

# EUROWD14 Montreal

## The instability strip of ZZ Ceti white dwarfs

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- Introduction of Time-Dependent Convection (TDC):  
Van Grootel et al. 2012, A&A, 539, 87
- Extension to Extremely Low Mass (ELM) pulsators:  
Van Grootel et al. 2013, ApJ, 762, 57

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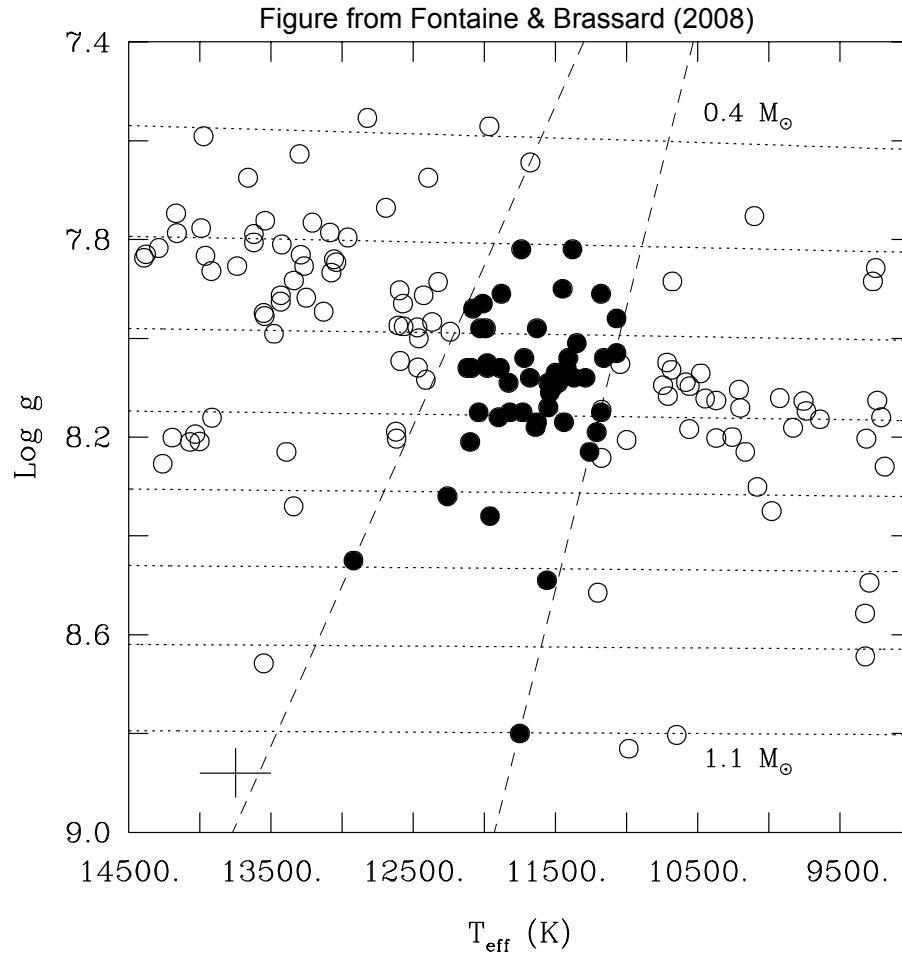


# Pulsations in DA white dwarfs

# Pulsating DA white dwarfs

## Empirical ZZ Ceti instability strip (classic view)

- Observed pulsator ; ○ non-variable DA white dwarf

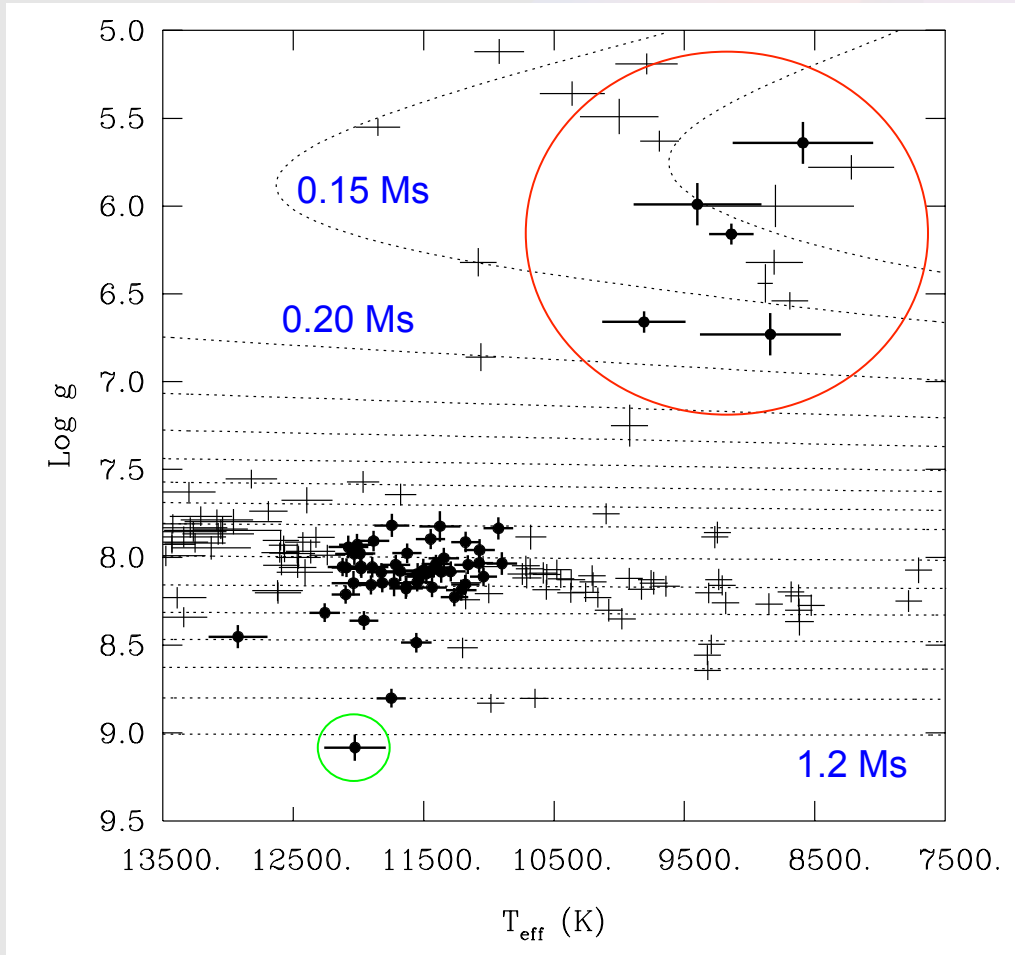


- Multiperiodic pulsators, observed period range: 100-1500 s (g-modes)
- Reliable atmospheric parameters: work of Bergeron et al., Gianninas et al., here with  $ML2/\alpha=0.6$
- (most probably) a **pure** strip
- $\log g/T_{\text{eff}}$  correlation (with a more pronounced slope for red edge): the lower  $\log g$ , the lower edge  $T_{\text{eff}}$

# Pulsating DA white dwarfs

## Empirical ZZ Ceti instability strip (2014 view)

⊕ non variable (<10mmag); ● pulsator



Hermes et al. (2012, 2013a,b):

**5 ELM pulsators**

(SDSS J1840, J1112, J1518, J1614, J2228)

Multiperiodic pulsators, 1500-6000 s

Hermes et al. (2013c):

**1 UHM pulsator**

(GD 518)

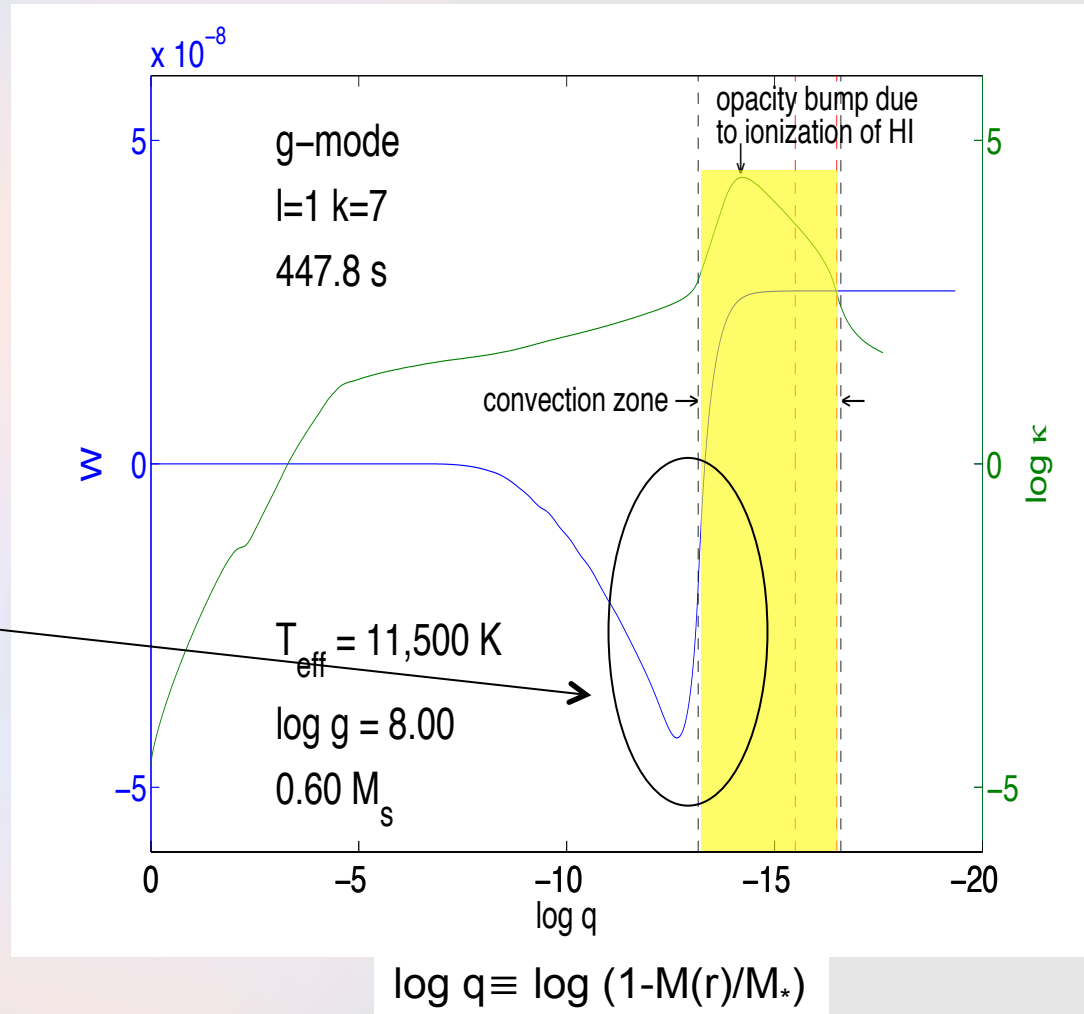
Multiperiodic pulsator, 425-595 s

# Pulsating DA white dwarfs

## Excitation mechanism of ZZ Ceti stars (general picture)

- Don Winget (1981):  
H recombination around  $T_{\text{eff}} \sim 12,000 \text{ K}$   
⇒ envelope opacity increase  
⇒ strangle the flow of radiation  
⇒ modes instabilities
- Pulsations are destabilized at the base of the convection zone (details: e.g. Van Grootel et al. 2012)

**“convective driving”**



Pulsations are driven when the convection zone is sufficiently deep and developed

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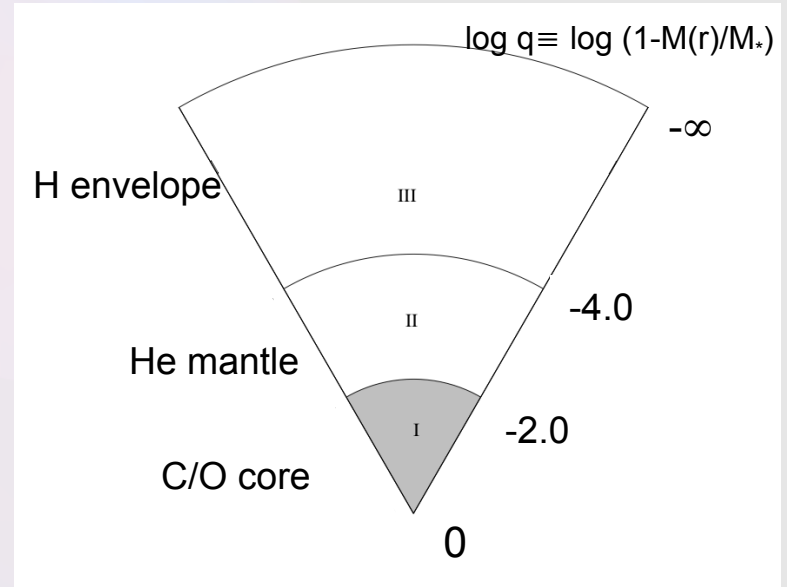
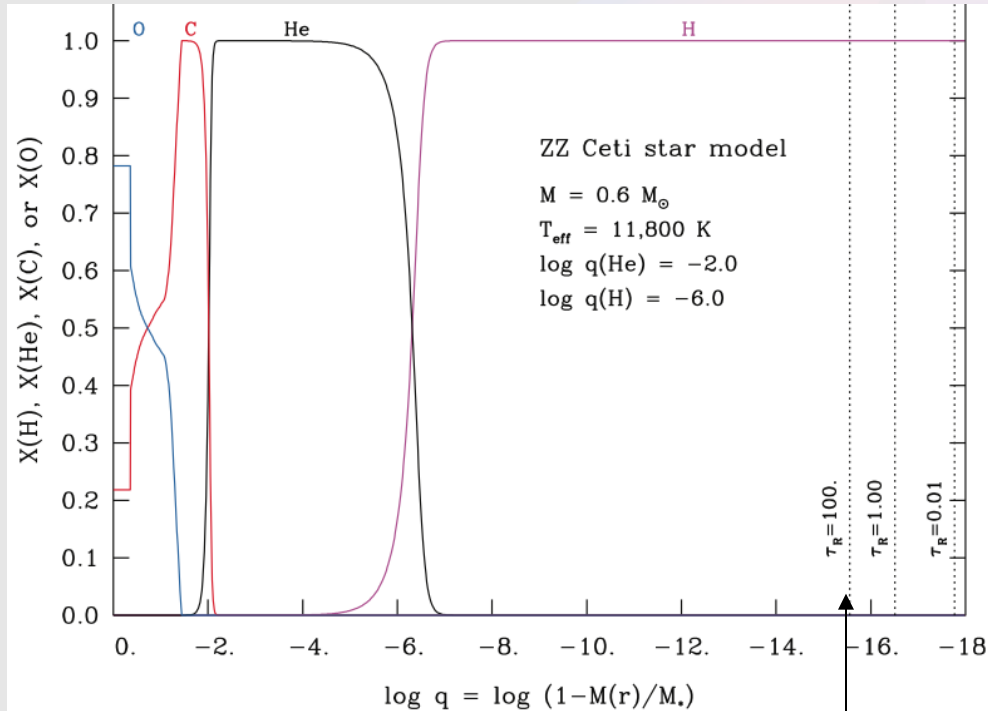
# **The theoretical instability strip**

- **Evolutionary DA White Dwarf Models**

# Evolutionary DA models

- A standard DA white dwarf structure model (C/O core)

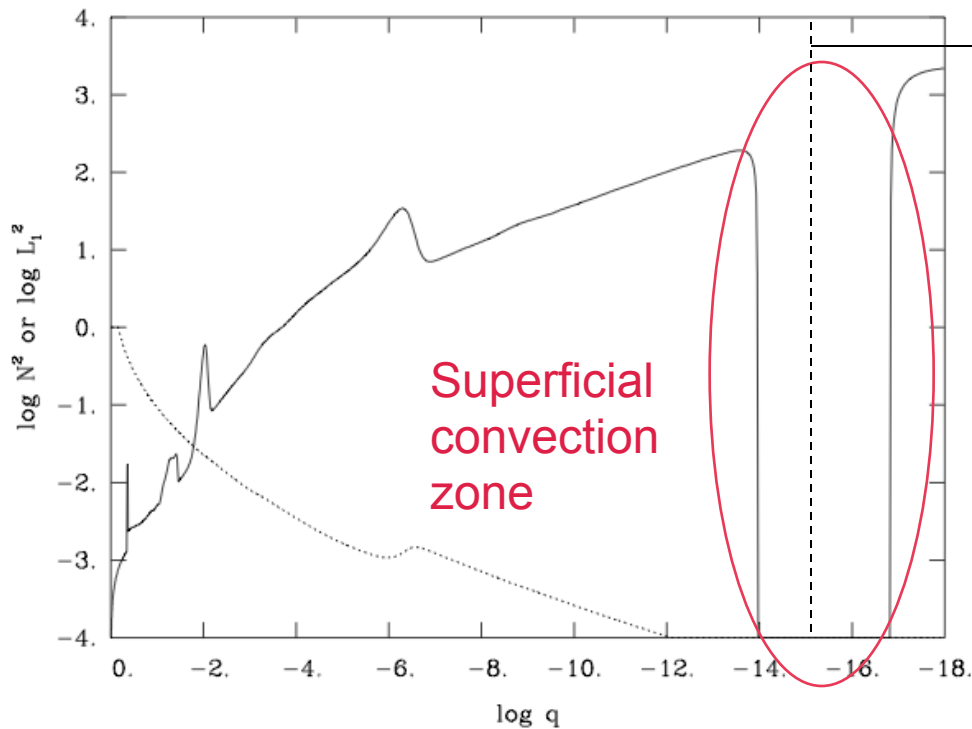
“onion-like” stratification



Base of the atmosphere

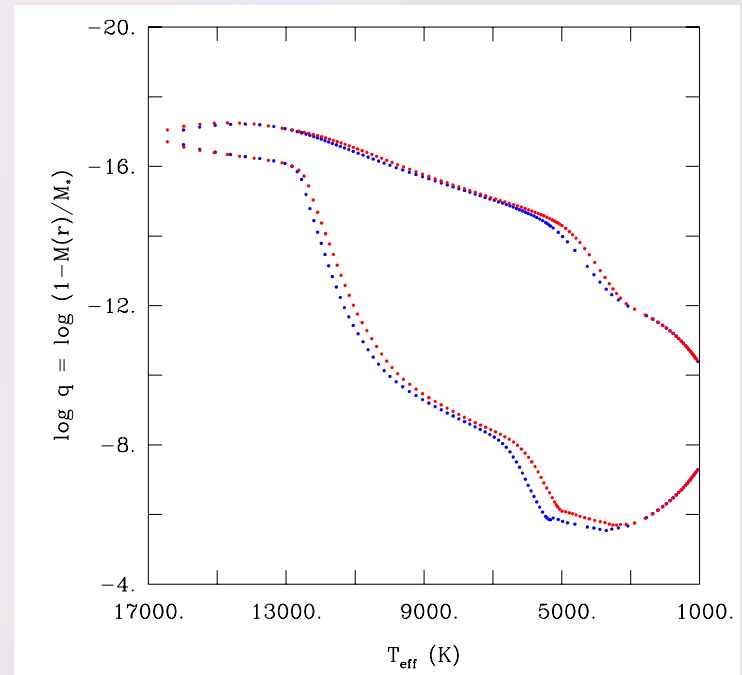
- Evolutionary tracks computed for  $0.4M_{\text{s}}$  to  $1.2M_{\text{s}}$  ( $0.1M_{\text{s}}$  step)
- from  $T_{\text{eff}}=35,000 \text{ K}$  to  $2,000 \text{ K}$  ( $\sim 150$  models)
- with ML2 version ( $a=1, b=2, c=16$ );  $\alpha = 1$  (ie  $I = H\text{p}$ )

# Evolutionary DA models



Base of the atmosphere

Detailed modeling of the superficial layers



Our evolutionary models have the same T stratification as the complete (1D) model atmospheres  
 $\Rightarrow$  "feedback" of the convection on the global atmosphere structure

- Standard grey atmosphere
- Detailed atmosphere

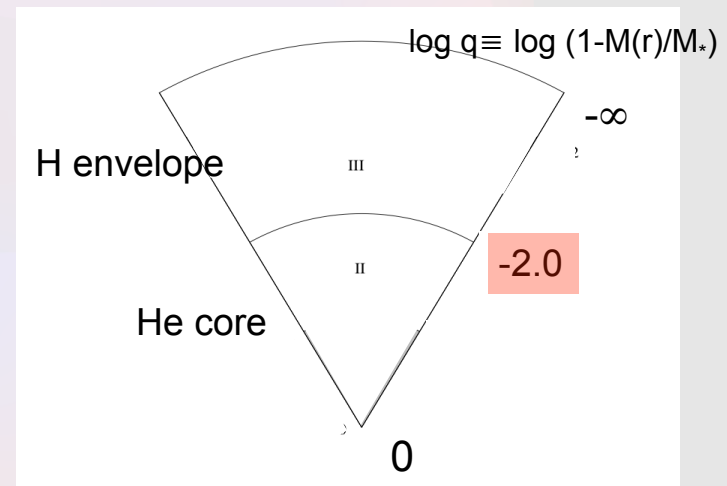
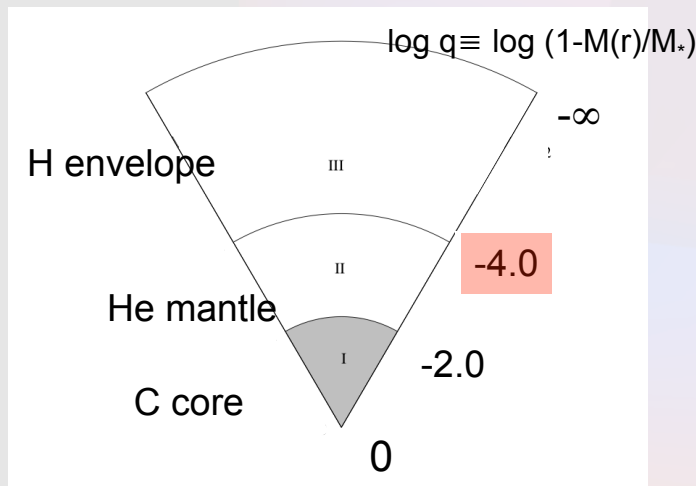


# Evolutionary DA models

- Extremely Low Mass (ELM) DA white dwarf:  
H envelope on top of He core

ELM white dwarfs come from stars that never experienced any He-flash, because of extreme mass loss on RGB (from binary interactions or due to high Z)

- 2 kinds of evolutionary tracks computed here:
  - Standard C core models, but for  $0.125M_{\odot}$  and  $0.15-0.4M_{\odot}$  (steps  $0.05M_{\odot}$ )
  - Pure He core/H envelope models, for the same masses, thick envelopes



*Instability strip location in  $T_{\text{eff}} - \log g$  plane **insensitive** to detailed core composition and envelope thickness*

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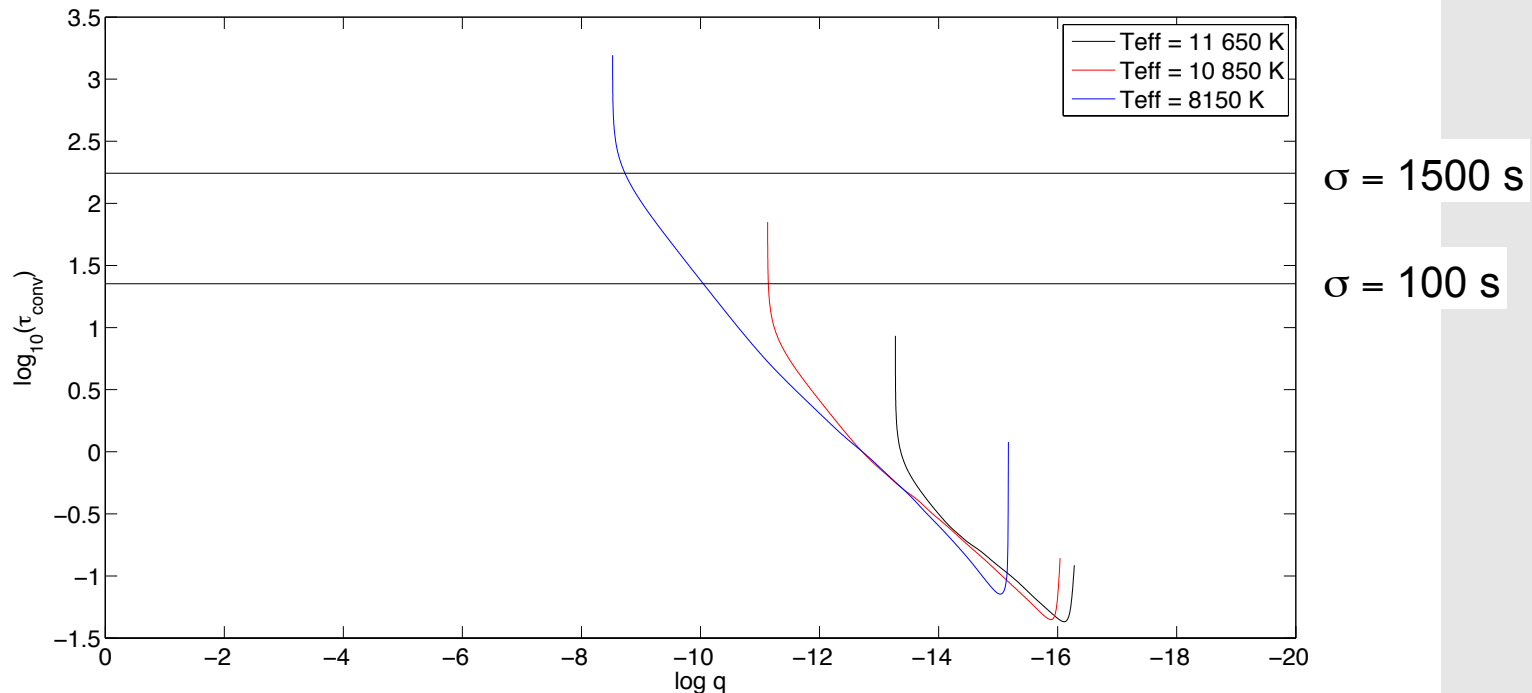
## **The theoretical instability strip**

- **Evolutionary DA White Dwarf Models**
- **Time-Dependent Convection (TDC) Approach**

# The Time-Dependent Convection approach

For a standard  $0.6M_s$  DA model:

- $T_{\text{eff}} \sim 12,000$  K: convective turnover timescale  $\tau_{\text{conv}} \ll \sigma$  (pulsation periods)  
 $\Rightarrow$  convection adapts quasi-instantaneously to the pulsations
- $T_{\text{eff}} \sim 11,000$  K:  $\tau_{\text{conv}} \approx \sigma \Rightarrow$  NEED full Time-Dependent Convection (TDC)
- Frozen convection (FC), i.e.  $\tau_{\text{conv}} \gg \sigma$ : NEVER justified in the ZZ Ceti  $T_{\text{eff}}$  regime  
*(FC is the usual assumption to study the theoretical instability strip)*



# The Time-Dependent Convection theory

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- Full development in [Grigahcène et al.\(2005\)](#), following the theory of [M. Gabriel \(1974,1996\)](#), based on ideas of [Unno et al. \(1967\)](#)
- The Liege nonadiabatic pulsation code **MAD** ([Dupret 2002](#)) is the only one to implement convenient TDC treatment
- The timescales of pulsations and convection are **both** taken into account
- Perturbation of the convective flux taken into account here:

$$\delta F_C = \overline{F_C} \left( \frac{\delta \rho}{\overline{\rho}} + \frac{\delta T}{\overline{T}} \right) + \overline{\rho T} (\overline{\delta \Delta s V} + \overline{\Delta s \delta V})$$

- Built within the mixing-length theory (MLT), with the adopted perturbation of the mixing-length:

$$\frac{\delta l}{l} = \frac{1}{1 + (\sigma \tau_c)^2} \frac{\delta H_p}{H_p}$$

if  $\sigma \gg \tau_{\text{conv}}$  (instantaneous adaption):  $\delta l/l \rightarrow \delta H_p/H_p$

if  $\sigma \ll \tau_{\text{conv}}$  (frozen convection):  $\delta l/l \rightarrow 0$

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# The theoretical instability strip

- **Evolutionary DA White Dwarf Models**
- **Time-Dependent Convection (TDC) Approach**
- **Results**

# Results: computing the theoretical instability strip

- We applied the MAD code to all evolutionary sequences

- “normal” CO-core DA models,  $0.4 - 1.2 M_{\odot}$ ,  $\log q(H) = -4.0$
- ELM, C-core models:  $0.125 - 0.4 M_{\odot}$ ,  $\log q(H) = -4.0$
- ELM, He-core models:  $0.125 - 0.4 M_{\odot}$ ,  $\log q(H) = -2.0$
- $0.17 M_{\odot}$ , He-core models, “thin” envelope  $\log q(H) = -3.7$

with  $ML2/\alpha = 1$ , detailed atmospheric modeling, and TDC treatment

- We computed the degree  $l=1$  in the range 10-7000 s (p- and g-modes)
- For the red edge (long-standing problem):

based on the idea of Hansen, Winget & Kawaler (1985): red edge arises when

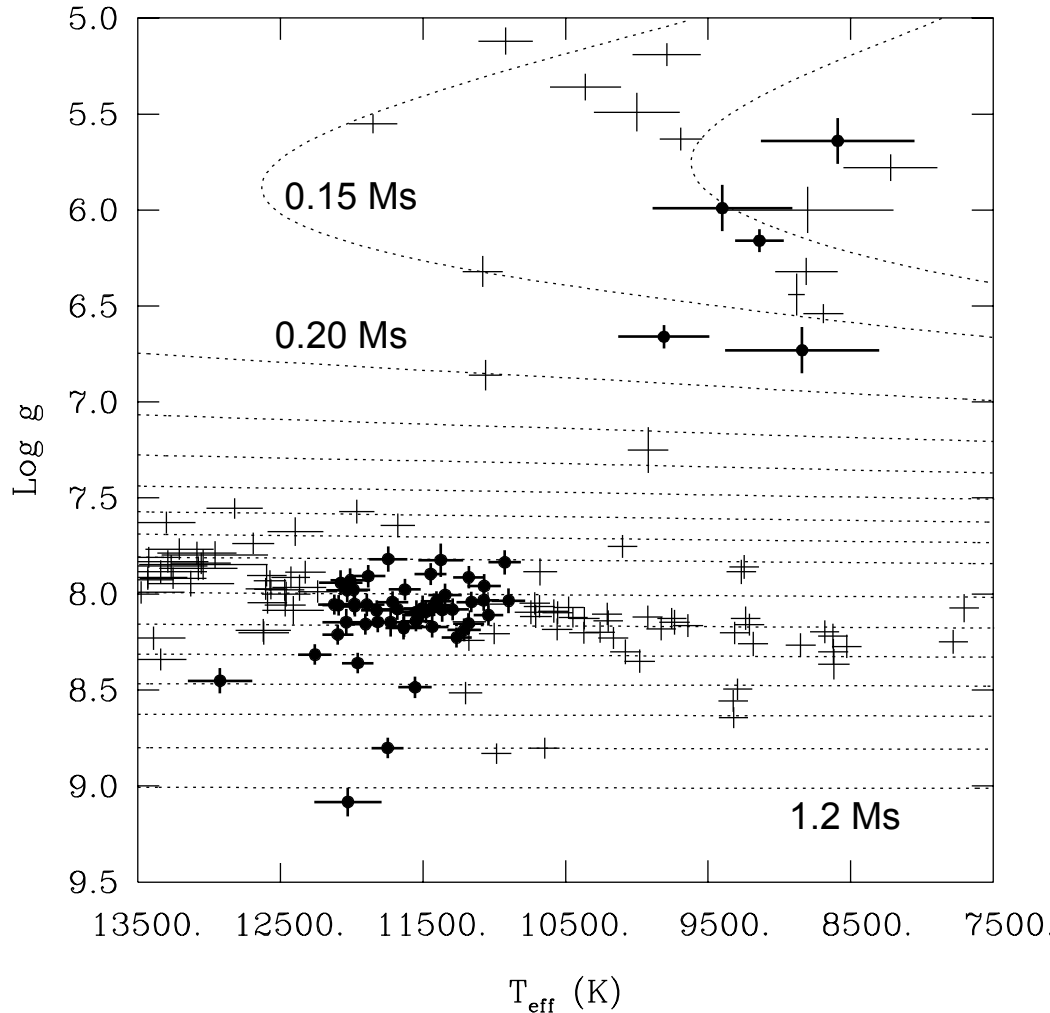
$$\tau_{\text{th}} \sim P_{\text{crit}} \propto (l(l+1))^{-0.5}$$

( $\tau_{\text{th}}$  : thermal timescale at the base of the convection zone),

which means the mode is no longer reflected back by star’s atmosphere

# Empirical ZZ Ceti instability strip (2014 view)

⊕ non variable (<10mmag); ● pulsator



## Spectroscopic estimates:

- ELM white dwarfs: D. Koester models (Brown et al. 2012)
- UHM white dwarf: Gianninas et al. (2011)
- Standard ZZ Ceti: P. Bergeron et al.

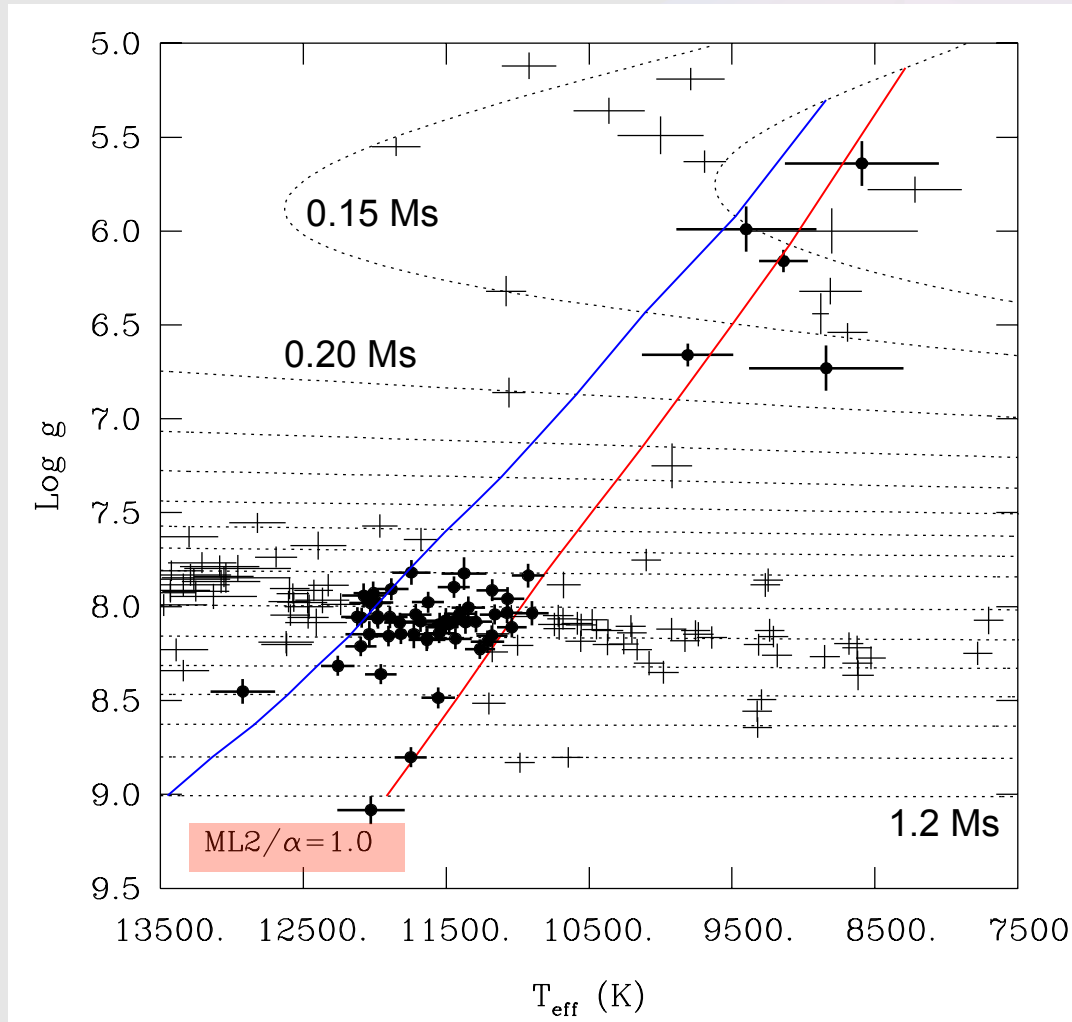
But all **ML2/α=0.6**

(must be consistent)

+ standard ZZCeti: spectroscopic observations gathered during several cycles of pulsations

# Theoretical instability strip (g-modes $l=1$ )

—+— non variable (<10mmag); —●— pulsator



— TDC blue edge

— Red edge

- Narrower strip at low masses (larger slope for the red edge)

- Structure models:

$$ML2/\alpha = 1$$

Model atmospheres:

$$ML2/\alpha = 0.6$$



Convective efficiency increases with depth?

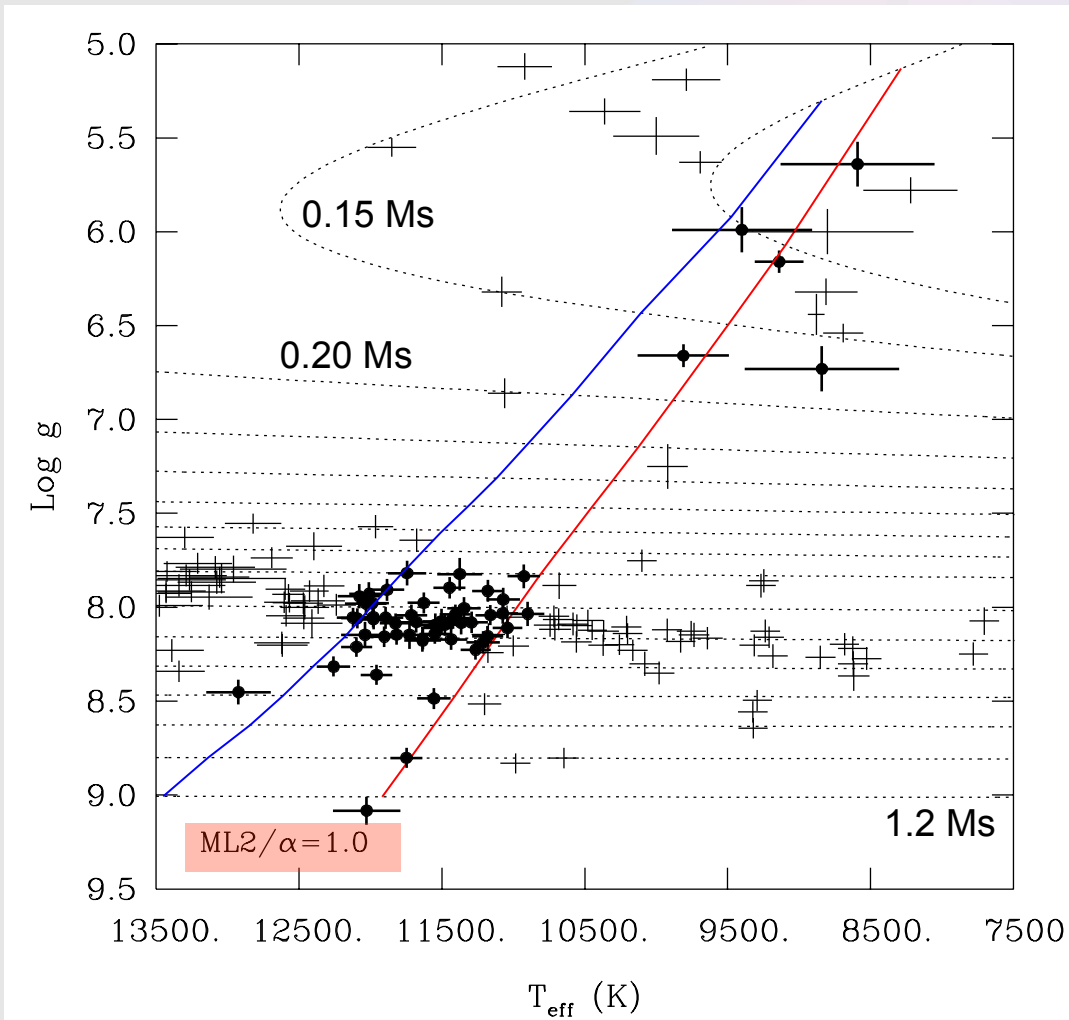
(consistent with hydrodynamical simulations; Ludwig et al. 1994, Tremblay & Ludwig 2011)

**NB: evolutionary and atmospheric MLT calibrations are dependent**



# Theoretical instability strip (g-modes $l=1$ )

Is the whole ZZ Ceti instability strip **pure**?



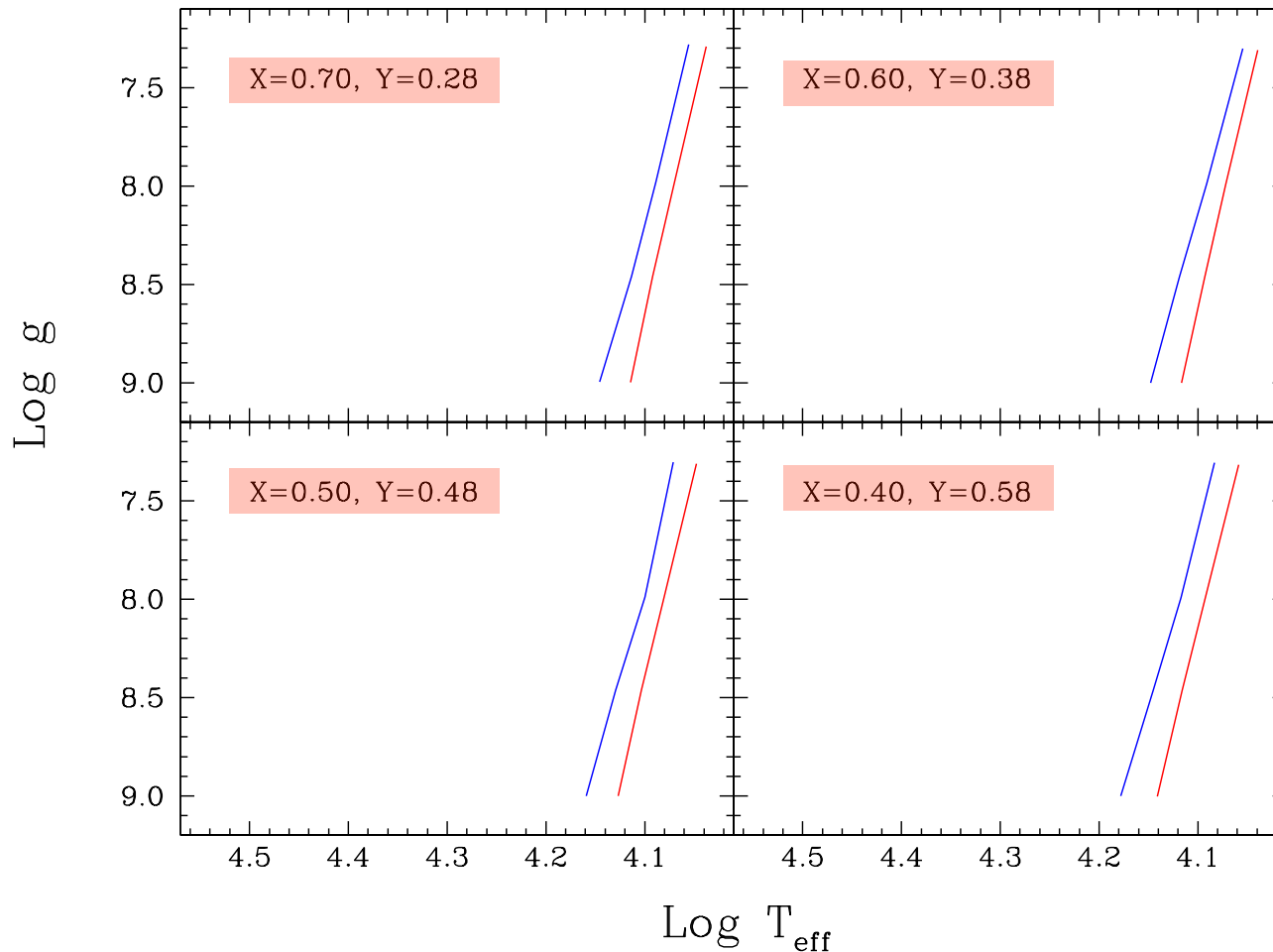
**YES**

- Need only small fine-tuning
- J2228 is a little bit tricky
- Consistency between ML calibrations atmospheres  $\Leftrightarrow$  structure models
- Spectra must cover a few pulsational cycles !

**BUT**

- Are all ELM pure H (DA) white dwarfs or with traces of He ?

# Instability strips of WDs with H/He atmospheres



The instability strip is dependent of the amount of H and He

Details in poster of Van Grootel et al.

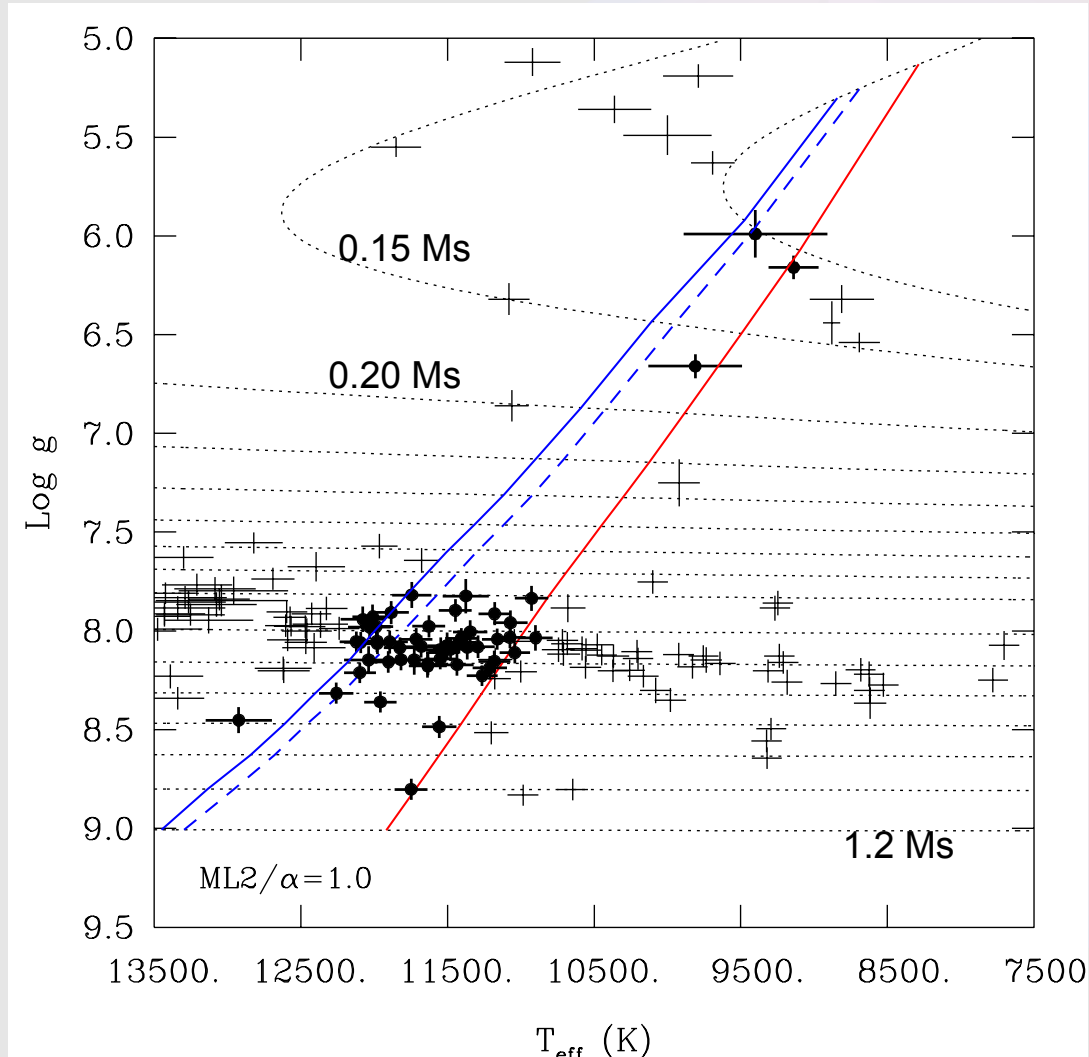
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# The theoretical instability strip

- **Evolutionary DA White Dwarf Models**
- **Time-Dependent Convection (TDC) Approach**
- **Results**
- **Convective Driving**

# Theoretical instability strip (g-modes $l=1$ )

⊕ non variable ( $<10\text{mmag}$ ); ● pulsator



— TDC blue edge  
- - FC blue edge  
— Red edge

Van Grootel et al. (2013)

## A last remark

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### Convective Driving ( $\neq$ $\kappa$ -mechanism or convective blocking)

TDC and FC blue edges are not dramatically different, but:

1. The difference ( $\sim 250$  K) is **not** negligible !

Width of instability strip:  $\sim 1000$  K at  $\log g = 8$  and  $\sim 600$  K at  $\log g = 6$

2. Van Grootel et al. (2012) and Saio (2012, Liege colloquium)

eigenfunctions TDC/FC are really different, and excitation mechanisms too:

- TDC: convective driving (convective flux can be modulated)
- FC:  $\kappa$ -mechanism with radiative luminosity ( $\ll L_{\text{conv}}$ )

But both mechanisms occurs at the same layers (partial ionization zone)

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# Conclusion and prospects

# Conclusion and Prospects

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## Conclusions:

- **Excellent agreement** between theoretical and observed instability strip:
  - Blue edge, TDC approach
  - Red edge, by energy leakage through the atmosphere
- ELM pulsators are low mass equivalent to standard ZZ Ceti pulsators excited by **convective driving**
  - ⇒ such pulsators exist from 0.15 to 1.2  $M_{\odot}$  ( $\log g = 5 - 9$  !)
- Is  **$ML^2/\alpha=1.0$**  the good flavor for convection inside white dwarfs?  
Related to spectroscopic calibration (here  $ML^2/\alpha=0.6$ ) and 3D hydrodynamical simulations (Tremblay et al. 2011,2012, this conference)

## Prospects:

- Is the ZZ Ceti instability strip **pure**? Traces of He in ELM white dwarfs?
- Instability strip with structure models including 3D atmospheres?
- Asteroseismology of ELM/standard/UHM ZZ Ceti white dwarf pulsators

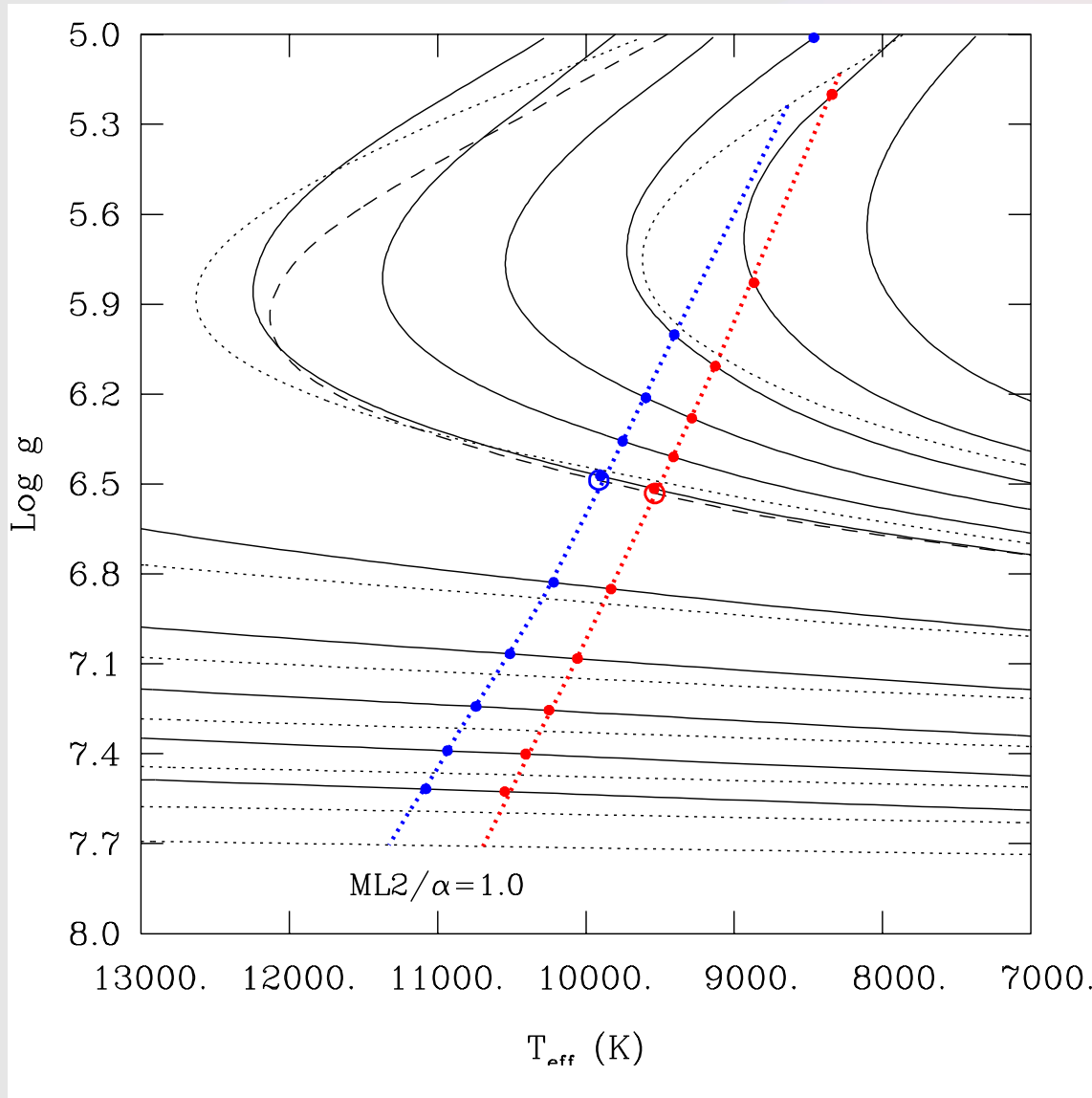
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# Supp. Slides



# Universality of the instability domain



## Tracks:

Solid lines: He core, thick env.  
Dotted lines: C-core, thin env.  
Dashed line:  $0.17M_{\odot}$ , thin env.

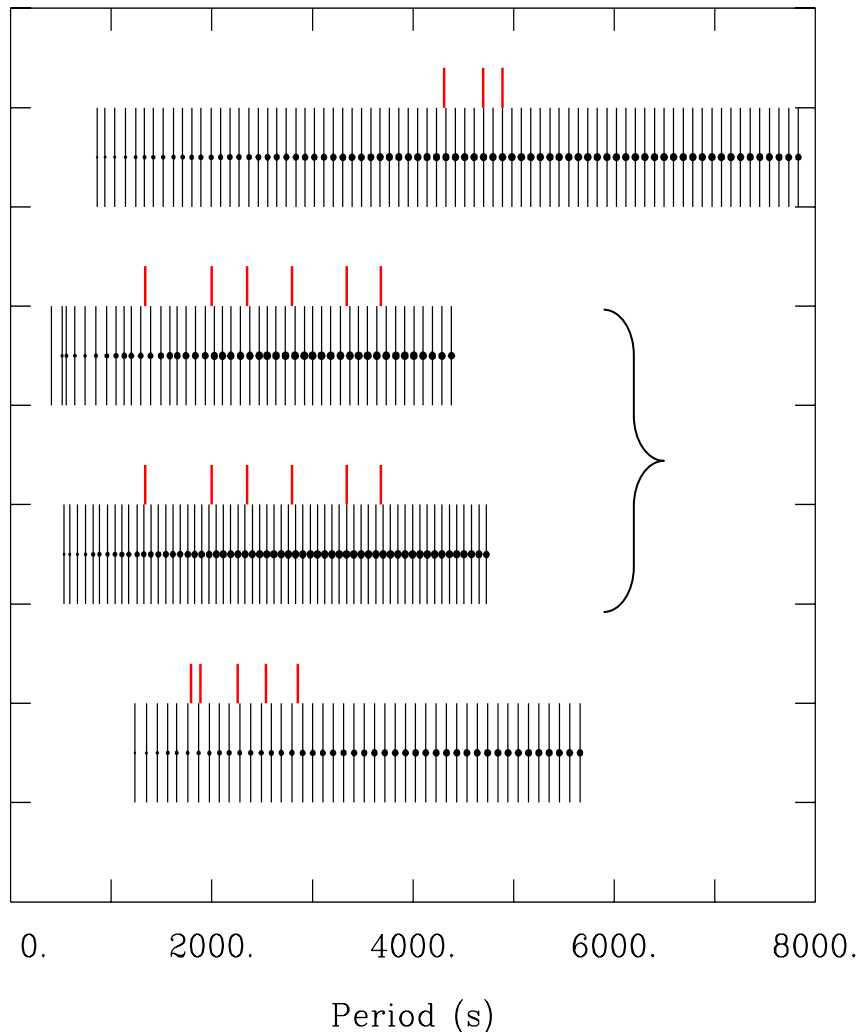
## Edges:

- ⋯ Edges C-core tracks
- Edges He-core tracks
- edges  $0.17M_{\odot}$  track



*Instability domain is insensitive to the exact core composition and envelope thickness for models with same  $T_{\text{eff}}/\log g$*

# Qualitative fit to the observed periods of the 3 ELM pulsators



## SDSS J1840+6423

$T_{\text{eff}} \sim 9140 \pm 170$  K,  $\log g \sim 6.16 \pm 0.06$

He-core model,  $\log q(\text{H}) = -2.0$

## SDSS J1518+0658

$T_{\text{eff}} \sim 9810 \pm 320$  K,  $\log g \sim 6.66 \pm 0.06$

He-core model,  $\log q(\text{H}) = 4.0$  and  $-2.0$

## SDSS J1112+1117

$T_{\text{eff}} \sim 9400 \pm 490$  K,  $\log g \sim 5.99 \pm 0.12$

He-core model,  $\log q(\text{H}) = -2.0$

*Adiabatic properties are sensitive to exact interior structure*