TRANSIENT PERFORMANCE EVALUATION OF WASTE HEAT RECOVERY RANKINE CYCLE BASED SYSTEM FOR HEAVY DUTY TRUCKS

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Abstract

The study presented in this paper aims to evaluate the transient performance of a waste heat recovery Rankine cycle based system for a heavy duty truck and compare it to steady state evaluation. Assuming some conditions to hold, simple thermodynamic simulations are carried out for the comparison of several fluids. Then a detailed first principle based model is also presented. Last part is focused on the Rankine cycle arrangement choice by means of model based evaluation of fuel economy for each concept where the fuels savings are computed using two methodologies. Fluid choice and concept optimization are conducted taking into account integration constraints (heat rejection, packaging ...). This paper shows the importance of the modeling phase when designing WHRS and yields a better understanding when it comes to a vehicle integration of a Rankine cycle in a truck.

Keywords: Waste heat recovery system, Modeling, Thermodynamic,

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1 1. INTRODUCTION

Even in nowadays heavy duty (HD) engines, which can reach 45% of effi-2 ciency, a high amount of the chemical energy contained in the fuel is released 3 as heat to the ambient. Driven by future emissions legislation and increase in fuel prices, engine gas heat recovering has recently attracted a lot of interest. 5 Over the last decades, most of the research has focused on waste heat recov-6 ery systems (WHRS) based on the Rankine cycle [???]. These systems 7 can lead to a decrease in fuel consumption and lower engine emissions [? ?]. Recent studies have brought a significant potential for such systems in a 9 HD vehicle [? ?]. However, before the Rankine cycle based system can be 10 applied to commercial vehicles, the challenges of its integration have to be 11 faced. The work done in [?] and [?] show that one of the main limitation 12 is the cooling capacity of the vehicle. But other drawbacks, such as the back 13 pressure, weight penalty or transient operation should not be minimized [? 14 ?]. Before tackling the problem of the control strategy of this system [? 15 ?], the architecture and components need to be selected to achieve a cer-16 tain objective that could be to maximize the fuel savings or minimize the 17 impact on the vehicle. This study focuses more on maximizing the system 18 performance by taking into account the different penalties induced by the 19 integration of the system on a heavy duty truck. Technical challenges and 20 optimization of stationnary ORC are well adressed [? ?] but for mobile 21 applications only few studies deal with fuel saving potential of WHRS on 22 dynamic driving cycles [??] and the latter is generally reduced to a certain 23 number of steady state engine operating points [??]. This last approach 24 leads to an overestimation of the WHRS performance [?] and therefore of 25 the fuel economy. In [?] different concepts are analyzed taking into ac-26 count the system integration into the vehicle cooling module. The concepts 27 differ in the number of heat sources used and the temperature level of the 28 cooling fluid. Each is simulated on different steady state engine operating 29 points and the fuel economy is calculated taking into account the increase 30 in cooling fan consumption, exhaust back pressure or intake manifold tem-31 perature. Depending on the Rankine configuration and the location of the 32 condenser, improvements from 2.2% (recovering heat only from exhaust gases 33

and condenser placed in front of the cooling package) to 6.9% (exhaust gas 34 recirculation and exhaust heat are recovered and condenser is fed with engine 35 coolant) are achieved. In [?], dynamic fuel economy is evaluated on a light 36 duty vehicle taking into account the main penalties induced by the integra-37 tion of the WHRS. Fuel savings from 3.4% to 1.3% are presented depending 38 on the level of integration of the system into the vehicle architecture. How-39 ever, no optimization is proposed either on the system architecture or on the 40 condenser integration into the cooling package. 41

This paper is organized as follows. The second section explains the different considerations to take when designing a Rankine cycle for a HD application. In the third section, the different models used in the rest of the study are explained. In the fourth section, the scope of the study and the different methodologies are explained. In the fifth section, simulation results are analyzed and possible improvements are proposed. Finally, conclusions are drawn and directions for future research work are discussed.

49 2. DESIGN ASPECTS TO CONSIDER

Figure 1 shows a simple waste heat recovery system mounted on a 6 cylinder heavy duty engine. Working fluid flows through four basic components which are: the pump, the evaporator linked to the heat source, the expansion machine and the condenser linked to the heat sink. For sake of clarity, the link between the expander and the engine driveline is represented by a dashed line since it can be either mechanical or electrical (by coupling a generator to the expansion machine and reinject the electricity on the on board network).

58 2.1. Working fluid choice

There are several aspects to take into account when choosing a working 59 fluid for this application. Unlike stationary power plants where the main 60 consideration is the output power or the efficiency, here other aspects have to 61 be considered such as fluid deterioration, environmental aspects or freezing. 62 Up to now, several studies have tried to identify the ideal fluid for WHRS 63 [? ? ?] but no single fluid has been found. Recently, new performance 64 indicators have been introduced [??], where cost and design issues enter 65 into consideration. 66



Figure 1: Simple waste heat recovery Rankine based system

67 2.2. Heat sources

On a commercial vehicle, a certain number of heat sources can be found such as exhaust gases, cooling water or engine oil. These ones have several grade of quality (temperature level) and quantity (amount of energy). If the number of heat sources often yields higher fuel savings, it also brings more complexity and more challenges for the design of the system (fluid, expansion machine, control).

74 2.3. Heat sink

On a HD Truck, the only heat sink available is the vehicle cooling package which is a module including radiators for the compressed air and the engine coolant and cooled down by means of the ram air effect and the cooling fan. Integration of a WHRS into the cooling module results on a higher load on the latter and limits the amount of waste heat that can be converted into useful work. As such, complete system analysis is necessary to find the optimal way of recovering heat from a vehicle.

82 2.4. Subsystem interaction

The engine operation is influenced by the introduction of a WHRS. For ex-83 ample, as the WHRS shares the cooling system of the vehicle, the charge air 84 cooling capacity can be lower, which has a negative behavior on the engine 85 performance. Another example is the use of exhaust gas recirculation (EGR) 86 as heat source. This leads to a trade-off between EGR cooling and Rank-87 ine cycle performance, which could impact negatively the engine emissions. 88 Several other interactions such as the exhaust back pressure or the weight 89 penalty could be cited. 90

91

The WHRS performance, and so the fuel economy induced by this later, is then dependent on all these aspects. It is therefore critical to model the complete system and its environment in order to optimize its architecture. It helps to select the best design and reduce the number of experimental tests to carry out.

97 3. RANKINE MODELING

98 3.1. Rankine process

⁹⁹ The Temperature Entropy (T-s) diagram represented in figure 2 shows the ¹⁰⁰ associated state changes of the working fluid through the Rankine cycle:

- The pressure of the liquid is increased by the pump work up to the evaporating pressure $(1 \rightarrow 2)$.
- The pressurized working fluid is pre-heated $(2 \rightarrow 3a)$, vaporized $(3a \rightarrow 3b)$ and superheated $(3b \rightarrow 3c)$ in a heat exchanger, by recovering heat (\dot{Q}_{in}) from the heat source.
- The superheated vapor expands from evaporating pressure to condensing pressure $(3c \rightarrow 4)$ in an expansion device creating mechanical power (\dot{W}_{out}) .
- The expanded vapor condenses $(4 \rightarrow 1)$ through a condenser (linked to the heat sink) releasing heat (\dot{Q}_{out}) .



Figure 2: Temperature-Entropy diagram of the Rankine cycle

In this process the changes of states in both the pump and the expander are 111 irreversible and increase the fluid entropy to a certain extent. To correctly 112 assess the performance of a system based on the Rankine cycle, two different 113 models have been developed: a simple 0D steady state model based on the 114 enthalpy change that undergoes the working fluid which does not intend to 115 represent components performance and where the dynamic is not taken into 116 account and a second, based on conservation principles applied on one spatial 117 dimension. This is required to represent real performance of the components 118 constituting the system either in steady state or in transient. 119

120 3.2. 0D steady state modeling of a Rankine cycle

In order to simulate a high number of working fluids, a 0D model of a Rankine 121 cycle using one heat source is developed. It does not represent a real system 122 but it allows a fast assessment of a various number of working fluids. It 123 helps to select the suitable working fluids for the studied application. This 124 model is based on the enthalpy changes in the process described in section 125 3.1. This model is able to perform either subcritical or supercritical cycle, 126 which avoids the vaporization process and leads to a smaller system and a 127 better heat recovery process [?]. Those relations are verified as long as 128

the heat losses in the system and in the components are neglected. The 0Dmodel used is given by the system of equations (1):

$$\begin{split} P_{cond} &= P_{sat}(T_{cond}), \\ P_{fin,pump} &= P_{cond}, \\ T_{fin,pump} &= T_{sat}(P_{fin,pump}) - \Delta T_{subcooling}, \\ h_{fin,pump} &= m(T_{fin,pump}, P_{fin,pump}), \\ s_{fin,pump} &= n(T_{fin,pump}, P_{fin,pump}), \\ P_{fout,pump} &= P_{evap}, \\ h_{fout,pump} &= h_{fin,pump} + \frac{(h_{fout,pump_{is}} - h_{fin,pump})}{\eta_{pump_{is}}}, \\ T_{fout,pump} &= T(h_{fout,pump}, P_{fout,pump}), \\ s_{fout,pump} &= s(h_{fout,pump}, P_{fout,pump}), \\ s_{fout,pump} &= n_{fout,pump}, P_{fout,pump}), \\ P_{fout,boiler} &= P_{fout,pump}, P_{fout,pump}), \\ P_{fout,boiler} &= h_{fout,pump}, P_{fout,boiler}), \\ s_{fout,boiler} &= s(h_{fout,pump}, P_{fout,boiler}), \\ s_{fout,boiler} &= s(h_{fout,boiler}, P_{fout,boiler}), \\ P_{fout,exp} &= P_{cond}, \\ h_{fout,exp} &= h_{fout,boiler} + (h_{fout,boiler} - h_{fout,exp_{is}})\eta_{exp_{is}}, \\ s_{fout,exp} &= s(h_{fout,exp}, P_{fout,exp}), \\ P_{fout,cond} &= P_{fout,exp}, \\ T_{fout,cond} &= r_{sat}(P_{fout,cond}) - \Delta T_{subcooling}, \\ h_{fout,cond} &= h(T_{fout,cond}, P_{fout,cond}), \\ s_{fout,cond} &= s(h_{fout,cond}, P_{fout,cond}). \end{split}$$

where

In table 1 one can find the simulation model parameters, and the abbrevia-tions are given in the appendix.

In addition to that, a routine verifying that the pinch point (*PP*) is respected
during the evaporation process.

Model parameters	Variable in (1)	unit	value
Pump isentropic efficiency	$\eta_{pump_{is}}$	%	65
Expander isentropic efficiency	$\eta_{exp_{is}}$	%	70
Maximum evaporating pressure	P_{evap}	bar	40
Minimum condensing pressure	P_{cond}	bar	1
Maximum pressure ratio	$\frac{P_{evap}}{P_{cond}}$	-	40:1
Pinch points HEX	PP	Κ	10
Pressure ratio among HEX	$\frac{P_{f_{out,boiler}}}{P_{f_{out,pump}}}$	-	1
Minimum quality after expansion	$x_{f_{out,exp,min}}$	-	0.9

Table 1: 0D model parameters

Refprop database [?] is used to compute the following quantity: h, s, T, P_{sat} and T_{sat} . Input variables of the model (1) are the gas mass flow and temperature (denoted by \dot{m}_{gas} and $T_{gas_{in,boiler}}$) entering in the system and the condensing temperature (T_{cond}). Outputs of the model are the power produced by the expansion \dot{W}_{exp} , the power consummed by the compression \dot{W}_{pump} and the net output power NOP which are defined as:

$$\begin{cases} NOP = \dot{W}_{exp} - \dot{W}_{pump}, \\ \dot{W}_{exp} = \dot{m}_f * (h_{f_{in,exp}} - h_{f_{out,exp}}), \\ \dot{W}_{pump} = \dot{m}_f * (h_{f_{in,pump}} - h_{f_{out,pump}}). \end{cases}$$

$$(3)$$

The model 1 is not dynamic and does not represent any real components
performance. A dynamic 1D model is therefore developed to evaluate the
system performance on more realistic dynamic driving conditions.

¹⁴⁴ 3.3. 1D dynamic modeling of a Rankine cycle

145 3.3.1. Tank

The reservoir is modeled by a fixed volume, which can be either vented to the atmosphere or be hermetic (depending on the condensing pressure) in order to avoid sub atmospheric conditions. Mass and energy conservation 149 equations are:

$$\begin{cases} \dot{m}_{f_{out,tank}} - \dot{m}_{f_{in,tank}} &= \frac{\partial m_{f_{tank}}}{\partial t}, \\ \dot{m}_{f_{in,tank}} h_{f_{in,tank}} - \dot{m}_{f_{out,tank}} h_{f_{out,tank}} &= m_{f_{tank}} \frac{\partial h_{f_{tank}}}{\partial t}. \end{cases}$$
(4)

150 3.3.2. Working fluid pump

The working fluid pump is simply represented by a fixed displacement and isentropic efficiency. The volumetric efficiency is a function of the outlet pressure. This law is identified thanks to experimental data:

$$\dot{m}_{f_{out,pump}} = \rho_{f_{in,pump}} \frac{N_{pump}}{60} C_{c_{pump}} \eta_{pump_{vol}}.$$
(5)

The outlet enthalpy is calculated as shown in the equation for $h_{f_{out,pump}}$ in the 0D model (1).

153 3.3.3. Heat exchangers: Evaporator(s) and condenser(s)

The models are developed to dynamically predict temperature and enthalpy 154 of transfer and working fluid at the outlet of each heat exchanger (HEX). 155 When coming to dynamic models of those components, two methodologies 156 can be found in the literature: moving boundary (MB) and finite volume 157 (FV) models. Usually more complex in terms of computational capacity 158 needed due to the high number of system states, the FV approach has the 159 advantage to be more powerful and robust concerning the prediction. Both 160 approaches have been widely used in large power recovery system and control 161 system design [????] and results in a simplification of the heat recovery 162 boiler/condenser geometry in a great extent (i.e. by representing the boiler 163 by a straight pipe in pipe counterflow heat exchanger). In this study, the FV 164 approach is preferred since it easily handles starting and shut down phases 165 [?] when only few papers addressed those cases with a MB approach [?]. 166 167

Model assumptions. Several assumptions are done to simplify the problem in a great extent. These ones are usually admitted when coming to heat exchanger modeling [? ?]:

- The transfer fluid is always considered in single phase, i.e. no condensation in the EGR/exhaust gases is taken into account.
- The conductive heat fluxes are neglected since the predominant phenomenon is the convection.
- All HEX are represented by a straight pipe in pipe counterflow heat exchanger of length L.
- Fluid properties are considered homogeneous in a volume.
- Pressure dynamics is neglected since it is very fast compared to those
 of heat exchanger.

Governing equations. Boiler(s) and condenser(s) models are based on mass
 and energy conservation principles.

• Working fluid (internal pipe):

$$\begin{cases} A_{cross_f} \frac{\partial \rho_f}{\partial t} + \frac{\partial \dot{m}_f}{\partial z} = 0, \\ A_{cross_f} \frac{\partial \rho_f h_f}{\partial t} + \frac{\partial \dot{m}_f h_f}{\partial z} + \dot{q}_{conv_{fint}} = 0, \\ \dot{q}_{conv_{fint}} = \alpha_f P e_{exch_f} (T_f - T_{wall_{int}}). \end{cases}$$
(6)

• Internal pipe wall: An energy balance is expressed at the wall between the working fluid and the gas and is expressed as follows:

$$\dot{Q}_{conv_{f_{int}}} + \dot{Q}_{conv_{g_{int}}} = \rho_{wall} c_{p_{wall}} V_{wall_{int}} \frac{\partial T_{wall_{int}}}{\partial t}.$$
(7)

• Gas side (external pipe): The energy conservation is then formulated under the following form:

$$\rho_g A_{cross_g} c_{p_g} \frac{\partial T_g}{\partial t} + c_{p_g} \dot{m}_g \frac{\partial T_g}{\partial z} + \dot{q}_{conv_{g_{int}}} + \dot{q}_{conv_{g_{ext}}} = 0, \qquad (8)$$

183 184 where the convection on the external side is used to represent the heat losses to the ambient.

• External pipe wall: As for the internal pipe an energy balance is expressed between the gas and the ambient:

$$\dot{Q}_{conv_{g_{ext}}} + \dot{Q}_{conv_{amb_{ext}}} = \rho_{wall} c_{p_{wall}} V_{wall_{ext}} \frac{\partial T_{wall_{ext}}}{\partial t}.$$
(9)

In equation (7) and (9) the convection heat flow rate (\dot{Q}_{conv}) is expressed as:

$$\dot{Q}_{conv_{j_k}} = \alpha_j A_{exch_{j_k}} (T_{wall_k} - T_j),$$
where $j = g, f, amb$
and $k = int, ext.$
(10)

Furthermore, to complete the system, one need boundary and initial conditions. Time-dependent boundary conditions are used at z = 0 and z = L(t > 0):

$$\dot{m}_f(t,0) = \dot{m}_{f_0}(t),$$
(11)

$$h_f(t,0) = h_{f_0}(t),$$
 (12)

$$\dot{m}_g(t,L) = \dot{m}_{g_L}(t), \tag{13}$$

$$T_g(t,L) = T_{g_L}(t).$$
 (14)

The initial conditions for the gas and wall temperatures and working fluid enthalpy are given by $(z \in [0, L])$:

$$h_f(0,z) = h_{f_{init}}(z),$$
 (15)

$$T_{wall_{int}}(0,z) = T_{wall_{int_{init}}}(z), \qquad (16)$$

$$T_g(0,z) = T_{g_{init}}(z), \qquad (17)$$

$$T_{wall_{ext}}(0,z) = T_{wall_{ext_{init}}}(z), \qquad (18)$$

Heat transfer and pressure drop. To model the convection from the transfer fluid to the pipe walls and from the internal pipe to the working fluid, a heat transfer coefficient (α) is needed. The convection from a boundary to a moving fluid is usually represented by the dimensionless number Nusselt (Nu) which is the ratio of convective to conductive heat transfer.

$$Nu(\alpha) = \frac{\alpha l}{\lambda},\tag{19}$$

where *l* represents a characteristic length and is, in this case, the hydraulic diameter. Numerous correlations to approach this number can be found in the literature and are usually derived from experiments, see for example [?]. In single phase, the Gnielinski correlation is chosen for both fluids. In two phase, Chen (for evaporation) and Shah (for condensation) correlations are used. Pressure drop in both fluids are taken into account in order to simulate

the real performance of the system. The pressure drop can be split into three main contributors:

$$\Delta P = \Delta P_{static} + \Delta P_{momentum} + \Delta P_{friction}, \tag{20}$$

where the static pressure drop (ΔP_{static}) is function of the change in static head (i.e. the height), the momentum pressure drop $(\Delta P_{momentum})$ depends on the change on density during phase change and the friction contribution $(\Delta P_{friction})$ is function of the speed of the fluid and the considered geometry. Table 2 shows the different correlations used depending on flow conditions. In laminar single phase, the assumption of a constant heat flux at the wall is made.

		Laminar	Turbulent
	Single phase	Nu = 4.36	Gnielinski
Heat transfer	Two phase evaporation	Chen	Chen
	Two phase condensation	Shah	Shah
Pressure drop	Single phase	Poiseuille	Blasius
	Two phase	Friedel	Friedel

Table 2: Correlations used in HEX

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198 3.3.4. Valve(s)

The fluid flow \dot{m} through the value is modeled using a compressible value equation of the form:

$$\dot{m}_{f_{in,v}} = C_{d_v} S_{eff_v} \sqrt{\rho_{f_{in,v}} P_{f_{in,v}} \phi}, \qquad (21)$$

¹⁹⁹ where the compressibility coefficient ϕ is defined as:

$$\phi = \frac{2\gamma_f}{\gamma_f - 1} (\varphi^{\frac{2}{\gamma_f}} - \varphi^{\frac{\gamma_f + 1}{\gamma_f}}), \qquad (22)$$

with

$$\varphi = \begin{cases} \frac{P_{f_{out,v}}}{P_{f_{in,v}}} & \text{if } \frac{P_{f_{out,v}}}{P_{f_{in,v}}} > \frac{2}{\gamma_f + 1} \frac{\gamma_f}{\gamma_{f-1}} \\ \frac{2}{\gamma_f + 1} \frac{\gamma_f}{\gamma_{f-1}} & \text{if } \frac{P_{f_{out,v}}}{P_{f_{in,v}}} \le \frac{2}{\gamma_f + 1} \frac{\gamma_f}{\gamma_{f-1}}, \end{cases}$$
(23)

where γ_f is the ratio of the specific heats of the working fluid and depends on the temperature and the pressure. Equation (23) means that the parameter φ is either the pressure ratio if the flow is subsonic or the critical pressure ratio when the flow is supersonic.

204 3.3.5. Expansion machine

Several studies have been carried out in order to choose the correct expansion machine for Rankine based recovery system [??]. In most of them where vehicle installation is considered, turbine expanders are preferred for their compactness and their good performance [??] since the major advantage of volumetric expander such as piston machines is the expansion ratio [?]. Though, recent study [?] has shown turbine with expansion ratio over 40:1 on a single stage with really good performance at tolerable speed for a vehicle installation. In this study, only a kinetic expander is modeled. The turbine nozzle is represented by the following equation:

$$\dot{m}_{f_{in,exp}} = K_{eq} \sqrt{\rho_{f_{in,exp}} P_{f_{in,exp}} \left(1 - \frac{P_{f_{in,exp}}}{P_{f_{out,exp}}}\right)^{-2}}.$$
(24)

²⁰⁵ And the isentropic efficiency is calculated according to the following relation:

$$\eta_{exp_{is}} = \eta_{exp_{is_{max}}} \left(\frac{2c_{us}}{c_{us_{max}}} - \frac{c_{us}}{c_{us_{max}}}^2 \right), \tag{25}$$

where

$$c_{us} = \frac{u}{c_s} = \frac{\omega_{exp} R_{exp}}{2\sqrt{h_{f_{in,exp}} - h_{f_{in,exp_{is}}}}}.$$
(26)

Model parameters are fitted using data from supplier and similarity relation [?].

$_{208}$ 3.3.6. Other heat exchanger(s)

In order to describe the vehicle cooling system, the number of transfer unit (NTU) approach is used. It is commonly adopted when it comes to single phase heat exchanger modeling. For an air cooled radiator the following relations are used:

$$\dot{Q}_{air} = \dot{m}_{air} c_{p_{air}} \varepsilon (T_{coolant_{in}} - T_{air_{in}}).$$
⁽²⁷⁾

For a given geometry, ε can be calculated using correlations based on the heat capacity ratio. By considering parallel flow configuration for the radiators, the effectiveness can be written:

$$\varepsilon = \frac{1 - e^{-NTU\left(1 + \frac{(\dot{m}c_p)_{min}}{(\dot{m}c_p)_{max}}\right)}}{1 + \frac{(\dot{m}c_p)_{max}}{(\dot{m}c_p)_{max}}},$$
(28)

with
$$NTU = \frac{UA}{(\dot{m}c_p)_{min}}$$
. (29)

212 3.3.7. Coolant pump and fan

The coolant pump model used is a map-based model function of engine speed and pressure rise. This one is sized to deliver enough subcooling even at high engine load. The engine fan is also a map-based model delivering a given mass flow at a given speed. The fan consumption is calculated according to:

$$\dot{W}_{fan} = C_{fan} \ \rho_{air} N_{eng} G_{ratio} N_{fan}^2, \tag{30}$$

where the coefficients C_{fan} and G_{ratio} are dependent on the fan model and vehicle. The mass flow rate blown by the fan is mapped according to data from supplier and depends on the fan speed and atmospheric conditions. The air mass flow rate going through the cooling package (\dot{m}_{air}) is a combination of the natural air mass flow rate (corresponding to a fraction of the vehicle speed) and the forced mass flow rate (corresponding to the mass flow blown by the fan).

$$\dot{m}_{air} = \rho_{air} A_{cool \ pack} Sr_{air} V_{vehicle} + \dot{m}_{fan} (N_{fan}, \rho_{air}), \tag{31}$$

where Sr_{air} is the ratio between the vehicle speed and the air speed in front of the cooling package and is either calculated via CFD or measured in a wind tunnel.

216 4. SYSTEM OPTIMIZATION

217 4.1. Key aspects

²¹⁸ In this section, the degrees of freedom used to optimize the WHRS are de-²¹⁹ tailed:

220 221 222 223	1.	<u>Fluid choice</u> : the fluid selection is a critical part of the system opti- mization. The correct fluid choice has to match both heat source and cold sink in order to generate as much power as possible [??]. From environmental and legal points of view, the working fluid has to respect:
224 225 226		• Its chemical class: chlorofluorocarbons (CFCs) have been ban- ished by the Montreal Protocol and hydrochlorofluorocarbons (HCFCs) production is planned to be phased out by 2030.
227 228		• Its presence on the global automotive declarable substance list (GADSL).
229 230		• Its chemical properties such as the global warming potential (GWP), the ozone depletion potential (ODP) or the risk phrases (R-phrases).
231 232		• Its classification according the national fire protection agency (NFPA) 704 classification (ranking above 1 in Health or Instability class)
233		In top of that, the freezing point which has to be below 0 $^{\circ}$ C.
234 235 236 237 238 239 240 241 242 243 244 245 246 247	2.	Components choice and design: the correct choice of components and particularly the expansion machine have an important impact on the system performance and the control design. Indeed, a volumetric ex- pander is less stringent in terms of degree of superheat and tolerate a given amount of liquid during the expansion process whereas a kinetic expander requires a higher degree of superheat in order to have a full vapor expansion (liquid droplets can cause blade erosion and broke the machine). The design of all other components of the Rankine system is also critical to maximize its potential. For example, too big heat exchangers show higher performance but also inertia which could be a disadvantage when coming to highly dynamic driving cycle since the more interesting points (i.e. high load engine operating points) are not lasting for long. A heavy evaporator is therefore not catching up the maximum potential of this high heat flow rate.
248 249 250 251 252 253	3.	Heat sources and sinks arrangement: the architecture of sources and sinks has to be adapted to increase overall performance. Heat sources choice and arrangement impact a lot the system performance by changing the heat input to the system. The cold sinks choice is influencing the condensing pressure so the overall pressure ratio (and therefore the power generated by the expander).

4. Other system interactions: as the final goal is to implement the system in a heavy duty vehicle, the WHRS must be considered not as a standalone system but as a connected sub system of the complete vehicle. The interactions of the Rankine system on the other sub-systems have to be taken into account (e.g. increase in fan consumption due to the heat rejection coming from the condenser).

260 4.1.1. Investigated architectures and components

Several studies have been conducted in the field of waste heat recovery Rankine based systems for mobile applications. A screening of the different heat sources available is reported in [?] and shows that the most promising ones are the EGR and the Exhaust streams. In the present study, only these two heat sources are considered since they present the higher grade of temperatures among other sources. Therefore four different Rankine layout are studied:

1. Exhaust recovery only where the only heat source are the exhaust gases.



Figure 3: Exhaust only system schematic

269
 2. EGR recovery only where only the EGR gases are used as the only heat
 270 source.



Figure 4: EGR only system schematic

- 3. Both sources in parallel where the working fluid is split into two streams 271 heated up separately by each source and then mixed before the ex-272 pander.
- 273



Figure 5: Exhaust and EGR in parallel system schematic

4. EGR and exhaust in series where the EGR gases are used to preheat 274 the fluid and the exhaust gases to vaporize and superheat. Using the 275 EGR as a preheater, instead of a superheater, is chosen to lower the 276 EGR gases temperature after the evaporation process. 277



Figure 6: Exhaust and EGR in series system schematic

- ²⁷⁸ Coupled to that, two different cooling architecture are approached:
- A first one (called in the following Cooling Config 1) which uses a low temperature radiator dedicated to the Rankine condenser and is placed between the charge air cooler (CAC) and the engine radiator.



Figure 7: Cooling config 1

• A second one (called in the following Cooling Config 2) using the engine

coolant as heat sink for the Rankine cycle. In that case, a derivation
of the coolant is done in front of the engine to benefit from the lowest
temperature grade.



Figure 8: Cooling config 2

Concerning the components, as previously said, the study is limited to one expansion machine technology: turbine expander. For the heat exchangers (evaporator(s) and condenser), only counter-current configurations which are usually used in this kind of applications [?] are considered.

290 4.2. Duty cycles

Driving conditions are acting as input disturbances and therefore, their impact on the target performance must be studied with care.

293 4.2.1. Steady state evaluation

²⁹⁴ Under steady state driving conditions, the performance is evaluated by ex-²⁹⁵ pressing the weighted average net output power of the 1D model (3.3) (the ²⁹⁶ NOP, which is the additional power that the engine receives, therefore cor-²⁹⁷ responds to the fuel economy) on 13 engine operating points (summarized

		Vehicle	EGR	EGR	Exhaust	Exhaust	Weight
	Name	speed	mass	tempe-	mass	tempe-	factor
			flow	rature	flow	rature	
	Parameter	$V_{vehicle}$	\dot{m}_{egr}	T_{egr_0}	\dot{m}_{exh}	T_{exh_0}	w_i
	Unit	km/h	g/s	$^{\circ}C$	g/s	$^{\circ}C$	%
1		20	31.5	263.1	78.7	237.9	6.9
2		85	38	409.5	119.8	338.2	9.0
3		60	59.5	635.0	309.3	443.9	4.9
4		85	54.6	544.0	252.4	413.0	2.6
5		75	46.1	454.0	154.6	366.4	18.9
6		85	56.3	247.5	85.7	212.5	10.5
7		30	85.9	631.0	352.7	425.1	2.8
8		85	69.4	562.5	290.5	405.5	3.6
9		50	58	473.0	183.2	336.2	12.7
10		85	59.8	251.0	95.2	216.0	11.2
11		45	87.1	581.0	326.8	400.8	2.3
12		75	68.9	472.0	198.4	359.6	10.7
13		85	62.9	252.5	102.8	217.5	3.9

Table 3: Steady state evaluation: Driving conditions and weight for 13 engine operating points

in table 3) These operating points are chosen to represent a classical long haul driving cycle and weighted according to the percentage of energy used on each operating point. Operating point number 5 is identified as the designing point whereas the operating points 3 and 11 are considered critical due to the high engine load and the low vehicle speed.

303 4.2.2. Dynamic evaluation

In order to accurately assess the potential of the WHRS, dynamic driving cycles are also used to complete the study and check whether the performance found with the previous method is correct. This is really important when coming to thermal systems performance estimation since they generally have long response time [?]. The driving cycle used is split into 7 phases (summarized in table 4) supposed to represent all conditions of a long haul truck usage.

Driving cycle	1	2	3	4	5	6	7
Road Type	Extra	Highway	Highway	Extra	Extra	Extra	Rolling
	urban			urban	urban	urban	
Vehicle speed	Medium	High	Medium	Low	Medium	High	High
Weight factor w_i (%)	10	10	50	7.5	10	7.5	5

Table 4: Dynamic evaluation: Driving conditions and weight for the 7 phases

In the previous 1D model (3.3), each phase is considered, in the rest of the study, as a driving cycle of approximately the same length (denoted by a number from 1 to 7) and weighted according to their real life importance (for a long haul truck highway is predominant).

315 4.3. System performance evaluation

The criterion used for the performance evaluation under steady state and dynamic driving conditions, is the total net reinjected power to the conventional driveline. This is done by taking into account the producer (WHRS expander) and different consumers (cooling fan, WHRS pump and WHRS coolant pump) and assuming them to be mechanically driven (this is not always true for the pumps but efficiencies are detuned to take into account the mechanical to electrical conversion). A complete vehicle model integrating engine, EATS, transmission, cooling package, WHRS and road environment is used to simulate the total vehicle approach and calculate the power needed to drive the vehicle. The performance criterion (PC) is then calculated as the ratio of this reinjected power to the engine power:

$$PC_{i} = \int_{t_{init}}^{t_{final}} \frac{\dot{W}_{exp} - \dot{W}_{pump} - \dot{W}_{cool,pump} - \dot{W}_{fan}}{\dot{W}_{eng}},$$
(32)

where the engine power (\dot{W}_{eng}) taking into account the mechanical auxiliaries consumption mounted on it and the increase in exhaust backpressure (due to the exhaust evaporator). The vehicle gross weight is assumed constant and equal to 36 tons which intends to represent the average load on a long haul truck. The performance criterion (*PC*) over the different steady state operating points or driving cycles is then calculated by summing the weighted PC on each points/cycles:

$$PC = \sum_{i=1}^{k} w_i PC_i, \tag{33}$$

where $k \in [1 \ 13]$ for steady state evaluation (presented in section 4.2.1) and $k \in [1 \ 7]$ for evaluation on dynamic driving cycle (presented in section 4.2.2).

318 5. RESULTS AND DISCUSSION

319 5.1. 1D model validation

In this section some component models, judged as critical for the overall 320 system performance evaluation, are first validated thanks to supplier or ex-321 perimental data. The different studied configurations being made of the same 322 components model it has been decided to validate the models components by 323 components. The validation is done by comparing experimental to the mod-324 eling results. A model is further considered as valid if the average modeling 325 error is below 5% of the predicted quantity. Since the main dynamic of the 326 system is contained in the evaporators [?] and the final aim is to predict 327 the power generated by the system only validation figures are presented for 328 the evaporators and the expansion machine. It should be said that a more 329 detailed validation on the whole system mounted on the vehicle should be 330 carried out but this requires the system to be built. Unfortunately this tech-331 nology is still under investigation at the truck makers level and no figures 332 are available yet. This study intends then to compare the architecture and 333 analyze their impact on the truck fuel consumption. 334

335 5.1.1. Heat exchangers

A high attention is paid to the evaporators in order to accurately predict the steady state and dynamic performance of those components (corresponding to the model presented in section 3.3.3). In this paper, a finite volume approach has been chosen to implement the continuous set of equations (equations 6, 7, 8, 9). Figure 9 shows the schematic of the discretized model.

Table 5 and 6 show respectively steady state and dynamic prediction errors. Note that in both cases the relative error is computed according to the maximum temperature difference between the heat exchanger bounds (usually



Figure 9: HEX model schematic

 $T_{g_L} - T_{f_0}$). The steady state validation is conducted on a lot of operating conditions supposed to represent the complete range of operation for those components. The dynamic behavior is evaluated on different load point variations but obviously need further validation especially on fast change that can take place on real driving conditions. However, the mean relative modeling error remains lower than 3.5%, which is considered acceptable.

	T_{f_L}	$T_{f_{L_{EGRB}}}$		$T_{f_{L_{ExhB}}}$		$T_{egr_{0}_{EGRB}}$		$T_{exh_{0}_{ExhB}}$	
Error	\max	mean	\max	mean	\max	mean	\max	mean	
Absolute (K)	2.95	1.30	9.15	4.16	7.54	2.54	15.47	4.71	
Relative (%)	0.57	0.29	8.84	3.28	2.34	0.61	8.61	3.40	

Table 5: Evaporators steady state validation

	T_{f_L}	EGRB	T_{f_L}	ExhB	T_{egr}	G_{EGRB}	T_{exh}	$v_{0_{ExhB}}$
Error	\max	mean	\max	mean	\max	mean	\max	mean
Absolute (K)	4.5	1.5	25.9	2.3	7.9	2.8	20	4.2
Relative (%)	1.38	0.46	14.37	1.28	2.43	0.86	11.1	2.33

Table 6: Evaporators dynamic validation

350 5.1.2. Expansion machine

The turbine expander model presented in 3.3.5 is fitted thanks to supplier data. Figure 10 and 11 respectively show the working fluid inlet pressure and the generated power predicted by the model versus the normalized working fluid mass flow entering in the turbine. Those two quantities are well fitted and this model is further considered validated.



Figure 10: Turbine pressure model validation



Figure 11: Turbine power model validation

356 5.1.3. Model analysis

The whole 1D models are built from the same component models. The iner-357 tial effect of the pipes are neglected since their effect are negligible compared 358 to the other components dynamics (namely the evaporators) [?]. The full 359 model is then a combination of validated detailed models (e.g. heat exchang-360 ers) and quasi-static models (pumps expansion machine and fan) used for 361 comparison purpose. This study then intends to compare the different heat 362 sources and sinks configurations possible on a heavy duty vehicle to select 363 the best system in terms of performance. 364

³⁶⁵ 5.2. Optimization of the WHRS

366 5.2.1. Working fluid selection

From an exhaustive fluid list [?], all those that do not respect the different 367 criteria mentioned in 4.1 have been removed. However, as water is a good 368 reference fluid since it is generally used in power plant [?], it has been kept. 369 The results presented hereafter are coming from the ideal thermodynamic 0D 370 model presented in section 3.2 where all 13 operating points are simulated for 371 two condensing temperatures 60° C and 90° C, which intends to represent the 372 two cooling configurations presented in the previous section. The parameters 373 of the cycle, $P_{f_{out, pump}}$ and \dot{m}_f are optimized to reach the highest performance 374 (i.e. maximize the NOP). Here, each hot stream is simulated separately in 375 order to see the impact of the heat source on the Rankine fluid selection. The 376 simulation matrix contains 13 operating points (listed in section 5.2.2) and 377 13 selected working fluids. For the sake of simplicity, the results presented 378 in figure 12 show the number of occurrences where the fluid is in the top 379 five ¹ regarding the NOP. When analyzing each operating point and config-380 uration separately among the 13x13 simulations, water is the best fluid for 381 heavily loaded operating points. For low and medium engine load, as gases 382 temperatures are lower and due to the large enthalpy of vaporization of water 383 and the high level of superheating required, it is not recommended to use it. 384 Acetone and ethanol show good performance at mid and high engine load no 385 matter of the cold sink temperature. Refrigerants such as R1233zd or Novec 386

 $^{^{1}}$ top five means the NOP related to the fluid is ranked in one of the five first position

649 show good results for heat source temperature under 280 °C for the lowest condensing temperature. More exotic fluids such as cis-butene or MM (silicon oil) could be attractive for low and medium engine load respectively at 60°C condensing temperature for the first one and 90°C for the second one.



Figure 12: Number of occurrences of each fluid in top five 1 for different boundary conditions

391

These first simulations results limit the number of investigated working fluids 392 for the remaining part of this paper to the following ones: Acetone, Ethanol. 393 Those two fluids represent the highest number of occurrences for the differ-394 ent configurations considered. As these fluids have similar volumetric flows 395 it would be possible to use the same components' characteristics with only 396 some minor changes (e.g. throat diameter for the turbine model and pump 397 displacement). However due to the low flash point of Acetone (-20°C) only 398 ethanol is then considered suitable for a mobile application. 390

400 5.2.2. Steady state performance analysis

Now, the performance criterion is analyzed on the 13 operating points and
the 2 cooling architectures (Cooling config 1 and 2) for the previously chosen working fluids. The savings are computed thanks to the weight factors
presented in table 3. Figure 13 presents the NOP to engine power ratio evaluated for the 2 cooling configurations. It can be observed that the decrease

due to higher condensing temperatures induced by cooling configuration 2 is 406 somehow constant (between 11 and 15 %) no matter of the Rankine cycle 407 arrangement. This drop in performance is due to the increase in condensing 408 pressure which affects the overall pressure ratio through the expansion ma-409 chine and therefore its performance. This could be partially balanced by a 410 specific design of the expansion machine in order to have a variable nozzle ge-411 ometry that keeps the pressure ratio constant when the condensing pressure 412 increases. A similar approach is done in [?] to adapt the nozzle geome-413 try to the mass flow entering in the turbine. With those components, the 414 parallel arrangement of the heat sources gives the best PC, followed by the 415 serial one, the exhaust only and the EGR recovery. However the difference 416 between series and parallel layout is not so important and the lower number 417 of values needed by the first one could compensate this drop in performance. 418 Moreover, in this configuration, as the working fluid mass flow is controlled 419 to get a superheated vapor state at the outlet of the tailpipe boiler the mass 420 flow rate is then higher than in any other configurations. It results into lower 421 EGR temperature which could be a benefit in terms of engine performance 422 and pollutant emission control [?]. Last but not least, with the EGR only 423 solution even if the weight and installation impact is low (the heaviest com-424 ponent is the EGR evaporator that replaces the traditional EGR cooler), 425 the PC seems too low for a vehicle installation. This obviously needs further 426 analysis taking into account also the cost impact of each solution on the total 427 cost of ownership. 428

429 5.2.3. Dynamic performance analysis

Then, in order to validate the previously used method, dynamic simulations 430 are run to further assess the performance criterion of the WHRS. Indeed, 431 as previously said, the Rankine based recovery systems could have long time 432 constant due to the boiler(s) inertia (wall capacity). This could help in terms 433 of control by filtering some high transient of the heat sources but reduce the 434 heat transferred to the fluid, since only a fraction of the heat contained in 435 the hot gases is then used. In the following, the performance is assessed on 7 436 different driving cycles (see table 4) representative of a long haul truck usage. 437 An example of two of those road profiles is presented in fig 14. 438

Each driving cycle is simulated separately starting from ambient conditions that can result in a lower PC due to the long warm up time of the exhaust



Figure 13: Steady state PC assessment

after treatment system (EATS). Weights (see 4) are applied to the different
driving cycles to calculate the total performance criterion of the WHRS.

Figures 15 and 16 show the *PC* reached by each Rankine configuration respectively for cooling configuration 1 and 2. As shown is 5.2.2 the decrease in performance using cooling configuration 2 rather than cooling configuration 1 is more or less constant and around 11%. The main information brought by this study remains the lower fuel savings when simulating the system in dynamic instead of steady state, which can be as big as 50% for the systems using exhaust as heat source. This is due to two main reasons:

- the exhaust after treatment system, which has a very important constant time, causes big temperature drop during fast highly loaded engine conditions where a lot of heat is supposed to be available.
- the non optimal design of the tailpipe boiler used in the simulation model. Indeed the validation of the model shown in section 5.1 is based on prototypes components that do not represent the optimum in terms of size and transient performance.
- the constraint implemented on the EGR temperature at the evaporator
 outlet not to derate the emission control. The maximum EGR temperature is set to 150 °C which on some phases is not going hand in hand
 with the superheat level control. The EGR temperature becomes the



Figure 14: Road profiles examples

control objective and when the superheat is not sufficient the expander
 is not fed with working fluid and therefore the power production is null.

Table 7 resumes the time (relative to the duty cylce time) where the superheat 463 is sufficient to feed the expansion vapor. Systems recovering heat from the 464 exhaust stream mainly suffer from a long start-up phase but then the system 465 never lose the superheat level needed to expand the working fluid in the 466 kinetic turbine. This long start-up is due to the boundary conditions used 467 where all the sub-systems initial temperatures are set to ambient. For the 468 system recovering heat only from the EGR the start-up is not significant since 469 on some cycles the system is generating power more than 99% of the time 470 (the EGR gets its normal operation temperature after few seconds whereas 471 the thermal inertia of the EATS makes the temperature rise very slow). 472 Nevertheless on highly loaded cycles (namely 3 and 7) the high engine load 473 results into high EGR temperature and to not interact too much with the 474 engine emissions system, the superheat is dropped to the detriment of the 475 EGR temperature. Superheated vapor is no longer generated by the boiler 476 and the fluid goes back to a diphasic state and the expansion machine is 477 bypassed. 478

Anyway, similarly to the previous results in steady state, the best system in
terms of fuel savings remains the EGR and exhaust in parallel with cooling
configuration 1 that brings 2.2% savings on the overall weighted driving cycle.

Driving cycle	Configuration	Exhaust	EGR	Serial	Parallel
1	-	93.37~%	99.11%	93.71%	93.93%
2		93.06%	99.30%	93.41%	93.25%
3		95.27%	83.38%	95.64%	95.44%
4		92.50%	93.37%	91.07%	92.06%
5		91.18%	97.26%	90.67%	91.55%
6		92.00%	98.30%	90.42%	91.46%
7		93.53%	88.94%	90.87%	92.92%

Table 7:	Vapor	creation	time	ratios	summary

⁴⁸² In addition to that, it can be seen that the relative performance are kept from arrangement to arrangement (compared to section 5.2.2).



Figure 15: PC for cooling configuration 1 over dynamic driving cycles

483

484 5.2.4. Optimal WHRS

The low performance figures presented in the previous sections are mainly due to non optimized components for the considered application. In order to evaluate what could be the economy brought by an optimized system, the different components constituting the WHRS are redesigned to perfectly match the targeted application. In addition to that, a perfect insulation of these



Figure 16: PC for cooling configuration 2 over dynamic driving cycles

different components is then considered. In this section, only cooling config-490 uration 1 is evaluated since it has been shown that it leads to larger savings. 491 Both approaches previously used (steady state and dynamic analysis) are 492 presented in figure 17. Optimization has been done on boilers and condenser 493 size with respect with the additional weight. Pump and expansion machine 494 performance are increased to reach standards in power plant Rankine cycles 495 $(\eta_{pump_{is}} = 70\%$ and $\eta_{exp_{is,max}} = 78\%)$. More acceptable results are reached 496 for a vehicle implementation of such a system, especially when considering a 497 system recovering from both EGR and exhaust in parallel. Again, a big step 498 is observed between the two evaluation methodologies which tends to prove 490 that the cycle division into a certain number of steady state engine operating 500 points is not adapted for performance evaluation of thermal systems which 501 generally have a long response time. 502

503 6. CONCLUSION

Performance simulations of different WHRS for heavy duty trucks application
was conducted to understand the potential of such a system in terms of fuel
consumption decrease. Two different methodologies are used and discussed.
Usually, only the first approach, which consists to split a driving cycle into
several steady state engine operating points, is used to assess the performance



Figure 17: PC for optimal sizing of the components

without any regards of the transient behavior of the different components 509 composing the WHRS [?]. The second one, where a total vehicle approach 510 is simulated over a wide variety of dynamic driving cycles representing the 511 usage of a long haul HD vehicle. In both methods architecture to architecture 512 ranking is the same which tends to prove that the first approach could be used 513 for qualitative but not quantitative study. Using the second approach results 514 into lower fuel savings and needs to be balanced in regards of the model 515 validation done based onto prototypes, which are not representing what could 516 be a mass-produced system. However, the absolute numbers should not be 517 interpreted as the maximal potential for WHRS in HD trucks, since transient 518 control of the system and components are not optimal. Different systems 519 layout have been analyzed to maximize the system performance over a broad 520 variety of driving cycles. However the results presented in this paper need to 521 be treated carefully and further completed with the cost and the packaging 522 effort for each configurations. An optimized scenario is also presented where 523 a specific attention has been paid to the components size and performance in 524 order to perfectly match the application. However fuel savings are rather low 525 compared to what can be found in the literature [??] and need to be further 526 validated by experimental results on a system mounted onto a vehicle. In 527 addition to that, control issues are not approached in this paper but remain 528 a big part of the system performance maximization. In this study, perfect 529 sensors and actuators are used, which reduce the control effort. Moreover, 530

actual mass-produced control units are not as powerful as current laptop CPU and reduce considerably the possibility in terms of advanced control algorithm development. Recent studies have brought significant advances in this field [???] but this still needs to be addressed when vehicle implementation is touched.

536 **REFERENCES**

537 APPENDIX

538 Nomenclature

539	Acrony	ms	561	γ	Specific heat ratio $(-)$
540	CAC	Charge air cooler	562	λ	Heat conductivity $(W/m/K)$
541	CFC	Chlorofluorocarbon	563	ω	Angular velocity (rad/s)
542	EGR	Exhaust gas recirculation	564	ϕ	Compresibiliy factor $(-)$
543	GADS	SL Global automotive declar	antonie	ρ	Density (kg/m^3)
544	SI	ubstance list	566	arphi	Critical pressure ratio $(-)$
545	GWP	Global warming potential	567	Latin le	tters
546	HCF0	C Hydrochlorofluorocarbon	568	\dot{m}	Mass flow (kg/s)
547	HD	Heavy duty	569	\dot{Q}	Heat flow rate (W)
548	HEX	Heat exchanger	570	\dot{q}	Linear heat flow rate (W/m)
549	NFP	4 National fire protect	ion	\dot{W}	Power (W)
550	a	gency	572	A	Area (m^2)
551	NOP	Net output power	573	C_c	Cubic capacity (m^3)
552	NTU	Number of transfer unit	574	C_d	Discharge coefficient $(-)$
553	ODP	Ozone depletion potential	575	c_p	Specific heat $(J/kg/K)$
554	PC	Performance criterion	576	G	Gear ratio $(-)$
555	WHR	S Waste heat recovery syste	enga ₇	h	Enthalpy (J/kg)
556	Greek l	etters	578	K_{eq}	Equivalent throat diameter
557	α	Heat transfer coefficient	e₽7₽	(r	$n^2)$
558	(1	$W/m^2/K$)	580	N	Rotational speed (rpm)
559	ϵ	Heat exchanger efficiency (-5)1	Nu	Nusselt number $(-)$
560	η	Efficiency $(-)$	582	P	Pressure (Pa)

583	Pe	Perimeter (m)	603	EgrB	EGR boiler
584	PP	Pinch point (K)	604	eng	Engine
585	r	Ideal gas constant $(J/kg/K)$	605	exh	Exhaust gas
586	S	Section (m^2)	606	ExhB	Exhaust boiler
587	s	Entropy $(J/kg/K)$	607	exp	Expander
588	Sr	Vehicle to ram air speed ra	tio	ext	External wall
589	_ (-	-)	609	f	Working fluid
590	T	Temperature (K)	610	fan	Cooling fan
591	t	Time (s)	611	g	Gas
592	V	Volume (m^3)	612	in	Inlet port
593	w	Driving cycle weight $(-)$	613	int	Internal wall
594	x	Quality $(-)$	015	0100	
595	z	Spatial direction (m)	614	max	Maximum
596	Subscri	pts	615	min	Minimum
597	air	Air	616	out	Outlet port
598	amb	Ambient	617	pump	Pump
599	conv	Convection	618	tank	Tank
600	cross	Cross section	619	v	Valve
601	eff	Effective	620	vol	Volumetric
602	egr	EGR gas	621	wall	Heat exchanger wall