

# **ON THE MODELLING OF ADHESIVE CONTACT AND STICTION FAILURE IN MICRO-SWITCHES**

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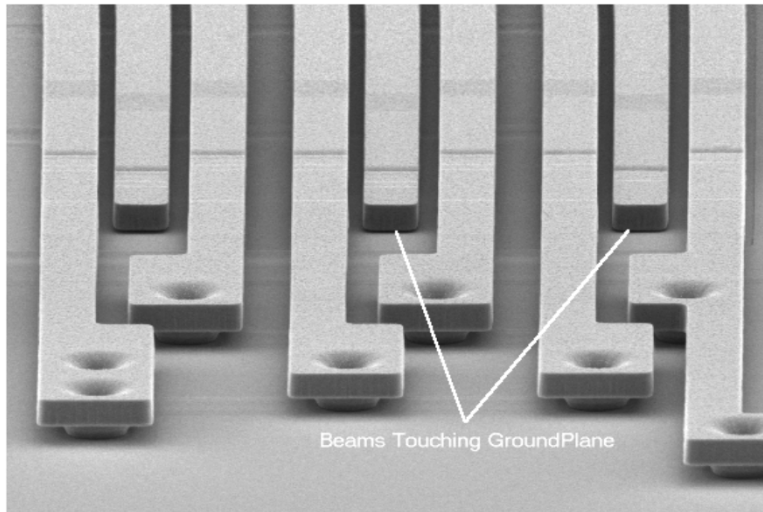
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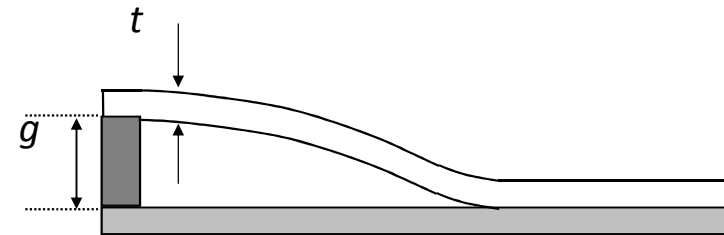
- 1. Introduction**
- 2. Micro-scale model**
- 3. Multi-scale model**
- 4. Elasto-plastic adhesive contact**
- 5. Conclusions**

## Stiction failure in MEMS (major issue for micro-switches)



*Stiction failure in a MEMS sensor*

*( Jeremy A. Walraven Sandia National  
Laboratories. Albuquerque, NM USA)*



### Reason

Relatively high surface area:  
volume ratio (1,000:1 to  
10,000:1  $\text{m}^{-1}$ )

### Adhesive forces

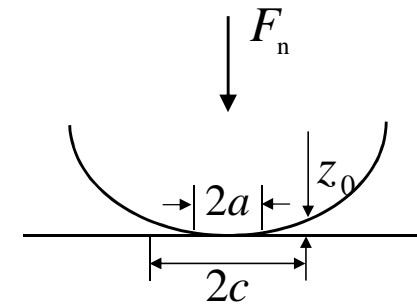
Electrostatic force, Van der  
Waals force, Capillary force,

...

The risk of in-use stiction increases when plasticity is involved during contact.

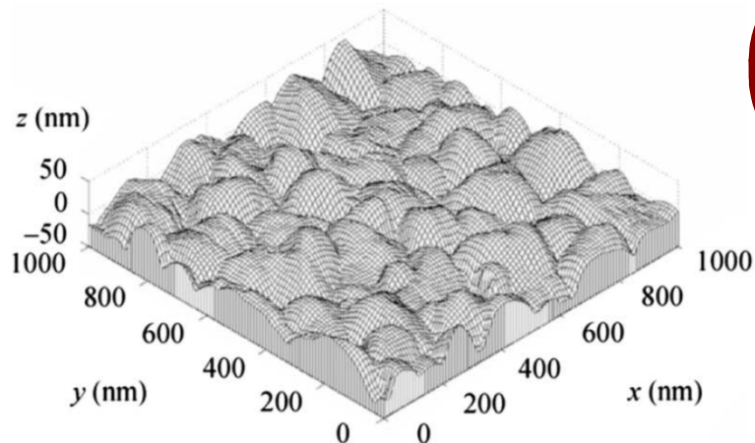
## Multi-scale approach

At the micro-scale



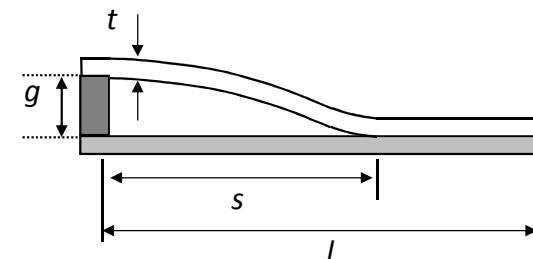
Single asperity subject to adhesive-micro contact forces

Contact model between rough surfaces  
→ prediction of the adhesive force



Integration with FEM

At the macro-scale



## 1. Introduction

## 2. Micro-scale model

- Single asperity adhesive-elastic contact
- Statistical model for rough surface

## 3. Multi-scale Model

## 4. Elasto-plastic adhesive contact

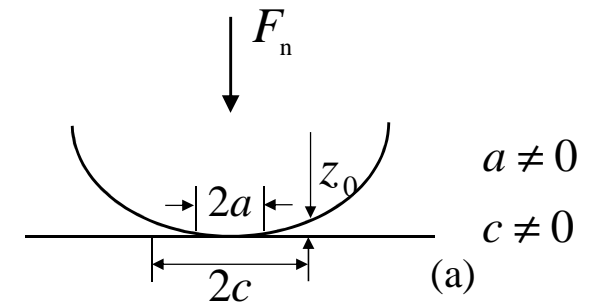
## 5. Conclusions

## Single asperity adhesive-elastic contact (Hertz) theories

- **Johnson, Kendall, and Roberts (JKR)**

- The surface forces are short ranged and act only inside the contact area

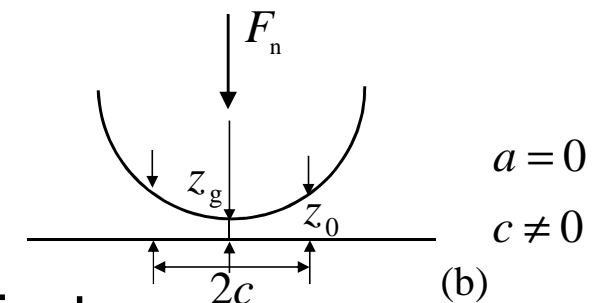
⇒ { Ideal for compliant materials with high surface energy and large contact curvature surface



- **Derjaguin, Muller and Toporov (DMT)**

- Accounts for the long-ranged adhesive forces acting outside the contact area

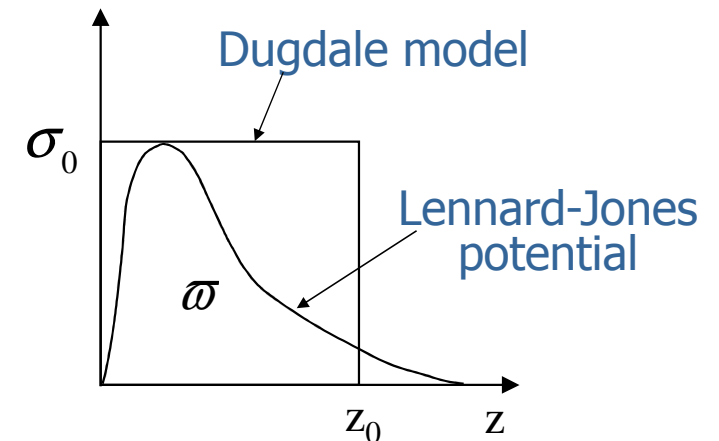
⇒ { Well suited for harder, less compliant materials with low surface energy and small asperity tip radius



- **Maugis model**

- for all elastic materials
- provides transition solutions for intermediate cases between the JKR and DMT regimes
- is based on a Dugdale assumption for interaction potential

- Constant traction  $\sigma_0$  within a critical value of separation  $z_0$
- Zero traction for gap larger than  $z_0$



Work of adhesion:  $\varpi = \sigma_0 \cdot z_0$

# Single asperity adhesive-micro contact

The Maugis transition parameter  $\lambda$  is defined in terms of the surface properties:

$$\lambda = \frac{2 \varpi^{2/3} R^{1/3}}{z_0 (\pi K^2)^{1/3}}$$

Work of adhesion ←      → asperity radius

equivalent elastic constant

⇒

$$\varpi \uparrow, R \uparrow, K \downarrow \Rightarrow \lambda \uparrow \quad \text{JKR model (short-ranged)}$$

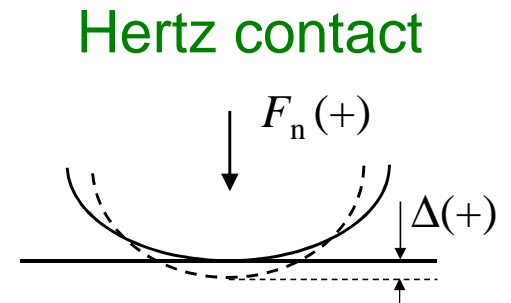
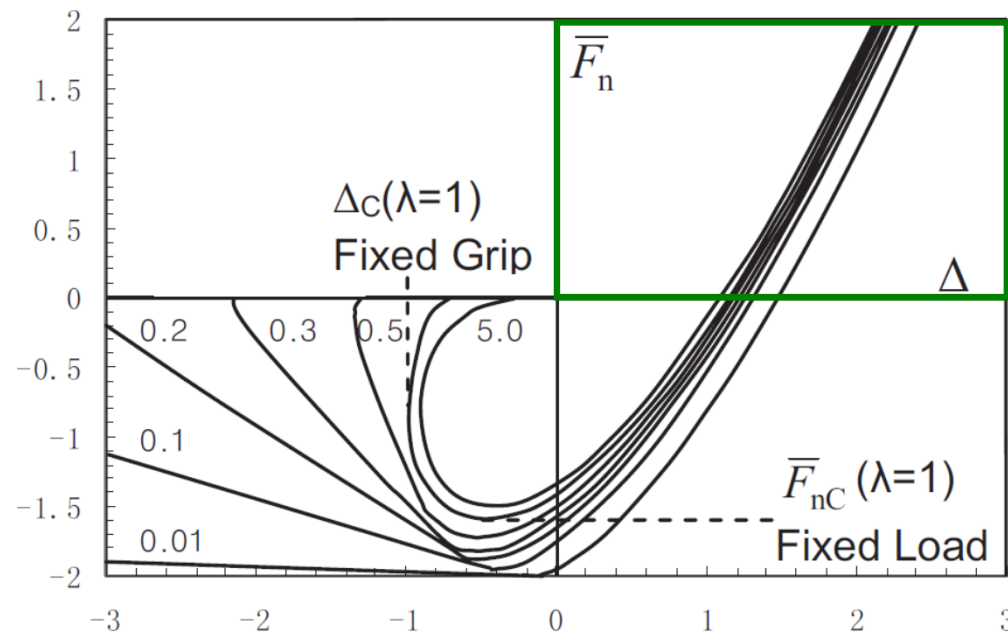
$$\varpi \downarrow, R \downarrow, K \uparrow \Rightarrow \lambda \downarrow \quad \text{DMT model (long-ranged)}$$



# Single asperity adhesive-micro contact

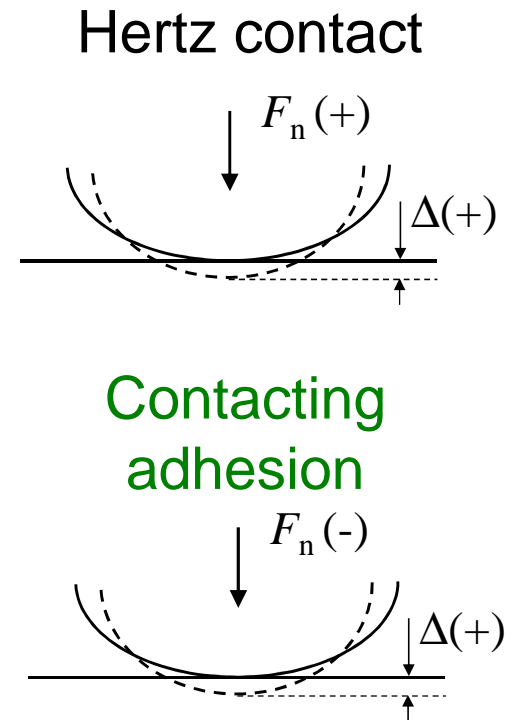
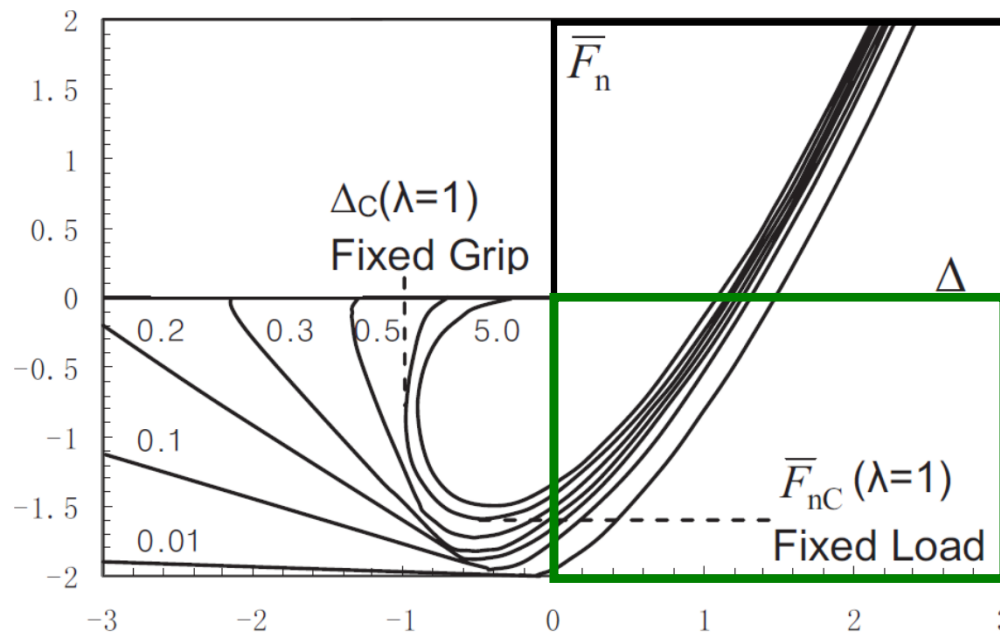
- **Maugis transition solution**

Calculation of the load in terms of the deflection for different values of the transition parameter  $\lambda$



- Maugis transition solution

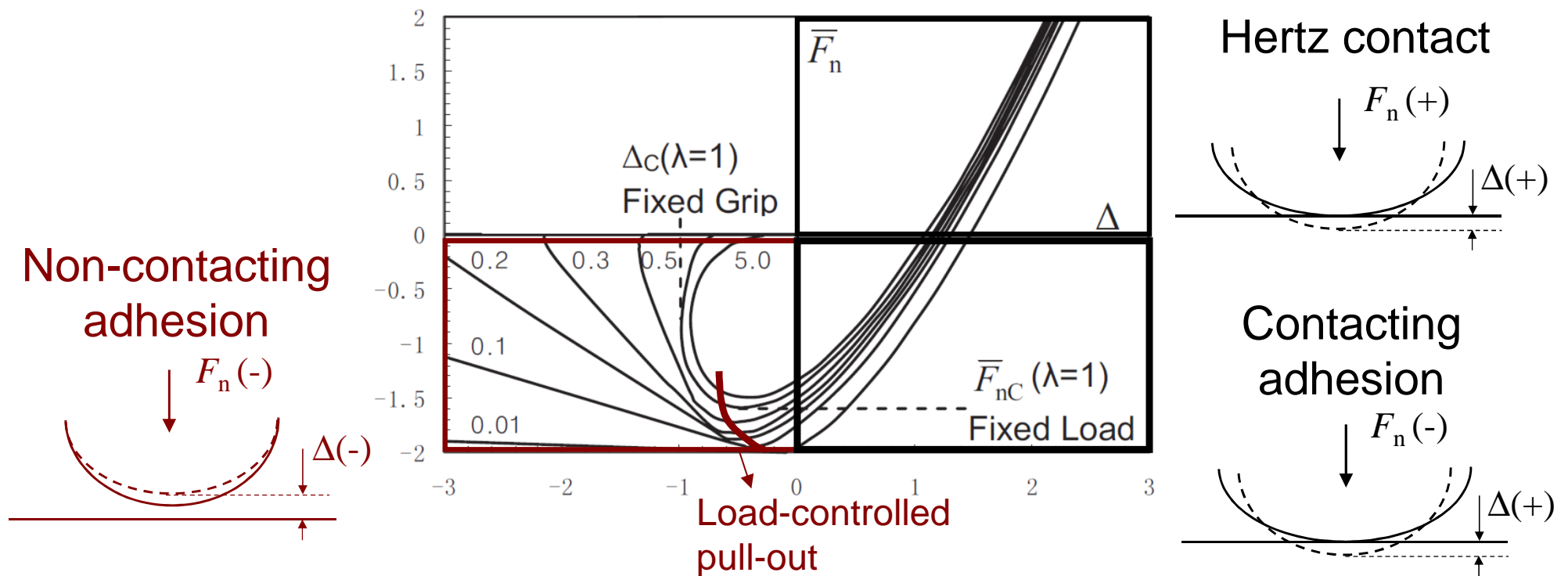
Calculation of the load in terms of the deflection for different values of the transition parameter  $\lambda$



# Single asperity adhesive-micro contact

- Maugis transition solution

Calculation of the load in terms of the deflection for different values of the transition parameter  $\lambda$



## Statistical model for rough surfaces

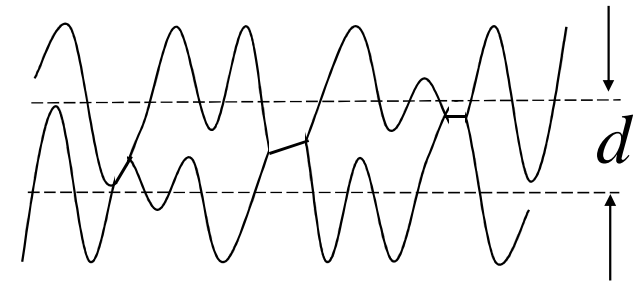
- The rough surface is described by a collection of spherical asperities with constant tip radius.

The heights  $h$  have a statistical distribution:

$$\varphi(h) = \frac{1}{\sigma \sqrt{2\pi}} \exp\left(\frac{-h^2}{2\sigma^2}\right)$$



- Rough surfaces interaction
  - Reduced number of interacting asperities



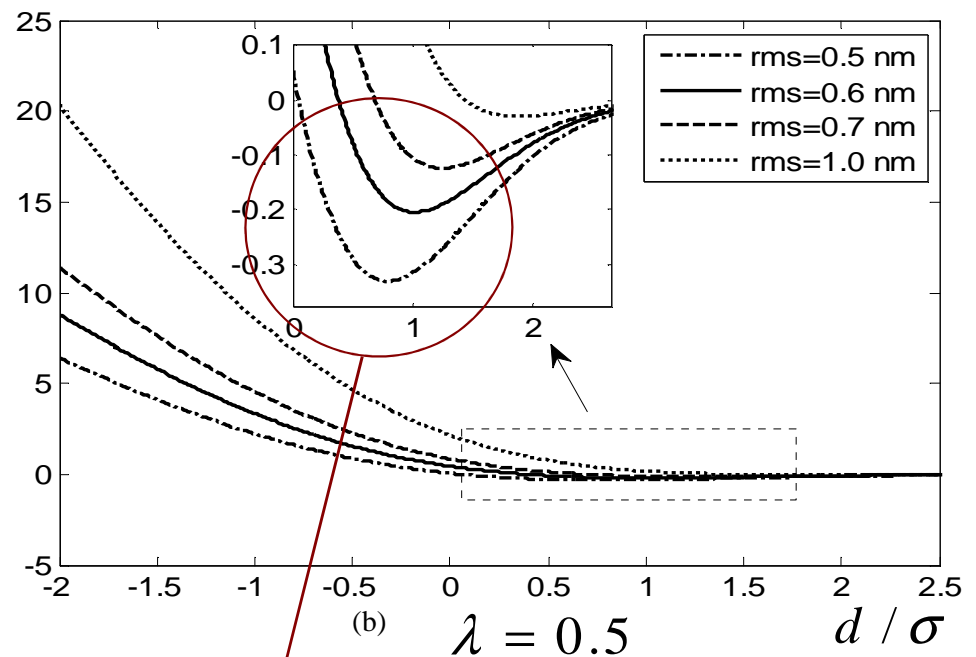
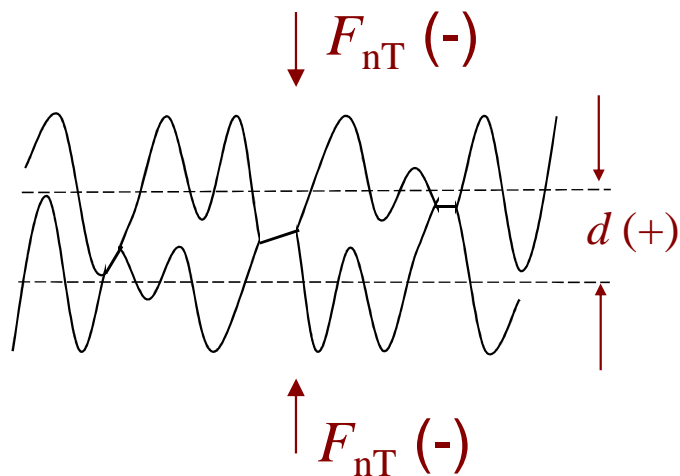
- The distance between the surfaces is defined in terms of distance  $d$

The micro adhesive contact forces between rough surfaces may be computed

by integration of the Maugis solution using

$$\varphi(h) = \frac{1}{\sigma \sqrt{2\pi}} \exp\left(\frac{-h^2}{2\sigma^2}\right)$$

Dimensionless  
contact force  $\frac{F_{nT}}{N \pi \omega R}$



Responsible for stiction

Contact  
distance

## 1. Introduction

## 2. Micro-scale model

## 3. Multi-scale Model

- **Design example: cantilever beam (FEM)**
- **Polysilicon to polysilicon interaction**
- **Validation with experiments**

## 4. Elasto-plastic adhesive contact

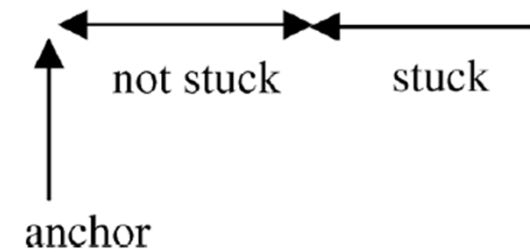
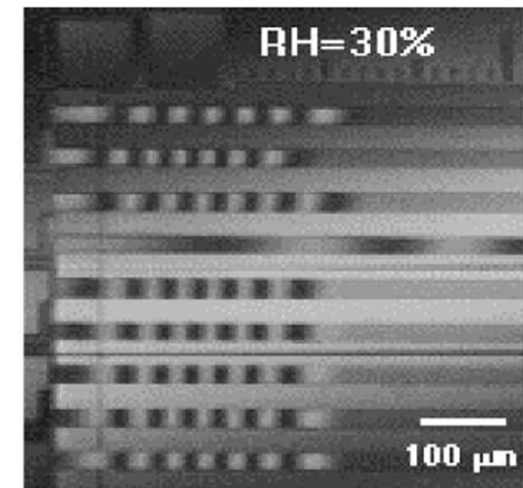
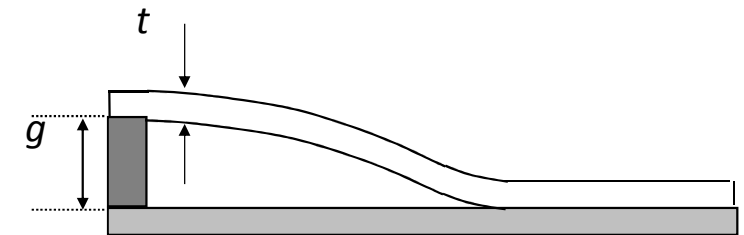
## 5. Conclusions

## Design example: cantilever beam entering into contact with the substrate

- Finite element model
  - Timoshenko beams
- Use of adhesive contact law at interface
  - Polysilicon-Polysilicon interactions
  - Surfaces properties from
    - AFM
    - Surface energy measured

In vacuum	$\gamma = 2.54 \text{ J/m}^2$
In air	$\gamma = 0.167 \text{ J/m}^2$

- Contact remains elastic
- Validation vs literature experiments\*

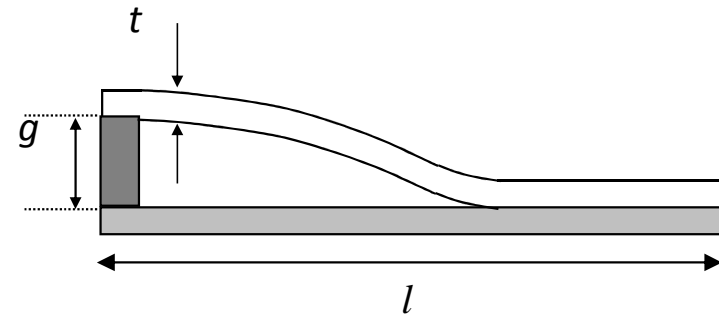


\* W. M. van Spengen,, R. Puers and I. De Wolf, "On the physics of stiction and its impact on the reliability of microstructures," *J. Adhesion Sci. Technol.*, vol. 17, no. 4, pp. 563–582, 2003 (Analytical)

\* M.P. de Boer, "Capillary adhesion between elastically hard rough surfaces," *Experim. Mech.*, vol. 47, pp. 171–183, 2007 (Experiment)

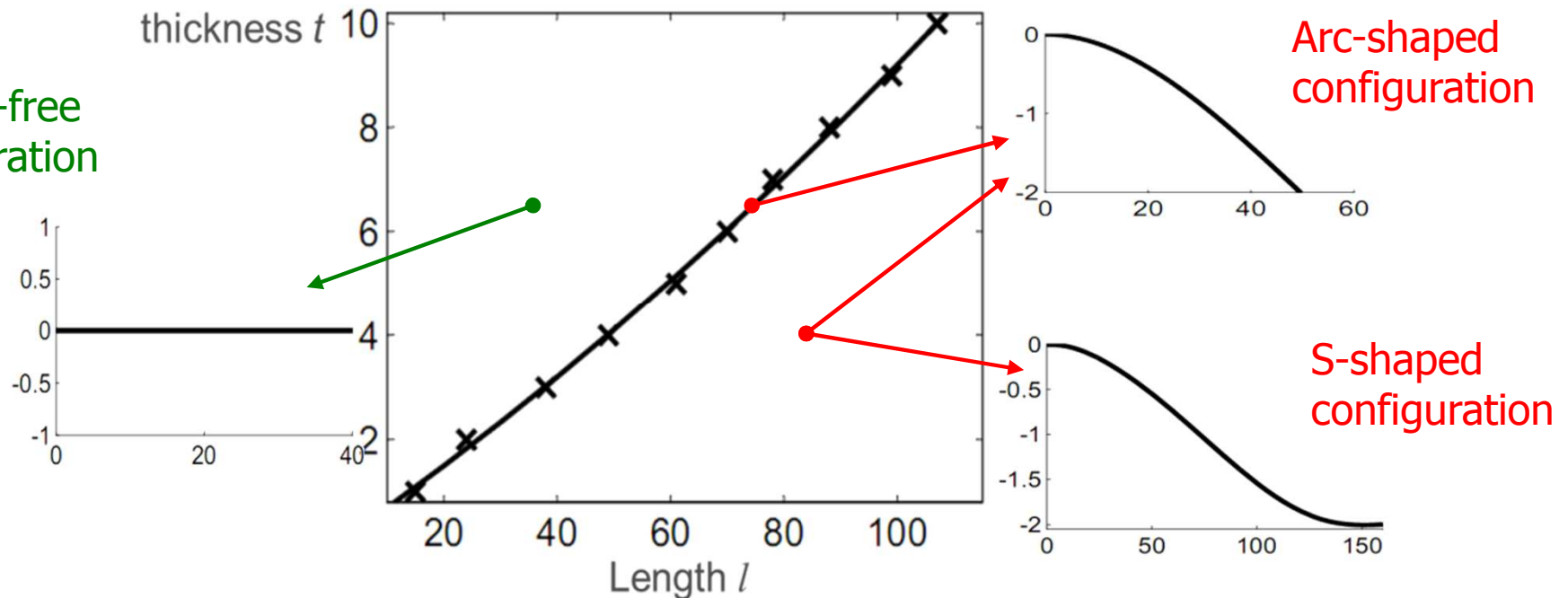
Design example: cantilever beam

Initial gap  $g = 2.0 \mu\text{m}$



The design limitations avoiding in-use stiction are calculated in terms of the beam's geometrical properties (thickness and length) for  $\varpi = 2.54 \text{ J/m}^2$

Stiction-free  
configuration





## 1. Introduction

## 2. Micro-scale model

## 3. Multi-scale Model

## 4. **Elasto-plastic adhesive contact**

- **Plastic deformation of a loaded single asperity**
- **Adhesive unloading of a single deformed asperity**
- **Adhesive unloading of rough surfaces**
- **Lifetime of MEMS**

## 5. Conclusions

- Extension of the multiscale model → plastic deformations of asperities
- In case of repeated contacts (cycling loading)

The height distribution and the tip radii  $R$  of asperities change until accommodation is reached

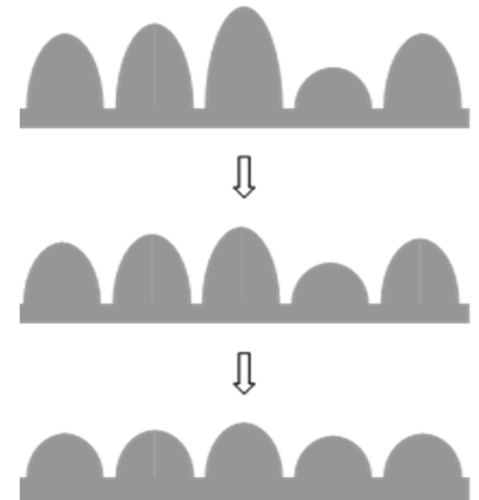
Surface roughness  $R_q$  ↓



Adhesive forces ↑



**Stiction may appear after  
a few cycles**



→ Elasto-plastic adhesive contact model is required !

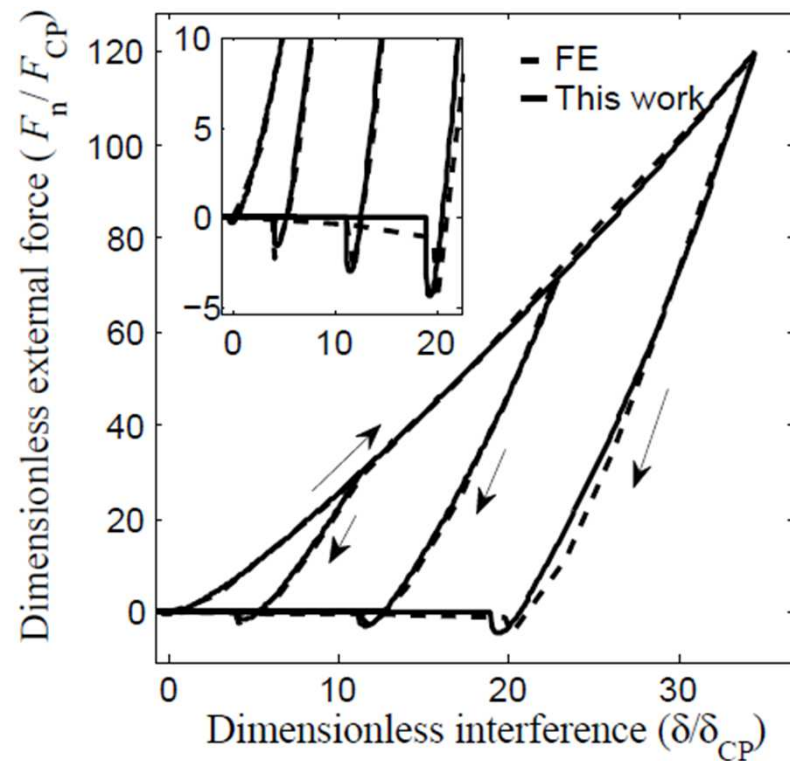
## Basic idea

- Adhesive contact model of the elastic-plastically deformed asperity
  1. The elasto–plastic deformation resulting from the contact of a single loaded sphere is first solved without considering adhesive effect.
  2. The Maugis' adhesive contact theory is performed on the equivalent elastic deformed asperity.
- Asperity-based rough surface model based on the statistical distribution of asperities.

## Adhesive loading/unloading of a single asperity

- Material: Ru
- Model vs FE\*

$R$	$E$	$\nu$	$S_Y$	$z_0$	$\bar{\omega}$
4 nm	410 GPa	0.3	3.42 GPa	0.169 nm	1 J/m <sup>2</sup>



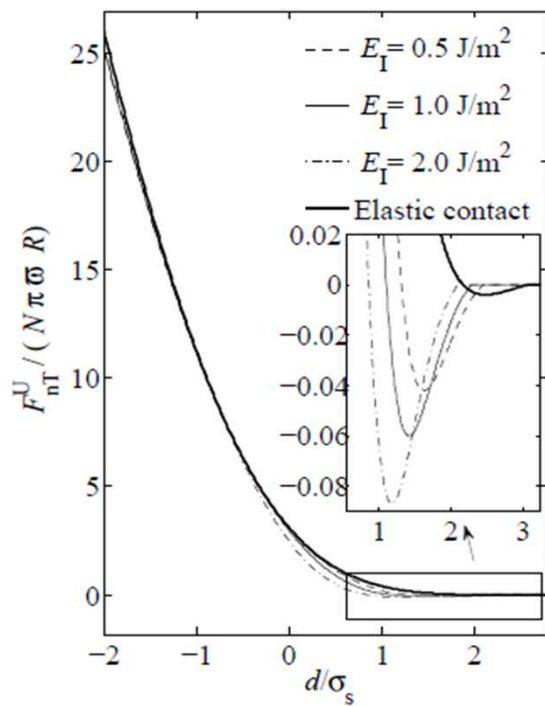
\* 28Y. Du, L. Chen, N. McGruer, G. Adams, and I. Etsion, Finite element model of loading and unloading of an asperity contact with adhesion and plasticity," Journal of Colloid and Interface Science 312, 522 - 528 (August 2007)

## Adhesive contact forces during unloading

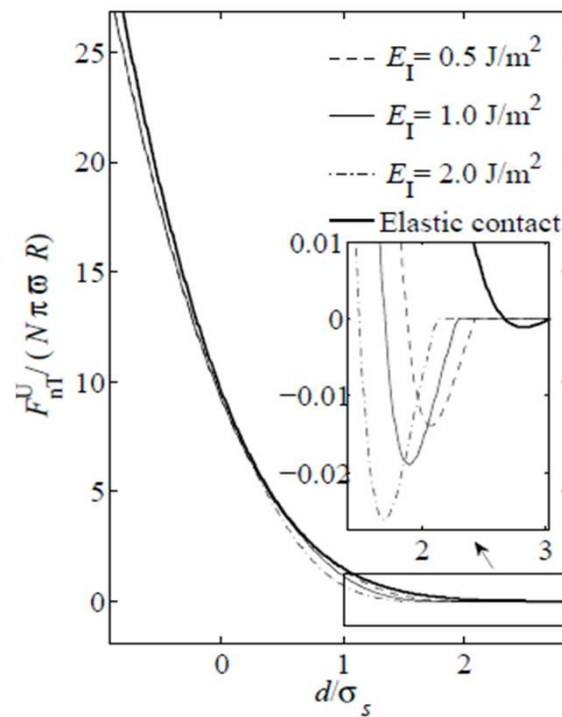
- For different Ru surface samples

Sample	A	B	C
$R_q$ (nm)	2.03	3.99	7.81

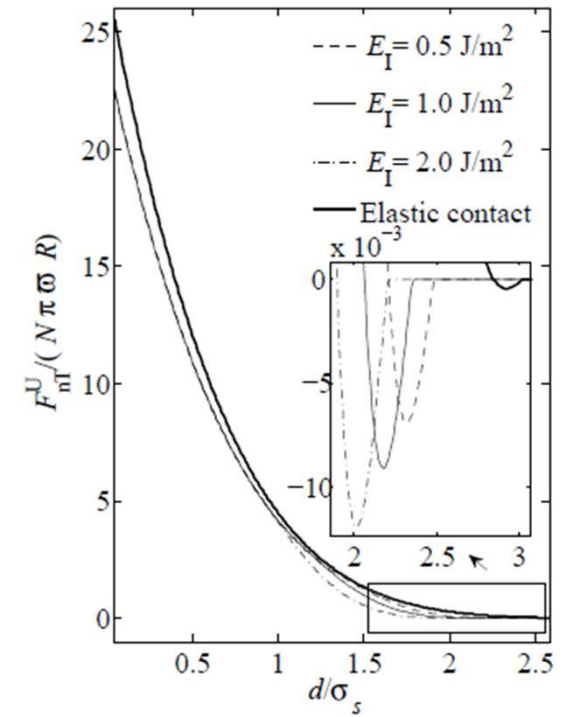
- Effect of impact energy at pull-in on plastic deformations



(a) Sample A



(b) Sample B

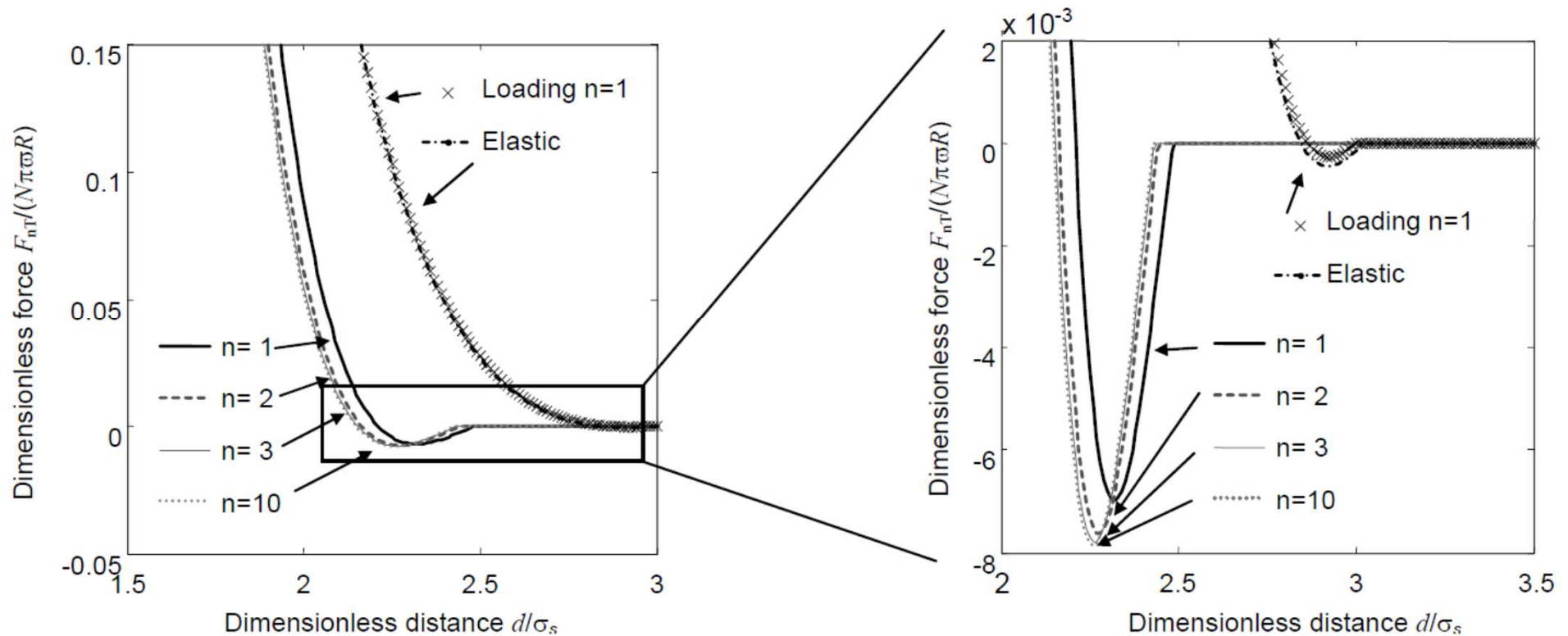


(c) Sample C

## Lifetime of MEMS

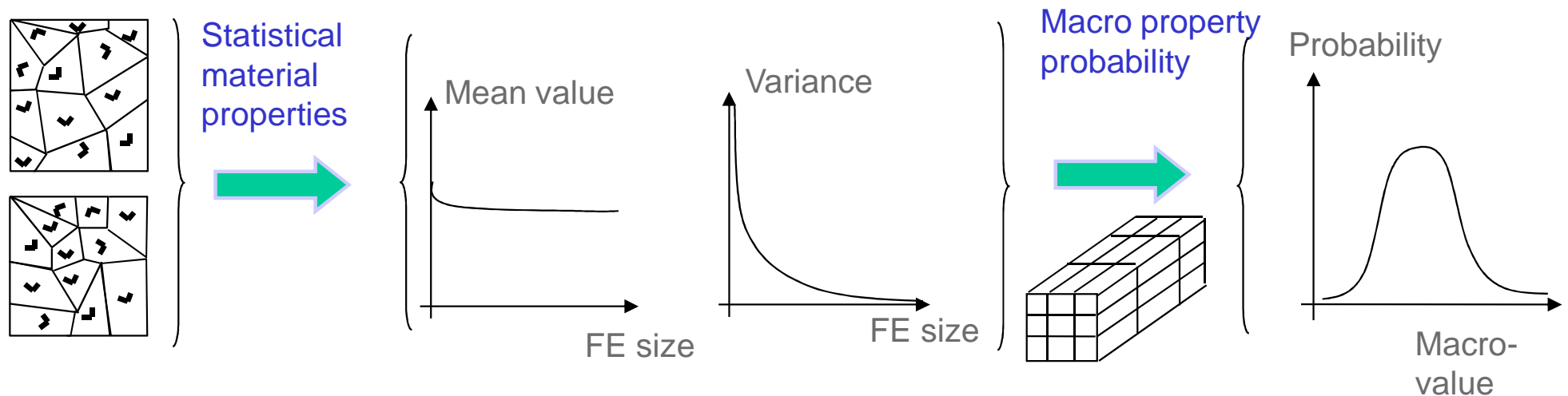
- Repeated loading/unloading  $\Rightarrow$  changes in surfaces profile
- Ru sample

Sample	Rq (nm)	$E_I$ (J/m <sup>2</sup> )
C	7.81	0.5



- The adhesion between the contact surfaces has a large influence on the design of micro-switches and needs to be considered carefully.
- The adhesive work and the surface roughness are the main factors to take into account.
- The analytical adhesive contact results can be combined with FEM to predict the stiction of more complicated structures.
- Effect of plasticity can be accounted for.
- The other kinds of adhesive forces, such as capillary force, electrostatic force from dielectric charging, are not considered.

- 3-scale modeling
  - MEMS
  - Separation of length scale violated
  - Uncertainties should be considered



- Application to robust design (Stiction risk, Q-factor range)
- 3SMVIB MNT.ERA-NET project
  - Open-Engineering, V2i, ULg (Belgium)
  - Polit. Warszawska (Poland)
  - IMT, Univ. Cluj-Napoca (Romania)





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**Thank you for your attention.**