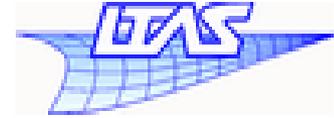


# Stiction failure in microswitches due to elasto- plastic adhesive contacts

L. WU, J.-C. GOLINVAL ,  
L. NOELS

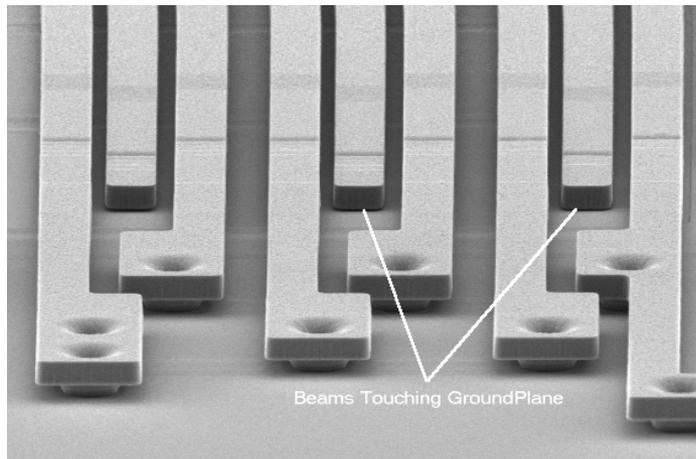
24th October 2012

# Content



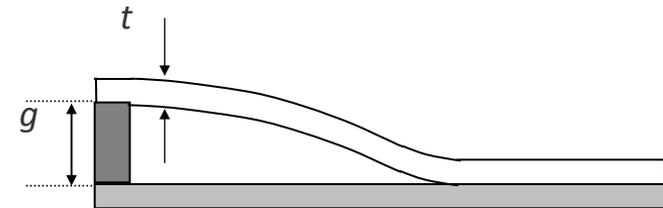
- **Introduction**
  - **Stiction in MEMS**
  - **Multiscale approach developed**
- **Model Description**
  - **Basic Theory for One asperity**
  - **Statistical Model of Rough Surface**
- **Multiscale Model**
  - **Polysilicon to Polysilicon Interaction**
  - **Cantilever beam (FEM): validation with experiments**
- **Elasto-plastic adhesive contact**
- **Conclusions**

- **Stiction in MEMS**



*Stiction failure in a MEMS sensor*

*( Jeremy A. Walraven Sandia National Laboratories.  
Albuquerque, NM USA)*



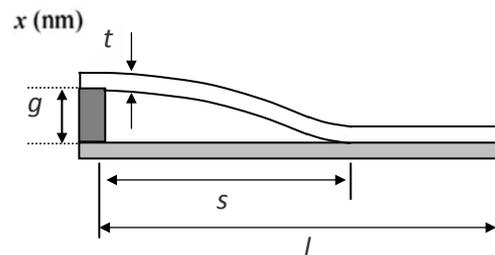
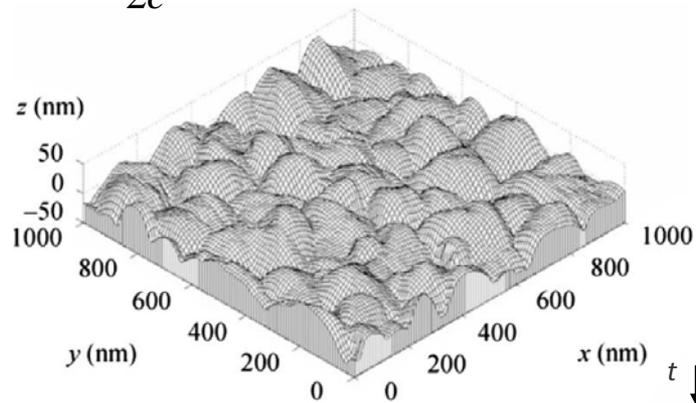
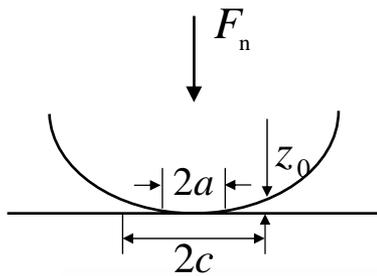
**Reason:**

Relatively high surface area:  
volume ratio (1,000:1 to  
10,000:1  $\text{m}^{-1}$ )

**Adhesive forces:**

Electrostatic force, Van der  
Waals force, Capillary force,  
Hydrogen bridging...

- **Multiscale approach developed**



Single asperity adhesive-micro contact



Adhesive elastic contact model  
between rough surfaces



Integration with  
FEM

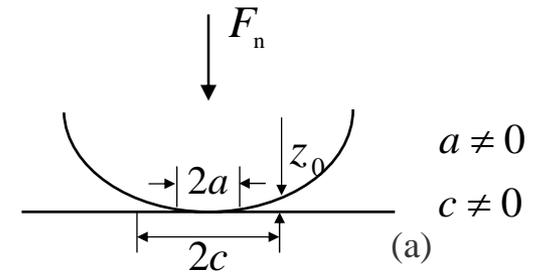
# Single asperity adhesive-micro contact



- **Adhesive-elastic contact (Hertz) theories**

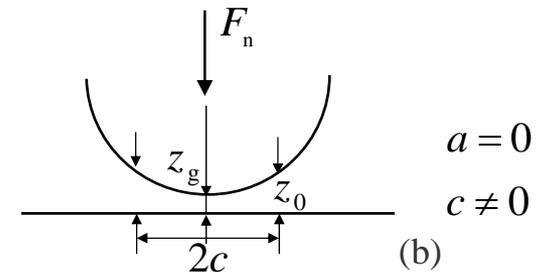
- **Johnson, Kendall, and Roberts (JKR)**

- Short ranged surface forces
- Act only inside the contact area
- ⇒ { Soft, compliant materials with high surface energy



- **Derjaguin, Muller and Toporov (DMT)**

- Long-ranged adhesive forces
- Outside of the contact area
- ⇒ { Harder, less compliant materials with low surface energy and small asperity tip radius



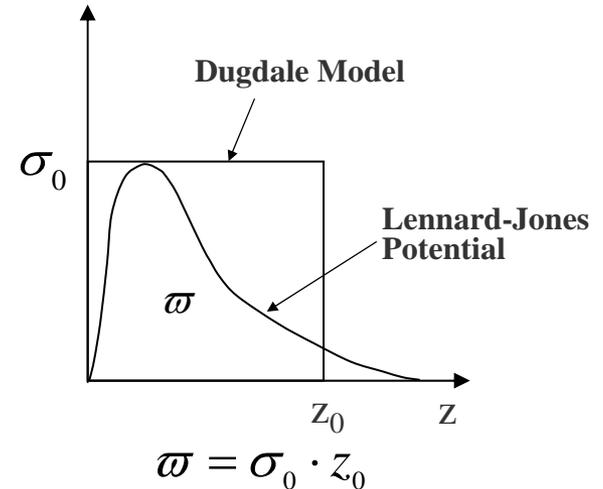
- **Maugis transition solution**

- Intermediate cases between JKR and DMT
- ⇒ For all elastic materials

# Single asperity adhesive-micro contact



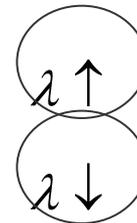
- **Maugis transition solution**
  - **Based on a Dugdale assumption for interaction potential**
    - Constant traction  $\sigma_0$  within a critical value of separation  $z_0$
    - Zero traction for gap larger than  $z_0$
  - **Maugis transition parameter  $\lambda$** 
    - Representation of the surface properties
      - $R$ : asperity radius
      - $K$ : equivalent elastic constant
      - $\varpi = \sigma_0 z_0$ : adhesive work



$$\lambda = \frac{2\varpi^{2/3} R^{1/3}}{z_0 (\pi K^2)^{1/3}}$$

$\Rightarrow$

$$\varpi \uparrow, R \uparrow, K \downarrow \Rightarrow$$



$$\varpi \downarrow, R \downarrow, K \uparrow \Rightarrow$$

JKR model  
(short ranged)

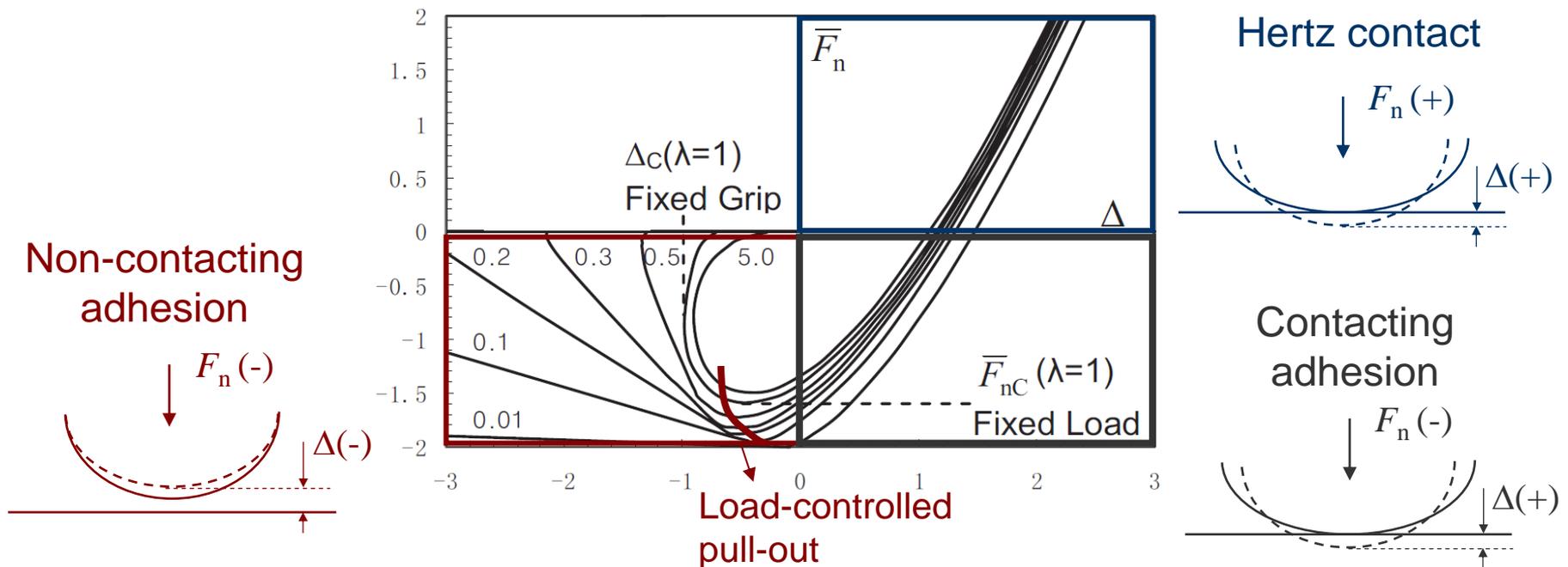
DMT model  
(long ranged)

# Single asperity adhesive-micro contact



- **Maugis transition solution (2)**
  - **Adhesive-micro (elastic) contact force during unloading**

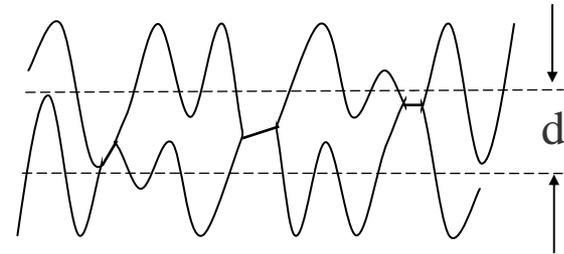
- In term of Maugis transition parameter  $\lambda = \frac{2\varpi^{2/3} R^{1/3}}{z_0 (\pi K^2)^{1/3}}$



# Adhesive contact between rough surfaces



- **Rough surfaces**
  - **Reduced number of interacting asperities**
  - **In terms of distance  $d$**



- **Rough surfaces model**
  - **Constant asperity tip radius**
  - **Statistical distribution in height  $h$**

$$\varphi(h) = \frac{1}{\sigma\sqrt{2\pi}} \exp\left(\frac{-h^2}{2\sigma^2}\right)$$

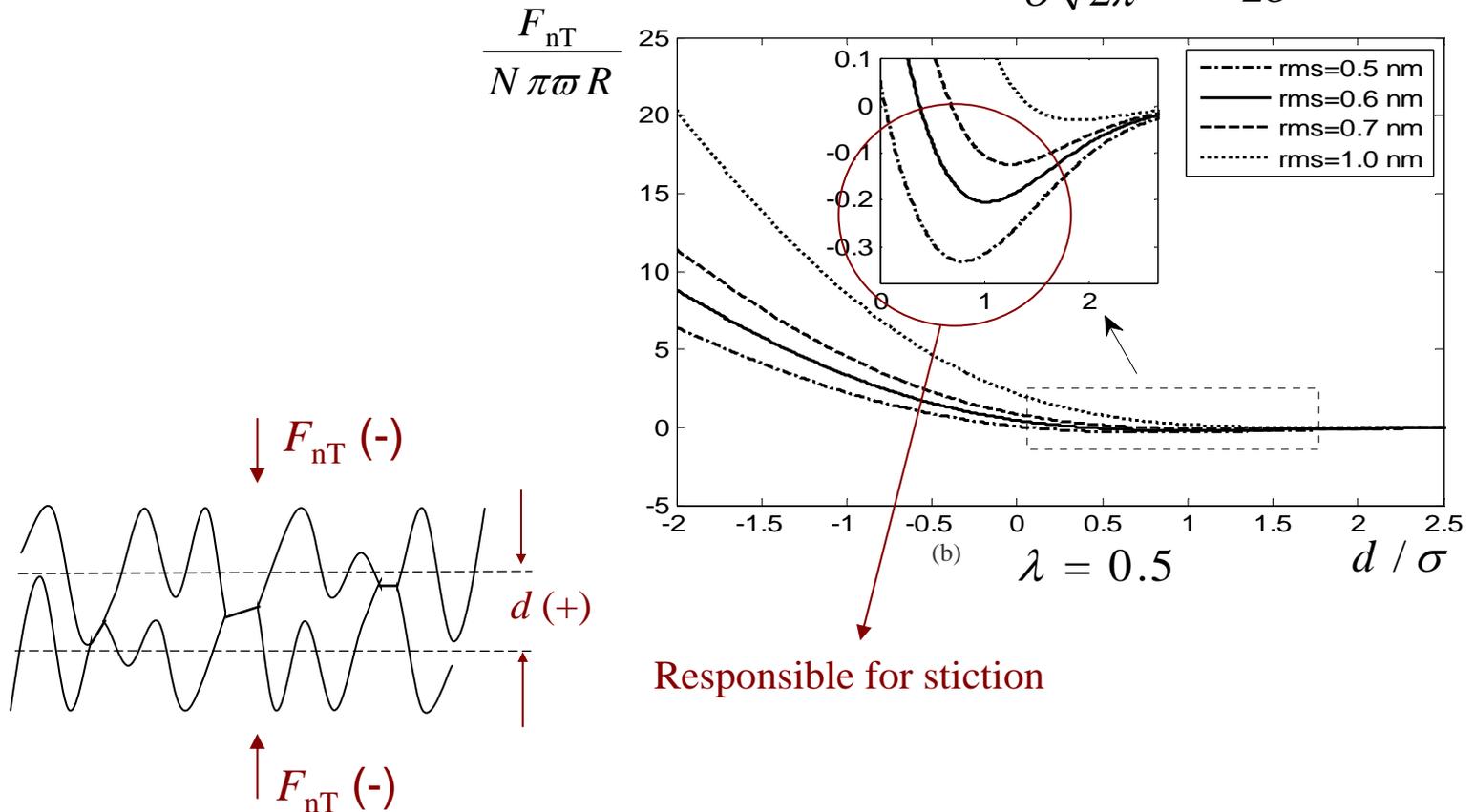


# Adhesive contact between rough surfaces

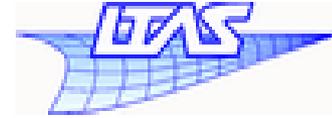


- Micro adhesive contact forces of rough surfaces

- Integrate Maugis solution using  $\varphi(h) = \frac{1}{\sigma\sqrt{2\pi}} \exp\left(\frac{-h^2}{2\sigma^2}\right)$



# Multiscale Model



- **Design example: cantilevers**

- **Finite element model**

- Timoshenko Beams
- Interacting with pad

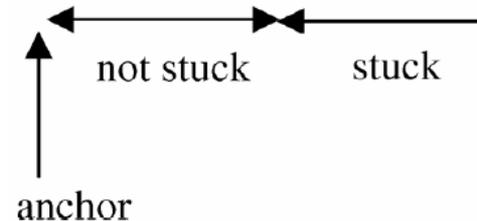
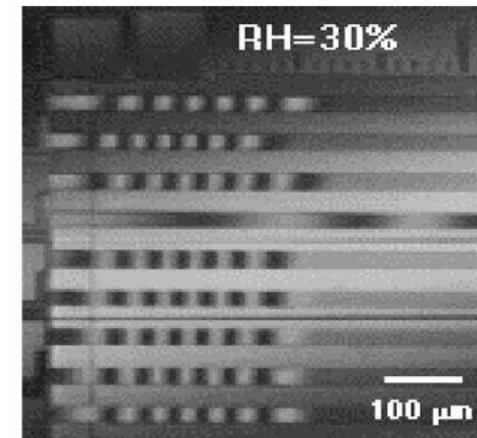
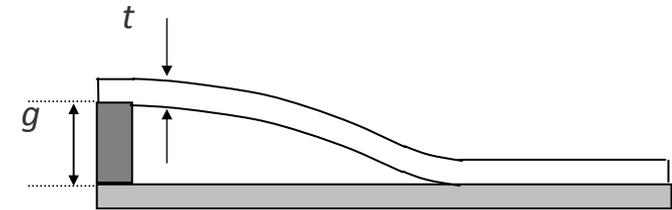
- **Use adhesive micro-contact law at interface**

- Polysilicon-Polysilicon interactions
- Surfaces properties from
  - AFM
  - Surface energy measured

In vacuum	$\varpi = 2.54 \text{ J/m}^2$
In air	$\varpi = 0.167 \text{ J/m}^2$

- Contact remains elastic

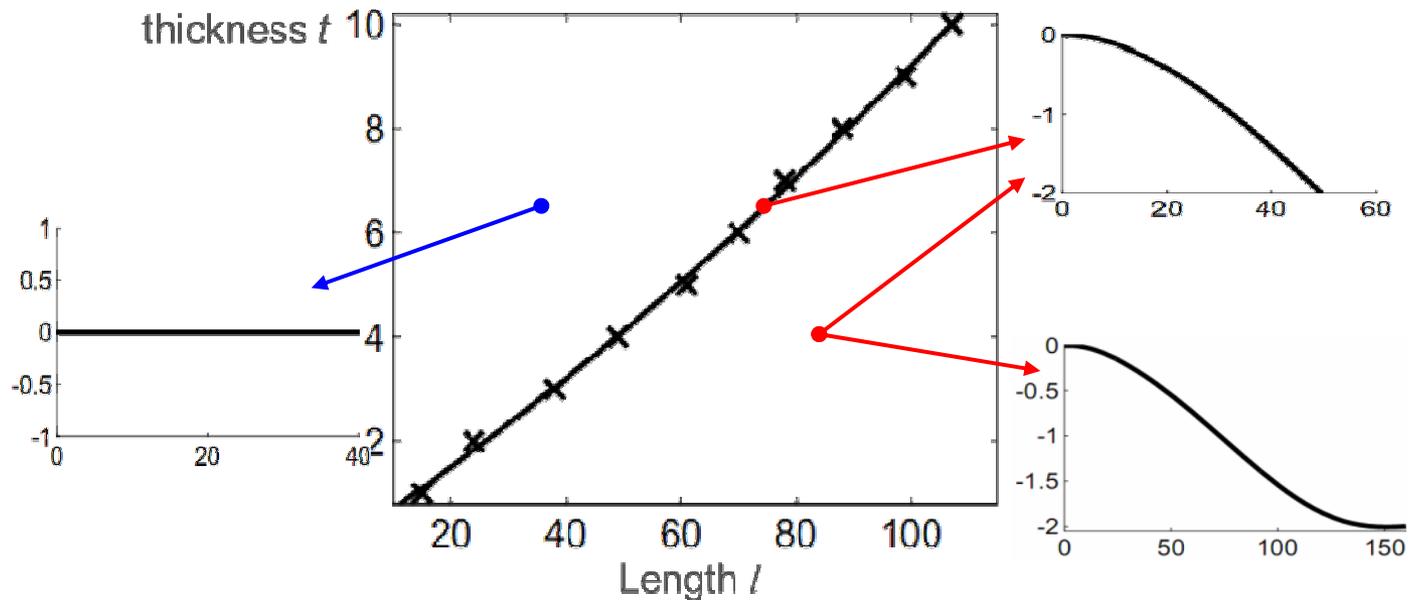
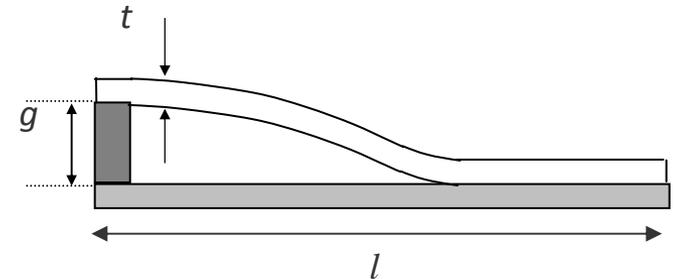
- **Validation vs literature experiments\***



\* W. M. van Spengen, R. Puers and I. De Wolf, "On the physics of stiction and its impact on the reliability of microstructures," *J. Adhesion Sci. Technol.*, vol. 17, no. 4, pp. 563–582, 2003 (Analytical)

\* M.P. de Boer, "Capillary adhesion between elastically hard rough surfaces," *Experim. Mech.*, vol. 47, pp. 171–183, 2007 (Experiment)

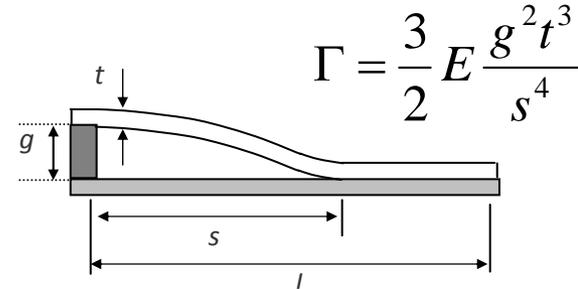
- Design example: cantilevers (2)**
  - Initial gap  $g = 2.0 \mu\text{m}$
  - Admissible thickness  $t$  ( $\mu\text{m}$ ) & length  $l$  ( $\mu\text{m}$ ) ???



# Validation



- **Literature\*:**
  - **Measures of apparent adhesion energy  $\Gamma$**
  - **Simplified models of  $\Gamma$**

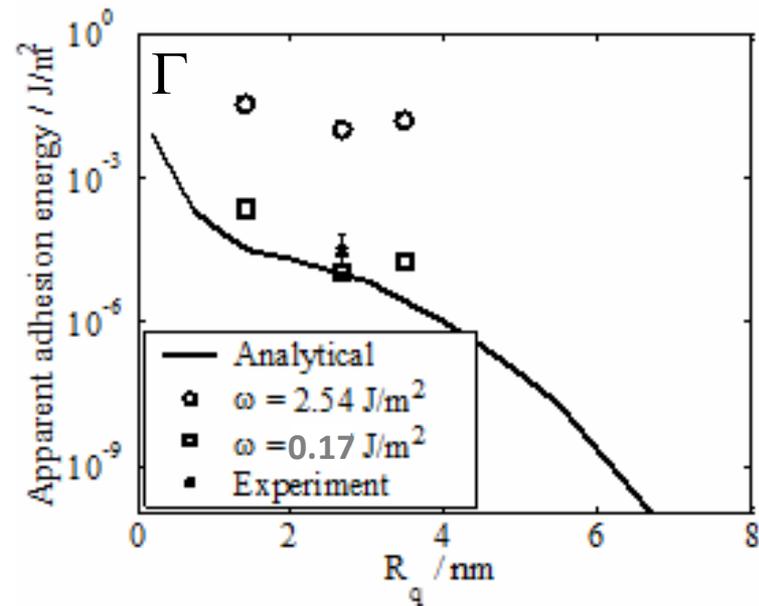


- **Numerical methods**
  - **Extract  $\Gamma$  from  $s$**
  - **Environmental effect**

In vacuum	$\varpi = 2.54 \text{ J/m}^2$
In air	$\varpi = 0.167 \text{ J/m}^2$

- **Different samples**
  - **Surface roughness**

Sample	A	B	C
$R_q$ (nm)	1.4	2.67	3.47



\* W. M. van Spengen, R. Puers and I. De Wolf, "On the physics of stiction and its impact on the reliability of microstructures," *J. Adhesion Sci. Technol.*, vol. 17, no. 4, pp. 563–582, 2003 (Analytical)

\* M.P. de Boer, "Capillary adhesion between elastically hard rough surfaces," *Experim. Mech.*, vol. 47, pp. 171–183, 2007 (Experiment)

# Elasto-plastic adhesive contact



- **Elasto-Plastic materials**
  - **Plastic deformations of asperities**
- **Repeated contact**

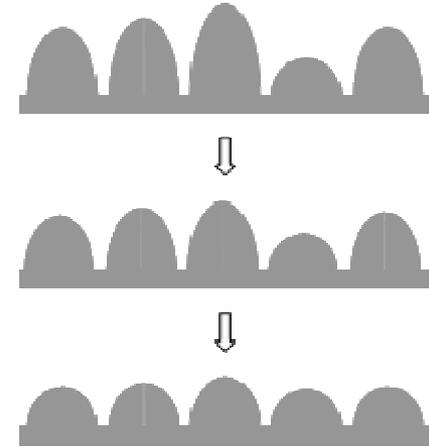
Tip radii  $R$  of a part of asperities  $\uparrow$   
Surface roughness  $R_q$   $\downarrow$



Adhesive forces  $\uparrow$



Stiction can appear after  
some cycles



- **Elasto-plastic adhesive contact model is needed !**

# Elasto-plastic adhesive contact



- **Basic idea**

- **Adhesive contact model of the elastic-plastically deformed of asperity**



Numerical results for an elasto-plastic loaded sphere in contact without adhesive forces

Maugis' adhesive contact theory is performed on the equivalent elastic deformed asperity

- **Asperity-based rough surface model**

- Plastic deformations of a loaded single asperity

- **Curve fitting of FE simulations\***

- Effect of maximum interference

$\delta_{\max}$  reached during loading

- Material parameters: yield  $S_Y$ ,

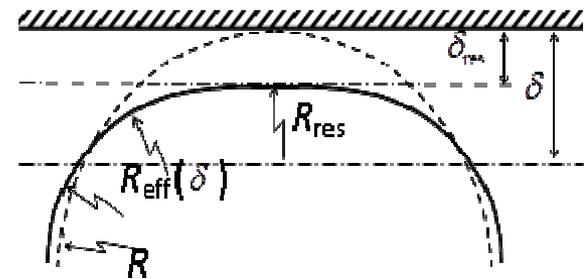
yield interference  $\delta_{CP}$

- **Residual interference**

$$\delta_{res} = \delta_{\max} \left(1 - \left(\frac{\delta_{CP}}{\delta_{\max}}\right)^{0.28}\right) \left(1 - \left(\frac{\delta_{CP}}{\delta_{\max}}\right)^{0.69}\right)$$

- **Residual tip radius**

$$R_{res} = R \left(1 + 1.275 \left(\frac{S_y}{E}\right)^{0.216} \left(\frac{\delta_{\max}}{\delta_{CP}} - 1\right)\right)$$



\* Etsion I., Kligerman Y., Kadin Y., Unloading of an elastic-plastic loaded spherical contact, International Journal of Solids and Structures 42 (2005) 3716–3729

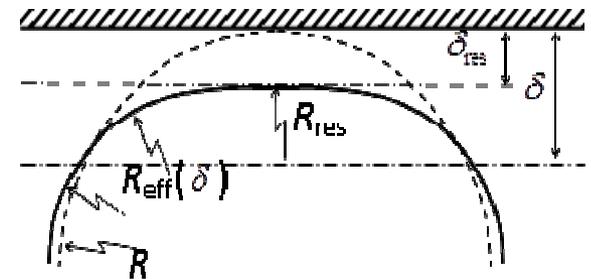
# Elasto-plastic adhesive contact



- **Adhesive unloading of a single deformed asperity**

- **Define an equivalent elastic asperity**

- Interference  $\delta_{\text{eff}} = \delta - \delta_{\text{res}}$
- Asperity tip radius  $R_{\text{eff}} = R_{\text{eff}}(R, \delta, \delta_{\text{max}})$



- **Apply Maugis**

- Extract adhesive-micro contact force

$$F_n = F_n(\delta - \delta_{\text{res}}, R_{\text{eff}})$$

\* Etsion I., Kligerman Y., Kadin Y., Unloading of an elastic-plastic loaded spherical contact, International Journal of Solids and Structures 42 (2005) 3716–3729

# Elasto-plastic adhesive contact

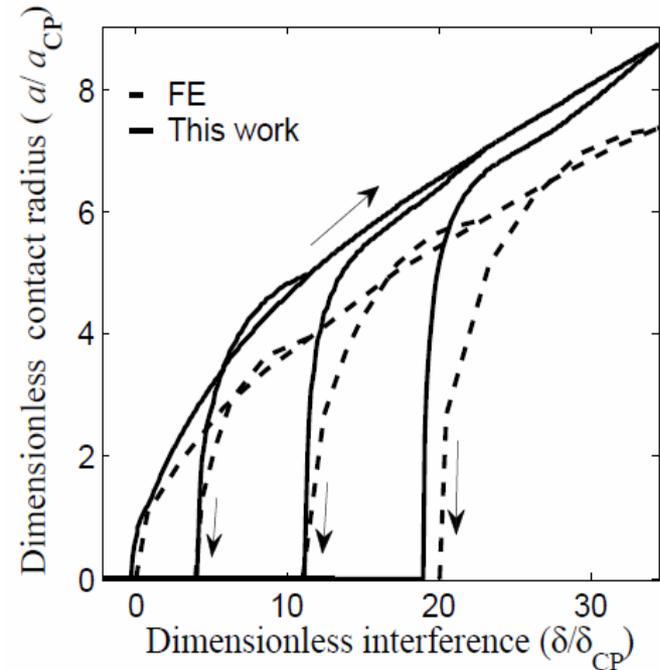
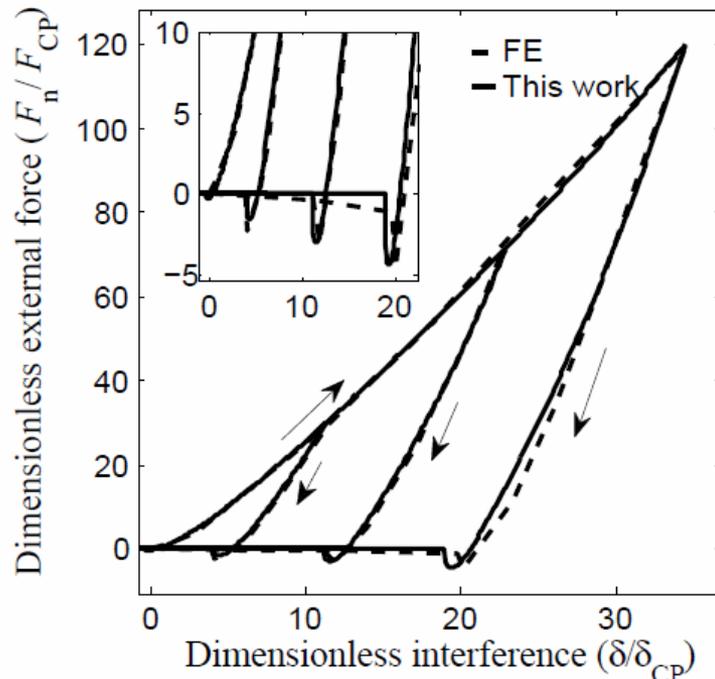


- Adhesive loading/unloading of a single asperity

- Material: Ru

$R$	$E$	$\nu$	$S_Y$	$z_0$	$\varpi$
4 nm	410 GPa	0.3	3.42 GPa	0.169 nm	1 J/m <sup>2</sup>

- Model vs FE\*



\* 28Y. Du, L. Chen, N. McGruer, G. Adams, and I. Etsion, Finite element model of loading and unloading of an asperity contact with adhesion and plasticity," Journal of Colloid and Interface Science 312, 522 - 528 (August 2007)

# Elasto-plastic adhesive contact

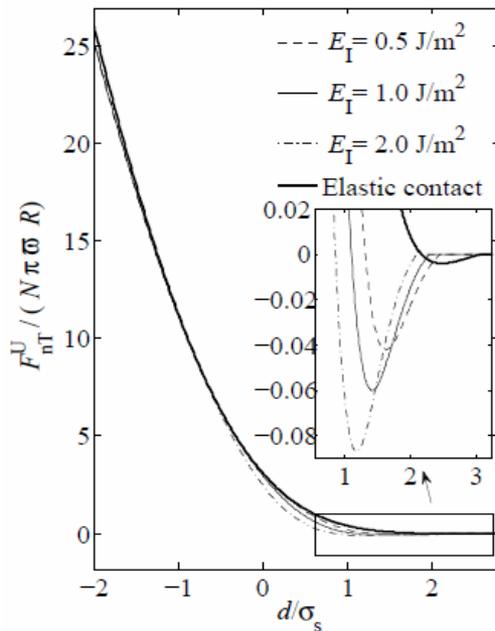


- Adhesive unloading of rough surfaces

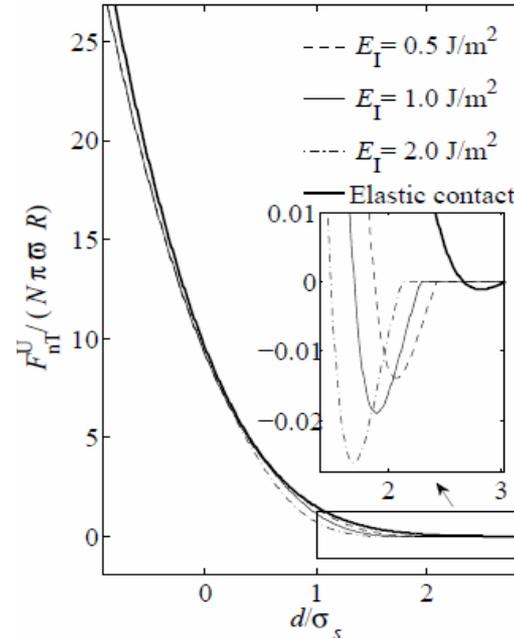
- Different Ru samples

Sample	A	B	C
$R_q$ (nm)	2.03	3.99	7.81

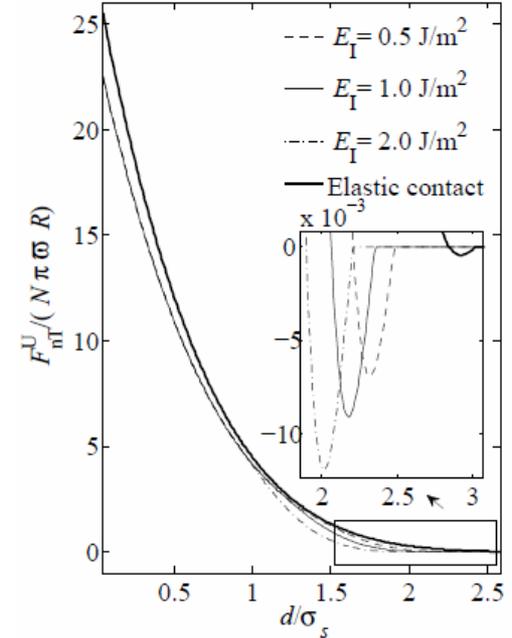
- Effect of impact energy at pull-in on plastic deformations



(a) Sample A



(b) Sample B



(c) Sample C

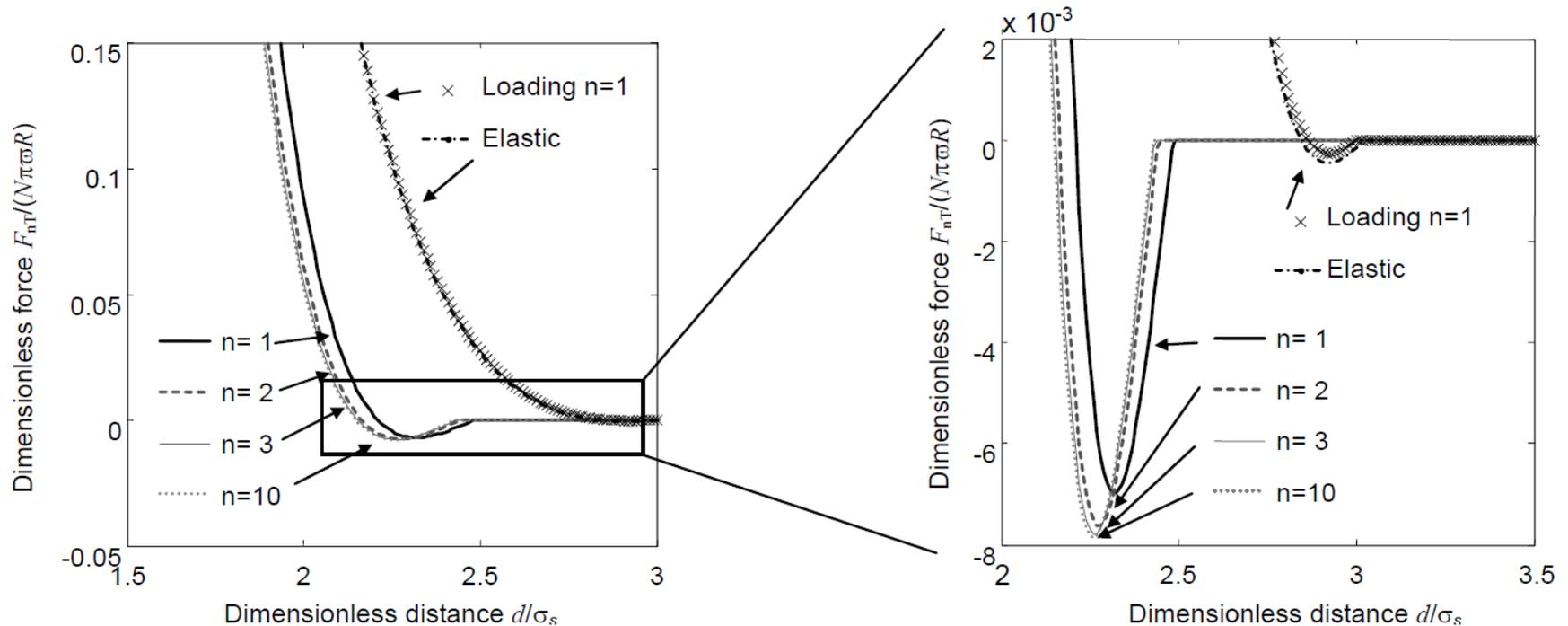
# Elasto-plastic adhesive contact



- Time life of MEMS

- Repeated loading/unloading → changes in surfaces profile
- Asperity profile can be updated by tracking history  $\delta_{\max}(h)$
- Ru sample

Sample	Rq (nm)	$E_T$ (J/m <sup>2</sup> )
C	7.81	0.5



# Conclusions



- The adhesion between the contact surfaces has large influence on the design of MEMS switches, and need to be considered carefully
- The adhesive work and the surface roughness are the main factors of adhesive force
- The analytical adhesive contact results can be combined with FEM to predict the stiction of more complicated structures
- Effect of plasticity can be accounted for
- The other kinds of adhesive forces, such as capillary force, electrostatic force from dielectric charging, are not considered

***Thank you!***