

# NUMERICAL AND EXPERIMENTAL INVESTIGATION OF FIBER DRAWING PROCESS

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- **Motivation**

- Physical model
  - Experimental setup
  - Numerical investigation
    - Heat transfers
    - Stresses
  - Conclusion & future work
-

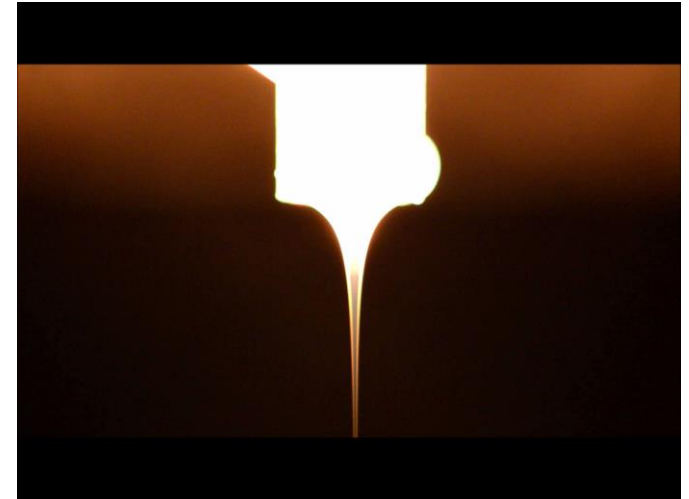
# Motivation & objectives

Glass fibers are used for the reinforcement of **composite materials**

Main challenges: **fiber breakage**



- **Shut down** of forming position
- Unrecyclable glass **waste**
- **Barrier** to optimization



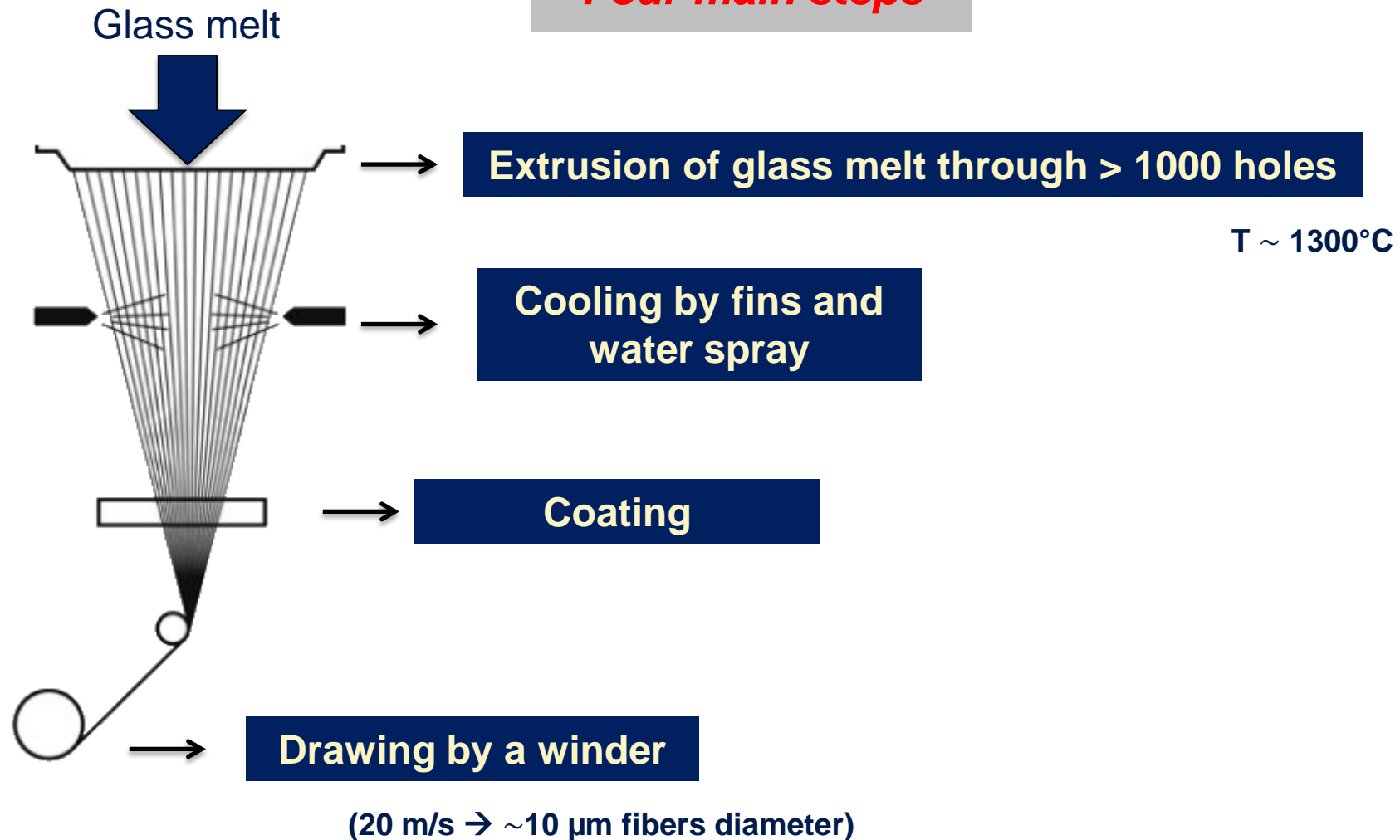
## Overall Goal

- Understand **fiber breaking**:
  - Step 1: Physical modeling of forming glass
  - Step 2: Characterization of breaking mechanisms
    - One single fiber
    - Multi-filaments bushing

# Fiberglass drawing process

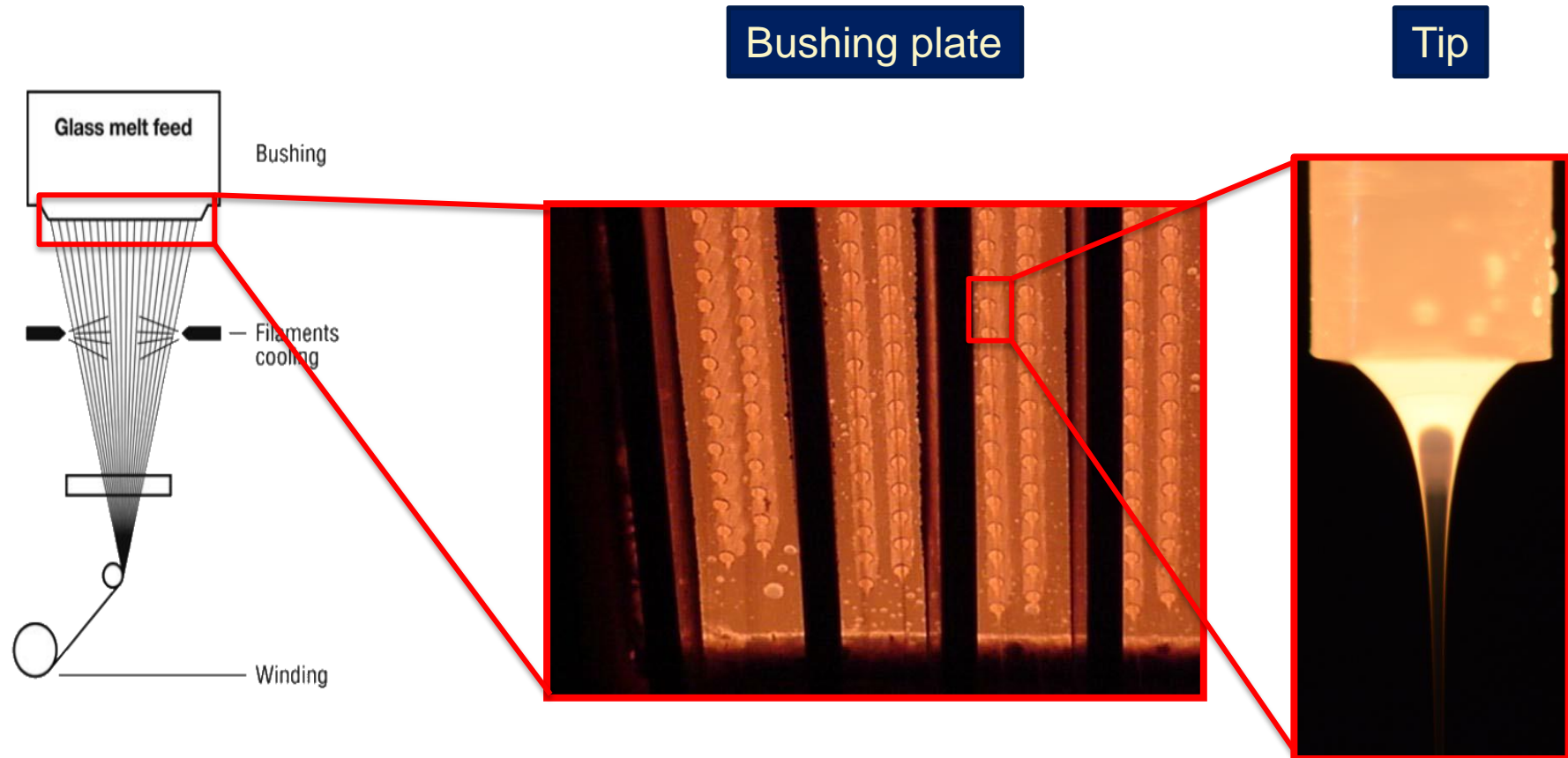
## General steps

### *Four main steps*



# Fiberglass drawing process

## Bushing plate & tips



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# Physics of the forming of a single fiber

Glass state

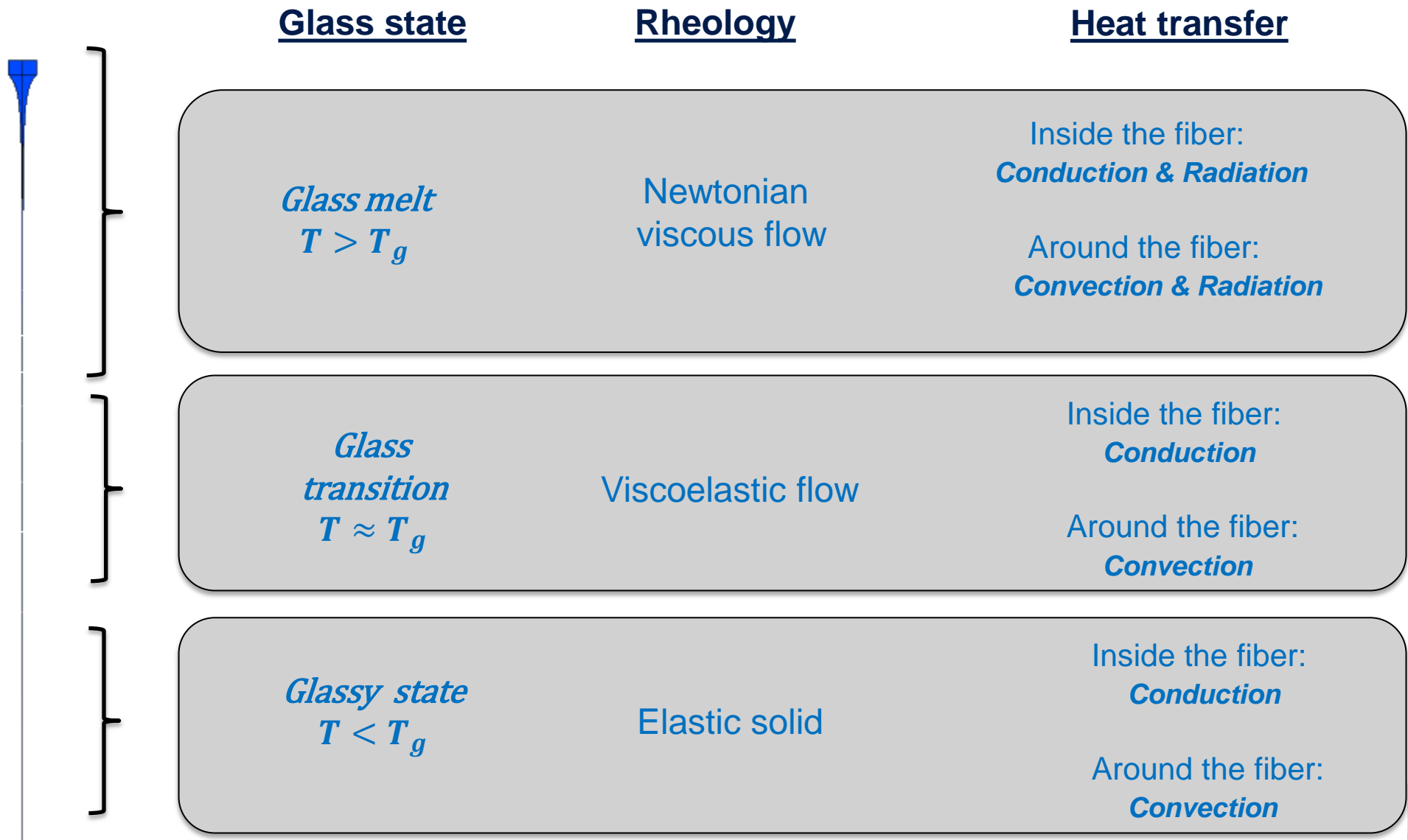
Rheology

Heat transfer

**Coupling**

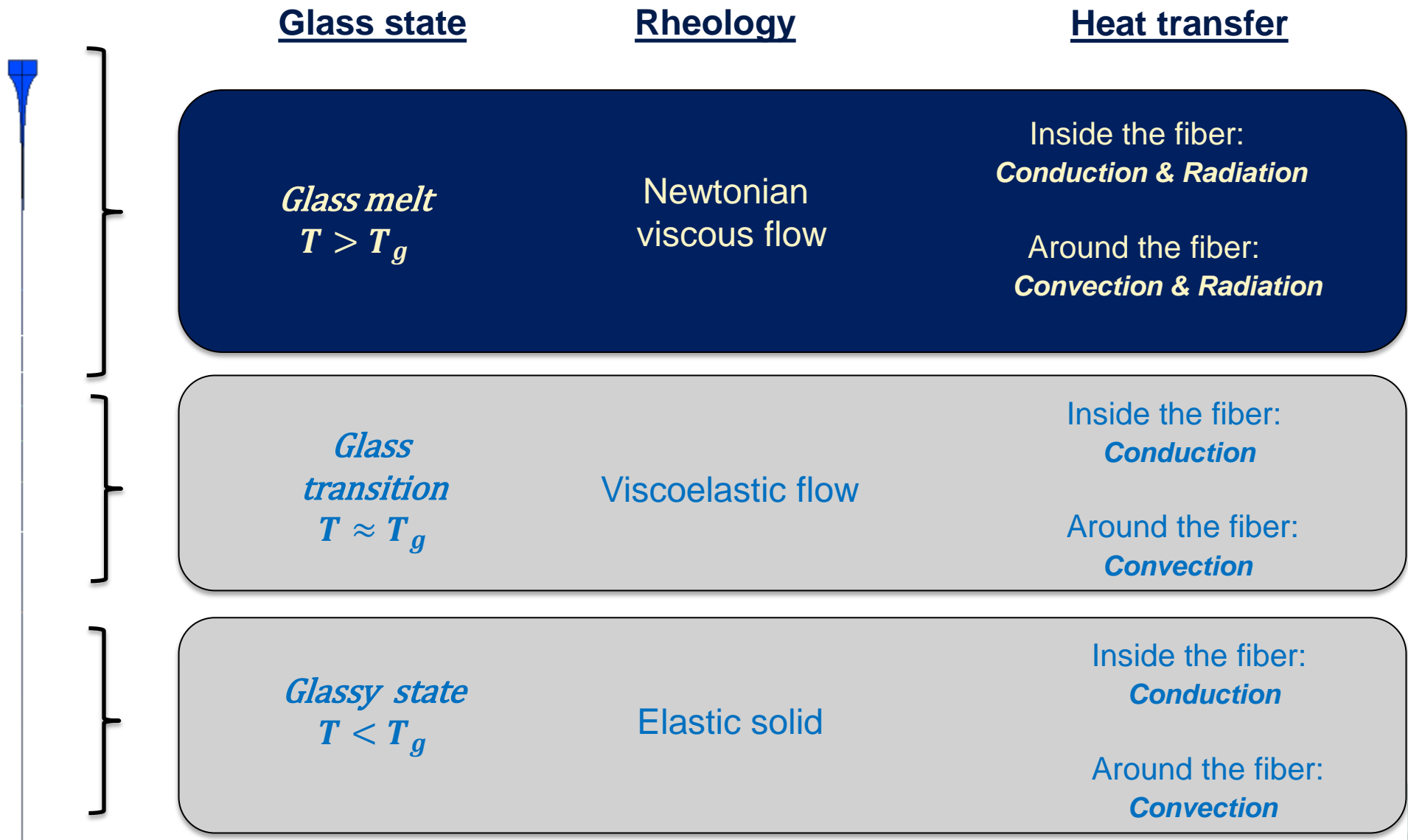


# Physics of the forming of a single fiber





# Physics of the forming of a single fiber



Mass conservation:

$$\frac{D\rho}{Dt} = 0$$

Momentum conservation:

$$\frac{D(\rho \mathbf{v})}{Dt} = \nabla \cdot \boldsymbol{\sigma} + \mathbf{f}$$

Energy conservation:

$$\frac{D(\rho C_p T)}{Dt} = \boldsymbol{\sigma} : \nabla \mathbf{v} - \nabla \cdot (\mathbf{q}_{cond} + \mathbf{q}_{rad})$$

**Assumption:** Internal radiation  $\rightarrow$  neglected

Mass conservation:

$$\frac{D\rho}{Dt} = 0$$

Momentum conservation:

$$\frac{D(\rho \mathbf{v})}{Dt} = \nabla \cdot \sigma + f$$

**Newtonian flow:**

$$\sigma = -p\mathbf{I} + 2\eta\mathbf{D}$$

Energy conservation:

$$\frac{D(\rho C_p T)}{Dt} = \sigma : \nabla \mathbf{v} - \nabla \cdot (\mathbf{q}_{cond} + \mathbf{q}_{rad})$$

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**Newtonian flow:**

$$\boldsymbol{\sigma} = -p\mathbf{I} + 2\eta \mathbf{D}$$

coupled through  
viscosity

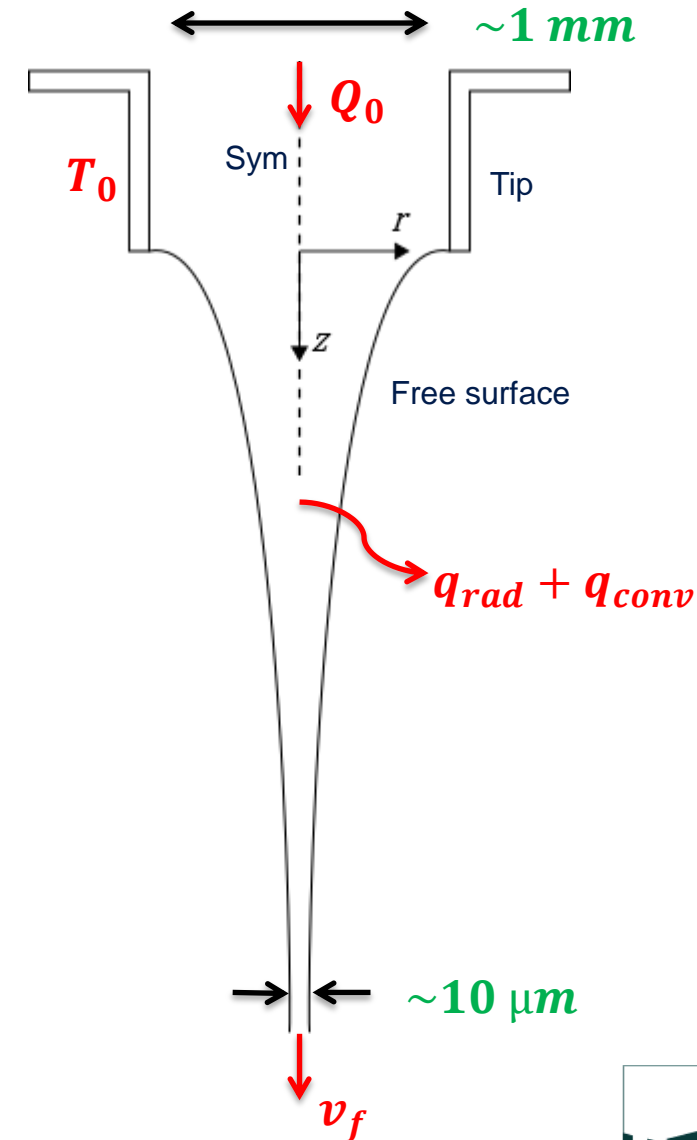
Fulcher law

$$\eta = 10^{-A + \frac{B}{T - T_0}}$$

( $\eta$  = dynamic viscosity)

**Assumption:** Internal radiation  $\rightarrow$  neglected

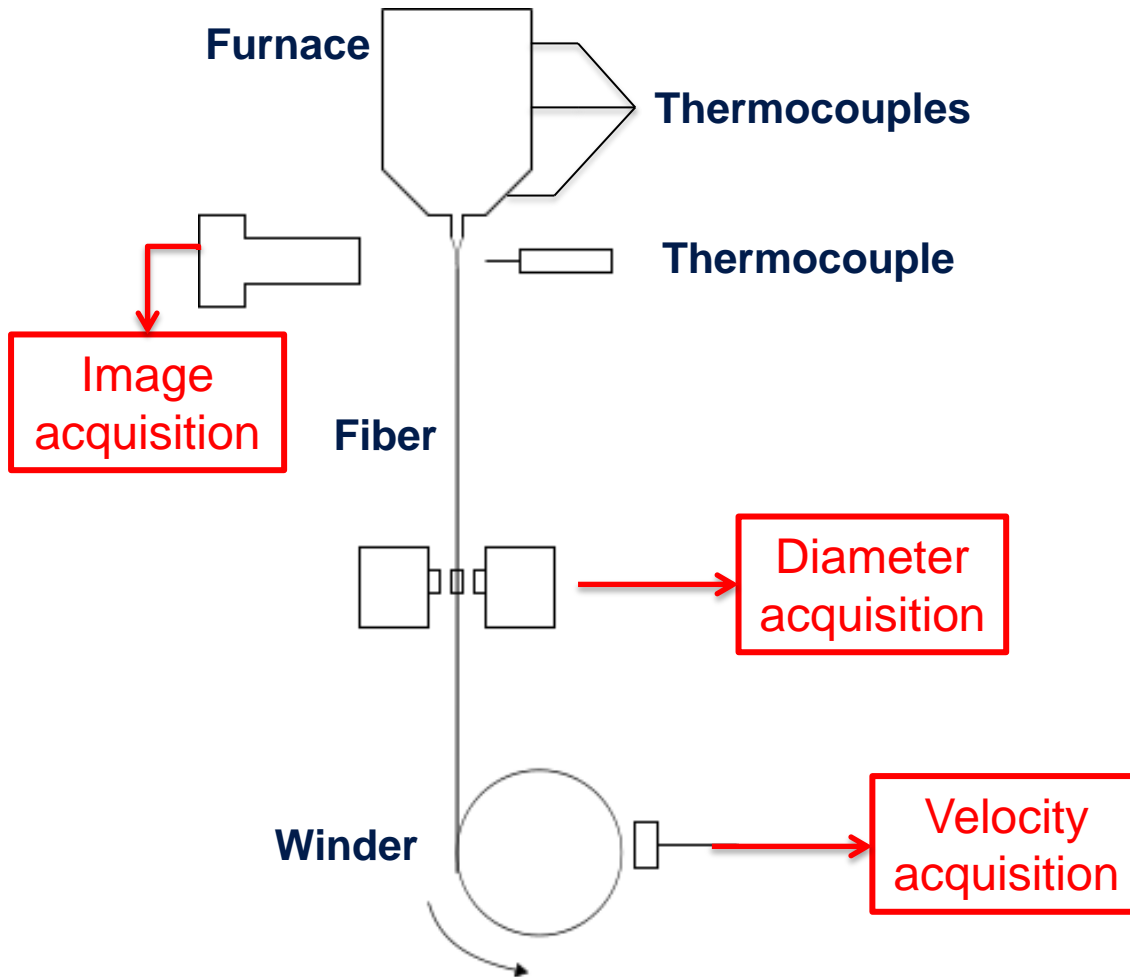
- At tip:
  - Volumetric flow rate (Poiseuille law)
  - $T_0$  constant
- At surface:
  - Free surface conditions & surface tension
  - $q = \underbrace{\varepsilon\sigma(T^4 - T_{ext}^4(z))}_{\text{Radiation}} + \underbrace{h(z)(T - T_{ext}(z))}_{\text{Convection}}$
- At outlet: Drawing velocity



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# Experimental investigation

## Fiber drawing unit

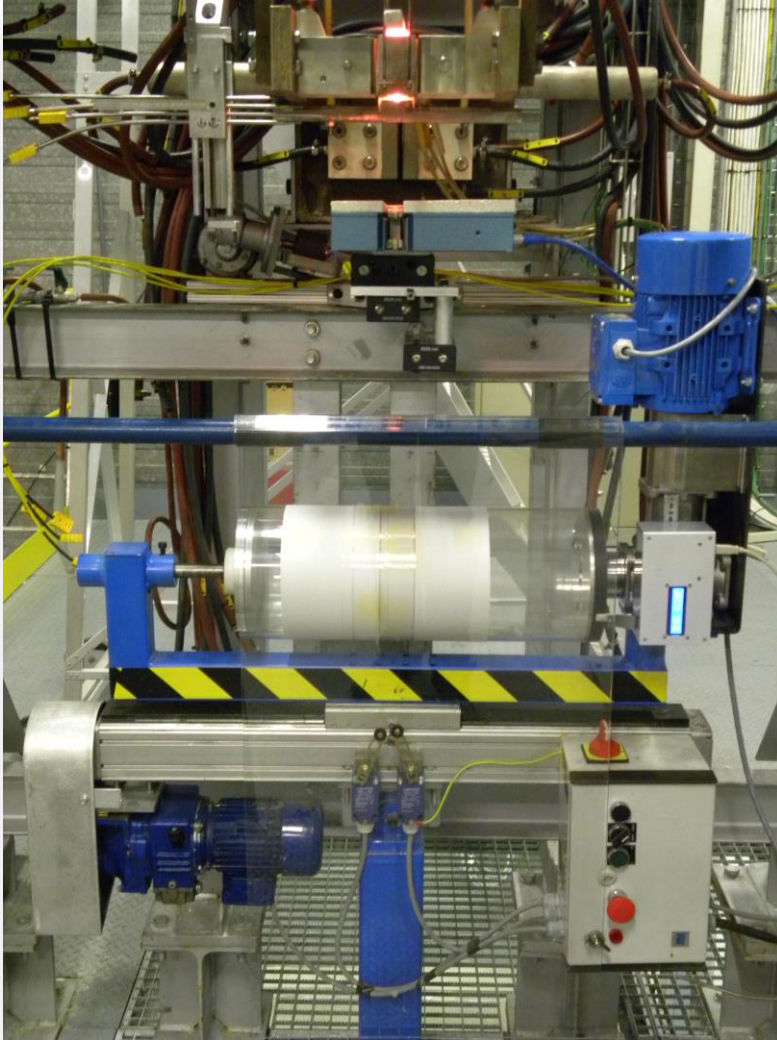


### Facilities

1. Velocity acquisition
2. Image acquisition
3. Diameter acquisition

# Experimental investigation

## Fiber drawing unit



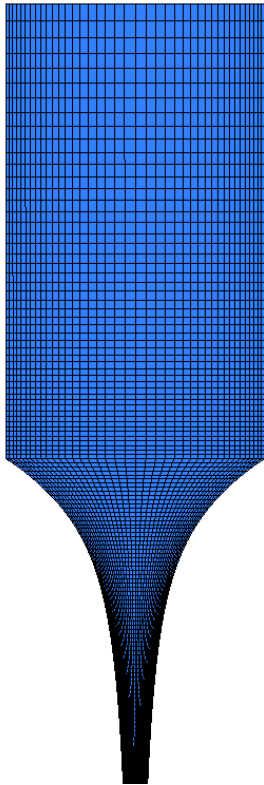
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Simulations are performed with ANSYS Polyflow software



### Cases of study

- Validation
- Heat transfers:
  - radiation
  - convection
- Stress: sensitive analysis

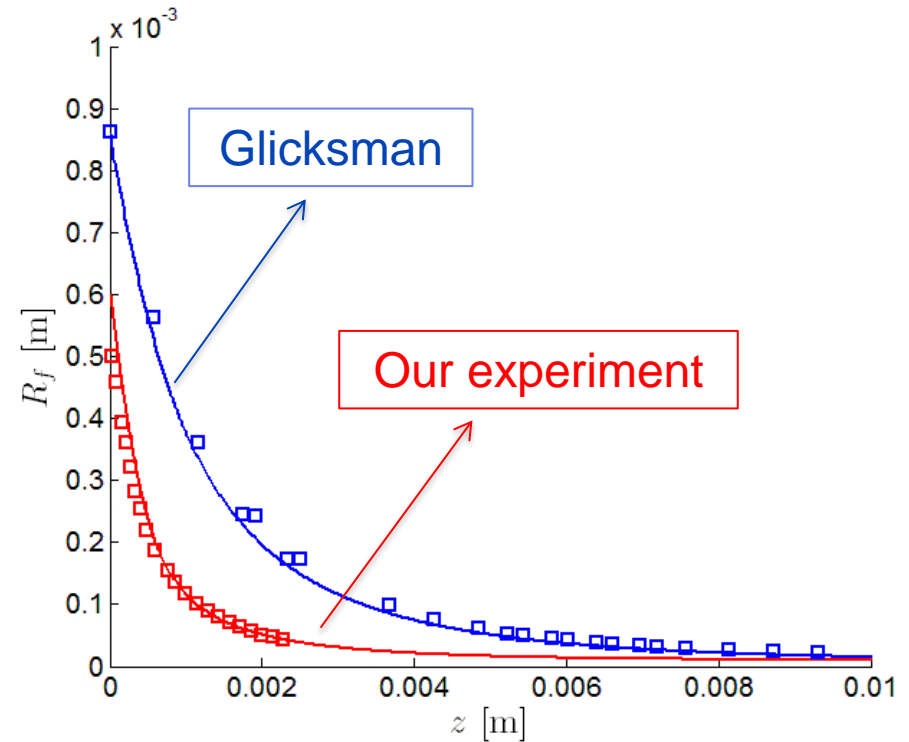
### Case study

Material	Glass M5	Advantex®
$T_0$	1227 °C	1308 °C
$Q_0$	$3.17 \cdot 10^9 \text{ m}^3/\text{s}$	$4.72 \cdot 10^{10} \text{ m}^3/\text{s}$
$v_f$	$25.88 \text{ m}^3/\text{s}$	$1.55 \text{ m}^3/\text{s}$

Glicksman  
1964

Our  
experiment

### Fiber radius



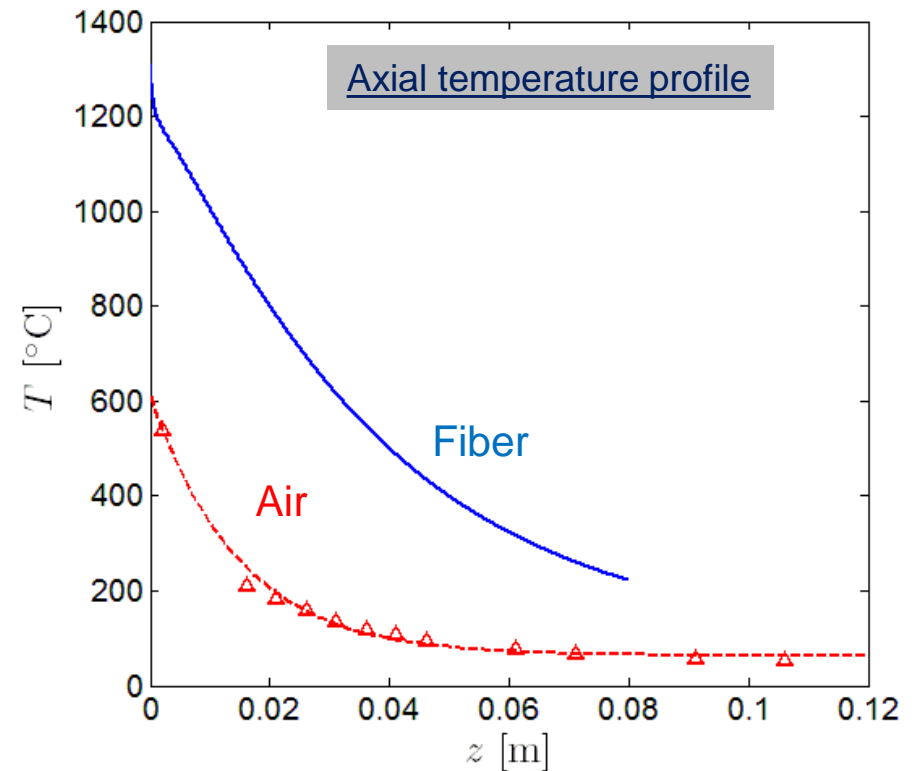
**Good agreement between simulation  
and experimental data**

Cooling is critical:

- impact on fiber properties
- impact on break origins



What are the factors that lead to this high cooling?



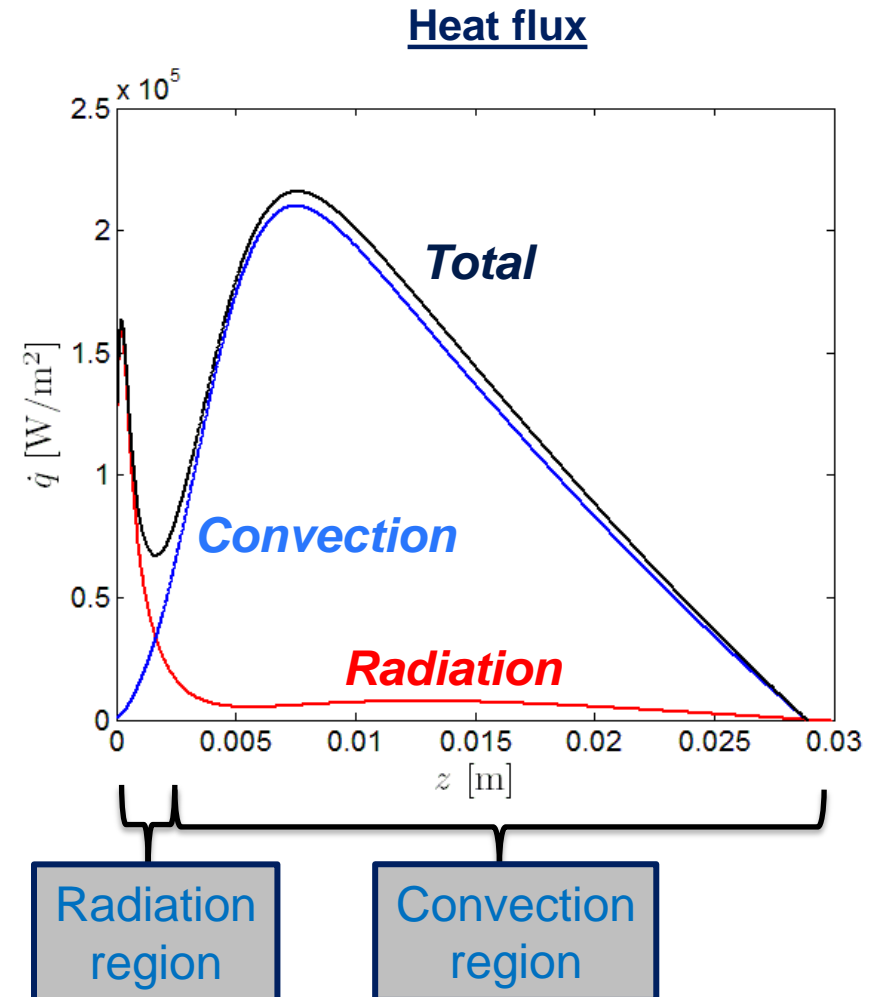
### Heat flux:

$$\dot{q}(z) = \underbrace{h(T - T_{ext})}_{\text{Convection}} + \underbrace{\varepsilon\sigma(T^4 - T_{ext}^4)}_{\text{Radiation}}$$

### Cooling rate:

$$\dot{T} = - \frac{\dot{q}(z)}{\rho C_p r_f(z)}$$

- Cooling depends both on **heat flux** and **radius attenuation**
- **Radius history** is important due to variation of **viscosity**



# Heat transfer

## Cooling rate - Radiation

**Radiation:**

$$\dot{q}_{rad} = \varepsilon \sigma (T^4 - T_{ext}^4)$$

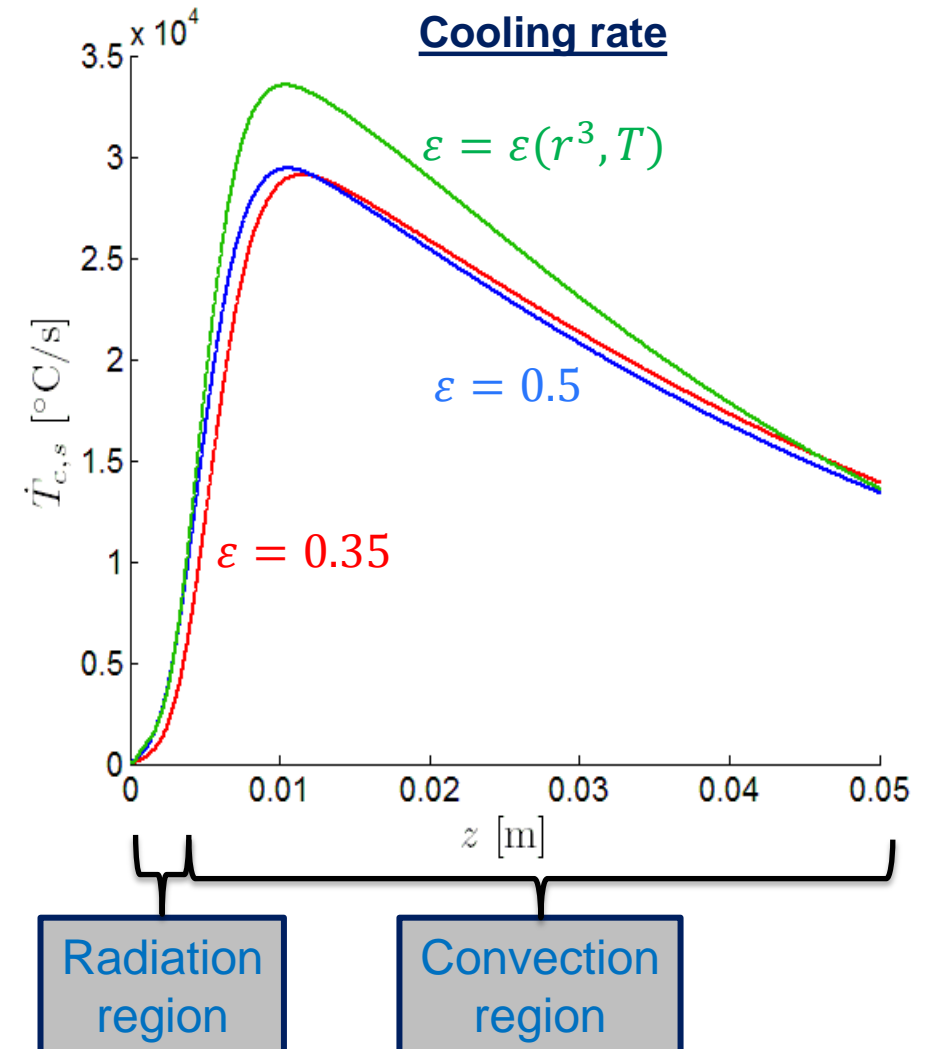
with

$$\varepsilon = \varepsilon(r^3, T)$$

**Cooling rate:**

$$\dot{T}_{c,s} = - \frac{\dot{q}(z)}{\rho C p r_f(z)}$$

→ Variability emissivity has a significant impact



# Heat transfer

## Cooling rate - Radiation

$$\text{Cooling rate: } \dot{T}_{c,s} = -\frac{\dot{q}(z)}{\rho C_p r_f(z)}$$

Variation of emissivity



Variation of viscosity



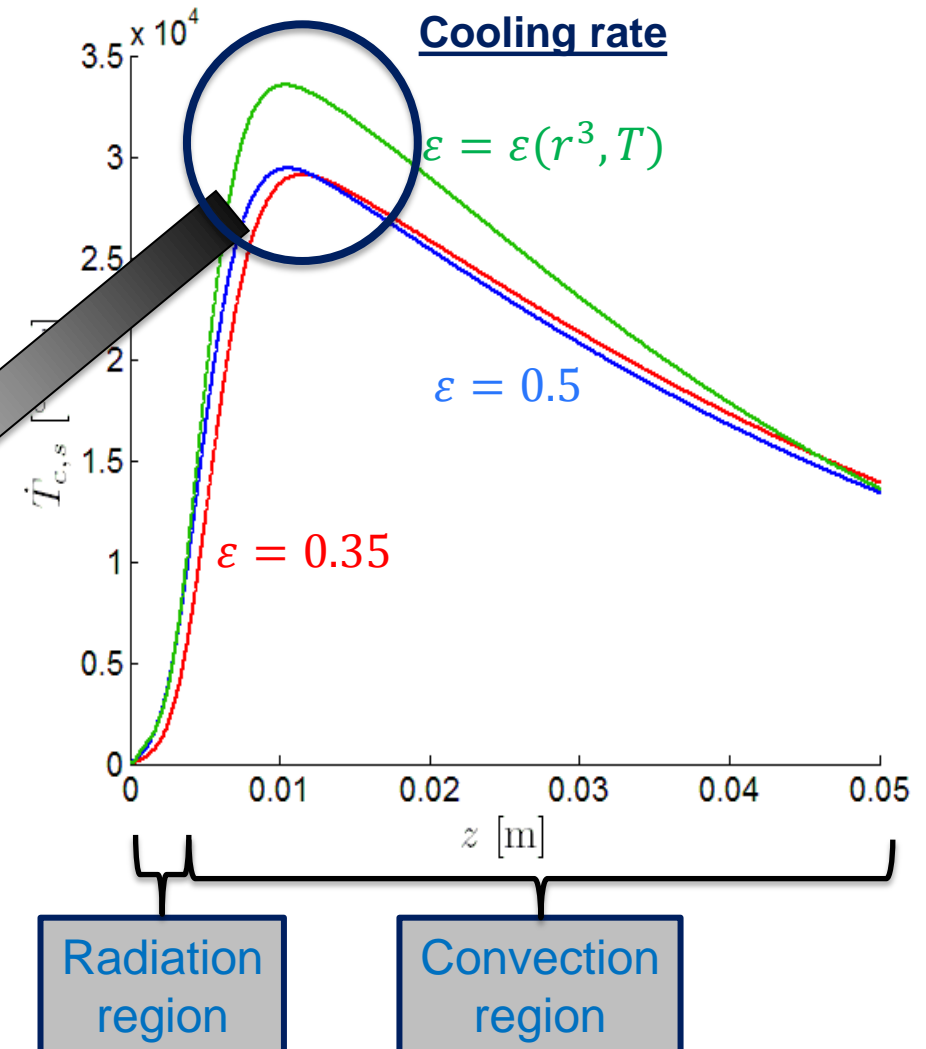
Variation of velocity



Variation of radius



Cooling rate is very sensitive to the cooling history



# Heat transfer

## Cooling rate - Convection

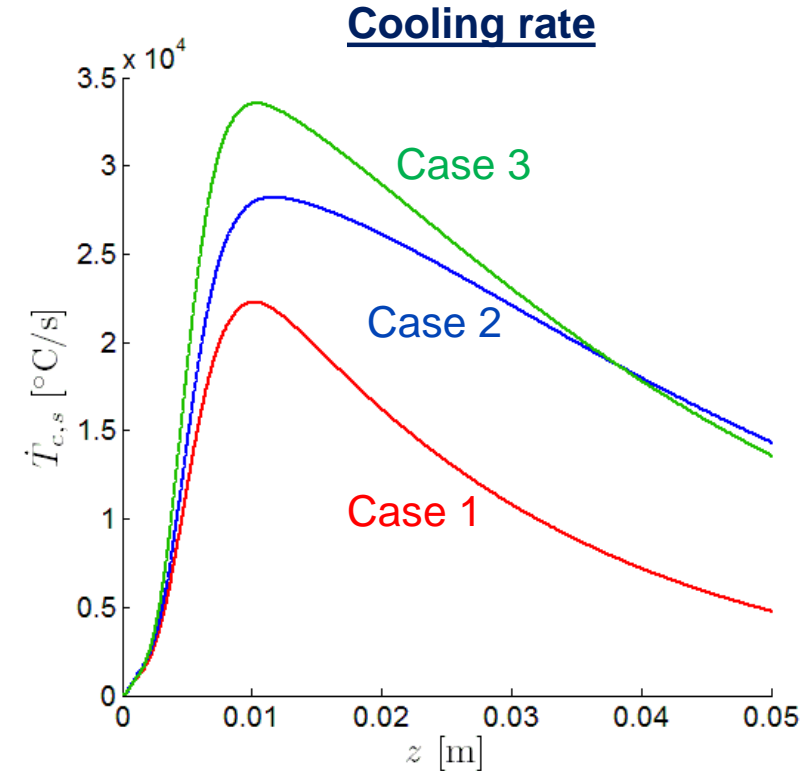
Convection:  $q_{conv} = h(T - T_{ext})$

**Kase-Matsuo** convective coefficient:

$$h = \frac{0.42 k_a}{D_f} \left( \frac{v_s D_f}{\mu_a} \right)^{0.334}$$

- Fiber diameter  $D_f$
- Fiber velocity  $v_f$
- Air properties  $k_a, \mu_a$
- Air temperature  $T_{ext}(z)$

- Surrounding air has a significant impact on the cooling rate
- Accurate description of air properties is needed



Case 1: **Constant** air temperature

Case 2: **Variable** air temperature with **constant** air properties

Case 3: **Variable** air temperature and air properties **depending on temperature**

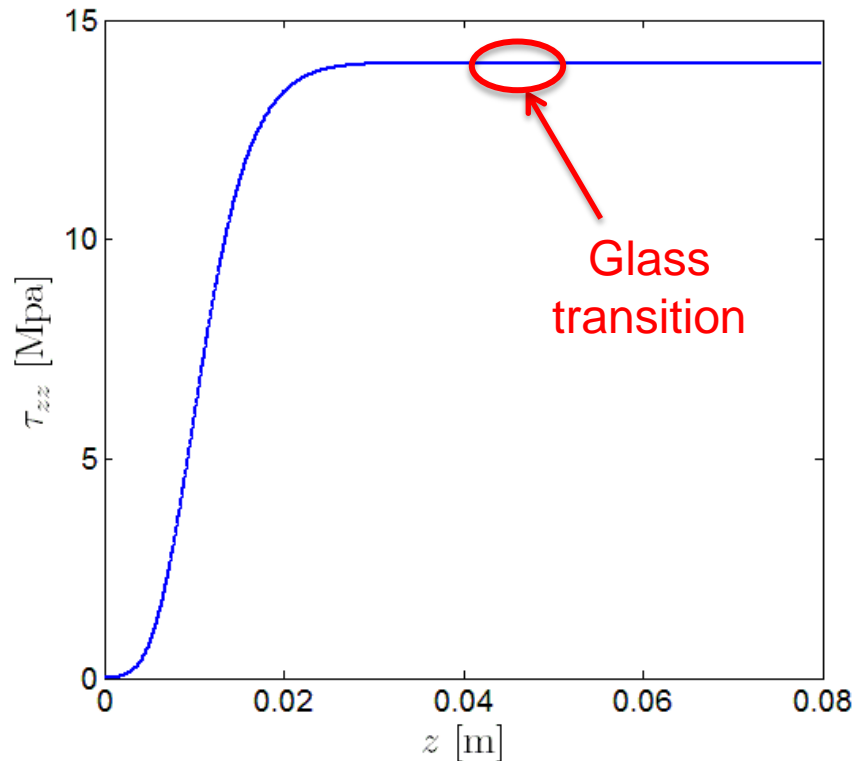


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Newtonian stress in z direction:

$$\tau_{zz} = \eta(T) \frac{dv_z(z)}{dz}$$

### Axial stress

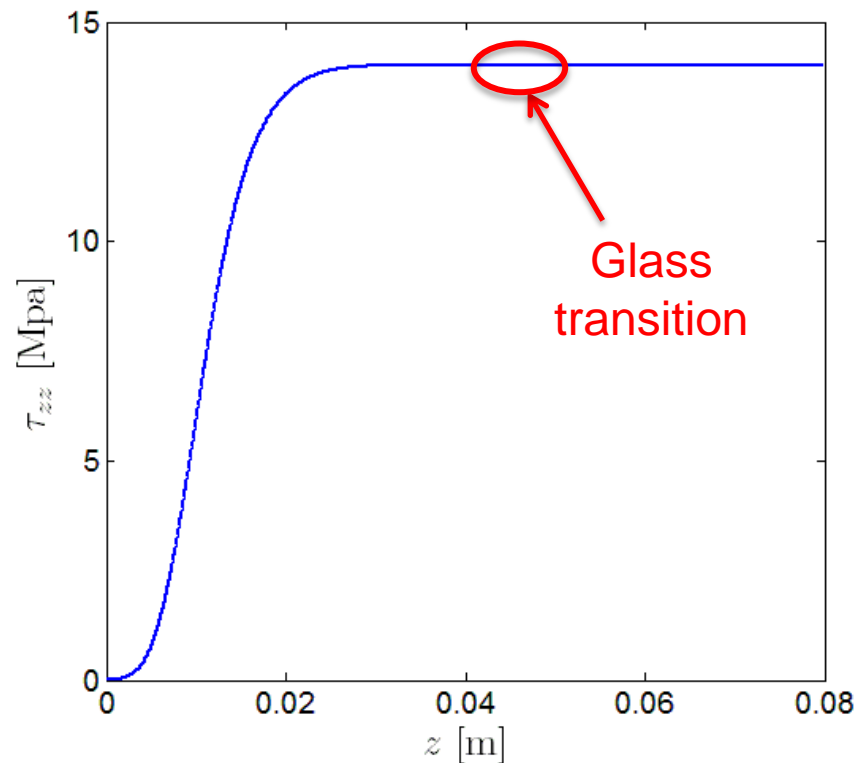


- **Axial stress** grows and takes a final constant value
- **Final value** before the transition
- **Newtonian model** seems to be sufficient

Newtonian stress in z direction:

$$\tau_{zz} = \eta(T) \frac{dv_z(z)}{dz}$$

Axial stress



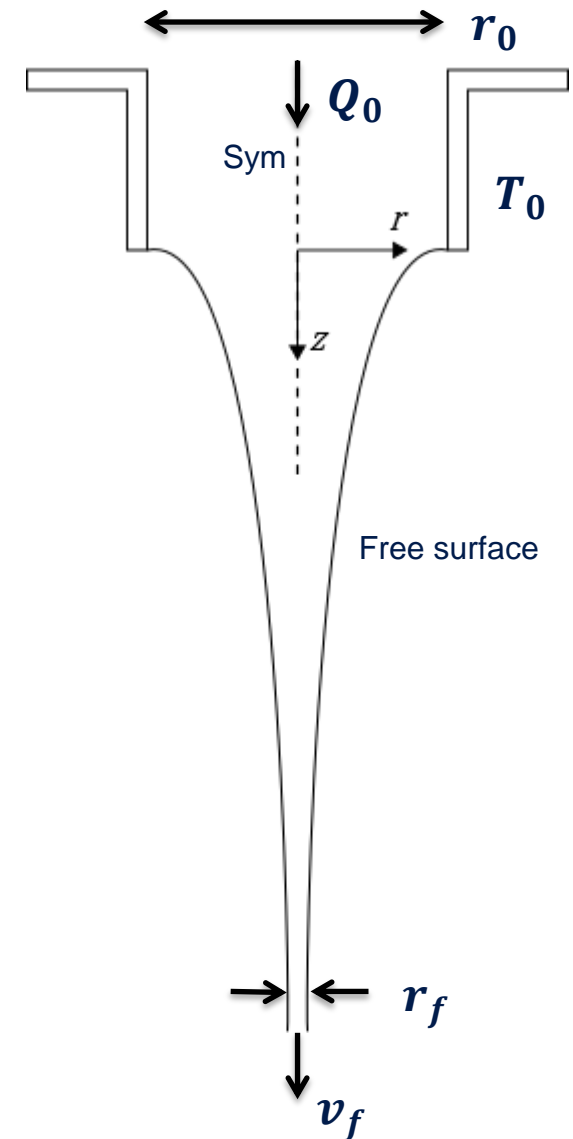
**Key question:**

*What are the key parameters controlling the internal stress?*

Given a target radius  
→ how the stress can be reduced ?

Mass conservation:

$$r_f^2 = \frac{Q_0(r_0, T_0)}{\pi v_f} = cst$$



# Stresses

## Main parameters

Given a target radius  
→ how the stress can be reduced ?

Mass conservation:

$$r_f^2 = \frac{Q_0(r_0, T_0)}{\pi v_f} = cst$$

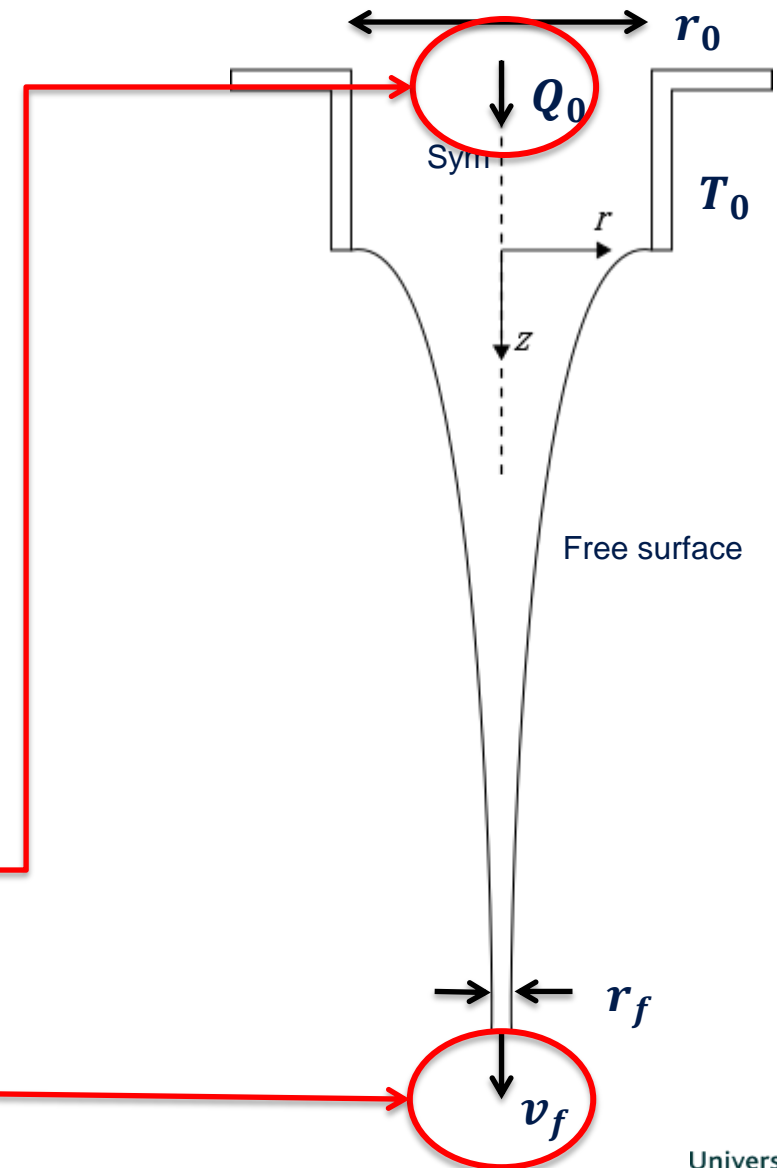
Main parameters:

Tip flow rate  $Q_0$

Tip geometry  $r_0$

Tip temperature  $T_0$

Winder velocity  $v_f$



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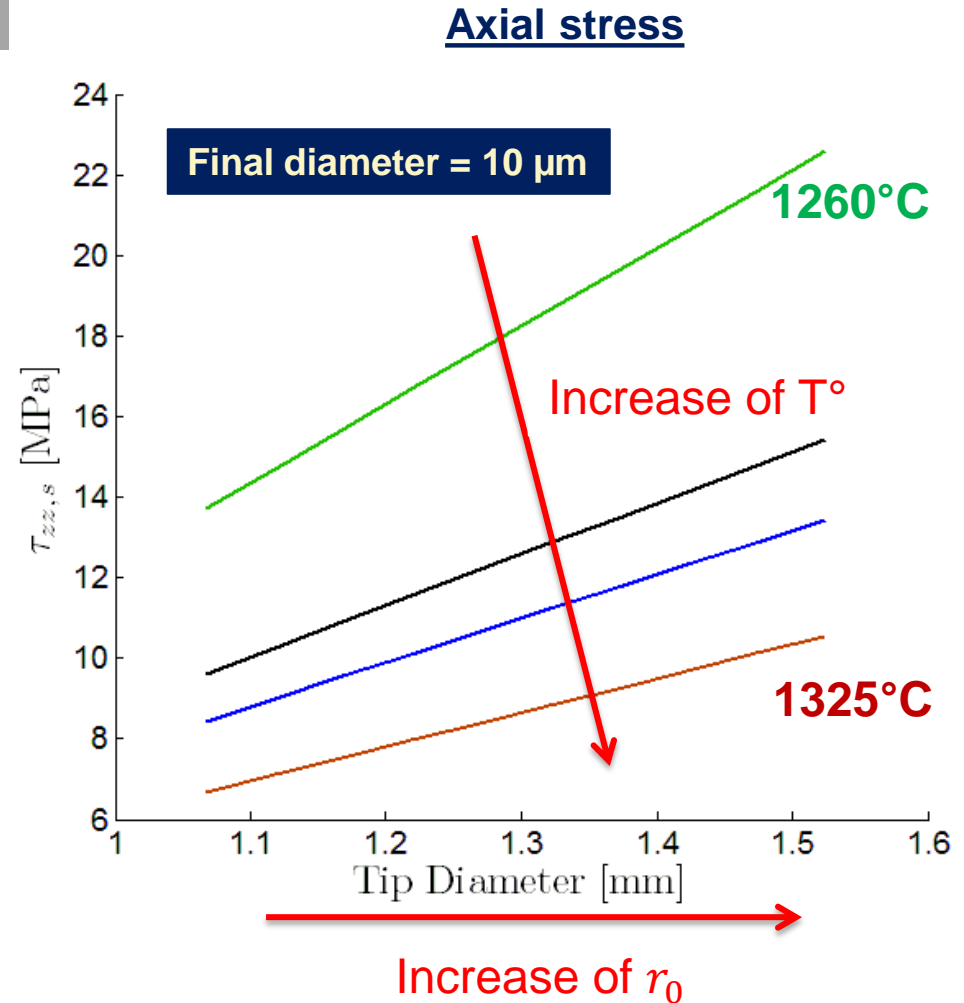
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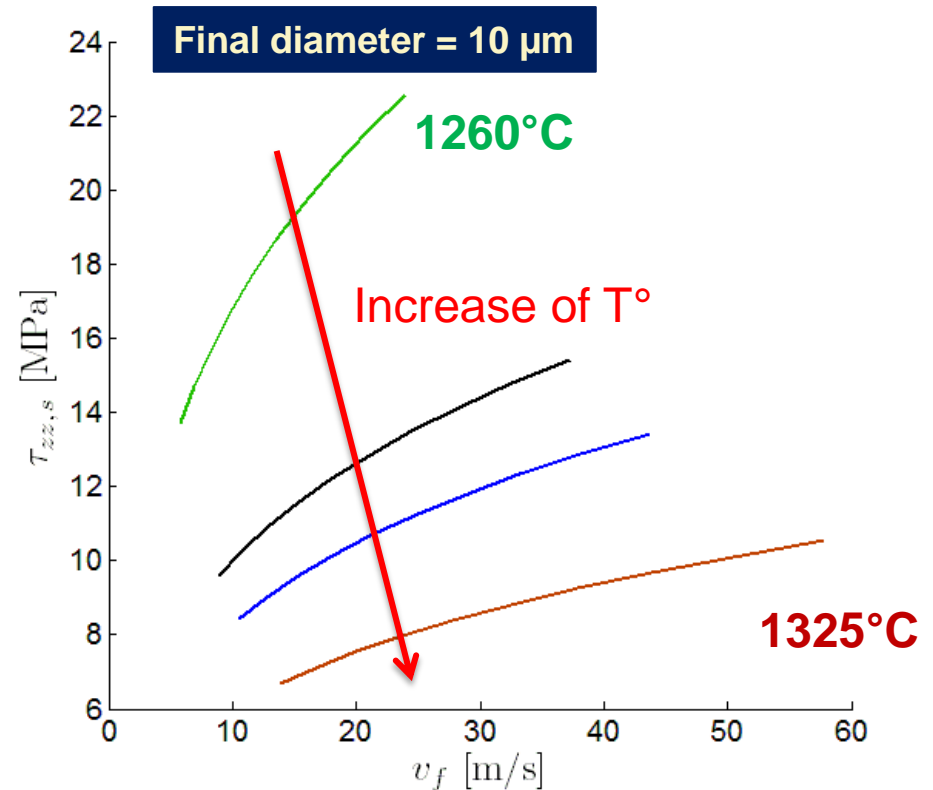
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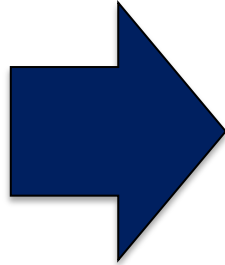
Tip temperature  $T_0$

Winder velocity  $v_f$

Axial stress



Given a target radius  
→ how the stress can be reduced ?



- Decrease tip radius
- Increase the tip temperature
- Decrease the winder velocity



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## Conclusion

- Physical model of one fiber drawing has been developed
- Numerical solutions give a good way to understand the process
- Fiber forming is strongly coupled with the air environment
- Stress in the fiber can be reduced by:
  - decreasing the winder velocity
  - decreasing the tip diameter
  - increasing the tip temperature

## Further work

- Add a radiation model for the heat transfer inside the glass
- Investigate the viscoelasticity
- Investigate the origins of the fiber breaks

- **Our industrial partner:** *3B – the fibreglass company, Binani group*
- **Financial support:** *3B – the fibreglass company & Walloon region*
- **R&D team from 3B:** D. Laurent, Y. Houet, B. Roekens, S. Pirard, P. Delit and technicians