# IMPACT OF $\eta_{\text {Earth }}$ ON THE CAPABILITIES OF AFFORDABLE SPACE MISSIONS TO DETECT BIOSIGNATURES ON EXTRASOLAR PLANETS 

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#### Abstract

We present an analytic model to estimate the capabilities of space missions dedicated to the search for biosignatures in the atmosphere of rocky planets located in the habitable zone of nearby stars. Relations between performance and mission parameters, such as mirror diameter, distance to targets, and radius of planets, are obtained. Two types of instruments are considered: coronagraphs observing in the visible, and nulling interferometers in the thermal infrared. Missions considered are: single-pupil coronagraphs with a 2.4 m primary mirror, and formation-flying interferometers with $4 \times 0.75 \mathrm{~m}$ collecting mirrors. The numbers of accessible planets are calculated as a function of $\eta_{\text {Earth }}$. When Kepler gives its final estimation for $\eta_{\text {Earth }}$, the model will permit a precise assessment of the potential of each instrument. Based on current estimations, $\eta_{\text {Earth }}=10 \%$ around FGK stars and $50 \%$ around M stars, the coronagraph could study in spectroscopy only $\sim 1.5$ relevant planets, and the interferometer $\sim 14.0$. These numbers are obtained under the major hypothesis that the exozodiacal light around the target stars is low enough for each instrument. In both cases, a prior detection of planets is assumed and a target list established. For the long-term future, building both types of spectroscopic instruments, and using them on the same targets, will be the optimal solution because they provide complementary information. But as a first affordable space mission, the interferometer looks the more promising in terms of biosignature harvest.


Key words: astrobiology - instrumentation: high angular resolution - instrumentation: interferometers instrumentation: miscellaneous - planets and satellites: terrestrial planets

Supporting material: machine-readable tables

## 1. INTRODUCTION

Exobiology outside the Solar System is a new field of science that should become accessible in the mid-term future if suitable instruments can be funded and built. They should be able to give us the first scientific answers to questions that humanity has been asking itself for over 2000 years (Democritus of Abdera 460-371 BC, Epicurus of Samos 341-270 BC).

In a founding article, Tobias Owen (1980) states: "... it is not a simple accident that life on Earth is based on carbon with water as its liquid. It seems possible that most of life elsewhere in the universe will rely on this same chemistry (...). With our present understanding of the requirements for life (...) we find some real support for carbon-water chauvinism." This statement has an important implication: the existence of biosignatures that can be searched for by remote sensing. The real course for life based on carbon chemistry, having $\mathrm{CO}_{2}$ (fully oxidized C) as an abundant raw material, is to synthesize its organic carbon (partially reduced C ) from it, using the most abundant source of free energy on a planet, the stellar radiation. A frequent output of this reduction of $\mathrm{CO}_{2}$ is $\mathrm{O}_{2}$, which can be searched for in the exoplanetary atmospheres. This biosignature has possible false negatives, but seems to have no false positive, because up to now (2015) the many attempts to falsify

[^0]it have failed. Making the case for our planet, Owen pointed out: "the huge abundance of free oxygen is very difficult to explain without invoking biology, since this highly reactive gas would rapidly combine with the crust." He also noted: "the A-band of $\mathrm{O}_{2}$ at $7600 \AA$ is remarkably strong." The way to go was traced.

Later, Angel et al. (1986) first-followed by Léger et al. (1993), Selsis et al. (2002), and other authors-showed that a solid alternative to the search for $\mathrm{O}_{2}$ at visible wavelengths $(0.76 \mu \mathrm{~m})$ was to look for $\mathrm{O}_{3}(9.6 \mu \mathrm{~m})$ in the thermal infrared (IR).

A number of questions to be discussed were put forward by several authors (Burke 1992a, 1992b; Schneider 1995; Beichman et al. 1996; Borucki et al. 1996; Léger 2001; Mennesson et al. 2005), the answers to which would require an ambitious instrumentation roadmap to be established for the search for possible biosignatures. These questions are as follow:

1. Are there giant planets around stars other than the Sun?
2. Are there telluric planets around stars other than the Sun?
3. Are there telluric planets located in the habitable zone (HZ) of their stars, and how many?
4. Can we identify the relevant planets around the nearest stars?
5. Can we build a mission that can search for biosignature (s) in the latter group?

Today, we have positive answers to questions (1) and (2) (Mayor \& Queloz 1995; Léger et al. 2009). Kepler was built to answer question (3) (Borucki et al. 1996), but at present there is no funded plan to answer question (4). To address goal (5), the choice of the mission to build was, for various reasons, decided before we knew the answer to question (3). The goal of the present paper is to revisit that point, and discuss how the answer to (3)-which we should get from Kepler-would influence our choices for answering question (5).

There are two avenues to do that: spectroscopic transits (with the James Webb Space Telescope (JWST) or one of the future extremely large ground-based telescopes), and spatially resolved spectroscopy. Only the second approach is discussed here for the sake of conciseness. Some preliminary estimates with Kepler of the parameter $\eta_{\text {Earth }}$, i.e., the mean number of Earth analogs and super-Earths in the HZ of stars, are of the order of $5 \%-10 \%$ around solar-type stars (Petigura et al. 2013; Batalha 2014), and 50\% around M stars (Kopparapu 2013). Considering the large number of stars in our galaxy $\left(\sim 3 \times 10^{11}\right)$, this field of science benefits from a huge reservoir of targets to be studied in the next decades, possibly centuries.
In the last decade, during the "golden age" of NGST, Darwin, and TPF, very large instruments were considered to conduct the spectroscopy of Earth analogs (Angel et al. 1986; Beichman et al. 1999; Cockell et al. 2009; Defrère et al. 2010). These included, for instance, coronagraphs on an $8 \times 3 \mathrm{~m}$ telescope (Levine et al. 2009) or on a 5 m diameter ( $\Phi$ ) telescope (Lunine et al. 2009), and interferometers made up of four telescopes with 2 m collecting mirrors.
In the post-JWST era only missions that cost no more than $\sim 2 \mathrm{G} \$$ can realistically be considered by any space agency. The sizes of the corresponding instruments must therefore be significantly smaller, typically a 2.4 m mirror for the singledish coronagraph approach, or four 0.75 m telescopes for the interferometric approach, as recently proposed to ESA for the L3 mission slot (Quirrenbach 2013).

In this paper, an analytic model is described (Sections 2 and 3) that can estimate the science return of such size-reduced instruments in terms of exo-Earth spectroscopy as a function of $\eta_{\text {Earth }}$, for both visible coronagraphs (Sections 4, 5, and 7) and IR interferometers (Sections 6 and 7). Conclusions are given in Section 9, after a short discussion of ground-based instruments in Section 8.

Note that most parts of this study assume that a precursor mission has identified the list of target stars that actually have at least one telluric planet in their HZ, before the spectroscopic mission is launched. This prior detection would save a significant fraction of time for the spectroscopic missions, thereby increasing their scientific return (see Sections 4.7 and 6.7). There is a second, and even more important, reason for such a precursor mission. The question of the presence of extrasolar life will have great importance in the science of our century with an impact on the general public, the tax-payers. It is our responsibility to make a statement only if we have firm indications. The example of too rapid claims by the Viking missions is still present in many minds. "Extraordinary claims require extraordinary proofs/evidence" said Marcello Truzzi (1978)/Carl Sagan in a modern version of the Laplace (1749-) statement, "the weight of evidence for an extraordinary claim must be proportioned to its strangeness." Detecting a gas mixture, possibly indicative of a biosignature, would be a real indication of extrasolar life only if we have a solid idea of the
physical conditions at the surface of the planet, which requires knowledge of the planetary mass. The mass, combined with a radius estimated from the direct imaging mission, gives the mean density of the planet and allows a first distinction between rocky planets, water ocean-planets, and planets with a hydrogen-rich atmosphere. This is needed before deriving any statement on the possible presence of life on a planet.

The prior detection of Earth-like planets amenable to characterization by a high-contrast imaging/interferometry mission could be done by indirect detection techniques, such as high-precision ground-based radial velocity surveys (provided that stellar convection noise can be mitigated, e.g., Meunier et al. 2010), or high-precision astrometry, which would need a dedicated space mission (e.g., Malbet et al. 2012). However, the case of detection by the spectrometric mission itself is considered in Sections 4.7 and 6.7, with the associated disadvantages.

## 2. HYPOTHESES FOR A SIMPLE MODEL

To build a simple model, the following hypotheses are made. Systematic noises are assumed to be under control and the limiting noise is the quantum ("photon") noise, a critical hypothesis.
For the sake of simplicity, quantities such as integration times are computed only for some values of different parameters: position within the HZ around the star, observing wavelengths, and planetary radius.

1. Position in the HZ: the inner and outer limits of the HZ have been the object of great activity since the pioneering paper by Kasting et al. (1993). Many recent works in astronomy, e.g., Kopparapu et al. (2013), rely on 1D, therefore cloud-free, models. For a Sun-like star, the latter find mean semi-major axis $a_{\mathrm{IHZ}}=0.99 \mathrm{AU}$ for the inner boundary, and $a_{\mathrm{OHZ}}=1.70 \mathrm{AU}$ for the outer. Regarding the inner boundary, a recent work in geophysics (Leconte et al. 2014) reports a detailed 3D simulation of the Earth case that includes water clouds and their feedback on the surface temperature. The authors find that if our present Earth were moved from 1.0 to 0.96 AU , increasing the insolation by $8 \%$, from 341 to $368 \mathrm{~W} \mathrm{~m}^{-2}$, it would trigger a greenhouse effect, leading to the vaporization of all the terrestrial oceans in a short geological time. This result supports the idea that Earth is very close to the inner limit of the solar HZ. Recently, a 3D model was used for calculating inner and outer HZ boundaries, taking into account the impact of clouds (Kopparapu et al. 2014). These boundaries are found to depend on the stellar luminosity $(L)$, but also on its effective temperature, the possible phase locking of the planet (around M and late K stars), and the planetary mass, pointing out that the idea of a HZ depending only on the stellar luminosity is a convenient but simplified concept.

The HZ concept is subject to different criticisms. However, it is clear that a planet outside this zone cannot support life based on carbon and on water as a solvent.

In the present paper, the values of Kopparapu et al. (2013) are adopted for both solar-type and M stars, even it these values were derived for $G$ stars only (R. K. Kopparapu, private communication). Their geometrical mean value, $a_{\mathrm{HZ}}=\left(a_{\mathrm{IHZ}} * a_{\mathrm{OHZ}}\right)^{1 / 2}=$ $(0.99 * 1.70)^{1 / 2} L_{i}^{1 / 2}=1.30 L_{i}^{1 / 2} \mathrm{AU}$, is used, where $L_{i}$
is the stellar luminosity in solar units. This mean value corresponds to a uniform distribution of orbits in $\log (P)$, or $\log (a)$, where $P$ is the planet orbital period, as found by Batalha et al. (2012).
2. Wavelengths $(\lambda)$ : in the visible, the most demanding wavelength for angular resolution is the longest one. It is necessary to permit access to the whole domain required for the characterization of $\mathrm{O}_{2}$ and $\mathrm{H}_{2} \mathrm{O}(0.6-0.8 \mu \mathrm{~m}$, Des Marais et al. 2002). $\mathrm{CO}_{2}$ requires observations up to $1.1 \mu \mathrm{~m}$ for large abundances, and up to $2.1 \mu \mathrm{~m}$ for abundances similar to terrestrial ones (Des Marais et al. 2002). This is considered to be too demanding and not achievable in the mid-term future. $\mathrm{CO}_{2}$ will therefore be discarded for coronagraphs, and we will use $0.8 \mu \mathrm{~m}$ as the observing wavelength in this study.

In the thermal IR, $\lambda=10 \mu \mathrm{~m}$ is used as a proxy for the $(6-18 \mu \mathrm{~m})$ domain, permitting the characterization of $\left(\mathrm{H}_{2} \mathrm{O}\right), \mathrm{O}_{3}$, and $\mathrm{CO}_{2}$ (Des Marais et al. 2002). When spatial resolution is important, the most demanding value, $18 \mu \mathrm{~m}$, is used (Sections 6.1-6.3).
3. Planetary radius: in the search for extrasolar life, the relevant planets are rocky (Owen 1980), and possibly water ocean-planets (Léger et al. 2004; Selsis et al. 2007), all without a major hydrogen content in their atmosphere. They can be Earth analogs $\left(R_{\mathrm{pl}}<1.25\right.$, in units of Earth's radius), or super-Earths ( $R_{\mathrm{pl}}=1.25-2.0$, Borucki et al. 2011). When this parameter is important, radii of $1.0,1.5$, and 2.0 are considered individually, otherwise the mean value $R_{\mathrm{pl}}=1.5$ is used. ${ }^{8}$

Analyzing Kepler data, Rogers (2015) found that most rocky planets have a radius $R_{\mathrm{pl}}<1.6$. For a same mass, water ocean-planets have a lower density and may be a major component of hydrogen-free planets in the range $R_{\mathrm{pl}}=1.5-2.0$. However, their ability to harbor life is possibly lower than that of rocky planets (Tian \& Ida 2015), and the case $R_{\mathrm{pl}}=2.0$ is presented in the figures with dashed lines instead of full lines, to remind that they have an interest different from that of $R_{\mathrm{pl}}=1.0-1.5$ planets.
4. Parameters such as the planet albedo, instrument yield, etc., are those adopted by the detailed studies used to adjust the model.
5. Exozodiacal light level: its impact is discussed in Section 4.5 for a coronagraph and Section 6.5 for interferometers. In the following, exozodiacal light is arbitrarily assumed to be sufficiently low around target stars that it is not a major source of noise or confusion, either for coronagraphs or for interferometers.
In summary, the estimates of the present paper are made under favorable hypotheses, namely: (i) systematic noises have been reduced down about to the level of quantum noise, which will require major technical efforts, (ii) exozodiacal light is low enough not to be a major source of noise or confusion. This last hypothesis must be revisited when we get real information on its level.

[^1]
## 3. REQUIRED INTEGRATION TIMES

### 3.1. Signal for Coronagraphs and Interferometers

For an observation $(i)$ the signal is proportional to the number of photoelectrons incident on the detector from the planet:

$$
\begin{equation*}
S_{i}=a \Phi^{2} \Delta \lambda R_{\mathrm{pl}, i}^{2} D_{i}^{2} t_{i} \tag{1}
\end{equation*}
$$

where $a$ is a constant, in units of $1 /$ time, depending on the instrument throughput, planetary albedo...; $\Phi$ is the telescope diameter(s); $\Delta \lambda$, the spectral bandwidth; $R_{\mathrm{pl}, i}$, the planetary radius; $D_{i}$, the distance of the system from us; and $t_{i}$, the integration time allocated to the observation.

### 3.2. Noise for Coronagraphs

For a coronagraph, the main sources of noise are the quantum noise from stellar leakage and speckles, if the latter are stable enough with time, plus the noise of exozodiacal light. Assuming the latter to be low enough (Section 4.5), the noise is the square root of the number of photoelectrons collected within the point-spread function (PSF) of the planet during the integration time $t_{i}$ (Guyon et al. 2006, Figure 14):

$$
\begin{equation*}
N_{i}=\left[b_{\mathrm{cor}} \Phi^{2} \Delta \lambda L_{i} \rho_{i} D_{i}^{-2} t_{i}\right]^{1 / 2} \tag{2}
\end{equation*}
$$

where $b_{\text {cor }}$ is a constant, in units of 1/time, analogous to $a ; L_{i}$, the stellar luminosity; $\rho_{i}$, the residual transmission of the stellar light at the planet angular separation, a steep function of the angular distance of the source from the telescope optical axis of the coronagraph.

### 3.3. Noise for Interferometers

If instability noise (Chazelas et al. 2006; Lay 2006) can be mitigated, the main source of noise is the quantum noise from the sum of the solar zodiacal (SZ) flux, the exozodiacal flux, and the stellar leakage (Defrère et al. 2010).

SZ flux. When a nulling interferometer uses a single-mode fiber (SMF), the field of view (FOV) is limited by the PSF of each collecting telescope. For an IR albedo $A$, an optical depth of the zodiacal cloud $\tau$, and a temperature of the zodiacal dust at the spacecraft position $T_{\text {zcl }}$, the SZ flux is proportional to the surface brightness $B\left(\lambda, T_{\mathrm{zcl}}\right)$ of the zodiacal cloud multiplied by $\tau$, the solid angle of the telescope PSF, and the mirror area:

$$
\begin{equation*}
F_{\mathrm{SZ}} \propto(1-A) B\left(\lambda, T_{\mathrm{ZCl}}\right) \tau(\lambda / \Phi)^{2} \pi \Phi^{2} \Delta \lambda \tag{3}
\end{equation*}
$$

Noticeably, $F_{\text {SZ }}$ is independent of the telescope diameter $\Phi$. Its value relative to the other noise sources such as stellar leakage is larger for smaller values of $\Phi$. It is dominating for telescopes with a diameter less than 1 m (Defrère et al. 2010).

Exozodiacal flux. It is proportional to $\Phi^{2}$ because the PSF of individual telescopes ( 2 arcsec in diameter at $10 \mu \mathrm{~m}$ for $\Phi=1 \mathrm{~m}$ ) is expected to contain most of the exozodiacal emission, which has a characteristic size of $0.1 \operatorname{arcsec}(1 \mathrm{AU}$ at 10 pc ). If the exozodiacal cloud were mainly symmetric, it would be removed by the detection process, and therefore produce quantum noise only (end of Section 2). Its relative contribution to noise decreases as the telescope diameter decreases. For $\Phi<1 \mathrm{~m}$, and exozodiacal cloud density less than 10 times that of the SZ cloud (" 10 zodi" hereafter), it is
negligible compared to the contribution of the SZ cloud (Defrère et al. 2010, Section 4 therein).

Stellar leakage. A key parameter is the planetary flux/stellar leakage flux ratio. The IR flux from a planet in the HZ of its star is independent of the stellar properties (an emitting body at $\sim 300 \mathrm{~K}$ ). The IR flux from the star is proportional to its bolometric flux, $\propto L_{i} / D_{i}^{2}$, with a correction specific to each spectral type, ${ }^{9}\left(T_{*} / T_{o}\right)^{-3}$, where $T_{*}$ is the stellar effective temperature and $T_{\mathrm{o}}$ the solar one. This correction is important for M stars. Their bolometric contrast with a 300 K planet is more favorable than for Sun-like stars, but this correction factor decreases in the thermal IR, due to their relatively low temperatures. For an M2 star, the bolometric contrast with a 300 K planet is 30 times lower than for a G2 star, but after this correction it is only 5 times lower.
The transmission of a nulling interferometer, $\rho$, is limited by the instrument rejection ratio and the geometrical losses due to a partial resolution of the stellar disc. For F, G, and K stars (FGK hereafter), it is typically $\rho=10^{-5}$ (Defrère et al. 2010). Total noise is:

$$
\begin{equation*}
N_{i}=\left[b_{\text {int-1 }}\left(1+b_{\text {int }-2} \rho \Phi^{2} L_{i}\left(T_{*} / T_{\odot}\right)^{-3} D_{i}^{-2}\right) \Delta \lambda t_{i}\right]^{1 / 2} \tag{4}
\end{equation*}
$$

where the two terms in the sum correspond to the SZ cloud and stellar leakage, respectively; $b_{\text {int } 1}$ and $b_{\text {int } 2}$ are parameters that can be determined by a fit to detailed studies; $b_{\text {int } \_2}$ is dimensionless while $b_{\text {int } 1}$ is in units of $1 /$ time.

Using Figure 6 from Defrère et al. (2010) at $\lambda=10 \mu \mathrm{~m}$, $D=15 \mathrm{pc}, L=1, \Phi=2 \mathrm{~m}$, one gets the flux ratio $F_{\mathrm{SZ}} / F_{\text {st leaks }} \sim 5$, which allows the determination of $b_{\text {int }}$. It reads: $\bar{b}_{\text {int_2 }} \rho \sim 11$.

### 3.4. Required Integration Times

A signal-to-noise ratio, $S_{i} / \mathrm{N}_{i}$, results from Equations (1), and (2) or (4). This $S_{i} / \mathrm{N}_{i}$ must have a sufficient value to permit actual measurements, e.g., $\mathrm{S}_{i} / \mathrm{N}_{i}=10$. Then, the needed integration time, $t_{i}$, results.

A possible observational sequence is as follows. In a target list, stellar systems are ordered by increasing time $t_{i}$ and studied one after the other until the total mission duration is reached. The number of accessible targets results.

1. For coronagraphs, $t_{i}$ reads

$$
\begin{equation*}
t_{i}=c \Phi^{-2} \Delta \lambda^{-1} R_{\mathrm{pl}}^{-4} L_{i} \rho(i) D_{i}^{2} \tag{5}
\end{equation*}
$$

where $c$ is a parameter in units of time. It can be obtained by fitting the results of detailed models of coronagraphs, e.g., Lunine et al. (2009) or Levine et al. (2009).
2. For interferometers, $t_{i}$ reads

$$
\begin{equation*}
t_{i}=d\left[1+11 L_{i}\left(T_{*} / T_{\odot}\right)^{-3} \Phi^{2} D_{i}^{-2}\right]^{1 / 2} \Phi^{-4} \Delta \lambda^{-1} R_{\mathrm{pl}}^{-4} D_{i}^{4} \tag{6}
\end{equation*}
$$

where $d$ is a parameter, in units of time, that can be determined in a similar way.
3. For both instruments, the number of accessible targets during the mission lifetime, e.g., five years, $N_{\text {tot }}$, is

[^2]

Figure 1. Earth's spectrum in the $0.6-0.8 \mu \mathrm{~m}$ domain calculated from Des Marais et al. (2002, Figure 3 therein) in the case of a medium cloud coverage, for different $\mathrm{S} / \mathrm{N}$ and spectral resolutions. The top plot corresponds to $\mathrm{S} / \mathrm{N}=10$ (at $0.8 \mu \mathrm{~m})$ and $\lambda / \delta \lambda=70$, and the bottom plot to $\mathrm{S} / \mathrm{N}=20($ at $0.8 \mu \mathrm{~m})$ and $\lambda \delta \lambda=140$. The error bars indicate the intervals $\pm 1 \sigma$. The top plot would allow only the $\mathrm{O}_{2}$ A band to be detected (a single spectral point, at $4 \sigma$ relative to the continuum). In the bottom plot, two species would be detected in three spectral bands: $\mathrm{O}_{2}$ in its A and B bands ( $8 \sigma$ and $3 \sigma$, respectively) and $\mathrm{H}_{2} \mathrm{O}$ in its $0.72 \mu \mathrm{~m}$ band $(3 \sigma)$. See text for implications.
obtained by resolving:

$$
\begin{equation*}
\sum_{i=1}^{N_{\text {tot }}} t_{i}=5 \text { years } \tag{7}
\end{equation*}
$$

Equations (5)-(7) provide explicit dependences of the instrument capabilities upon quantities such as $\Phi$ [m], $\Delta \lambda[\mu \mathrm{m}], R_{\mathrm{pl}}\left[R_{\text {Earth }}\right], L_{i}\left[L_{\mathrm{o}}\right], \rho_{i}, D_{i}[\mathrm{pc}]$, and $\eta_{\text {Earth }}$, and are exploited hereafter. They make the impact of these parameters easy to grasp.

### 3.5. Required Signal-to-noise and Spectral Resolution

The upper parts of Figures 1 and 2 show the Earth's spectrum as it would be seen by a distant observer using $\mathrm{S} / \mathrm{N}=10, \lambda / \delta \lambda=70$ in the visible and 20 in the thermal IR. The lower plot of these two figures shows the case of a $\mathrm{S} / \mathrm{N}$ that is twice as large ( $\times 4$ integration time, no systematic noise) and a spectral resolution that is twice as large ( $\times 2$ integration time). The information content is significantly larger in these lower plots.

This suggests that the higher spectral resolutions ( $\lambda / \delta \lambda=140$ in the visible and $\lambda / \delta \lambda=40$ in the mid-IR) should be included in future visible coronagraphs and the midIR spectrometer. We note that $\mathrm{S} / \mathrm{N}=10$ for an Earth turns into $\mathrm{S} / \mathrm{N}=20$ for a $1.4 R_{\text {Earth }}$ super-Earth, which would make the detection of molecular species significantly easier.

In the thermal IR, the spectrum shown in the top plot of Figure 2 would allow $\mathrm{CO}_{2}(>10 \sigma)$ and possibly $\mathrm{O}_{3}(\sim 3 \sigma)$ to be detected. The bottom plot would allow the same species to be detected but without ambiguity for $\mathrm{O}_{3}(\sim 7 \sigma)$. In addition, one may argue for a marginal detection of the temperature inversion


Figure 2. Same as Figure 1 but for Earth's emission in the thermal IR calculated from Des Marais et al. (2002, Figure 2 therein). Spectral resolution, $\lambda / \delta \lambda$, is constant over the $5-20 \mu \mathrm{~m}$ domain. The top plot corresponds to $\mathrm{S} / \mathrm{N}=10($ at $18 \mu \mathrm{~m})$ and $\lambda \delta \lambda=20$, the bottom plot to $\mathrm{S} / \mathrm{N}=20($ at $18 \mu \mathrm{~m})$ and $\lambda / \delta \lambda=40$. The top plot would allow $\mathrm{CO}_{2}(>10 \sigma)$ and possibly $\mathrm{O}_{3}(\sim 3 \sigma)$ to be detected. The bottom plot would allow the same species to be detected but without ambiguity for $\mathrm{O}_{3}(\sim 7 \sigma)$. In addition, one may argue for a marginal detection of the temperature inversion in the atmosphere from the shape of the $15 \mu \mathrm{~m} \mathrm{CO}_{2}$ band, and of the presence of the $7.8 \mu \mathrm{~m} \mathrm{CH}_{4}$ band $(\sim 2 \sigma)$. The footprint of $\mathrm{H}_{2} \mathrm{O}$ in the $6-8 \mu \mathrm{~m}$ domain could also enter the discussion. It appears as a broad deviation from a blackbody spectrum obtained in the equivalent of the Earth's atmospheric windows, 8.2-9.2 and $10.5-12.0 \mu \mathrm{~m}$. This blackbody background $(T=254 \mathrm{~K} \pm 9 \mathrm{~K})$ is obtained by a twoparameter fit (amplitude and $T$ ) to the calculated spectral points plus an added Gaussian noise realization with $\sigma=N$.
in the atmosphere from the shape of the $15 \mu \mathrm{~m} \mathrm{CO}_{2}$ band, and of the presence of the $7.8 \mu \mathrm{~m} \mathrm{CH}_{4}$ band $(\sim 2 \sigma)$. The footprint of $\mathrm{H}_{2} \mathrm{O}$ in the $6-8 \mu \mathrm{~m}$ domain could also enter the discussion. It appears as a broad deviation from a blackbody spectrum determined from the simulated data points, including noise, obtained in the equivalent of the Earth's atmospheric windows, 8.2-9.2 and $10.5-12.0 \mu \mathrm{~m}$. This discussion suggests the need for the mid-IR spectrometer to reach a spectral resolution $\lambda / \delta \lambda=40$.

In the rest of the paper, the lower values for $\mathrm{S} / \mathrm{N}(=10)$ and $\lambda / \delta \lambda(=70$ or 20$)$ are adopted. The corresponding limited quality of the spectra is not as severe as it may seem. If the spectra actually observed were similar to those of the top plots of Figures 1 and 2, the detection of $\mathrm{O}_{2}$ in the visible $(0.76 \mu \mathrm{~m})$ and $\mathrm{CO}_{2}$ in the thermal IR $(15 \mu \mathrm{~m})$ would be at least suspected. The observers' enthusiasm would be such that longer integration times (e.g., $\times 8$ ) would be attributed to the corresponding planets, and better spectra obtained, in the favorable case where systematic noise does not dominate the error budget, a key point for attention when building the missions.

In conclusion, we think that the selected values are relevant to compare the capabilities of different instruments, but are probably not the final ones.

## 4. CORONAGRAPHS

### 4.1. Double-star Problem

Can a stellar companion prevent the study of a target star, the companion being physically bound, or not (object in projection)?

In the vicinity of the target, the light from a companion is from its Airy rings and from its speckles due to defects in the mirrors. The former are deterministic and can be subtracted if the instrumental PSF is known, leaving only the quantum noise. The latter requires that the speckles can be reduced by a specific method, such as that proposed by Thomas et al. (2014).
The corresponding $\mathrm{S} / \mathrm{N}$ requirement leads to a constraint on the angular distance of the companion. The signal is the number of photoelectrons incident on the detector from a possible planet, $N_{\mathrm{pl}}$, and a minimum estimate of the noise is the quantum noise from the Airy rings of the companion, $\left(N_{\text {comp }}\right)^{1 / 2}$.

Using typical values for the nearest stars: $D=3 \mathrm{pc}$, a companion with an $R$ magnitude $R_{\text {comp }}=3$, a $\Phi=2.4 \mathrm{~m}$ telescope, and an integration time of one day, a $\mathrm{S} / \mathrm{N}$ of 10 requires an angular separation (see Appendix A):

$$
\begin{align*}
\theta_{\text {comp }}> & 35.5(D / 3 \mathrm{pc})^{1.33} 10^{-0.13\left(R_{\text {comp }}-3\right)}  \tag{8}\\
& \times(\Phi / 2.4 \mathrm{~m})^{2}(t / 1 \text { day })^{-1 / 3} \quad[\operatorname{arcsec}]
\end{align*}
$$

Only stellar systems fulfilling this requirement are kept in the target list. This is a minimum requirement, assuming full cancelation of the speckles due to the companion and the mirror defects by an appropriate system (Thomas et al. 2014), probably an optimistic assumption.
The Hipparcos cataloge of nearby F, G, K, M stars is used in its 2007 version of data reduction (van Leeuwen 2007), with stellar features (distance, luminosity...) as compiled by J. Maldonado (2015, private communication) and M. Turnbull (2015, in preparation). Features of the 15 nearest FGK stars with a bright companion and resulting minimum integration time are given in Table 1. The key $\alpha$ Cen (A, B) multiple system would require a special effort, $3.6 \times 10^{-2}$ years $=13$ days of continuous integration, whereas the other ones, with the exception of 70 Oph A, should be observable (see also Section 6.1).

### 4.2. Orbital and Orientation Problems

For face-on circular orbits, the signal from a planet is continuously that at full elongation, i.e., that from an illuminated half disc.
For inclined orbits the situation is less favorable. Planets close to the IWA at full elongation spend only a small fraction of their time outside of it along their orbit. For $\alpha=60^{\circ}$, the mean value of inclination angle for randomly oriented orbits, this fraction is only $31 \%$ for a planet whose full elongation is 1.1 times the IWA. Without a prior detection determining the planetary mass, orbit, and ephemerides, four visits would be needed. For planets closer to their stars, e.g., $1.05 \times$ IWA, the fraction would be $23 \%$, requiring five visits. A compromise could be to limit the search to three or four visits per target, accepting not being exhaustive. However, the planetary mass would remain unknown, with the corresponding lack in our

Table 1
Nearby FGK Double Stars ${ }^{\text {a }}$

| Target Star | $\alpha$ Cen B | $\epsilon$ Eri | 61 Cyg B | Procyon A |
| :--- | :---: | :---: | :---: | :---: | :---: |
| $D[\mathrm{pc}]$ | 1.29 | 3.21 | 3.5 | 3.5 |
| $R_{\text {comp }}[\mathrm{mag}]$ | 0.0 | 17.3 | 5.2 | 10.8 |
| $\theta_{\text {comp }}[\mathrm{arcsec}]$ | $10($ in 2030$)$ | 17.1 | $>20$ as | 4.7 |
| $t_{\text {integ }}[\mathrm{yr}]$ | $3.6 \mathrm{E}-2$ | $\ll 1.0 \mathrm{E}-3$ | $<4.1 \mathrm{E}-3$ | $2.2 \mathrm{E}-3$ |

Note.
${ }^{\mathrm{a}}$ For a 2.4 m mirror.


Figure 3. Schematic light transmission by an optical system vs. the angular distance of the source from its optical axis for a telescope free from central obscuration (full line = Airy function), and for a telescope with a coronagraph having a transmission of $10^{-10}$ at $2.5 \lambda / \Phi$ (dashed line). Solar zodiacal light (dotted line) is stable and can be subtracted, but produces quantum noise. Exozodiacal light is not represented. The PSF of a possible Earth-like planet is represented by a full line at the low part of the figure (from Lunine et al. 2009).
understanding of the physics at the planetary surface (see Section 9).

In most of the following sections, a prior detection of planets in the HZ of the nearby stars is assumed.

### 4.3. Light Rejection by a Coronagraph

Following Lunine et al. (2009, Figure 11.2 therein), a simplified dependence of the light transmission as a function of the angle between source and instrument axis is used (Figure 3), with transmission $\rho$ :

$$
\begin{array}{rlr}
\rho\left(\theta_{i}\right) & =10^{-10 \theta_{i} / \overline{\mathrm{IWA}}} \text { for } \theta_{i} / \overline{\mathrm{IWA}}<1 \\
& =10^{-10} \quad & \text { for } \theta_{i} / \overline{\mathrm{IWA}}>1, \tag{9}
\end{array}
$$

where $\theta_{i}$ is the angular distance of the HZ of star $i$, the starplanet angular distance when the planet is at full elongation, $\theta_{i}=\theta_{\mathrm{HZ}, i},=a_{\mathrm{HZ}, i} / D_{i}$, and $\overline{\text { IWA }}$ is the IWA of the coronagraph, in radian.

For a system at distance $D_{i}$, the transmission reads

$$
\begin{align*}
\rho\left(D_{i}\right) & =10^{-10 /\left(D_{i} / D_{\mathrm{c} i}\right)} & & \text { for } D_{i} / D_{\mathrm{c} i}<1  \tag{10}\\
& =10^{-10} & & \text { for } D_{i} / D_{\mathrm{c} i}>1
\end{align*}
$$

where $D_{\mathrm{c}, i}$ is the critical distance of system $i, D_{\mathrm{c}, i}=a_{\mathrm{HZ}, i}$. $\overline{\mathrm{IWA}}^{-1}$. At $\lambda=0.8 \mu \mathrm{~m}$, it reads: $\left(D_{\mathrm{c}, i} / 1 \mathrm{pc}\right)=6.06(\Phi / 1 \mathrm{~m})$

IWA $^{-1} a_{\mathrm{HZ}, i} L_{i}^{1 / 2}[\mathrm{pc}]$, with IWA in units of $\lambda / \Phi$, and $a_{\mathrm{HZ}, i}$ in units of AU $L_{i}^{-1 / 2}$.

### 4.4. Calibrating the Integration Time and the Value of $c$

A detailed study by Lunine et al. (2009, Table 2 therein) states that a coronagraph with a 5 m telescope, IWA $=3 \lambda / \Phi$, or 100 mas at $\lambda=0.8 \mu \mathrm{~m}$, searching for Earth-size planets $\left(R_{\mathrm{pl}}=1.0\right)$ at $a_{\mathrm{HZ}}=1.0 L_{i}^{1 / 2}[\mathrm{AU}]$ with a spectral resolution suitable for detection $(\lambda / \Delta \lambda \sim 2)$, can investigate 44 stars in five years.

The parameter $c$ can be determined by using Equations (5) and (7) and that requirement, $N_{\text {tot }}=44$ for a five-year mission. Table 2 gives the integration times divided by $c, t_{i} / c$, and their sum, $S\left(t_{i} / c\right)$, for stars in the target list, until rank 44 is reached (Hip15371, with $S\left(t_{i} / c\right)=1.78 \times 10^{-8}$ ). The value of $c$ results:

$$
c=5 \text { years } / 1.78 \times 10^{-8}=2.81 \times 10^{8} \text { years }
$$

The uncertainty on the model predictions can be estimated by using the parameter value determined above, $c=2.81 \times 10^{8}$ years, and applying the model to coronagraphs with different features, such as those studied by Levine et al. (2009), and comparing the predictions from the model to those from the detailed studies. For the flagship TPF-C instrument (2002), an 8 m mirror working at IWA $=4 \lambda / \Phi$, and a $R_{\mathrm{pl}}=1.0$ planet in the HZ, the model predicts that 71.6 stellar systems can be investigated in three years, whereas Levine et al. (2009) find 73 systems. For $\Phi=2.5 \mathrm{~m}$, IWA $=2.5 \lambda / \Phi$, and a three-year mission, the model finds 14.3 systems, instead of 16 (Levine et al. 2009). The similarity between these numbers indicates the robustness of the model.

### 4.5. Distinguishing Planet and Exozodiacal Disc

It is well known that the presence of exozodiacal dust around a star can hamper the direct detection and characterization of telluric planets in the HZ (e.g., Beichman et al. 2006; Roberge et al. 2012). Its light produces a signal much stronger than the planetary signal, 350 times in the case of 1 zodi (the zodiacal light luminosity of the Solar System) at $10 \mu \mathrm{~m}$ (Defrère et al. 2010), and a similar value in the visible. The planetary signal must be disentangled from it by studying the image of the system, at low spatial resolution (a few resolution elements, $\lambda / \Phi$, in the image of the planet-disc system). The impact is twofold: (1) as a source of noise, and (2) as a source of confusion (e.g., Defrère et al. 2012).
Roberge et al. (2012) published the first report by NASA's ExoPAG working group on that problem, and concluded that, for a 2 m class telescope, the required observing time increases dramatically with the level of exozodiacal light, even from zero to one zodi (Figure 2, therein). They also point out that this has

Table 2
Integration Times Divided by $c$ for FGK Stars ${ }^{\text {a }}$

| HIP | Common Name | $D$ (pc) | V | $L_{\text {bol }} / L_{0}$ | Spec. Type | $\rho$ | $t_{i} / c$ | Star \# | $S\left(t_{i} / c\right)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 71681 | $\alpha$ Cen B | 1.29 | 1.35 | 0.525 | K0V | $1.00 \mathrm{E}-10$ | $6.99 \mathrm{E}-12$ | 1 | $6.99 \mathrm{E}-12$ |
| 104217 | 61 Cygni B | 3.50 | 5.95 | 0.097 | K7.0V | $9.97 \mathrm{E}-10$ | $9.49 \mathrm{E}-12$ | 2 | $1.65 \mathrm{E}-11$ |
| 104214 | 61 Cygni A | 3.50 | 5.20 | 0.134 | K5.0V | $1.00 \mathrm{E}-10$ | $1.31 \mathrm{E}-11$ | 3 | $2.96 \mathrm{E}-11$ |
| 71683 | $\alpha$ Cen A | 1.29 | -0.01 | 1.611 | G2.0V | $1.00 \mathrm{E}-10$ | $2.14 \mathrm{E}-11$ | 4 | $5.10 \mathrm{E}-11$ |
| (...) | ... | ... | ... | ... | ... | ... | ... | $\ldots$ | ... |
| 10644 | NA | 10.78 | 4.86 | 1.213 | G0V | $1.00 \mathrm{E}-10$ | $1.13 \mathrm{E}-09$ | 43 | $1.67 \mathrm{E}-08$ |
| 15371 | NA | 12.03 | 5.24 | 1.034 | G2V | $2.91 \mathrm{E}-09$ | $1.20 \mathrm{E}-09$ | 44 | 1.78E-08 |
| 80337 | NA | 12.78 | 5.37 | 1.034 | G3/5V | $9.16 \mathrm{E}-09$ | $1.35 \mathrm{E}-09$ | 45 | $1.91 \mathrm{E}-08$ |
| (...) | ... | ... | ... | ... | ... | ... | ... | $\ldots$ | ... |

Notes. The star \# in bold (44) corresponds to the number of stars that can be studied with the instrument described by Lunine et al. (2009).
${ }^{\text {a }}$ Conditions are those by Lunine et al. (2009). An exhaustive list, up to rank 200, is available in electronic form.
(This table is available in its entirety in machine-readable form.)
greater consequences for the capability of a 2 m coronagraph than $\eta_{\text {Earth }}$ being small. Obviously, if all stars have very bright exozodiacal disks, the value of $\eta_{\text {Earth }}$ does not really matter since it will be extremely difficult to detect any planet anyway.

Very little is currently known about the prevalence of exozodiacal dust around nearby main-sequence stars. Based on Keck Nuller observations of a sample of 20 solar-type stars with no far-IR excess previously detected (i.e., no detectable outer dust reservoir), a recent study by Mennesson et al. (2014) concludes with high confidence (95\%) that the median level of exozodiacal dust around such stars is below 60 times the solar value. This state-of-the-art sensitivity to exozodiacal dust, however, is much too high to decide what is the fraction of stars with sufficiently low dust levels to enable the detection of telluric planets in the HZ. This requires a better knowledge of the faint end of the exozodiacal dust luminosity function, which should be obtained soon by the LBTI instrument (Defrère et al. 2015). Therefore, given the lack of knowledge on this topic, we make the arbitrary assumption in this study that the level of exozodiacal emission is sufficiently low, and ignore it, leaving the study of the impact of this spurious light on coronagraphs for a more detailed paper.

### 4.6. Performances of an Affordable Coronagraph

What could be an affordable coronagraph? Within the present and mid-future funding possibilities, a 2.4 m telescope seems more likely than a 5 m one. Recently, NASA acquired two such telescopes and is considering the implementation of a coronagraph on one of them, WFIRST-AFTA (WFIRST 2014). Unfortunately, it has a central obstruction and six struts for holding the secondary mirror, making it less suitable than an off-axis telescope. This translates into a contrast that cannot reach the required $10^{-10}$ value, but makes it still valuable for characterizing larger planets, an opportunity not to miss.
An optimized off-axis telescope, with the same mirror size, seems affordable in the mid-future, at mass and cost similar to that of WFIRST-AFTA. The capabilities of a coronagraph on a 2.4 m telescope are used, with a $10^{-10}$ transmission, IWA $=$ $2.5 \lambda / \Phi$ or 170 mas at $\lambda=0.8 \mu \mathrm{~m}$, assuming that progress in the future will make this performance reachable. A worksheet similar to Table 2 is made with the above values and those from Sections 2 and 4.3: $a_{\mathrm{HZ}, \mathrm{I}}=1.30 L_{i}^{1 / 2}[\mathrm{AU}]$,
$D_{\mathrm{c}, i}=7.56 L_{i}^{1 / 2} \quad[\mathrm{pc}], \quad R_{\mathrm{pl}}=1.5, \quad \lambda \Delta \lambda=70$ suitable for spectroscopy searching for the 0.70 and $0.77 \mu \mathrm{~m} \mathrm{O}_{2}$ bands (Des Marais et al. 2002), and $c=2.81 \times 10^{8}$ years (Table 3).

The impact of $\eta_{\text {Earth }}$ is estimated as follows. A target list is used with stars ranked by increasing integration time $t_{i}$. The total time up to rank $i, S\left(t_{i}\right)$, is calculated. If $\eta_{\text {Earth }}$ is less than $100 \%$ only one star out of $1 / \eta_{\text {Earth }}$ has a planet. If the stars with relevant planets are known in advance, it could be possible to go deeper in the list, leaving aside the irrelevant stars. For a given mission duration it will be equivalent to investigate all stars, up to number $N_{\text {virt }}$, in a virtual mission that would last longer, $5 \mathrm{yr} / \eta_{\text {Earth }}$, but of these only $N_{\text {virt }} \times \eta_{\text {Earth }}$ have planets.

If all stars had the same observation times, the value of $\eta_{\text {Earth }}$ would have no impact on the number of studied planets: $N_{\mathrm{pl}}=N_{\mathrm{pl}}\left(1 / \eta_{\text {Earth }}\right) \times \eta_{\text {Earth }}$. In reality, the integration time increases steeply with the rank in the lists (Tables 2 and 3), and lower values of $\eta_{\text {Earth }}$ lead to significantly lower numbers of planets. This reasoning would be exact for objects in large numbers. For objects in small numbers it has the limitations of small number statistics.

Previous identification of the suitable stars is assumed, and the ephemerides determined, so that the whole mission time can be spent on spectroscopy. This is of special importance if $\eta_{\text {Earth }}$ is significantly smaller than $100 \%$ so that many nearby stars have no suitable planet. The spectroscopic mission would not lose time on them (Section 9).

Using Table 3, one finds that for $\eta_{\text {Earth }}=100 \%$, a five-year mission, and $R_{\mathrm{pl}}=1.5$, eight planets can be studied in spectroscopy around the first eight stars; for $\eta_{\text {Earth }}=10 \%$ the virtual mission lasts 50 years, $N_{\text {virt }}$ is 15 , and 1.5 planets can be studied; for $\eta_{\text {Earth }}=1 \%, N_{\text {virt }}$ is 34 , and $N_{\mathrm{pl}}=0.34$.
It is noticeable that among these best 100 systems, there is no $M$ star. The first M star is Proxima Cen $(D=1.30 \mathrm{pc})$ with rank 210; Barnard's star $(D=1.83 \mathrm{pc})$ is 224th. This is due to the low efficiency of coronagraphs for planets inside the IWA, which is the case for the HZ of low-luminosity stars. Coronagraphic transmission in the HZ is $1.9 \times 10^{-2}$ and $3.1 \times 10^{-3}$ for the two quoted M stars, far from the $10^{-10}$ value outside the IWA.

This procedure can be repeated for different values of $\eta_{\text {Earth }}$ and planetary radius. The number of planets that can be studied in spectroscopy is found as a function of $\eta_{\text {Earth }}$ (Table 4 and Figure 4). When the size distribution of planets in the HZ and

Table 3
Possible Target List for a 2.4 m Coronagraph

| Hipparcos | Common Name | $D(\mathrm{pc})$ | V | $L_{\text {bol }}\left(L_{\text {Sun }}\right)$ | Spec. Type | $\rho$ | $t_{i}(\mathrm{yr})$ | $i$ | $S\left(t_{i}\right)(\mathrm{yr})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 71681 | $\alpha$ Cen B | 1.29 | 1.35 | 0.525 | K0V | $1.00 \mathrm{E}-10$ | $5.87 \mathrm{E}-02$ | 1 | $5.87 \mathrm{E}-02$ |
| 71683 | $\alpha$ Cen A | 1.29 | -0.01 | 1.611 | G2.0V | $1.00 \mathrm{E}-10$ | $1.80 \mathrm{E}-01$ | 2 | $2.39 \mathrm{E}-01$ |
| 108870 | $\epsilon$ Indi A | 3.62 | 4.69 | 0.227 | K4V | $1.16 \mathrm{E}-10$ | $2.32 \mathrm{E}-01$ | 3 | $4.71 \mathrm{E}-01$ |
| 16537 | $\epsilon$ Eri | 3.21 | 3.71 | 0.351 | K2.0V | $1.00 \mathrm{E}-10$ | $2.44 \mathrm{E}-01$ | 4 | $7.15 \mathrm{E}-01$ |
| 8102 | $\tau$ Ceti | 3.65 | 3.49 | 0.519 | G8.5V | $1.00 \mathrm{E}-10$ | $4.65 \mathrm{E}-01$ | 5 | $1.18 \mathrm{E}+00$ |
| 19849 | o 2 Eri | 4.98 | 4.43 | 0.425 | K0.5V | $1.30 \mathrm{E}-10$ | $9.21 \mathrm{E}-01$ | 6 | $2.10 \mathrm{E}+00$ |
| 88601 | 70 Oph | 5.10 | 4.03 | 0.681 | K0V | $1.00 \mathrm{E}-10$ | $1.19 \mathrm{E}+00$ | 7 | $3.29 \mathrm{E}+00$ |
| 15510 | 82 Eri | 6.04 | 4.26 | 0.691 | G8.0V | $1.00 \mathrm{E}-10$ | $1.70 \mathrm{E}+00$ | 8 | $4.99 \mathrm{E}+00$ |
| 3821 | $\eta$ Cas A | 5.94 | 3.45 | 1.312 | G3V | $1.00 \mathrm{E}-10$ | $3.12 \mathrm{E}+00$ | 9 | $8.11 \mathrm{E}+00$ |
| 99240 | $\delta \mathrm{Pav}$ | 6.11 | 3.53 | 1.332 | G8.0IV | $1.00 \mathrm{E}-10$ | $3.34 \mathrm{E}+00$ | 10 | $1.15 \mathrm{E}+01$ |
| 37279 | Procyon A | 3.51 | 0.40 | 7.118 | F5IV-V | $1.00 \mathrm{E}-10$ | $5.88 \mathrm{E}+00$ | 11 | $1.73 \mathrm{E}+01$ |
| 61317 | $\beta \mathrm{CVn}$ | 8.44 | 4.24 | 1.268 | G0V | $1.00 \mathrm{E}-10$ | $6.07 \mathrm{E}+00$ | 12 | $2.34 \mathrm{E}+01$ |
| 1599 | ... | 8.59 | 4.23 | 1.333 | G0V | $1.00 \mathrm{E}-10$ | $6.61 \mathrm{E}+00$ | 13 | $3.00 \mathrm{E}+01$ |
| 64394 | $\ldots$ | 9.13 | 4.24 | 1.477 | G0V | $1.00 \mathrm{E}-10$ | $8.27 \mathrm{E}+00$ | 14 | $3.83 \mathrm{E}+01$ |
| 105858 | $\ldots$ | 9.26 | 4.22 | 1.545 | F7V | $1.00 \mathrm{E}-10$ | $8.91 \mathrm{E}+00$ | 15 | $4.72 \mathrm{E}+01$ |
| 89937 | $\chi$ Dra | 8.06 | 3.56 | 2.141 | F7Vvar | $1.00 \mathrm{E}-10$ | $9.34 \mathrm{E}+00$ | 16 | $5.65 \mathrm{E}+01$ |
| 86974 | ... | 8.31 | 3.41 | 2.776 | G5IV | $1.00 \mathrm{E}-10$ | $1.29 \mathrm{E}+01$ | 17 | $6.94 \mathrm{E}+01$ |
| 22449 | 1 Ori | 8.07 | 3.17 | 2.997 | F6V | $1.00 \mathrm{E}-10$ | $1.31 \mathrm{E}+01$ | 18 | $8.25 \mathrm{E}+01$ |
| 104214 | 61 Cyg A | 3.50 | 5.20 | 0.134 | K5.0V | $1.22 \mathrm{E}-08$ | $1.34 \mathrm{E}+01$ | 19 | $9.59 \mathrm{E}+01$ |
| 27072 | ... | 8.93 | 3.59 | 2.514 | F7V | $1.00 \mathrm{E}-10$ | $1.35 \mathrm{E}+01$ | 20 | $1.09 \mathrm{E}+02$ |
| 2021 | $\beta \mathrm{Hyi}$ | 7.46 | 2.82 | 3.702 | G1IV | $1.00 \mathrm{E}-10$ | $1.38 \mathrm{E}+01$ | 21 | $1.23 \mathrm{E}+02$ |
| 32349 | Sirius A | 2.63 | -1.44 | 30.483 | A1.0V | $1.00 \mathrm{E}-10$ | $1.42 \mathrm{E}+01$ | 22 | $1.37 \mathrm{E}+02$ |
| 14632 | $\ldots$ | 10.54 | 4.05 | 2.355 | G0V | $1.00 \mathrm{E}-10$ | $1.76 \mathrm{E}+01$ | 23 | $1.55 \mathrm{E}+02$ |
| 17378 | $\ldots$ | 9.04 | 3.52 | 3.374 | K0IV | $1.00 \mathrm{E}-10$ | $1.85 \mathrm{E}+01$ | 24 | $1.74 \mathrm{E}+02$ |
| 97649 | Altair | 5.12 | 0.76 | 10.649 | A7IV-V | $1.00 \mathrm{E}-10$ | $1.87 \mathrm{E}+01$ | 25 | $1.92 \mathrm{E}+02$ |
| 12777 | $\ldots$ | 11.13 | 4.10 | 2.418 | F7V | $1.00 \mathrm{E}-10$ | $2.01 \mathrm{E}+01$ | 26 | $2.12 \mathrm{E}+02$ |
| 96100 | $\sigma$ Dra | 5.75 | 4.67 | 0.436 | G9.0V | $2.10 \mathrm{E}-09$ | $2.04 \mathrm{E}+01$ | 27 | $2.33 \mathrm{E}+02$ |
| 27913 | $\chi$ Ori | 8.66 | 4.39 | 1.166 | G0V | $3.78 \mathrm{E}-10$ | $2.22 \mathrm{E}+01$ | 28 | $2.55 \mathrm{E}+02$ |
| 78072 | ... | 11.25 | 3.85 | 3.134 | F6V | $1.00 \mathrm{E}-10$ | $2.67 \mathrm{E}+01$ | 29 | $2.82 \mathrm{E}+02$ |
| 57757 | $\ldots$ | 10.93 | 3.59 | 3.792 | F9V | $1.00 \mathrm{E}-10$ | $3.04 \mathrm{E}+01$ | 30 | $3.12 \mathrm{E}+02$ |
| 109176 | $\ldots$ | 11.73 | 3.77 | 3.631 | F5V | $1.00 \mathrm{E}-10$ | $3.36 \mathrm{E}+01$ | 31 | $3.46 \mathrm{E}+02$ |
| 7513 | $\ldots$ | 13.49 | 4.09 | 3.636 | F8V | $1.00 \mathrm{E}-10$ | $4.45 \mathrm{E}+01$ | 32 | $3.90 \mathrm{E}+02$ |
| 116771 | $\ldots$ | 13.71 | 4.13 | 3.698 | F7V | $1.00 \mathrm{E}-10$ | $4.67 \mathrm{E}+01$ | 33 | $4.37 \mathrm{E}+02$ |
| 61941 | $\ldots$ | 11.68 | 3.44 | 5.276 | F1V | $1.00 \mathrm{E}-10$ | $4.84 \mathrm{E}+01$ | 34 | $4.85 \mathrm{E}+02$ |
| 102485 | $\ldots$ | 14.68 | 4.13 | 4.056 | F5V | $1.00 \mathrm{E}-10$ | $5.87 \mathrm{E}+01$ | 35 | $5.44 \mathrm{E}+02$ |
| 81693 | $\ldots$ | 10.72 | 2.81 | 7.732 | F9IV | $1.00 \mathrm{E}-10$ | $5.97 \mathrm{E}+01$ | 36 | $6.04 \mathrm{E}+02$ |
| 70497 | $\ldots$ | 14.53 | 4.04 | 4.419 | F7V | $1.00 \mathrm{E}-10$ | $6.27 \mathrm{E}+01$ | 37 | $6.66 \mathrm{E}+02$ |
| 16852 | $\cdots$ | 13.96 | 4.29 | 3.292 | F8V | $1.50 \mathrm{E}-10$ | $6.46 \mathrm{E}+01$ | 38 | $7.31 \mathrm{E}+02$ |
| 113368 | Fomalhaut | 7.70 | 1.23 | 16.466 | A3V | $1.00 \mathrm{E}-10$ | $6.57 \mathrm{E}+01$ | 39 | $7.97 \mathrm{E}+02$ |
| 59199 | ... | 14.94 | 4.02 | 4.558 | F0IV/V | $1.00 \mathrm{E}-10$ | $6.84 \mathrm{E}+01$ | 40 | $8.65 \mathrm{E}+02$ |

Notes. A list up to rank 100 is available in machine-readable form.
${ }^{\mathrm{a}}$ Required integration time for target $i$ and $R_{\mathrm{pl}}=1.5$.
${ }^{\mathrm{b}}$ Cumulative time for targets $1,2, \ldots, i$.
(This table is available in its entirety in machine-readable form.)

Table 4
Number of Planets Accessible to a 2.4 m Coronagraph

| $\eta_{\text {Earth }}(\%)$ | $R_{\mathrm{pl}}=1.0$ | $R_{\mathrm{pl}}=1.5$ | $R_{\mathrm{pl}}=2.0$ |
| :--- | :---: | :---: | :---: |
| 1 | 0.19 | 0.34 | 0.48 |
| 3 | 0.39 | 0.75 | 1.05 |
| 10 | 1.00 | 1.50 | 2.30 |
| 30 | 2.10 | 3.30 | 4.80 |
| 100 | 5.00 | 8.00 | 11.00 |

$\eta_{\text {Earth }}$ are known, a precise estimate of the number of accessible planets will be possible.

The dependence of $N_{\mathrm{pl}}$ on $\eta_{\text {Earth }}$ can be fitted by a power law with an exponent $\beta_{\text {coron }}=0.71$.

Table 4 and Figure 4 are one of the major results of the present paper. They give the number of planets that can be studied in spectroscopy, with a built-in coronagraph. For $\eta_{\text {Earth }}=10 \%$, it is between 1 and 2.3 according the planetary radius, $N_{\mathrm{pl}}=1.5$ for $R_{\mathrm{pl}}=1.50$. This is very small number statistics and it is therefore affected by the corresponding uncertainties.

### 4.7. Possible Detection by the Coronagraph

Although there would be major disadvantages to a situation where suitable planets are not previously identified (Section 9), one can estimate how many stars could be investigated by the coronagraph, searching for suitable planets, and later performing spectroscopy on the detected objects. Assuming that this


Figure 4. Number of planets located in the habitable zone that can be studied in spectroscopy $(\lambda \Delta \lambda \sim 70)$ with a IWA $=2.5 \lambda / \Phi$ coronagraph on a 2.4 m telescope, vs. $\eta_{\text {Earth }}$, for different values of the planetary radius, under the major hypothesis that exozodiacal light does not prevent planet detection. The case of $R_{\mathrm{pl}}=2.0 R_{\text {Earth }}$ planets is represented with a dashed line to indicate that they are probably not rocky (Rogers 2015, Figure 2 therein). Data points are calculated on target lists and are rather well aligned on power-law lines with an exponent $\beta_{\text {coron }}=0.71$ (lines).
could be done with three visits to limit the phase problems (Section 4.2), and a spectral resolution $\lambda \Delta \lambda=4$, the proportionality of the required time per visit to $\Delta \lambda$ (Equation (5)) gives the observing time. Explicitly, if 2.5 years are dedicated to the detection, the equivalent time in Table 3 is 2.5 years $\times(1 / 3) \times 70 / 4=14.6$ years. The coronagraph could investigate targets up to rank 11, Procyon A ( 3.51 pc ).
For $\eta_{\text {solar }}=10 \%$, the 2.5 years left would correspond to a virtual mission of 25 years, which exceeds cumulated times for rank 11. These 2.5 years are then sufficient to study in spectroscopy $11 \times 0.10=1.1$ planets, with the high risks of statistics on very small numbers, and the hypothesis on the level of exozodiacal light.

## 5. STARSHADE

A starshade is an interesting option for direct imaging, because it can suppress stellar light to a very high level, e.g., a few $10^{-11}$ transmission outside its IWA, the remaining light being due not to the defects of the collecting telescope but to those of the starshade, which is subjected to variable sunshine.

Its IWA is driven by wavelength, required rejection, shade size, and associated telescope-shade distance, but not by the telescope features. The size of the latter determines the required integration time and the capability to separate the planetary image from the exozodiacal cloud. The Interim Report on ExoS by NASA (Seager et al. 2014) provides an estimate of the capabilities of an affordable starshade.

In that report, the capabilities are calculated for the detection of Earth-like planets located at $1.0 L^{1 / 2} \mathrm{AU}$ from their stars, and $R_{\mathrm{pl}}=1.0, \lambda=0.6 \mu \mathrm{~m}, \lambda / \Delta \lambda=7, \mathrm{~S} / \mathrm{N}=3$. The integration times are estimated for the best 20 stars ranked in a target list
(Tables 3.2-1 and 3.3-1 therein). The total integration time of that program is 68 days, and detections have a mean completeness of about $40 \%$.

The calculation can be transposed to the spectroscopy of identified planets: for spectroscopy in the $0.6-0.8 \mu \mathrm{~m}$ band $\left(\mathrm{O}_{2}\right.$ A-band at $0.76 \mu \mathrm{~m}$ ) with $\lambda / \Delta \lambda=70, \mathrm{~S} / \mathrm{N}=10$, with a 2.4 m telescope, on $R_{\mathrm{pl}}=1.0,1.5$, or 2.0 planets in the HZ (1.30 renormalized AU). Assuming quantum noise only, a total integration time of $\leqslant 350$ days is found for $\eta_{\text {Earth }}=100 \%$, a situation where all the 20 targets could be studied. The fiveyear duration of the mission is sufficient for data transmission and star retargeting, as described in the Interim Report. The limitation of such a mission comes from the IWA permitted by the 34 m starshade, not the size of the telescope even for spectroscopy, and the extraction of the planetary image from that of the exozodiacal disc, which depends on the telescope size. With a 2.4 m telescope these limitations are similar to those for a built-in coronagraph (Section 4.5).

Table 5 shows the target list for the instrument proposed by Seager et al. (2014) and a 2.4 m mirror. Systems are ranked by decreasing angular distance for planets located at $1.3 L^{1 / 2} \mathrm{AU}$ at full elongation, until the IWA of the instrument ( 115 mas ) is reached, which determines the cut-off of the list. Whatever the value of $\eta_{\text {Earth }}$, a maximum of 20 stellar systems can be investigated with a 34 m starshade, at least in the approximation where the integration time increase prohibitively when the IWA is reached.

The number of accessible planets results (Table 6 and Figure 5). For $\eta_{\text {Earth }}=10 \%, R_{\mathrm{pl}}=1.50$, this number is slightly larger than for the in-built coronagraph, 2.0 instead of 1.5 .
This would decrease to 0.8 planets if an independent detection is not performed beforehand, due to the low completeness of the detection by the starshade (about $40 \%$, Seager et al. 2014).
Turnbull et al. (2012) presented a preliminary discussion of starshades within a broader range of parameters (mirror diameter, shade diameter...), including a 4 m mirror and a 50 m shade, which could detect at least one Earth-like planet, possibly three, in the HZ of its star, if $\eta_{\text {Earth }}$ is larger than $10 \%$.

## 6. NULLING INTERFEROMETERS

### 6.1. Double-star Problem

Nulling interferometers inject the stellar light from their collecting mirrors into a SMF centered on the target star. The impact of a stellar companion depends on how much of its light is also injected in the fiber. A possible requirement is that this light is less than the target leaks, $10^{-5}$ times the target flux. Guyon (2002) gives the efficiency of the coupling of a source, $E_{\text {coupl }}$, as a function of its angular distance to the SMF axis. For an interferometer with $\Phi=0.75 \mathrm{~m}$ mirrors, at the most demanding wavelength $\lambda=18 \mu \mathrm{~m}$, and with $\Delta m_{18}$ the difference between the companion and target magnitudes at $18 \mu \mathrm{~m}$, the condition on the ratio, $r$, of light from the companion to that from the target into the SMF is $r=10^{-0.4 \Delta m_{18}} \times E_{\text {coupl }}\left(\theta_{\text {comp }}\right)<10^{-5}$. The upper envelope of the $E_{\text {coupl }}\left(\theta_{\text {comp }}\right)$ curve by Guyon (2002, Figure 1) can be fit by a second-degree polynomial, and the condition on the angular distance of the companion reads

$$
\begin{equation*}
\theta_{\text {comp }}>20-0.96 \times \Delta m_{18}-0.055 \times \Delta m_{18}^{2} \quad[\operatorname{arcsec}] . \tag{11}
\end{equation*}
$$

Table 5
Possible Target List for a Starshade

| Hipparcos | Common Name | $D(\mathrm{pc})$ | V | $L_{\text {bol }}$ | Spec. Type | Sep. 1.3 AU (mas) | Star \# |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 17378 | GL 150 | 9.04 | 3.52 | 3.37 | K0IV | 272 | 1 |
| 86974 | GL 695 | 8.31 | 3.41 | 2.78 | G5IV | 269 | 2 |
| 8102 | ¢ Ceti | 3.65 | 3.49 | 0.52 | G8.5V | 264 | 3 |
| 3821 | $\eta$ Cas A | 5.94 | 3.45 | 1.31 | G3V | 258 | 4 |
| 99240 | $\delta \mathrm{Pav}$ | 6.11 | 3.53 | 1.33 | G8.0IV | 253 | 5 |
| 27072 | GL 216A | 8.93 | 3.59 | 2.51 | F7V | 238 | 6 |
| 14632 | GL 124 | 10.54 | 4.05 | 2.36 | G0V | 195 | 7 |
| 12777 | GL 107A | 11.13 | 4.10 | 2.42 | F7V | 187 | 8 |
| 15510 | 82 Eri | 6.04 | 4.26 | 0.69 | G8.0V | 184 | 9 |
| 1599 | GL 17 | 8.59 | 4.23 | 1.33 | G0V | 180 | 10 |
| 105858 | GL827 | 9.26 | 4.22 | 1.54 | F7V | 180 | 11 |
| 61317 | $\beta \mathrm{CVn}$ | 8.44 | 4.24 | 1.27 | G0V | 179 | 12 |
| 64394 | GL 502 | 9.13 | 4.24 | 1.48 | G0V | 178 | 13 |
| 19849 | o 2 Eri | 4.98 | 4.43 | 0.42 | K0.5V | 175 | 14 |
| 77257 | GL 598 | 12.12 | 4.41 | 2.22 | G0Vvar | 165 | 15 |
| 96100 | $\sigma$ Dra | 5.75 | 4.67 | 0.44 | G9.0V | 154 | 16 |
| 64924 | 61 Vir | 8.56 | 4.74 | 0.87 | G5V | 147 | 17 |
| 23693 | GL 189 | 11.65 | 4.71 | 1.54 | F6/7V | 143 | 18 |
| 57443 | GL 442A | 9.22 | 4.89 | 0.86 | G3/5V | 135 | 19 |
| 29271 | GL 231 | 10.20 | 5.08 | 0.91 | G6V | 125 | 20 |

Table 6
Number of Planets Accessible for a 34 m Star Shade and a 2.4 m Telescope

| $\eta_{\text {Earth }}(\%)$ | $R_{\mathrm{pl}}=1.0$ | $R_{\mathrm{pl}}=1.5$ | $R_{\mathrm{pl}}=2.0$ |
| :--- | :---: | :---: | :---: |
| 1 | 0.21 | 0.21 | 0.21 |
| 3 | 0.63 | 0.63 | 0.63 |
| 10 | 2.10 | 2.10 | 2.10 |
| 30 | 6.30 | 6.30 | 6.30 |
| 100 | 21.00 | 21.00 | 21.00 |

Only binary stars with a companion fulfilling that requirement are kept in the target list, with the exception of the $\alpha$ Cen system for which an adequate integration time should allow that limit to be pushed down.

It should be noted that the case of our nearest neighbors, the triple system $\alpha$ Cen A, B, and Proxima Cen, is special. These stars are at 1.3 pc , significantly nearer than what a uniform density of stars would give (if the stellar density were uniform, the first solar-type star, ${ }^{10}$ would be at 2.6 pc ). As a consequence, this triple system is at the very top of all target lists: astrometry, coronagraphs, and nulling interferometers. Two questions remain: (i) Will all these instruments be able to separate the A and B components? (ii) Do these stars have habitable planet(s)?

### 6.2. Orbital and Orientation Problems

For interferometers in the thermal IR, the question of the orbital inclination can also impact the observations, although less severely than for coronagraphs thanks to the higher angular resolution. For inclined orbits the planet must be outside the instrument IWA ( $\sim \lambda / B$, e.g., 20 mas assuming a typical (long) baseline $B \sim 100 \mathrm{~m}$ at a wavelength of $10 \mu \mathrm{~m})$. Thanks to formation flying, the interferometer baselines can be chosen in a broad interval, at least when $\theta_{\mathrm{HZ}} \gg 20$ mas (see next section), so that the planet is seen at an angle significantly larger than the IWA during most of the time, e.g., $67 \%$ of the time for

[^3]

Figure 5. Number of planets located in the HZ that can be studied in spectroscopy $(\lambda \Delta \lambda=70)$, with a 34 m starshade and a 2.4 m telescope, as a function of $\eta_{\text {Earth }}$, assuming that the exozodiacal light of the target stars is low enough not to prevent the detection of telluric exoplanets in the HZ (see Section 4.5). The limitation of that number is driven by the inner working angle (IWA) of the shade, and independent of the planetary radius. However, the larger the planet is, the larger the $\mathrm{S} / \mathrm{N}$. The planet is assumed to be at full elongation and located at $1.30 L^{1 / 2} \mathrm{AU}$ from its star. Data points follow a power law with an exponent $\beta_{\text {shade }}=1.0$. A prior detection of stars with suitable planet(s) is assumed, e.g., by astrometry. If detection is done by the starshade itself, all numbers must be divided by 2.5 , due to the low completeness of the detection by the starshade (about 40\%, Seager et al. 2014).
$\theta_{\mathrm{HZ}}=2 \times$ IWA. In the case of a prior detection and identification of the relevant stellar systems, e.g., by an astrometric mission, the ephemerides will be known, allowing the selection of spectroscopic observations at dates when the systems are close to full elongation.

Many nearby stars overfulfil the requirement $\theta_{\mathrm{HZ}}>20$ mas, so a detection by the spectroscopic mission itself could be possible, by observing the targets three to four times to avoid unfavorable configurations. However, this would not be not optimal because we would ignore the mass of the planets (see Section 9).
The impact of the inclination of a planet's orbit and the phase curve of the mid-IR signal with time of the planet is not large when it has an atmosphere. It is mainly that from a uniformly warm disc because, when not vanishing, the atmosphere redistributes the heat from the dayside to the nightside, and the thermal IR emission is similar when either side is observed. In a quantitative study of the Earth's mid-IR spectrum as seen from distance, Gómez-Leal et al. (2012) found that spectra change by few per cent with the rotation of our planet, mainly due to the type of landscape seen at a given time, e.g., continents/oceans, rather than the alternation of day and night. The IR emission comes from the upper parts of the atmosphere (the mid and lower parts are mostly opaque), whereas the day-night cycle mainly affects the boundary layer between atmosphere and ground (first few kilometers; same reference).

As for coronagraphs, a prior detection and orbital characterization of planets in the HZ of the target stars is assumed, and as often as possible observations are performed close to the full elongation of the planet to allow a good angular separation of the planet from other sources.

### 6.3. Angular Resolution of the Star-Planet System

The interferometer can reject the stellar light at the level $10^{-5}$ only if its short baseline, $B_{1}$, is not too large (Defrère et al. 2010); meanwhile, the long base, $B_{2}$, determines the angular resolution for resolving the planetary system. One of the advantages of the formation-flying configuration is to allow an independent choice of these two quantities. To avoid penalizing optical distortions, the maximum size of the long baseline that is compatible with the 1200 m focal length considered in the Darwin project (Defrère et al. 2010) is $B_{2}=400 \mathrm{~m}$. Even in a version cheaper than the 2007 Darwin or TPF-I projects, with 0.75 m mirrors rather than $\geqslant 2 \mathrm{~m}$ ones, the size of the interferometer geometry should be kept similar so as to preserve the resolution power of the instrument. This should be possible in the formation-flying setup of the interferometer. Long baselines require good control of the attitude of the flotilla, therefore accurate metrology, which would have some, but limited, impact on the cost, and a significant one on the performance. Accurate formation flying should be accessible in the near future thanks to the heritage of the PRISMA (Delpech et al. 2013) and PROBA-3 (ESA 2012) missions. Assuming a $4: 1\left(B_{2}: B_{1}\right)$ configuration, which is understood as a minimum requirement to control instability noise (Lay 2006), the maximum baseline $B_{2}$ is 400 m . To be observed, the HZ must be seen by the interferometer as a few resolution elements $\left(\lambda B_{2}\right), 9 \mathrm{mas}$ at $18 \mu \mathrm{~m}$ and 5 mas at $10 \mu \mathrm{~m}$. If the requirement is

$$
\begin{equation*}
\left.\theta_{\mathrm{HZ}}>20 \text { [mas }\right], \tag{12}
\end{equation*}
$$

the minimum number of resolution elements will be $k=$ 4.0 at $10 \mu \mathrm{~m}$ and $k=2.2$ at $18 \mu \mathrm{~m}$, possibly sufficient to separate the planet from the (mostly symmetrical) exozodiacal light.

This requirement is satisfied for most FGK stars with rank $<100$ (Table 9), but it is of special importance for lowluminosity M stars $\left(a_{\mathrm{HZ}}=1.30 L_{i}^{1 / 2} \mathrm{AU}\right.$; Table 8). Only stars respecting this constraint are considered in our target list.

### 6.4. Calibrating the Integration Time (Value of d)

In a way similar to coronagraphs, the constant $d$ of Equation (6) can be determined by fitting the predictions of the model to the values given in Defrère et al. (2010) that are obtained with the DarwinSim software (den Hartog 2005). For 2 m telescopes and $2.0 R_{\text {Earth }}$ planets, Defrère et al. (2010) find that 36 G stars can be studied in spectroscopy $(\lambda / \Delta \lambda=20)$ in 1.5 years (Table 4 therein).

Comparing with the model (Table 7) yields

$$
d=1.5 \text { years } / 4.44 \times 10^{4}=3.4 \times 10^{-5} \text { years }
$$

For the interferometer, the accuracy of the model can also be estimated by applying it to different interferometer designs. Defrère et al. (2010) considered several of them, and the associated numbers of accessible stars can be compared with the model predictions. For planets with radius 1.0, 1.5, and $2.0 R_{\text {Earth }}$ around M stars, during 0.3 yr and $\eta_{\text {Earth }}=100 \%$, Defrère et al. (2010) find 24,44 , and 69 planets, respectively. With the same conditions and $d$ fixed to $3.4 \times 10^{-5} \mathrm{yr}$, the model finds 24,47 , and 70 planets, respectively. As in the case of coronagraphs, the similarity between the two series indicates a fair robustness of the model.

### 6.5. Distinguishing a Planet from Exozodiacal Dust

For the interferometer, the presence of exozodiacal dust around a star can also hamper the direct detection and characterization of telluric planets in the thermal IR. However, nulling interferometers are less affected by exozodiacal dust than coronagraphs for two reasons: (1) their internal modulation eliminates the signal from centrally symmetric sources, leaving only their quantum noise (Mennesson et al. 2005; Defrère et al. 2010); and (2) their angular resolution is determined by their baselines, not by the diameters of the light collectors (individual mirrors), and can be high.

In an affordable version of a formation-flying nulling interferometer (Section 6.6), the mirrors must be reduced, e.g., to $\sim 0.75 \mathrm{~m}$, whereas the baselines can remain large, e.g., 400 m (Section 6.3). This provides many resolution elements in the FOV, which is about the size of the HZ, e.g., $(12)^{2}=144$ in the case considered by Defrére et al. (2012, Figure 4 therein), who concluded that "unlike the coronagraph, there is no significant detection $($ SNR $>3)$ of false positives beyond 20 zodis."

For parity with coronagraphs, we will ignore the problem of exozodiacal dust, keeping in mind that it is significantly less severe than for coronagraphs, the two instruments in an affordable version.

### 6.6. Performances of an Affordable Nulling Interferometer

What could be an affordable interferometer? By rough analogy with the 2.4 m class coronagraph and starshade that are currently being studied by NASA, a $4 \times 0.75 \mathrm{~m}$ interferometer is considered as affordable. It is notable that this does not include the technological effort needed before building the

Table 7
Integration Times Divided by $d$ for G Stars ${ }^{\text {a }}$

| Hipparcos | Common Name | Double Star (arcsec) | $D(\mathrm{pc})$ | $\theta_{\mathrm{HZ}}$ (mas) | V | $L_{\text {bol }}\left(L_{\text {Sun }}\right)$ | Spec. Type | $t_{i} / d$ | Star \# | S_( $\left.t_{i} / d\right)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 71683 | $\alpha$ Cen A | $10^{\text {b }}$ | 1.29 | 984 | -0.01 | 1.61 | G2.0V | $1.43 \mathrm{E}+00$ | 1 | $1.43 \mathrm{E}+00$ |
| 8102 | $\tau$ Ceti | 137 | 3.65 | 197 | 3.49 | 0.52 | G8.5V | $2.31 \mathrm{E}+01$ | 2 | $2.45 \mathrm{E}+01$ |
| 96100 | $\sigma$ Draco | ... | 5.75 | 115 | 4.67 | 0.44 | G9.0V | $1.08 \mathrm{E}+02$ | 3 | $1.33 \mathrm{E}+02$ |
| (...) | ... | $\ldots$ | ... | ... | ... | ... | ... | ... | (...) | ... |
| 67927 | $\ldots$ | $\ldots$ | 11.4 | 272 | 2.68 | 9.6 | G0IV | $2.70 \mathrm{E}+03$ | 35 | 4.17E+04 |
| 22263 | $\ldots$ | $\ldots$ | 13.28 | 76 | 5.49 | 1.01 | G3V | $2.72 \mathrm{E}+03$ | 36 | $4.44 \mathrm{E}+04$ |
| 79537 | $\ldots$ | $\ldots$ | 13.89 | 33 | 7.53 | 0.21 | G8/K0V | $2.98 \mathrm{E}+03$ | 37 | $4.73 \mathrm{E}+04$ |
| (...) | $\ldots$ | $\ldots$ | ... | $\cdots$ | ... | ... | ... | ... | (...) | ... |

Notes. The star \# in bold (36) corresponds to the number of G stars that can be studied with the instrument described by Defrére et al. (2010) with condition (a) in 1.5 years.
${ }^{\text {a }}$ Conditions are $\Phi=2 \mathrm{~m}, R_{\mathrm{pl}}=2.0, \lambda / \Delta \lambda=20$.
${ }^{\mathrm{b}}$ In year 2030.
(This table is available in its entirety in machine-readable form.)
instrument to raise it to the required Technical Readiness Level (TRL).

As discussed in Section 6.3, there is a major advantage in keeping the possibility of long baselines even for nearby targets where short baselines are expected to be sufficient: if an interesting system is found, it will be possible to qualify/falsify it by using a higher spatial resolution, to better separate the planetary signal from that of the exozodiacal cloud.

The IR luminosity of a planet with given radius and albedo, located in the HZ of its star, is an intrinsic property of the planet, independent of the parent star's features. It is that of a $\sim 300 \mathrm{~K}$ body, with a given size. As the thermal IR luminosity of an M2 star is $\sim 5$ times lower than that of a G2 star (Section 3.3), the planet/star contrast is more favorable for M than for G stars. In addition, M stars are more numerous than FGK stars, per unit volume, so that if all stars were considered on the criterion of integration time alone (Equations (6) and (7)), M stars would fully dominate the target list.

Planets in the HZ of M stars are expected to have their spin and orbital rotations phase-locked (Ulmschneider 2006), a situation very different from that of Earth regarding their habitability. They would have one hemisphere continuously irradiated and the other continuously in the dark, which may be considered as worse or better for harboring life, but certainly different. The surface of a planet around an $M$ star should present an environment very different from that of our planet. Therefore, it seems desirable to balance M and solar types in the target list in order to study the diversity of different situations. ${ }^{11}$ The two groups are considered separately, and it is proposed to spend the appropriate time on each of them to balance the numbers of stars in the two groups. Spending four years on FGK stars and one year on $M$ stars leads approximately to that result (Tables 8 and 9).

Table 8 illustrates the case of planets of M stars for an observation time of one year, $R_{\mathrm{pl}}=1.5$, the condition $\theta_{\text {comp }}>$ $18.5-\Delta m_{18}$ [arcsec] but for Prox Cen and $\theta_{\mathrm{HZ}}>20$ [mas]. The impact of $\eta_{\text {Earth }}$ is calculated as in Section 4.6 and shown for

[^4]$\eta_{\text {Earth }}=100 \%$ and $10 \%$, leading to 14 and 3.6 planets, respectively.

The same procedure is shown in Table 9 for FGK stars, and an observation time of four years, $R_{\mathrm{pl}}=1.5$. For $\eta_{\text {Earth }}=100 \%$ and $10 \%$, one gets $N_{\mathrm{pl}}=14$ and 3.3, respectively.

### 6.6.1. Assuming that $\eta_{\text {Earth }}$ is Common for M Stars and FGK Stars

Table 10 and Figure 6 give the number of planets that can be studied, as a function of a common $\eta_{\text {Earth }}$ for FGK and M stars, for various planetary radii. The dependence of $N_{\mathrm{pl}}$ on $\eta_{\text {Earth }}$ can also be fitted by a power law with an exponent $\beta_{\text {interf }}=0.62$, indicating a somewhat slower dependence than for the coronagraph $\left(\beta_{\text {coron }}=0.71\right)$.

### 6.6.2. Assuming that $\eta_{\text {Earth }}$ is $50 \%$ for $M$ Stars, but Unknown for FGK Stars

In the present state of Kepler data analysis, $\eta_{\text {Earth }}$ is better constrained for M stars than for FGK stars because the orbital period of planets in the HZ around the former is a few weeks rather than few months. The present Kepler catalog is considered as sufficient for addressing their statistics (Batalha 2014). Gaidos (2013) found $\eta_{\mathrm{M}} \sim 50 \%$. This is in agreement with an estimate by the radial velocity technique, $\eta_{\mathrm{M}}=0.41_{-0.13}^{+0.54}$ (Bonfils et al. 2013). An alternative to the procedure of Section 6.6.1 is to fix $\eta_{\mathrm{M}}=50 \%$ for M stars and leave $\eta_{\text {solar }}$ variable for FGK stars.

The corresponding number of planets is shown in Table 11 and Figure 7. As expected, the total number of planets is significantly larger for low values of $\eta_{\text {solar }}$ than in Section 6.6.1. For instance, 13 planets can be studied for $\eta_{\text {solar }}=10 \%$ and $R_{\mathrm{pl}}=1.5$, instead of 7.1 for $\eta_{\mathrm{M}}=\eta_{\text {solar }}=10 \%$.

### 6.7. Detections by the Interferometer

In a way similar to the case of coronagraphs, one can estimate how many stars could be investigated by the spectroscopic mission itself to search for planets, being aware of the associated disadvantages, in particular the absence of knowledge of the planetary masses (Section 9). Assuming that this could be done with three visits to avoid phase problems, and a spectral resolution $\lambda \Delta \lambda=2$, the proportionality of the required observation time to $\Delta \lambda$ (Equation (6)) and the need for three visits give the observing time from Tables 8 and 9 .

Table 8
M Stars for One-year Observations with a $\Phi=4 \times 0.75 \mathrm{~m}$ Interferometer, $R_{\mathrm{pl}}=1.5 R_{\text {Earth }}{ }^{\mathrm{a}}$

| Hipparcos | Common Name | $\begin{gathered} \mathrm{D} \\ (\mathrm{pc}) \end{gathered}$ | V | $\begin{gathered} L_{\mathrm{bol}} \\ \left(L_{\mathrm{Sun}}\right) \end{gathered}$ | $\begin{gathered} \theta_{\mathrm{HZ}} \\ (\mathrm{mas}) \end{gathered}$ | Spec. Type | $\begin{aligned} & T_{\text {eff }} \\ & (\mathrm{K}) \end{aligned}$ | $\begin{gathered} t_{i} \\ (\mathrm{yr}) \end{gathered}$ | $i$ | $\begin{gathered} \mathrm{S}\left(t_{i}\right) \\ (\mathrm{yr}) \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 70890 | Prox Cen | 1.30 | 11.01 | $8.56 \mathrm{e}-04$ | 29.3 | M5.0V | 2425 | $1.25 \mathrm{E}-03$ | 1 | $1.25 \mathrm{E}-03$ |
| 87937 | Barnard's Star | 1.83 | 9.51 | $3.69 \mathrm{E}-03$ | 43.2 | M3.5V | 2578 | $4.92 \mathrm{E}-03$ | 2 | $6.17 \mathrm{E}-03$ |
| 54035 | Lalande 21185 | 2.54 | 7.49 | $2.46 \mathrm{E}-02$ | 80.3 | M2.0V | 3136 | $1.85 \mathrm{E}-02$ | 3 | $2.47 \mathrm{E}-02$ |
| 92403 | Ross 154 | 2.97 | 10.50 | $4.44 \mathrm{E}-03$ | 29.2 | M3.5V | 2614 | $3.41 \mathrm{E}-02$ | 4 | $5.88 \mathrm{E}-02$ |
| 114046 | Lacaille 9352 | 3.28 | 7.35 | $4.15 \mathrm{E}-02$ | 80.7 | M1.0V | 3361 | $5.13 \mathrm{E}-02$ | 5 | $1.10 \mathrm{E}-01$ |
| 57548 | Ross 128 | 3.35 | 11.10 | $4.39 \mathrm{E}-03$ | 25.7 | M 4.0 V | 2612 | $5.51 \mathrm{E}-02$ | 6 | $1.65 \mathrm{E}-01$ |
| 91772 | ... | 3.52 | 9.70 | $9.02 \mathrm{E}-03$ | 35.1 | M3.5V | 2790 | $6.73 \mathrm{E}-02$ | 7 | $2.32 \mathrm{E}-01$ |
| 91768 | $\ldots$ | 3.52 | 8.94 | $1.26 \mathrm{E}-02$ | 41.5 | M3.0V | 2892 | $6.74 \mathrm{E}-02$ | 8 | $3.00 \mathrm{E}-01$ |
| 1475 | GX Andromedae | 3.57 | 8.13 | $2.38 \mathrm{E}-02$ | 56.2 | M1.5V | 3122 | $7.15 \mathrm{E}-02$ | 9 | $3.71 \mathrm{E}-01$ |
| 36208 | Luyten's Star | 3.76 | 9.87 | $1.14 \mathrm{E}-02$ | 36.9 | M3.5V | 2860 | $8.76 \mathrm{E}-02$ | 10 | $4.59 \mathrm{E}-01$ |
| 24186 | Kapteyn's Star | 3.91 | 8.85 | $1.20 \mathrm{E}-02$ | 36.4 | M 2.0 V | 2876 | $1.02 \mathrm{E}-01$ | 11 | $5.61 \mathrm{E}-01$ |
| 110893 | Kruger 60 A | 4.03 | 9.59 | $1.42 \mathrm{E}-02$ | 38.4 | M3.0V | 2931 | $1.16 \mathrm{E}-01$ | 12 | $6.77 \mathrm{E}-01$ |
| 30920 | Ross 614 A | 4.09 | 11.07 | $7.61 \mathrm{E}-03$ | 27.7 | M 4.5 V | 2742 | $1.23 \mathrm{E}-01$ | 13 | $8.00 \mathrm{E}-01$ |
| 80824 | Wolf 1061 | 4.27 | 10.08 | $1.20 \mathrm{E}-02$ | 33.4 | M3.5V | 2877 | $1.46 \mathrm{E}-01$ | 14 | $9.46 \mathrm{E}-01$ |
| 439 | ... | 4.34 | 8.56 | $2.28 \mathrm{E}-02$ | 45.3 | M1.5V | 3106 | $1.56 \mathrm{E}-01$ | 15 | $1.10 \mathrm{E}+00$ |
| 85523 | $\ldots$ | 4.54 | 9.41 | $1.70 \mathrm{E}-02$ | 37.4 | M 2.5 V | 2996 | $1.86 \mathrm{E}-01$ | 16 | $1.29 \mathrm{E}+00$ |
| 86162 | ... | 4.54 | 9.15 | $2.24 \mathrm{E}-02$ | 42.8 | M3.0V | 3098 | $1.86 \mathrm{E}-01$ | 17 | $1.47 \mathrm{E}+00$ |
| 113020 | Ross 780 | 4.66 | 10.18 | $1.53 \mathrm{E}-02$ | 34.5 | M 2.5 V | 2957 | $2.07 \mathrm{E}-01$ | 18 | $1.68 \mathrm{E}+00$ |
| 54211 | ... | 4.86 | 8.82 | $2.28 \mathrm{E}-02$ | 40.4 | M1.0V | 3105 | $2.45 \mathrm{E}-01$ | 19 | $1.93 \mathrm{E}+00$ |
| 106440 | $\ldots$ | 4.95 | 8.67 | $3.04 \mathrm{E}-02$ | 45.8 | M1.5V | 3223 | $2.64 \mathrm{E}-01$ | 20 | $2.19 \mathrm{E}+00$ |
| 86214 | ... | 5.05 | 10.94 | $1.04 \mathrm{E}-02$ | 26.2 | M4.0 | 2831 | $2.85 \mathrm{E}-01$ | 21 | $2.47 \mathrm{E}+00$ |
| 112460 | EV Lacertae | 5.05 | 10.33 | $1.37 \mathrm{E}-02$ | 30.1 | M3.5V | 2920 | $2.85 \mathrm{E}-01$ | 22 | $2.76 \mathrm{E}+00$ |
| 57544 | ... | 5.34 | 10.80 | $8.40 \mathrm{E}-03$ | 22.3 | M3.5V | 2769 | $3.56 \mathrm{E}-01$ | 23 | $3.12 \mathrm{E}+00$ |
| 67155 | Wolf 498 | 5.41 | 8.43 | $3.92 \mathrm{E}-02$ | 47.6 | M1.0V | 3335 | $3.76 \mathrm{E}-01$ | 24 | $3.49 \mathrm{E}+00$ |
| 21088 | Stein 2051 | 5.54 | 10.82 | $1.12 \mathrm{E}-02$ | 24.9 | M4.0V | 2856 | $4.12 \mathrm{E}-01$ | 25 | $3.90 \mathrm{E}+00$ |
| 33226 | ... | 5.61 | 9.89 | $1.75 \mathrm{E}-02$ | 30.7 | M3.0V | 3006 | $4.34 \mathrm{E}-01$ | 26 | $4.34 \mathrm{E}+00$ |
| 25878 | Wolf 1453 | 5.68 | 7.97 | $6.69 \mathrm{E}-02$ | 59.2 | M1.0V | 3594 | $4.58 \mathrm{E}-01$ | 27 | $4.80 \mathrm{E}+00$ |
| 103039 | ... | 5.71 | 11.46 | 7.68E-03 | 20.0 | M3.5V | 2745 | $4.65 \mathrm{E}-01$ | 28 | $5.26 \mathrm{E}+00$ |
| 29295 | $\ldots$ | 5.75 | 8.15 | $5.74 \mathrm{E}-02$ | 54.2 | M1.5V | 3517 | $4.81 \mathrm{E}-01$ | 29 | $5.74 \mathrm{E}+00$ |
| 86990 | ... | 5.84 | 10.78 | $9.54 \mathrm{E}-03$ | 21.7 | M3.0V | 2806 | $5.09 \mathrm{E}-01$ | 30 | $6.25 \mathrm{E}+00$ |
| 94761 | Wolf 1055 | 5.85 | 9.12 | $3.37 \mathrm{E}-02$ | 40.8 | M 2.5 V | 3267 | $5.14 \mathrm{E}-01$ | 31 | $6.76 \mathrm{E}+00$ |
| 73182 | ... | 5.86 | 8.07 | $1.28 \mathrm{E}-01$ | 79.4 | M1.5V | 3952 | $5.22 \mathrm{E}-01$ | 32 | $7.29 \mathrm{E}+00$ |
| 76074 | $\ldots$ | 5.93 | 9.31 | $3.16 \mathrm{E}-02$ | 39.0 | M 2.5 V | 3239 | $5.42 \mathrm{E}-01$ | 33 | $7.83 \mathrm{E}+00$ |
| 117473 | ... | 5.95 | 8.98 | $2.72 \mathrm{E}-02$ | 36.0 | M1.0V | 3176 | $5.49 \mathrm{E}-01$ | 34 | $8.38 \mathrm{E}+00$ |
| 37766 | Ross 882 | 5.98 | 11.23 | $1.34 \mathrm{E}-02$ | 25.2 | M 4.0 V | 2913 | $5.60 \mathrm{E}-01$ | 35 | $8.94 \mathrm{E}+00$ |
| 45343 | ... | 6.11 | 7.64 | $8.20 \mathrm{E}-02$ | 60.9 | M0.0V | 3701 | $6.14 \mathrm{E}-01$ | 36 | $9.55 \mathrm{E}+00$ |
| 34603 | QY Aurigae A | 6.12 | 11.67 | $1.21 \mathrm{E}-02$ | 23.4 | M 4.5 V | 2880 | $6.14 \mathrm{E}-01$ | 37 | $1.02 \mathrm{E}+01$ |
| 99701 | $\cdots$ | 6.20 | 7.97 | $6.72 \mathrm{E}-02$ | 54.3 | M0.0V | 3596 | $6.50 \mathrm{E}-01$ | 38 | $1.08 \mathrm{E}+01$ |
| 71253 | HN Librae | 6.22 | 11.32 | $1.16 \mathrm{E}-02$ | 22.5 | M4.0V | 2866 | $6.55 \mathrm{E}-01$ | 39 | $1.15 \mathrm{E}+01$ |
| 74995 | Wolf 562 | 6.34 | 10.57 | $1.32 \mathrm{E}-02$ | 23.6 | M3.0V | 2908 | $7.07 \mathrm{E}-01$ | 40 | $1.22 \mathrm{E}+01$ |

Note.
${ }^{\text {a }}$ A list up to rank 180 is available in machine-readable form.
(This table is available in its entirety in machine-readable form.)

If 0.5 year is dedicated to planet detection around $M$ stars, the $4 \times 0.75 \mathrm{~m}$ interferometer could search for $1.5 R_{\text {Earth }}$ planets, up to the star ranked 19 (Hip54211, $D=4.86 \mathrm{pc}$ ), but for $\eta_{\mathrm{M}}=50 \%$, only 5.5 planets could be studied in spectroscopy during the remaining 0.5 year, instead of 7.5 if planets are identified beforehand.

If 2.0 years are dedicated to the search for planets around FGK stars, 17 stars could be surveyed (up to Hip12114, $D=7.18 \mathrm{pc})$, but for $\eta_{\text {solar }}=10 \%$ and $R_{\mathrm{pl}}=1.5 R_{\text {Earth }}$, only 2.5 planets could be studied during the 2.0 years left for spectroscopy, instead of 3.3 if planets are identified beforehand.

Around all targets, M and FGK stars, eight telluric planets could be studied in spectroscopy without prior detection, but it would be at the cost of ignoring their mass and therefore their physical nature.

## 7. MISSION REQUIREMENTS FOR A GIVEN NUMBER OF PLANETS TO BE STUDIED

Another interesting use of the model is the search for the requirements on an instrument with a given objective in terms of number of planets that can be studied. Only the case of $\eta_{\text {solar }}=10 \%, \eta_{\mathrm{M}}=50 \%$, will be considered, with two instruments: a built-in coronagraph and an interferometer.

The procedure is as follows. Equation (5), or (6), gives the integration time per target. New tables are built, analogous to Tables 3, 8, and 9, but for various parameters including the mirror diameter. For a given goal of $N_{\mathrm{p} 1}$ planets, the requirements for cases with $\eta_{\text {solar }} \neq 1$ and planets identified beforehand are obtained by studying $N_{\mathrm{pl}} \times 1 / \eta_{\text {Earth }}$ stars, during virtual sequences of observation $1 / \eta_{\text {Earth }}$ longer than the allocated time for that sequence (Section 4.6). The case of one year spent on M stars and four years on FGK

Table 9
FGK Stars for Four-year Observations with a $\Phi=4 \times 0.75 \mathrm{~m}$ Interferometer, $R_{\mathrm{pl}}=1.5 R_{\text {Earth }}{ }^{\text {a }}$

| Hipparcos | Common Name | Double Star (arcsec) | $\begin{gathered} d \\ (\mathrm{pc}) \end{gathered}$ | $\begin{gathered} \theta_{\mathrm{HZ}} \\ (\mathrm{mas}) \end{gathered}$ | V | $\begin{gathered} L_{\mathrm{bol}} \\ \left(L_{\mathrm{Sun}}\right) \end{gathered}$ | Spec. Type | Star \# | $\begin{gathered} t_{i} \\ (\mathrm{yr}) \end{gathered}$ | $\begin{gathered} S\left(t_{i}\right) \\ (\mathrm{yr}) \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 71681 | $\alpha$ Cen B | 10 (2030) | 1.29 | 562 | 1.35 | 0.52 | K0V | 1 | $2.11 \mathrm{E}-03$ | $2.11 \mathrm{E}-03$ |
| 71683 | $\alpha$ Cen A | 10 (2030) | 1.29 | 984 | -0.01 | 1.61 | G2.0V | 2 | $3.21 \mathrm{E}-03$ | $5.32 \mathrm{E}-03$ |
| 104217 | 61 Cyg B | 31.6 | 3.5 | 89 | 5.95 | 0.1 | K7.0V | 3 | $6.72 \mathrm{E}-02$ | $7.25 \mathrm{E}-02$ |
| 104214 | 61 Cyg A | 31.6 | 3.5 | 105 | 5.2 | 0.13 | K5.0V | 4 | $6.77 \mathrm{E}-02$ | $1.40 \mathrm{E}-01$ |
| 108870 | $\epsilon$ Indi A | 400 | 3.62 | 131 | 4.69 | 0.23 | K4V | 5 | $7.96 \mathrm{E}-02$ | $2.20 \mathrm{E}-01$ |
| 8102 | $\tau$ Ceti | 137 | 3.65 | 197 | 3.49 | 0.52 | G8.5V | 6 | $8.69 \mathrm{E}-02$ | $3.07 \mathrm{E}-01$ |
| 105090 | AX Micro | ... | 3.95 | 71 | 6.69 | 0.08 | K9.0V | 7 | $1.08 \mathrm{E}-01$ | $4.15 \mathrm{E}-01$ |
| 49908 | ... | $\ldots$ | 4.87 | 67 | 6.6 | 0.11 | K7.0V | 8 | $2.49 \mathrm{E}-01$ | $6.64 \mathrm{E}-01$ |
| 19849 | o 2 Eri | $\ldots$ | 4.98 | 131 | 4.43 | 0.42 | K0.5V | 9 | $2.85 \mathrm{E}-01$ | $9.49 \mathrm{E}-01$ |
| 96100 | $\sigma$ Dra | ... | 5.75 | 115 | 4.67 | 0.44 | G9.0V | 10 | $5.00 \mathrm{E}-01$ | $1.45 \mathrm{E}+00$ |
| 73184 | ... | 25.6 | 5.86 | 92 | 5.72 | 0.29 | K4.0V | 11 | $5.31 \mathrm{E}-01$ | $1.98 \mathrm{E}+00$ |
| 99461 | $\ldots$ | ... | 6.01 | 88 | 5.32 | 0.28 | K2.5V | 12 | $5.88 \mathrm{E}-01$ | $2.57 \mathrm{E}+00$ |
| 120005 | $\ldots$ | $\ldots$ | 6.11 | 46 | 7.7 | 0.08 | K7.0V | 13 | $6.14 \mathrm{E}-01$ | $3.18 \mathrm{E}+00$ |
| 15510 | 82 Eri | $\ldots$ | 6.04 | 138 | 4.26 | 0.69 | G8.0V | 14 | $6.18 \mathrm{E}-01$ | $3.80 \mathrm{E}+00$ |
| 99240 | $\delta \mathrm{Pav}$ | $\ldots$ | 6.11 | 189 | 3.53 | 1.33 | G8.0IV | 15 | $6.75 \mathrm{E}-01$ | $4.47 \mathrm{E}+00$ |
| 114622 | ... | $\ldots$ | 6.54 | 84 | 5.57 | 0.31 | K3.0V | 16 | 8.21E-01 | $5.30 \mathrm{E}+00$ |
| 12114 | $\ldots$ | $\ldots$ | 7.18 | 75 | 5.82 | 0.29 | K3V | 17 | $1.19 \mathrm{E}+00$ | $6.49 \mathrm{E}+00$ |
| 3765 | $\ldots$ | $\ldots$ | 7.45 | 73 | 5.74 | 0.3 | K1V | 18 | $1.38 \mathrm{E}+00$ | $7.87 \mathrm{E}+00$ |
| 7981 | $\ldots$ | ... | 7.53 | 91 | 5.24 | 0.47 | K1V | 19 | $1.45 \mathrm{E}+00$ | $9.32 \mathrm{E}+00$ |
| 5336 | $\ldots$ | $\ldots$ | 7.55 | 90 | 5.17 | 0.46 | G5Vp | 20 | $1.46 \mathrm{E}+00$ | $1.08 \mathrm{E}+01$ |
| 113283 | $\ldots$ | $\cdots$ | 7.61 | 59 | 6.48 | 0.2 | K4VP | 21 | $1.49 \mathrm{E}+00$ | $1.23 \mathrm{E}+01$ |
| 88574 | $\ldots$ | $\ldots$ | 7.76 | 24 | 9.36 | 0.04 | K4/5V | 22 | $1.59 \mathrm{E}+00$ | $1.39 \mathrm{E}+01$ |
| 2021 | $\beta$ Hyd | $\ldots$ | 7.46 | 258 | 2.82 | 3.7 | G1IV | 23 | $1.61 \mathrm{E}+00$ | $1.55 \mathrm{E}+01$ |
| 5496 | ... | $\ldots$ | 8.19 | 25 | 9.82 | 0.04 | K | 24 | $1.98 \mathrm{E}+00$ | $1.74 \mathrm{E}+01$ |
| 113576 | $\ldots$ | ... | 8.22 | 38 | 7.87 | 0.1 | K5/M0V | 25 | $2.01 \mathrm{E}+00$ | $1.95 \mathrm{E}+01$ |
| 22449 | 1 Ori | $\ldots$ | 8.07 | 215 | 3.17 | 3 | F6V | 26 | $2.10 \mathrm{E}+00$ | $2.16 \mathrm{E}+01$ |
| 86974 | $\cdots$ | $\ldots$ | 8.31 | 200 | 3.41 | 2.78 | G5IV | 27 | $2.34 \mathrm{E}+00$ | $2.39 \mathrm{E}+01$ |
| 61317 | $\beta \mathrm{CVn}$ | $\ldots$ | 8.44 | 133 | 4.24 | 1.27 | G0V | 28 | $2.34 \mathrm{E}+00$ | $2.62 \mathrm{E}+01$ |
| 113229 | ... | $\ldots$ | 8.62 | 18 | 10.38 | 0.03 | K | 29 | $2.42 \mathrm{E}+00$ | $2.87 \mathrm{E}+01$ |
| 64924 | $\ldots$ | $\ldots$ | 8.56 | 109 | 4.74 | 0.87 | G5V | 30 | $2.43 \mathrm{E}+00$ | $3.11 \mathrm{E}+01$ |
| 1599 | $\ldots$ | $\ldots$ | 8.59 | 134 | 4.23 | 1.33 | G0V | 31 | $2.51 \mathrm{E}+00$ | $3.36 \mathrm{E}+01$ |
| 32984 | $\ldots$ | $\ldots$ | 8.71 | 56 | 6.58 | 0.24 | K3V | 32 | $2.55 \mathrm{E}+00$ | $3.61 \mathrm{E}+01$ |
| 23311 | $\ldots$ | $\ldots$ | 8.71 | 62 | 6.23 | 0.3 | K4III | 33 | $2.55 \mathrm{E}+00$ | $3.87 \mathrm{E}+01$ |
| 99825 | $\ldots$ | $\ldots$ | 8.91 | 73 | 5.72 | 0.42 | K3V | 34 | $2.81 \mathrm{E}+00$ | $4.15 \mathrm{E}+01$ |
| 47103 | $\ldots$ | $\ldots$ | 9.02 | 14 | 10.91 | 0.02 | K | 35 | $2.91 \mathrm{E}+00$ | $4.44 \mathrm{E}+01$ |
| 57939 | $\ldots$ | $\ldots$ | 9.09 | 53 | 6.42 | 0.23 | G8Vp | 36 | $3.02 \mathrm{E}+00$ | $4.74 \mathrm{E}+01$ |
| 27072 | ... | $\ldots$ | 8.93 | 178 | 3.59 | 2.51 | F7V | 37 | $3.03 \mathrm{E}+00$ | $5.05 \mathrm{E}+01$ |
| 23512 | $\ldots$ | $\ldots$ | 9.21 | 11 | 11.73 | 0.01 | K: | 38 | $3.15 \mathrm{E}+00$ | $5.36 \mathrm{E}+01$ |
| 15457 | $\ldots$ | $\ldots$ | 9.14 | 102 | 4.84 | 0.88 | G5V | 39 | $3.15 \mathrm{E}+00$ | $5.68 \mathrm{E}+01$ |
| 64394 | $\cdots$ | $\cdots$ | 9.13 | 133 | 4.24 | 1.48 | G0V | 40 | $3.20 \mathrm{E}+00$ | $6.00 \mathrm{E}+01$ |

Note.
${ }^{\text {a }}$ A list up to rank 200 is available in machine-readable form.
(This table is available in its entirety in machine-readable form.)

Table 10
Number of Accessible Planets for a Common $\eta_{\text {Earth }}$

| $\eta_{\text {Earth }}(\%)$ | $R_{\mathrm{pl}}=1.0$ | $R_{\mathrm{pl}}=1.5$ | $R_{\mathrm{pl}}=2.0$ |
| :--- | :---: | :---: | :---: |
| 1 | $0.49 / / 0.52$ | $0.96 / / 0.88$ | $1.6 / / 1.2$ |
| 3 | $0.93 / / 0.96$ | $1.83 / / 1.83$ | $2.9 / / 2.7$ |
| 10 | $2.1 / / 2.0$ | $3.3 / / 3.6$ | $6.0 / / 6.0$ |
| 30 | $4.2 / / 3.6$ | $7.5 / / 7.2$ | $11.2 / / 11.1$ |
| 100 | $10 / / 7$ | $14 / / 14$ | $24 / / 24$ |

Note. FGK stars are left of // and M stars are right.
stars is considered, both for the coronagraph and the interferometer. The number of accessible planets is obtained by adjusting $N_{\text {pl }}$ so that the total durations are those allocated.

### 7.1. Coronagraphs

The impact of the mirror diameter on coronagraphs is twofold: (i) the IWA $(2.5 \lambda / \Phi)$ decreases with increasing $\Phi$, which has an important impact on the transmission $\rho(D)$ (Equation (10)), and (ii) the integration time varies according to Equation (5) ( $\left.\propto D^{-2}\right)$. The resulting number of accessible planets in spectroscopy is plotted in Figure 8, as a function of the mirror diameter.

The goal of ten planets (seven around FGK stars and three around M stars) requires a mirror diameter of 5.5 m corresponding to a very expensive mission that is not likely to be affordable in the near future. ${ }^{12}$ A goal of three planets (all around FGK stars) would still require a 3.5 m telescope.

[^5]

Figure 6. Total number of planets located in the HZ of stars that can be studied in spectroscopy $(\lambda \Delta \lambda=20)$, in the thermal IR , with a nulling interferometer having four 0.75 m mirrors, vs. an $\eta_{\text {Earth }}$ parameter that is common to all spectral types. Four years are spent on FGK stars and one year on M stars. As in Figure 4, the case of $R_{\mathrm{pl}}=2.0 R_{\text {Earth }}$ planets is represented with a dashed line to indicate that they are probably not rocky (Rogers 2015, Figure 2 therein). Data points are calculated from the target list, and are well fitted by power laws with an exponent $\beta_{\text {inter }}=0.62$ (lines).

Table 11
Number of Planets for the Case $\eta_{\mathrm{M}}=50 \%$, Varying $\eta_{\text {solar }}$

| $\eta_{\text {solar }}(\%)$ | $R_{\mathrm{pl}}=1.0$ | $R_{\mathrm{pl}}=1.5$ | $R_{\mathrm{pl}}=2.0$ |
| :--- | :--- | :---: | :---: |
| 1 | $0.5 / / 4.5$ | $1.0 / / 10$ | $1.6 / / 15.5$ |
| 3 | $0.9 / / 4.5$ | $1.8 / / 10$ | $2.9 / / 15.5$ |
| 10 | $2.1 / / 4.5$ | $3.3 / / 10$ | $6.0 / / 15.5$ |
| 30 | $4.2 / / 4.5$ | $7.5 / / 10$ | $11.2 / / 15.5$ |
| 100 | $10 / / 4.5$ | $14 / / 10$ | $24 / / 15.5$ |

Note. FGK stars are left of // and M stars are right.

### 7.2. Comparison With Another Published Model

The model can also be applied to the cases of coronagraphs recently considered by Stark et al. (2014), and its results compared with those of these authors. With the same conditions: detection only $\quad(\lambda \Delta \lambda=5), \quad \lambda=0.55 \mu \mathrm{~m}$, IWA $=2.0 \lambda / \Phi, \eta_{\text {solar }}=10 \%$, ignoring the need for several visits to avoid the planetary orbital phase problem, and searching for strict Earth analogs $\left(R_{\mathrm{pl}}=1.0, a=1.0 L^{1 / 2} \mathrm{AU}\right)$ during a five-year mission, the present model (respectively, Stark et al.'s model) finds that a 4 m coronagraph can discover 6.2 (4.0) planets, a 8 m coronagraph 18 (15) planets, and a 15 m coronagraph 48 (50) planets. This reasonable agreement backs up both independent approaches.

### 7.3. Interferometers

For interferometers, the mirror size impacts the quantum noise, but not the angular resolution when using formation flying (Section 6.3). Equation (6) determines the impact of $\Phi$


Figure 7. Same as Figure 6, but assuming $\eta_{\mathrm{M}}=50 \%$ for M stars, and a variable $\eta_{\text {solar }}$ for FGK stars.


Figure 8. Number of planets around FGK and $M$ stars that can be studied in spectroscopy by a coronagraph, as a function of the mirror diameter $\Phi$, for IWA $=2.5 \lambda / \Phi, \lambda=0.8 \mu \mathrm{~m}\left(\mathrm{O}_{2}\right.$ spectral band A), resolution $\lambda \Delta \lambda=70$, $1.5 R_{\text {Earth }}$ radius planets located at $1.3 L^{1 / 2}$ [AU], a five-year mission, $\eta_{\text {solar }}=10 \%, \eta_{\mathrm{M}}=50 \%$, and a prior identification of the suitable stars. M stars appear in the target list for diameter $\geqslant 4 \mathrm{~m}$, and their fraction increases rapidly for larger diameters.
on the detection time in the target list, and Equation (7) gives the number of possible targets. For diameters smaller than 1.5 m , noise is dominated by the first term in the sum of Equation (6) (the SZ emission, Defrère et al. 2010), so that an integration time $\propto \Phi^{-4}$ results. The number of planets that can be investigated in spectroscopy around M stars is calculated


Figure 9. Number of planets that can be studied by an interferometer around FGK and M stars, as a function of the diameter of the four collecting mirrors, for a spectral resolution $\lambda \Delta \lambda=20$ (spectroscopy), 1.5 $R_{\text {Earth }}$ planets located at $1.3 L^{1 / 2}[\mathrm{AU}]$, and a prior identification of the suitable stars. The mission is five years long: one year is spent on M stars with $\eta_{\mathrm{M}}=50 \%$, four years are spent on FGK stars with $\eta_{\text {solar }}=10 \%$.
from Table 8, considering a longer virtual mission (Section 4.6) of $1 \times 2 \times(\Phi / 0.75 \mathrm{~m})^{4}$ yr. For FGK stars Table 9 is used, with time $4 \times 10 \times(\Phi / 0.75 \mathrm{~m})^{4}$ yr. The number of planets is the product of the target rank and $1 / \eta_{\text {Earth }}$. The cases of both M and FGK stars are shown in Figure 9.

The goal of 10 planets ( 7.5 around M stars, 2.5 around FGK) requires 0.63 m mirrors. With 1.0 m mirrors the spectroscopic study of 21 planets, could be done, 5.5 planets around FGK stars and 15.5 around M stars.

## 8. CAPABILITIES OF GROUND-BASED INSTRUMENTS

The advent of extremely large telescopes on the ground in the foreseeable future, e.g., the 39 m E-ELT with first light expected in 2024 (http://www.eso.org/public/teles-instr/e-elt/), and its diffraction-limited resolution in the IR, should also be considered for direct observation of small planets, especially in systems with a reduced star/planet contrast, such as M stars. Quanz et al. (2015) state that "METIS [the mid-IR E-ELT imager and spectrograph] might be the first instrument to image a nearby (super-) Earth-sized planet with an equilibrium temperature near that expected to enable liquid water on a planet surface."

This is hoped for imaging in broad bands, but ground-based, spatially resolved spectroscopy is not expected to be applicable to the search for biosignature(s), as the Earth's atmosphere is fully opaque in most of the relevant spectral bands, such as $\mathrm{CO}_{2}(15 \mu \mathrm{~m})$ for instance. The atmospheric bands of the gas are optically thick and enlarged by collisions with other gaseous species at 1 bar pressure, preventing the detection of extraterrestrial $\mathrm{CO}_{2}$ through the comb of the atmospheric lines.

There is another niche for ground observations, the observation of planetary atmospheres during transits. The contrast is different because (i) the source is much brighter (the
star, not the illuminated planet) but the cross-section is lower (the atmospheric layer, not the planetary disc), (ii) the effective altitude (pressure) for the line widths is higher, 24 km (lower, 65 mbar ) for an Earth-like planet (Ehrenreich et al. 2006), and lines are narrower. However, the present situation is unclear. Based on a lunar eclipse observation, Arnold et al. (2014) concluded that a ground-based detection of the strongest oxygen $\mathrm{O}_{2}$-A band with low-resolution spectroscopy seems possible, in principle, under a perfectly stable sky, with the E-ELT in the visible for an Earth-like planet in front of a G2 star at 10 pc , that of $\mathrm{O}_{3}$ and $\mathrm{H}_{2} \mathrm{O}$ being even more challenging. In a remarkable paper, Snellen et al. (2015) showed that combining high-dispersion spectroscopy with high-contrast imaging on a future telescope could allow the probing of a 300 K super-earth, or even an earth, orbiting the G2V star $\alpha$ Cen A. On the other hand, Rodler \& López-Morales (2014) showed that $\mathrm{O}_{2}$-A detection with an ELT could be feasible only for Earth twins orbiting a close-by ( $D<8 \mathrm{pc}$ ) M-dwarf with a spectral type later than M3.

We conclude that if ground-based ELTs could make the first direct image of an Earth-sister planet, and possibly perform spectroscopy of $\mathrm{O}_{2}$ in the visible for some transiting planets around (probably late M-type) nearby stars, they cannot replace space-based observatories for an exhaustive search of biosignatures by spectroscopy.

## 9. DISCUSSION AND CONCLUSION

Our parametric model estimates the capabilities of instruments able to perform the spectroscopy of habitable planets, which could be affordable in the mid-future, e.g., coronagraphs and starshade in the visible with a $\Phi=2.4 \mathrm{~m}$ mirror, and nulling interferometers in the thermal IR with $4 \times 0.75 \mathrm{~m}$ telescopes. Their goal is searching for biosignatures in the atmosphere of terrestrial planets located in the HZ of nearby stars, and we study the expected mission yield as a function of $\eta_{\text {Earth }}$, and of the radius of planets.
The selected target list is specific to each instrument. Starting from the list of the nearest stars, the fist step is to select the subsample that can be observed with each instrument. For both types of coronagraphs, there is no M star, because the HZ around these stars is seen at too small an angle, around 20 to 60 mas for the nearest $M$ stars (Table 8), whereas the IWA is 170 mas for the built-in coronagraph with $\Phi=2.4 \mathrm{~m}$, IWA $=2.5 \lambda / \Phi$, and $\lambda=0.8 \mu \mathrm{~m}$; or 115 mas for a 34 m starshade. For the interferometer, the target list comprises both M stars and solar-type (FGK) stars due to adjustable baseline length.

Mission yields depend on $\eta_{\text {Earth }}$. For large values, say $\eta_{\text {Earth }}=50 \%$, all three instruments can study a reasonable number of planets, around 5,10 , and 20 , respectively, assuming that the problem of separating the planet from the exozodiacal emission can be solved for each of them. This would justify a dedicated mission in all cases.

For a low value of $\eta_{\text {Earth }}$, coronagraphs and interferometers are not equally equipped. For $\eta_{\text {Earth }}=10 \%$, both built-in and starshade coronagraphs with 2.4 m mirrors can study only a very limited sample, 1.5 and 2.0 planets respectively, for $R_{\mathrm{pl}}=1.50 R_{\text {Earth }}$. This would probably be prohibitive for dedicated missions, but a mission with other astrophysical goals could be worth it.

For the values currently favored by Kepler, $\eta_{M}=50 \%$ for $M$ stars and $\eta_{\text {solar }}=10 \%$ for FGK stars, an interferometer with

Table 12
Mirror Sizes for Different Goals in Planet Number $N_{\mathrm{pl}}$

|  | Coronagraph: <br> Roal <br> $\left(N_{\text {pl }}\right)$ | Required <br> $\Phi_{\text {coro }}(\mathrm{m})$ | Composition $^{\text {a }}$ | Interferometer: <br> Required $\Phi_{\text {inter }}$ <br> $(\times 4)(\mathrm{m})$ |
| :--- | :---: | :---: | :---: | :---: |
| 1 | 2.2 | $(\mathrm{~S}): 1.0$ | 0.13 | Composition $^{\text {a }}$ |

Note. For $R_{\mathrm{pl}}=1.5 R_{\text {Earth }}, \eta_{\mathrm{M}}=50 \%$, and $\eta_{\text {solar }}=10 \%$.
${ }^{\mathrm{a}}(\mathrm{S})=$ solar star, $(\mathrm{M})=\mathrm{M}$ star.

Table 13
Same as Table 12, but for $\eta_{\text {solar }}=20 \%$

| Goal $\left(N_{\mathrm{pl}}\right)$ | Coronagraph: <br> Required <br> $\Phi_{\text {coro }}$ (m) | Composition ${ }^{\text {a }}$ | Interferometer: <br> Required $\Phi_{\text {inter }}$ $(\times 4)(\mathrm{m})$ | Composition ${ }^{\text {a }}$ |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 1.6 | (S): 1.0 | 0.15 | (S): 0.5 |
|  |  | (M): 0 |  | (M): 0.5 |
| 3 | 2.5 | (S): 2.5 | 0.25 | (S): 1.5 |
|  |  | (M): 0 |  | (M): 1.5 |
| 10 | 4.2 | (S): 8 | 0.55 | (S): 4 |
|  |  | (M): 2 |  | (M): 6 |
| 30 | 7.2 | (S): 21 | 1.05 | (S): 13 |
|  |  | (M): 9 |  | (M): 17 |

Note.
${ }^{\mathrm{a}}(\mathrm{S})=$ solar star, $(\mathrm{M})=\mathrm{M}$ star
$4 \times 0.75 \mathrm{~m}$ mirrors could study $\sim 14$ planets. Even with the risks of small number statistics, several objects of very high scientific significance could be studied, which would legitimate a dedicated mission.

The capabilities of both types of instrument are summarized in Table 12 for these values of $\eta_{\text {Earth }}$, and in, Table 13, for $\eta_{\mathrm{M}}=50 \%$ and $\eta_{\text {solar }}=20 \%$.

However, the maturity of the technology required for the different missions is not the same. Thanks to large efforts, built-in coronography is closer to maturity. Relevant contrasts have been obtained in the laboratory with instruments that are not far from being space-qualified. The WFIRST-AFTA project (WFIRST 2014) should fly with such a coronagraph but the central obstruction will make the $10^{-10}$ rejection not feasible. The starshade technology is currently being developed at JPL (NASA 2014).
For the interferometer, the maturity is lower. At JPL, Martin et al. (2012) demonstrated in the laboratory the capacity of cancelling the stellar light and recovering that of an artificial planet, with the contrast needed in the thermal IR $\left(\sim 10^{-7}\right)$. However, this was made at high fluxes, e.g., using $\mathrm{CO}_{2}$ lasers. To go further and demonstrate that capacity with astronomical fluxes, a cryogenic experiment is needed, which is not planned. In addition, the instrument must be compact and spacequalified. There is no identified show-stopper, but an important technology effort is required to reach the appropriate TRL.

On the other hand, formation flying is not that far from maturity. In 2010, the success of the Swedish mission PRISMA
qualified the navigation at the centimetre level using radiofrequency sensors for intersatellite distances ranging from 2 to $10,000 \mathrm{~m}$, without loss or collision. When the distance was kept fixed, the standard deviation in $X, Y$, and $Z$ was $\sim 2.5 \mathrm{~cm}$ for satellites in a low Earth orbit (LEO), which is not a gravitationally quiet environment. During a series of simulated astronomical observations, the pointing of the two satellites was set in predefined directions with a typical accuracy of 1.7 arcmin (Delpech et al. 2013). In 2017, the approved PROBA-3 mission (ESA 2012) should qualify it at the level of laser sensors $(0.1 \mathrm{~mm})$, which is more than enough for the requirements of nulling interferometers having internal delay-lines.

Most of the estimates made in this paper are made under the hypothesis that a prior mission has detected the planets of interest.

Building both types of spectroscopic instruments, coronagraph and interferometer, would be, by far, the best solution because they are complementary (Beichman et al. 2007). Most of the scientific community agrees that this is what we need in the longer term. The two instruments work in different parts of the electromagnetic spectrum, and each one is better suited for detecting a given group of gases: $\mathrm{O}_{2}, \mathrm{H}_{2} \mathrm{O}, \mathrm{CH}_{4}$ for coronagraphs, $\mathrm{O}_{3}, \mathrm{CH}_{4}, \mathrm{CO}_{2}$, for interferometers $\left(\mathrm{H}_{2} \mathrm{O}\right.$ can be detected only with difficulty). Having access to both wavelength ranges on the same planets would provide a much firmer basis for our conclusions. Fortunately, there is some overlap between the two lists of accessible solar-type stars. For instance, among the 15 best stars in the built-in coronagraph list (Table 3), 10 are also in the interferometer list limited to rank 100 (full Table 9).
Now, the present paper addresses the question: which affordable first mission can provide the largest harvest? If $\eta_{\text {Earth }}$ were to be confirmed small for FGK stars, then a built-in coronagraph on a large $(\sim 5 \mathrm{~m})$ mirror, or $\mathrm{a} \geqslant 60 \mathrm{~m}$ starshade, would be necessary to obtain a significant sample of planets $(\sim 10)$, whereas a middle-sized interferometer, e.g., $4 \times 0.6 \mathrm{~m}$, could do it (Table 12 and Table 13).

This also stresses the interest in reaching a consensus on the value of $\eta_{\text {Earth }}$ from Kepler data. The values of $\eta_{\text {solar }}$ already obtained by Petigura et al. (2013) and Silburt et al. (2015) are in good agreement when the same definition of the HZ is adopted. If the definition used is that of Section 2, i.e., $a_{\text {in }}=0.99 L_{i}^{1 / 2}$ and $a_{\text {out }}=1.70 L_{i}^{1 / 2}$ for a Sun-like spectrum and $R_{\mathrm{pl}}=1.0-2.0 R_{\text {Earth }}$ planets, these authors find $\eta_{\text {solar }}=8.6 \%$ $\pm 3 \%$, and $\eta_{\text {solar }}=6.4 \%+3 /-1 \%$, respectively. Were these numbers the ultimate values, Figures 4 and 7 would indicate the number of planets that could be studied by each instrument.
In summary, Table 12 and Table 13 point out that the interferometer remains an important part of the (Darwin, TPFI) $/($ TPF-C, Starshade $)$ debate.

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Note added in proof. The derivation of the best value of $\eta_{\text {earth }}$ from the Kepler mission data is still an on-going work. The latest, but still preliminary, estimate by the Kepler team is M stars $0.25 \pm 0.11$, K stars $0.10 \pm 0.06$, and G stars $0.36 \pm 0.21$ (N. Batalha, private communication). The value, 0.50 , used in the present paper for M stars seems to be overestimated, but this would not drastically change our conclusions. The model presented in the present paper can be applied for any value of $\eta_{\text {earth }}$ for the different spectral types.

## APPENDIX A <br> MINIMUM DISTANCE OF A STELLAR COMPANION FOR A BUILT-IN CORONAGRAPH

The number of photoelectrons on the detector from the planet (signal), from the target star, and from a companion star are, in order,

$$
\begin{aligned}
N_{\mathrm{pl}} & =(1 / 128 h \nu) \mathrm{AY}_{*}^{\prime}\left(R_{\mathrm{pl}} / a\right)^{2}(\Phi / D)^{2} t \\
N_{*} & =(1 / 16 h \nu) \rho \mathrm{Y}_{*}^{\prime}(\Phi / D)^{2} t \\
N_{\text {comp }} & =(1 / 16 h \nu) \operatorname{Airy}(\theta) \mathrm{Y} L_{\text {comp }}^{\prime}(\Phi / D)^{2} t
\end{aligned}
$$

where $L^{\prime}$ are the stellar luminosities within the spectral band of the instrument $(0.6-0.8 \mu \mathrm{~m})$, approximately the R band for Si based detectors, and $\operatorname{Airy}(\theta)$ the Airy function.

1. Using $F_{0}=3.6 \times 10^{-9}\left[\mathrm{~W} \mathrm{~m}^{-2}\right]$ for a $R=0$ object, the luminosity of a $R$ magnitude star at distance $D[\mathrm{~m}]$ is

$$
L^{\prime}=4.5 \times 10^{-8} \times 10^{-0.4 R} D^{2} \quad[\mathrm{~W}]
$$

2. The number of photoelectrons from the planet is

$$
N_{\mathrm{pl}}=3.0 \times 10^{8}(D / 1 \mathrm{pc})^{-2}(\Phi / 1 \mathrm{~m})^{2}(t / 1 \text { day })
$$

3. From a companion, at angular distance $\theta$, this is
$N_{\text {comp }}=1.19 \times 10^{17} \operatorname{Airy}(\theta) 10^{-4 R_{\text {comp }}}(\Phi / 1 \mathrm{~m})^{2}(t / 1$ day $)$.
Requiring a signal/noise, $N_{\mathrm{pl}} / N_{\text {comp }}{ }^{1 / 2}$, of 10 , the Airy function must decrease the companion flux by a factor
Airy $(\theta)=1.8310^{-8}(D / 1 \mathrm{pc})^{-4} 10^{0.4 R_{\text {comp }}}(\Phi / 2.4 \mathrm{~m})^{2}(t / 1$ day $)$
The Airy envelope at large angle $\theta$ is $\operatorname{Airy}(x)=(8 / \pi) x^{-3}$, $x \equiv \theta \Phi / \lambda$. With the reference values for the nearest target stars: $D=3 \mathrm{pc}$, and $R_{\text {comp }}=3$ and a 2.4 m mirror, the angular separation of a companion must satisfy Equation (8):

$$
\begin{aligned}
\theta_{\text {comp }}> & 35.5(D / 3 \mathrm{pc})^{1.33} 10^{-0.13\left(R_{\text {comp }}-3\right)} \\
& \times(\Phi / 2.4 \mathrm{~m})^{2}(t / 1 \text { day })^{-1 / 3} \quad[\operatorname{arcsec}]
\end{aligned}
$$

## REFERENCES

Angel, R., Cheng, A., \& Woolf, N. 1986, Natur, 324, 518
Arnold, L., Ehrenreich, D., Vidal-Madjar, A., Dumusque, X., Nitschelm, C., et al. 2014, A\&A, 564, A58
Atlast 2009, a NASA Astrophysics Strategic Mission Concept Study, M. Postman PI (Baltimore, MD: STScI)

Batalha, N. 2014, PNAS, 111, 12647
Batalha, N. M., Rowe, J. F., Bryson, S. T., et al. 2012, ApJS, 204, 24

Beichman, C. A., Allen, R., Bely, P., Capps, R., Carlstrom, J., et al. 1996, http://exep.jpl.nasa.gov/exnps/index.html
Beichman, C. A., Woolf, N. J., \& Lindensmith, C. A. 1999, JPL publication 99-3, NASA
Beichman, C. A., Bryden, G., Stapelfeldt, K. R., Gautier, T. N., Grogan, K., Shao, M., et al. 2006, ApJ, 652, 1674
Beichman, C. A., Fridlund, M., Traub, W. A., Stapelfeldt, K. R., et al. 2007, in Protostars and Planets V, ed. B. Reipurth, D. Jewitt \& K. Keil (Tucson, AZ: Univ. Arizona Press), 915
Bonfils, X., Delfosse, X., Udry, S., Forveille, T., Mayor, M., et al. 2013, A\&A, 549, A109
Borucki, W. J., Dunham, E. W., Koch, D. G., Cochran, W. D., Rose, J. D., et al. 1996, Ap\&SS, 241, 111
Borucki, W. J., Koch, D. G., Basri, G., Batalha, N., Brown, T. M., et al. 2011, ApJ, 736, 19
Burke, B. F. 1992a, in Astrophysics on the Threshold of the 21st Century, ed. N. S. Kardashev (New York: Gordon \& Breach), 303

Burke, B. F. 1992b, in Targets for Space-Based Interferometry, ed. C. Mattok (Paris: European Space Agency), 81
Chazelas, B., Brachet, F., Bordé, P., Mennesson, B., Ollivier, M., et al. 2006, ApOpt, 45, 984
Chen, D., Wu, J., \& Li, B. 2013, in Step Mission, European Planetary Science Congress (EPSC) Abstracts 8, 1102
Cockell, C. S., Herbst, T., Léger, A., Absil, O., Beichman, C., et al. 2009, ExA, 23, 435
Danchi, W., Bailey, V., Bryden, G., Defrère, D., Haniff, C., et al. 2014, Proc. SPIE, 9146, 914607
Defrère, D., Absil, O., den Hartog, R., Hanot, C., \& Stark, C. 2010, A\&A, 509, A9
Defrère, D., Stark, C., Cahoy, K., \& Beerer, I. 2012, Proc. SPIE, 8442, 84420M
Defrère, D., Hinz, P. M., Skemer, A. J., Kennedy, G. M., Bailey, V. P., et al. 2015, ApJ, 799, 42
Delpech, M., Berges, J.-C., Karlsson, T., \& Malbet, F. 2013, Int. J. Space Science and Engineering, 1, 382
Democritos of Aidera, 460-371 BC, http://en.wikipedia.org/wiki/Democritus
den Hartog, R. 2005, The DarwinSim Science Simulator, Tech. Rep. Issue 1, ESA (SCI-A/297)
Des Marais, D. J., Harwit, M. O., Jucks, K. W., Kasting, J. F., Lin, D. N. C., et al. 2002, AsBio, 2, 153
Ehrenreich, D., Tinetti, G., Lecavelier Des Etangs, Vidal-Madjar, A., \& Selsis, F. A. 2006, A\&A, 448, 379
Epicurus of Samos, 341-270 BC: http://en.wikipedia.org/wiki/Epicurus
ESA 2012, The Proba-3 mission, http://www.esa.int/Our_Activities/ Technology/Proba_Missions/
Forget, F., \& Pierrehūmber, R. T. 1997, Sci, 278, 1273
Gaidos, E. 2013, ApJ, 770, 90
Gomez-Leal, I., Palle, E., \& Selsis, F. 2012, ApJ, 752, 28
Guyon, O. 2002, A\&A, 387, 366
Guyon, O., Pluzhnik, E. A., Kuchner, M. J., Collins, B., \& Ridgway, S. T. 2006, ApJS, 167, 81
Kasting, J. F., Whitmire, D. P., \& Reynolds, R. T. 1993, Icar, 101, 108
Kharecha, P., Kasting, J. F., \& Siefert, J. L. 2005, Geobiology,, 3, 53
Kopparapu, R. K. 2013, ApJL, 767, L8
Kopparapu, R. K., Ramirez, R., Kasting, J. F., Eymet, V., Robinson, T. D., et al. 2013, ApJ, 765, 131
Kopparapu, R. K., Ramirez, R. M., SchottelKotte, J., et al. 2014, ApJL, 787, L29
Kouveliotou 2013, Enduring Quests, Daring Visions http://science.nasa.gov/ media/medialibrary/2013/12/20/secure-Astrophysics_Roadmap_2013.pdf.
Lagrange, A.-M., Meunier, N., Desort, M., \& Malbet, F. 2011, A\&A, 528, L9
Laplace, P. S. 1878, in Les oeuvres complétes de Laplace (Paris: GauthierVillars), http://gallica.bnf.fr/
Lay, O. 2004, ApOpt, 43, 6100
Lay, O. 2005, ApOpt, 44, 5870
Lay, O. P. 2006, Proc. SPIE, 6268, 62681A
Leconte, J., Forget, F., Charnay, B., Wordsworth, R., \& Pottier, A. 2014, Natur, 504, 268
Léger, A. 2001, l'Astronomie,, 115, 310
Léger, A., Pirre, M., \& Marceau, F. J. 1993, A\&A, 277, 309
Léger, A., Rouan, D., Schneider, J., et al. 2009, A\&A, 506, 287
Léger, A., Selsis, F., Sotin, C., Guillot, T., Despois, D., et al. 2004, Icar, 169, 499
Levine, M., Lisman, D., \& Shaklan, S. 2009, TPF-C Report, JPL, NASA Doc. 34923

Lunine, J., Fischer, D., Hammel, H., Henning, T., Hillenbrand, L., et al. 2009 arXiv:0808.2754v3
Maire, A.-L., Galicher, R., Boccaletti, A., Baudoz, P., Schneider, J., et al. 2012, A\&A, 541, 83
Malbet, F., et al. 2012, ExA, 34, 385
Martin, S., Booth, A., Liewer, K., et al. 2012, ApOpt, 51, 10
Mayor, M., \& Queloz, D. 1995, Natur, 378, 355
Mennesson, B., Léger, A., \& Ollivier, M. 2005, Icar, 178, 570
Mennesson, B., Millan-Gabet, R., Serabyn, E., Colavita, M. M., Absil, O., et al. 2014, ApJ, 797, 119
Meunier, N., Desort, M., \& Lagrange, A.-M. 2010, A\&A, 512, A39
NASA 2014, Starshades for Exoplanet Imaging and Characterisation, Solicitation NNH09ZDA001N-TDEM
Owen, T. 1980, in Strategies for the Search of Life in the Universe, ed. M. D. Papagiannis (Dordrecht: Reidel), 177
Petigura, E. A., Howard, A. W., \& Marcy, G. W. 2013, PASP, 124, 418
Quanz, S. P., Crossfield, I., Meyer, M. R., Schmalzl, E., \& Held, J. 2015, IJAsB, 14, 279
Quirrenbach, A. 2013, Exploring Habitable Worlds beyond our Solar System http://sci.esa.int/white-papers-2013/
Reach, W. T., Franz, B. A., Weiland, J. L., et al. 1995, Natur, 374, 521

Roberge, A., Chen, C. H., Millan-Gabet, R., Weinberger, A. J., Hinz, P. M., et al. 2012, PASP, 124, 799
Rodler, F., \& López-Morales, M. 2014, ApJ, 781, 54
Rogers, L. A. 2015, ApJ, in press (arXiv:1407.4457v1)
Schneider, J. 1995, Ap\&SS, 223, 185
Seager, Sara., Cash, Webster, C., Kasdin, N. J., Sparks, W. B., Turnbull, M. C., et al. 2014, AAS Meeting Abstracts, 224, 311.06
Selsis, F., Despois, D., \& Parisot, J.-P. 2002, A\&A, 388, 985
Selsis, F., Chazelas, B., Bordé, P., Ollivier, M., et al. 2007, Icar, 191, 453
Silburt, A., Gaidos, E., \& Wu, Y. 2015, ApJ, 799, 180
Stark, C. C., Roberge, A., Mandell, A., \& Robinson, T. D. 2014, ApJ, 795, 122
Thomas, S. J., Bendek, E., \& Belikov, R. 2014, Proc. SPIE, 9143, 914335
Tian, F., \& Ida, S. 2015, NatGe, 8, 177
Traub, W. 2013, at Kepler Conf. II
Truzzi, M. 1978, Zetetic Scholar, 1, 11
Turnbull, M. C., Glassman, T., Roberge, A., et al. 2012, PASP, 124, 418
Ulmschneider 2006, Intelligent Life in the Universe (Berlin: Springer)
van Leeuwen 2007, A\&A, 474, 653
WFIRST 2014, The Wide-Field Infrared Survey Telescope (WFIRST), http:// wfirst.gsfc.nasa.gov
Yang, J., Cowan, N. B., Dorian, S., \& Abbot, D. S. 2013, ApJL, 771, L45


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[^1]:    8 For direct detection spectroscopy, the signal is $\propto R_{\mathrm{pl}}^{2}$, and integration time $\propto R_{\mathrm{pl}}^{-4}$. When time is the limiting parameter, the mean planetary radius between 1.0 and 2.0 is 1.58 . For a radius distribution constant in $\log \left(R_{\mathrm{pl}}\right)$, the mean value is 1.41 . The adopted mean value of 1.50 is close to these two values.

[^2]:    9 The IR stellar flux is $\propto k T_{*}$ (Rayleigh regime), the bolometric is $\propto k T_{*}^{4}$, and the correction is $\propto k T_{*}^{3}$.

[^3]:    ${ }^{10}$ Based on the $380 \mathrm{~F}, \mathrm{G}, \mathrm{K}$ stars at $D<20 \mathrm{pc}$.

[^4]:    ${ }^{11}$ The boundary between stars having, or not, phase-locked planets in their HZ is complex. For $a_{\mathrm{HZ}}=1.3 \mathrm{L1} 1^{/ 2}[\mathrm{AU}]$, the boundary would be at the limit between M and K stars only in the absence of other planets that could prevent this locking by maintaining some eccentricity. This boundary is used thereafter, being warned of the corresponding simplification. The knowledge of individual planetary systems, and an estimate of possible resonances, would allow a better selection.

[^5]:    $\overline{{ }^{12}}$ Even if some enthusiasts are considering telescopes with diameters up to 10 m (Atlast 2009).

