



# Bayesian inference of a dynamic vegetation model for grassland

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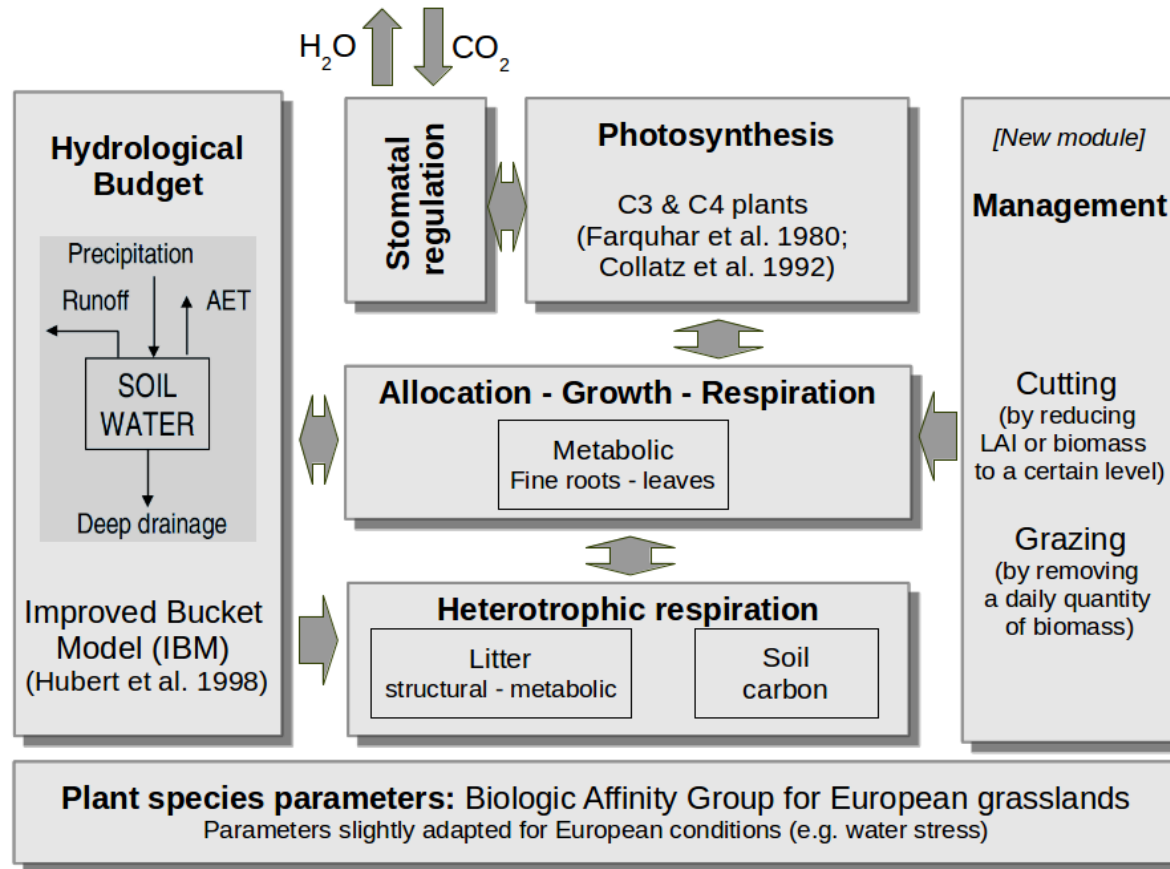


# Framework

- MACSUR task L2.4 Grassland model intercomparison, G. Bellocchi.
- Phase 1 : Blind runs (end in January 2014)
- Phase 2 : Calibrated runs (on-going) : how to calibrate ?

→ Calibration of a grassland model (CARAIB) by a Bayesian method

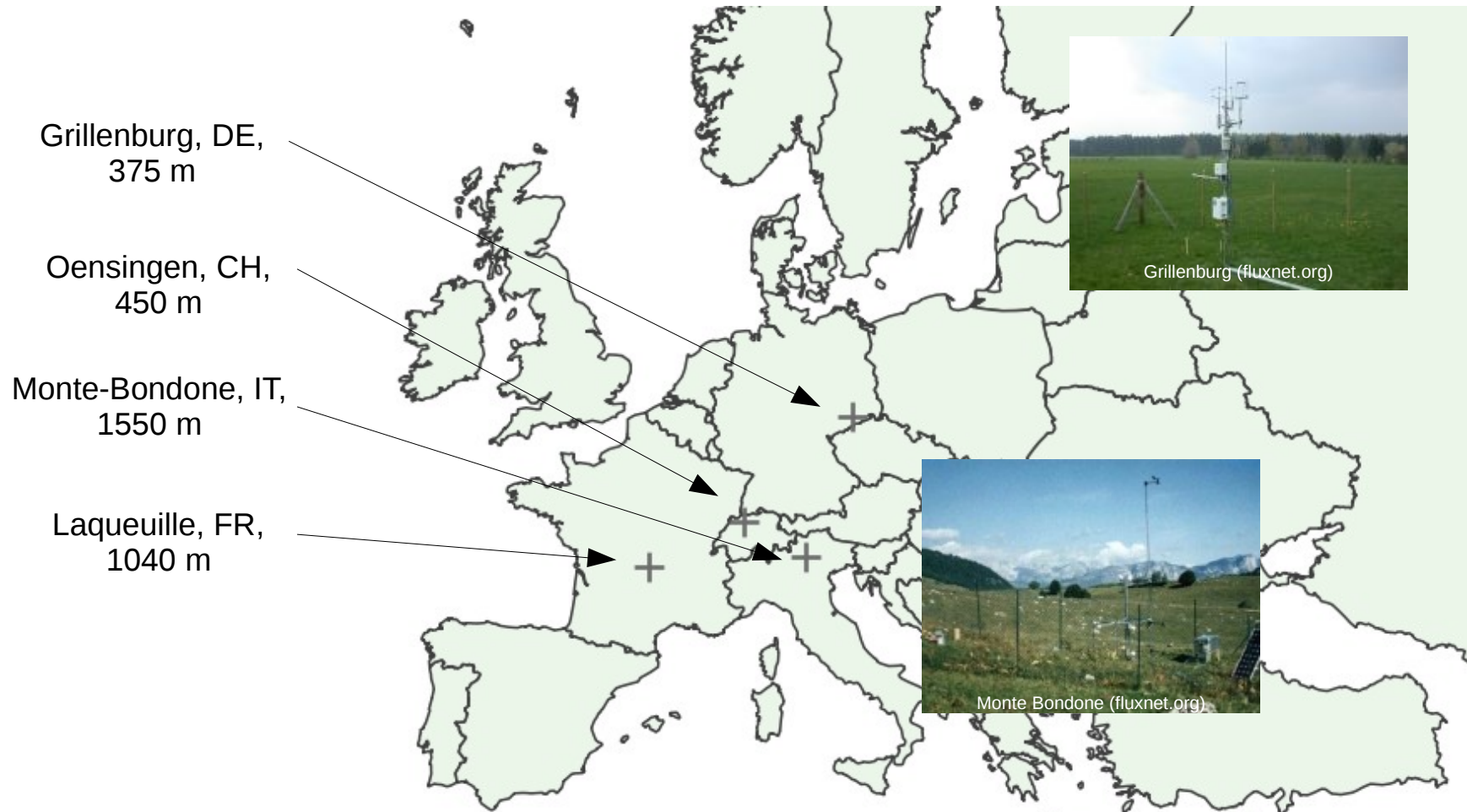
# The grassland model : CARAIB



- See talk of Louis François on Wednesday 3rd April
- Focused on grassland
- New management functions for grassland: cut & grazing

Reference website: [http://www.umccb.ulg.ac.be/Sci/m\\_car\\_e.html](http://www.umccb.ulg.ac.be/Sci/m_car_e.html)

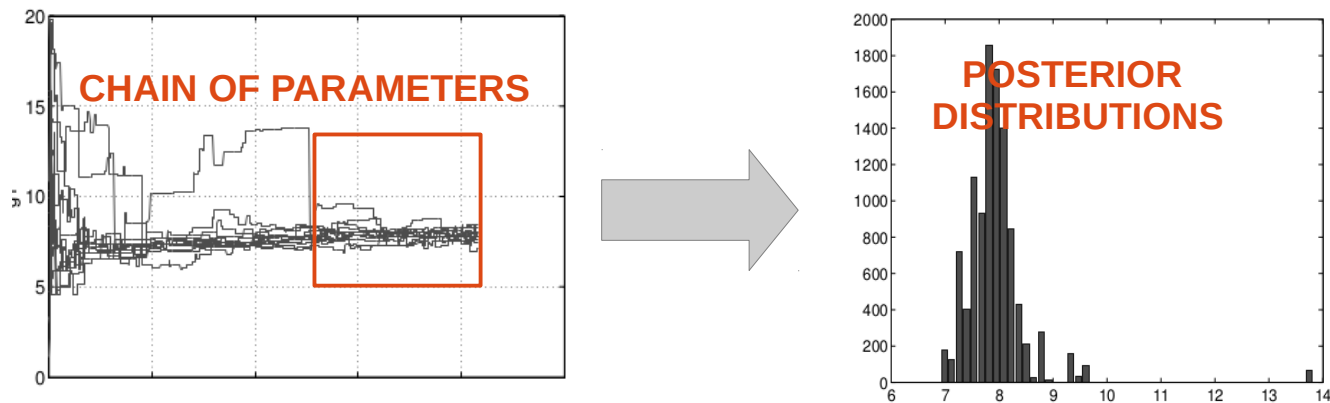
# The sites



- Semi-natural grasslands : grazed (Laqueuille) or cut (other 3)
- Eddy-covariance sites : flux measurements available : GPP, RECO, ET, ...

# The algorithm : DREAM\_ZS

- Inverse problem:  $Optimal\ parameters = argmin(Observations - Modeled(parameters))$
- DREAM\_ZS: a Markov-Chain Monte-Carlo sampler
- Ideal for sampling a large number of parameters
- Multiple-chain : deal with local minima and correlation between parameters.



Laloy, E., and J.A. Vrugt, *High-dimensional posterior exploration of hydrologic models using multiple-try DREAM\_(ZS) and high-performance computing*, *Water Resources Research*, 48, W01526, 2012

Vrugt, J.A., C.J.F. ter Braak, C.G.H. Diks, D. Higdon, B.A. Robinson, and J.M. Hyman, *Accelerating Markov chain Monte Carlo simulation by differential evolution with self-adaptive randomized subspace sampling*, *International Journal of Nonlinear Sciences and Numerical Simulation*, 10(3), 273-290, 2009.

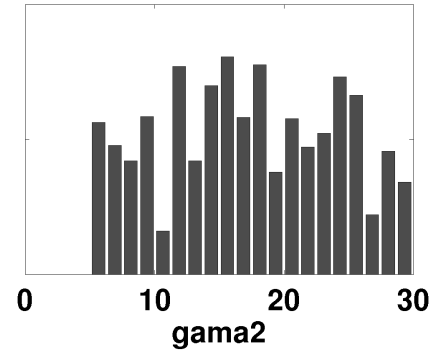
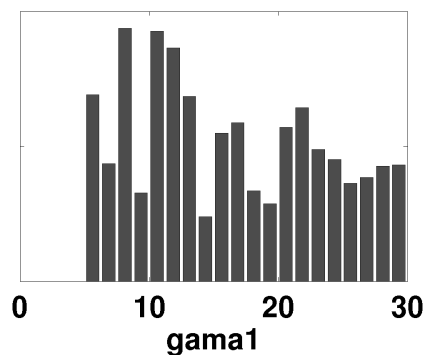
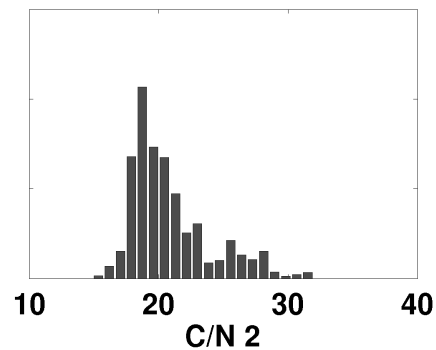
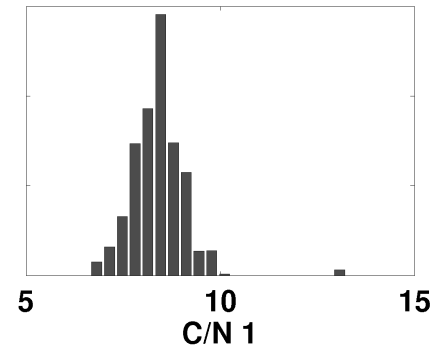
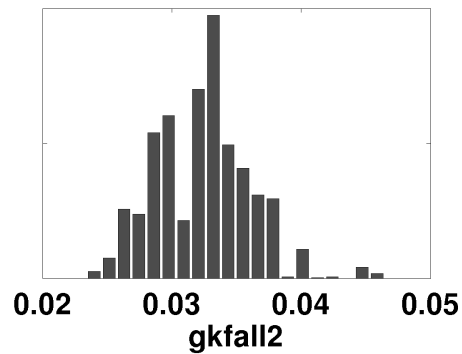
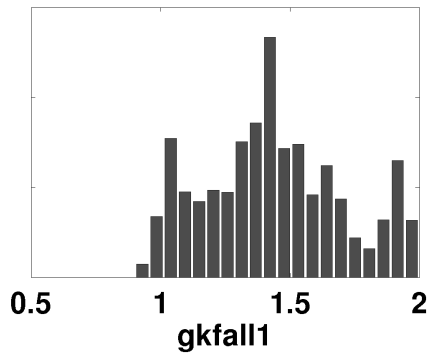
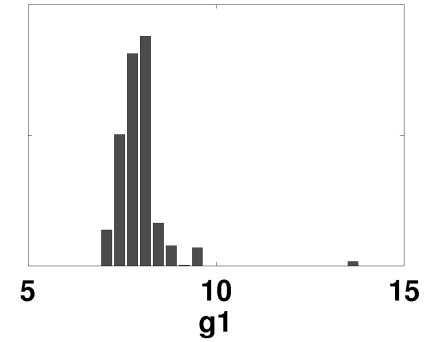
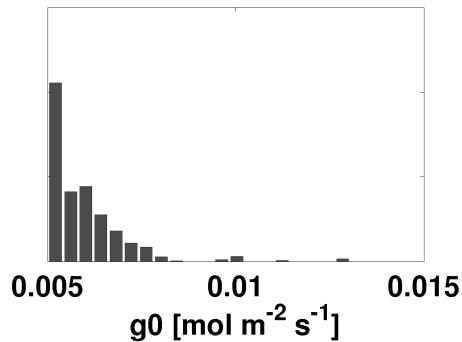
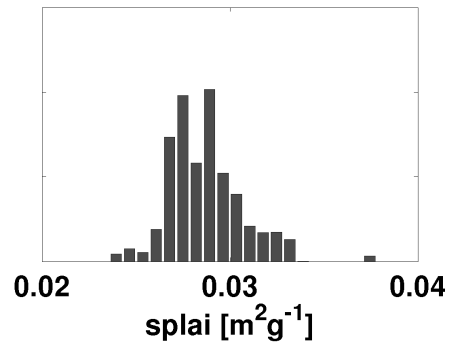
# The algorithm : DREAM\_ZS

- Inverse problem:  $Optimal\ parameters = argmin(Observations - Modeled(parameters))$
- 12 parameters were sampled using 3 measurements variables from Eddy covariance: RECO, GPP, ET
- A multi-objective cost function (CF) was used :  $CF = f(RECO, U_{RECO}, GPP, U_{GPP}, ET, U_{ET})$
- Uncertainties on measurement  $U$  were considered as follow (homoscedastic):

Meas. variables	U
RECO	1.5 gC m <sup>-2</sup> day <sup>-1</sup>
GPP	3 gC m <sup>-2</sup> day <sup>-1</sup>
ET	1 gC m <sup>-2</sup> day <sup>-1</sup>

# Results : parameter samplings

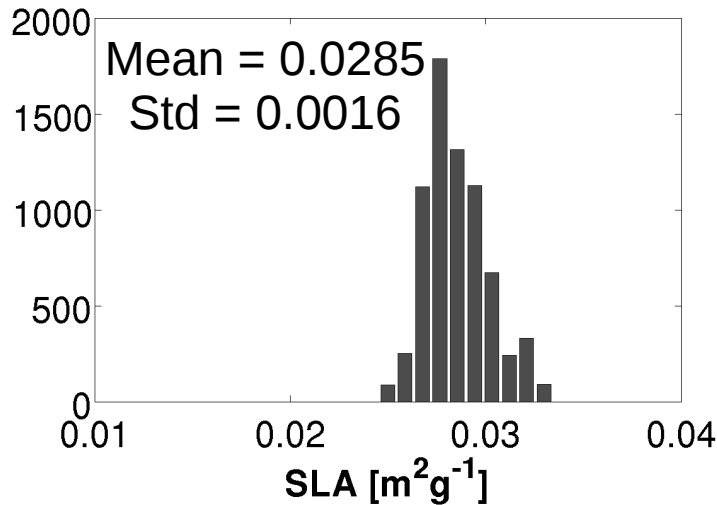
Posterior distributions of 9 parameters, Oensingen



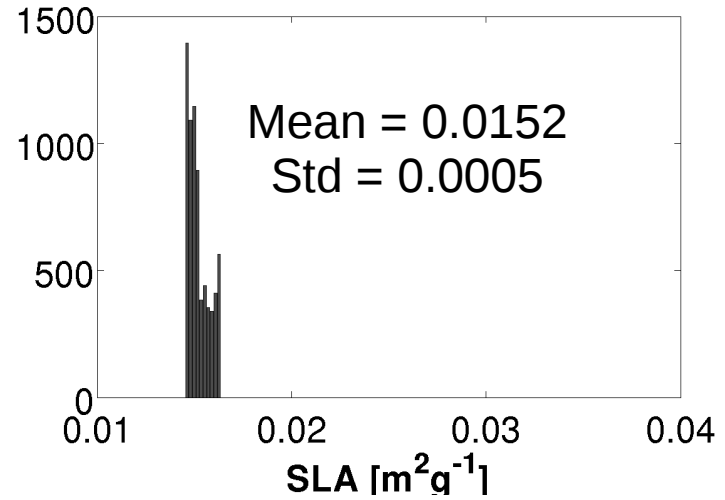
# Results : parameter samplings

## Specific leaf area (SLA) [ $\text{m}^2/\text{gC}$ ]

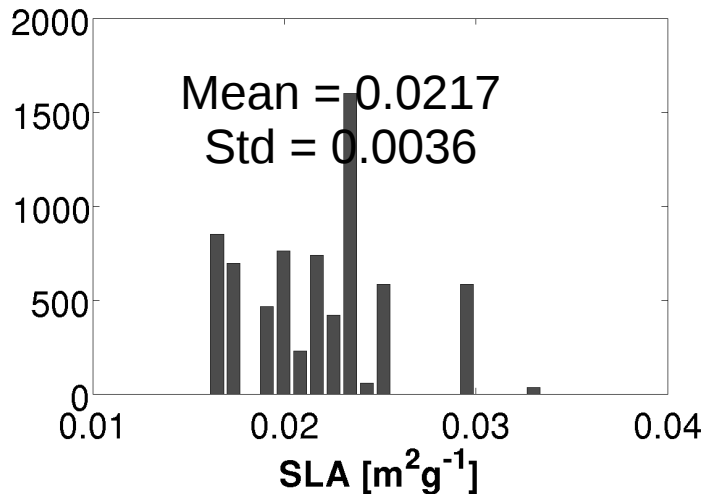
Oensingen



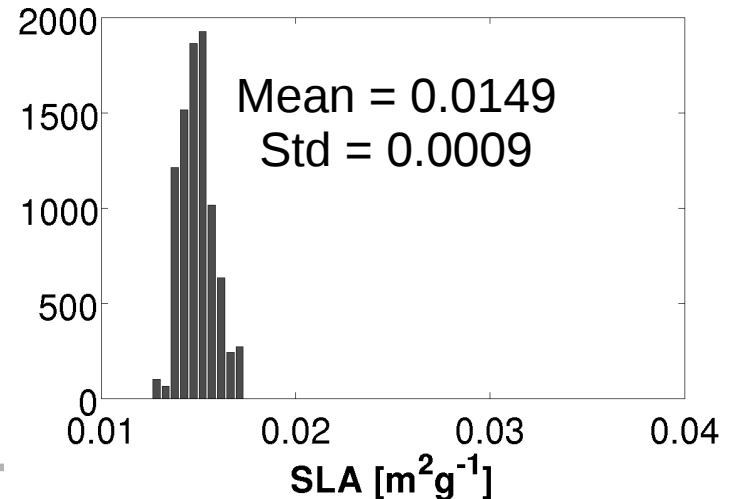
Grillenburg



Laqueuille



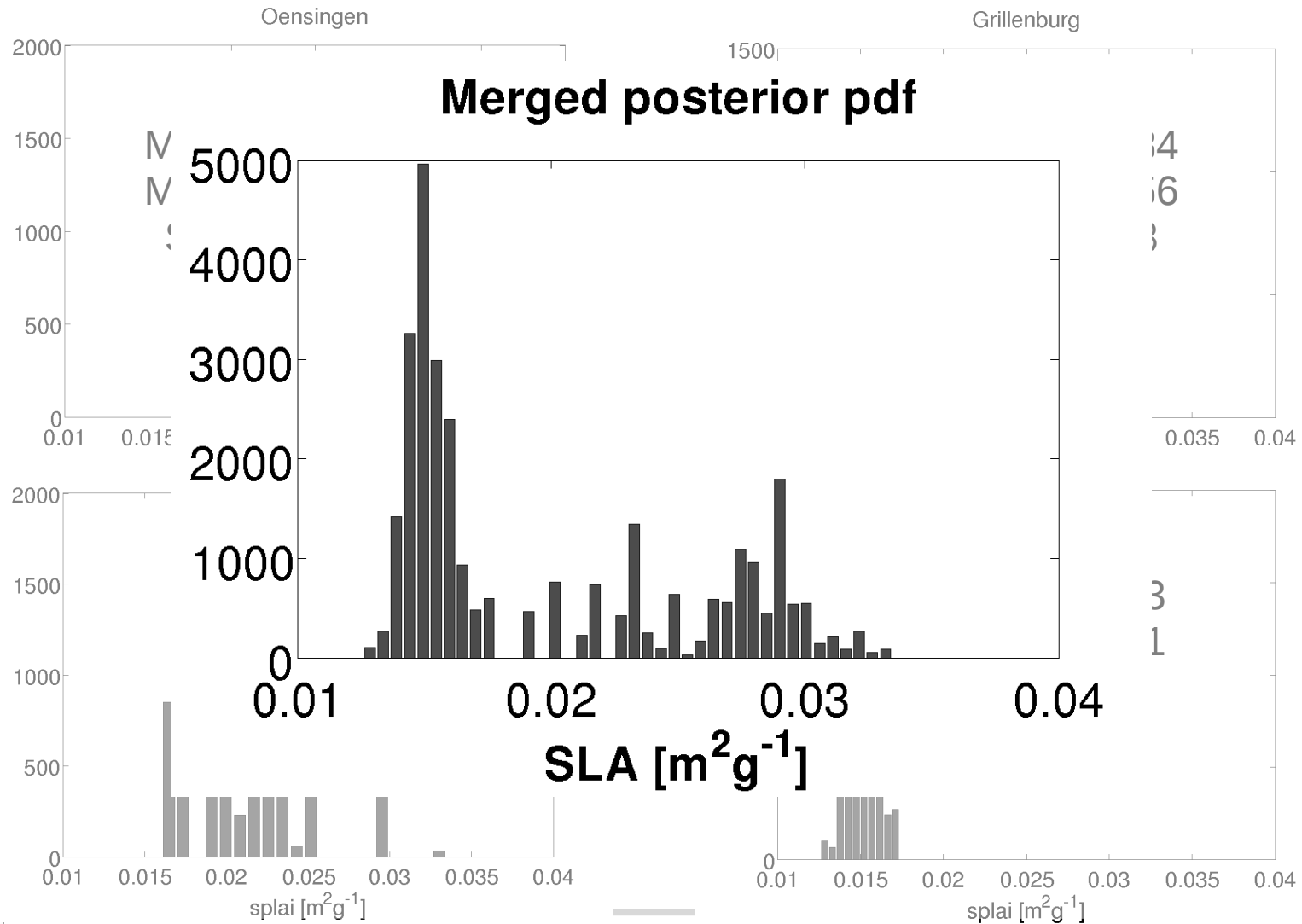
Monte-Bondone





# Results : parameter samplings

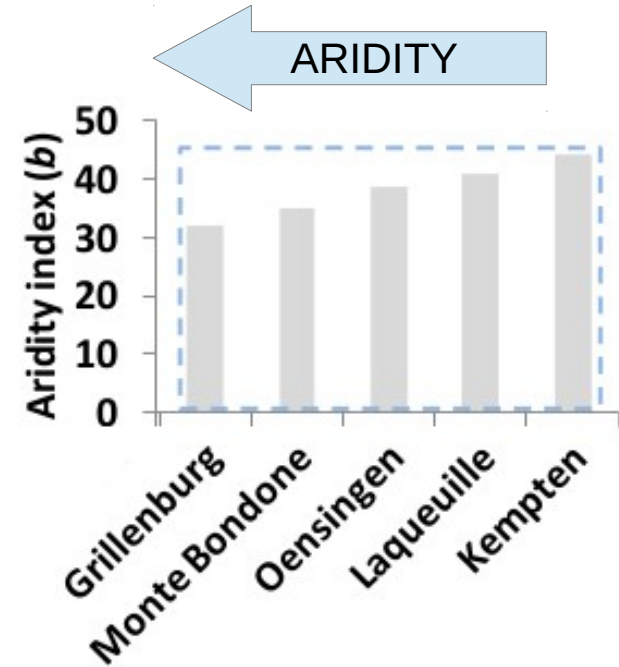
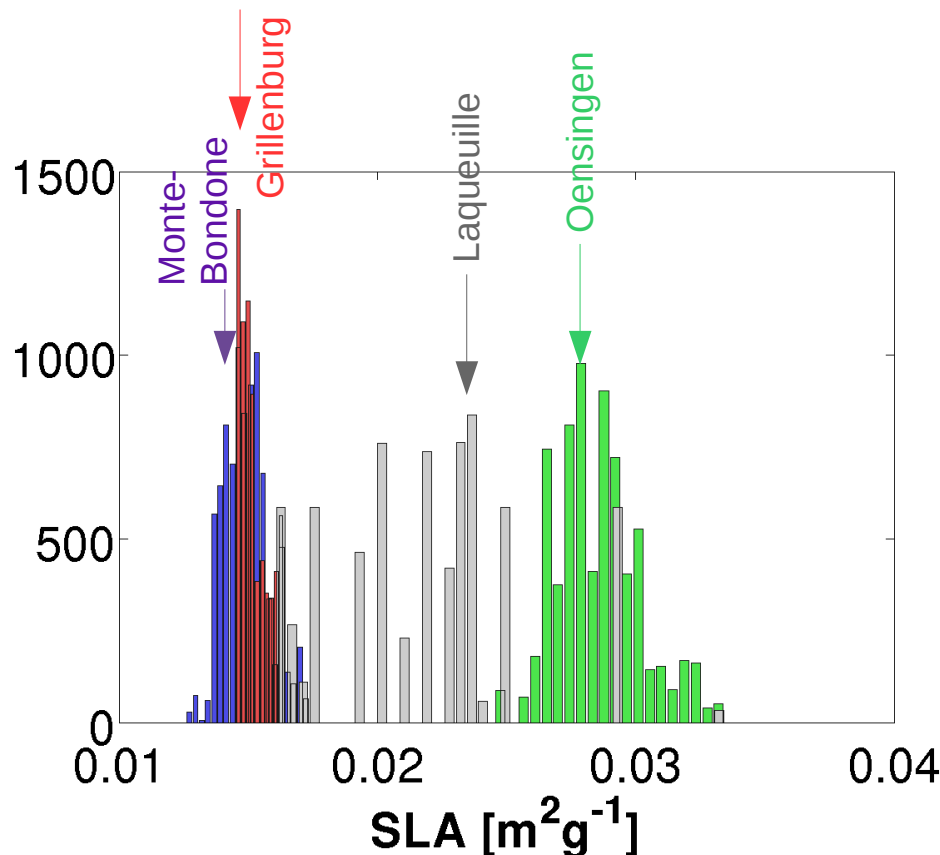
Specific leaf area [ $\text{m}^2/\text{gC}$ ]



# Results : parameter samplings

Specific leaf area (SLA) [ $\text{m}^2/\text{gC}$ ]

- SLA in CARAIB : *effective* SLA for a plant functional type !
- Actually, SLA is variable between leaves and along the season
- SLA is known to depend on aridity (-) and intensification (+)

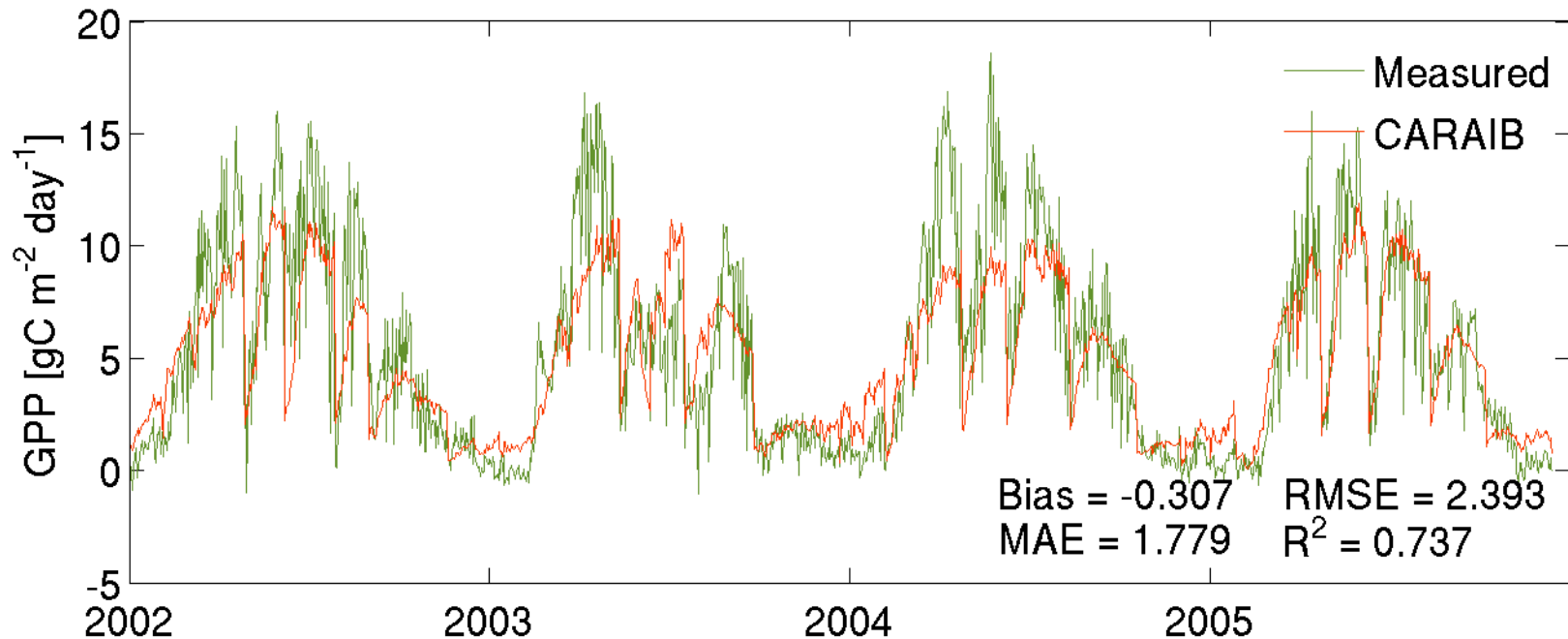


De Martonne-Gottmann aridity index  
from Ma et al. iEMSS, 2014

# Results : modeling improvement

## Oensingen, blind run

Measured VS modeled gross primary productivity (GPP), blind runs, Oensingen

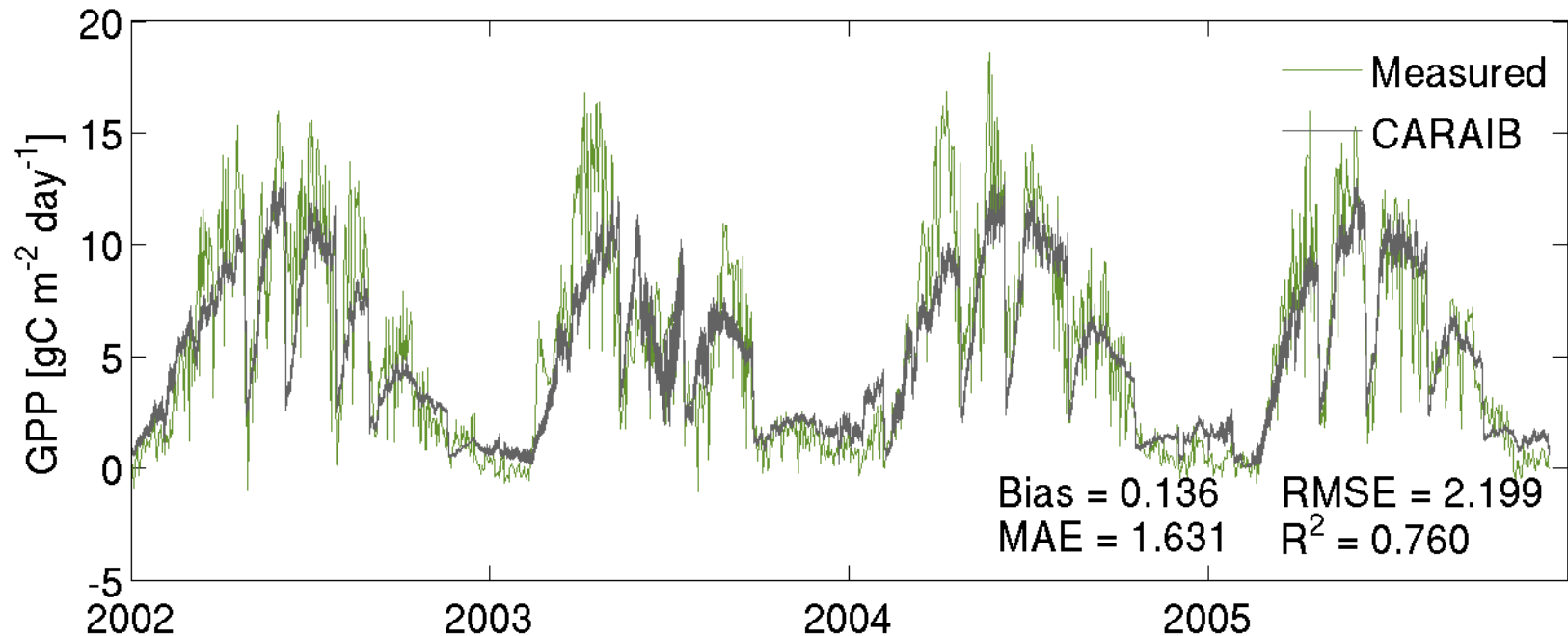


	Bias	RMSE	R <sup>2</sup>
NEE [gC m <sup>-2</sup> day <sup>-1</sup> ]	-0.513	2.034	0.487
GPP [gC m <sup>-2</sup> day <sup>-1</sup> ]	-0.307	2.392	0.737
RECO [gC m <sup>-2</sup> day <sup>-1</sup> ]	-0.820	1.615	0.805
ET [mm day <sup>-1</sup> ]	-0.107	0.910	0.549

# Results : modeling improvement

Oensingen, after calibration (1000's of model outputs)

Measured VS modeled gross primary productivity (GPP), after calibration, Oensingen



	Bias	RMSE	R <sup>2</sup>
NEE [gC m <sup>-2</sup> day <sup>-1</sup> ]	-0.013	1.991	0.477
GPP [gC m <sup>-2</sup> day <sup>-1</sup> ]	0.136	2.199	0.760
RECO [gC m <sup>-2</sup> day <sup>-1</sup> ]	0.123	1.260	0.808
ET [mm day <sup>-1</sup> ]	-0.020	0.675	0.751

# Conclusion

## Bayesian sampling with DREAM\_ZS :

- Obtain a uncertainty assessment on model parameters
- Obtain an interval on model output due to parameters uncertainties
- Assess model sensitivity to its parameters

## Future work :

- Interact with other modelers teams and intercompare...

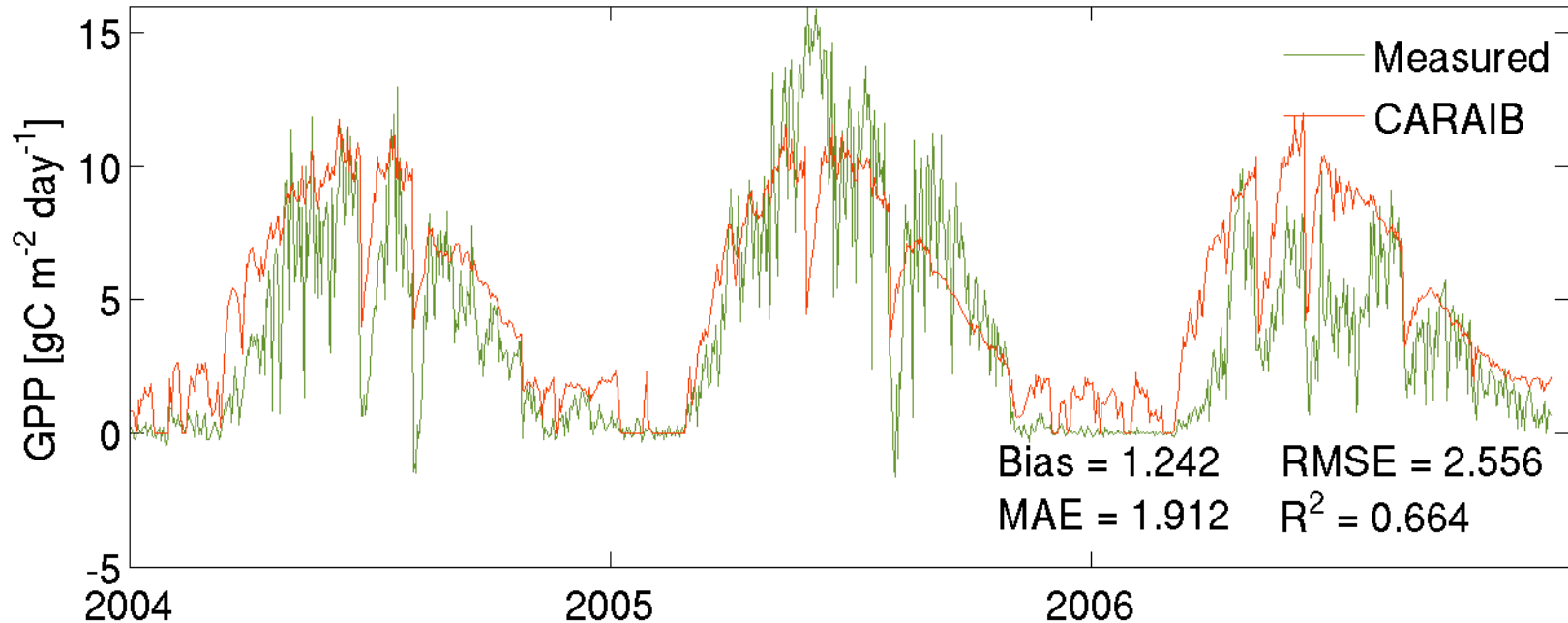
# Thanks for your attention



# Results : modeling improvement

Grillenburg, blind run:

Measured VS modeled gross primary productivity (GPP), blind run, Grillenburg



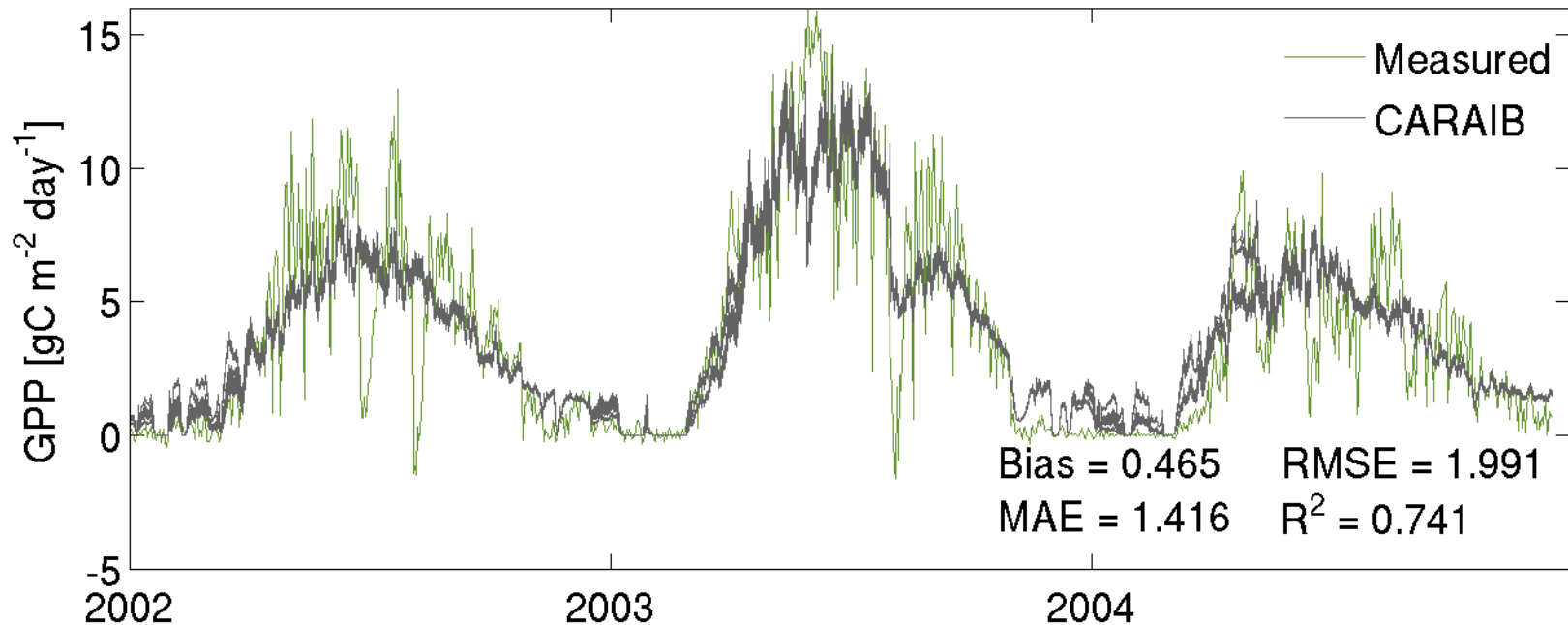
	Bias	RMSE	R <sup>2</sup>
NEE [gC m <sup>-2</sup> day <sup>-1</sup> ]	-0.715	1.901	0.343
GPP [gC m <sup>-2</sup> day <sup>-1</sup> ]	1.242	2.556	0.664
RECO [gC m <sup>-2</sup> day <sup>-1</sup> ]	0.238	0.728	0.498
ET [mm day <sup>-1</sup> ]	0.526	1.879	0.555



# Results : modeling improvement

Grillenburg, after calibration (1000's of modeled GPP):

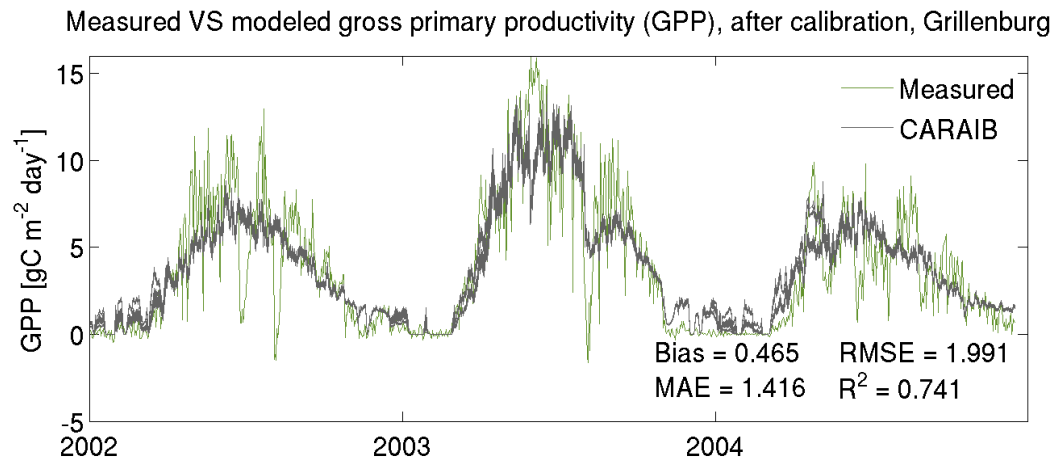
Measured VS modeled gross primary productivity (GPP), after calibration, Grillenburg



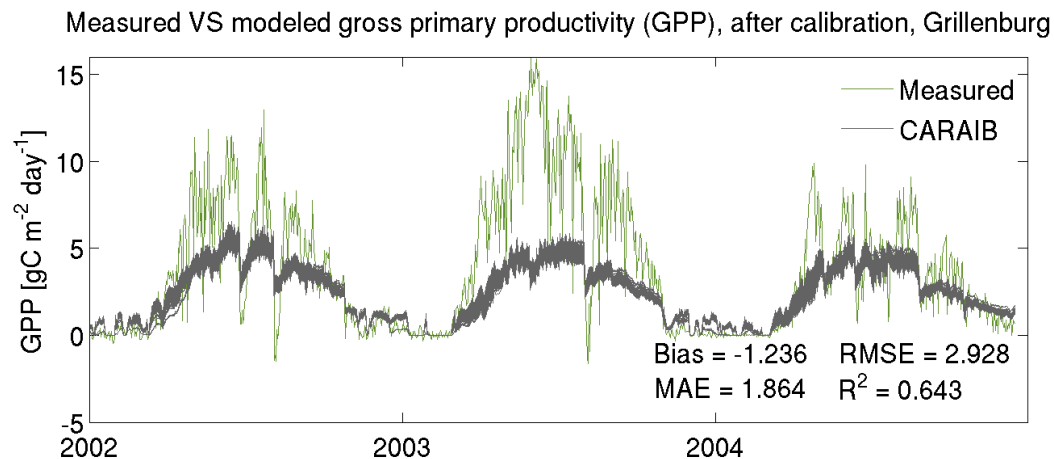
	Bias	RMSE	$R^2$
NEE [ $\text{gC m}^{-2} \text{ day}^{-1}$ ]	-0.340	1.898	0.477
GPP [ $\text{gC m}^{-2} \text{ day}^{-1}$ ]	0.465	1.991	0.741
RECO [ $\text{gC m}^{-2} \text{ day}^{-1}$ ]	0.125	1.596	0.660
ET [ $\text{mm day}^{-1}$ ]	0.100	0.616	0.584

# Results : Error in measurements

Homoscedastic :



Heteroscedastic :



# The algorithm : DREAM\_ZS

- Inverse problem:  $Optimal\ parameters = argmin(Observations - Modeled(parameters))$
- 12 parameters were sampled using 3 measurements variables: RECO, GPP, ET
- A multi-objective cost function (CF) was used :  $CF = f(RECO, U_{RECO}, GPP, U_{GPP}, ET, U_{ET})$
- Uncertainties on measurement  $U$  were considered as homoscedastic or heteroscedastic (i.e., constant or variable):

→ HOMOSCEDASTIC:

$$U = U_0$$

→ HETEROSCEDASTIC:

$$U = \frac{U_0}{2} + \frac{U_0}{2\bar{X}} * X$$

Where  $U_0$  is a user-defined uncertainty for each variable  $X$ :

X	$U_0$
RECO	1.5 gC m <sup>-2</sup> day <sup>-1</sup>
GPP	3 gC m <sup>-2</sup> day <sup>-1</sup>
ET	1 gC m <sup>-2</sup> day <sup>-1</sup>