

**Particle size distribution of limestone fillers: granulometry and specific
surface area investigations**

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Abstract

Mineral fillers can be defined as “inert materials included in a mix design for some useful purpose”. They can be added to compounds in order to complete a large variety of final properties without increasing costs or to improve specific characteristics like hardness, brittleness, impact strength, compressive strength, softening point, fire resistance, surface texture, electrical conductivity, ...etc. In Belgium, locally available limestone fillers are specifically very well-adapted for the optimisation of particle packing and flow behaviour of cementitious pastes in concrete mixes.

Limestone fillers may be easily characterized in terms of chemical and mineralogical properties. These properties are fundamental for the study of the behaviour of concrete mixes in fresh state and for understanding interactions existing at the level of the Interfacial Transition Zone between aggregates and cement paste.

These properties are however insufficiently discriminant and particle size, as well as shape distribution, seem to have a potential influence on physical phenomena which happen during the setting process.

The aim of this paper is to compare five major techniques used to quantify the size and the shape of limestone fillers particles: laser diffraction scattering, wet sieving and image analysis for particle size measurement and BET adsorption and Blaine permeability methods for specific surface area.

Keywords: Limestone fillers, particle size distribution, specific surface area, image analysis, BET adsorption, Blaine.

1. Introduction

Limestone fillers are largely used in the concrete industry, especially for Self Compacting Concrete mix design (Ghezal et al. 2002; Ho et al. 2002). Besides heterogeneous nucleation effect leading to a chemical activation of the cement hydration, it is now generally accepted that the main effect of the limestone powder is of physical nature (Tsvivilis et al. 1999). In addition to cement, limestone particles modify the grain size distribution. The final effect depends on the fineness and the amount of powder. In the favourable case where an improvement in blended particles size distribution is observed, i.e. a continuous sieving curve, limestone particles fill the voids between clinker particles and improve the packing density of the granular skeleton; this consequently densifies the microstructure of the hardened cement paste (Sprung et Siebel 1991). The correlative effects are lower water retention and, subsequently, lower water demand for specific workability. This suggests that particle size distribution has a considerable influence on the water demand of paste. Moreover, the shape of fine particles was reported as having a significant effect on water demand (Wills 1967; Ferraris et al. 2001).

Relationship between physical characteristics of particles and water requirement is not so evident and clearly demonstrated (Courard et al. 2011). The reason is partially due to the test needed for characterizing these physical parameters (Diederich et al. 2013). The purpose of this article is to review different techniques for analysing size and shape of micrometric particles such as limestone fillers. Particle size measurement has been studied by means of laser light scattering, wet sieving (45, 63 and 125 μm) and static image analysis. This last technique enables also to characterize the shape of particles. BET adsorption and Blaine permeability methods were also used to determine specific surface area of fillers.

2. Materials and methodology

2.1 Powders

Six limestone fillers, labelled F1 to F6 [8], have been collected in Belgium (Wallonia region). They differ from each other by production process (Table 1).

Table 1. Origin and production process of limestone fillers.

Limestone fillers	Production process	Industrial Sector
F1	Dry	Crushing Lime
F2		
F3	Drying / crushing	Aggregates
F4	Wet	Sawing Ornamental stones
F5		
F6	Washing	Aggregates

Residual fillers coming from lime kiln feed (F1, F2) and sawing of ornamental stones (F4) present a very high CaCO_3 content whereas large amounts of impurities are observed in the case of fillers produced in limestone quarries (15% of quartz for F3 and 23% of dolomite for F6) (Table 2). Moreover, Al_2O_3 and alkalis (Na_2O and K_2O) contents indicate a contamination by clay for fillers coming from aggregate production industry (Courard et al. 2011). This is confirmed by Methylene Blue Adsorption results (Meerseman et al. 2006; Michel et al. 2007).

Table 2. Mineralogical and chemical characterization of limestone fillers.

Limestone filler reference	F1	F2	F3	F4	F5	F6
<i>Mineralogical analysis by DRX (main phases)[7]</i>						
Calcite CaCO ₃ [%]	99.5	99.5	82.0	94.5	86.0	75.0
Quartz SiO ₂ [%]	0.0	0.0	<u>15.5</u>	1.8	6.5	2.0
Dolomite Ca(Mg,Fe)(CO ₃) ₂ [%]	0.5	0.5	2.5	3.7	7.5	<u>23.0</u>
<i>Chemical analysis (minor components)</i>						
Al ₂ O ₃ [%]	0.15	0.07	<u>2.38</u>	0.63	<u>4.45</u>	<u>1.38</u>
Na ₂ O [%]	0.07	0.03	0.33	0.27	0.10	0.06
K ₂ O [%]	0.03	0.02	0.61	0.11	1.02	0.28
Fe ₂ O ₃ [%]	0.15	0.04	0.90	0.33	1.71	0.82
Methylene Blue Adsorption [g/kg filler]	0.7	0.7	4.0	1.3	5.0	3.3

2.2. Laser diffraction (LD)

Laser diffraction is based on a complex theory of interaction between monochromatic light and individual particles. This involves the detection of the angular distribution of light scattered by a set of monodispersed spherical particles to provide a “sphere”-equivalent size diameter distribution using a reverse optical scattering-based model calculation (Fig.1).

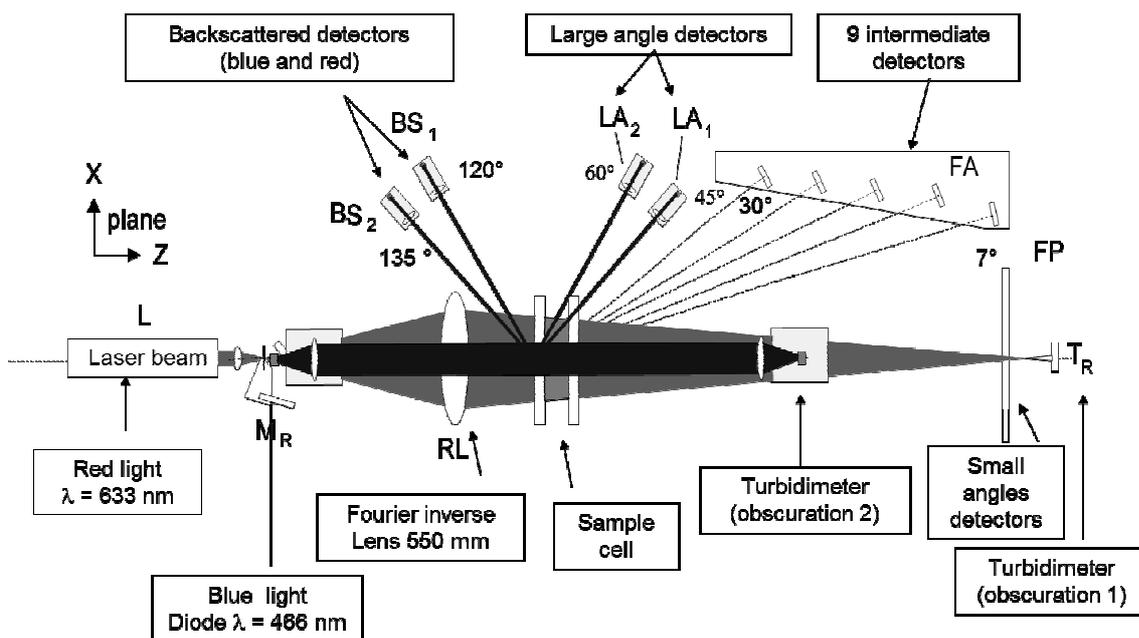


Fig. 1. Principles of Laser Diffraction

Two models are commonly used to build Particle Size Distribution (PSD-V) weighted by apparent volume (volume of equivalent sphere of diameter d). The Mie theory-based model predicts scattering of light by homogeneous sphere of arbitrary size; it is probably the most rigorous model available (Mie 1908). It requires, as input, the refractive index (both real n and imaginary k) of both the particle and the medium. In another hand, Fraunhofer approximation considers particles as opaque disks and, consequently, does not require any knowledge of the material's optical properties. This assumption is fairly acceptable when the particle scattering the incident light is significantly larger than the incident wavelength, with a refractive index significantly different from the surrounding medium. The bounding conditions for which the Fraunhofer diffraction theory adequately describes the scattering phenomena were given by Van der Hulst (Van der Hulst 1957). Cyr (Cyr 1991) calculated these boundaries conditions in the case of typical building materials and found particle critical diameters ranged from 8 to 18 μm depending on optical properties of materials and dispersant used.

Limestone fillers are mainly composed of fine divided particles ($< 20\mu\text{m}$). Mie theory (Mie 1938) is therefore more adequate to deconvolve the diffraction pattern. However, although the samples studied are not fully pure, CaCO_3 mineral is strongly birefringent (refractive indices ranging from 1.48 to 1.66) and makes very difficult the selection of representative refractive index average. Fig.2 and Table 3 illustrate how the change of refractive index value can lead to different particle size distributions mainly in the range of submicron particles (for $k = 0.1$). It can be observed how Fraunhofer approximation disregards the very weak scattering for thin particles, taking into consideration the constancy of the extinction efficiency, whatever the particle's size: it fails to report any quantity of particles below $0.45 \mu\text{m}$ (Fig.2). For the purpose of this research, Fraunhofer and Mie theories were both considered in order to compare the PSD. In the case of Mie, a refractive index of 1.57 was selected according to specification of

the manufacturer. For each sample, six potential values of absorption indices (0 – 0.01 – 0.05 – 0.1 – 0.15 – 0.20) were computed. The one which gave the best match between real and calculated angular distribution of light – it means the lowest weighted residual - was then selected.

Wet dispersion measurements were performed using a Mastersizer 2000 instrument coupled to a Hydro 2000S wet dispersion unit (Malvern, UK). Through a series of experiments, the optimum operating conditions for dispersion were selected (Michel 2006). Limestone particles were dispersed in a sodium pyrophosphate solution. Afterwards, the samples were transferred to dispersion unit that contains deionized water and subjected to 90 seconds of ultrasonic waves. The concentration of solid in the dispersion unit is selected in order to allow scattering but limiting multiple scattering (15% of obscuration rate). Laser diffraction is repeated three times on each filler sample.

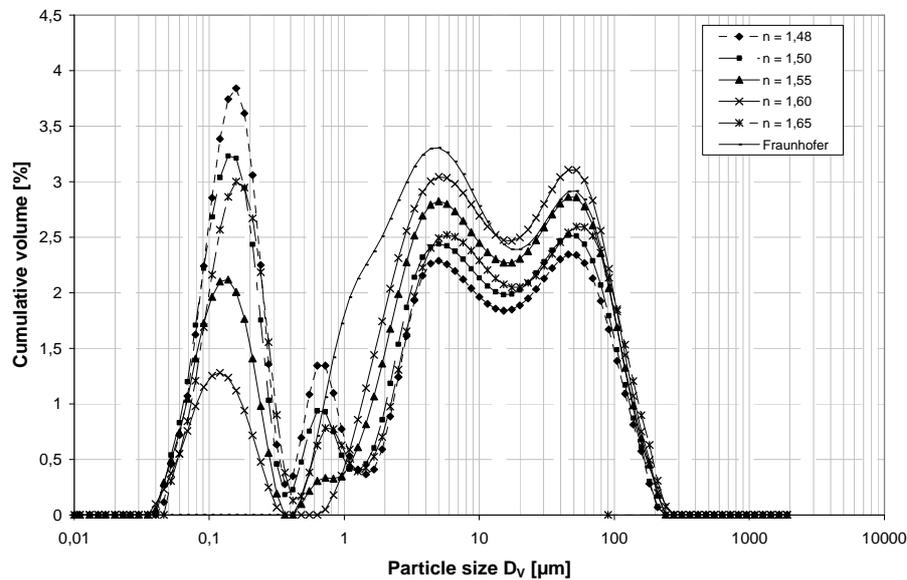


Fig. 2. Influence of the value of the refractive index on the PSD of limestone filler F1 (for $k=0.1$).

Table 3. Volume weighted percentiles D_x^v [μm] of the size distribution obtained from laser diffraction of limestone filler for different refractive indices

	Refractive index					Fraunhofer
	1.48	1.5	1.55	1.6	1.65	
D_5^v	0.1	0.1	0.1	0.1	1.5	0.9
D_{10}^v	0.1	0.1	0.1	0.2	2.1	1.3
D_{50}^v	4.3	5.3	7.7	9.6	12.6	8.5
D_{90}^v	60.0	6.2	68.2	71.2	75.2	68.5
D_{95}^v	85.7	94	93.8	97.0	100.8	100.8

2.2. Static Image Analysis (SIA)

Static image analysis has been performed by means of the Occhio 500 Nano image analyser. This instrument includes an integrated vacuum dispersion system and a high-quality optical component which allows assessing size and shape of a set of dispersed particles. Few milligrams of particles are dispersed onto a circular glass slide which is moved in front of a collimated violet LED backlighting. Pictures of individual particles are captured with a 1392*1040 pixels video camera fitted with a telecentric lens of 480nm resolution. The inscribed disk diameter (D_{IN}) of each particle is calculated in real time to build size distribution curves weighted by apparent volume (PSD-V') (Gregoire et al. 2007), making the assumption that particles have identical flatness ratios, whatever their size.

Particle image acquisition method proceeds by scanning the first 50000 particles, ensuring that particles are scanned at least once on the whole diameter of the glass slice: this is needed in order to avoid any deviation due to heterogeneous dispersion of the particles. Two scans have been conducted for a total of 100000 particles. The accuracy associated to the estimation of PSD-V, expressed as the two-sided 95% confidence interval, is computed by means of the

bootstrap method (Gregoire et al. 2007; Michel et al. 2007). In practice, 500 bootstrap samples of 10000 particles are used to build confidence interval.

2.3. Sieving

Sieving is a reference simple method for the classification of powders with regards only to their physical but real size. It can be performed either in a dry or a wet way, with manual or mechanical vibration, and for fixed duration or until a sufficiently low powder flow rate is observed through the sieves. It is however limited by physical dimensions of the sieve, i.e. usually 45µm.

2.4. Blaine Permeability

The Blaine fineness tester is used for the measurement of the specific surface area of particles on the base of air permeability method: the time t necessary for a volume of air to flow through a packed bed of particles is recorded. The European Standard EN 196-6 gives the evaluation of specific surface area (Carman 1956) with Kozeny-Carman equation (Eq.1):

$$S_{S,koz} = K_{app} \frac{\varepsilon^{3/2}}{\rho_s (1 - \varepsilon)} \frac{t^{1/2}}{(0,1\eta)^{1/2}} \quad (1)$$

where ε is the porosity of the packed bed of powder, η is the viscosity of air [Pa.s] and ρ_s the density of the solid [g.cm⁻³]. The constant K_{app} [g^{1/2}.cm^{3/2}.s⁻¹], which is a characteristic of the apparatus, is determined with a calibration cement powder linked up to a standard reference material. Assuming that the air is compressible (Michel 2006), the Kozeny-Carman equation can be used to give a more accurate relationship for the apparatus constant (Eq.2).

$$K_{app} = 10^{-2} \sqrt{\frac{0,1\rho_L D_{cell}}{kC_{air} D_{tube} L_{sample}}} \quad (2)$$

where ρ_L is the density of the manometer fluid, D_{cell} and D_{tube} are the inner diameter of the cell and of the tube [cm], respectively, k is the Kozeny constant, L_{sample} is the height of the packed bed of powder [cm]. C_{air} is a term which takes into account air compressibility due to pressure drop between the opposite sides of the sample; it depends on atmospheric pressure and geometrical characteristics of the instrument (Niesel 1973). Kozeny constant is related to the shape of particles and the bed tortuosity. Eq.2 clearly points out that the apparatus constant depends on several parameters including hygrometric conditions but also the height of packed bed of particles: these should be selected in accordance with operational conditions, in order to avoid serious misinterpretation. That's the reason why we propose to calculate Kozeny constant k linked up to a standard reference material and to measure L_{sample} and C_{air} for each new test.

2.6. *B.E.T. Nitrogen Absorption*

The determination of the specific surface by means of the B.E.T. theory is based on the physical adsorption of gases on the total surface of a porous material, which means outside as well as inside surfaces. The surface area is obtained from Eq.3 (Brunhauer 1938):

$$\frac{P}{v(P - P_0)} = \frac{c - 1}{v_m c} \frac{P}{P_0} + \frac{1}{v_m c} \quad (3)$$

where v is the adsorbed volume of nitrogen at a given pressure P , P_0 is the saturation pressure, v_m is the volume corresponding to a monolayer of N_2 on the surface and c is related to the heat of adsorption in the first and subsequent adsorbed layers. When equalling these quantities to the experimental slope and intercept of the straight line, one obtains two equations which may be solved for v_m . From this value and knowing the cross sectional area σ of the adsorbed molecule, the specific surface area of the absorbent may be calculated directly with Eq.4.

$$S_{S,BET} = \sigma \frac{v_m \cdot N}{V} \quad (4)$$

3. Results and discussion

3.1. Granulometry analysis

The volume weighted percentiles $D_{10}^V, D_{50}^V, D_{90}^V$ of limestone fillers performed by laser diffraction (LD) and static image analysis (SIA) are reported on Table 1; D_{MAX}^V is corresponding to the biggest particle. In case of SIA, examination of dataset shows how a very few particles with superior extreme values greatly affect statistics.

For this reason, besides a first analysis based on raw data, a second analysis was conducted on numerical filtered dataset to better visualize the size distribution of the remaining particles. It consists in considering the 5 biggest particles of each samples as statistical outliers and, consequently, removing them from the dataset. Moreover, Fig. 3 shows how the confidence interval gets appreciably narrower after filtration. In the case of LD, both Fraunhofer and Mie theories seem to lead to reasonably similar size distributions.

Table 1. Volume weighted Xth percentiles of the diameter of limestone filler obtained from Mie and Fraunhofer models.

		Model	F1	F2	F3	F4	F5	F6
D_{10}^V	LD	Fraunhofer	1.5	1.2	1.2	1.2	1.4	1.7
		Mie	1.7	1.3	1.1	1.2	1.5	1.8
[μm]	SIA	Raw	6.4	4.8	4.4	4.2	4.2	5.0
		Filtered	6.4	4.8	4.4	4.2	4.2	5.0
D_{50}^V	LD	Fraunhofer	13.8	9.4	8.8	7.2	9.2	14.5
		Mie	16.5	10.8	10.3	8.0	9.9	15.8

[μm]	SIA	Raw	20.6	11.0	11.8	9.5	10.5	13.0
		Filtered	19.0	8.9	11.4	9.5	10.2	12.2
D_{90}^V	LD	Fraunhofer	73.1	68.7	50.8	47.4	47.8	101.8
		Mie	73.4	67.1	50.1	45.0	47.6	107.7
[μm]	SIA	Raw	62.5	34.5	33.8	24.0	32.4	43.6
		Filtered	50.9	27.4	28.4	22.1	28.6	34.9
D_{MAX}^V [μm]	SIA	Raw	107.4	82.1	61.7	47.2	58.7	107.9
		Filtered	71.8	47.5	46.8	35.6	44.7	51.7

Fig. 3 illustrates the typical discrepancy existing between SIA and LD. It clearly shows that LD extends the size distribution towards both the lower and upper sizes. In the case of lower size, one could argue that SIA is unable to take into account particles smaller than 3 pixels in width (1.44 μm). However, the pendant question is to know if this argument may explain the whole discrepancy. In order to shift the size distributions towards lower values and try to correlate SIA with LD, enormous amounts (> 90% by number) of very fine material are needed (Brunhauer 1938). On the other hand, even if the whole dataset is used for static image analysis, results demonstrate that LD extends the size distribution towards the upper sizes. The presence of 63 – 125 μm particles observed in the case of LD analysis is confirmed by wet sieving (Table 5). We can then partially explain the absence of big particles by the probability of inclusion of a particle within the image frame: only particles fitting entirely within the image frame are indeed considered for measurement. That means that, the bigger the particle, the higher the probability to have contact with the frame: consequently, the “risk” to be excluded from the analysis really exists. However, this phenomenon is not so important for particles between 80 and 125 μm .

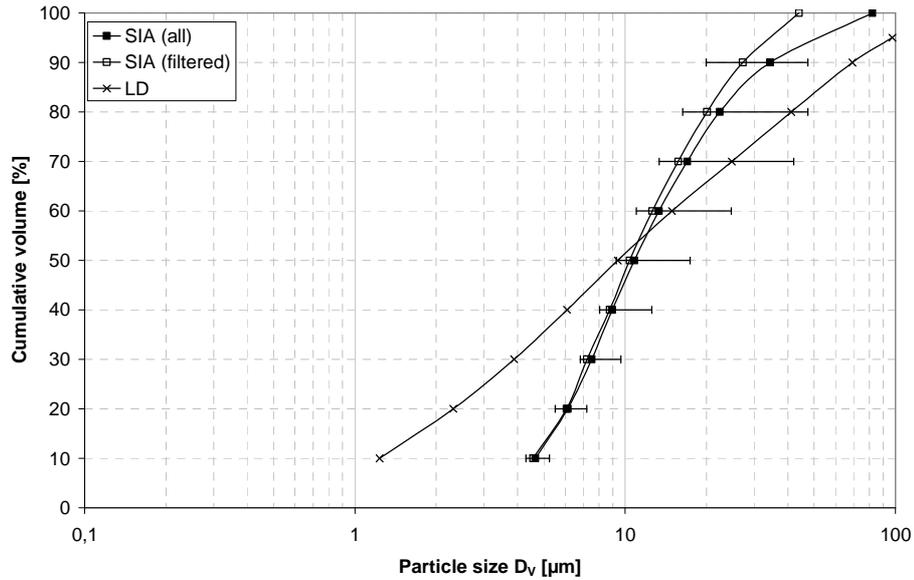


Fig. 3. Cumulative size distributions obtained for limestone filler F1 from LD (Mie model) and SIA.

Table 5. Cumulative average particle weight (%) of limestone fillers for wet sieving.

Passing sieve size	F1	F2	F3	F4	F5	F6
45 µm	78.1	80.6	90.6	89.4	73.5	69.6
63 µm	85.9	87.1	95.6	92.3	81.2	76.8
125 µm	99.6	97.6	99.9	95.4	95.9	88.9

The comparison between 45 and 63 µm passing sieve particles, obtained by the three different methods, is illustrated in Fig. 4 and Fig. 5; considering that all the particles have the same density, volume V_V is equal to weight W_W . It can be observed that the 45µm and 63µm passing sieve obtained by LD and wet sieving techniques are similar, except in the case of sample F5.

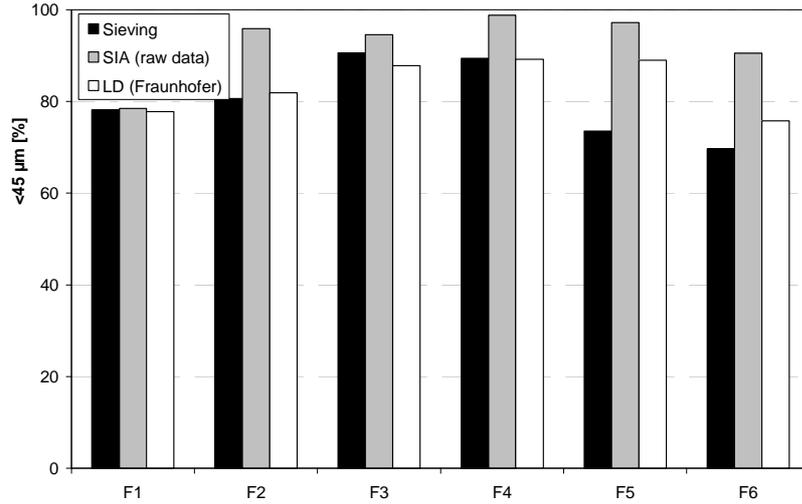


Fig. 4. Comparison of 45 μm passing sieve particles obtained with LD, SIA and wet sieving techniques.

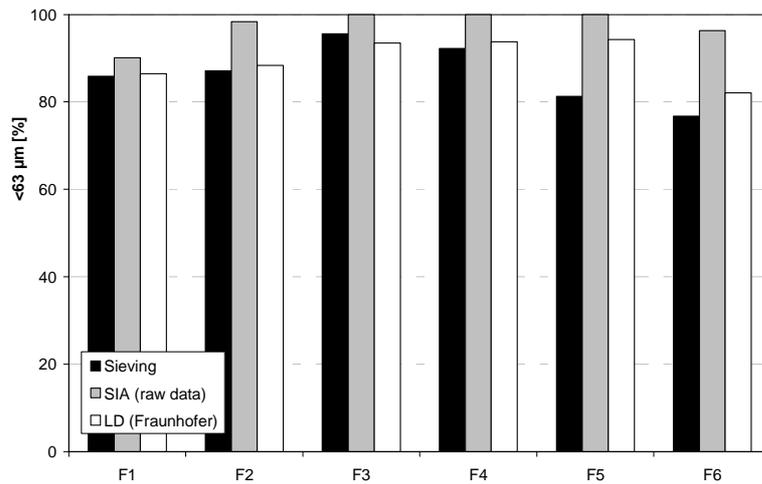


Fig. 5. Comparison of 63 μm passing sieve particles obtained with LD, SIA and wet sieving techniques.

3.2. Specific surface area

Three samples of each type of filler have been analysed and Table 6 presents the results of specific surface area (SSA) obtained from N₂ adsorption isotherms and air permeability (Blaine). An estimation of SSA area is also calculated from the PSD (laser) measurement, in accordance with Eq.5.

$$S_{S,PSD} = \frac{6}{\rho_s \cdot D[3,2]} \quad (5)$$

$$D[3,2] = \frac{\sum n_i \cdot d_i^3}{\sum n_i \cdot d_i^2} \quad (6)$$

The volume to surface mean diameter $D[3,2]$ of the sample is calculated from the size distribution curve by means of Eq.6, in which n_i corresponds to the number of particles of diameter d_i . These equations assume that the particles are spherical and that they are not porous.

The average values of SSA from BET analysis are greater than for Blaine. For limestone fillers F3, F5 and F6, internal porosity contributes to global surface area, specifically for very fine clay particles, for which surface can be measured by fine-scale N_2 adsorption (Michel and Courard 2006). Limestone filler F4 is the finest filler we tested with high organic material content (Courard et al. 2011). Blaine method is indeed insensitive to internal porosity and is not able to take it into account in the calculation. This last remark could also explain the good correlation between specific surfaces calculated by laser diffraction and Blaine methods.

Table 6. Comparison of specific surface area SSA [$m^2 \cdot g^{-1}$] using multipoint N_2 adsorption isotherms, laser diffraction and air permeability.

Method	F1	F2	F3	F4	F5	F6
$S_{S,Blaine}$	0.48	0.53	0.65	0.77	0.61	0.45
SS.PSD (laser diffraction)	0.57	0.41	0.56	0.80	0.60	0.45
$S_{S,BET}$	1.3	1.2	5.5	4.0	5.7	3.7

4. Conclusions

On the basis of the experimental program and the results, the following conclusions can be drawn for the limestone fillers that have been tested here:

- limestone fillers are mainly composed of strongly birefringent calcite mineral with refractive indices ranging from 1.48 to 1.66. For laser diffraction and in the case of using Mie diffusion model, the value of refractive index influences the particle size distribution. Refractive index value of 1.57 was selected as reference value. Absorption index was selected in such a way that real and calculated angular distribution of light were better fitted;
- although the use of Mie or Fraunhofer models can slightly influence the shape of the relative particle size distribution, it does not significantly affect the volume weighted percentiles of limestone filler samples;
- a discrepancy was observed between SIA and LD size distributions towards both the lower and upper sizes. The fact that SIA is unable to take into account particles smaller than 3 pixels in width ($1.44\ \mu\text{m}$) could explain the under estimation of fine elements;
- the interest of wet sieving technique is to confirm the presence of 63-125 μm particles in filler samples analyzed by laser diffraction technique. The under estimation of big particles by SIA is confirmed; they are excluded from analysis due to contact with frame. It could be partially corrected by taking into account the probability of total inclusion of a particle within the image frame;
- the average values of SSA from BET are greater than from Blaine. In case of F3, F5 and F6, these results can be explained by the presence of fine clay minerals;
- good correlation was found between specific surface area measured by Blaine permeability tester and calculated from laser diffraction data.

On the base of these conclusions, it appears that the specific surface area and granulometry of limestone fillers may be efficiently estimated from complementary techniques. This description is absolutely needed for understanding particles behaviour in contact with water, when used in cementitious materials: water demand is for example greatly dependent on these physical characteristics. Finally, the techniques can be easily extended to other fine particles like silica fume, fly ashes or metakaolin that are also used for concrete mix design.

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