

A rocky planet transiting a nearby low-mass star

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M-dwarf stars – hydrogen-burning stars that are smaller than 60 per cent of the size of the Sun – are the most common class of star in our Galaxy and outnumber Sun-like stars by a ratio of 12:1. Recent results have shown that M dwarfs host Earth-sized planets in great numbers^{1,2}: the average number of M-dwarf planets that are between 0.5 to 1.5 times the size of Earth is at least 1.4 per star³. The nearest such planets known to transit their star are 39 parsecs away⁴, too distant for detailed follow-up observations to measure the planetary masses or to study their atmospheres. Here we report observations of GJ 1132b, a planet with a size of 1.2 Earth radii that is transiting a small star 12 parsecs away. Our Doppler mass measurement of GJ 1132b yields a density consistent with an Earth-like bulk composition, similar to the compositions of the six known exoplanets with masses less than six times that of the Earth and precisely measured densities^{5–11}. Receiving 19 times more stellar radiation than the Earth, the planet is too hot to be habitable but is cool enough to support a substantial atmosphere, one that has probably been considerably depleted of hydrogen. Because the host star is nearby and only 21 per cent the radius of the Sun, existing and upcoming telescopes will be able to observe the composition and dynamics of the planetary atmosphere.

We used the MEarth-South telescope array¹² to monitor the brightness of the star GJ 1132, starting on 28 January 2014. The array consists of eight 40-cm robotic telescopes located at the Cerro Tololo Inter-American Observatory (CTIO) in Chile, and observes a sample of M-dwarf stars that are within 33 parsecs of Earth and smaller than 0.35 Solar radii. Since early 2014, the telescopes have gathered data almost every night that weather has permitted, following a strategy similar to that of the MEarth-North survey¹³. On 10 May 2015, GJ 1132 was observed at 25-minute cadence until a real-time analysis system identified a slight dimming of the star indicative of a possible ongoing transit, and commanded the telescope to observe the star continuously at 0.75-minute cadence. These triggered observations confirmed the presence of a transit with a sharp egress (Fig. 1).

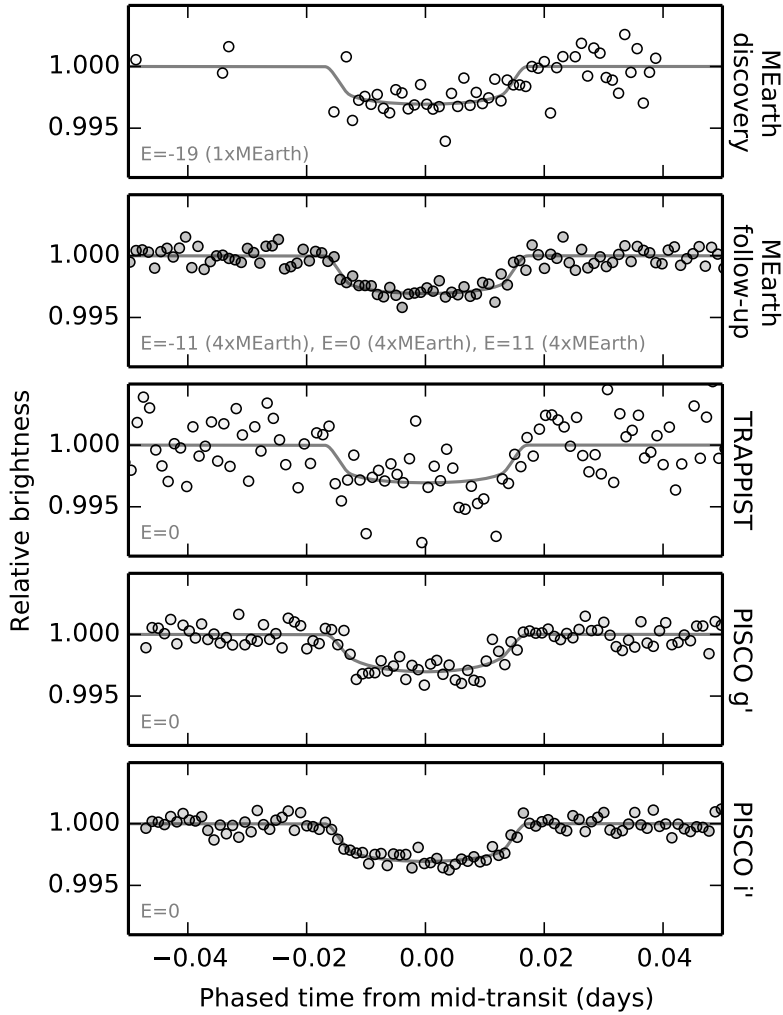


Figure 1: Photometric measurements of transits of GJ 1132b. Light curves from the MEarth-South, TRAPPIST and PISCO telescopes/imagers were fitted with a transit model (grey lines) and a Gaussian process noise model (subtracted from this plot), and averaged to 1.5-min bins for visual clarity. For MEarth-South, both the initial triggered ‘discovery’ observations and the subsequent ‘follow-up’ observations are shown. Labels indicate the transit event (with E as an integer number of planetary periods) and, for MEarth-South, the number of telescopes used. The opacities of binned points are inversely proportional to their assigned variances, representing their approximate weights in the model fit. The raw data and details of the fit are presented in Methods; g' and i' refer to the wavelength bandpasses used from the PISCO imager.

A search of extant data (4,208 observations over 333 nights) for periodic signals revealed a 1.6-day candidate that included this event and reached a detection statistic¹³ of 9.1σ . Follow-up photometry of subsequent predicted transits with four MEarth-South telescopes, the TRAPPIST (TRANSiting Planets and PlanetesImals Small Telescope) telescope¹⁴, and the PISCO (Parallel Imager for Southern Cosmology Observations) multiband imager¹⁵ on the Magellan Clay telescope confirmed the transit signal as being consistent with a planet-sized object blocking 0.26% of the star’s light. We began precise Doppler monitoring with the HARPS (High Accuracy Radial Velocity Planet Searcher) spectrograph¹⁶ on 6 June 2015 and gathered 25 radial velocity measurements for determining the planetary mass (Fig. 2).

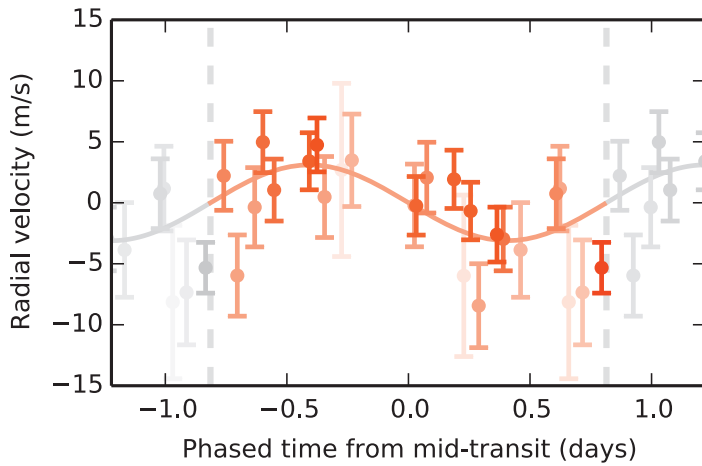


Figure 2: Radial velocity changes over the orbit of GJ 1132b. Measurements of the star’s line-of-sight velocity, taken by the HARPS spectrograph, are shown phased to the planetary orbital period determined from the light curves (orange points, with duplicates shown in grey). Error bars correspond to 1σ . The darkness of each point is proportional to its weight in the model fit, which is the inverse of its variance as predicted by a radial velocity noise model. For a circular orbit, the star’s reflex motion to the planet has a semi-amplitude of $K_* = 2.76 \pm 0.92 \text{ m s}^{-1}$.

The distance to GJ 1132 has been measured through trigonometric parallax to be 12.04 ± 0.24 parsecs¹⁷, a value that we independently validate with MEarth astrometry (see Methods). Together with empirical relations among the intrinsic luminosities, masses and radii of M-dwarf stars^{18,19}, the parallax enables us to estimate the mass and radius of GJ 1132. These estimates are not biased by physically associated luminous companions, which are ruled out by published photometry results and the HARPS spectra. Likewise, unassociated background stars are too faint in archival imaging at the current sky position of this high-proper-motion star to corrupt our estimates of the stellar parameters. Table 1 presents the physical properties of the star (GJ 1132) and planet (GJ 1132b), combining the inferred stellar properties with analyses of the transit light curves (Fig. 1) and radial velocity observations (Fig. 2). The radius of the planet is 40% that of GJ 1214b (ref. 20), a well studied mini-Neptune exoplanet that orbits with a similar period around a similar host star.

Table 1: System properties for GJ 1132b

Parameter	Value
Stellar parameters	
Photometry	$V = 13.49, J = 9.245, K = 8.322$
Distance to star, D_\star	12.04 ± 0.24 parsecs
Mass of star, M_\star	$0.181 \pm 0.019 M_\odot$
Density of star, ρ_\star	$29.6 \pm 6.0 \text{ g cm}^{-3}$
Radius of star, R_\star	$0.207 \pm 0.016 R_\odot$
Luminosity of star, L_\star	$0.00438 \pm 0.00034 L_\odot$
Effective temperature, T_{eff}	$3270 \pm 140 \text{ K}$
Metallicity, $[\text{Fe}/\text{H}]$	-0.12 ± 0.15
Age of star, τ_\star	$> 5 \text{ Gyr}$
Transit and radial velocity parameters	
Orbital period, P (days)	1.628930 ± 0.000031
Time of mid-transit, t_0 (BJD _{TDB} ; days)	$2457184.55786 \pm 0.00032$
Eccentricity, e	0 (fixed)
Planet-to-star radius ratio, R_p/R_\star	0.0512 ± 0.0025
Scaled orbital distance, a/R_\star	16.0 ± 1.1
Impact parameter, b	0.38 ± 0.14
Radial velocity semi-amplitude, K_\star	$2.76 \pm 0.92 \text{ m s}^{-1}$
Systemic velocity, γ_\star	$+35 \pm 1 \text{ km s}^{-1}$
Planet parameters	
Radius of planet, R_p	$1.16 \pm 0.11 R_\oplus$
Mass of planet, M_p	$1.62 \pm 0.55 M_\oplus$
Density of planet, ρ_p	$6.0 \pm 2.5 \text{ g cm}^{-3}$
Surface gravity on planet, g_p	$1170 \pm 430 \text{ cm s}^{-2}$
Escape velocity, V_{esc}	$13.0 \pm 2.3 \text{ km s}^{-1}$
Equilibrium temperature, T_{eq}	
assuming Bond albedo of 0.00	$579 \pm 15 \text{ K}$
assuming Bond albedo of 0.75	$409 \pm 11 \text{ K}$

Transit and radial velocity parameters were estimated from a Markov chain Monte Carlo (MCMC) analysis, including an external constraint on the stellar density when deriving P , t_0 , R_p/R_\star , a/R_\star , and b (see Methods). Planetary properties were derived from the combined stellar, transit, and radial velocity parameters. L_\odot , luminosity of the Sun; M_\odot , mass of the Sun; R_\odot , radius of the Sun; BJD_{TDB}, Barycentric Julian Date in the Barycentric Dynamical Time system; a , orbital semimajor axis; M_\oplus , mass of Earth; R_\oplus , radius of Earth.

GJ 1132b’s average density resembles that of the Earth, and is well matched by a rock/iron bulk composition. A theoretical mass-radius curve²¹ for a two-layer planet composed of 75% magnesium silicate and 25% iron (by mass) is consistent with our estimates for GJ 1132b (Fig. 3). This model assumes that the core is pure iron, the mantle is pure magnesium silicate, and the interior contains no water²¹. These simplifications mean that the iron fraction should not be taken as absolute; the model simply represents a characteristic mass-radius locus that matches Earth and Venus. This same composition also matches the masses and radii of Kepler-78b (refs 8, 9), Kepler-10b (ref. 7), Kepler-93b (ref. 10), Kepler-36b (ref. 6), CoRoT-7b (ref. 5), and HD 219134b (ref. 11) to within 1σ . All of these planets are smaller than 1.6 Earth radii, a transition radius above which most planets require thick hydrogen/helium envelopes to explain their densities²². At the 1σ lower bound of GJ 1132b’s estimated mass, models²³ indicate that replacing only 0.2% of the rock/iron mix with a hydrogen/helium layer would increase the planet’s radius to 1.4 times that of the Earth, substantially larger than the observed value. Detection of GJ 1132b’s mass is currently only at the 3σ level, but continued Doppler monitoring will shrink the 35% mass uncertainty and enable more detailed comparison with other planets and compositional models.

We searched for additional planets both as other transits in the MEarth-South light curve and as periodic signals in the HARPS residuals. Although we made no notable discoveries, we highlight that compact, coplanar, multiple-planet systems are common around small stars^{24,25}. Further exploration of the GJ 1132 system could reveal more, potentially transiting, planets.

As a relatively cool rocky exoplanet with an equilibrium temperature between 580 K (assuming a Bond albedo of 0) and 410 K (assuming a Venus-like Bond albedo of 0.75), GJ 1132b may have retained a substantial atmosphere. At these temperatures, the average thermal speeds of atoms or molecules heavier than helium are less than one-eighth of the escape velocity, suggesting an atmosphere could be stable against thermal escape. This is not the case for the other rocky exoplanets for which precise densities are known, all of which are considerably hotter. The rocky planet Kepler-78b (refs 8, 9), which is comparable in size and density to GJ 1132b, receives 200 times more irradiation than GJ 1132b. Whether the atmosphere of GJ 1132b was initially dominated by hydrogen/helium-rich gas accreted from the primordial nebula or by volatiles outgassed from the planetary interior, its composition probably evolved substantially over the age of the system, which we estimate to exceed 5 billion years (gigayears, Gyr) (see Methods). Irradiated well beyond the runaway greenhouse limit²⁶, surface water would extend up to high

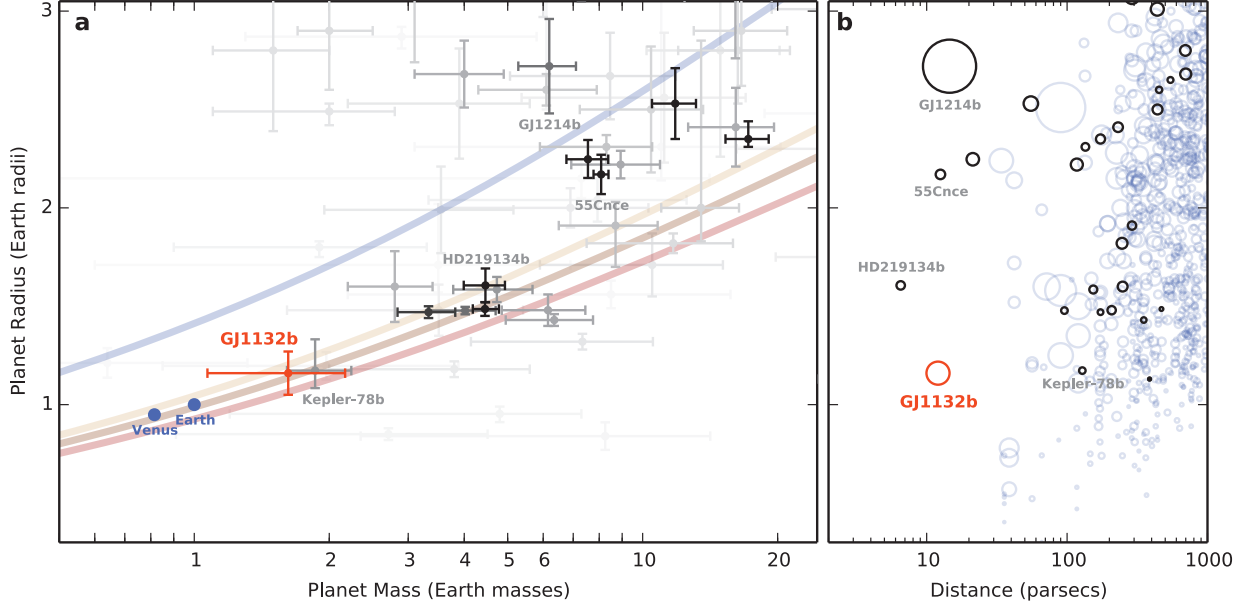


Figure 3: Masses, radii, and distances of known transiting planets. **a**, The radius and mass of GJ 1132b (orange) are shown, along with those of other exoplanets (grey). Also shown are mass-radius curves predicted by theoretical models²¹ for planets composed of 100% H_2O (blue line), and for two-component planets composed of MgSiO_3 on top of Fe cores that are 0% (light brown), 25% (darker brown) or 50% (red) of the total mass. Planets with smaller fractional mass and radius uncertainties are darker. **b**, Symbol area is proportional to transit depth. In comparison with other transiting exoplanets, those with masses detected at $> 2.5\sigma$ (black) and those without masses detected at such level (blue), GJ 1132b is the most accessible terrestrial planet for spectroscopic observations of its atmosphere, owing to the proximity and small size of its parent star.

altitudes where it could be destroyed by photolysis and its hydrogen rapidly lost to space. When the star was young and bright at ultraviolet wavelengths, an atmosphere with high concentrations of water could lose hydrogen at the diffusion limit, of the order of 10^{13} atoms per cm^2 per second or 10 Earth oceans per gigayear. Depending on surface weathering processes, the oxygen left behind might persist as O_2 in the atmosphere^{26,27}. In this scenario, water would constitute a trace component in an atmosphere otherwise dominated by O_2 , N_2 , and CO_2 . However, large uncertainties in the size of the initial hydrogen reservoir, in the history of the star’s ultraviolet luminosity, in the contribution of late volatile delivery, and in the evolutionary effect of the system’s likely spin-orbit synchronization preclude firm *a priori* statements about the composition of the atmosphere.

Future spectroscopic investigation of the planetary atmosphere will be enabled by the proximity and small radius of the star. When viewed in transmission during transit, one scale height of an O_2 -rich atmosphere would overlap 10 parts per million (p.p.m.) of the stellar disk. For comparison, a 60-orbit Hubble Space Telescope transmission spectrum of GJ 1214b achieved a transit depth precision of 25 p.p.m. in narrow wavelength bins²⁸. Deeper Hubble observations of GJ 1132, which is 50% brighter than GJ 1214, would have the potential to detect molecular absorption features in GJ 1132b’s atmosphere. Observations with the James Webb Space Telescope (JWST), set to launch in 2018, could measure the transmission spectrum over a broader wavelength range and require less telescope time. The long-

wavelength capabilities of JWST may also allow it to detect the thermal emission from the planet; such emission represents 40-130 p.p.m. of the system flux at a wavelength of $10\ \mu\text{m}$, and 160-300 p.p.m. of the flux at $25\ \mu\text{m}$ (for the range of albedos considered above). Provided that the planet is not too cloudy, combined transmission and emission spectra could ascertain the abundances of strongly absorbing molecular species. If such constraints on the dominant infrared opacity sources can be obtained, observations of the planet's thermal phase curve would be sensitive to complementary information, including the total atmospheric mass^{29,30}. Such observations will inform our understanding of how the strong tides and intense stellar activity of the M-dwarf planetary environment influence the evolution of terrestrial atmospheres. This understanding will be important for the long-term goal of looking for life on planets orbiting nearby small stars.

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Supplementary Information is available in the online version of the paper.

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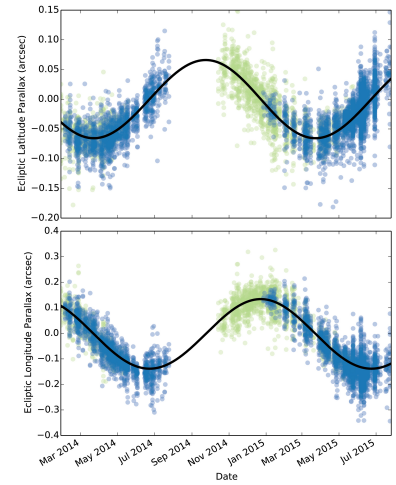
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Author Contributions The MEarth team (D.C., J.I., Z.K.B.-T., E.R.N. and J.A.D.) discovered the planet, organized the follow-up observations, and led the analysis and interpretation. Z.K.B.-T. analysed the light curve and radial velocity data, and wrote the manuscript. J.I. designed, installed, maintains, and operates the MEarth-South telescope array, identified the first triggered transit event, and substantially contributed to the analysis and interpretation. D.C. leads the MEarth Project, and assisted in analysis and writing the manuscript. E.R.N. determined the metallicity, kinematics, and rotation period of the star. J.A.D. confirmed the star’s trigonometric parallax and helped install the MEarth-South telescopes. The HARPS team (N.A.-D., X.B., F.B., X.D., T.F., C.L., M.M., V.N., F.P., N.C.S., S.U. and A.W.) obtained spectra for Doppler velocimetry, with N.A.-D. and X.B. leading the analysis of those data. M.G. and E.J. gathered photometric observations with TRAPPIST. A.A.S. and B.S. gathered photometric observations with PISCO. All authors read and discussed the manuscript.

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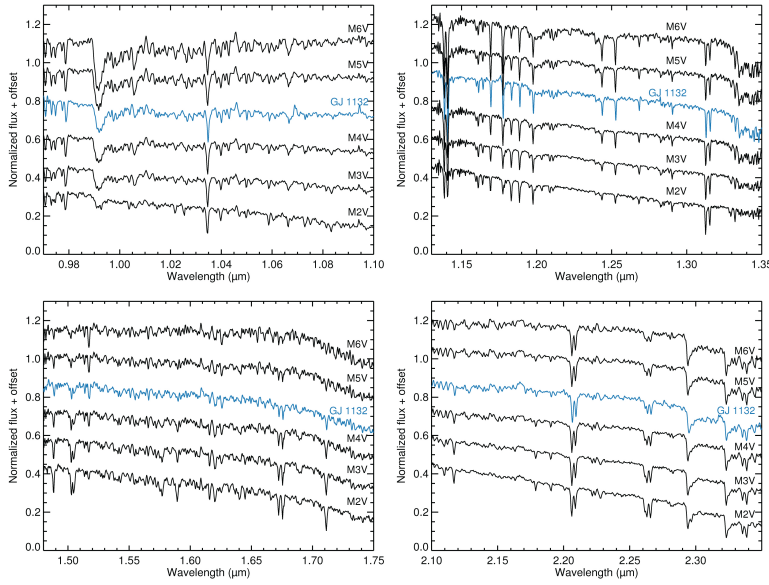
Methods

Distance to the star GJ 1132’s coordinates are 10:14:51.77 -47:09:24.1 (International Celestial Reference System, epoch 2000.0), with proper motions of $(-1046; 416)$ milliarcseconds (mas) per year and a trigonometric parallax of $\pi = 83.07 \pm 1.69$ mas, as determined by the RECONS (Research Consortium on Nearby Stars) survey¹⁷. We qualitatively confirm this parallax with independent observations from MEarth-South, using analyses like those that have been applied to the northern survey³¹. The motion of GJ 1132 relative to background stars in MEarth-South imaging closely matches the prediction made by the RECONS parallax (Extended Data Fig. 1). We do not quote the value of π derived from MEarth-South because we have not yet cross-validated the astrometric performance of the system against other measurements. Literature photometric observations of GJ 1132 include photoelectric photometry ($U = 16.51 \pm 0.03$, $B = 15.17 \pm 0.03$)³², charge-coupled device (CCD) photometry ($V = 13.49 \pm 0.03$, $RC = 12.26 \pm 0.02$, $I_C = 10.69 \pm 0.02$)¹⁷, 2MASS near-infrared photometry ($J = 9.245 \pm 0.026$, $H = 8.666 \pm 0.027$, $K_s = 8.322 \pm 0.027$)³³, and WISE infrared photometry ($W1 = 8.170 \pm 0.023$, $W2 = 8.000 \pm 0.020$, $W3 = 7.862 \pm 0.018$, $W4 = 7.916 \pm 0.184$). The colour ($V - K_s = 5.168 \pm 0.040$) and absolute magnitude ($M_V = 13.088 \pm 0.054$) of GJ 1132 are consistent with those of single M4V dwarfs³⁴.



Extended Data Figure 1: Astrometry of GJ 1132 from MEarth-South. Measurements of the star GJ 1132’s position in MEarth-South images, along the directions of ecliptic latitude (top) and longitude (bottom). As described elsewhere³¹, a fitted offset between data gathered at a field rotation of 0° (blue) and 180° (green) has been removed. The published RECONS proper motion¹⁷ has been subtracted, and a model fixed to the published 83.07 mas parallax (black line) closely matches the MEarth-South observations.

Metallicity of the star Before discovering the planet, we gathered a near-infrared spectrum of GJ 1132 with the FIRE spectrograph on the Magellan Baade telescope. We shifted the spectrum to a zero-velocity wavelength scale³⁵, measured equivalent widths and compared the spectra by eye with solar metallicity spectral type standards³⁵. The spectrum indicates a near-infrared spectral type of M4V-M5V (Extended Data Fig. 2), slightly later than the optical spectral of M3.5V listed in the PMSU (Palomar/Michigan State University) catalogue³⁶. Using the measured equivalent width of the K-band sodium feature (4.7Å) and an empirical calibration³⁵ that has been corrected for its known temperature dependence³⁷, we estimate the stellar metallicity to be $[\text{Fe}/\text{H}] = -0.12 \pm 0.15$ and quote this value in Table 1. For comparison, a relation using additional spectral regions and calibrated for stars of GJ 1132’s spectral type and earlier³⁸ also yields $[\text{Fe}/\text{H}] = -0.1$, while one for GJ 1132’s spectral type and later³⁹ yields $[\text{Fe}/\text{H}] = -0.2$ (both with uncertainties of about 0.15 dex).



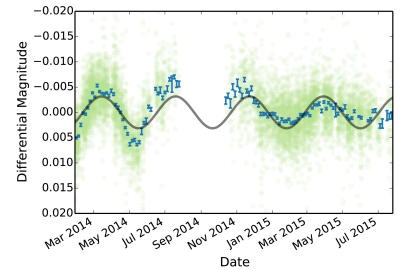
Extended Data Figure 2: Near-infrared spectrum of GJ 1132. Observations of GJ 1132’s spectrum obtained with the FIRE spectrograph on the Magellan Baade telescope are compared in the z , J , H and K telluric windows (left to right, top to bottom) to the solar-metallicity composite spectral type standards from ref. 35. The FIRE spectra have been smoothed to match the $R = 2,000$ resolution of the standards. GJ 1132’s near-infrared spectral type is M4V-M5V.

Mass of the star Dynamical mass measurements of M-dwarfs show that tight relationships exist between near-infrared absolute magnitudes and stellar mass¹⁸. We use these calibrations to calculate masses from the J , H and K magnitudes (after converting between the 2MASS and CIT photometric systems). Taking the mean of these masses and adopting an uncertainty that is the quadrature sum of the 2.7% error propagated from the measurement uncertainties and the 10% scatter we assume for the relations, we adopt a stellar mass of $M_{\star} = 0.181 \pm 0.019 M_{\odot}$, where M_{\star} is the mass of the star and M_{\odot} is the mass of the Sun.

Radius of the star From this mass, we use an empirical $M_\star - \rho_\star$ relation¹⁹ calibrated to eclipsing binary systems to estimate a density of $\rho_\star = 29.6 \pm 6.0 \text{ g cm}^{-3}$, corresponding to $R_\star = 0.207 \pm 0.016 R_\odot$ for GJ 1132. We adopt those values, noting that they agree with two other mass-radius relations: the radius predicted by long-baseline optical interferometry of single stars⁴⁰ is $R_\star = 0.211 \pm 0.014 R_\odot$, and that by the Dartmouth evolutionary models⁴¹ is $R_\star = 0.200 \pm 0.016 R_\odot$ (for $[\text{Fe}/\text{H}] = -0.1$, assuming a uniform prior on age between 1 Gyr and 10 Gyr). The quoted errors do not include an assumed intrinsic scatter in any of the mass-radius relations, but the consistency among the three estimates suggests that any contribution from scatter would be smaller than the uncertainty propagated from the stellar mass.

Bolometric luminosity of the star We combine the parallax and photometry with bolometric corrections to determine the total luminosity of GJ 1132, testing three different relations to estimate bolometric corrections from colour. The Mann et al. relation⁴² between BC_V and $V - J$ colour yields a bolometric luminosity of $0.00402 L_\odot$. The Leggett et al. relation⁴³ between BC_K and $I - K$ colour yields $0.00442 L_\odot$. The Pecaut and Mamajek compilation of literature bolometric corrections⁴⁴, when interpolated in $V - K_s$ colour to determine BC_V , yields $0.00469 L_\odot$. We adopt the mean of these three values, with an uncertainty that is the quadrature sum of the systematic error (the 6.3% standard deviation of the different estimates) and the uncertainty propagated from the measurement uncertainties (about 5% in all three cases), as our final estimate of the bolometric luminosity: $L_\star = 0.00438 \pm 0.00034 L_\odot$. From this, we calculate the stellar effective temperature as $T_{\text{eff}} = 5772 \text{ K} \times (L_\star / L_\odot)^{1/4} \times (R_\star / R_\odot)^{-1/2} = 3270 \pm 140 \text{ K}$. The luminosity and temperature we infer³⁷ from the FIRE spectra ($L_\star = 0.0044 \pm 0.001 L_\odot$, $T_{\text{eff}} = 3130 \pm 120 \text{ K}$) are consistent with the quoted values.

Age of the star GJ 1132's motion through the Galaxy of $(U_{\text{LSR}}, V_{\text{LSR}}, W_{\text{LSR}}) = (-47, -32, -2) \text{ km s}^{-1}$ is consistent with a kinematically older stellar population*. M4 dwarfs tend to show strong $\text{H}\alpha$ emission for about 4 Gyr⁴⁵; the lack of $\text{H}\alpha$ emission in the HARPS spectrum indicates that GJ 1132 is probably older than that. The star instead shows weak $\text{H}\alpha$ absorption, which is an indicator of non-zero magnetic activity in stars as cool as this⁴⁶. We detect emission in the Ca II H line, with a weak intensity that is comparable to that of Barnard's Star and other slowly rotating stars in the HARPS M-dwarf sample⁴⁷. Applying published methods⁴⁸ to the MEarth-South photometry, we measure a rotation period of 125 days for GJ 1132 (Extended Data Fig. 3). M-dwarfs spin more slowly as they age, with less massive stars



Extended Data Figure 3: Photometric starspot modulations of GJ 1132.

MEarth-South photometry (with dots representing single pointings and error bars representing $\pm 1\sigma$ uncertainty ranges on weighted averages over four-day bins) probes starspots that are rotating in and out of view, and indicates that GJ 1132 has a rotation period of approximately 125 days. The rotational modulation was identified using a methodology similar to that used in previous MEarth work⁴⁸.

* UVW velocities have been updated to use the proper motion stated above. The values given in the published article were based on the proper motion from ref. 64, and were also with respect to the local standard of rest. We adopt the solar velocities of ref. 65.

reaching longer rotation periods at old ages⁴⁸. Therefore, the rotation period suggests that the system could be almost as old as Barnard’s Star ($0.16 M_{\odot}$), which has a 130-day rotation period⁴⁹ and is 7–13 Gyr old⁵⁰. GJ 1132’s age is probably comparable to or greater than that of Proxima Centauri ($0.12 M_{\odot}$), which has an 83-day period^{49,51} and is 5–7 Gyr old, assuming it to be coeval with the gyrochronologically and asteroseismically age-dated α Centauri system⁵². From these comparisons, we conclude that GJ 1132 is probably older than 5 Gyr.

Assumption of a circular orbit Calculating the timescale for tidal circularization⁵³ as $t_{\text{circ}} = \frac{2PQ}{63\pi} \times \frac{M_p}{M_*} \times \left(\frac{a}{R_p}\right)^5$, assuming a tidal quality factor of $Q = 100$ appropriate for rocky exoplanets, yields 4×10^5 years for GJ 1132b. This is much shorter than the age of the system; therefore, we assume the eccentricity to be negligible and fix it to 0 in our estimation of the other planetary properties. Perturbations from other (undetected) planets in the system could potentially induce a small equilibrium eccentricity.

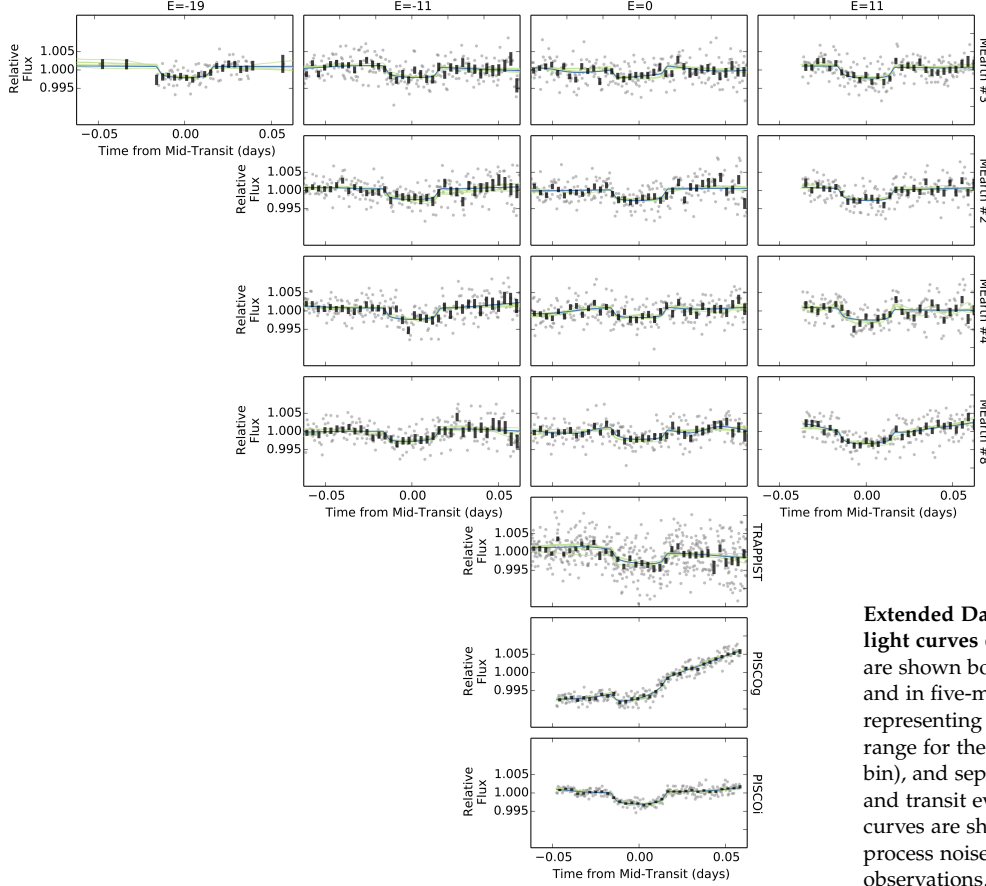
Photometric observations and analysis The high-cadence light curves analysed here were gathered over four nights using six telescopes on three mountains. The triggered event (event $E = -19$, relative to the ephemeris in Table 1) was collected on MEarth-South telescope 3. At the time of this triggered detection, 296 stars in the MEarth-South sample had been observed at least 100 times, but only nine of these stars had been observed as thoroughly as GJ 1132. After identification of the periodic signal, we obtained follow-up photometry with MEarth-South telescopes 2, 3, 4 and 8 on the nights of 23 May 2015, 10 June 2015 and 28 June 2015 ($E = -11, 0$ and 11). Exposure times were 18 s, yielding a 47-s cadence for the high-cadence light curves. We observed the transit on the night of 10 June 2015 ($E = 0$) with the TRAPPIST telescope, in a wide $I + z$ bandpass, with exposure times of 10 s and a cadence of 21 s. We also observed this transit with the PISCO multiband imager, which was installed on the Magellan Baade telescope and undergoing a commissioning run, taking 10-s exposures simultaneously in g', r', i', z' bandpasses at a cadence of 36 s. We actively defocused Baade, resulting in donut-shaped point spread functions spreading each star’s light over about 200 pixels. The PISCO r' and z' light curves exhibited unexplained systematics and were not used for further analysis.

To the high-cadence light curves, we fitted a transit model⁵⁴ with the following parameters: orbital period P , time of mid-transit t_0 , planet-to-star radius ratio R_p/R_* , star-to-orbit radius ratio R_*/a , impact parameter b , and separate baseline flux levels for each transit observed on each telescope. The PISCO and TRAPPIST photome-

try showed trends that correlated with airmass, so we also included coefficients for a trend linear with airmass as free parameters. Limb-darkening was treated with a quadratic approximation, using fixed coefficients⁵⁵ calculated from a PHOENIX atmosphere model for a 3,300 K, $[\text{Fe}/\text{H}] = 0$, $\log g = 5$ star. These coefficients (u_1, u_2) were: (0.1956, 0.3700) for MEarth and TRAPPIST (both approximated as $\frac{1}{3}i' + \frac{2}{3}z'$), (0.4790, 0.3491) for PISCO g' (approximated as Sloan g'), and (0.2613, 0.3737) for PISCO i' (approximated as Sloan i'). We performed a Levenberg-Marquardt maximization of the posterior probability of this model, rejected $> 4\sigma$ outliers among the data, repeated the maximization, and increased the per-point uncertainty estimates until each transit exhibited a reduced $\chi^2 \leq 1$. This resulted in typical per-point uncertainties of 2.6 (MEarth), 3.6 (TRAPPIST), 1.9 (PISCO g'), and 1.2 (PISCO i') mmag. Most light curves showed some evidence for time-correlated noise in their residuals. To marginalize over the uncertainty introduced by these correlations, we use the Gaussian process regression package *George*⁵⁶ to model each set of transit residuals as a Gaussian process with non-zero covariance between the datapoints⁵⁷. We use a Matérn-3/2 kernel function to describe this covariance as a function of separation in time, and include two free parameters per transit: $\log t_{\text{gp}}$ (where t_{gp} is the correlation timescale) and $\log a_{\text{gp}}$ (where a_{gp} is an amplitude). We mapped the probability distribution of the model parameters using the *emcee* implementation⁵⁸ of an affine-invariant Markov chain Monte Carlo (MCMC) sampler⁵⁹, assuming flat priors on all parameters. Extended Data Fig. 4 shows raw light curves of individual transits, along with model curves sampled from the posterior.

The ingress time ($\tau = 3.7 \pm 1.0$ min from first to second contact) is measured imprecisely in this fit, compared to the total transit duration ($T_{\text{tot}} = 47.0 \pm 1.4$ min from first to fourth contact). Systematic astrophysical errors (incorrect limb-darkening, starspots, unidentified transit timing variations) can bias light-curve estimates of the ingress time, and therefore also the parameters R_*/a and b that depend strongly on τ . Therefore, we estimate the planet properties without relying on this ingress measurement, by including external constraints on both the stellar mass and the stellar density. We sample values of M_* and ρ_* from Gaussian distributions ($0.181 \pm 0.019 M_\odot$ and $29.6 \pm 6.0 \text{ g cm}^{-3}$), use Kepler’s Third Law to compute R_*/a from the stellar density and the period, and then calculate b from the transit duration and these new R_*/a samples. We quote the marginalized values and uncertainties for these and other light-curve parameters in Table 1. This procedure forces consistency between the light-curve fit and the inferred stellar properties and shifts the estimates from $R_*/a = 0.0738 \pm 0.0092$ and $b = 0.58 \pm 0.14$ (inferred

from the light curves alone) to the values in Table 1. The effect on P , t_0 , or R_p/R_* is negligible. If we ignore the external ρ_* information, the inferred stellar and planetary radii would be consistent with those in Table 1 but with larger error bars ($R_* = 0.243 \pm 0.031 R_\odot$ and $R_p = 1.37 \pm 0.22 R_\oplus$).



Extended Data Figure 4: Raw transit light curves of GJ 1132b. Light curves are shown both unbinned (grey points) and in five-minute bins (black bars, representing the $\pm 1\sigma$ uncertainty range for the weighted average in each bin), and separated by telescope (row) and transit event (column). Model curves are shown, with the Gaussian process noise model conditioned on the observations, for parameters sampled from the posterior (green) and for the maximum likelihood parameters (blue). This is the complete set of light-curve data behind the transit parameter fits.

Radial velocity observations and analysis We first gathered reconnaissance spectra of GJ 1132 with the CHIRON⁶⁰ spectrograph on the SMARTS 1.5-metre telescope at CTIO. Once these spectra ruled out large radial-velocity variations corresponding to binary star companions, we began observations with the HARPS spectrograph on the La Silla 3.6-metre telescope. We gathered 25 HARPS spectra of GJ 1132 between 6 June 2015 and 18 July 2015, using an exposure time of 40 min. The spectra span 380 nm to 680 nm in wavelength. For each observation, we constructed a comparison template by co-adding all the other spectra and measured the relative radial velocity as the shift required to minimize the χ^2 of the difference between the spectrum

and this template^{61,62}. Telluric lines were masked using a template of lines made with a different, much larger, data set. We see no evidence for rotational broadening of the spectra, indicating that the projected rotational velocity, $v \sin i$, is less than 2 km s^{-1} . The median of the internal radial velocity uncertainty estimates⁶¹ is 3 m s^{-1} per observation.

Over the timespan of our observations, these radial velocities are dominated by the orbital motion of the known transiting planet, rather than by other planets, blended stellar binaries, or stellar activity. The tallest peak in the periodogram of the radial velocities is consistent with the transit-derived period for GJ 1132b. The line bisectors show no significant correlation with the measured velocities (Pearson correlation p -value of 0.27) and no clear periodicities. The H α equivalent width and the full-width half-maximum of the HARPS cross-correlation function are not correlated with the velocities (Pearson correlation p -values of 0.72 and 0.57).

We fit the velocities with a model corresponding to a circular orbit for the planet, with flat priors on three free-floating parameters: the radial velocity semi-amplitude K_* , the systemic velocity γ_* , and a stellar jitter term $\sigma_{*,\text{jitter}}$ that is added in quadrature to the internal velocity uncertainties. We include all terms that depend on $\sigma_{*,\text{jitter}}$ in the likelihood, as well as the usual χ^2 term. P and t_0 were fixed to the values determined from the transit analysis. We use `emcee`⁵⁸ to sample from the posterior probability distributions of these parameters, and quote marginalized uncertainties on K_* in Table 1. In this fit, the value of K_* is > 0 in 99.7% of the MCMC samples. The inferred value of $\sigma_{*,\text{jitter}}$ is smaller than the individual uncertainties ($< 1.9 \text{ m s}^{-1}$ at 68% confidence), and a good fit is obtained if $\sigma_{*,\text{jitter}}$ is fixed to 0 ($\chi^2 = 26.67$ for 23 degrees of freedom). The χ^2 of a fit where both K_* and $\sigma_{*,\text{jitter}}$ are fixed to 0 is significantly worse (38.56 for 24 degrees of freedom). As a check, we repeated the MCMC fit allowing the phase (t_0) to float. This radial velocity fit predicted the known mid-transit times to within 1.5σ ($3.0 \pm 1.9 \text{ h}$ after the true transit times). Relaxing the assumption of a circular orbit yields inferred distributions of $(e \cos \omega, e \sin \omega)$ that are consistent with (0, 0) but substantially increases the uncertainty on the semi-amplitude ($K_* = 3.6 \pm 2.4 \text{ m s}^{-1}$). With future Doppler measurements, it will be possible to measure the planet's eccentricity and independently test the assumption we make here that tides damped the eccentricity to small values.

Transiting exoplanet population comparison Figure 3 compares GJ 1132b to other known transiting exoplanets. Data for this plot were drawn from the NASA Exoplanet Archive⁶³ on 25 August 2015.

Egregious errors in the catalogue were replaced with appropriate literature values. In the mass-radius panel, individual planets are shaded with a white-to-black greyscale that is inversely proportional $(\sigma_M/M_p)^2 + (\sigma_R/R_p)^2$, where σ_M and σ_R are the uncertainties on the planet mass, M_p , and radius, R_p . Planets with precise measurements are dark, and those with large mass or radius uncertainties are light. In the distance-radius panel, some planets did not have distances listed in the Exoplanet Archive. For those systems, we calculated approximate distances from the J -band magnitudes, estimated stellar radii, effective temperatures, and a table of bolometric corrections⁴⁴ (interpolating in T_{eff} to estimate BC_J).

Code availability Analyses were conducted primarily in Python. Although not cleanly packaged for general use, for the sake of transparency we make the custom code used for transit and radial velocity fitting available at <http://github.com/zkbt/transit>. It relies on three freely available packages: *eb* (<http://github.com/mdwarfgeek/eb>), *emcee* (<http://github.com/dfm/emcee>), and *George* (<http://github.com/dfm/george>). Code used to generate the exoplanet population comparison is available at <http://github.com/zkbt/exopop>.

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