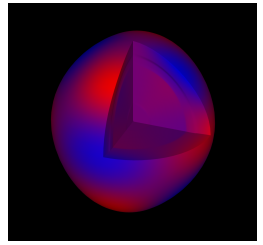




Current challenges in the physics of white dwarfs  
Santa Fe, 12-16 June 2017



## Pulsations in white dwarf stars

Valerie Van Grootel

(STAR Institute, Liège University, Belgium)

---

### Main collaborators:

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E.M. Green  
(U. Arizona)

# Outline

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- I. What is asteroseismology ?
- II. The zoo of pulsations in white dwarfs
- III. What can be learned from white dwarf asteroseismology
- IV. What do we need for white dwarf asteroseismology

# Outline

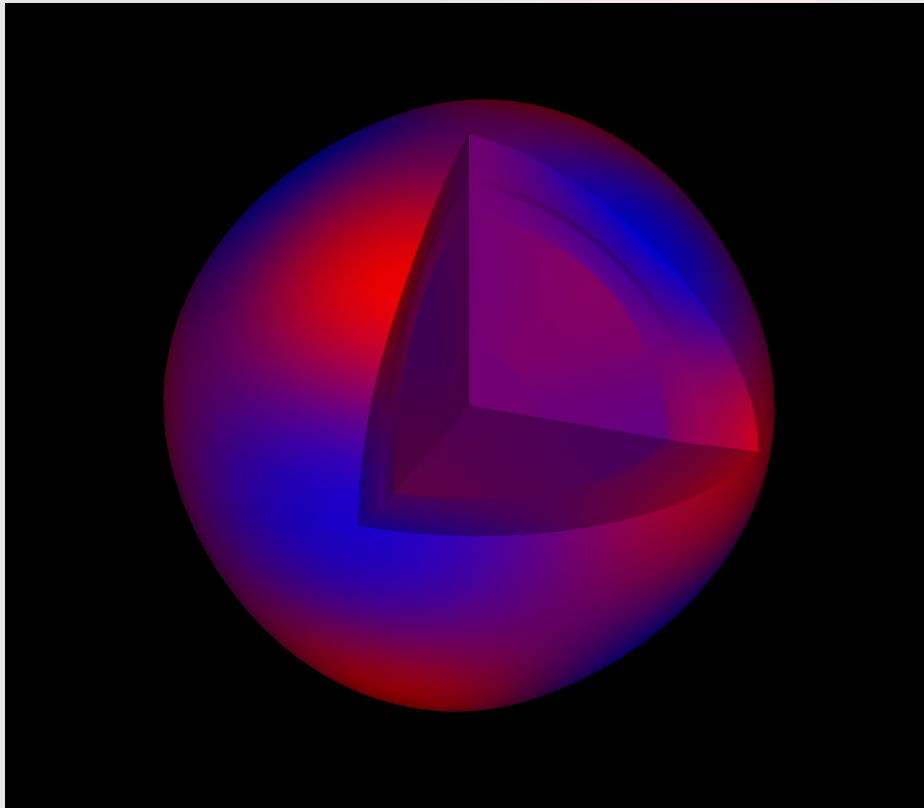
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# What is asteroseismology ? (“stellar seismology”)

*Study the interiors of stars by interpreting their pulsations*

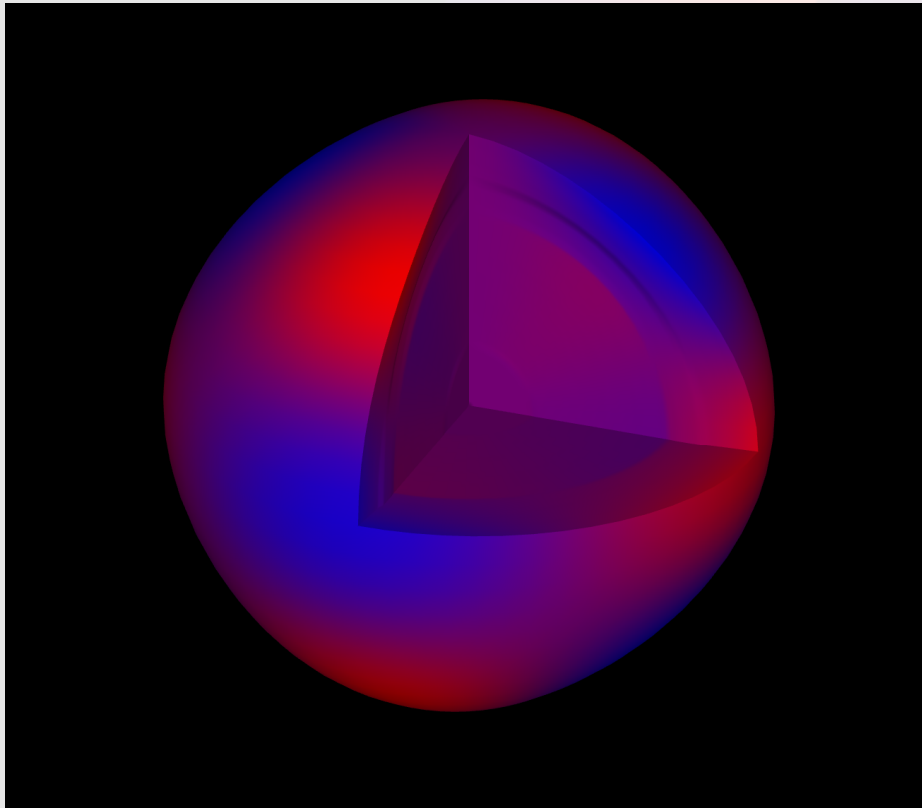
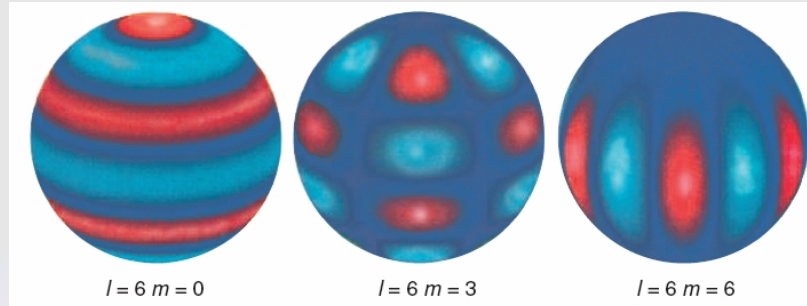
Goal: improve our knowledge of stellar interiors (stars are opaque...)



## What is not well known ?

- Global properties (mass, radius,...)
- Thermonuclear fusion properties
- Microphysics (opacities)
- Convection properties  
(core, envelope)
- Microscopic transport (gravitational settling, radiative forces)
- Macroscopic transport (differential rotation, magnetism, etc.)
- ...

# What is asteroseismology ? (“stellar seismology”)

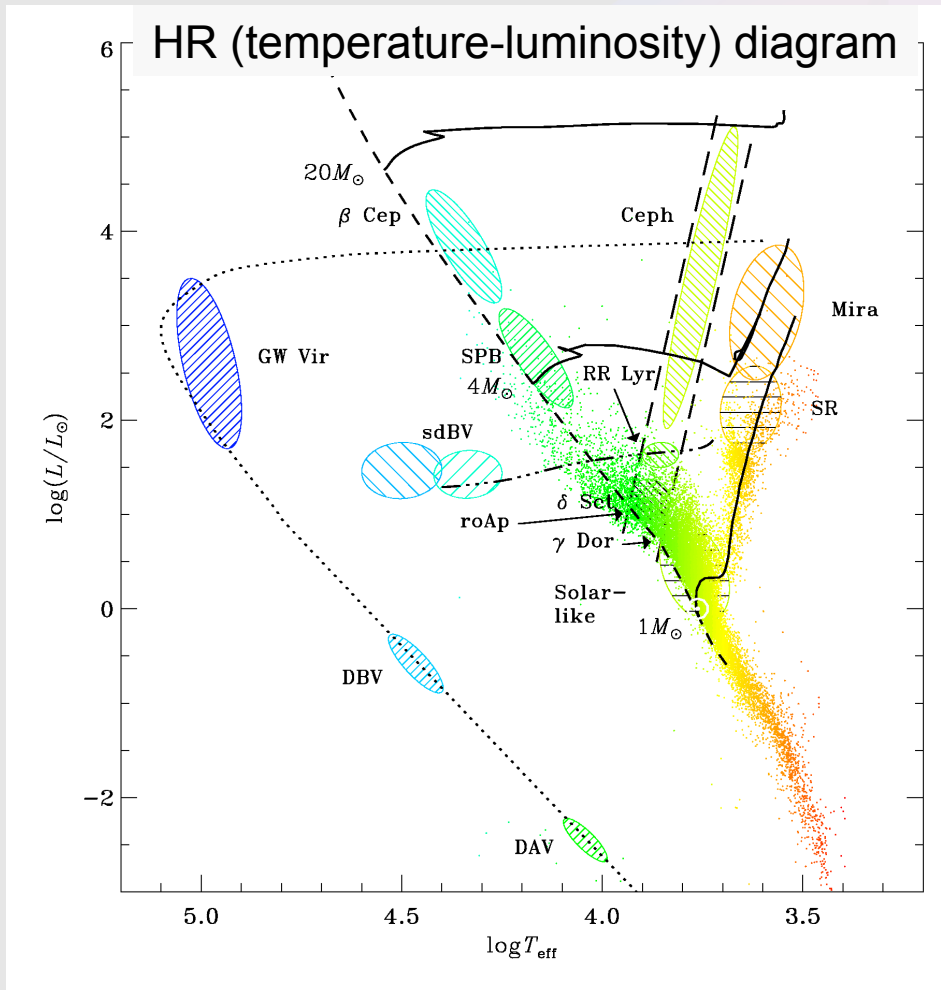


## Theoretical grounds:

- Linearized equations of hydrodynamics
- Angular dependence described with spherical harmonics
- Pulsations are excited and propagate in some regions, and are evanescent in others
- In white dwarfs: gravity modes

# A zoo of pulsating stars

*representative of different stages of evolution (from birth to death)*



Main sequence stars  
(H-burning)  
including the Sun

Intermediate stages of evolution

- Red Giants
- Horizontal Branch stars  
(He-burning), eg. sdB stars

Late stages of evolution

White dwarfs (no burning)

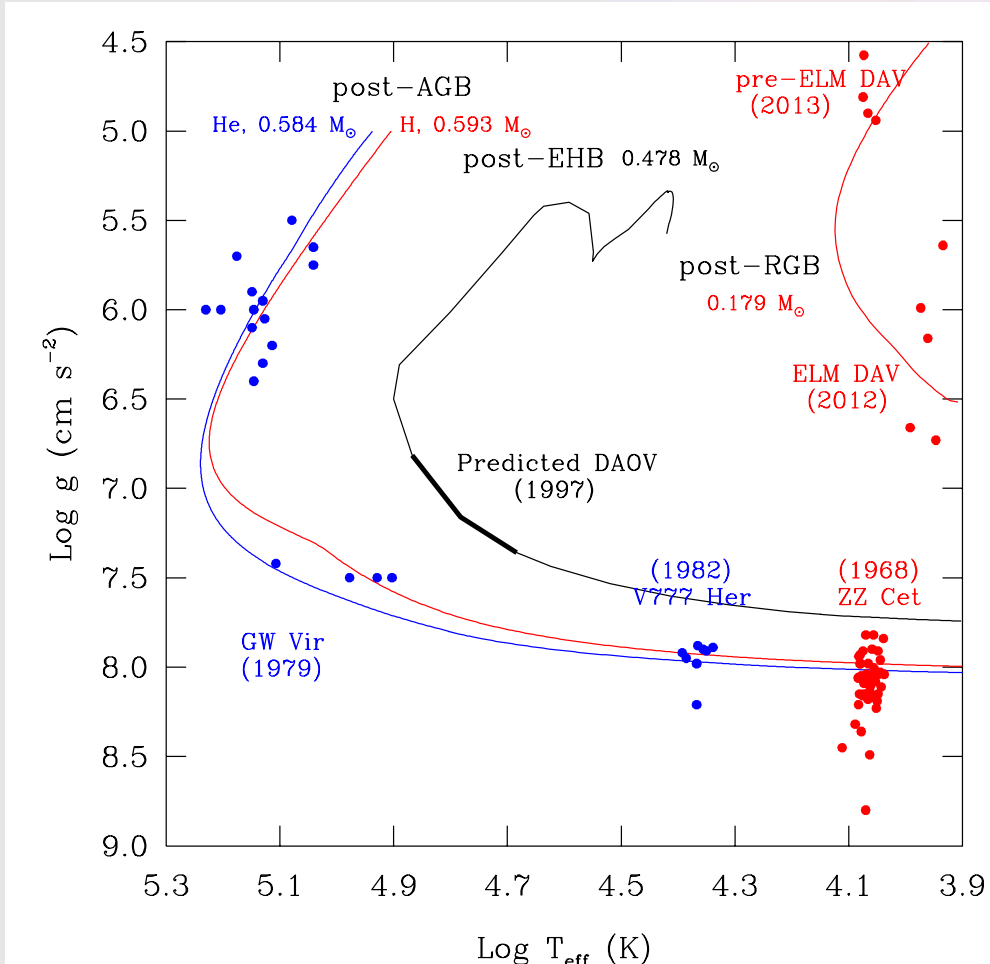
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# The zoo of pulsating white dwarfs

Pulsators are present at various masses and evolutionary stages



Courtesy: G. Fontaine

## Classical ( $\sim 0.6 M_{\odot}$ , $0.5-1.2 M_{\odot}$ )

- **GW Vir or PG1159**, He-C-O atmo ( $\sim 140,000-80,000$  K,  $\sim 20$  pulsators are known)
- **V777 Her (DBV)**, He-rich atmo ( $\sim 30,000-25,000$  K,  $\sim 15$  known)
- **ZZ Ceti (DAV)**, H atmo ( $\sim 12,000-11,000$  K,  $\sim 60$  known)

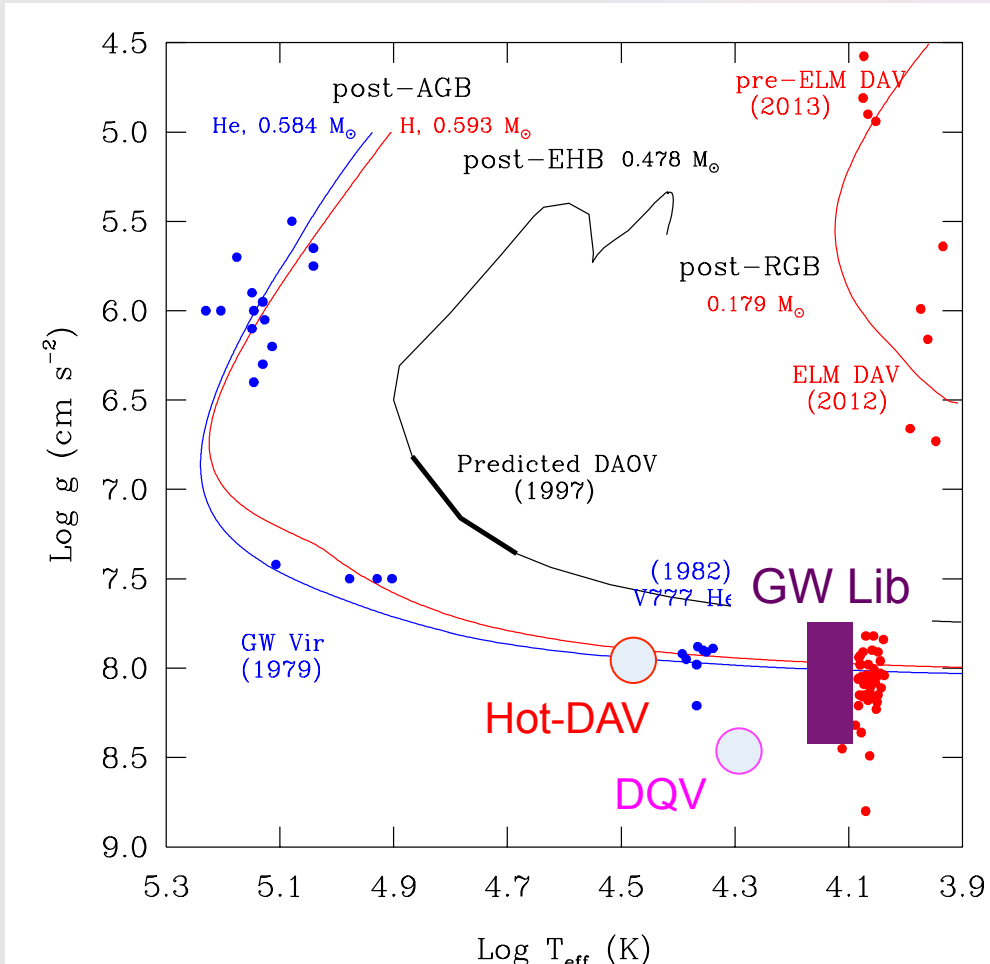
## Extremely Low-Mass ( $\sim 0.2 M_{\odot}$ )

- **Pre-ELM**, H-He atmo, 5 known
- **ELM DAV**, H atmo, 5 known



# The zoo of pulsating white dwarfs

Pulsators are present at various masses and evolutionary stages



Courtesy: G. Fontaine

## Predicted

- DAOV (post-EHB)
- Hot-DAV ( $\sim 30,000$  K)

## Exotics

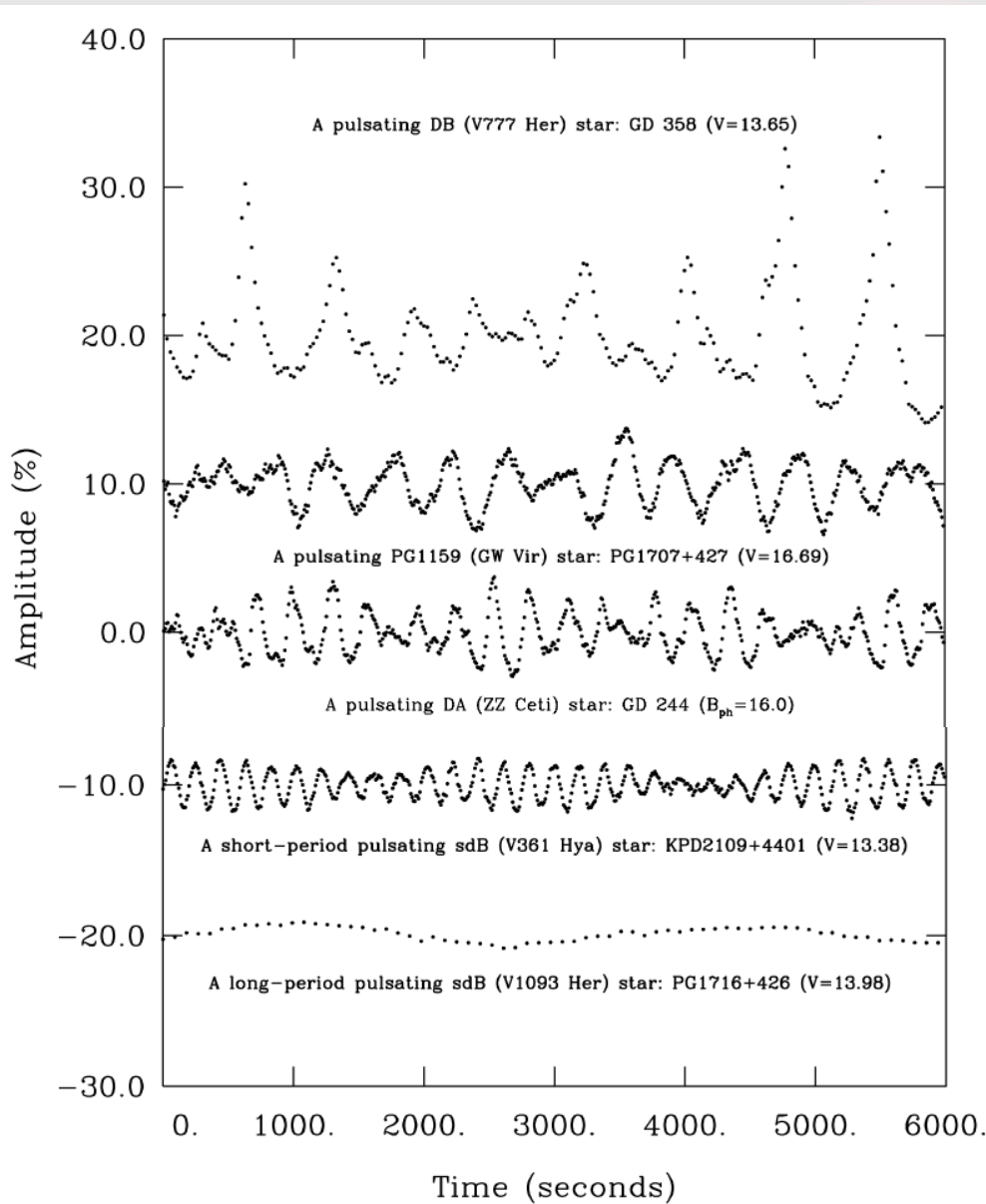
- GW Lib, accreting white dwarfs, H-He atmo,  $\sim 15$  known

## Dismissed? (as self-driven pulsator)

- DQV, C-rich atmo,  $\sim 5$  known, highly magnetic (MG)

*Rotation rather than pulsations?*  
(not multiperiodic + theoretical works)

# The zoo of pulsating white dwarfs



## Multiperiodic pulsators ( $V \sim 15 - 20$ )

- GW Vir stars: 500-5000 s
- V777 Her stars: 150 - 1000 s
- ZZ Ceti stars: 100 - 1000 s
- Pre-ELM white dwarfs: 300-1000 s
- ELM white dwarfs: 1500-5000 s

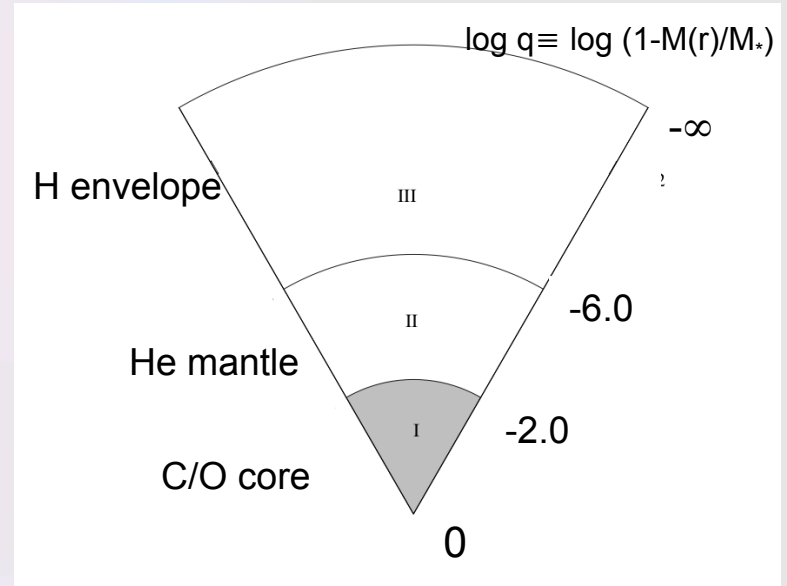
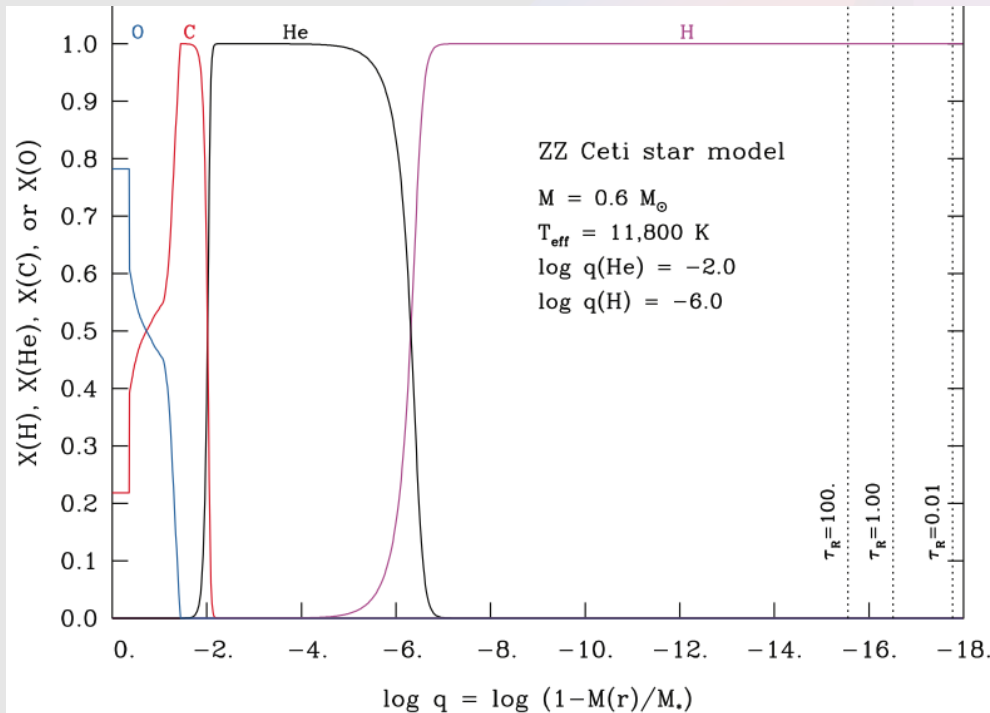
← short-period pulsating sdB

← long-period pulsating sdB

# Typical internal structure of a white dwarf

Here: ZZ Ceti model,  $0.6M_{\odot}$ ,  $T_{\text{eff}}=11,800$  K

“onion-like” stratification



ELM: He-core

Very massive: Ne-Mg core

**Internal stratification and core composition not well known !**

(reflects uncertainties on the previous phases of stellar evolution:  $^{12}\text{C}(\alpha,\gamma)^{16}\text{O}$  rate, various mixing processes, thermal pulses on AGB, etc)

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---

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# 1. “Quantitative asteroseismology” ( $P_{\text{obs}} \Leftrightarrow P_{\text{theo}}$ )

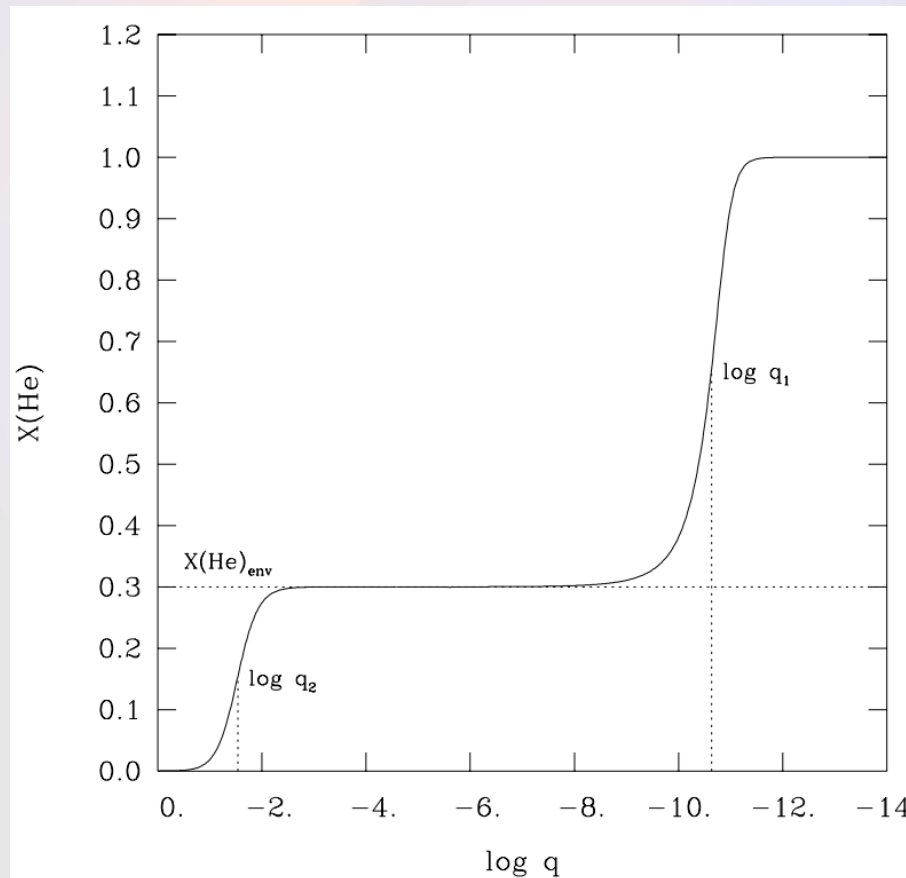
Search the stellar model(s) whose theoretical periods best fit all the observed ones, in order to minimize

$$S^2(a_1, a_2, \dots, a_N) = \sum_{i=1}^{N_{\text{obs}}} (P_{\text{obs}}^{(i)} - P_{\text{th}}^{(i)})^2$$

- > **Models:** Parametrized/static models (*independent of stellar evolution*), or grids of fully evolutionary models  
*N parameters:*  $T_{\text{eff}}$ ,  $\log g$ , envelope layering, core composition, convection efficiency
- > **Optimization procedure:** Efficient optimization codes (based on *Genetic Algorithms*) to thoroughly explore the parameter space and find the minima of  $S^2$   
Under *external* constraints from spectroscopy + mode identification (if available)
- > **Results:** structural and core parameters of the star ( $M_*$ ,  $M_{\text{env}}$ ,  $M_{\text{core}}$ , etc.), internal chemical stratification (elements profiles)

# The example of the V777Her star KIC08626021 (Giammichele et al.)

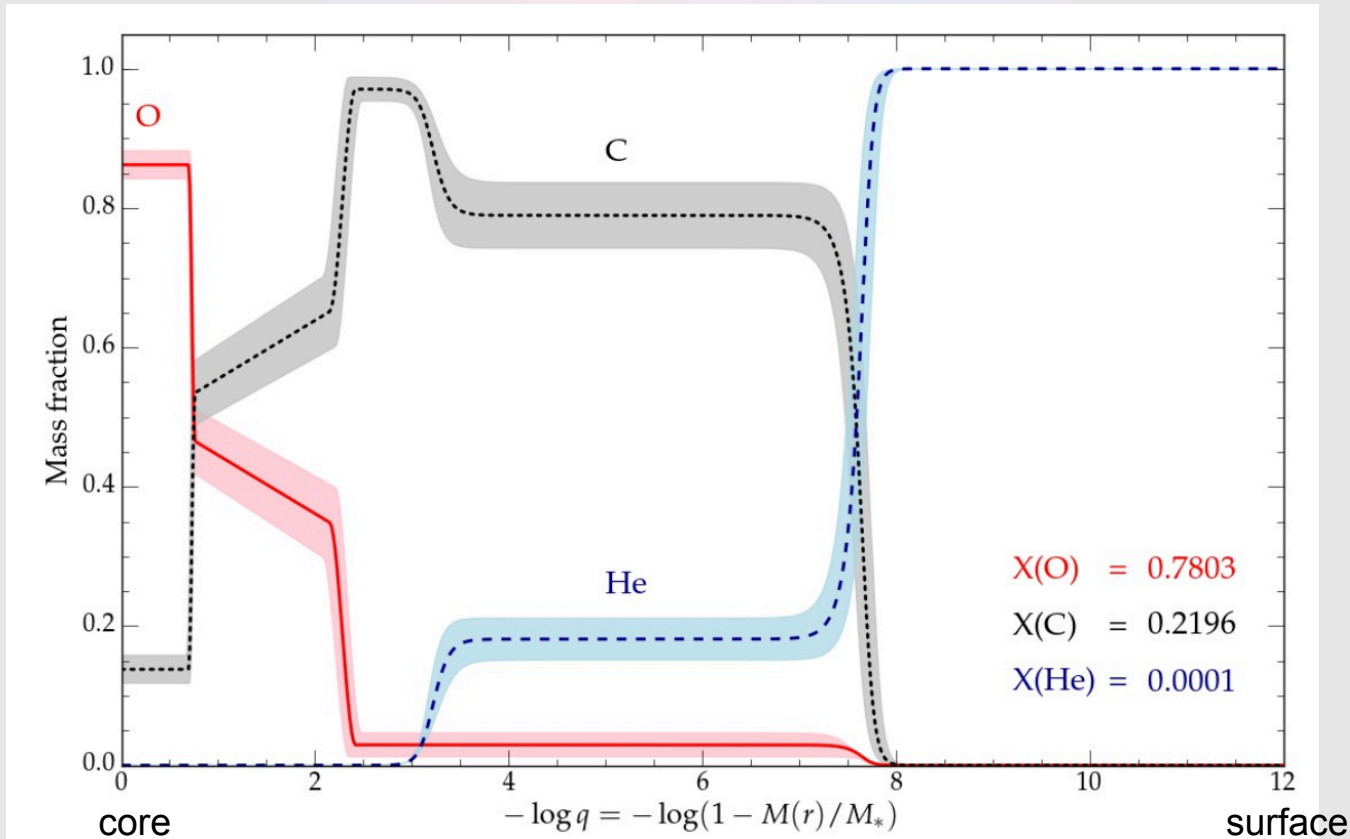
- 23 months of *Kepler* high-precision observations (0.6 nHz)
- 8 observed independent modes, 143-376 s
- Spectroscopy:  $T_{\text{eff}}=29,360\pm 780$  K,  $\log g=7.89\pm 0.05$
- Parametrized models for DB stars: ex. He profile parametrization:



Giammichele et al.

# The example of the V777Her star KIC08626021 (Giammichele et al.)

- Fit to the 8 periods *at the precision of the observations* ( $S^2 \sim 10^{-15}$ )
- Inferred chemical profile:



Giammichele  
et al.  
(submitted)

Higher central and total O abundance and bigger core  
than predicted from stellar evolution

# The example of the V777Her star KIC08626021 (Giammichele et al.)

**Table 1 | Derived properties of KIC08626021**

Quantity	Estimated value
$\log g$ (cm s <sup>-2</sup> )	$7.917 \pm 0.009$
$T_{\text{eff}}$ (K)	$29,968 \pm 150$
$X(\text{He})_{\text{env}}$	$0.18 \pm 0.03$
$\log q_1$	$-7.63 \pm 0.09$
$\log q_2$	$-3.23 \pm 0.05$
$X(\text{O})_{\text{center}}$	$0.86 \pm 0.02$
$\log q_3$	$-0.72 \pm 0.01$
$M(\text{He})/M_*$	$0.0113 \pm 0.0006\%$
$M(\text{C})/M_*$	$21.96 \pm 2.7\%$
$M(\text{O})/M_*$	$78.03 \pm 2.7\%$
$M_*/M_{\odot}$	$0.570 \pm 0.004$
$R_*/R_{\odot}$	$0.0138 \pm 0.0001$
$L_*/L_{\odot}$	$0.137 \pm 0.005$
$M_r^{\text{a}}$	$10.28 \pm 0.03$
$d$ (pc) <sup>b</sup>	$422 \pm 45$
$P_{\text{rot}}$ (h)	$46.3 \pm 2.5$
$V_{\text{eq}}$ (km s <sup>-1</sup> )	$0.36 \pm 0.02$
$J$ (kg m <sup>2</sup> s <sup>-1</sup> ) <sup>c</sup>	$6.59 \pm 0.38 \times 10^{38}$
$J/J_{\odot}$	1/291
$dP/dt_{197}$ (s/s) <sup>d</sup>	14.4 or $2.8 \times 10^{-14}$
$dP/dt_{232}$ (s/s) <sup>d</sup>	15.1 or $2.8 \times 10^{-14}$
$dP/dt_{271}$ (s/s) <sup>d</sup>	15.5 or $3.0 \times 10^{-14}$

Access to stellar radius, mass, luminosity, distance,...

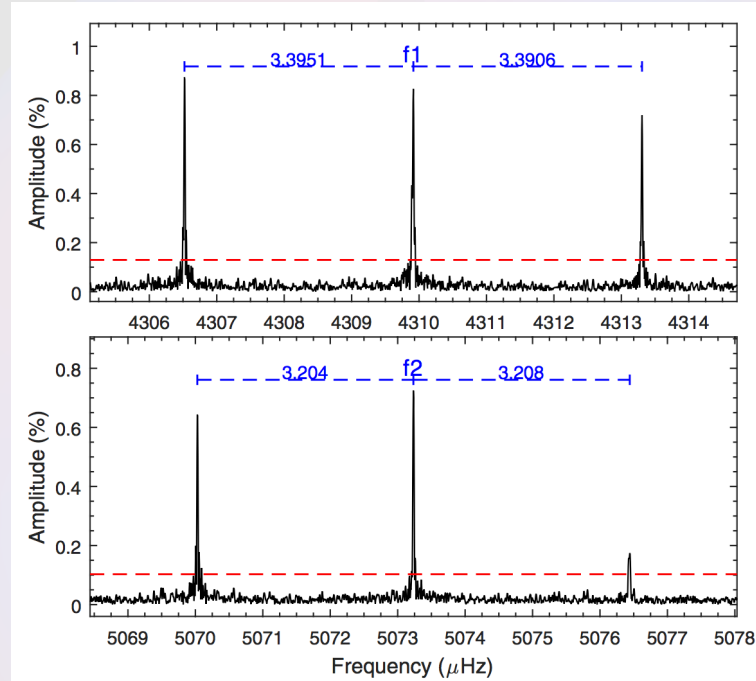
Asteroseismic results important for:

- Constraints for stellar evolution
- WD cosmochronology (GAIA)
  - C/O content
  - « insulating » envelope



# Internal rotation profile in white dwarfs

By exploiting the fine structure of modes, interpreted as *rotational splitting* (rotation lifts the  $(2l+1)$ -fold degeneracy of pulsation modes)



KIC08626021  
(Zong et al. 2016)

How to compute pulsation periods in presence of rotation is a whole field of asteroseismology, but, if Pmodes  $\ll$  Prot:

$$\sigma_{klm} = \sigma_{kl} - m \int_0^R \Omega(r) K_{kl}(r) dr$$

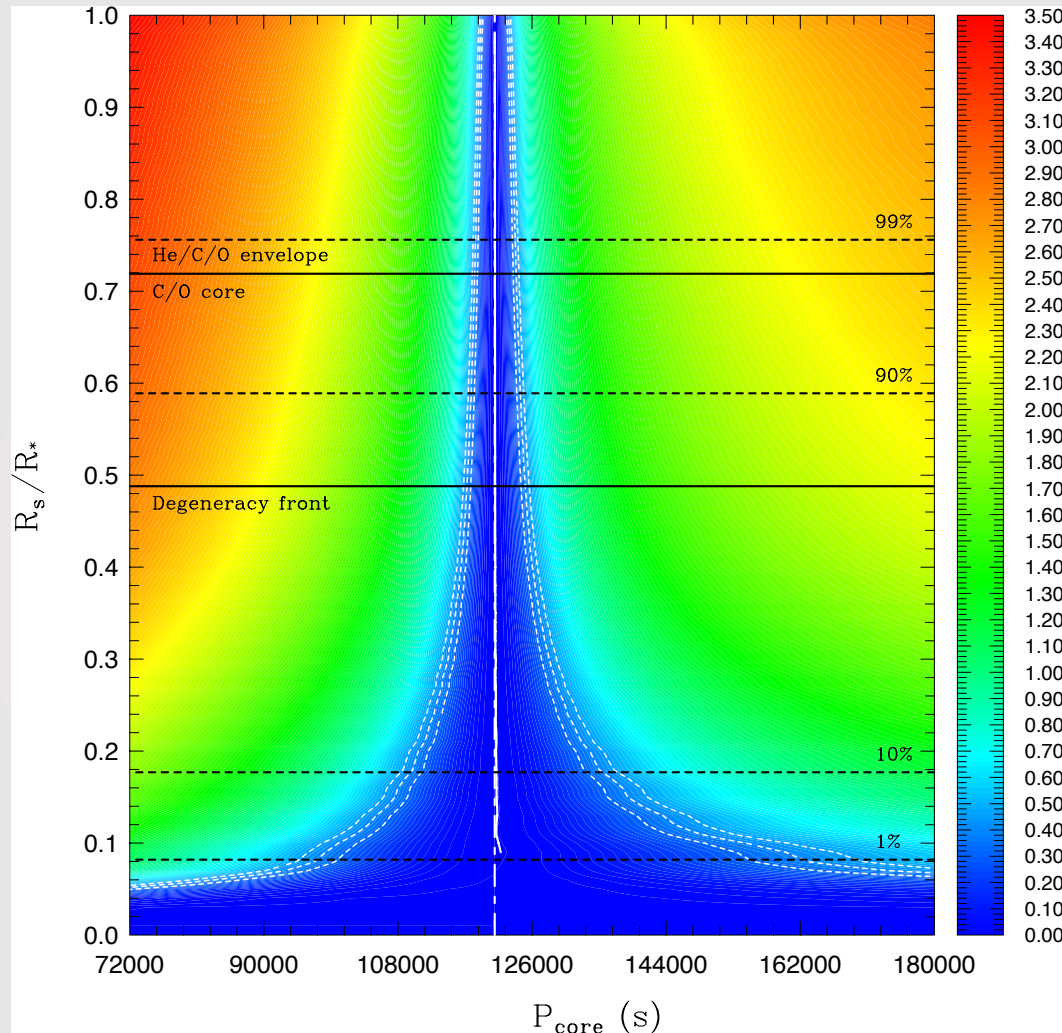
$$K_{kl}(r) = \frac{\xi_r^2 - [l(l+1) - 1]\xi_h^2 - 2\xi_r\xi_h}{\int_0^R [\xi_r^2 + l(l+1)\xi_h^2] \rho r^2 dr} \rho r^2$$

$\xi_r, \xi_h$ : eigenfunctions

# Internal rotation profile in white dwarfs: PG 1159-035 (=GW Vir)

Charpinet et al.  
(2009), Nature

12+5 multiplets



Solid-body rotation over 99% of the stellar mass;  $P_{\text{rot}} = 33.67 \pm 0.24 \text{ h}$

**A pre-WD has already lost **all** of its angular momentum**

## 2. “Non-adiabatic asteroseismology”

Understanding how pulsations are excited, trying to reproduce observed instability strips

General picture: opacity-driven mechanism:

- Don Winget (1981) for ZZ Ceti:

H ionization/recomb. around  $T_{\text{eff}} \sim 12,000$  K

⇒ envelope opacity increase

⇒ strangle the flow of radiation, convection zone develops

⇒ g-modes instabilities

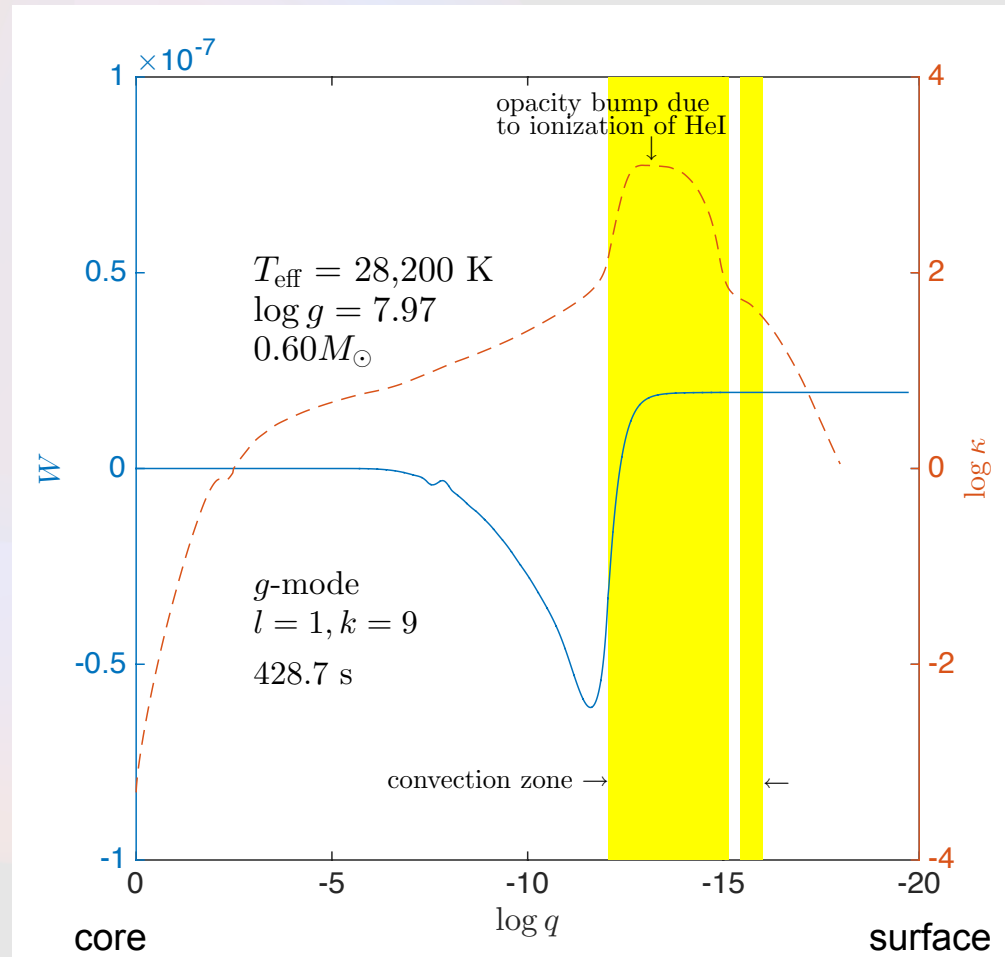
// ELM pulsators (H atmo)

- By analogy, Winget proposed pulsating He-rich, V777 Her white dwarfs:

HeII partial ionization around  $T_{\text{eff}} \sim 30,000$  K

// pre-ELM pulsators (H-He atmo)

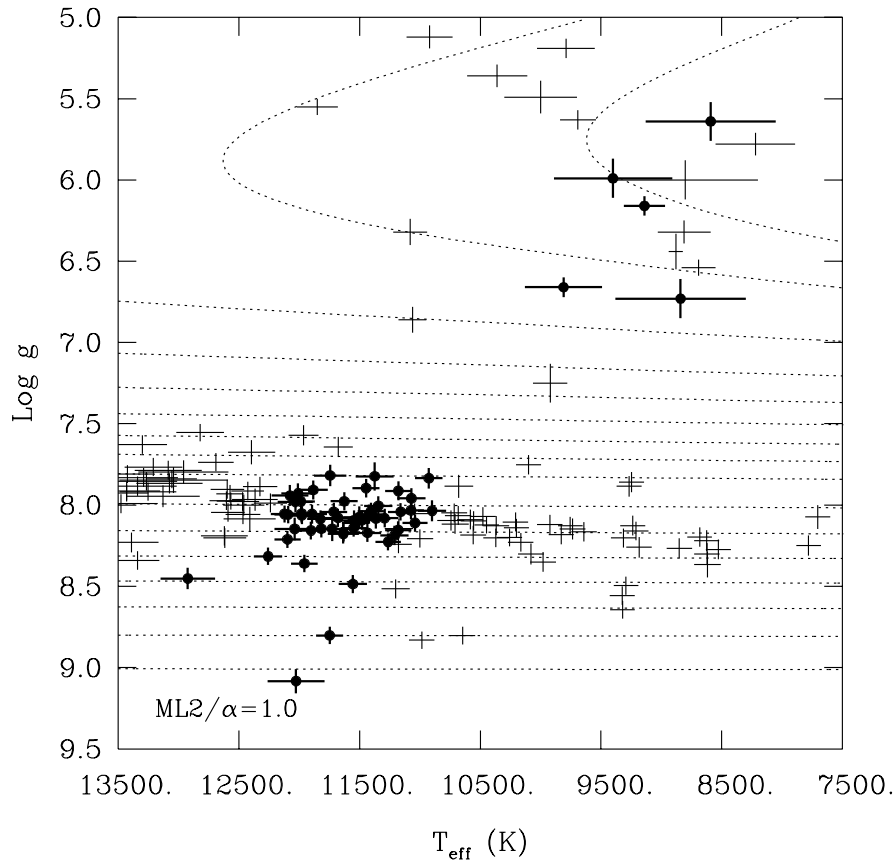
- Partial ionization of K-shell  $e^-$  of C and O for GW Vir, no convection development ( $\kappa$ -mechanism)



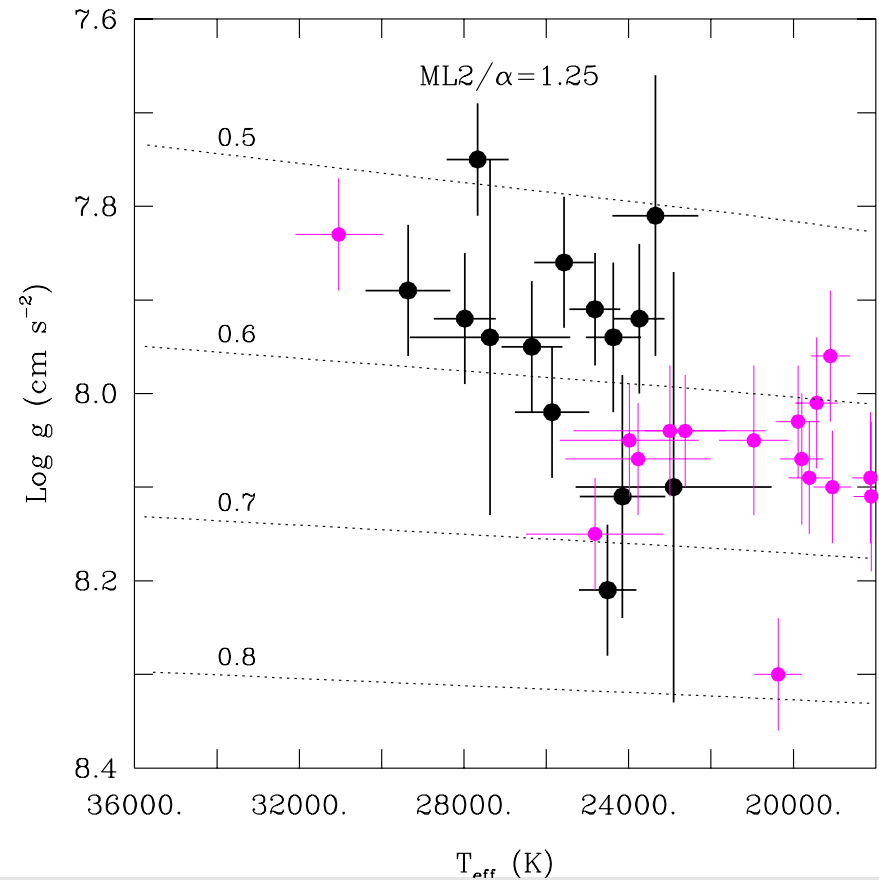
## 2. “Non-adiabatic asteroseismology”

Understanding how pulsations are excited, trying to reproduce observed instability strips

ZZ Ceti & ELM (H-atmo)



V777 Her (He-rich atmo)



What can be learned: convection in WDs (depth, efficiency)

## 2. “Non-adiabatic asteroseismology”

---

Understanding how pulsations are excited, trying to reproduce observed instability strips

**Empirical strips** (e.g. group of P. Bergeron, WET collaboration):

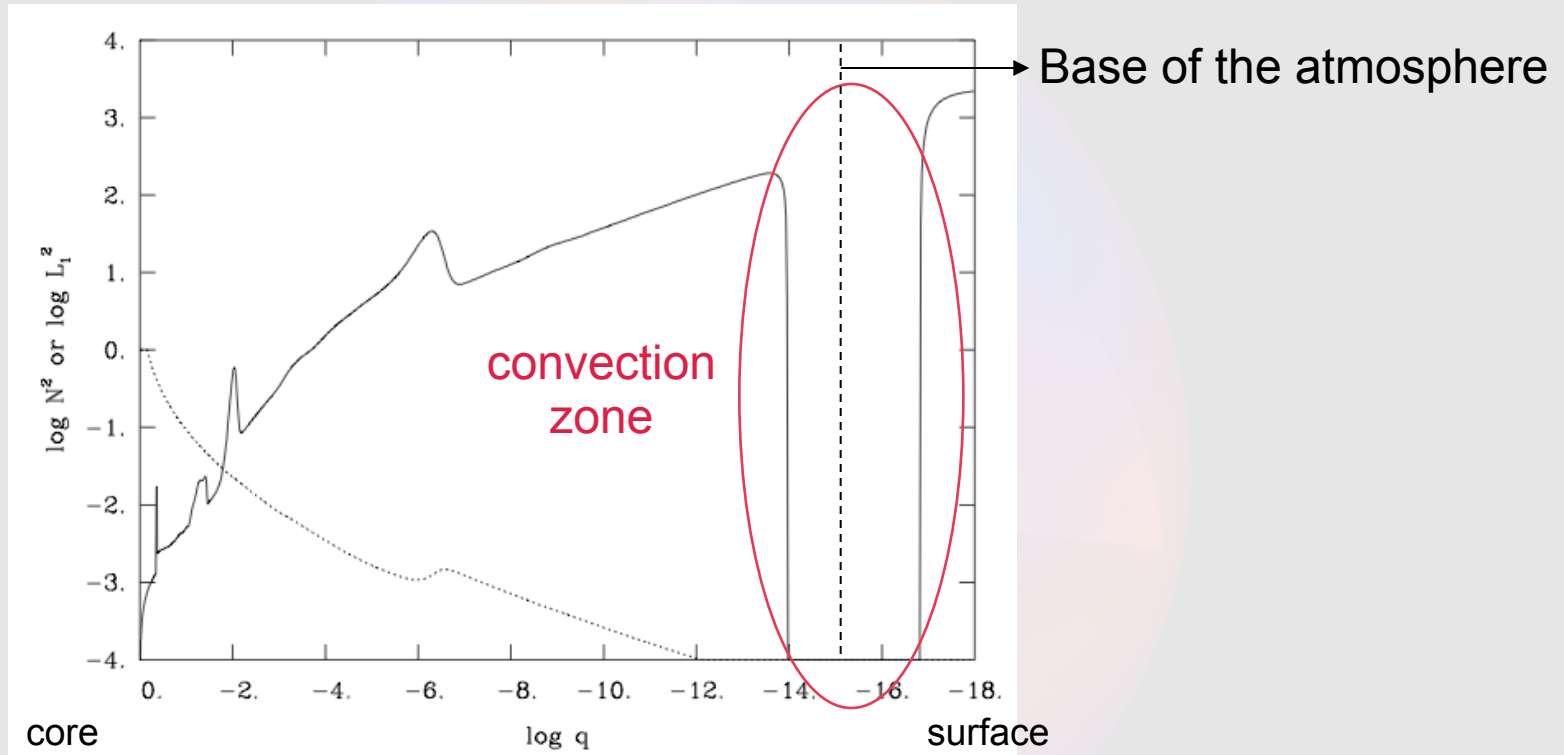
- Decades of work to reach a homogeneous view of the empirical strips (high-quality photometric & spectroscopic observations + high-quality model atmospheres)
- In both cases: most likely a **pure** strip
- Efficiency of convection in *atmospheres*:  $\alpha/\text{MLT}=0.6$  (ZZ Ceti) and  $\alpha/\text{MLT}=1.25$  (V777Her)

**Theoretical strips** (e.g. Van Grootel et al.):

- $T_{\text{conv}} \ll$  Periods of pulsations (blue edge), or  $T_{\text{conv}} \lesssim$  Periods (later in cooling)  
⇒ need of **Time-Dependent Convection (TDC)**, as in MAD code (Dupret, Liège)
- TDC still fails to reproduce the red edge: energy leakage argument (mode are no longer reflected back by the atmosphere)
- **1D** stellar models with, for upper layers, same T stratification than full 1D model atmospheres

# Modeling details

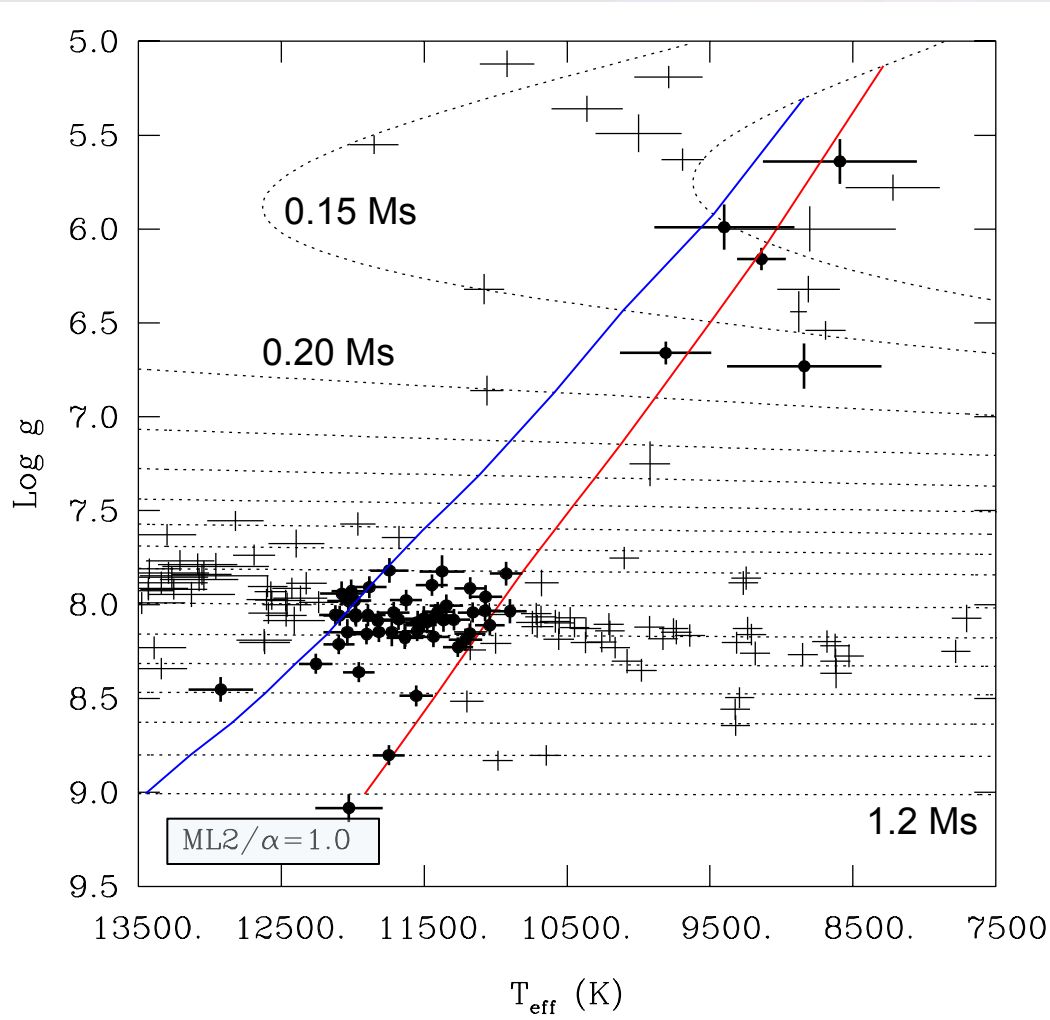
Detailed modeling of the superficial layers:



Our structure models have the same T stratification as the complete (1D) model atmospheres  
⇒ "feedback" of the convection on the global atmosphere structure

# Theoretical instability strip for ZZ Ceti and ELM DA pulsators

⊕ non variable (<10mmag); ● pulsator



— TDC blue edge

— Red edge  
(energy leakage)

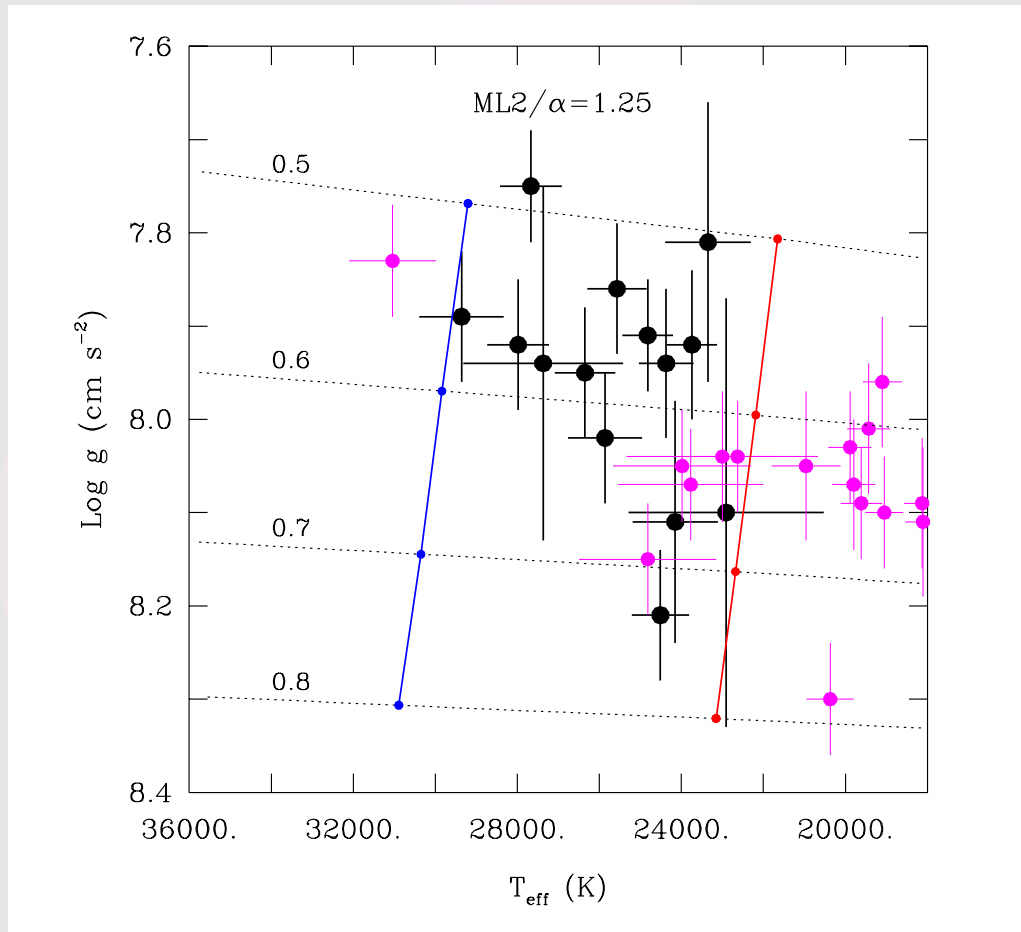
**Homogeneous** atmospheric parameters (here  $ML2/\alpha = 0.6$ )

Structure ( $ML2/\alpha = 1.0$ ) and atmospheric ( $ML2/\alpha = 0.6$ ) MLT calibrations are dependent

Van Grootel et al. (2013)

# Theoretical instability strip for V777Her stars

Van Grootel et al.  
(2017)



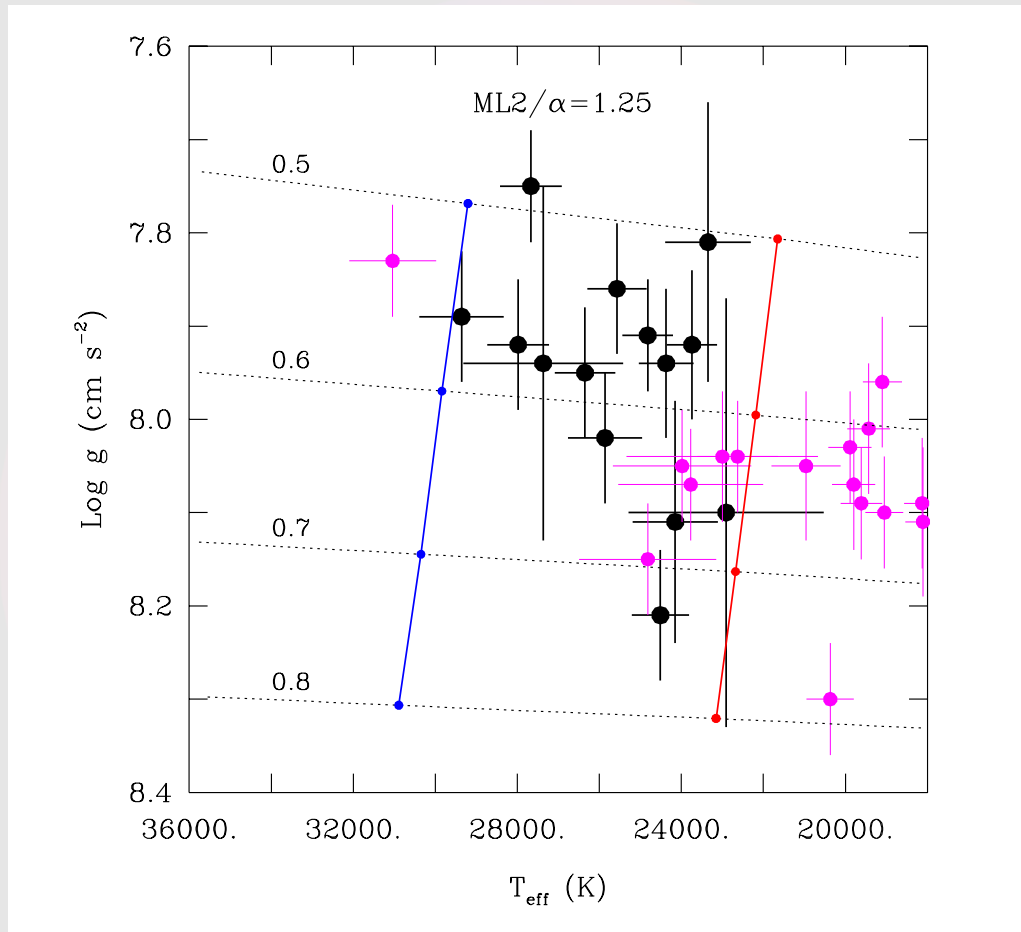
- pulsator
- non variable

Structure and  
atmosphere:  
ML2/α = 1.25



# Theoretical instability strip for V777Her stars

Van Grootel et al.  
(2017)



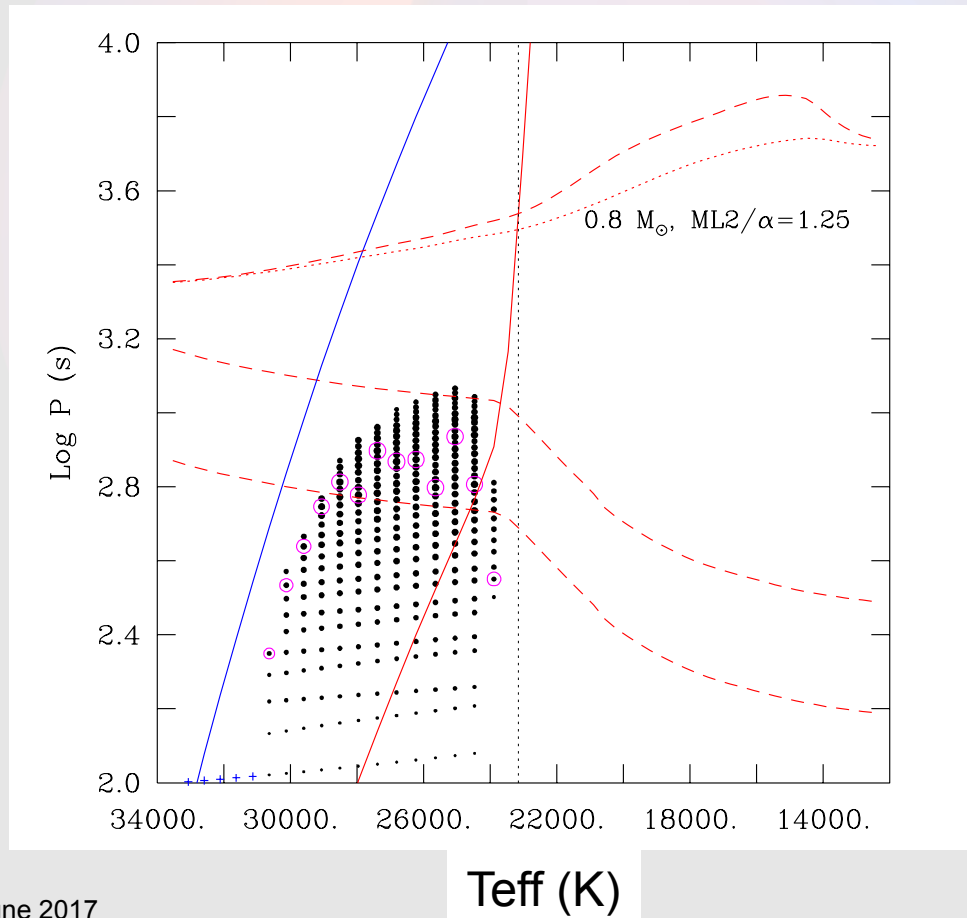
- BUT:**
- Red edge leakage *slightly* too cool (?)
  - Kepler observations: 2 pulsators hotter than blue edge !

# Possibilities for improvement ?

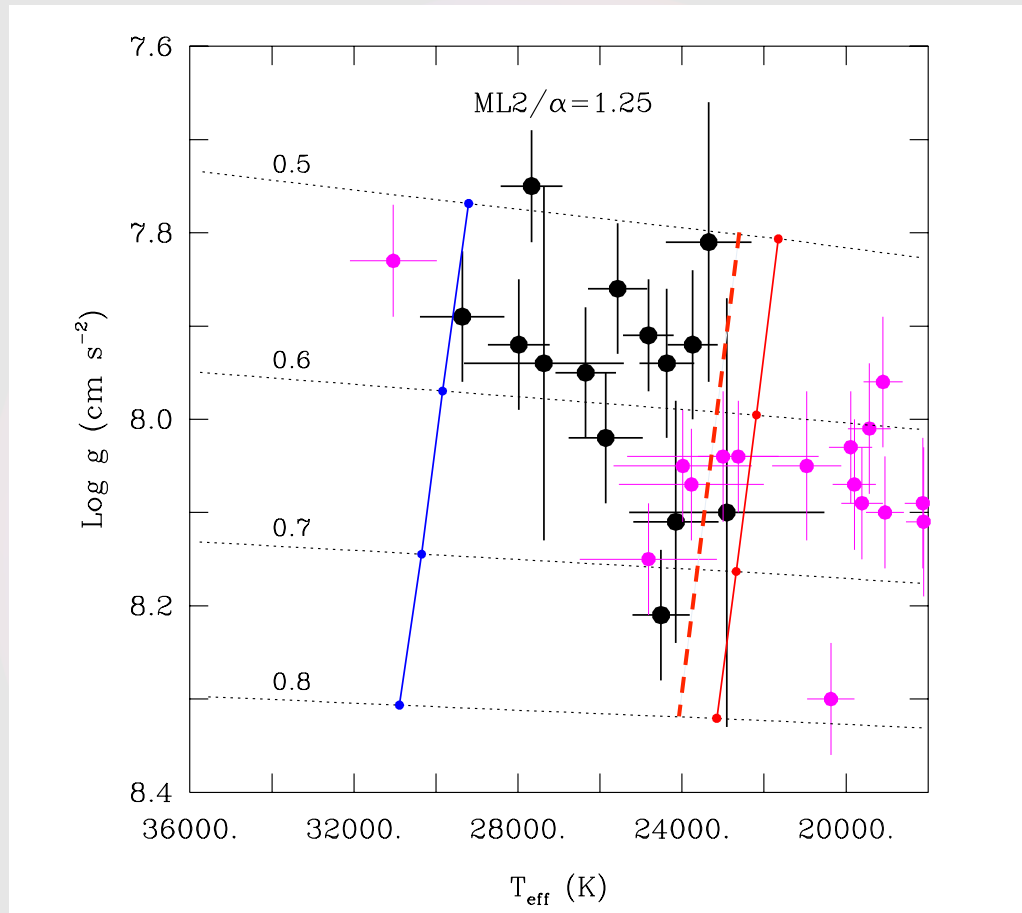
- TDC **with** turbulent pressure perturbations

$$\frac{\delta P_t}{P_t} = \frac{\delta \rho}{\rho} + 2 \frac{\overline{\delta V_r}}{V_r}$$

- With  $\delta P_t=3$ :



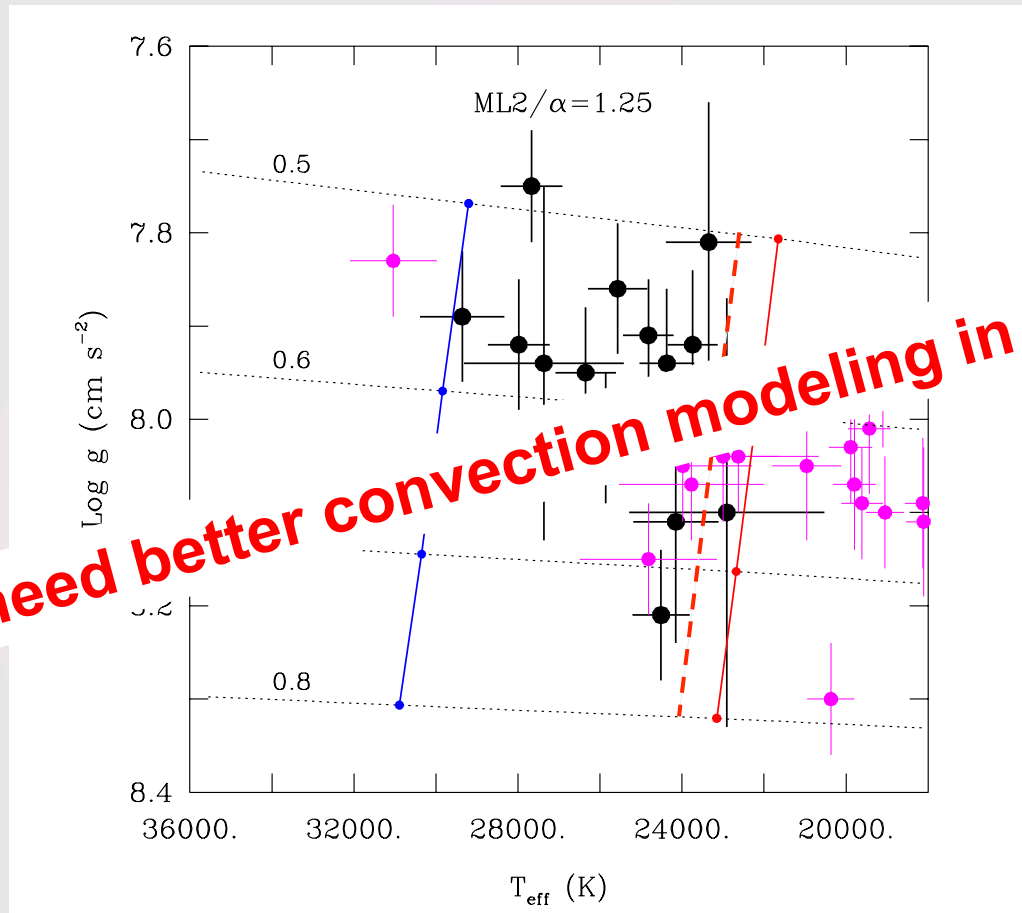
# Theoretical instability strip for V777Her stars



Red edge « with turbulent pressure »:  $\sim 500$  K hotter than red edge leakage

But  $3\delta Pt$  is not physically realistic. Mimic other components of the Reynolds stress tensor ( $Pt = rr$  component), i.e. **turbulent viscosity** ?

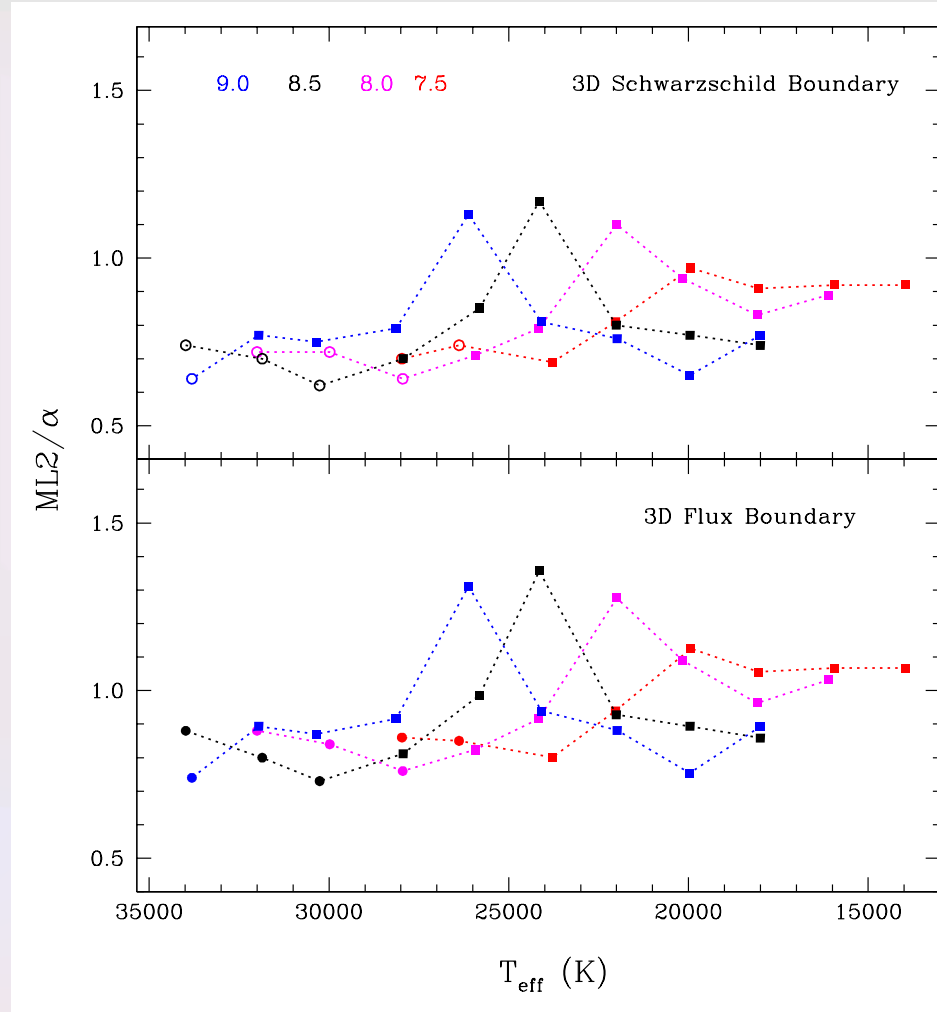
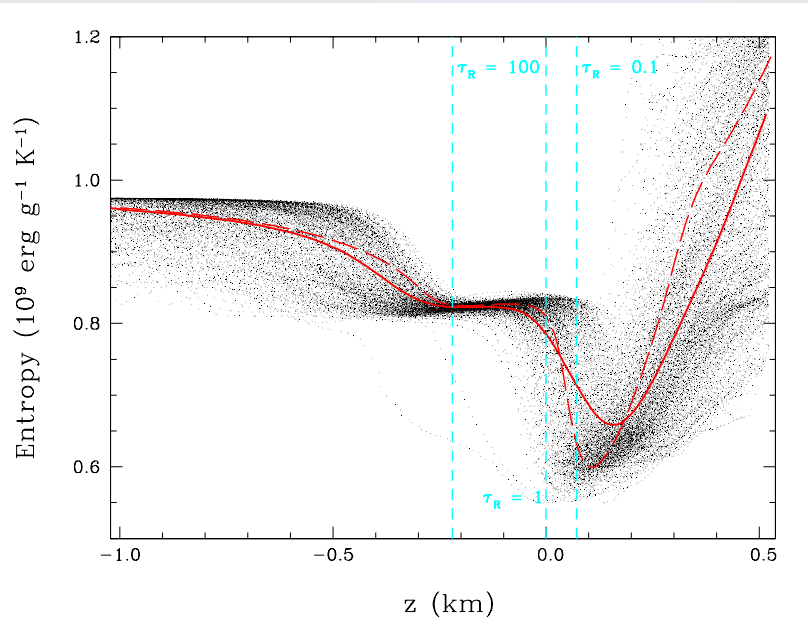
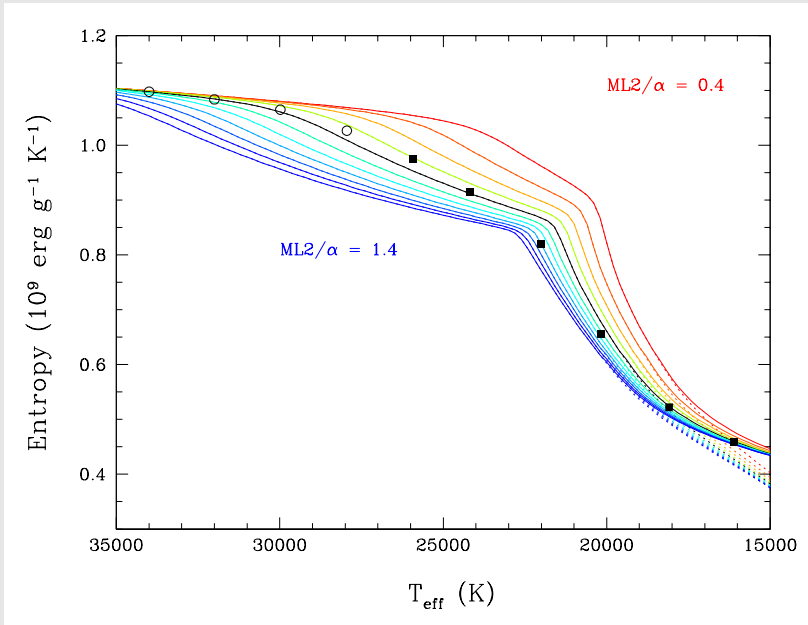
# Theoretical instability strip for V777Her stars



Red edge « with turbulent pressure »:  $\sim 500$  K hotter than red edge leakage

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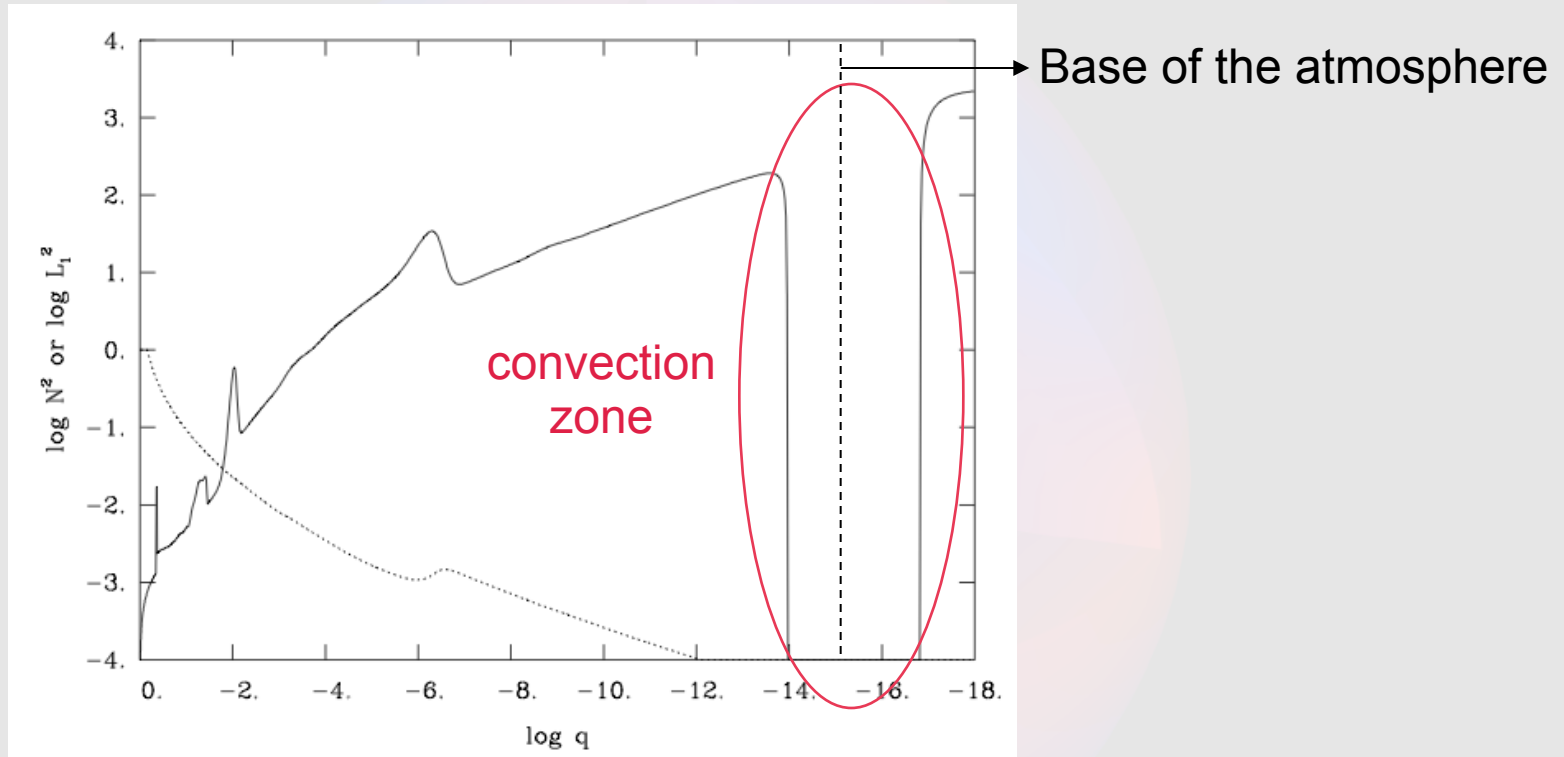
# 3D simulations for DA and DB white dwarfs (P.E. Tremblay)



See also poster of E. Cukanovaite

# Modeling details

Detailed modeling of the superficial layers:



Our structure models have the same T stratification as the complete (1D) model atmospheres  
⇒ "feedback" of the convection on the global atmosphere structure

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- IV. **What do we need for white dwarf asteroseismology**

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To improve further equilibrium structures used for asteroseismology, including for WD cosmochronology:

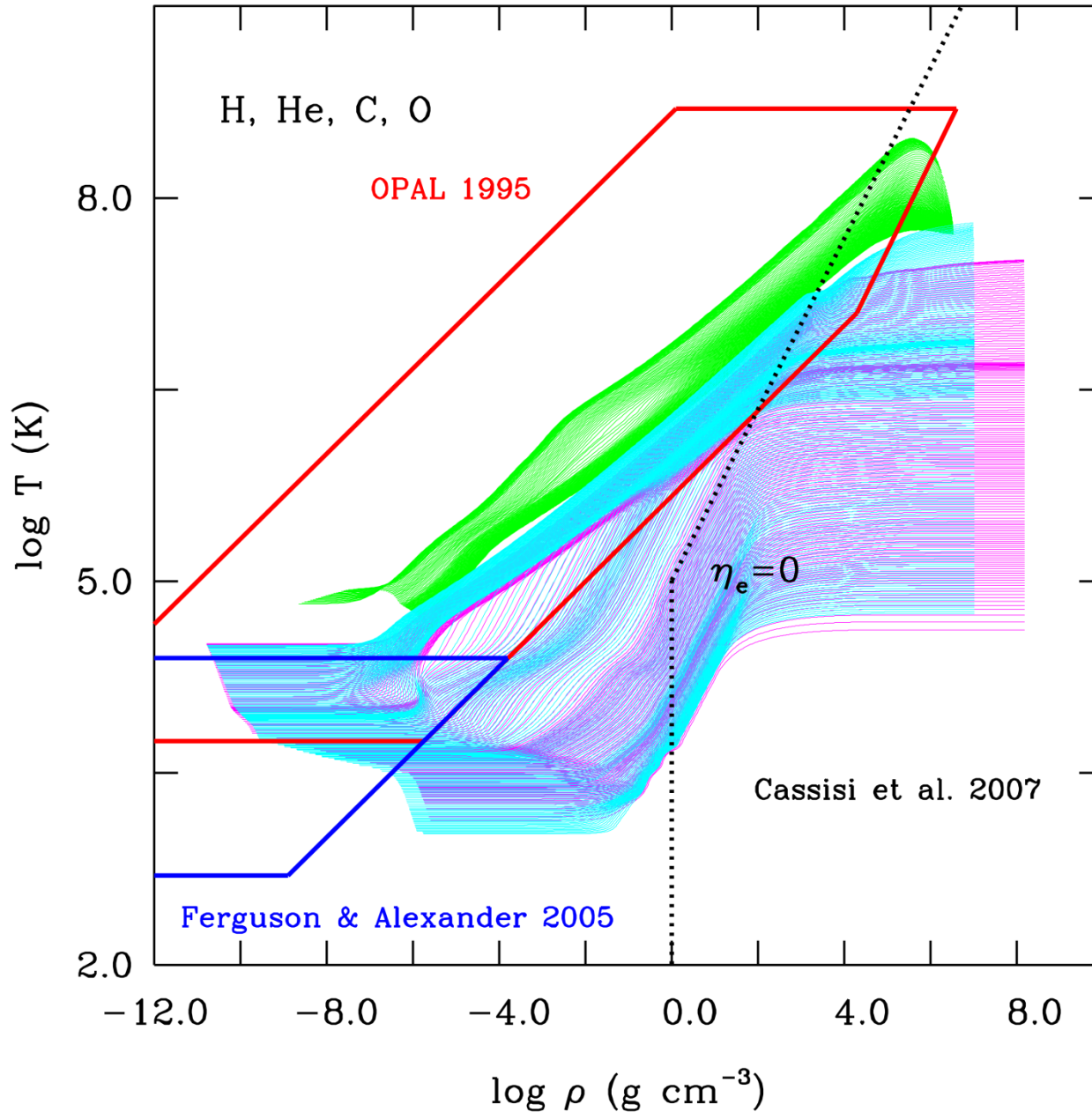
- Extended EOS
- Radiative & conductive opacities

To understand better driving/damping pulsations in WDs:

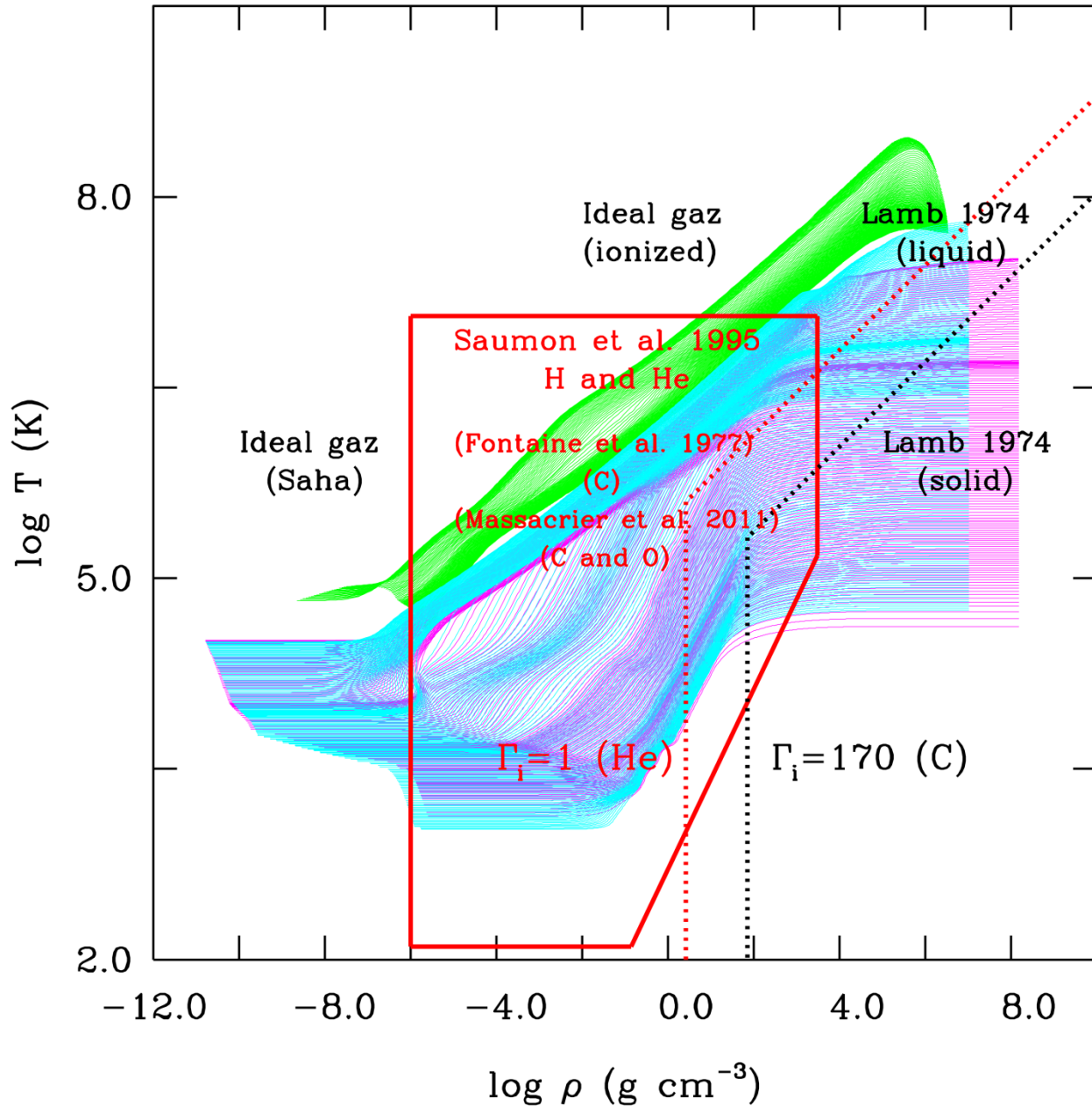
- Patched 1D models + improved treatment for interaction between convection and pulsations by including turbulent viscosity (work in progress)



# Radiative and conductive opacities



# Equation of state



# Conclusions

---

## What we can learned from WD seismology:

- **Quantitative asteroseismology:**
  - Global parameters
  - Internal layering and chemical stratification
  - Internal rotation profile
- **Non-adiabatic asteroseismology:**
  - how pulsations are driven
  - how convection behaves in WD

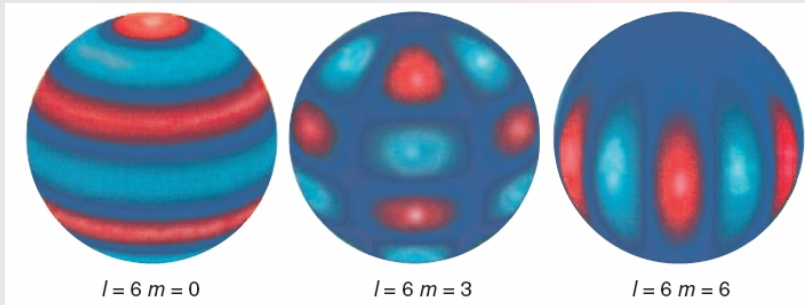
## What do we need from WD seismology:

- About physics: EOS & opacities
- Patched 1D models + improved treatment for interaction between convection and pulsations (work in progress)

# Theoretical grounds of asteroseismology

- From the linearized equations of hydrodynamics (small perturbations to equilibrium):

$$f'_{klm}(r, \theta, \phi, t) = f'_{kl}(r) Y_l^m(\theta, \phi) e^{i\sigma_{kl}t} \quad (f' = p, v, T, \dots)$$



- eigenfunction  $f'(r)$  (radial dependence)
- oscillation eigenfrequency  $\sigma_{kl}$  (temporal dep.)
- spherical harmonics  $Y_l^m$  (angular dep.)

- Lamb and Brunt-Väisälä frequency

$$L_l^2 = \frac{l(l+1)c_s^2}{r^2}$$

$$N^2 = \frac{g^2 \rho}{p} \frac{\chi_T}{\chi_\rho} (\nabla_{\text{ad}} - \nabla + B)$$

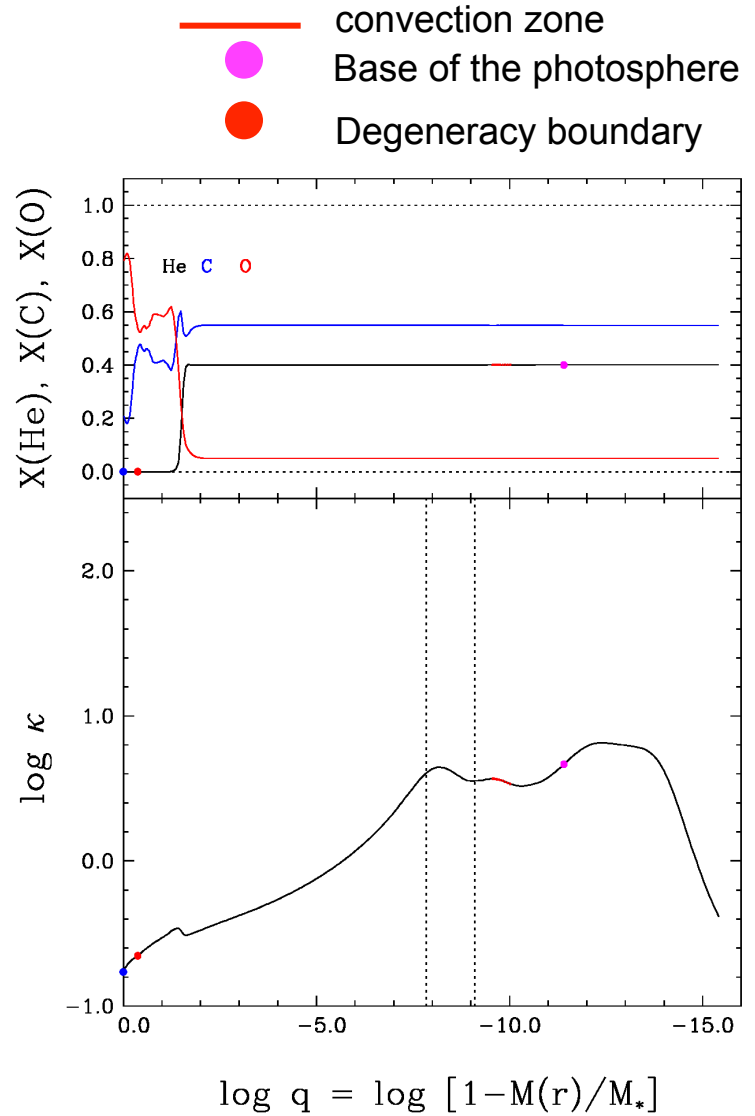
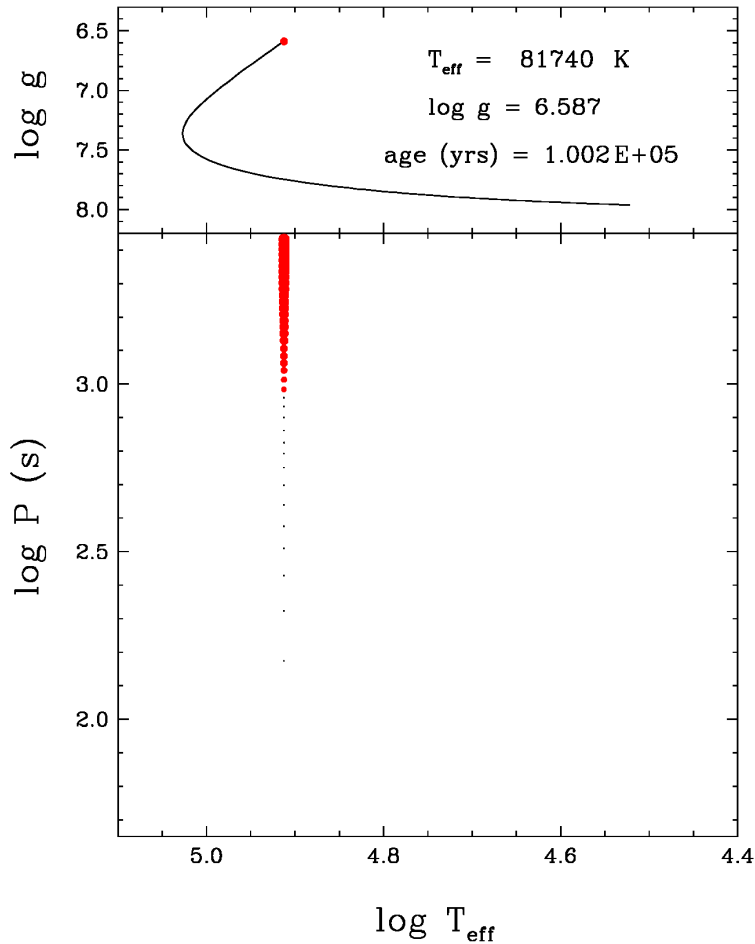
Oscillations are excited and propagate in some regions, and are evanescent in others

- if  $\sigma^2 > L_l^2, N^2$ : **p-modes** (restoring force : pressure), acoustic waves
- if  $\sigma^2 < L_l^2, N^2$ : **g-modes** (restoring force : buoyancy), gravity waves

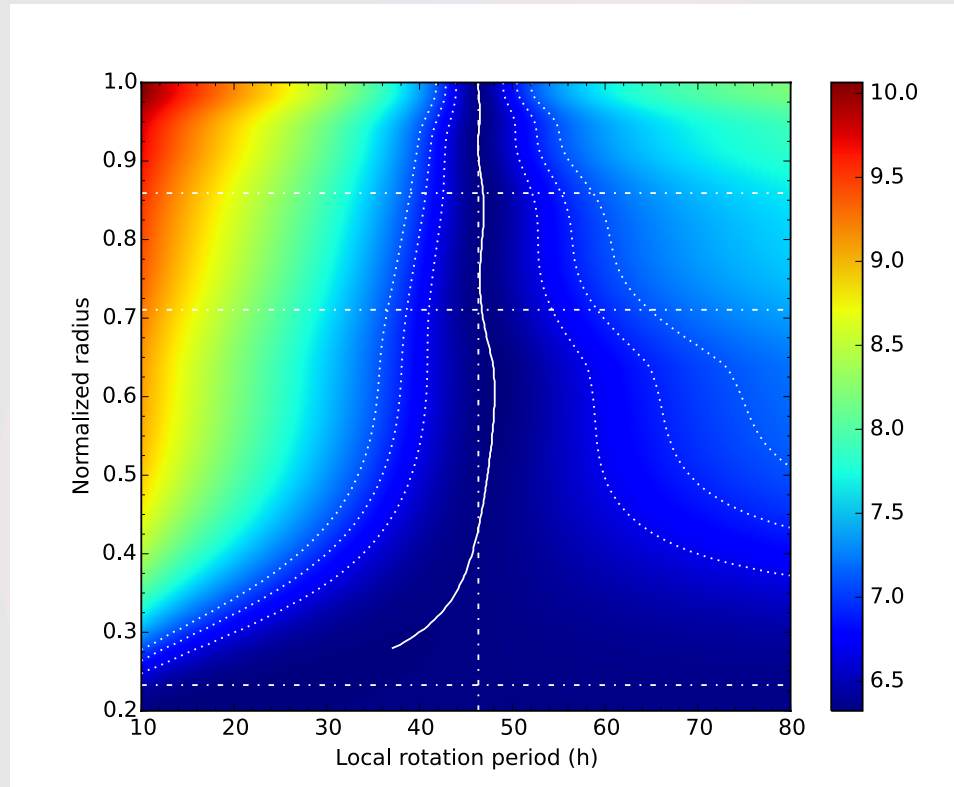
# Driving and damping of pulsations in GW Vir white dwarf

Courtesy: G. Fontaine

● Bipping: pulsations are driven



# Internal rotation profile in white dwarfs: KIC08626021



(Giammichele et al.)

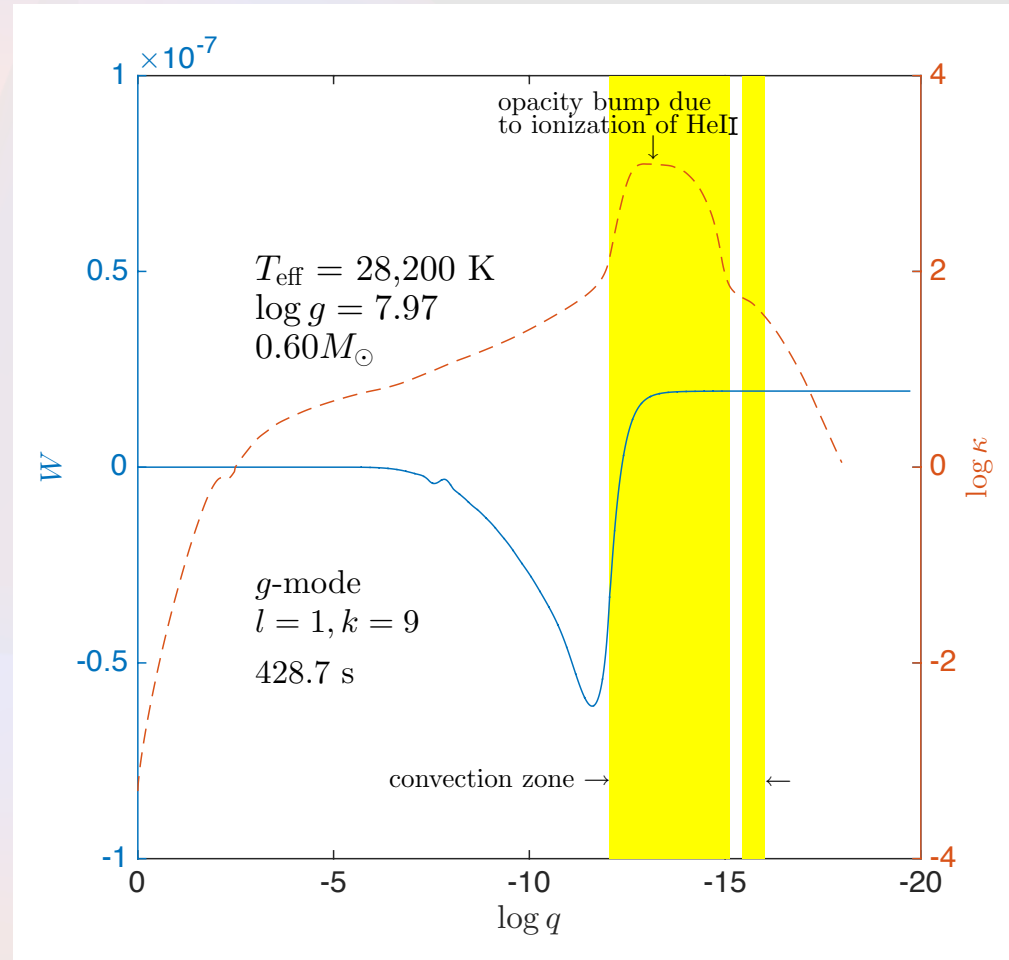
Pulsation modes probe  $\sim 70\%$  of the stellar radius (81% of the stellar mass)

Solid-body rotation down to  $0.3 R_*$ ,  $P_{\text{rot}} = 46.34 \pm 2.54$  h

# Driving mechanism for pulsations

## Common point: opacity-driven mechanism

- Don Winget (1981) for ZZ Ceti:  
**H ionization/recomb. around  $T_{\text{eff}} \sim 12,000$  K**  
⇒ envelope opacity increase  
⇒ strangle the flow of radiation, convection zone develops  
⇒ g-modes instabilities  
**// ELM pulsators (H atmo)**
- By analogy, Winget proposed pulsating He-rich, V777 Her white dwarfs:  
**HeII partial ionization around  $T_{\text{eff}} \sim 30,000$  K**  
**// pre-ELM pulsators (H-He atmo)**
- **Partial ionization of K-shell  $e^-$  of C and O** for GW Vir, no convection development ( $\kappa$ -mechanism)



## Energy leakage argument

- For the red edge (long-standing problem):

based on the idea of Hansen, Winget & Kawaler (1985): red edge arises when

$$\tau_{\text{th}} \sim P_{\text{crit}} \propto (l(l+1))^{-0.5}$$

( $\tau_{\text{th}}$  : thermal timescale at the base of the convection zone),

which means the mode is no longer reflected back by star's atmosphere