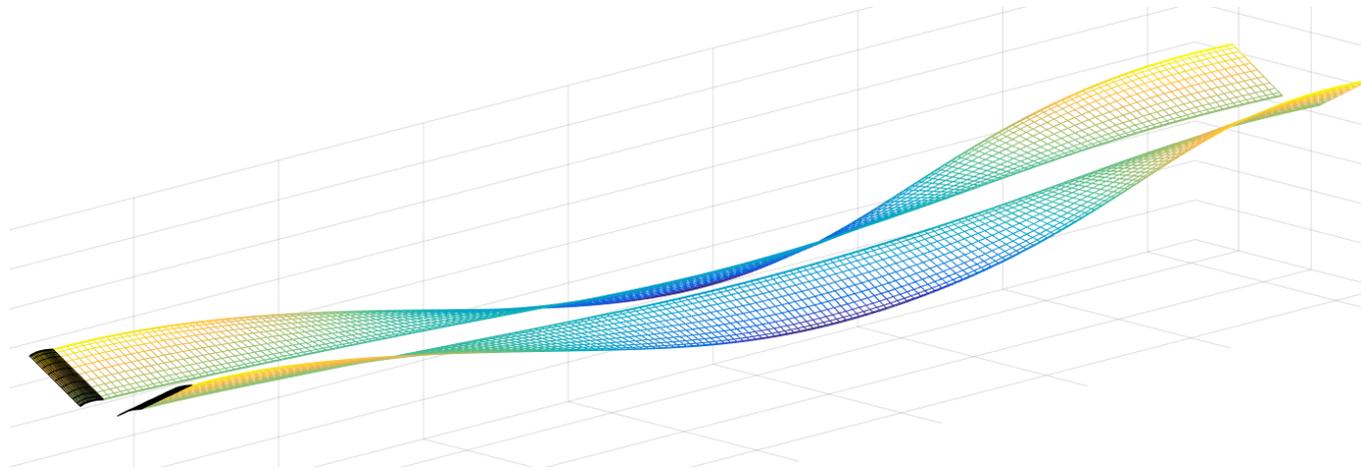


Modeling of aerodynamic forces in flapping flight with the UVLM



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2nd Master in aerospace engineering

Academic year 2014-2015

Objective

Compare two methods used to compute the aerodynamic forces for the UVLM

- Validity
- Convergence

Motivation

Verify and extend the results presented in an article* for flat plates

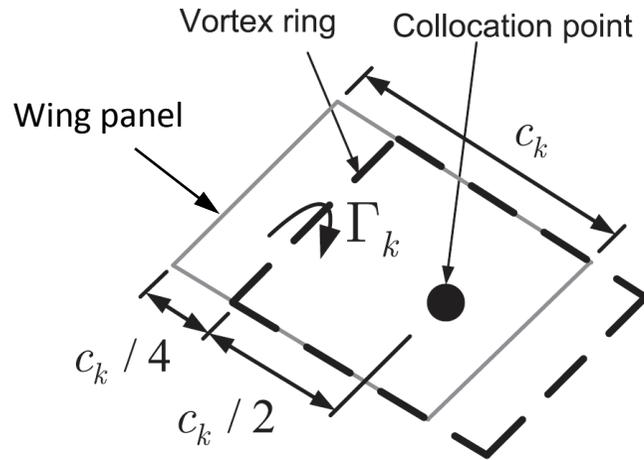
Contents

Test cases (harmonic pitching and plunging)

Flapping with pitching

*Simpson, Palacios and Murua, *Induced-drag calculations in the unsteady vortex lattice method*.
AIAA Journal, 51(7):1775-1779, July 2013.

Unsteady Vortex Lattice Method

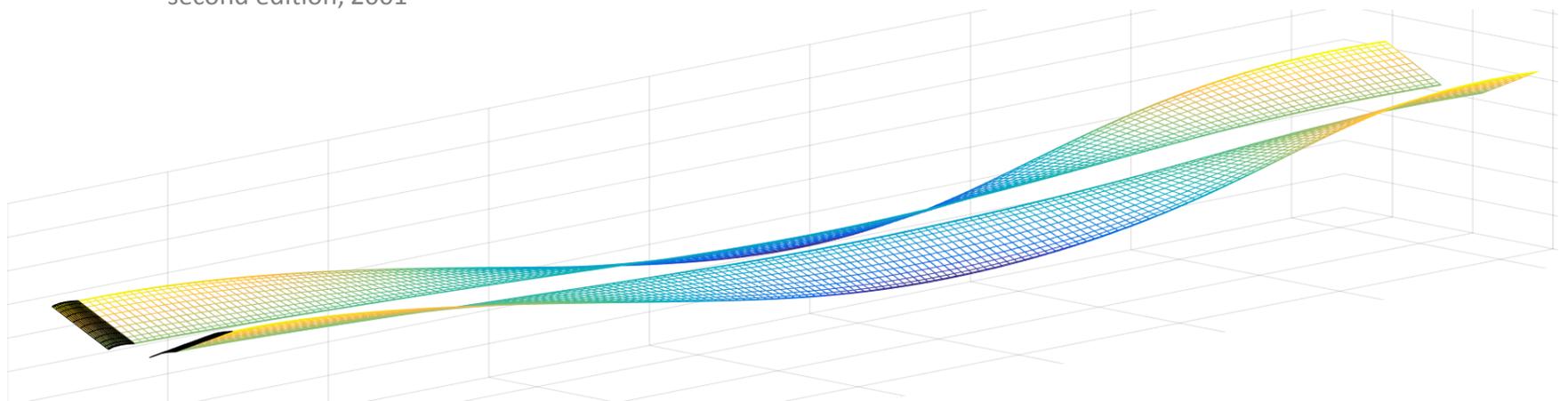


Source: Katz and Plotkin, *Low-Speed Aerodynamics*. Cambridge University Press, second edition, 2001

Hypotheses

- Sub-sonic
- Non-viscous
- Incompressible
- Irrotational
- **Attached flow**

- Thin airfoil



Katz method

- Bernoulli's equations
 - Small angle assumption
- Velocities at collocation points
- Need correction for induced-drag

Joukowski method

- Joukowski's equations
- Velocities at mid point of vortex segments
- No correction required

Test cases - Introduction

Geometry

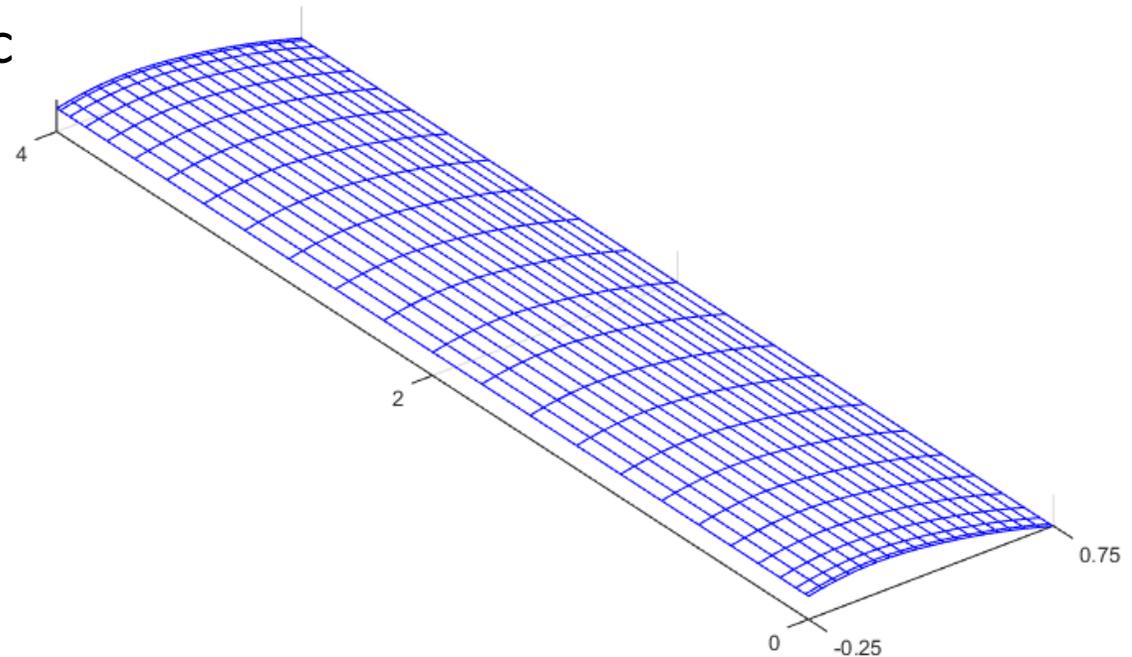
- 2D or 3D
- Cambered or symmetric

Wings

- Perfectly rectangular
- $AR_{2D} = 4000$
- $AR_{3D} = 4$

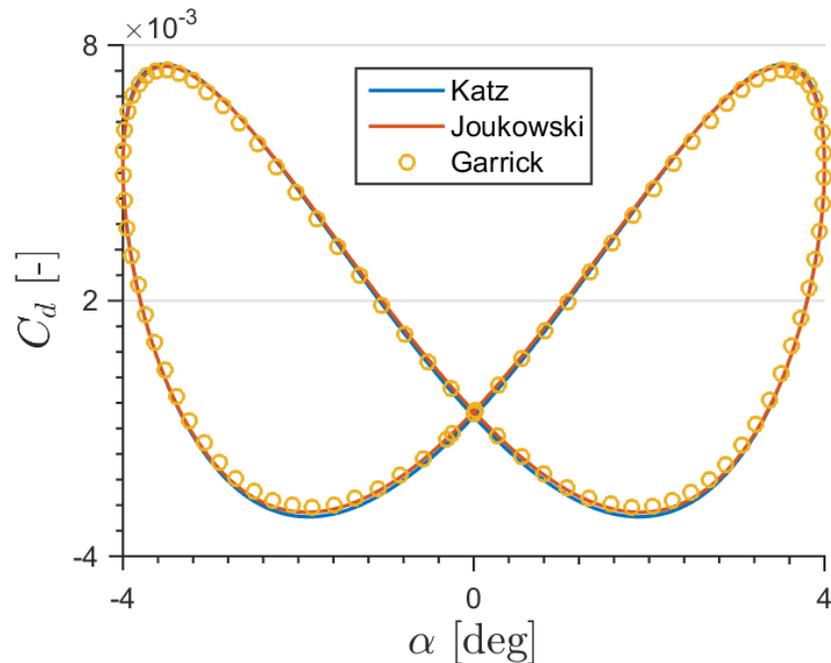
Kinematics

- Pitching: $\alpha = \bar{\alpha}_p \sin(ks)$
- Plunging: $h = \bar{h} \cos(ks)$



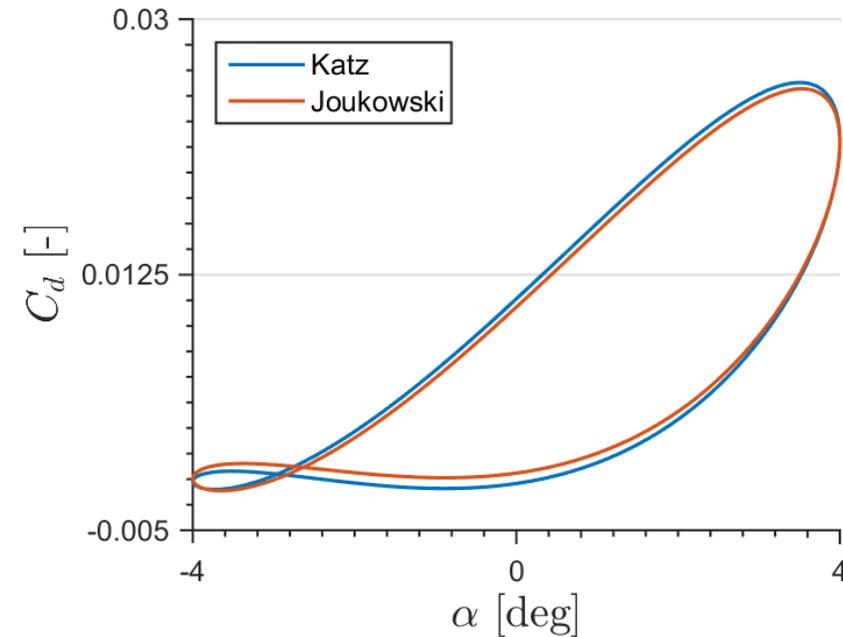
Test cases – Pitch 2D

NACA 0012



- Similar results for both methods
- Good approximation of the analytical solution

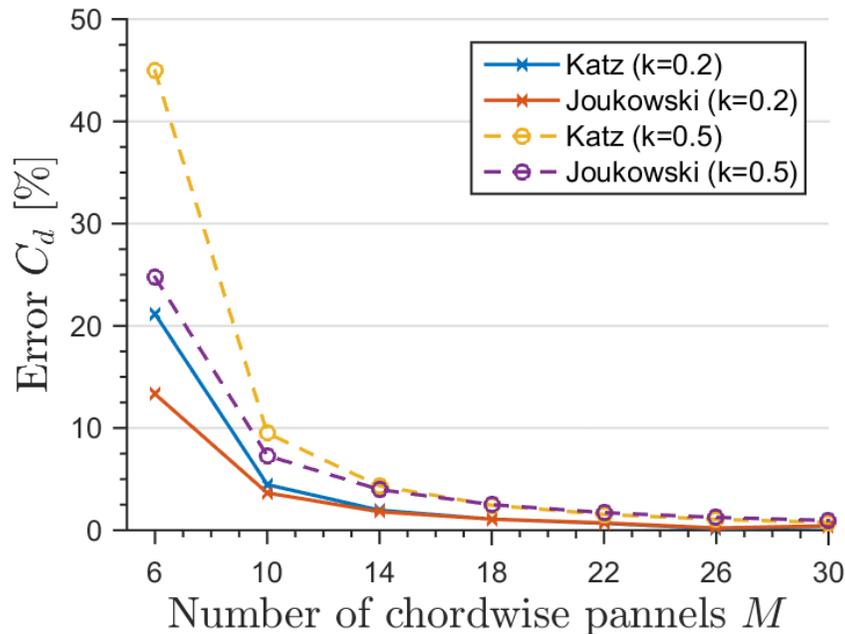
NACA 6409



- Small differences between the two methods

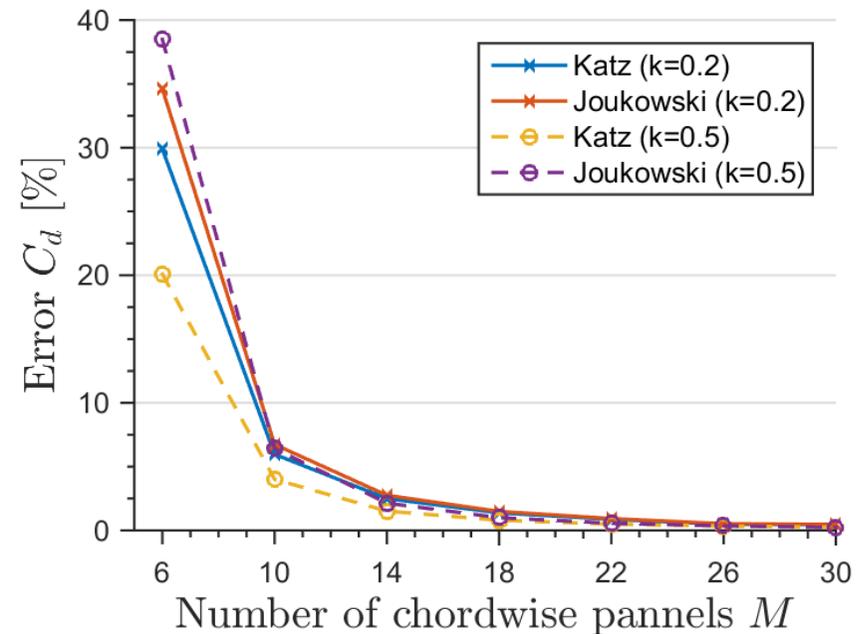
Test cases – Pitch 2D

NACA 0012



- Joukowski converges slightly better
- Convergence reached for the same M

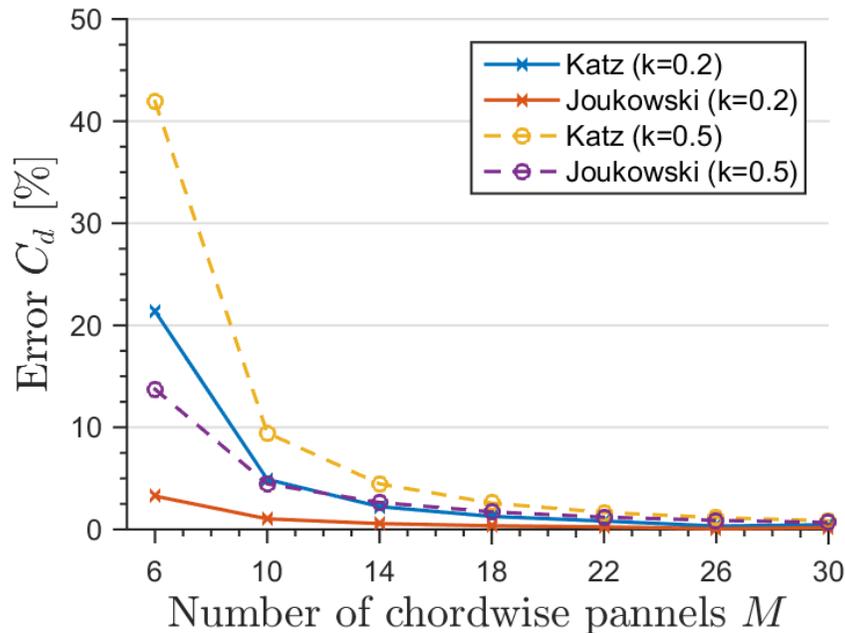
NACA 6409



- Convergence rate nearly the same

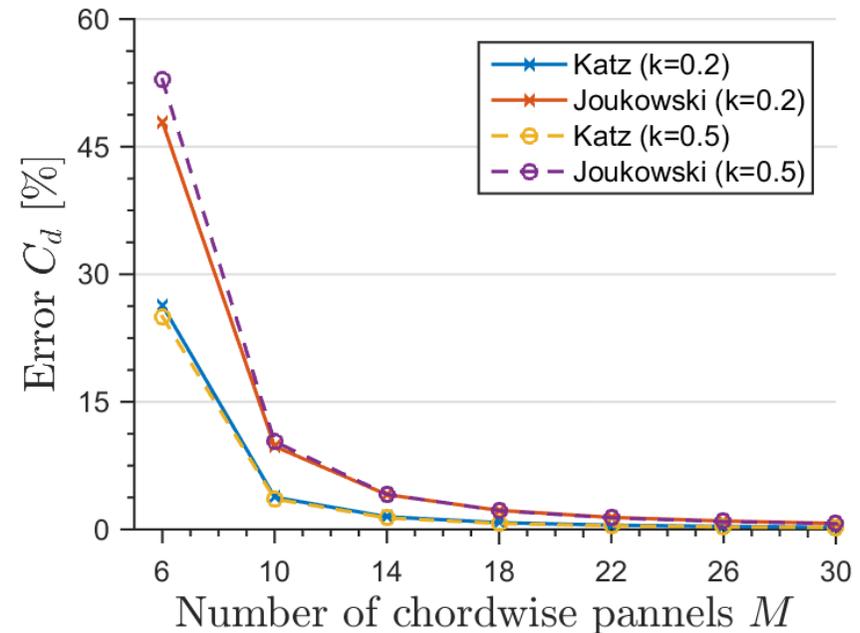
Test cases – Pitch 3D

NACA 0012



- Joukowski converges faster

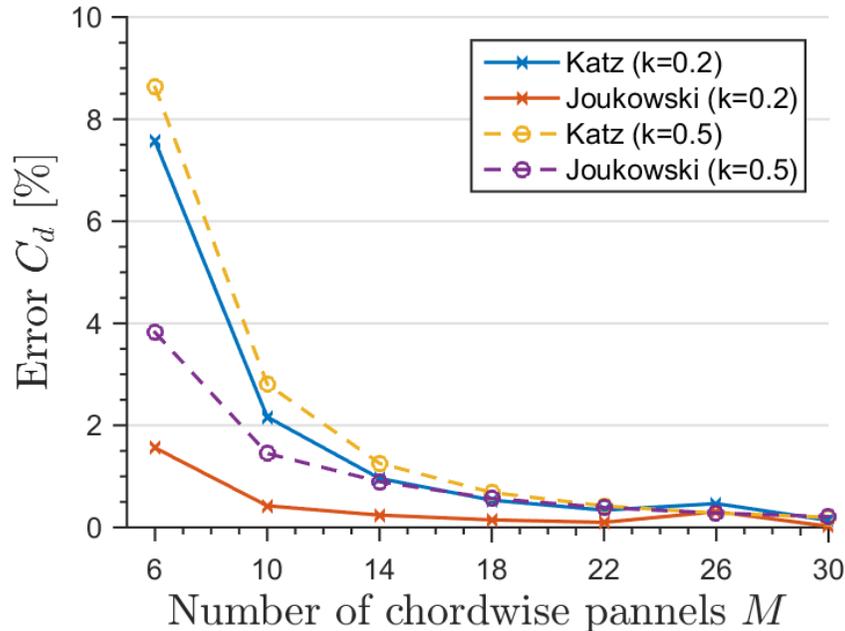
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- Katz converges faster
- No influence of the frequency

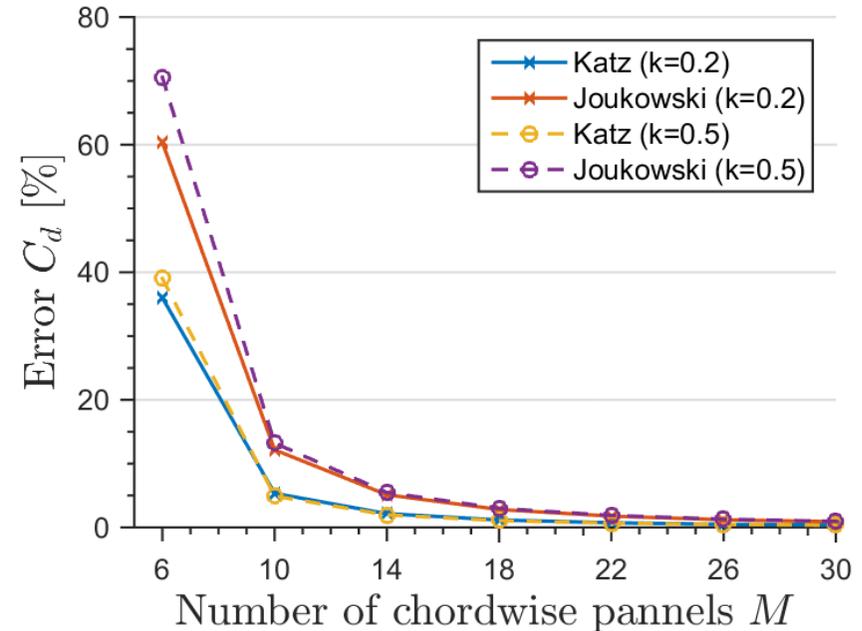
Test cases – Plunge 3D

NACA 0012



- Joukowski converges faster

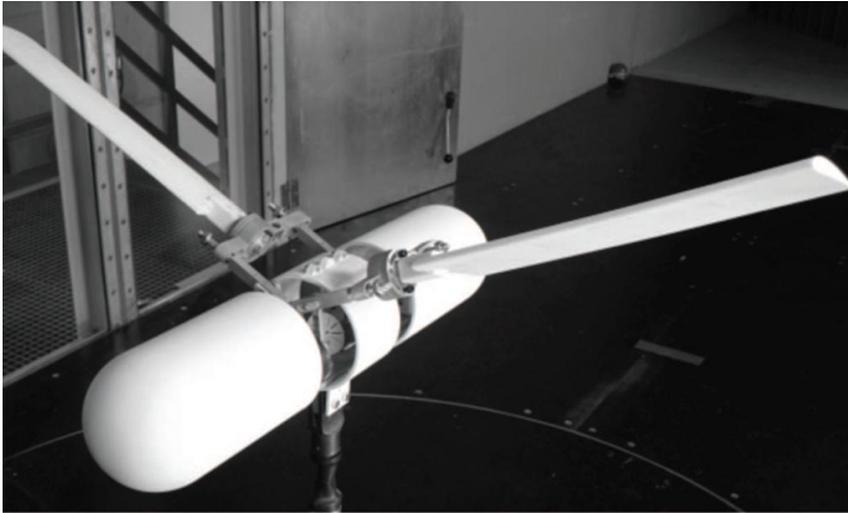
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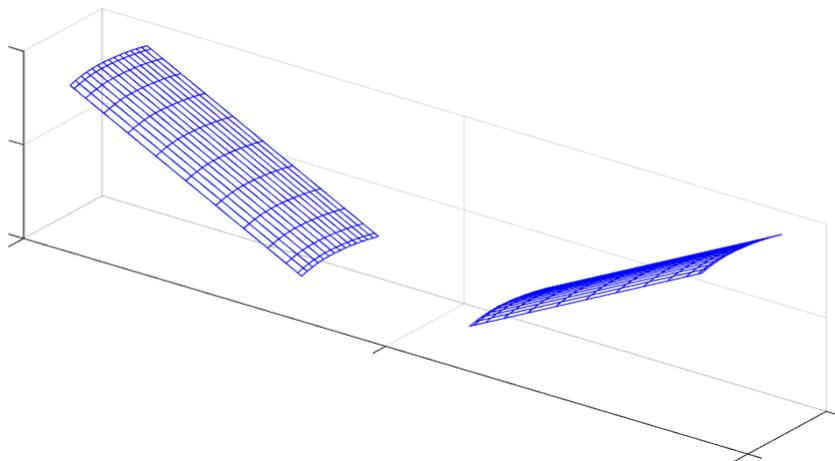
- Katz converges faster
- No influence of the frequency

- Results
 - Similar C_d for both methods
 - Good match with analytical solution
- Convergence
 - Joukowski converges faster for uncambered wings but slower for cambered ones

Flapping – Experimental setup



Source: N. Abdul Razak, *Experimental Investigation of the Aerodynamics and Aeroelasticity of Flapping, Plunging and Pitching Wings*. PhD thesis, University of Liege, 2012



The measured force is a combination of

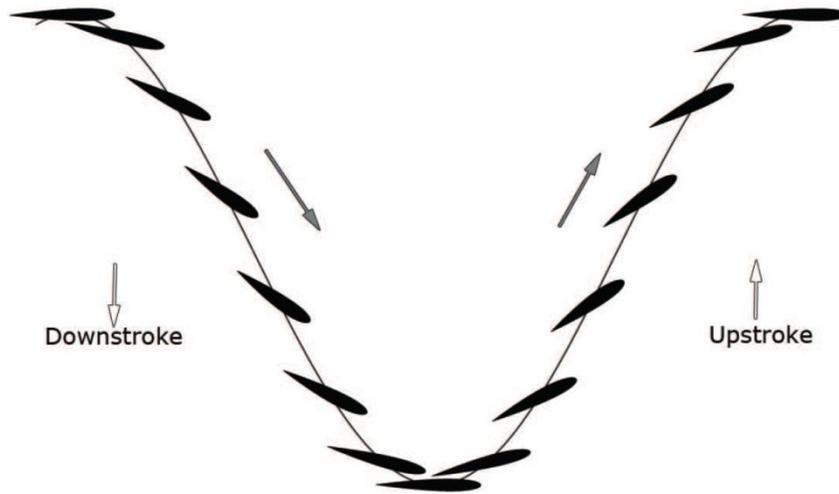
- **Unsteady aerodynamic loads**
- Inertial forces
- Added mass forces

The inertial and added mass forces must be subtracted

- Lead to larger errors in lift measurement

Only the wings are represented with UVLM

Flapping – Pitch leading

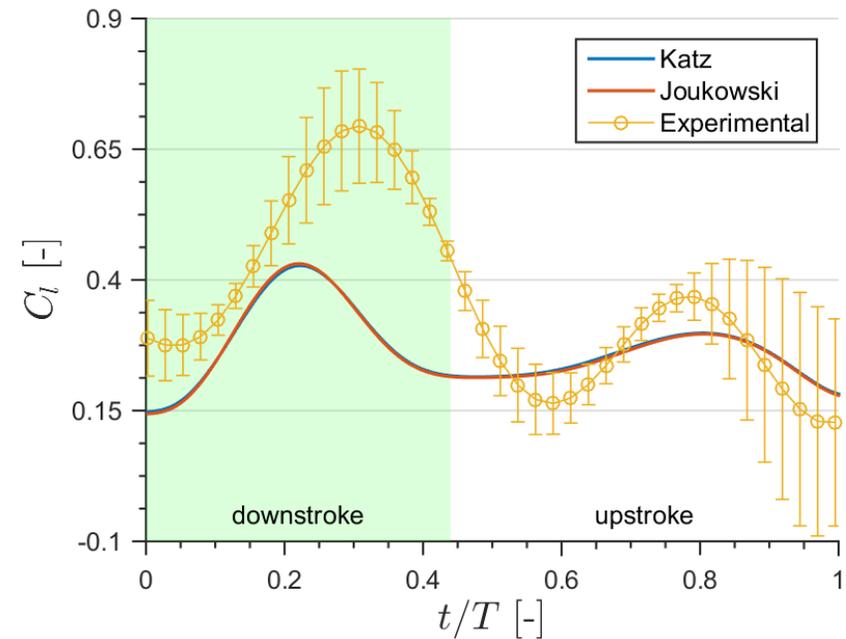
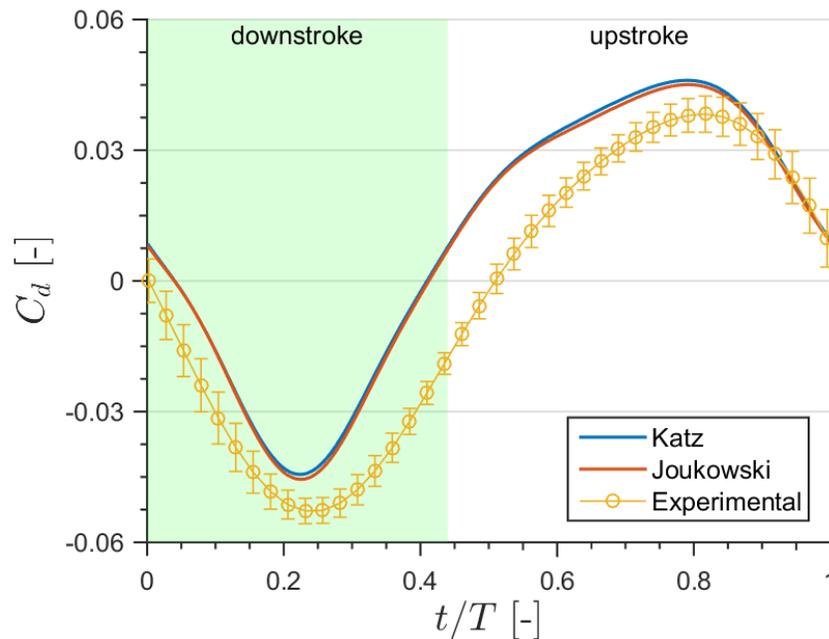


- Pitch leads flap by 90°
- Flow always attached
- Best kinematics for UVLM analysis

Source: N. Abdul Razak, *Experimental Investigation of the Aerodynamics and Aeroelasticity of Flapping, Plunging and Pitching Wings*. PhD thesis, University of Liege, 2012

Flapping – Pitch leading

NACA 6409 $f=1.23$ Hz, $U=9.4$ m/s



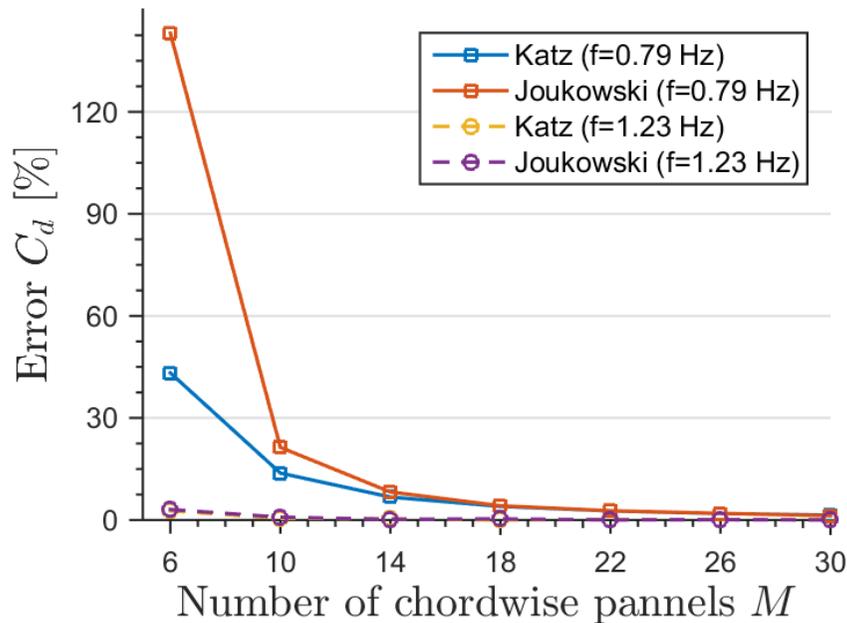
- Negligible difference between Katz and Joukowski
- Underprediction of thrust
- Same behavior than experimental

- Same prediction for both methods
- Not a good fit of experimental data

Flapping – Pitch leading

NACA 0012

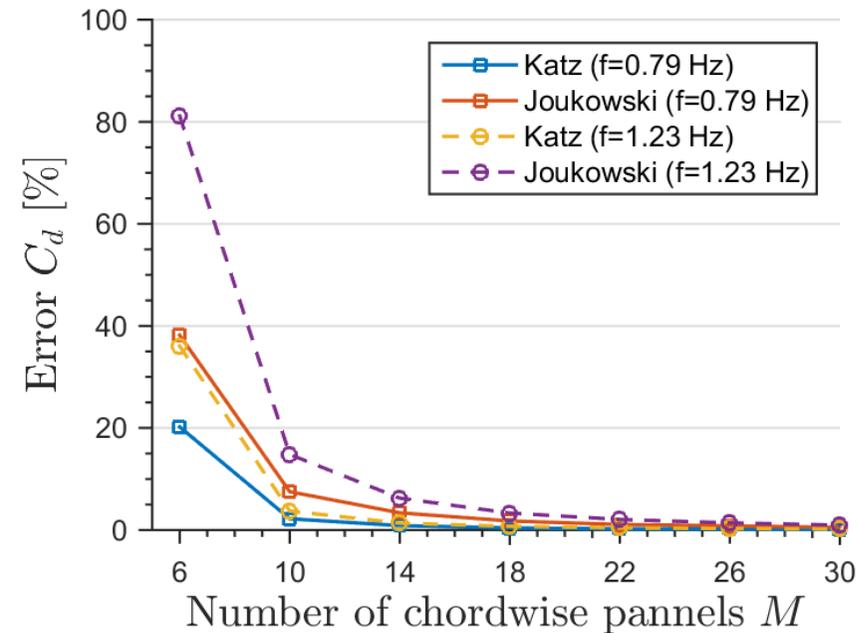
$f=1.23$ Hz, $U=9.4$ m/s



- Katz converges faster
- Convergence reached for the same M

NACA 6409

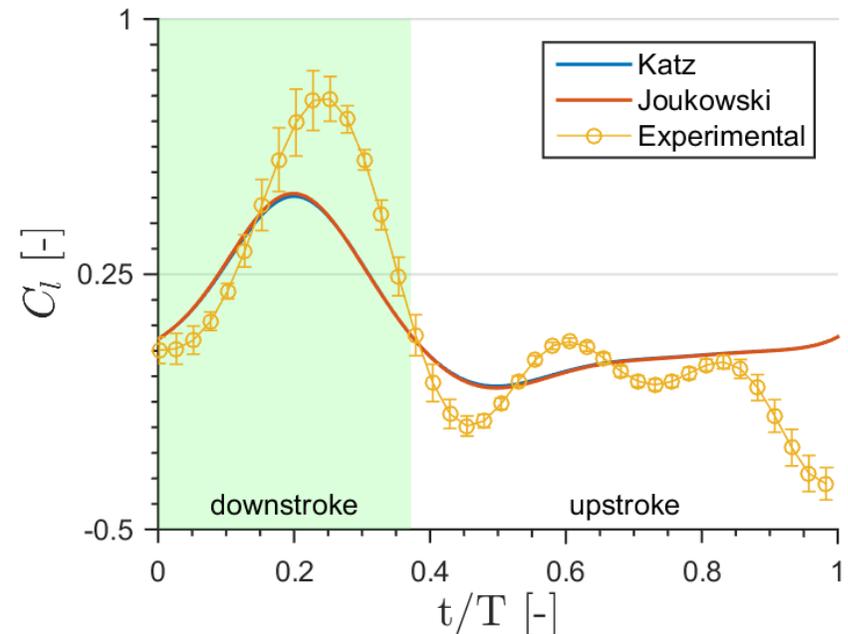
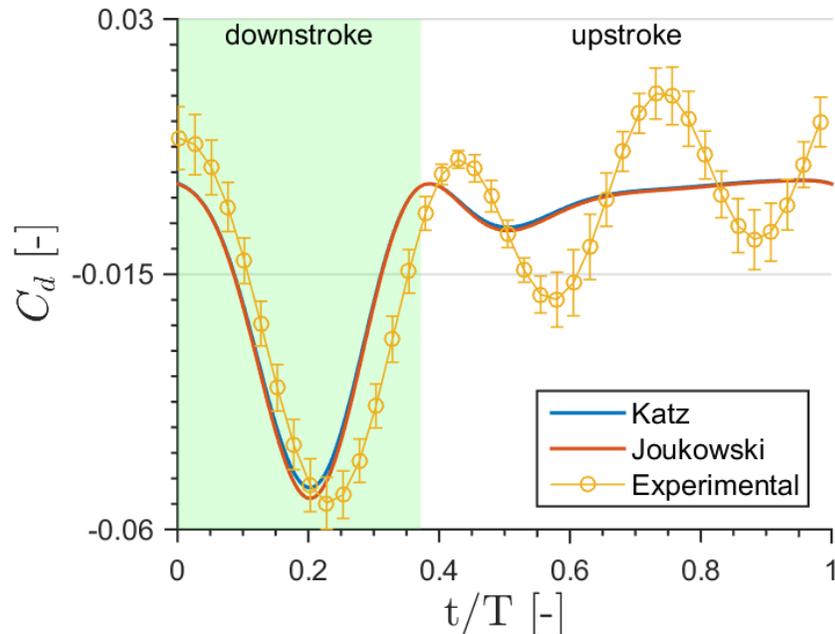
$f=1.23$ Hz, $U=9.4$ m/s



- Katz converges faster

Flapping – Pure flapping

Attached case: NACA 2412

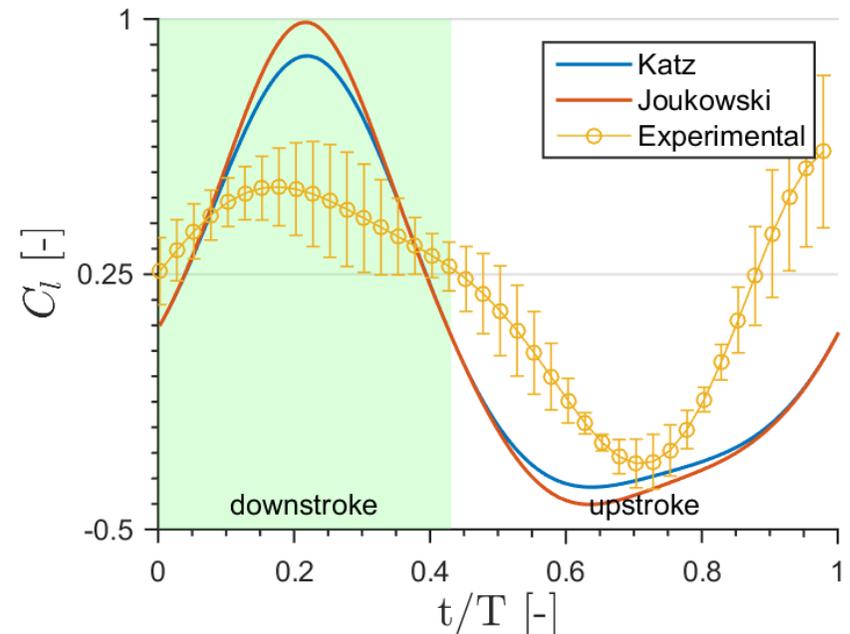
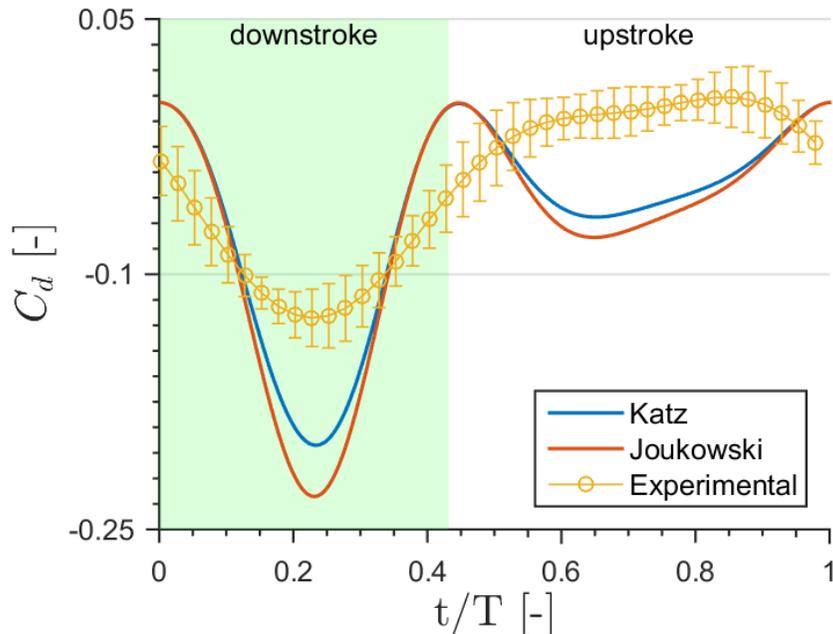


- Joukowski predicts a little bit more thrust
- Good fit of the data during downstroke
- Problem with experimental data for upstroke

- Not a good fit of experimental

Flapping – Pure flapping

Detached case: NACA 2412



- Both methods completely wrong (stall)
- Both methods completely wrong (stall)
- Joukowski even “more wrong”

Validity

- Joukowski and Katz give the **same solution** in most of the cases
 - Joukowski slightly better for high a.o.a.
 - Joukowski “more wrong” in stall

Convergence

- Joukowski better only for **uncambered airfoils** in pitch or plunge
- Katz converges faster in **all the other cases**

Thank you

Thank you for your attention