

Coalescence Modelling for Settler Design

David Leleu, Andreas Pfennig

dleleu@uliege.be

Products, Environment, and Processes (PEPs)

Department of Chemical Engineering

Université de Liège

www.chemeng.uliege.be/Pfennig

agenda

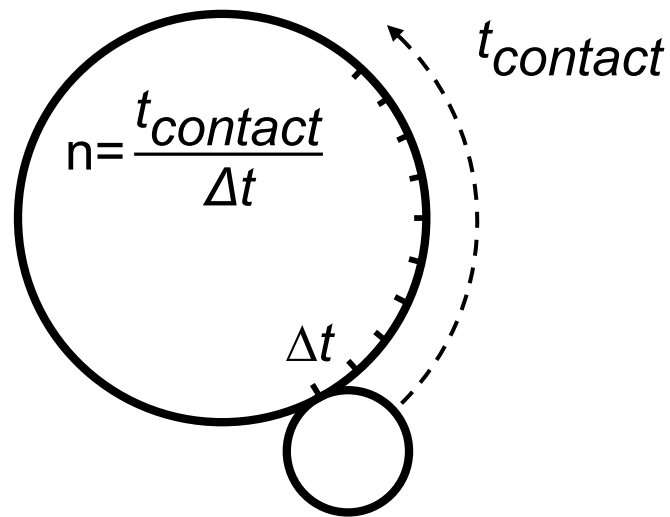
- introduction
- coalescence probability
- contact time
- coalescence time
- summary
- settling simulation

technical equipment's



coalescence probability: fundamental investigation

$$p_{coal,C\&T} = \exp\left(-\frac{t_{coal}}{t_{contact}}\right)$$



$$p_{non-coal,n\Delta t} = p_{non-coal,\Delta t}^n$$

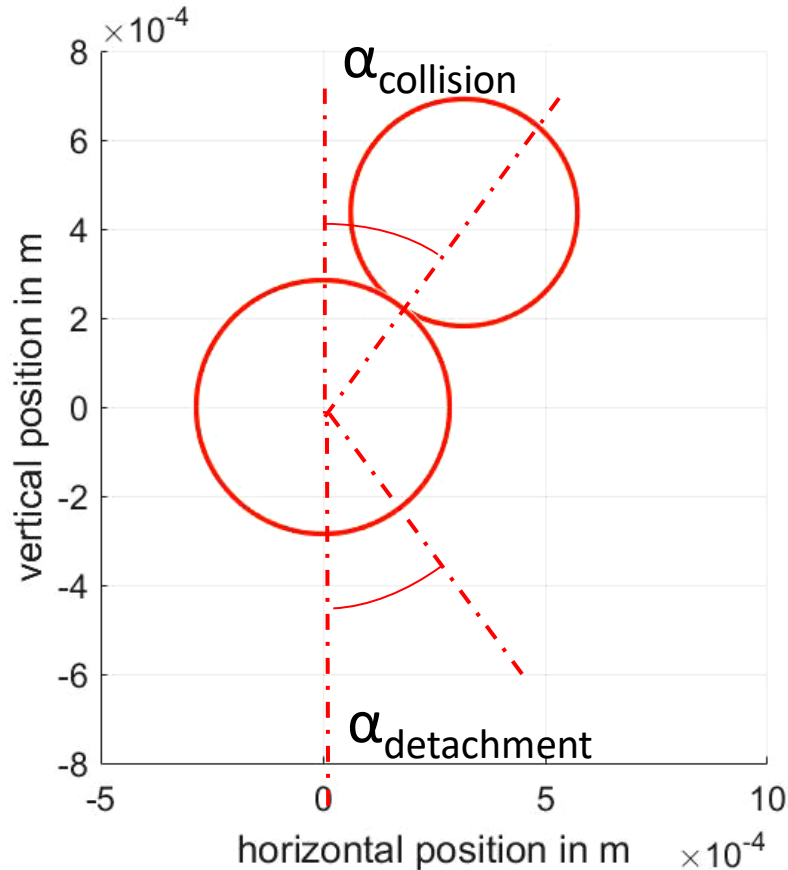
$$p_{non-coal,\Delta t} = \exp\left(-\frac{\Delta t}{t_{coal}}\right)$$

$$p_{non-coal,n\Delta t} = \exp\left(-\frac{n\Delta t}{t_{coal}}\right)$$

$$p_{non-coal} = \exp\left(-\frac{t_{contact}}{t_{coal}}\right)$$

$$p_{coal} = 1 - \exp\left(-\frac{t_{contact}}{t_{coal}}\right)$$

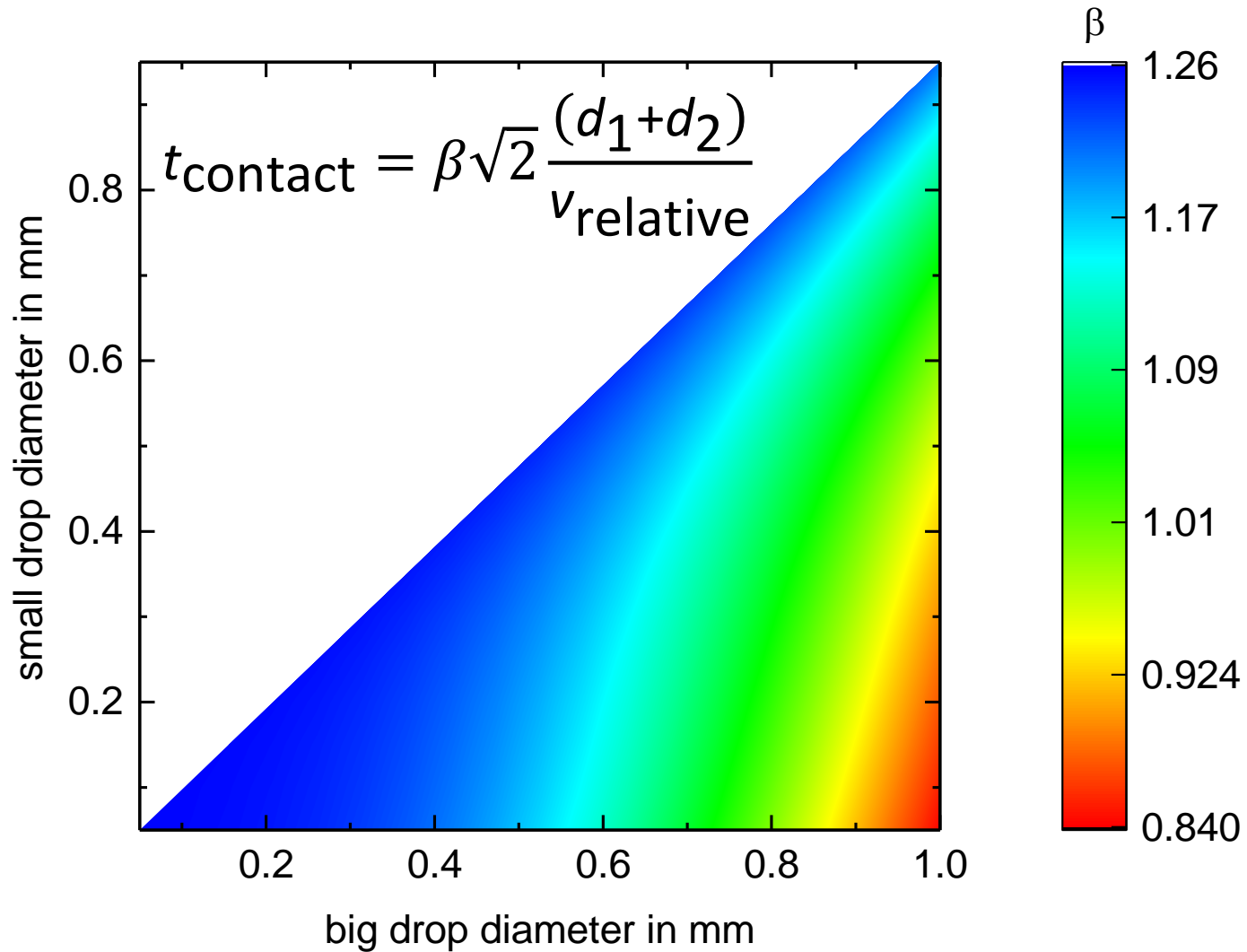
contact time: motion simulation



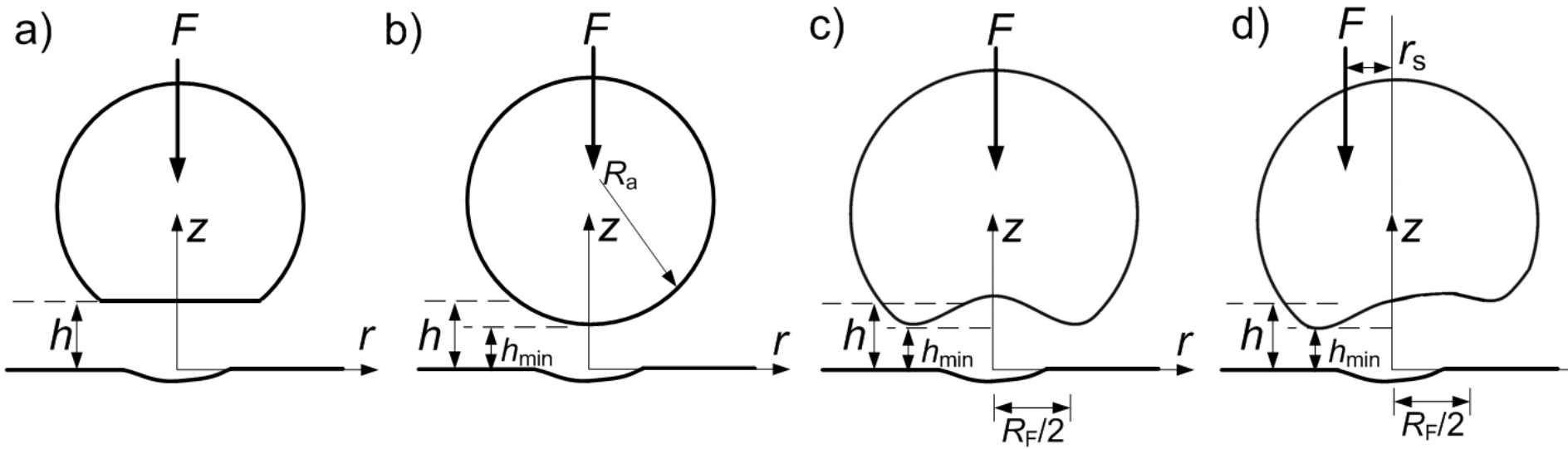
$$t_{\text{contact}} \approx \sqrt{2} \frac{(d_1 + d_2)}{v_{\text{relative}}}$$

- assumptions:
 - drops follow contour during the sedimentation
 - detachment angle = random between $\pi/2$ and π

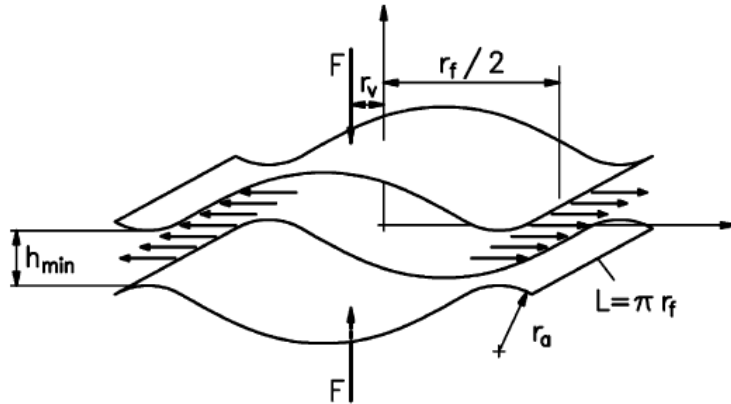
contact time: simulations vs model



coalescence time: asymmetric dimple



coalescence time: film drainage process

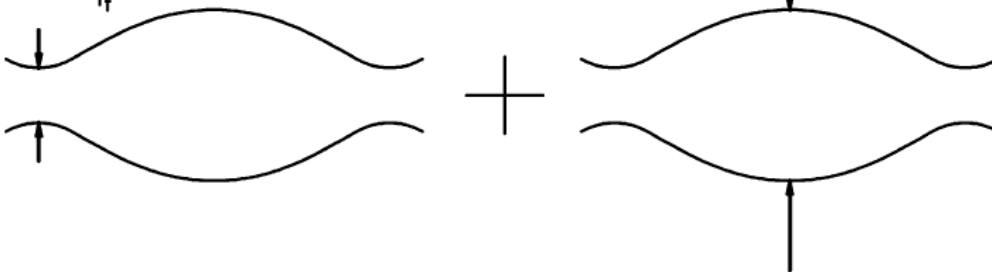


(superposition)

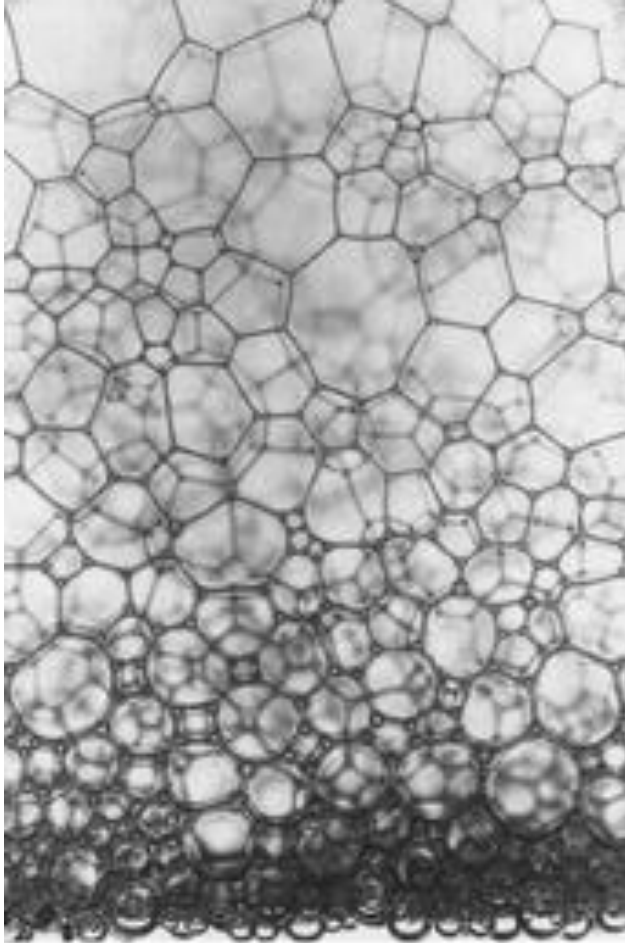
$$t_{\text{coalescence}} = \frac{3\pi^{1.5} \mu R_f R_a^{1.5}}{4r_s^* F_{\text{driving}} \sqrt{h_{\min}}}$$

$$F_v = F \frac{2r_v}{r_f}$$

$$F_z = F - F_v$$



close-packed zone



Arnaud Saint-Jalmes, 2006

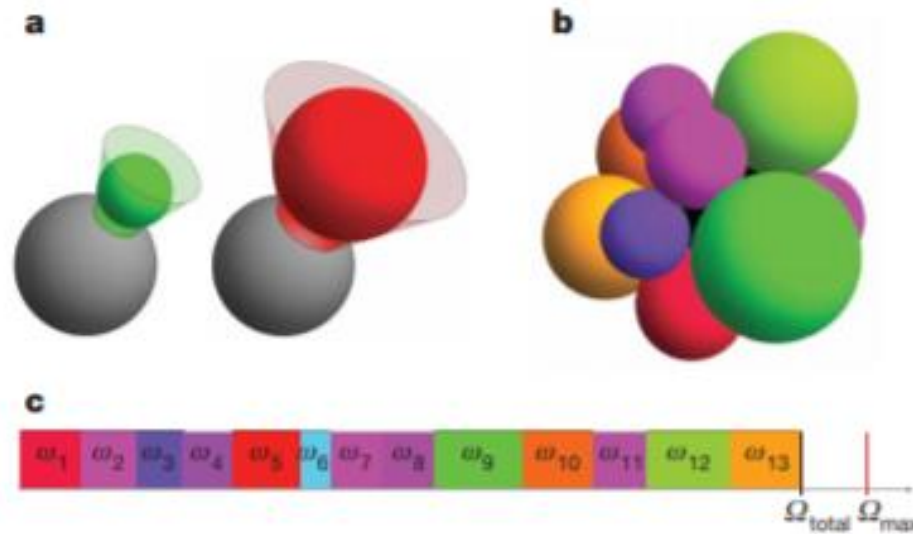
- drops deformation

$$R_{\text{dimple}} \propto A_{\text{contact}}$$

- film drainage

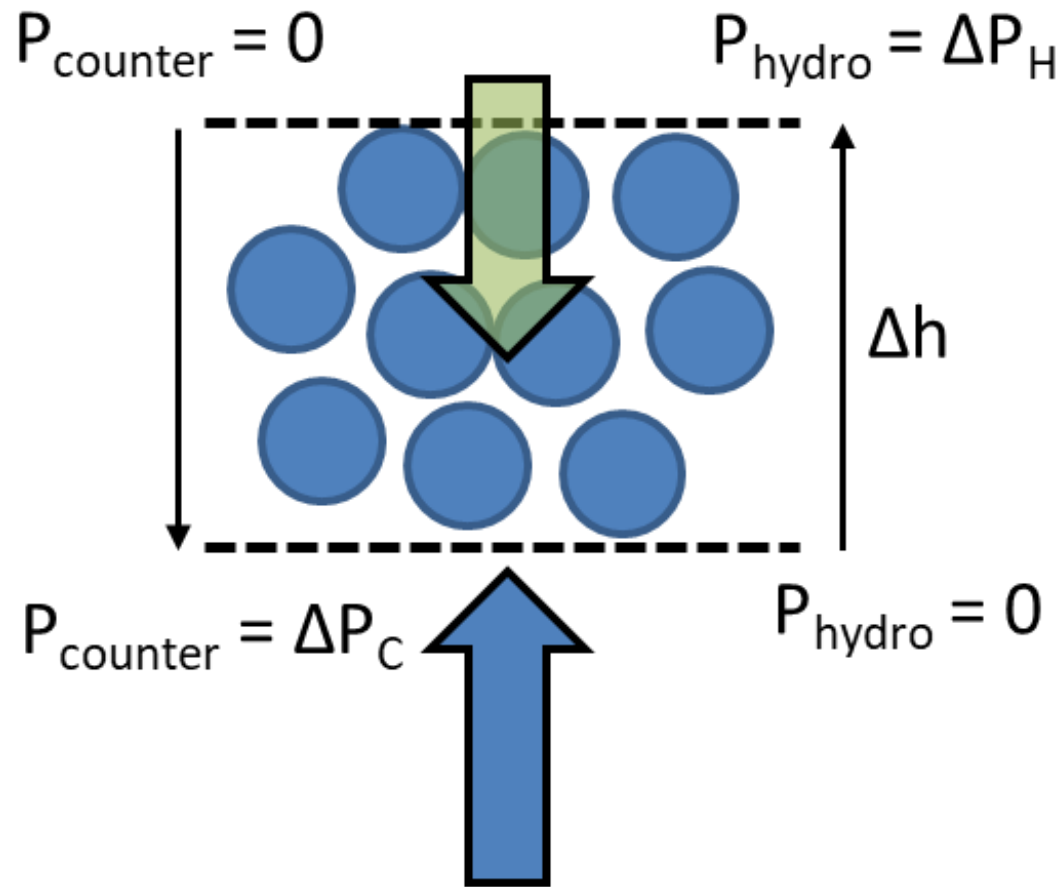
$$F_{\text{driving}} \propto \Delta P_{\text{hydro}} - \Delta P_{\text{flow}}$$

polydispersed packing



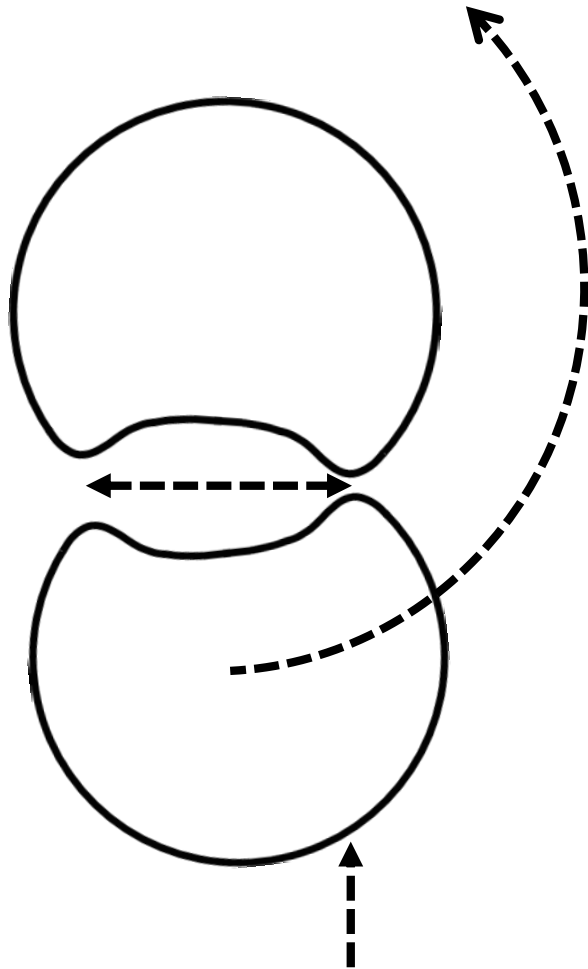
$$\mu \in [0; 1\text{mm}] \text{ and } \sigma \in [0; 50\%]$$
$$\rightarrow \varepsilon \in [70\%; 80\%]$$

counterflow



$$\Delta P_{\text{total}} = \Delta P_H - \Delta P_C$$

summary



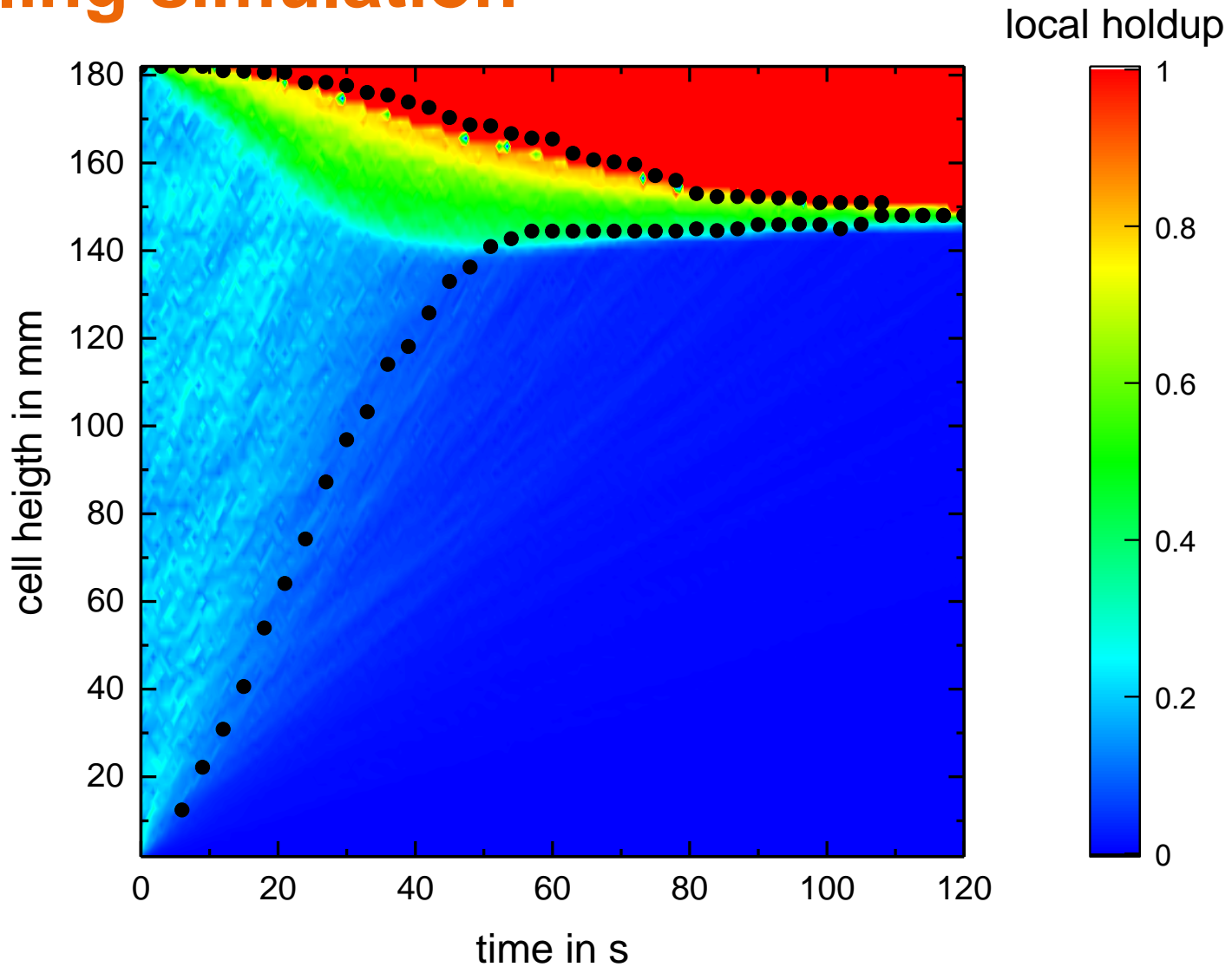
$$p_{\text{coal}} = 1 - \exp\left(-\frac{t_{\text{contact}}}{t_{\text{coal}}}\right)$$

$$t_{\text{contact}} \propto \frac{(d_1 + d_2)}{v_{\text{relative}}}$$

$$\text{dimple} \propto \begin{cases} \text{drops diameter} \\ \text{deformed drops dimension} \end{cases}$$

$$F_{\text{driving}} = \begin{cases} F_{\text{buoyancy}} \\ F_{\text{turbulences}} \\ F_{\text{hydrostatic_pressure}} \end{cases}$$

settling simulation



Coalescence Modelling for Settler Design

David Leleu, Andreas Pfennig

dleleu@uliege.be

Products, Environment, and Processes (PEPs)

Department of Chemical Engineering

Université de Liège

www.chemeng.uliege.be/Pfennig