

# Large-scale probabilistic optimization using non-stationary geostatistics for uncertainty assessment of groundwater flow and solute transport

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### Introduction

**Uncertainty quantification** is very much needed to support decision making related to *e.g.* **environmental impact** assessment for waste disposal sites. A probabilistic result provides a much stronger basis for **decision making** compared to a single deterministic outcome. Accurate **posterior** exploration of highdimensional and CPU-intensive models, which are often used for environmental impact assessment, is however a challenging task. To quantify the uncertainty associated with groundwater flow and solute transport in the framework of a near surface radioactive waste disposal in Mol/Dessel, Belgium (Fig 1), we investigate combining the adaptive Metropolis (AM; Haario et al. McMC algorithm, and **iterative spatial** 2001) resampling (ISR; Mariethoz et al. 2009) for large-scale **probabilistic optimization** of a steady-state groundwater flow model (Rogiers et al. 2014).

### **Results**

- ✓ 50 random realizations were optimized with the AM-ISR interrupted Markov chain approach (Fig 4)
- ✓ Global model parameter posterior distributions remain poorly characterized with only 50 samples (Fig 5)
- Model performance increased considerably, mainly due to better simulation of vertical head differences (Fig 6)
- ✓ Groundwater table elevation is mainly affected in the southern part; the variance is lowest near the river and drain network, and high observationdensity areas (Fig 7)
- ✓ General **solute plume evolution** is similar, but



Fig 7: A) Ensemble mean groundwater table elevation (masl). B) Difference with reference model. C) Variance.

1x10<sup>4</sup> days/porosity 2x10<sup>4</sup> days/porosity 5x10<sup>4</sup> days/porosity 1x10<sup>6</sup> days/porosity 2x10<sup>6</sup> days/porosity





#### Fig 1: Study area and site investigation points.

Fig 2: Nonstationarity in the variogram for the K<sub>h</sub> and VANI principal components.



differences exist in terms of **arrival time** and location of the **plume in the lower aquifer** (Fig 8)

✓ Correspondence between ensemble mean log<sub>10</sub>K fields and reference model depends on position in stratigraphy, as well as the variance, which additionally reflects the presence of primary and secondary data (Fig 9)

Fig 8: Solute plume evolution based on a convolution of the random walk particle tracking results, with a unit mass per 100 days input flux at 12 50x50 m source cells.



Fig 9: K fields for the reference model and the ensemble mean and variance.

### **Methods**

### **Groundwater flow model**

- Conditioned on borehole and direct push data (Fig 1), accounting for non-stationary heterogeneity in hydraulic conductivity (*K*) using distance-weighted geostatistics (Machuca-Mory & Deutsch 2012; Figs 2 & 3)
- ✓ Global parameters (*i.e.*, spatially uniform)
  - ✓ HK\_HUF\_1D:  $K_h$  multiplier for lower part model
  - ✓ R\_BUILT\_AREA: built area recharge (% of meadow recharge)
  - ✓ R\_TOTAL: total recharge multiplier

### Spatially distributed parameters

- ✓  $K_h$  & VANI (vertical anisotropy)
- ✓ 41183 cells (each 5th grid cell; interpolated in between)
- ✓ Principal components are used for simulation, with hydraulic data as primary variable, and CPT and grain-size based K predictions as secondary variable
- ✓ Compared to reference model parameterization with homogeneous hydrogeological units

#### **Probabilistic optimization**

- ✓ AM for updating global model parameters, ISR for spatially distributed K
- ✓ We use a non-exact variant of rejection sampling known as interrupted Markov chain, where we only accept better performing candidates, and interrupt



Fig 3: Non-stationarity in the mean and primarysecondary data correlation along the stratigraphical succession..



Fig 4: Evolution of the log-likelihood in function of the number of iterations, for 50 interrupted Markov chains



## Conclusions

- Combination of AM and ISR proved to be effective for optimization of the non-stationary random fields
- More interrupted Markov chains should be run in order to get more robust posterior parameter distributions
- ✓ The random walk particle tracking code should be further optimized to reduce computation times

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the chain with probability  $\alpha = \exp(\log-likelihood) - target log-likelihood)$ 

#### Random walk particle tracking

- Preliminary results from a **basic implementation** based on LaBolle *et al.* (2000), assuming constant porosity and isotropic dispersion
- Relative dispersivity fields estimated from outcrop investigations (Rogiers *et al.* 2013) and CPT-based K variance (Rogiers 2013)
- ✓ 1500-m scale dispersivity in the reference model, 250-m scale for the updated model simulations, using dispersivity-scale dependency from literature (Rogiers 2013)

plots, histograms and correlations.



Fig 6: Mean and 95% confidence interval for the model ensemble head observations and vertical head differences (inset graph). The reference model values are shown in red triangles.