# MS49: Abstract 48 – EMI 2018 An implicit non-local damage to crack transition framework for ductile materials involving a cohesive band model

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### Introduction

- Goal:
  - To capture the whole ductile failure process made of:
    - A diffuse stage
    - damage onset / nucleation, growth...
       followed by
    - A localised stage
      - damage coalescence
      - crack initiation and propagation



[http://radome.ec-nantes.fr/]







- State-of-the-art:
  - 2 principal approaches to describe material failure:
    - Continuous:
      - Damage models
        - » Lemaitre-Chaboche,
        - » Gurson,
        - » ...



- Discontinuous:
  - Fracture mechanics
    - » Cohesive zone,
    - » XFEM
    - » ...









State of art: two main approaches – 1. Continuous approaches

- Material properties degradation modelled by internal variables (= damage):
  - Lemaitre-Chaboche model,
  - Gurson model,
    - Porosity evolution



- Continuous Damage Model (CDM) implementation: ۲
  - Local form
    - Mesh-dependent
  - Non-local form needed [Peerlings et al. 1998]





#### State of art: two main approaches – 2. Discontinuous approaches

- Similar to fracture mechanics
- One of the most used methods:
  - Cohesive Zone Model (CZM) modelling the crack tip behaviour inserted by:
    - Interface elements between two volume elements
    - Element enrichment (EFEM) [Armero et al. 2009]
    - Mesh enrichment (XFEM) [Moes et al. 2002]
    - ...
- Consistent and efficient hybrid framework for brittle fragmentation: [Radovitzky et al. 2011]
  - Extrinsic cohesive interface elements
  - Discontinuous Galerkin (DG) framework (enables inter-elements discontinuities)









# State of art: two main approaches - Comparison (2)

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**Continuous:** 

Continuous Damage Model (CDM)

- + Capture the diffuse damage stage
- + Capture stress **triaxiality** and **Lode** variable effects
- Mesh dependency without implicit non-local
- Numerical problems with highly damaged elements
- Cannot represent cracks
   without remeshing / element deletion
   at D → 1 (loss of accuracy, mesh
   modification ...)
- Crack initiation observed for lower damage values

**Discontinuous:** 

Extrinsic Cohesive Zone Model (CZM)

+ Multiple crack initiation and propagation naturally managed

- Cannot capture diffuse damage
- No triaxiality effect
- Currently valid for brittle / small scale yielding elasto-plastic materials





- Goal:
  - Simulation of the whole ductile failure process with accuracy
- Main idea:
  - Combination of 2 complementary methods in a single finite element framework:
    - continuous (non-local damage model)
      - + transition to ----> Damage to crack transition
    - discontinuous (cohesive model)



- Discontinuous model here = Cohesive Band Model (CBM):
  - Hypothesis
    - In the last stage of failure, all damaging process occurs in an uniform thin band
  - Principles
    - Replacing the traction-separation law of a cohesive zone by the behaviour of a • uniform band of given thickness  $h_{\rm b}$  [Remmers et al. 2013]
  - Methodology [Leclerc et al. 2017]
    - 1. Compute a band strain tensor  $\mathbf{F}_{b} = \mathbf{F} + \frac{\|\boldsymbol{u}\| \times \boldsymbol{N}}{h_{b}} + \frac{1}{2} \nabla_{T} \|\boldsymbol{u}\|$
    - 2. Compute then a band stress tensor  $\sigma_{\rm h}$
    - 3. Recover traction forces  $t(\llbracket u \rrbracket, F) = \sigma_{\rm b} \cdot n$



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  - At crack insertion, framework only dependent on  $h_{\rm b}$  (band thickness)
    - $h_{\rm b} \neq$  new material parameter
    - A priori determined with underlying non-local damage model to ensure energy consistency





- Influence of  $h_b$  (for a given  $l_c$ ) on response in a 1D elastic case [Leclerc et al. 2017]:
  - Total dissipated energy :
    - Has to be chosen to conserve energy dissipation (physically based)





- 2D elastic plate with a defect
  - Biaxial loading
    - Ratio  $\overline{F}_x/\overline{F}_y$  constant during a test
  - In plane strain
  - Path following method
  - Comparison between:
    - Pure non-local
    - Non-local + cohesive zone (CZM)
    - Non-local + cohesive band (CBM)







• 2D plate in plane strain:  $\overline{F}_x/\overline{F}_y = 0$ 



Non-local only

Non-local + CZM

Non-local + CBM

no crack insertion

cohesive models calibrated on 1D bar in plane stress





- 2D plate in plane strain:

  - Force evolution







- Porous plasticity (or Gurson) approach
  - Assuming a J2-(visco-)plastic matrix







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  - Assuming a J2-(visco-)plastic matrix
  - Including effects of void/defect or porosity on plastic behavior
    - Apparent macroscopic yield surface  $f(\tau_{eq}, p) \le 0$  due to microstructural state:







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        - » Before failure: coalescence or localised plastic flow between voids
          - » GTN or Thomason models







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        - » Before failure: coalescence or localised plastic flow between voids
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  - Including evolution of microstructure during failure process
    - Void growth by diffuse plastic flow
    - Apparent growth by shearing
    - Nucleation / appearance of new voids
    - Void coalescence until failure







#### Non-local porous plasticity model

• Yield surface is considered in the co-rotational space

- Non-local form: 
$$f\left(\tau_{\rm eq}, p, \tau_{\rm y}, \boldsymbol{Z}, \tilde{\boldsymbol{Z}}\right) \leqslant 0$$
 with  $\tilde{f}_{\rm V} - l_{\rm c}^2 \Delta \tilde{f}_{\rm V} = f_{\rm V}$ 

- $\tau^{eq}$  is the von Mises equivalent Kirchhoff stress and p the pressure
- $\tau_{\rm Y} = \tau_{\rm Y}(\hat{p},\dot{p})$  is the viscoplastic yield stress
- $f_{\rm V}$  is the porosity and  $\tilde{f}_{\rm V}$ , its non-local counterpart
- Z is the vector of internal variables
- $l_{\rm c}$  is the non-local length
- Normal associated plastic flow  $\mathbf{D}^{\mathrm{p}}$
- Microstructure evolution (spherical voids):
  - Eq. plastic strain of the matrix:  $\dot{\hat{p}} = \frac{\boldsymbol{\tau}: \mathbf{D}^{\mathrm{p}}}{(1 - f_{\mathrm{V0}})\tau_{\mathrm{Y}}}$
  - Porosity:

$$\dot{f}_{\rm V} = (1 - f_{\rm V}) \operatorname{tr} \mathbf{D}^{\rm p} + \dot{f}_{\rm nucl} + \dot{f}_{\rm shear}$$

• Ligament ratio:

$$\dot{\chi} = \dot{\chi} \left( \chi, \tilde{f}_V, \kappa, \lambda, \mathbf{Z} \right)$$

► Microstructure parameters





### Non-local porous plasticity – Comparison with literature results

- Plane strain specimen [Besson et al. 2003]
  - Only an half is modelled \_
  - Three  $\neq$  mesh sizes





Fine mesh (5987 elements,  $l_{\rm m} \cong 8 l_{\rm c}$ )







Non-local porous plasticity - void growth





Non-local porous plasticity – void growth and coalescence



- Phenomenological coalescence model:
  - replace  $\tilde{f}_{\rm V}$  by an effective value  $\tilde{f}_{\rm V}^*$ :

$$\tilde{f}_{\mathrm{V}}^{\star} = \begin{cases} \tilde{f}_{\mathrm{V}} & \text{if } \tilde{f}_{\mathrm{V}} \leq f_{\mathrm{C}} \\ f_{\mathrm{C}} + R\left(\tilde{f}_{\mathrm{V}} - f_{\mathrm{C}}\right) & \text{if } \tilde{f}_{\mathrm{V}} > f_{\mathrm{C}} \end{cases}$$



•  $f_c$  can be constant or determined by Thomason criterion [Benzerga2014]:  $\max \operatorname{eig}(\boldsymbol{\tau}) - C_{\mathrm{T}}^{\mathrm{f}}(\chi) \tau_{\mathrm{Y}} > 0$ 



Non-local porous plasticity – void coalescence

- Thomason model [Benzerga 2014,Besson 2009]:  $f_{\rm T} = \frac{2}{3}\tau^{\rm eq} + |p| - C_{\rm T}^{\rm f}(\chi) \tau_{\rm Y} \leqslant 0$ 
  - Higher porosity to trigger coalescence
  - No lateral contraction due to plasticity





Non-local porous plasticity – void growth and coalescence

- Coupled non-local Gurson-Thomason:
  - Competition between  $f_{\rm G}$  and  $f_{\rm T}$ \_





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#### Damage to crack transition for porous plasticity

- When coalescence is detected at interface:  $\boldsymbol{n} \cdot \boldsymbol{\tau} \cdot \boldsymbol{n} C_{\mathrm{T}}^{\mathrm{f}}(\chi) \tau_{\mathrm{Y}} > 0$ 
  - Crack insertion using cohesive band model and arbitrary crack paths
  - Coalescence law used at the cracked interfaces only
    - Phenomenological approach with  $\tilde{f}_{\mathrm{V}}^*$
  - Crack path in cup-cone shape



# Conclusion

# • Objective:

 Simulation of material degradation and crack initiation / propagation during the ductile failure process

# • Already done:

- First version of damage to crack transition for ductile materials:
  - Implementation of hyperelastic non-local porous-plastic model
    - Coupled Gurson-Thomason model
  - Cohesive band framework [Leclerc2018] for damage to crack transition

# Upcoming tasks:

- Enrichment of nucleation model and coalescence model
  - Probably with Tekoglu criterion
- Calibration of the band thickness
- Validation/Calibration with literature/experimental tests





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# Thank you for your attention

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### State of art: two main approaches – 1. Continuous approaches

- Non-local model
  - Principles
    - variable  $\xi \rightarrow$  non-local / "averaged" counterpart  $\tilde{\xi}$
  - Formulation
    - Integral form [Bažant 1988]

$$\tilde{\xi}(\boldsymbol{x}) = \frac{1}{V} \int_{V} W(\boldsymbol{x} - \boldsymbol{y}) \xi(\boldsymbol{y}) dV$$

- » not practical for complex geometries
- Differential forms [Peerlings et al. 2001]
  - Explicit formulation / gradient-enhanced formulation:  $\tilde{\xi}(x) = f(\xi, \nabla \xi, \nabla^2 \xi, ...)$ 
    - » does not remove mesh-dependency

- Implicit formulation: 
$$\tilde{\xi}(\boldsymbol{x}) = f\left(\xi, \nabla \tilde{\xi}, \nabla^2 \tilde{\xi}, ...\right)$$
  
 $\tilde{\xi}(\boldsymbol{x}) - l_c^2 \Delta \tilde{\xi}(\boldsymbol{x}) = \xi(\boldsymbol{x})$ 

» removes mesh-dependency but one added unknown field







- Influence of  $h_{\rm b}$  (for a given  $l_{\rm c}$ ) on response in a 1D elastic case [Leclerc et al. 2017]:
  - Total dissipated energy  $\Phi$  = linear with  $h_{\rm b}$ :
    - Has to be chosen to conserve energy dissipation (physically based)









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#### Comparison with phase field

- Single edge notched specimen [Miehe et al. 2010]:
  - Calibration of damage and CBM parameters with 1D case [Leclerc et al. 2018]:



- Validation with Compact Tension Specimen [Geers 1997]:
  - Better agreement with the cohesive band model than the cohesive zone model or the non-local model alone [Leclerc et al. 2018]







- Yield surface is considered in the co-rotational space
  - Local form:  $f\left( au_{ ext{eq}}, p, au_{ ext{y}}, oldsymbol{Z}
    ight) \leqslant 0$ 
    - $\tau^{eq}$  is the von Mises equivalent Kirchhoff stress and p, the pressure
    - $\tau_{\rm Y} = \tau_{\rm Y}(\hat{p},\dot{\hat{p}})$  is the viscoplastic yield stress
    - Z is the vector of internal variables
    - Normal plastic flow decomposition:

$$\mathbf{D}^{\mathrm{p}} = \dot{\mathbf{F}}^{\mathrm{p}} \cdot \mathbf{F}^{\mathrm{p}-1} = \dot{\lambda} \frac{\partial f}{\partial \boldsymbol{\tau}} = \dot{d} \frac{\partial \tau_{\mathrm{eq}}}{\partial \boldsymbol{\tau}} + \dot{q} \frac{\partial p}{\partial \boldsymbol{\tau}}$$

- Plastic deformation of the matrix from the equivalence of plastic energy:  $(1 f_{\rm V0}) \tau_{\rm Y} \dot{\hat{p}} = \boldsymbol{\tau} : \mathbf{D}^{\rm p}$
- Microstructure evolution (porosity  $f_V$  and ligament ratio  $\chi$ ):

$$\dot{f}_{\rm V} = (1 - f_{\rm V}) \operatorname{tr} \mathbf{D}^{\rm p} + \dot{f}_{\rm nucl} + \dot{f}_{\rm shear}$$
  
 $\dot{\chi} = \dot{\chi} \left( \chi, f_{V}, \mathbf{Z} \right)$ 

- Drawbacks
  - The numerical results change with the size and the direction of mesh



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• Evolution of local porosity

$$\dot{f}_{\rm V} = (1 - f_{\rm V}) \operatorname{tr} \mathbf{D}^{\rm p} + \dot{f}_{\rm nucl} + \dot{f}_{\rm shear}$$

- Void nucleation  $\dot{f}_{nucl}$ 
  - Modify porosity growth rate (where  $A_N$ ,  $f_N$ ,  $\epsilon_N$ ,  $s_N$  are material parameters)
    - Linear strain-controlled growth

$$\dot{f}_{\text{nucl}} = A_{\text{N}}\dot{\hat{p}}$$
 with  $A_{\text{N}}\begin{cases} \neq 0 & \text{if } f_{\text{V}} > f_{\text{N}}, \\ = 0 & \text{otherwise.} \end{cases}$ 

- Gaussian strain-controlled growth

$$\dot{f}_{\rm nucl} = \frac{f_{\rm N}}{\sqrt{2\pi s_{\rm N}^2}} \exp\left(-\frac{(\hat{p}-\epsilon_{\rm N})^2}{2s_{\rm N}^2}\right) \dot{\hat{p}}$$





• Evolution of local porosity

$$\dot{f}_{\rm V} = (1 - f_{\rm V}) \operatorname{tr} \mathbf{D}^{\rm p} + \dot{f}_{\rm nucl} + \dot{f}_{\rm shear}$$

- Shear-induced voids growth  $\dot{f}_{\rm shear}$ 
  - Includes Lode variable effect (where  $k_w$  is a material parameter)

$$\dot{f}_{\mathrm{shear}} = f_{\mathrm{V}} k_{\mathrm{w}} \omega \left( \boldsymbol{\tau} \right) rac{ \boldsymbol{\tau}^{\mathrm{dev}} : \mathbf{D}^{\mathrm{p}} }{ \boldsymbol{\tau}^{\mathrm{eq}} }$$







# Hyperelastic formulation:

- Multiplicative decomposition of deformation gradient in elastic and plastic parts:  $\mathbf{F} = \mathbf{F}^{e} \cdot \mathbf{F}^{p}$
- Logarithmic elastic potential  $\psi$ : \_

$$\psi(\mathbf{C}^{e}) = \frac{K}{2} \ln^{2} J^{e} + \frac{G}{4} \left( \ln \mathbf{C}^{e} \right)^{\text{dev}} : \left( \ln \mathbf{C}^{e} \right)^{\text{dev}}$$
with  $\mathbf{C}^{e} = \mathbf{F}^{e} \cdot \mathbf{F}^{e^{T}}$  and  $J^{e} = \det \mathbf{F}^{e}$ 

- Stress tensor definition PK1 stress:  $\mathbf{P} = 2\mathbf{F} \cdot \frac{\partial \psi}{\partial \mathbf{C}}$ 

  - Kirchhoff stresses:  $\kappa = \mathbf{P} \cdot \mathbf{F}^{\mathrm{T}}$  or again:

$$\boldsymbol{\kappa} = p\mathbf{I} + (\boldsymbol{\kappa})^{\text{dev}} = p\mathbf{I} + \mathbf{F}^{\text{e}} \cdot \left[\mathbf{C}^{\text{e}-1} \cdot (\boldsymbol{\tau})^{\text{dev}}\right] \cdot \mathbf{F}^{\text{e}T}$$
$$\boldsymbol{\tau} = p\mathbf{I} + (\boldsymbol{\tau})^{\text{dev}} = p\mathbf{I} + 2G\left(\ln\sqrt{\mathbf{C}^{\text{e}}}\right)^{\text{dev}}$$





- Predictor-corrector procedure
  - Elastic predictor
  - Plastic corrector (radial return-like algorithm)
    - 3 Unknowns  $\Delta \hat{d}$ ,  $\Delta \hat{q}$ ,  $\Delta \hat{p}$
    - 3 Equations
      - Consistency equation:

$$f\left(\tau_{\rm eq}(\Delta \hat{d}), p(\Delta \hat{q}), \tau_{\rm Y}(\Delta \hat{p}), \boldsymbol{Z}(\Delta \hat{d}, \Delta \hat{q}, \Delta \hat{p}), \tilde{\boldsymbol{Z}}\right) = 0$$

- Plastic flow rule:

$$\Delta \hat{d} \frac{\partial f}{\partial p} - \Delta \hat{q} \frac{\partial f}{\partial \tau_{\rm eq}} = 0$$

- Matrix plastic strain evolution:

$$(1 - f_{\rm V0}) \tau_{\rm Y} \Delta \hat{p} = \tau_{\rm eq} \Delta \hat{d} + p \Delta \hat{q}$$



