

Numerical modelling of hydromechanical coupling :

permeability dependence on strain path

FE Meeting – Mont Terri – St-Ursanne – 9 feb 2016

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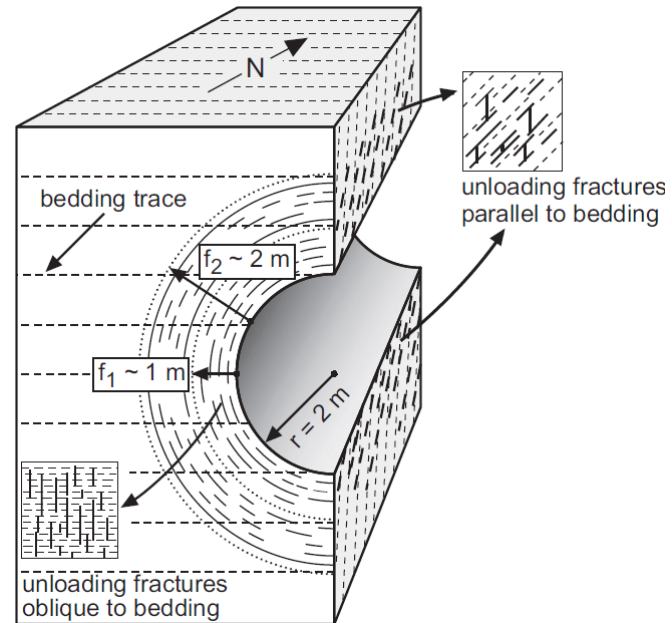
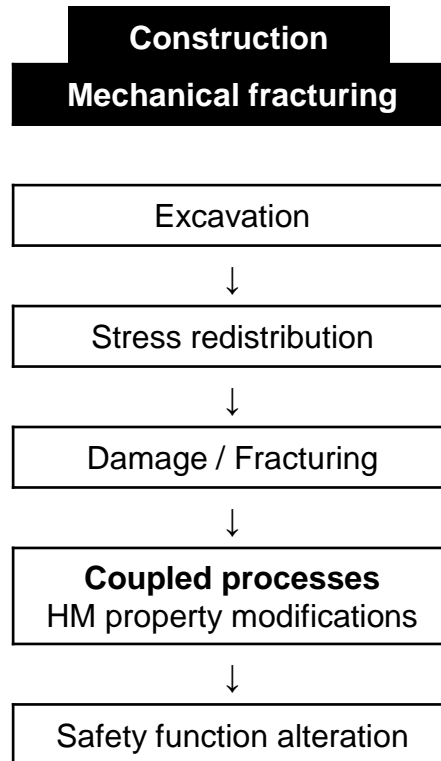
University of Liege + ANDRA

2 hydromechanical coupling applications

- Permeability in EDZ (Benoit Pardoën thesis)
- Permeability in compacted bentonite (Anne-Catherine Dieudonné thesis)
- *Simple hydromechanical coupling, however highly nonlinear !*
- Numerical modelling with the finite element code LAGAMINE, developed at University of Liege : multiphysical coupling and failure
- Experiments developed by ANDRA at Bure LSMHM URL

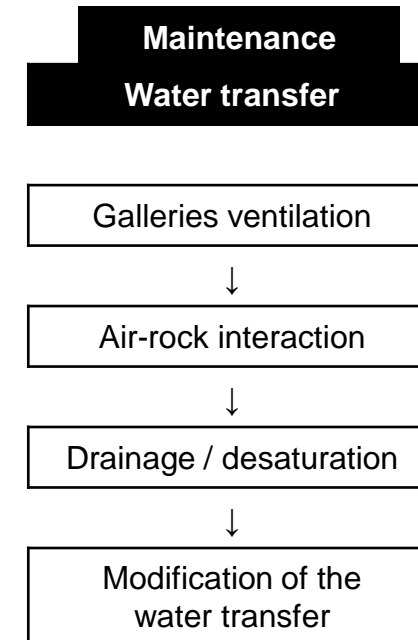
EDZ permeability

Excavation Damaged Zone (EDZ)



Fracturing & permeability increase
(several orders of magnitude)

Opalinus clay in Switzerland
(Bossart et al., 2002)



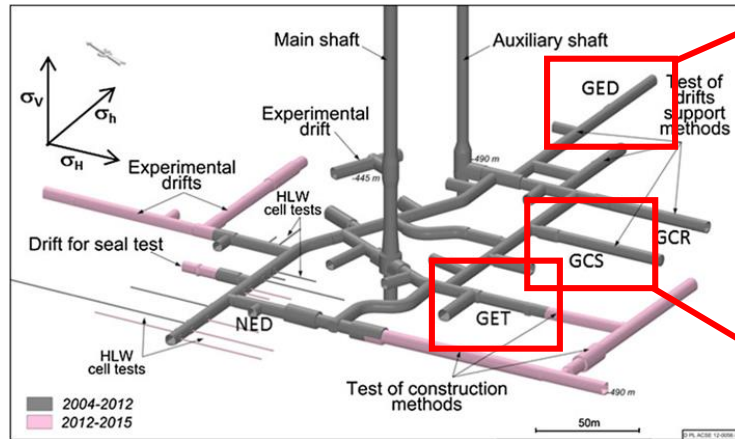
EDZ permeability

- Fracturing

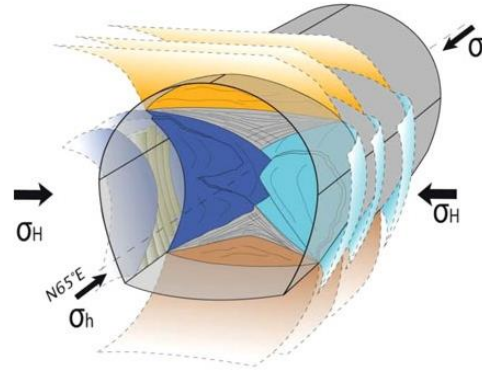
Anisotropies: - stress : $\sigma_H > \sigma_h \sim \sigma_v$

- material : HM cross-anisotropy.

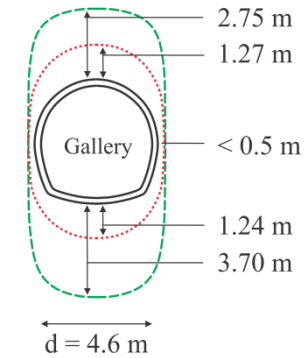
(Armand et al., 2014)



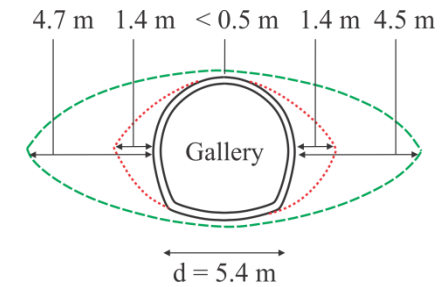
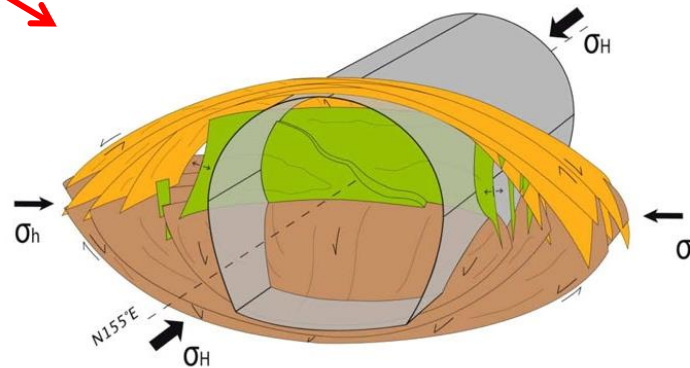
Galery // to σ_h



--- Shear fractures
 Mixed fractures



Galery // to σ_H



Issues: Prediction of the fracturing.
 Effect of anisotropies ?
 Permeability evolution & relation to fractures ?

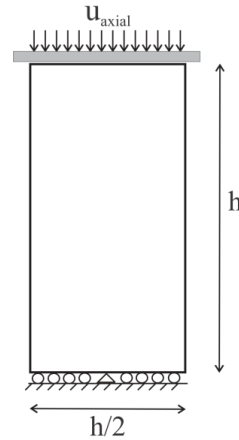
Strain localisation

Finite element methods

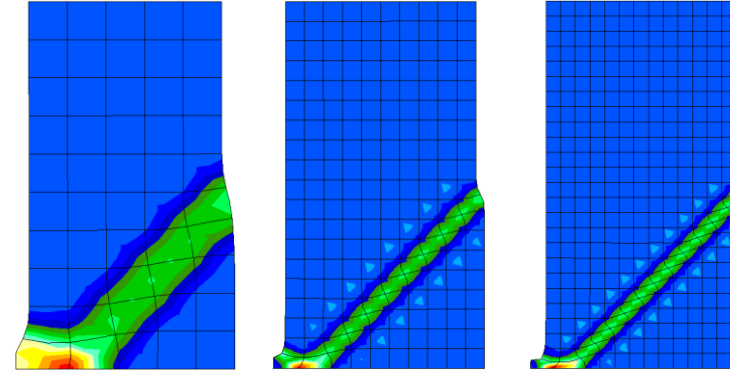
- Classical FE

Mesh dependency

Need to introduce an **internal length** scale for a correct modelling of the post-peak behaviour.



Equivalent total deviatoric strain $\hat{\varepsilon}_{eq} = \sqrt{\frac{2}{3} \hat{\varepsilon}_{ij} \hat{\varepsilon}_{ij}}$



- Regularisation

Enrichment of the kinematics :

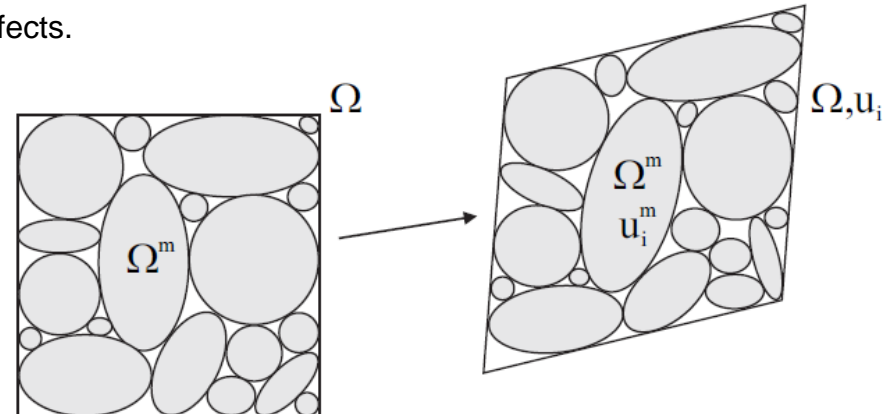
The continuum is enriched with microstructure effects.
Macro-kinematics + micro-kinematics

Macro Ω :

$$F_{ij} = \frac{\partial u_i}{\partial x_j} = \varepsilon_{ij} + r_{ij}$$

Micro Ω^m :

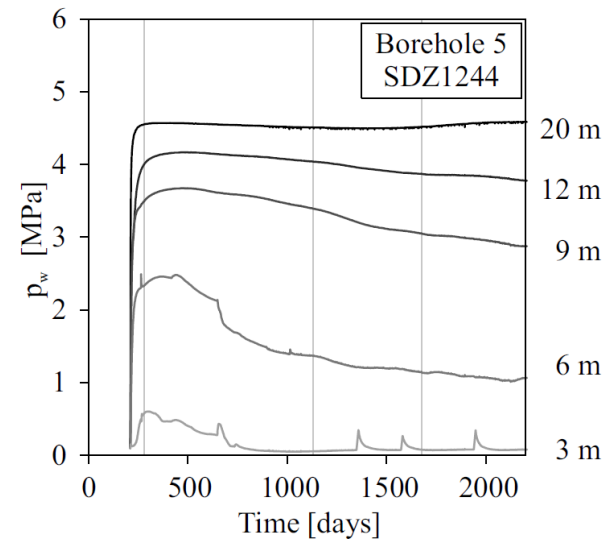
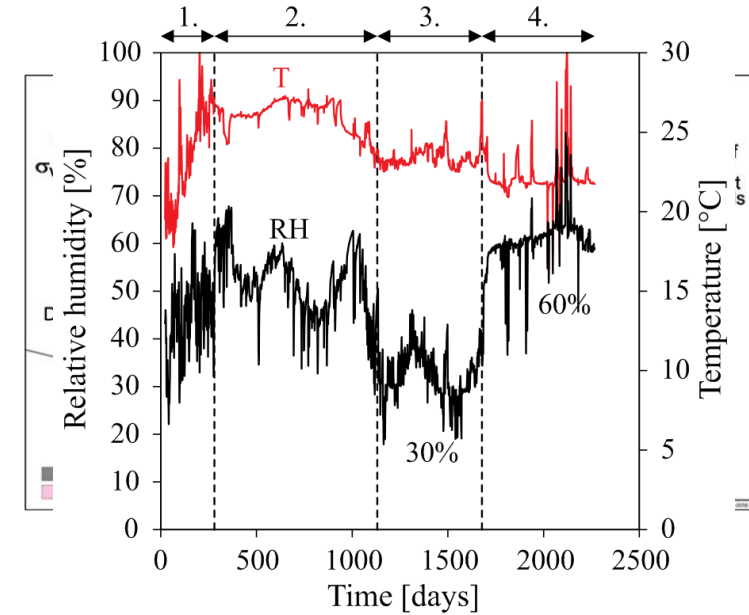
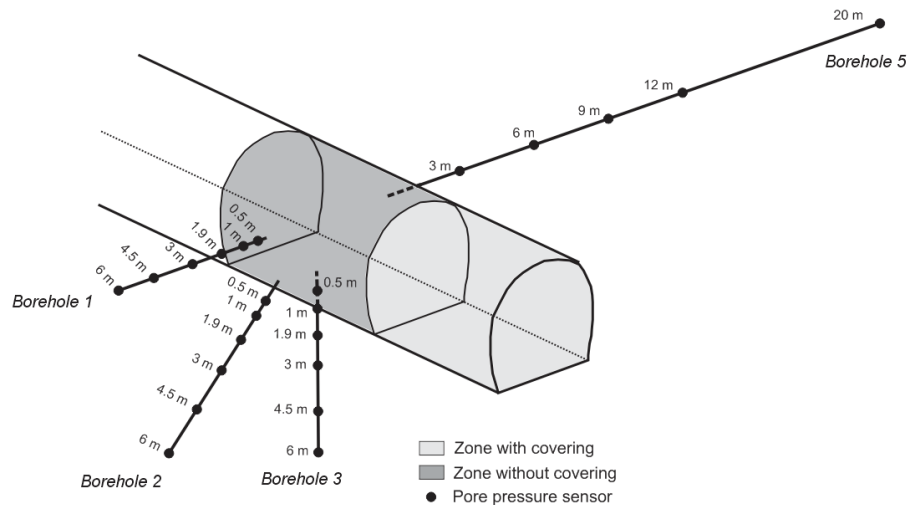
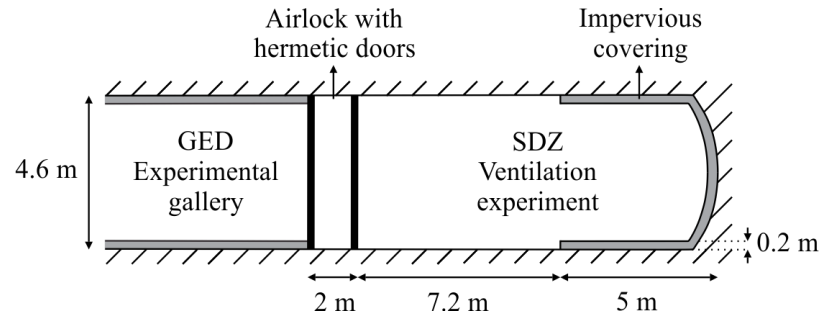
$$v_{ij} = \frac{\partial u_i^m}{\partial x_j} = \varepsilon_{ij}^m + r_{ij}^m$$



Large-scale experiment of gallery ventilation (SDZ)

Characterise the effect of gallery ventilation on the hydraulic transfer around it.

- drainage / desaturation
- exchange at gallery wall



EDZ permeability

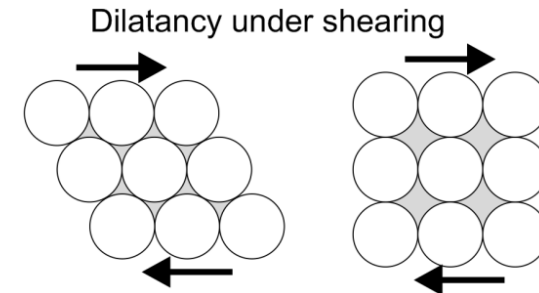
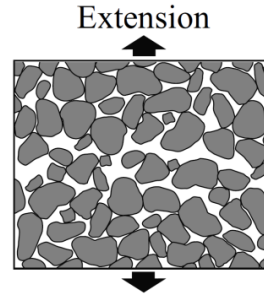
Evolution of intrinsic water permeability

Various approaches: deformation, damage, cracks...

- Relation to deformation

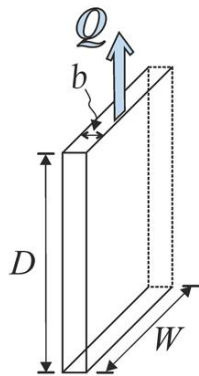
Volumetric effects = increase of porous space
(Kozeny-Carman)

$$k_w = k_{w,0} \frac{(1-\phi_0)^{\xi_1}}{\phi_0^{\xi_2}} \frac{\phi^{\xi_2}}{(1-\phi)^{\xi_1}} \quad \varepsilon_v = \frac{\varepsilon_{ii}}{3}$$

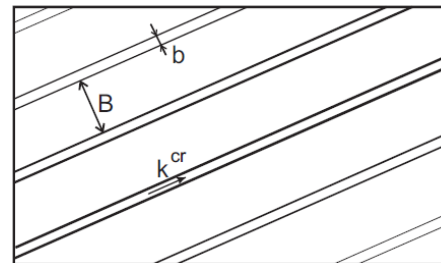


- Fracture permeability

Cubic law for parallel-plate approach
(Witherspoon 1980; Snow 1969, Olivella and Alonso 2008)



$$k_w^{cr} = \frac{b^2}{12}$$



$$k_w = \frac{b^3}{12B}$$

$$b = b_0 + B \langle \varepsilon^n - \varepsilon_0^n \rangle$$

$$k_w = k_{w,0} \left(1 + A \langle \varepsilon^n - \varepsilon_0^n \rangle \right)^3$$

Localised deformation
Fracture initiation

- Empirical law (Pardo et al., under review)

Related to strain localisation effect
Permeability variation threshold

$$k_{w,ij} = k_{w,ij,0} \left(1 + \beta_{per} \langle YI - YI^{thr} \rangle \hat{\varepsilon}_{eq}^3 \right)$$

$$YI = \frac{\Pi_{\hat{\sigma}}}{\Pi_{\hat{\sigma}}^p}$$

Hydraulic boundary condition for exchanges at gallery wall

- Classical approach

Instantaneous equilibrium (Kelvin's law) $RH = \frac{\rho_v}{\rho_{v,0}} = \exp\left(\frac{-p_c M_v}{\rho_w RT}\right)$

- Experimental

Drainage / desaturation → Progressive hydraulic transfer & equilibrium

- Non-classical mixed boundary condition (Gerard et al. 2008)

Liquid water + water vapour

$$\bar{q}_w = \bar{S} + \bar{E}$$

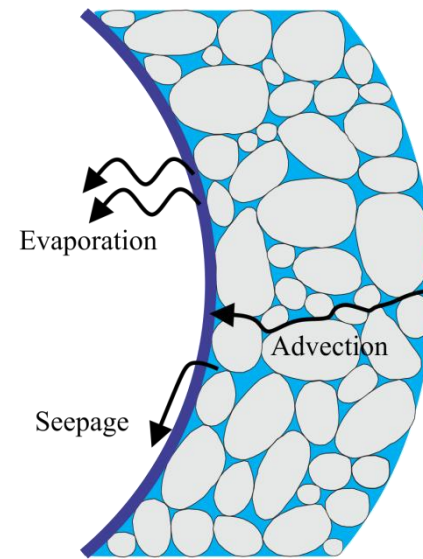
- Seepage flow :

$$\begin{cases} \bar{S} = K^{pen} (p_w^\Gamma - p_{atm})^2 & \text{if } p_w^\Gamma \geq p_w^{air} \text{ and } p_w^\Gamma \geq p_{atm} \\ \bar{S} = 0 & \text{otherwise} \end{cases}$$

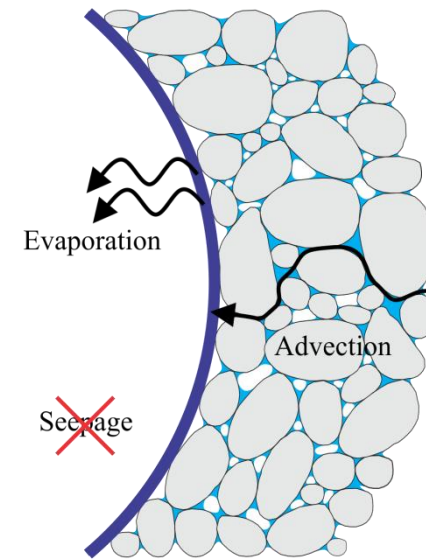
- Evaporation flow :

(Nasrallah and Perre, 1988)

$$\bar{E} = \underline{\alpha}_v (\rho_v^\Gamma - \rho_v^{air})$$



$S_{r,w} = 1$



$S_{r,w} < 1$

Modelling of excavation and SDZ experiment

(Pardoen et al., under review)

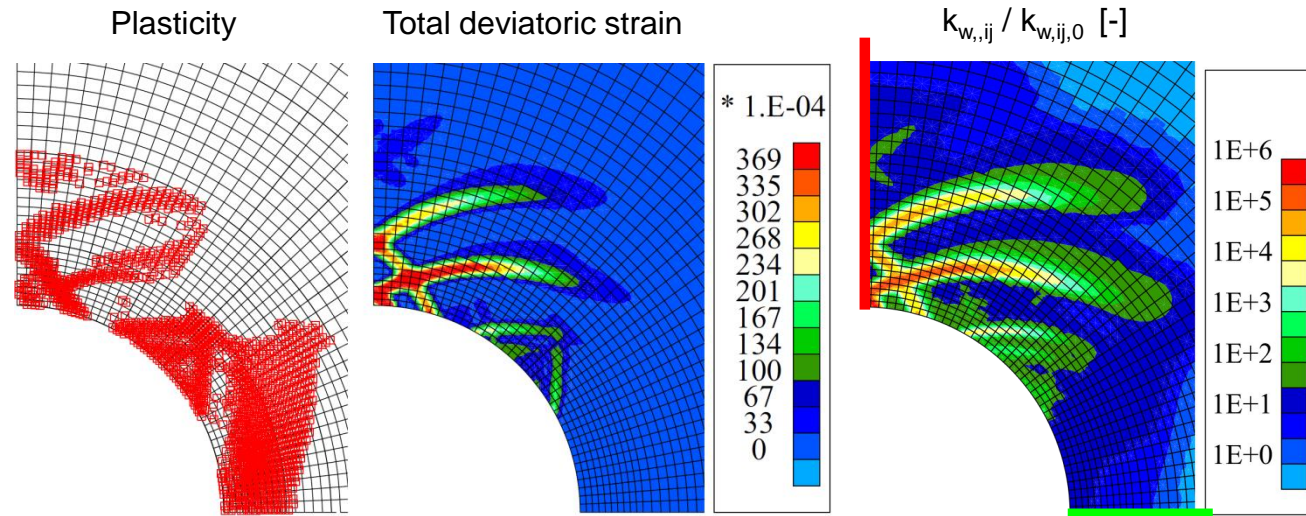
HM coupling in EDZ

- Gallery excavation

SDZ → GED gallery // σ_h

Anisotropic $\sigma_{ij,0}$ and material

→ Localisation zone dominated by stress anisotropy

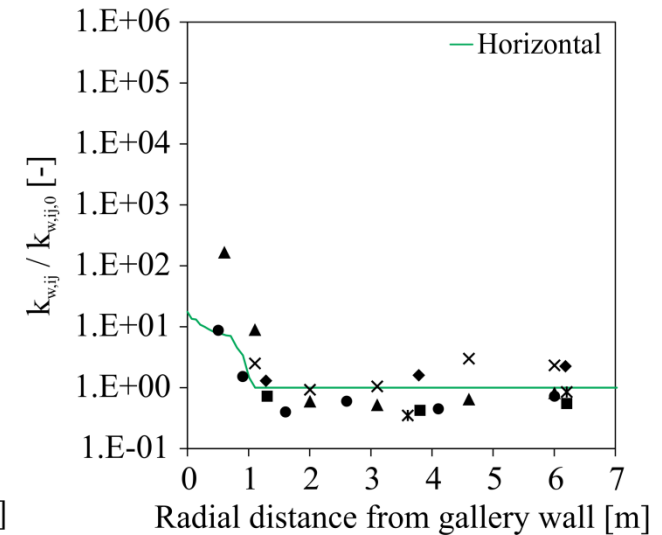
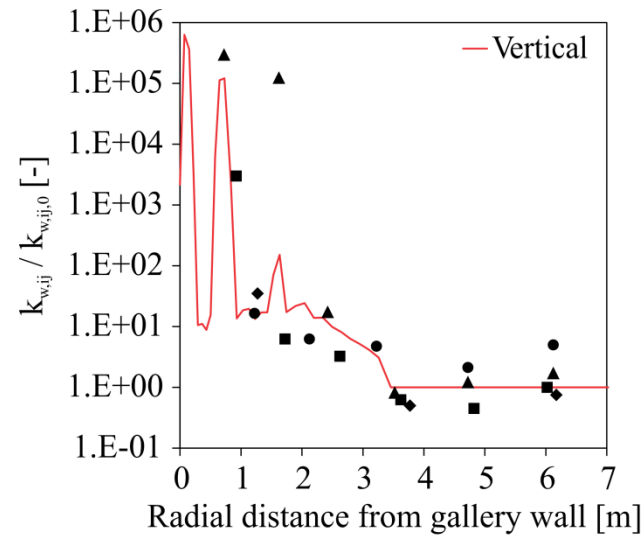


- Intrinsic permeability evolution

$$\frac{k_{w,ij}}{k_{w,ij,0}} = \left(1 + \beta \langle YI - YI^{thr} \rangle \hat{\epsilon}_{eq}^3\right)$$

$$YI^{thr} = 0.95$$

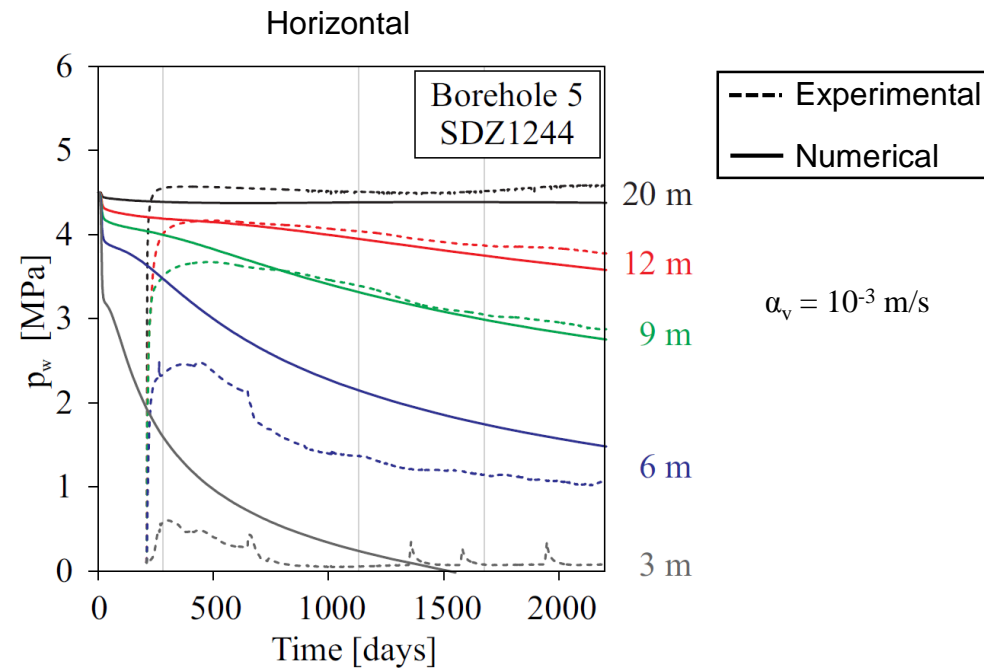
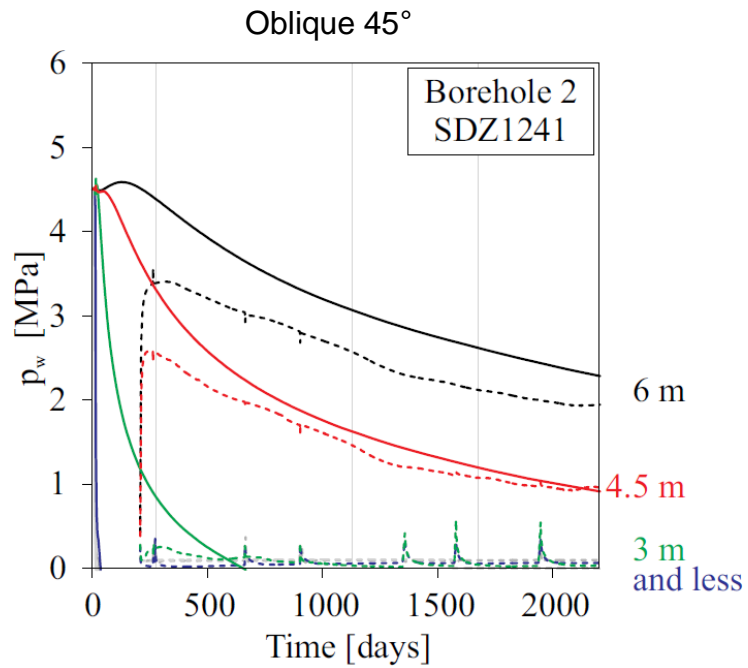
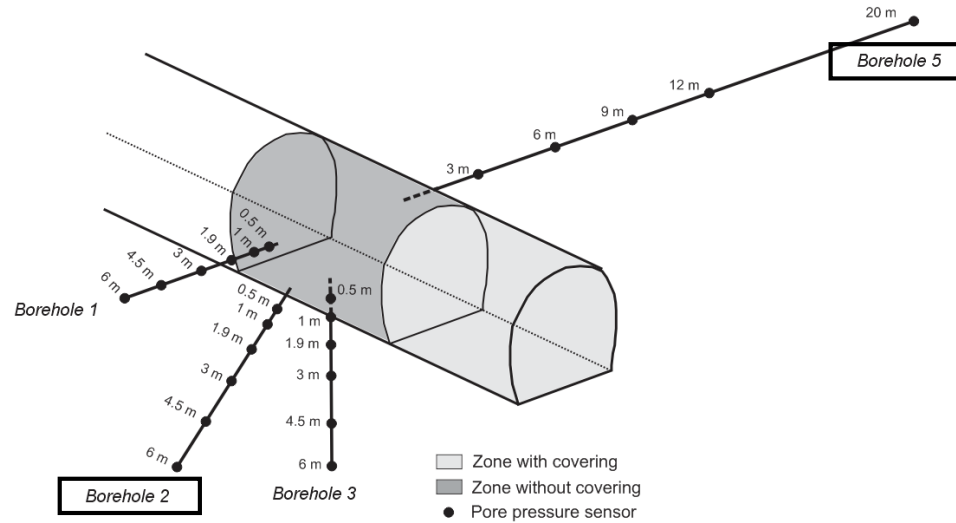
Cross-sections



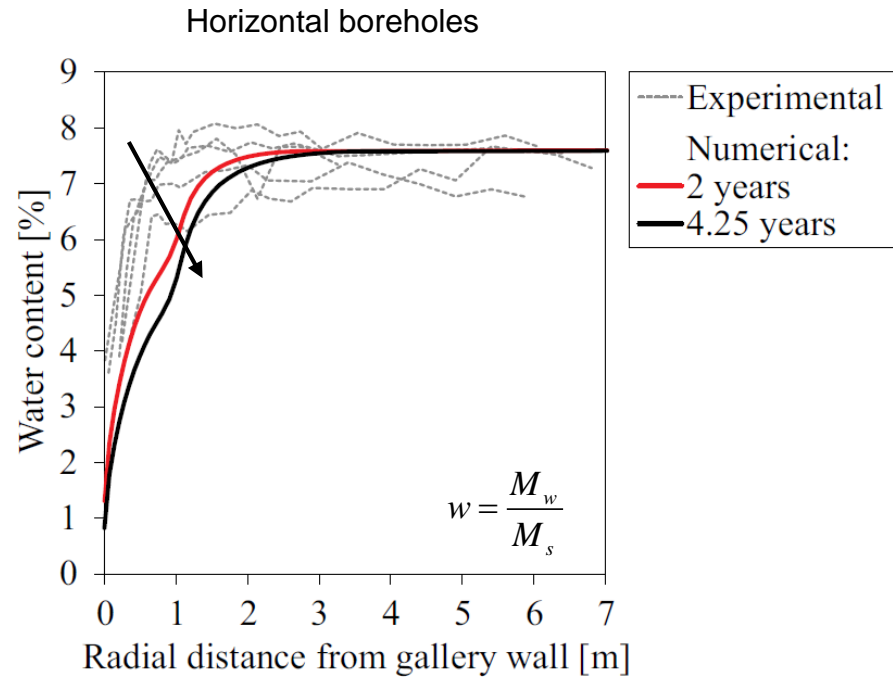
Plastic strain and a part of the elastic one → EDZ extension + k_w increase

EDZ permeability

Drainage / p_w reproduction

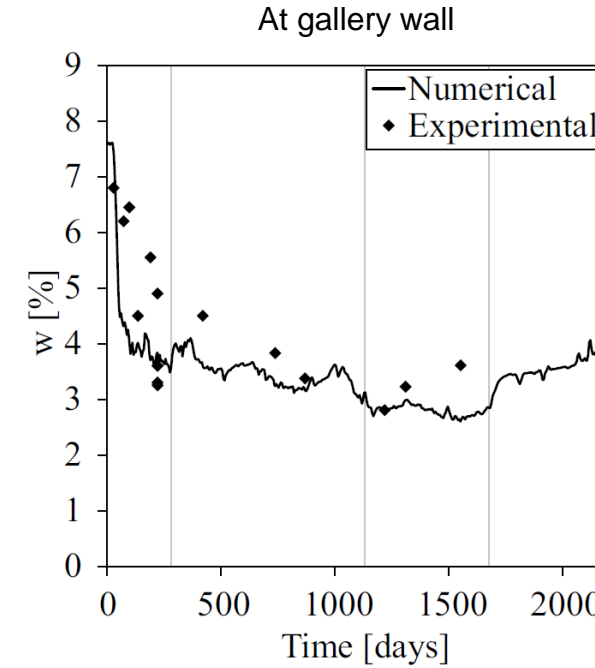


Desaturation EDZ / w reproduction



→ Desaturation: overestimation in long term

→ Vapour transfer ($\alpha_v = 10^{-3}$ m/s)



→ Good reproduction at gallery wall

Exchanges at gallery wall

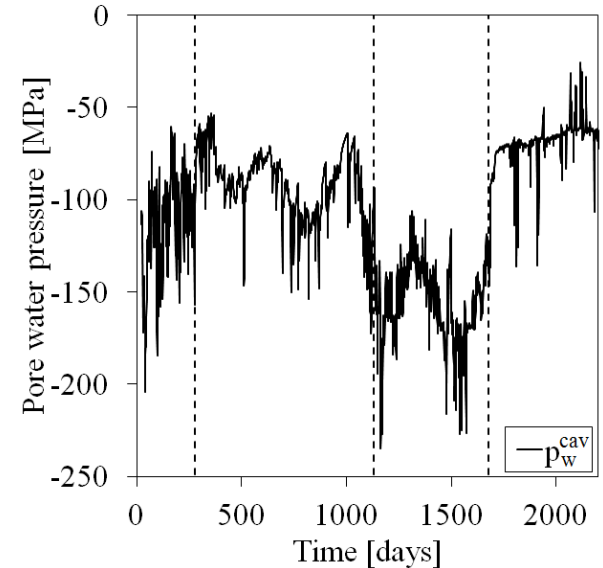
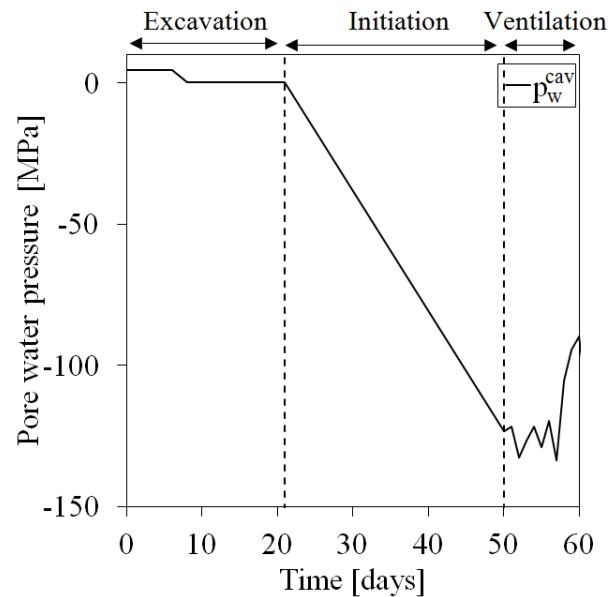
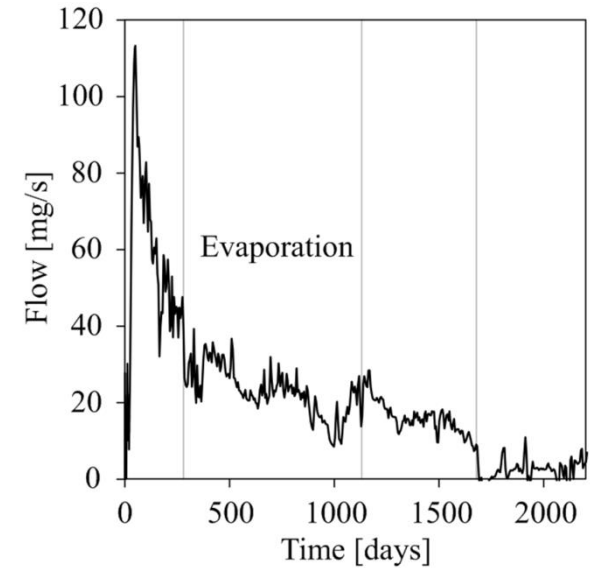
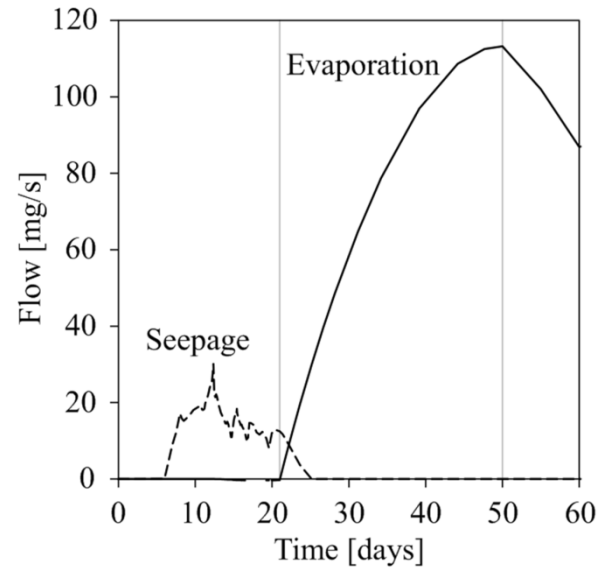
Flows:

$$\begin{cases} \bar{S} = K^{pen} (p_w^\Gamma - p_{atm})^2 & \text{if } S_{r,w}^\Gamma = 1 \\ \bar{S} = 0 & \text{if } S_{r,w}^\Gamma < 1 \end{cases}$$

$$\bar{E} = \alpha_v (\rho_v^\Gamma - \rho_v^{air})$$

Water pressure in cavity:

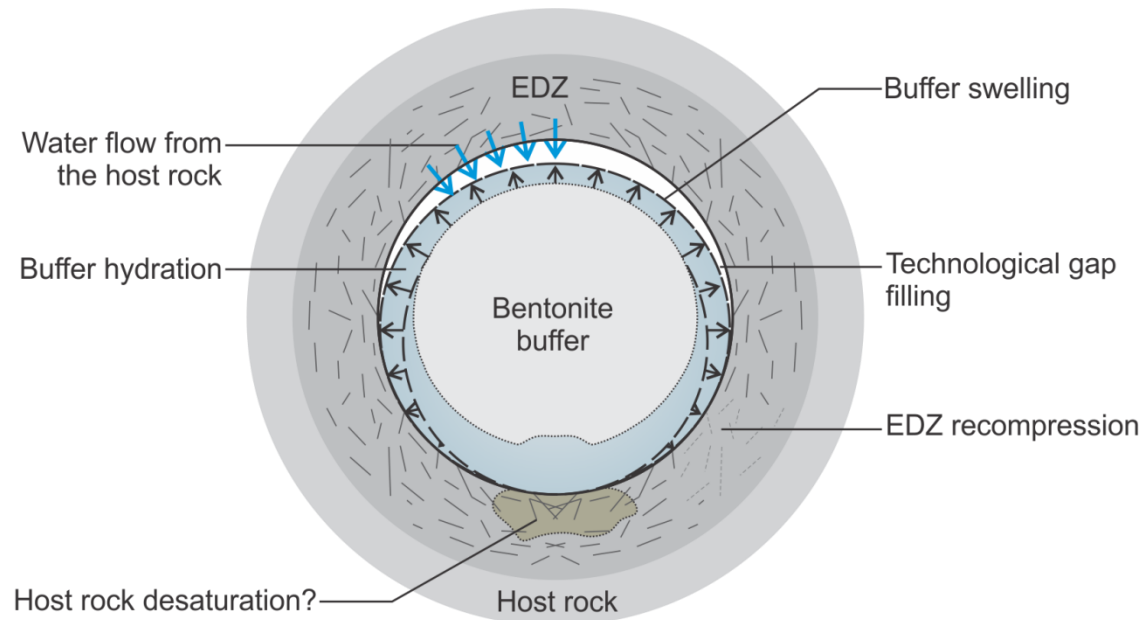
→ Transfer depends on α_v



Bentonite permeability

The processes taking place under repository conditions include

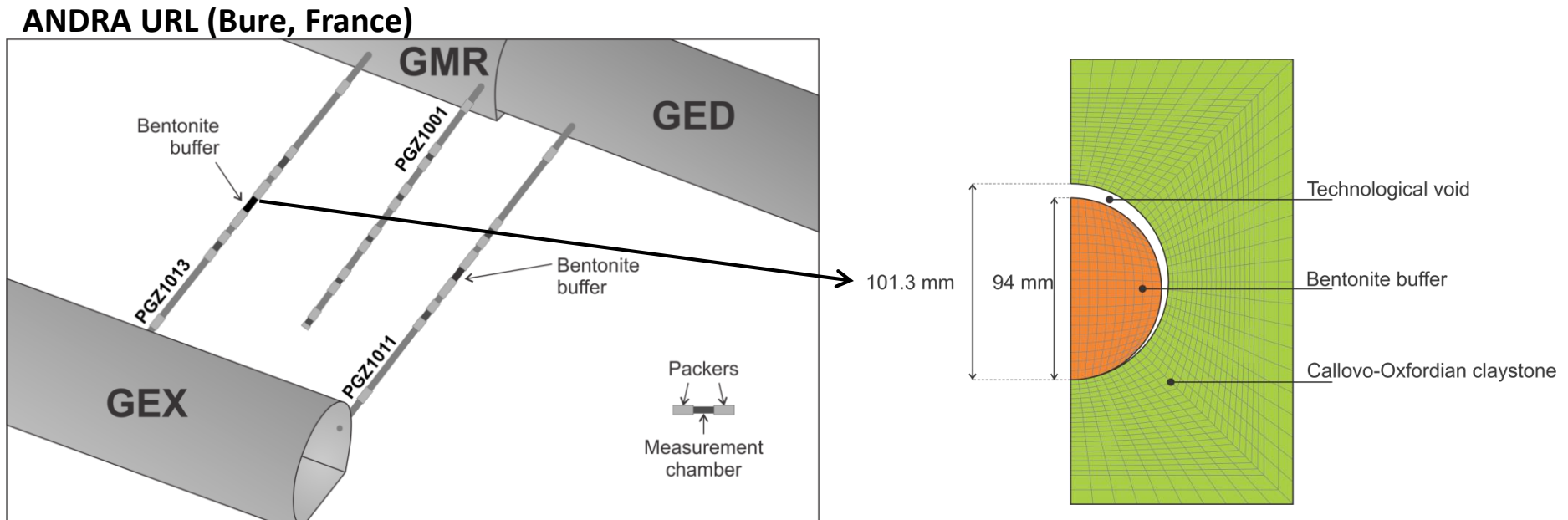
- Development of swelling strain / pressure
- Evolution of the water retention properties, the permeability...
- Structure changes



→ Complex and strongly coupled multiphysical & multiscale processes !

PGZ2 *in situ* experiments

- Objective: characterization of the water saturation process of bentonite buffers under natural conditions.
- PGZ1013: compacted MX-80 bentonite / sand mixture (70/30 in dry mass).
 - $\rho_{d0} = 2.06 \text{ Mg/m}^3$ ($n = 0.25$), $\sim 13\%$ technological void.



Material

MX-80 bentonite
(70% in dry mass)

**Uniaxially compacted
samples**

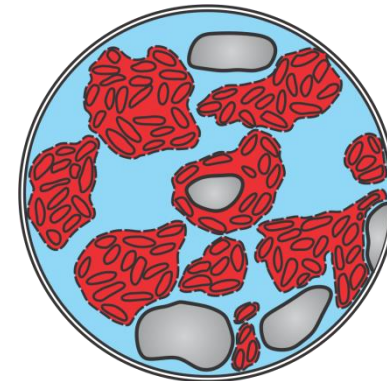
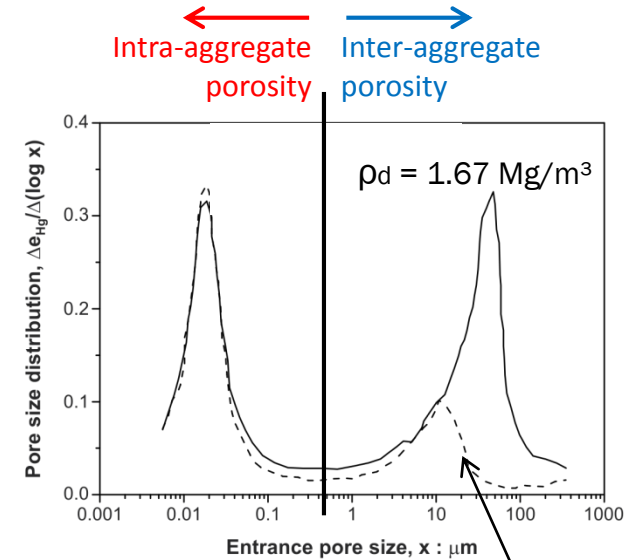


Quartz sand
(30% in dry mass)

$$\rho_d = 1.67 - 2.00 \text{ Mg/m}^3$$

$$w = 7 - 11\%$$

(used in Bure and
Tournemire URLs, France)



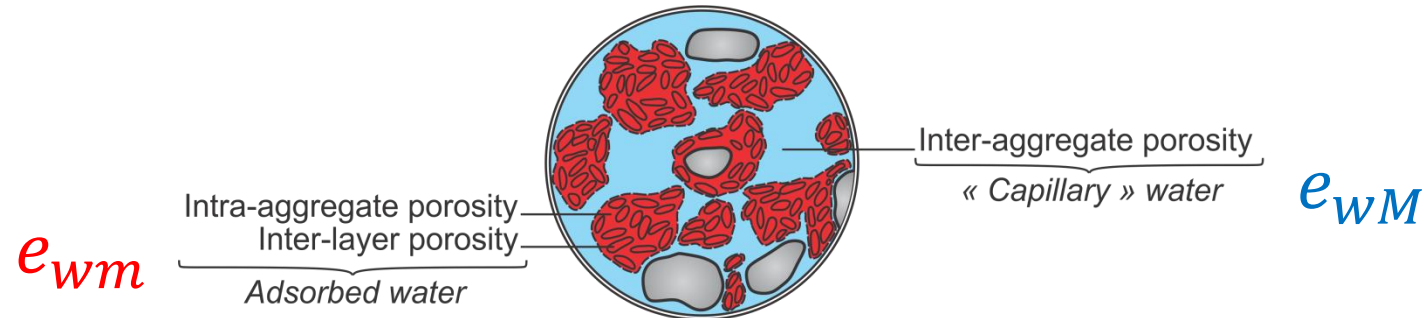
Experimental characterization performed in:

- [CEA Saclay](#), France (Gatabin et al. 2016)
- [Ecole des Ponts ParisTech](#), France (Wang 2012, Saba 2013)

Constitutive model

(Dieudonne et al., submitted)

$$e_w = S_r \cdot e = e_{wm} + e_{wM}$$



➤ Microstructural water ratio: $e_{wm}(s, e_m) = e_m \exp[-(C_{ads}s)^{n_{ads}}]$

➤ Macrostructural water ratio: $e_{wM}(s, e, e_m) = (e - e_m) \left[1 + \left(\frac{s}{a}\right)^n \right]^{-m}$

➤ Coupled modelling (HM): $K_w = K_0 \frac{(1-\phi_{M0})^M}{(\phi_{M0})^N} \frac{(\phi_M)^N}{(1-\phi_M)^M} \quad m^2$

HM formulation

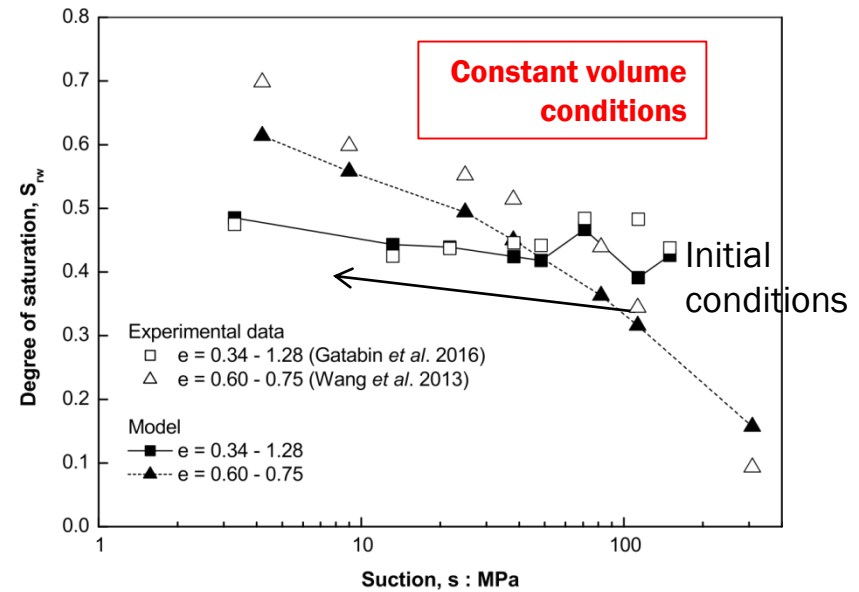
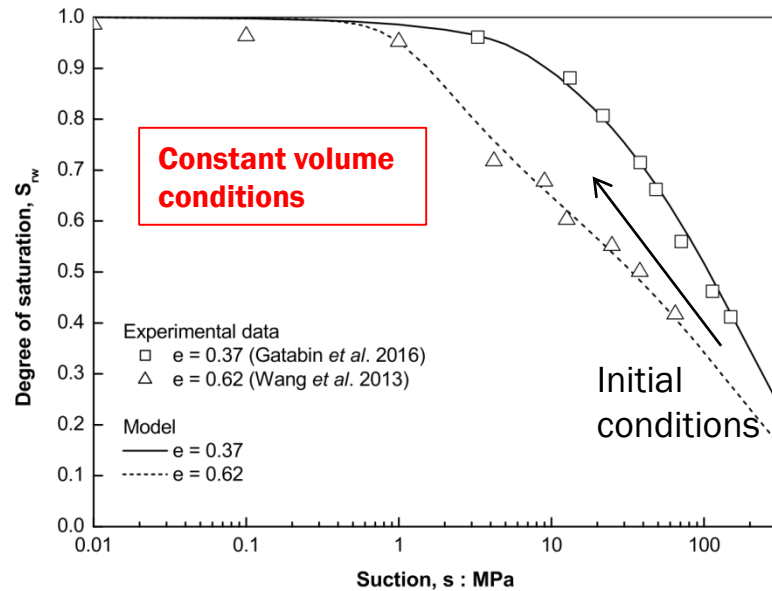
Bentonite buffer

- Double-structure water retention model:

$$e_w = S_{RW} \cdot e = \underbrace{e_{wm}(s, e_m)}_{\text{Adsorption mechanism}} + \underbrace{e_{wM}(s, e_M = e - e_m)}_{\text{Capillary mechanism}}$$

Adsorption mechanism

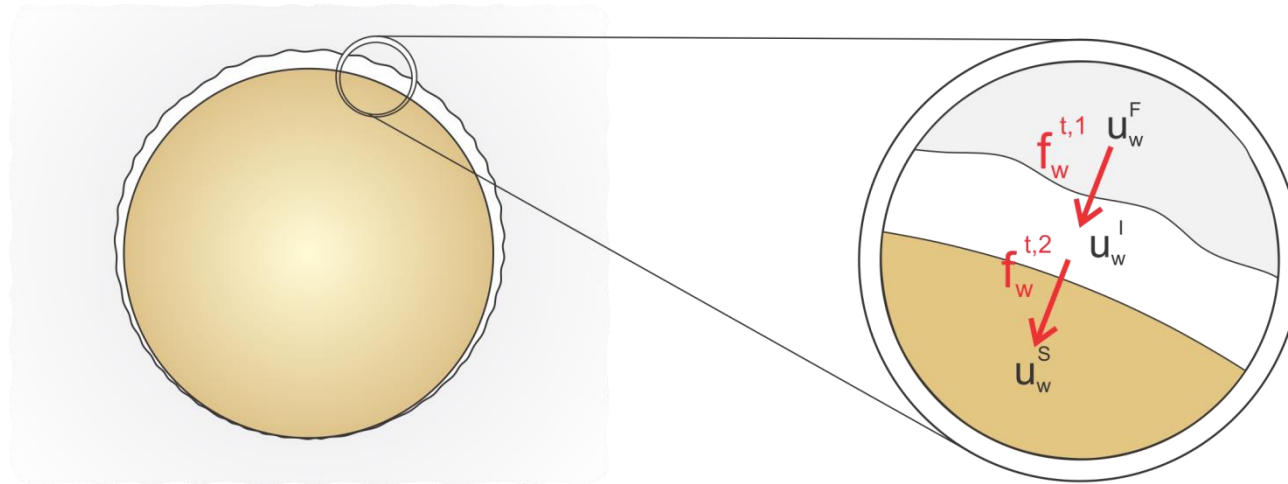
Capillary mechanism



HM formulation

Technological void / interface

- Zero-thickness interface finite element. (Cerfontaine et al. 2015)
- HM coupled formulation for partially saturated interfaces:
 - Absence of contact / contact (penalty method).
 - Transversal fluxes computed according to the pressure drop between both interface sides and the inside.

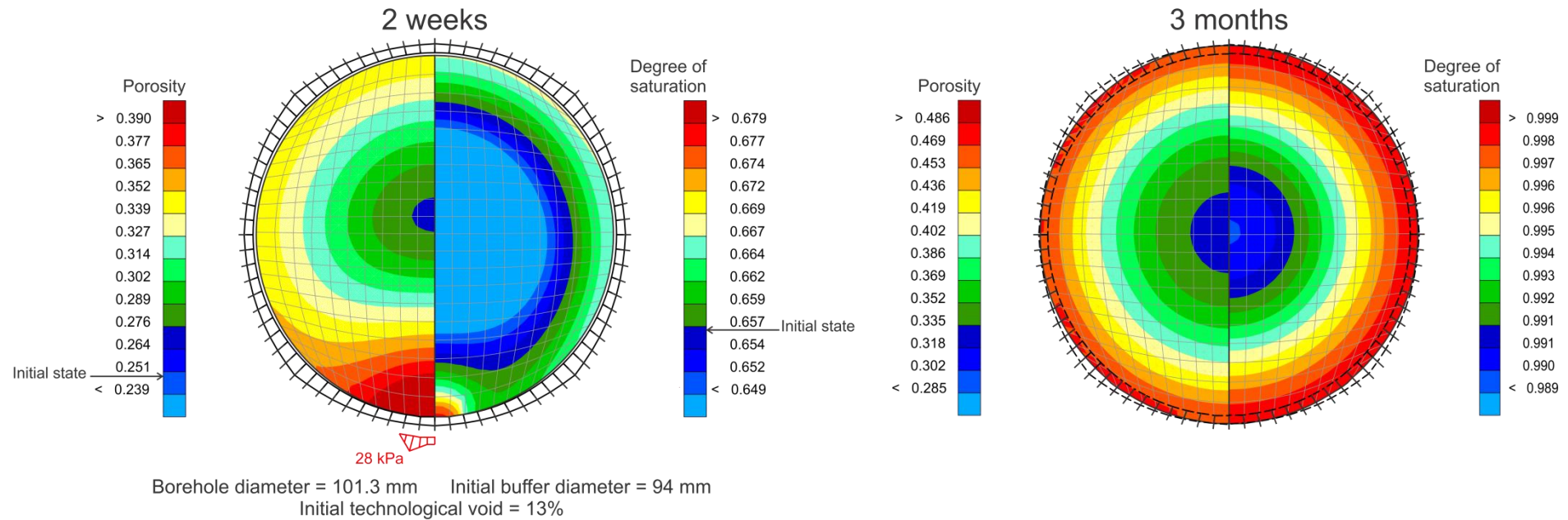


$$f_w^{t1} = T_t (u_w^F - u_w^I) \rho_w$$

$$f_w^{t2} = T_t (u_w^I - u_w^S) \rho_w$$

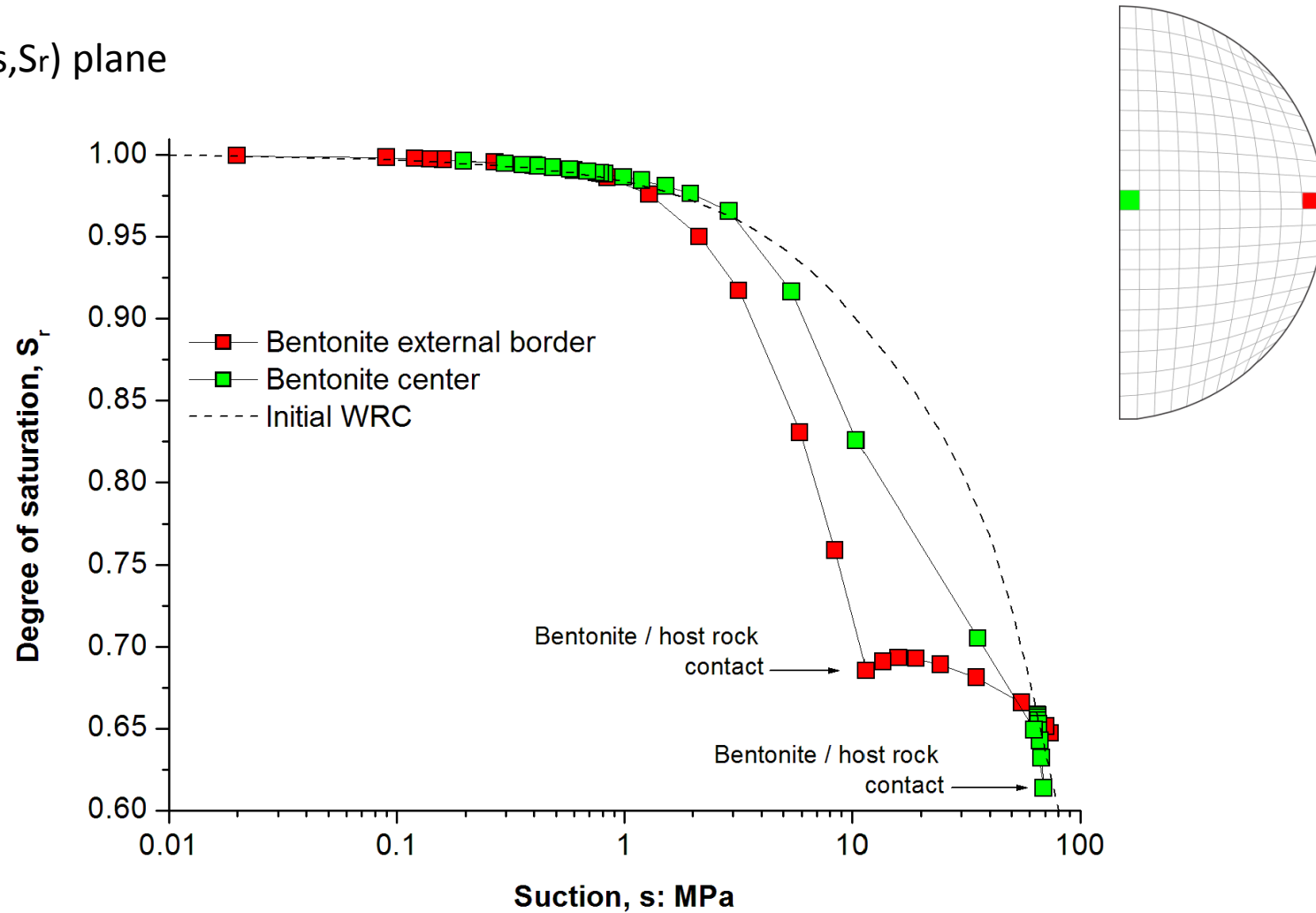
Numerical results

- Evolution of the bentonite buffer:
 - Very high transmissivity if contact, lower if technological void.
 - Preferential hydration from the bottom in the early process.



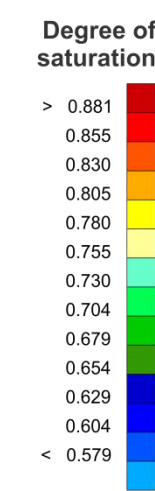
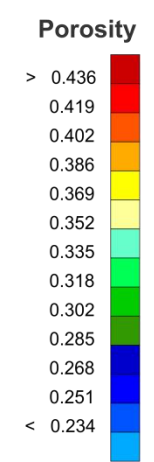
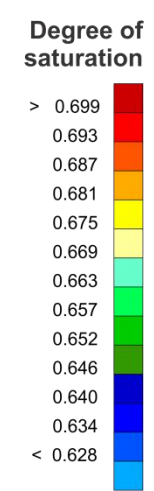
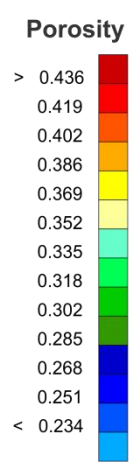
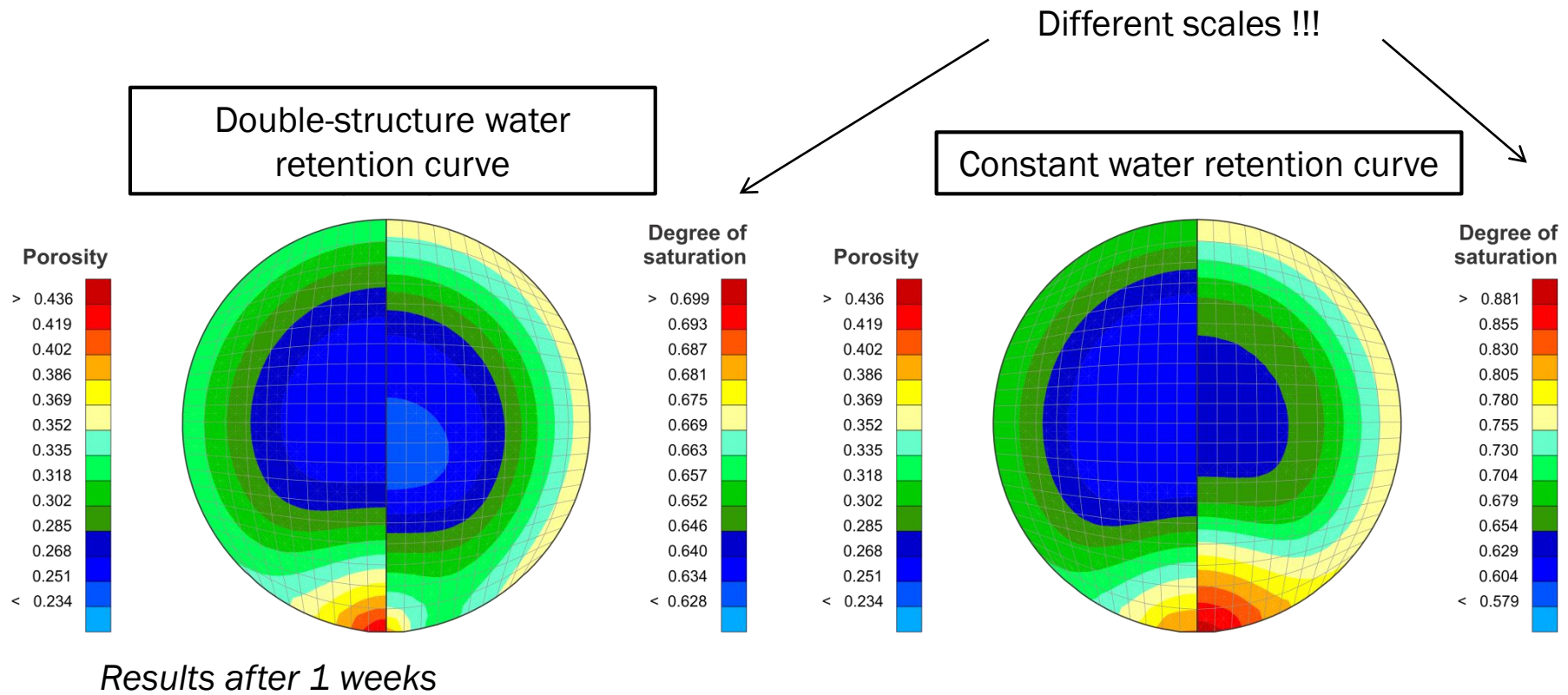
Numerical results

- Stress path in the (s, S_r) plane



Numerical results

- Strong influence of the water retention model:
 - Higher degree of saturation if a constant WRC is used.
 - Saturation kinetics overestimated if a constant WRC is used.



Conclusion

- The challenges : highly non linear coupling terms
- Permeability evolution based on micro scale considerations
- EDZ : fractures in an anisotropic context – Permeability evolution with fracturing
- Bentonite : free swelling vs confined swelling, permeability evolution
- Adoption of a double-structure water retention curve to model the evolving properties of the bentonite buffer.
- Use of interface finite elements to model the progressive closing of technological voids.

References

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