



CTML



Center for Transport, Mobility and Logistics

LEMA

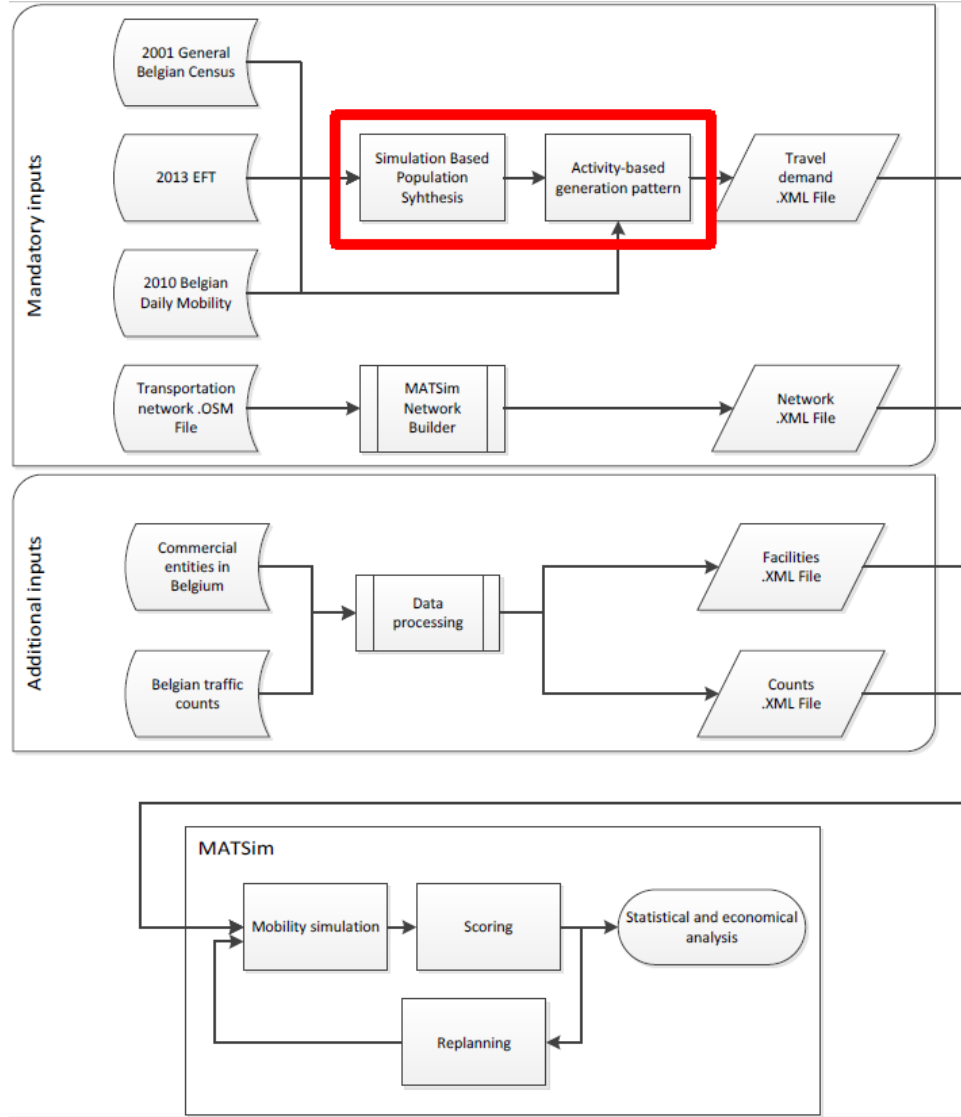


Iterative Proportional Fitting (IPF) to expand a synthetic sample into a synthetic population

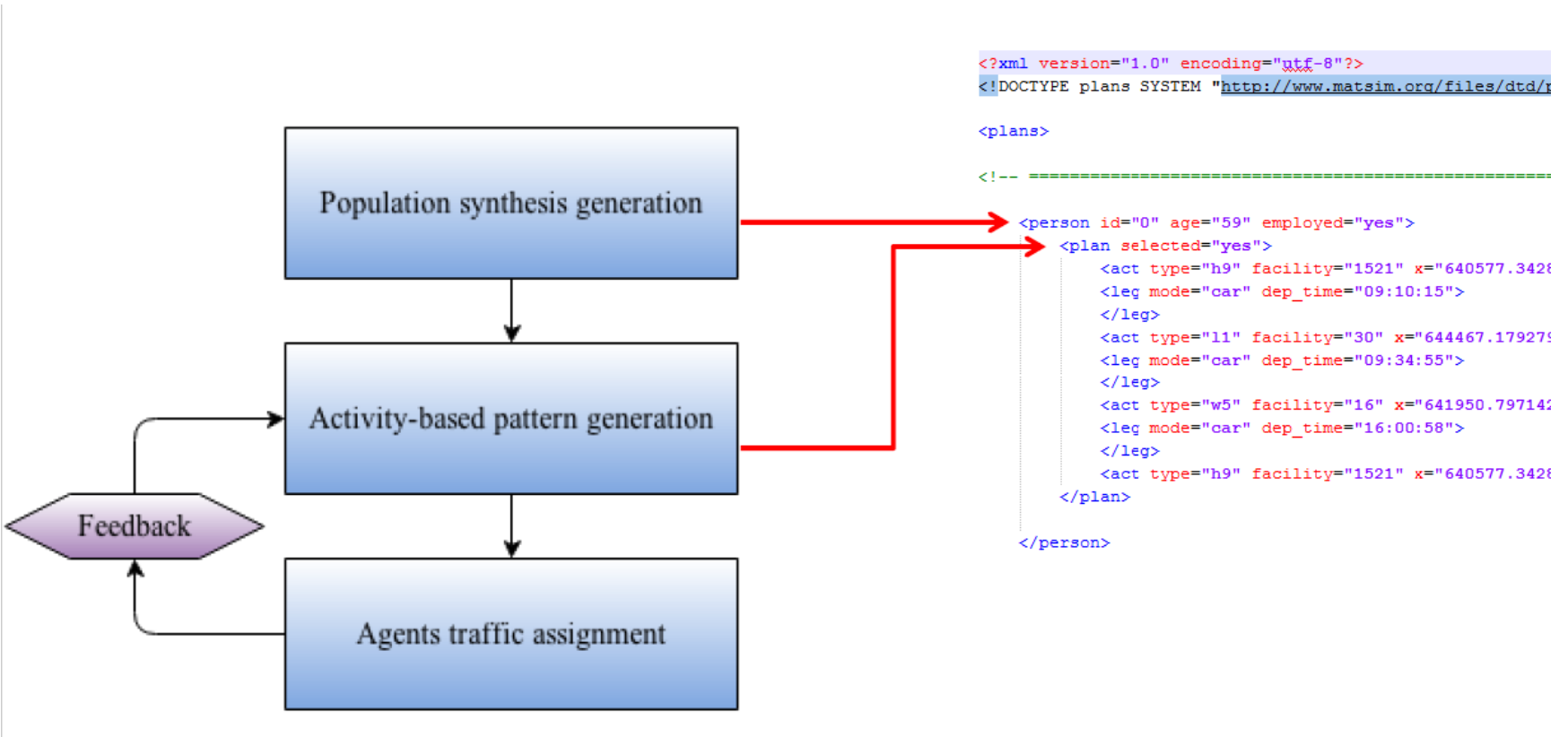
Mario Cools

- 1. Context
- 2. Overview of techniques
- 3. IPF (Iterative Proportional Fitting)
- 4. Other results
 - Simulation based approach (MCMC)
- 5. Conclusions
- 6. References

1. Context (1/2)



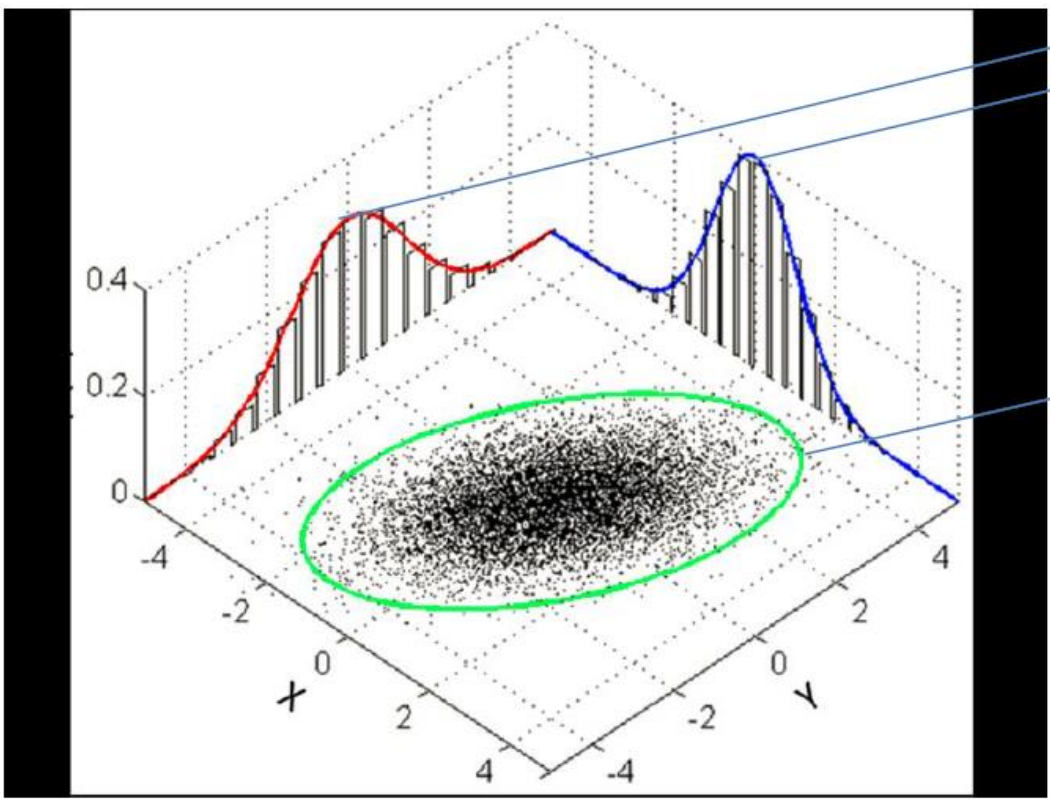
1. Context (2/2)



2. Overview of techniques

- Fitting methods
 - E.g. data matching, data fusion, IPF
- Reweighting methods
 - E.g. deterministic reweighting, combinatorial optimization
- Simulation-based methods
 - MCMC (Farooq et al., 2013)

3. IPF (1/8)



Marginal distributions:
Available information

Joint distribution:
initialized by a micro-sample

3. IPF (2/8)

	Y_1	Y_2	Y_n	<i>Marginal Probabilities of X</i>
X_1	p_{11}	p_{12}	p_{1n}	P_1
X_2	p_{21}	p_{22}	p_{2n}	P_2
.
.
X_m	p_{m1}	p_{m2}	p_{mn}	P_m
<i>Marginal Probabilities of Y</i>	P'_1	P'_2	P'_n	1

Fitting algorithm is applied until meeting the convergence

Problems in terms of convergence
Zero-cell problem

3. IPF (3/8)

Problems in terms of
convergence
Zero-cell problem

0,41%	4,07%	8,13%	16,26%	20,39%
0,00%	4,07%	0,00%	0,00%	23,45%
4,07%	8,13%	0,41%	8,13%	20,39%
8,13%	16,26%	20,33%	1,63%	35,78%
13,25%	20,39%	25,48%	40,88%	

3. IPF (4/8)

1. Estimation of a multivariate demographic table of proportions using IPF
2. Drawing of a synthetic population of households from the PUMS in such a way that it matches the proportions of the above estimated table

3. IPF (5/8)

- Four attributes were synthesized,
 - Housing location (20 categories/zones)
 - Age (14 categories)
 - socio-professional status (14 categories)
 - Gender
- Data: BELDAM
 - Assumption: BELDAM true population
 - Samples from BELDAM as micro-sample

3. IPF (6/8)

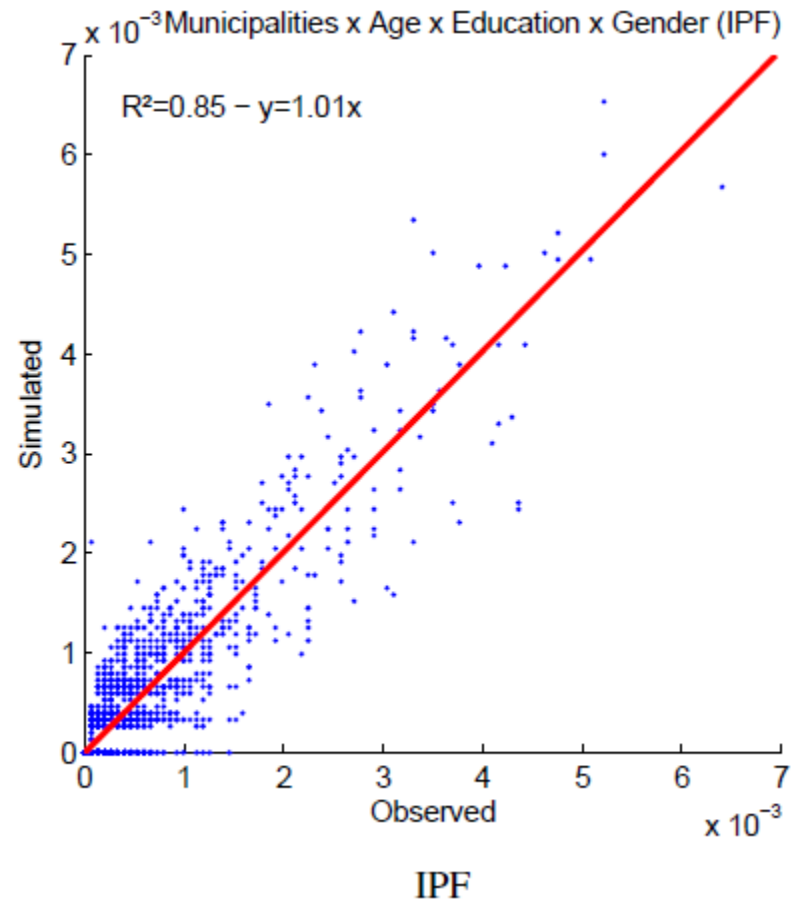
- Goodness of fit:
standardized root mean square error (SRMSE)

$$SRMSE = \frac{\sqrt{\frac{1}{N} \sum \sum \sum \dots (\tilde{J}_{ijk\dots} - J_{ijk\dots})^2}}{\frac{1}{N} \sum \sum \sum \dots J_{ijk\dots}^2}$$

where $\tilde{J}_{ijk\dots}$ and $J_{ijk\dots}$ represent the number of agents characterized by the combination of attributes i, j, k, \dots of the synthesized and observed population, and N is the total number of cells within the matrix.

3. IPF (7/8)

Sampling rate(%)	IPF
1	0.558
2	0.370
3	0.329
4	0.263
5	0.199
10	0.137
15	0.104
20	0.091
25	0.076



3. IPF (8/8)

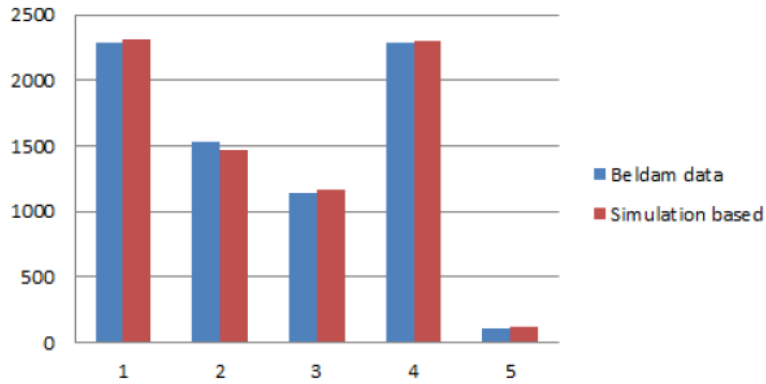
- Software packages
 - For the analysis: Barthelemy et al. (2015)
<https://cran.r-project.org/web/packages/mipfp/index.html>
 - Other:
<http://www.demog.berkeley.edu/~eddieh/datafitting.html>

4. MCMC (1/2)

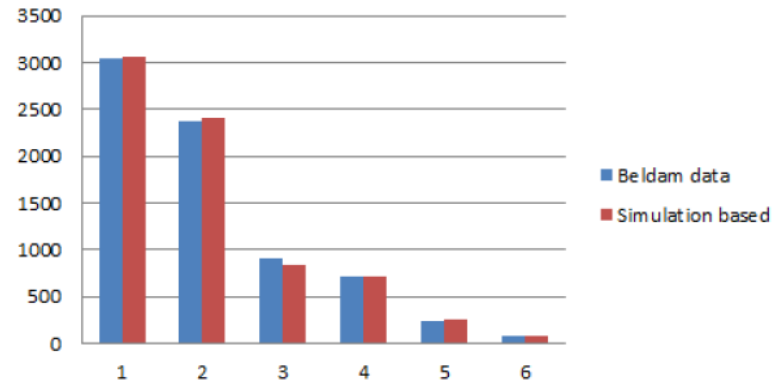
- Approach: Farooq et al. (2013)
- Data used: BELDAM
- 4 covariates
 - Dwelling type
 - Number of cars per HH
 - Number of persons per HH
 - Income level/month per HH
- Full conditionals used
- No dependence with initial condition

4. MCMC (2/2)

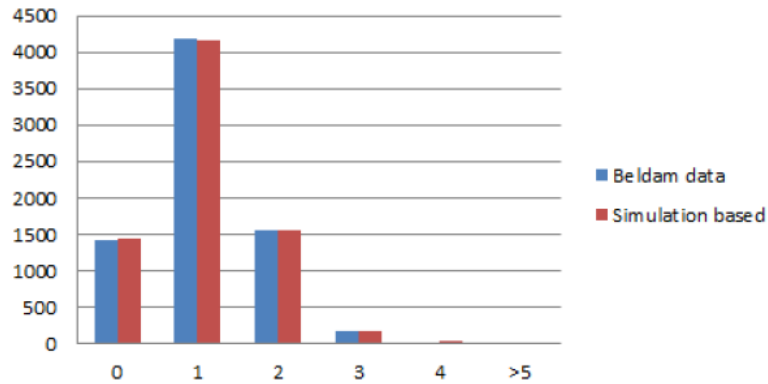
Dwelling type



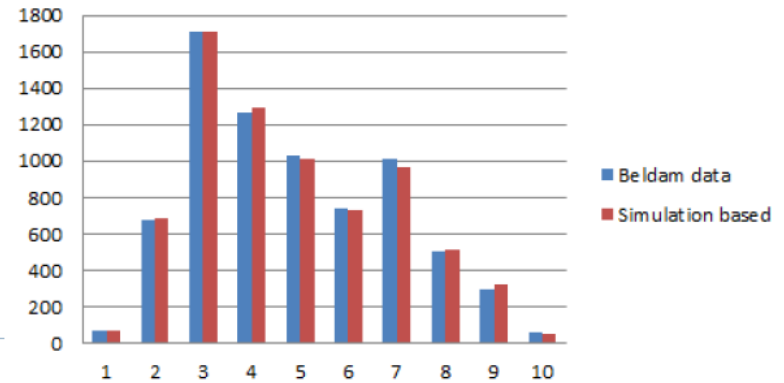
Number of individuals per HH



Number of cars per HH



Income per month per HH



5. Conclusions

- IPF
 - Can only be used with discrete variables containing a limited number of categories
 - Fitting a high number of attributes makes the computational process relatively costly
 - Conceptually easy
 - Works well for large micro-samples

6. Selected References

- Farooq, B., Bierlaire, M., Hurtubia, R., & Flötteröd, G. (2013). Simulation based population synthesis. *Transportation Research Part B: Methodological* 58, 243–263.
- Saadi, I., Eftekhar, H., El Saeid Mustafa, A. M., Teller, J., & Cools, M. (2014). An agent-based micro-simulation framework to assess the impact of river floods on transportation systems: implementation trajectory for an assessment in the Brussels metropolitan area. *Proceedings of the International Conference on Traffic and Transport Engineering*.
- Saadi, I., El Saeid Mustafa, A. M., Teller, J., & Cools, M. (2016). An integrated framework for forecasting travel behavior using Markov Chain Monte-Carlo simulation and profile Hidden Markov Models. *Proceedings of the 95th Annual Meeting of the Transportation Research Board*. Washington, DC: Transportation Research Board of the National Academies.
- Saadi, I., Liu, F., El Saeid Mustafa, A. M., Teller, J., & Cools, M. (in press). A framework to identify housing location patterns using profile Hidden Markov Models. *Advanced Science Letters*.

Acknowledgements

- Ismaïl Saadi
- ARC Project “Floodland” funded by the Fédération Wallonie-Bruxelles
- FSR Project “VEEAT” funded by the Fédération Wallonie-Bruxelles

Questions?



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