{Sf}(\mathbf{Y}) = \frac{\sqrt{3}\tau}{\sigma_Y} = \xi (1 - \chi^2)$$

- Parameter ξ

- $\xi = 1$ for σ_Y uniform inside localization band
- $\xi > 1$ is used for real distribution

- New yield surface

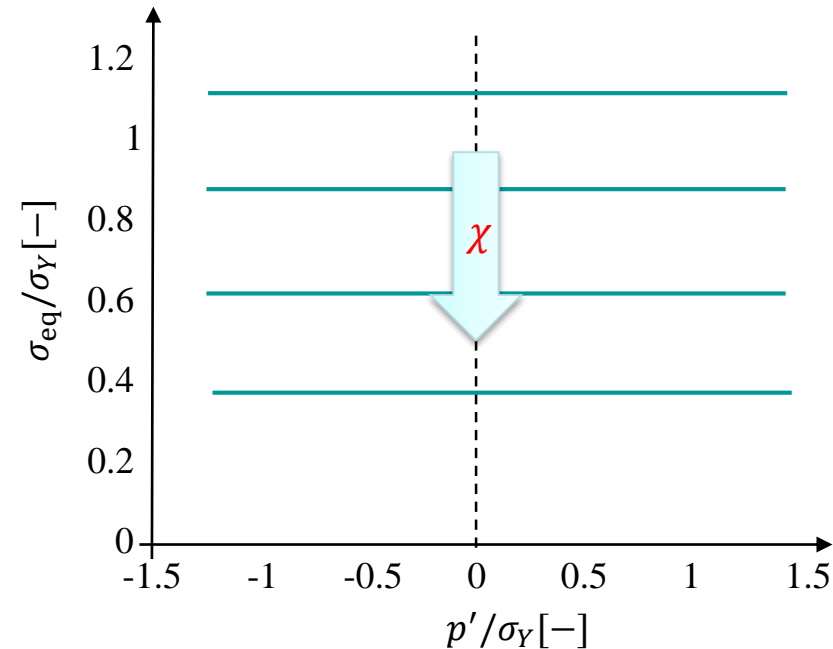
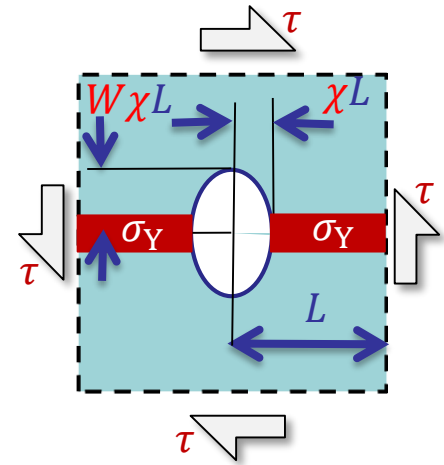
- Driven by maximum shear stress (MSS)

$$\left\{ \begin{array}{l} \Phi_{nl} = \Phi_S = \frac{\hat{\sigma}_S}{\sigma_Y} - 1 = 0 \\ \hat{\sigma}_S = \frac{\sqrt{3}\tau}{C_{Sf}} = \frac{\sigma_{eq}}{C_{Sf}} \left(\frac{\sin \theta}{2} + \frac{\sqrt{3} \cos \theta}{2} \right) \end{array} \right. \quad \text{MSS}$$

$$\theta(\sigma_{eq}, J_3) = \frac{1}{3} \arccos \frac{27J_3}{2\sigma_{eq}^3}$$

- Evolution laws for void characteristics

$$\mathbf{Y}_{nl} = \mathbf{Y}_S(\varepsilon_m, \varepsilon_v, \varepsilon_d, \bar{\varepsilon}_m, \bar{\varepsilon}_v, \bar{\varepsilon}_d, \boldsymbol{\sigma})$$



Multi-surface nonlocal porous model

- Competition between different modes

- Yield surface

$$\Phi_e = \frac{\hat{\sigma}}{\sigma_Y} - 1 = 0$$

- Effective stress

$$\hat{\sigma} = \max(\hat{\sigma}_G, \hat{\sigma}_T, \hat{\sigma}_S)$$

- Approximated form

$$\hat{\sigma} = (\hat{\sigma}_G^m + \hat{\sigma}_T^m + \hat{\sigma}_S^m)^{\frac{1}{m}}$$

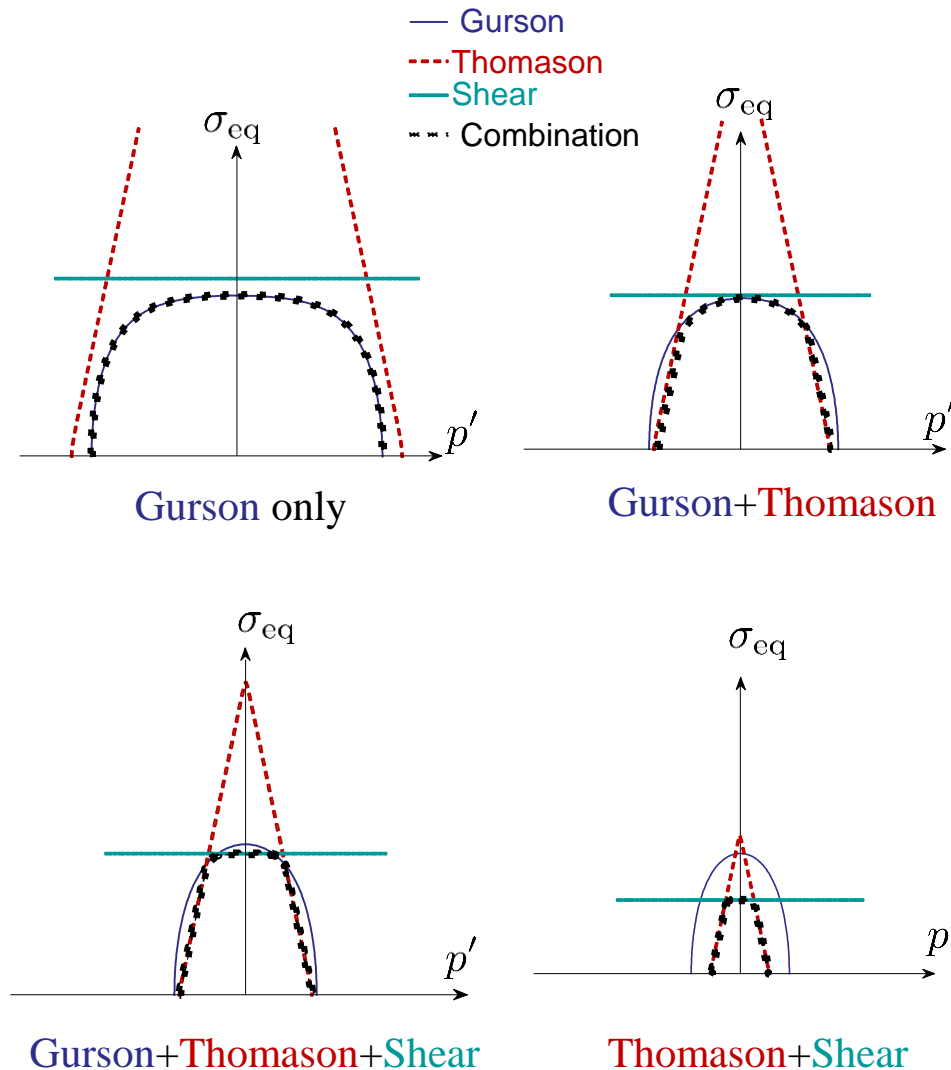
- Smoothing using $m \gg 1$

- Onset of void necking coalescence

$$\dot{\epsilon}_m > 0, \text{ and } \hat{\sigma}_T > \max(\hat{\sigma}_G, \hat{\sigma}_S)$$

- Onset of void shear coalescence

$$\dot{\epsilon}_m > 0, \text{ and } \hat{\sigma}_S > \max(\hat{\sigma}_G, \hat{\sigma}_T) .$$



Multi-surface nonlocal porous model

- Solution under proportional loadings

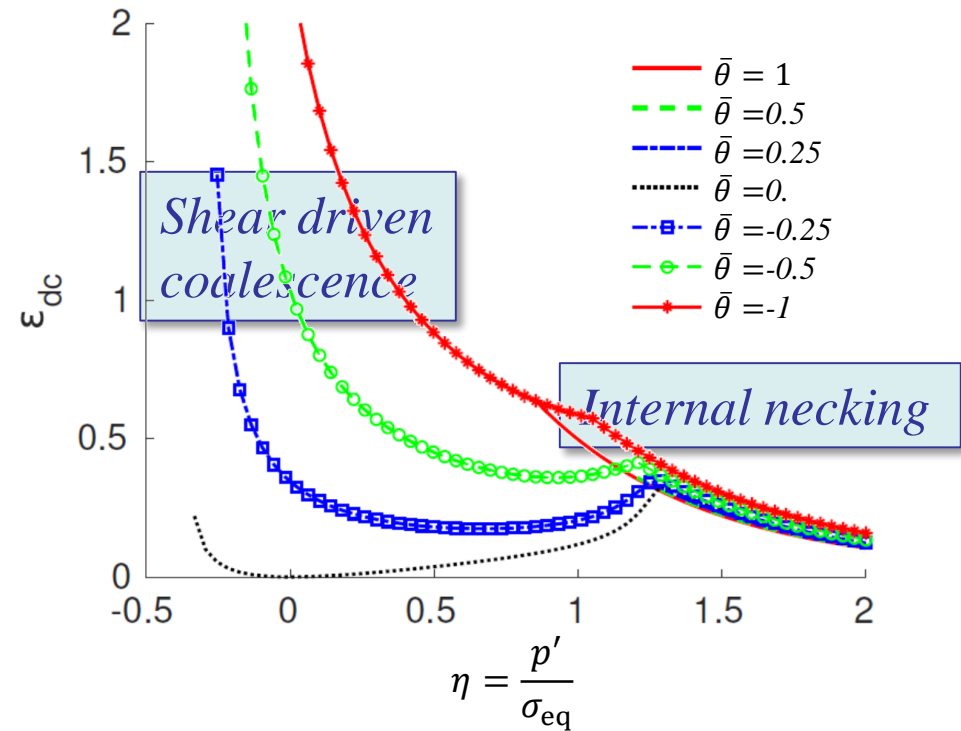
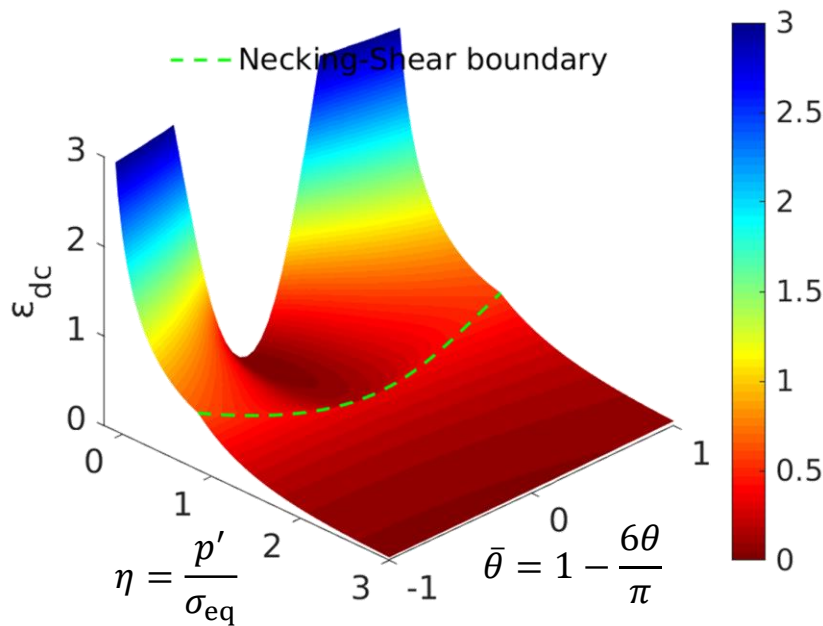
- Constant
 - Stress triaxiality (η); and
 - Normalized Lode angle ($\bar{\theta}$)
- ε_{dc} - ductility = plastic deformation at coalescence onset

$$\eta = \frac{p'}{\sigma_{eq}} \quad p' = \frac{\text{tr}(\boldsymbol{\sigma})}{3}$$

$$\sigma_{eq} = \sqrt{\frac{3}{2} \text{dev}(\boldsymbol{\sigma}) : \text{dev}(\boldsymbol{\sigma})}$$

$$\bar{\theta} = 1 - \frac{6\theta}{\pi}$$

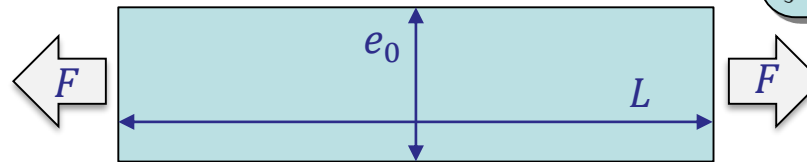
$$\theta(\sigma_{eq}, J_3) = \frac{1}{3} \arccos \frac{27J_3}{2\sigma_{eq}^3}$$



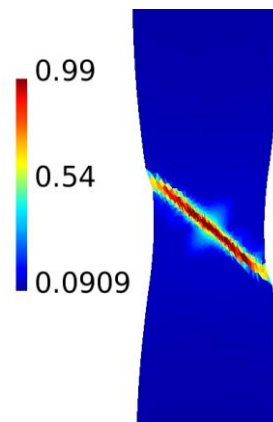
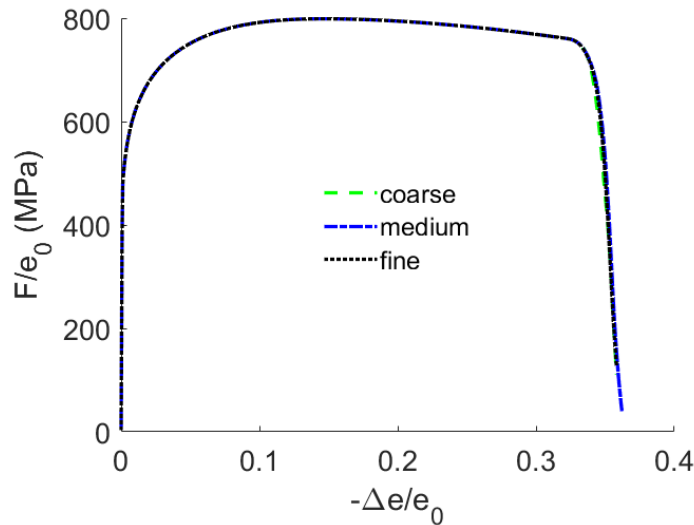
Numerical examples

- Plane strain smooth specimen under tensile loading
 - Verification of the nonlocal model: mesh convergence

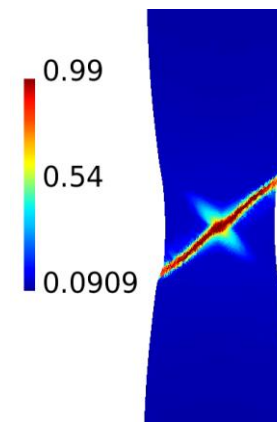
$L = 12.5 \text{ mm}$
 $e_0 = 3 \text{ mm}$
 $\xi = 1.015$ ($\varepsilon_{ds} = 0.95$)



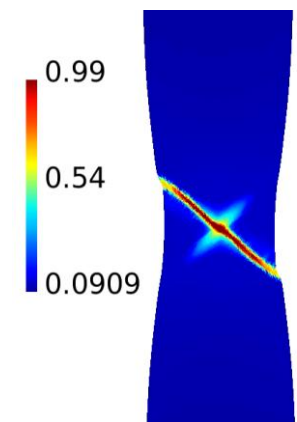
Distribution of void ligament ratio χ



Coarse



Medium



Fine

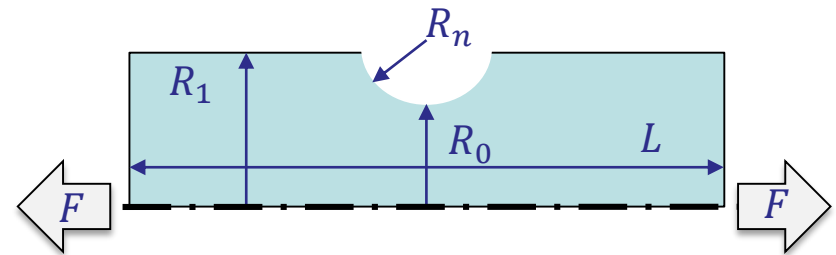
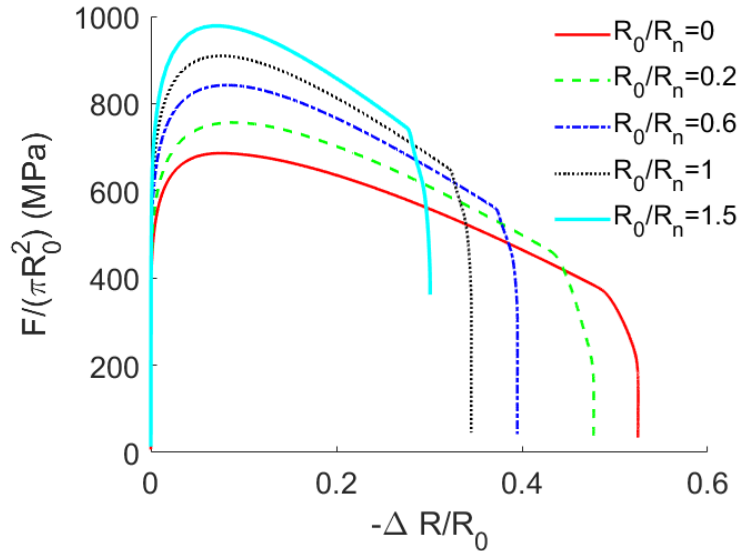
Capture slant fracture

Numerical examples

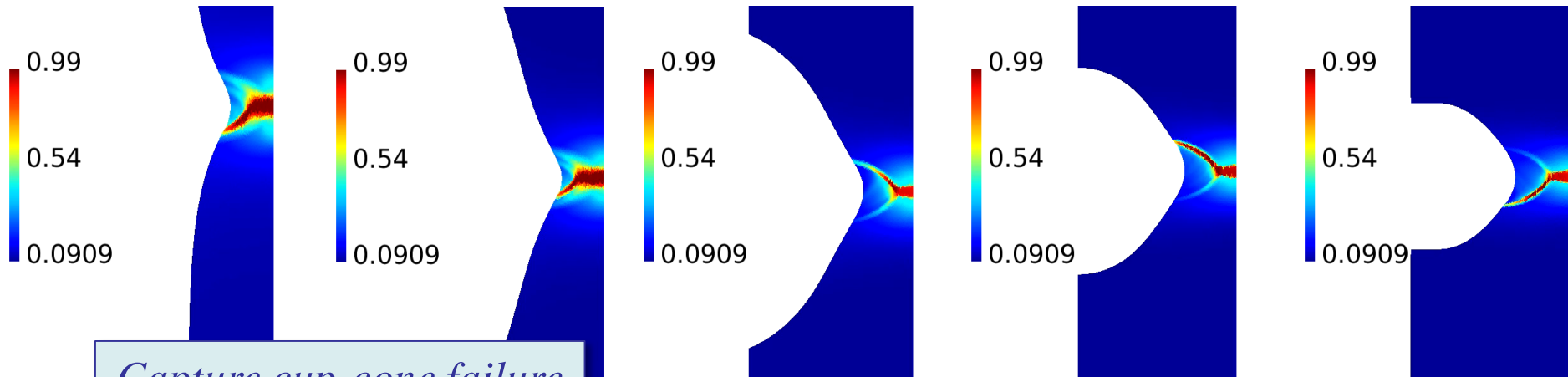
- Axisymmetric (notched) specimens under tensile loading

- Different notch radii: $R_0/R_n = 0, 0.2, 0.6, 1, 1.5$

$R_0 = 3 \text{ mm}$
 $R_1 = 6 \text{ mm}$
 $L = 25 \text{ mm}$
 $\xi = 1.015 \ (\epsilon_{ds} = 0.95)$



Distribution of void ligament ratio χ



Capture cup-cone failure



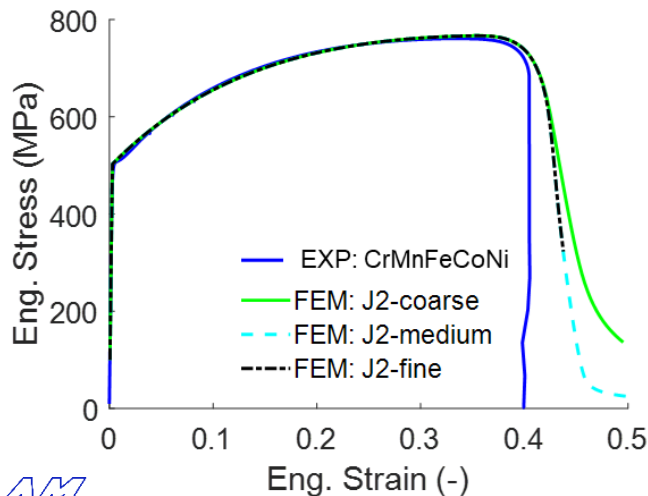
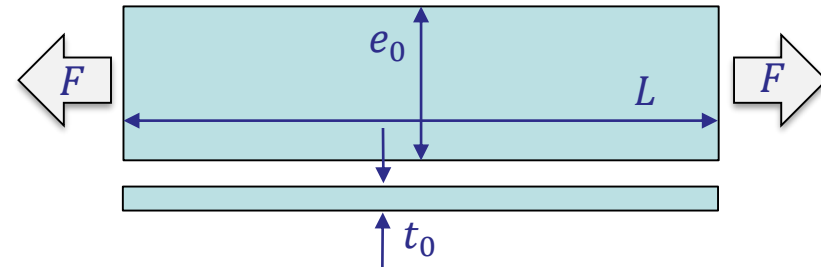
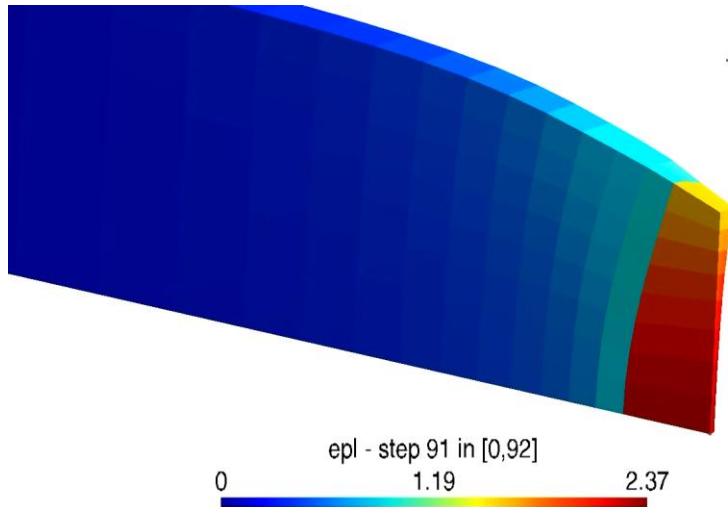
Application to HEA: Preliminary tests without MSS-driven coalescence

- Parameters identification of CrMnFeCoNi

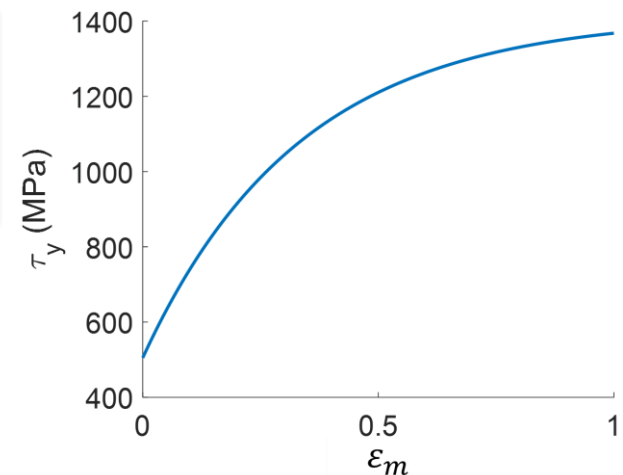
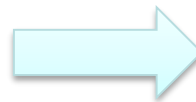
- Hardening law $\sigma_Y(\varepsilon_m)$ identification

Distribution of plastic strain ε_d

$e_0 = 6 \text{ mm}$
 $t_0 = 1.05 \text{ mm}$
 $L = 26 \text{ mm}$



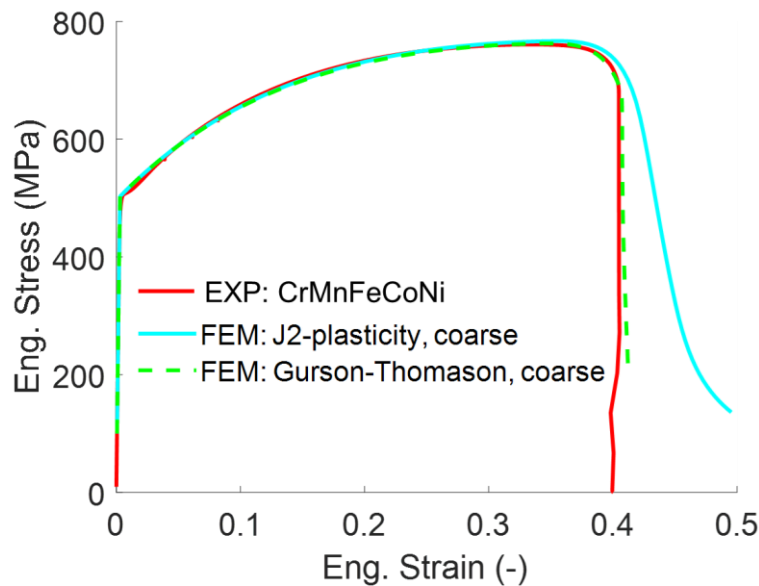
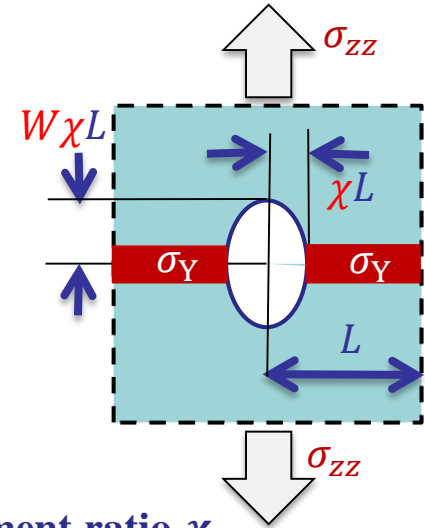
*Elasto-plastic
hardening
identification*



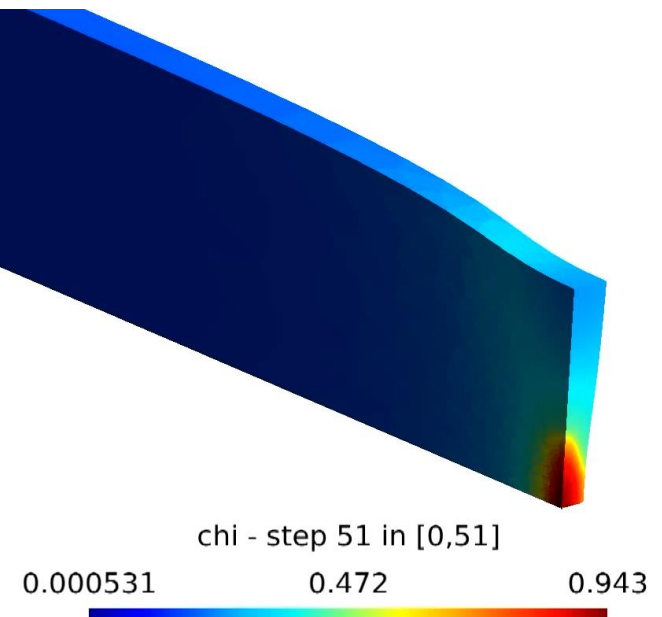
Application to HEA: Preliminary tests without MSS-driven coalescence

- Parameters identification of CrMnFeCoNi
 - Gurson-Thomason parameters identification

$$\begin{cases} \dot{\chi} &= \frac{3}{4} \frac{\lambda}{W} \left(\frac{3}{2\chi^2} - 1 \right) \dot{\epsilon}_d, \\ \dot{W} &= \frac{9}{4} \frac{\lambda}{\chi} \left(1 - \frac{1}{2\chi^2} \right) \dot{\epsilon}_d, \\ \dot{\lambda} &= \kappa \lambda \dot{\epsilon}_d, \end{cases} \quad \Rightarrow \quad \begin{cases} \lambda_0 = 1 \\ \kappa = 1.5 \end{cases}$$



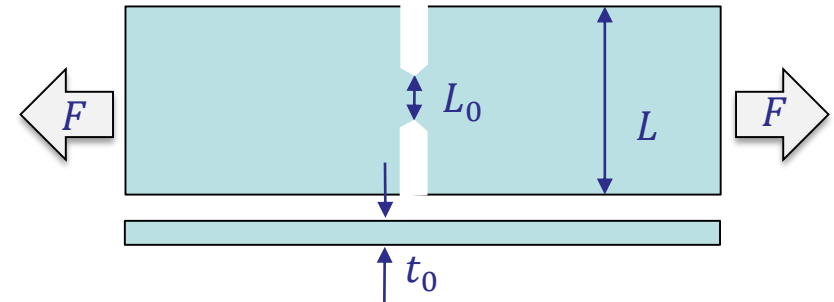
Distribution of void ligament ratio χ



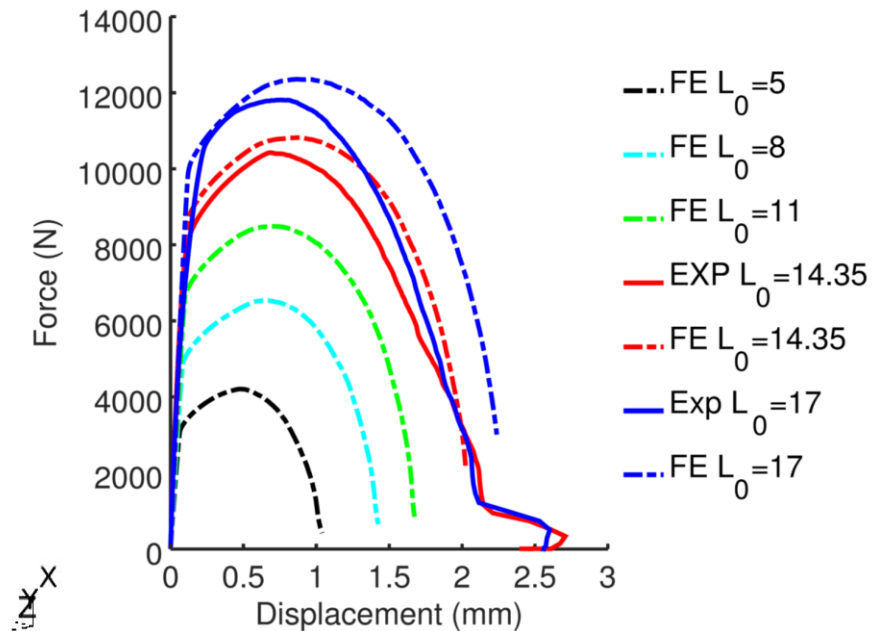
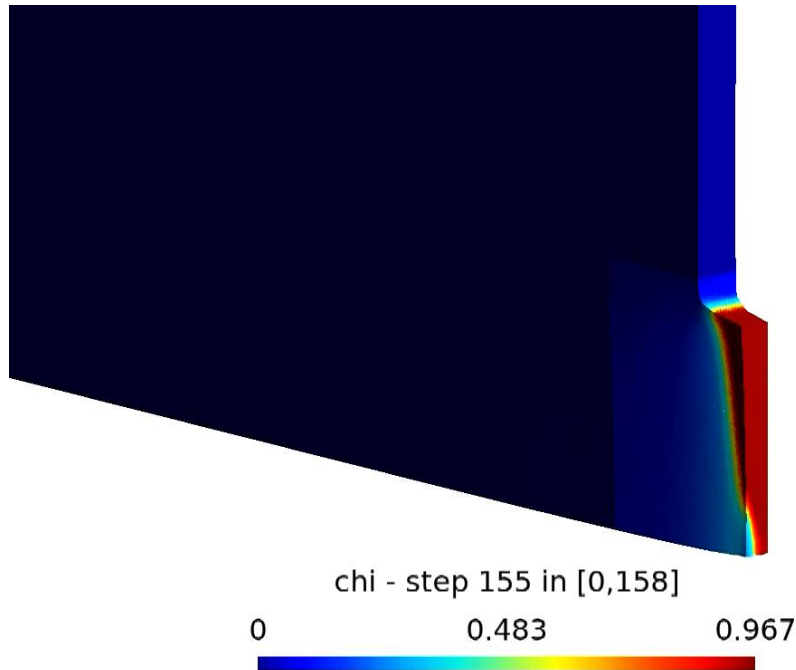
Application to HEA: Preliminary tests without MSS-driven coalescence

- Double notched specimen of CrMnFeCoNi
 - Preliminary results
 - To characterize non-local length
 - To extraction essential work of failure

$$t_0 = 1. \text{ mm}$$
$$L = 26 \text{ mm}$$



Distribution of void ligament ratio χ



Conclusion

- Objective
 - Simulation of ductile failure incorporating void growth & coalescence deformation modes
- Methodology
 - Nonlocal porous plasticity
 - Multi-surface model incorporating
 - Void growth;
 - Internal necking coalescence; and
 - Shear driven coalescence
- Results
 - The proposed framework is able to model
 - The slant fracture mode in plane strain smooth specimens
 - The cup-cone fracture mode in axisymmetric smooth & notched specimens
- In progress
 - Validation/Calibration with HEAs



Thank you for your attention

Computational & Multiscale Mechanics of Materials – CM3

<http://www.ltas-cm3.ulg.ac.be/>

B52 - Quartier Polytech 1

Allée de la découverte 9, B4000 Liège

L.Noels@ulg.ac.be



- Elastic predictor

$$\mathbf{F}^{\text{ppr}} = \mathbf{F}_n^{\text{p}} \quad \mathbf{F}^{\text{epr}} = \mathbf{F} \cdot \mathbf{F}^{\text{ppr}-1}$$

- Plastic corrector (fully implicit radial return)

$$\left\{ \begin{array}{l} \boldsymbol{\tau} = \boldsymbol{\tau}^{\text{pr}} - \mathbb{C} : \Delta \mathbf{E}^{\text{p}}, \\ \boldsymbol{\sigma} = J^{-1} \boldsymbol{\tau}, \\ \sigma_{\text{Y}} = \sigma_{\text{Y}} (\varepsilon_{\text{mn}} + \Delta \varepsilon_{\text{m}}), \\ \mathbf{Y} = \mathbf{Y}_n + \Delta \mathbf{Y} (\Delta \bar{\mathbf{Z}}, \boldsymbol{\sigma}), \\ \Phi_{\text{nl}} (\boldsymbol{\sigma}; \sigma_{\text{Y}}, \mathbf{Y}) = 0, \\ \Delta \mathbf{E}^{\text{p}} - \Delta \mu \mathbf{N}^{\text{p}} (\boldsymbol{\sigma}; \sigma_{\text{Y}}, \mathbf{Y}) = \mathbf{0}, \text{ and} \\ \boldsymbol{\sigma} : \Delta \mathbf{E}^{\text{p}} - (1 - f) \sigma_{\text{Y}} \Delta \varepsilon_{\text{m}} = 0. \end{array} \right.$$

Unknowns: $\boldsymbol{\tau}$, $\boldsymbol{\sigma}$, σ_{Y} , $\Delta \varepsilon_{\text{m}}$, \mathbf{Y} , $\Delta \mathbf{E}^{\text{p}}$, and $\Delta \mu$