

The instability strip of ZZ Ceti white dwarfs and its extension to extremely low mass pulsators

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Introduction of Time-Dependent Convection (TDC):

Van Grootel et al. 2012, A&A, 539, 87

Extension to Extremely Low Mass (ELM) pulsators: Van Grootel et al., ApJ, in press

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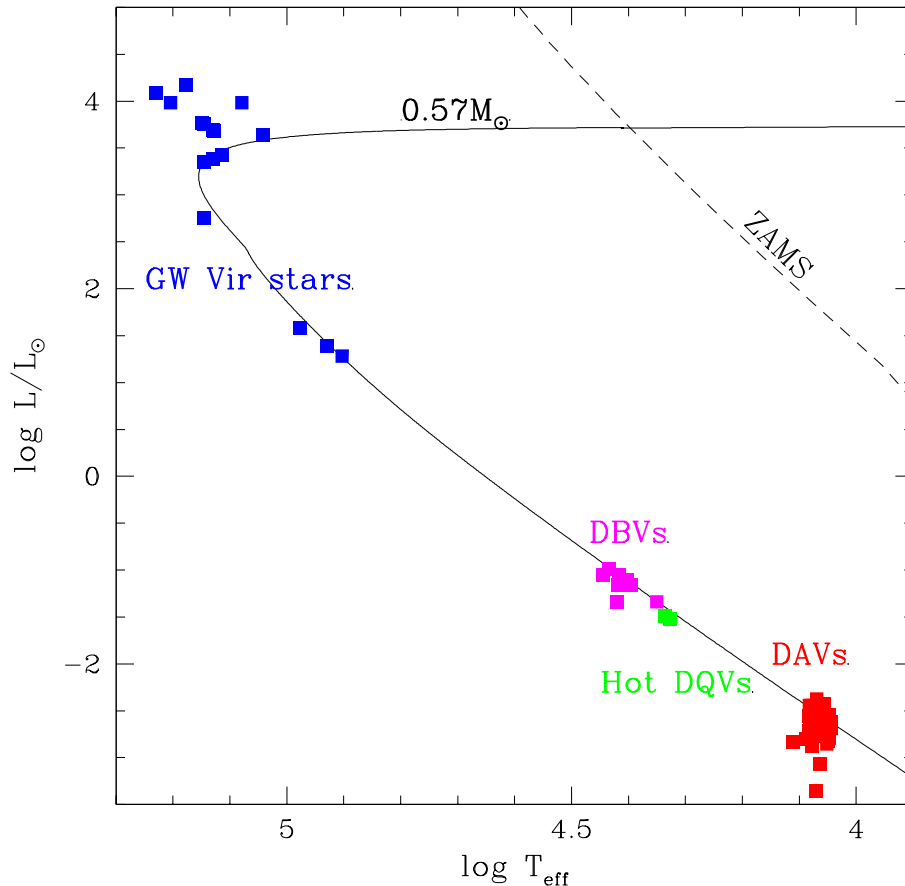
(2) Université de Montréal, Canada

1. Introduction to ZZ Ceti, DA white dwarfs pulsators

1. White dwarfs

Late stages of evolution of ~97% of stars in the Universe

DA (H-rich atmosphere): ~80%; DB (no/little H atmosphere): ~20% of WDs



4 types of g-mode pulsators along the cooling sequence:

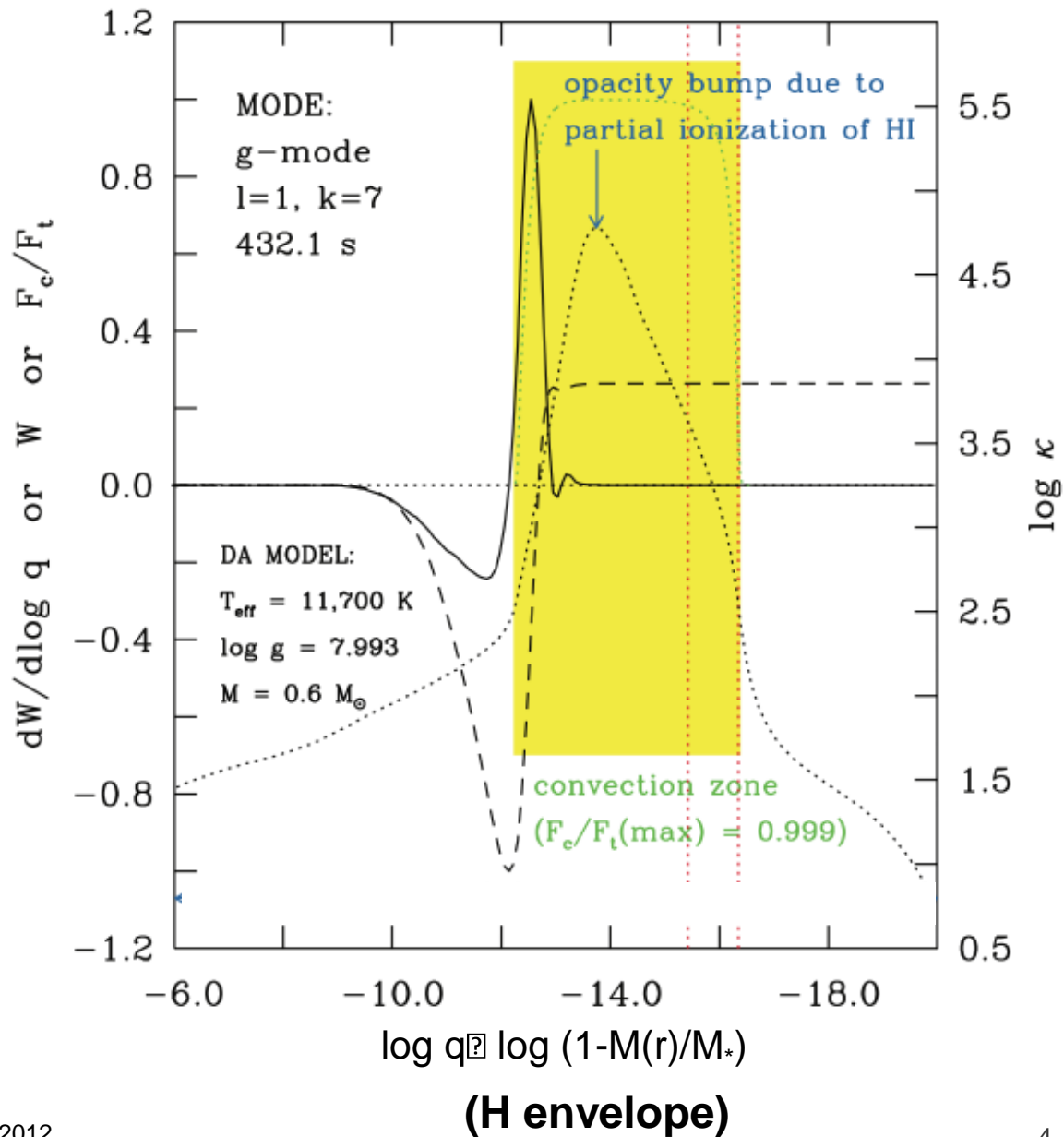
- GW Vir stars (He/C/O atmospheres)
 $T_{\text{eff}} \sim 120,000$ K, discovered in 1979
 - V777 Her stars (He-atmosphere), 1982
 $T_{\text{eff}} \sim 25,000$ K
 - Hot DQ stars (C-rich/He atmosphere)
 $T_{\text{eff}} \sim 20,000$ K, discovered in 2007
 - ZZ Ceti stars (H-atmosphere, DA)
 $T_{\text{eff}} \sim 12,000$ K, discovered in 1968
- Most numerous (~160 known including SDSS+Kepler)

From Saio (2012), LIAC40 proceedings

Excitation mechanism of ZZ Ceti stars (general picture)

- Don Winget (1981):
H recombination around $T_{\text{eff}} \sim 12,000$ K
 \Rightarrow envelope opacity increase
 \Rightarrow strangle the flow of radiation
 \Rightarrow modes instabilities
- Pulsations are destabilized at the base of the convection zone
 (details: e.g. Van Grootel et al. 2012)

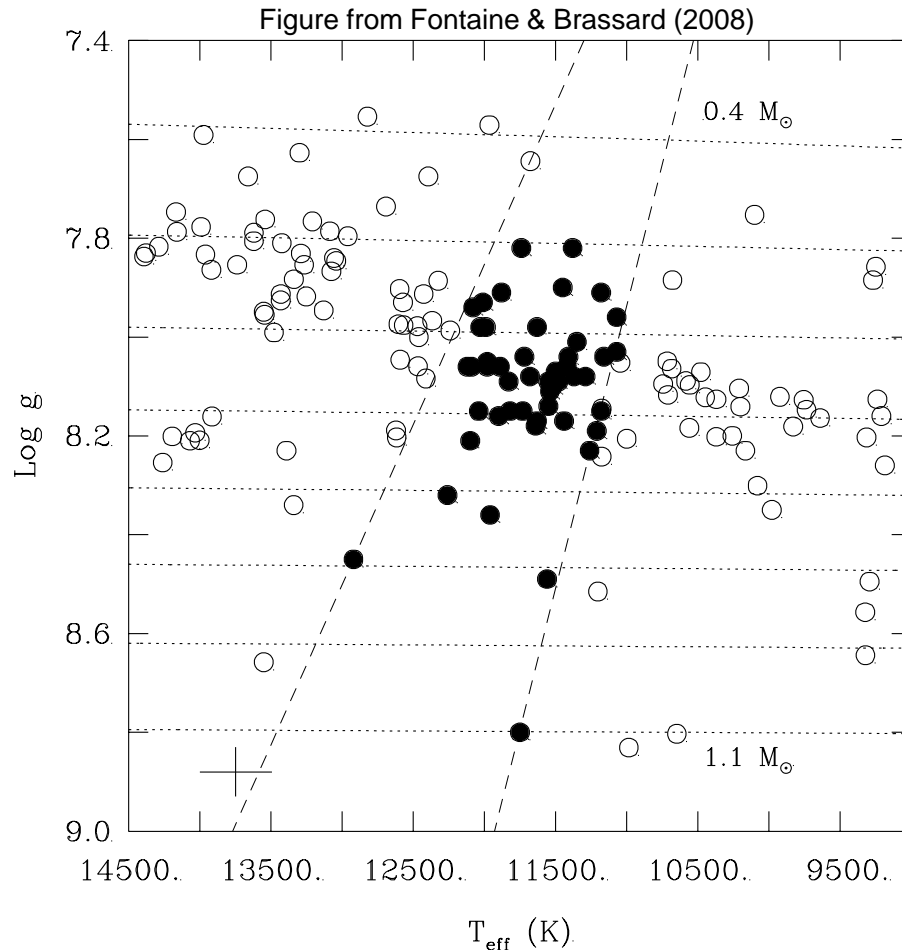
“convective driving”



1. Pulsating DA white dwarfs

Empirical ZZ Ceti instability strip (classic view)

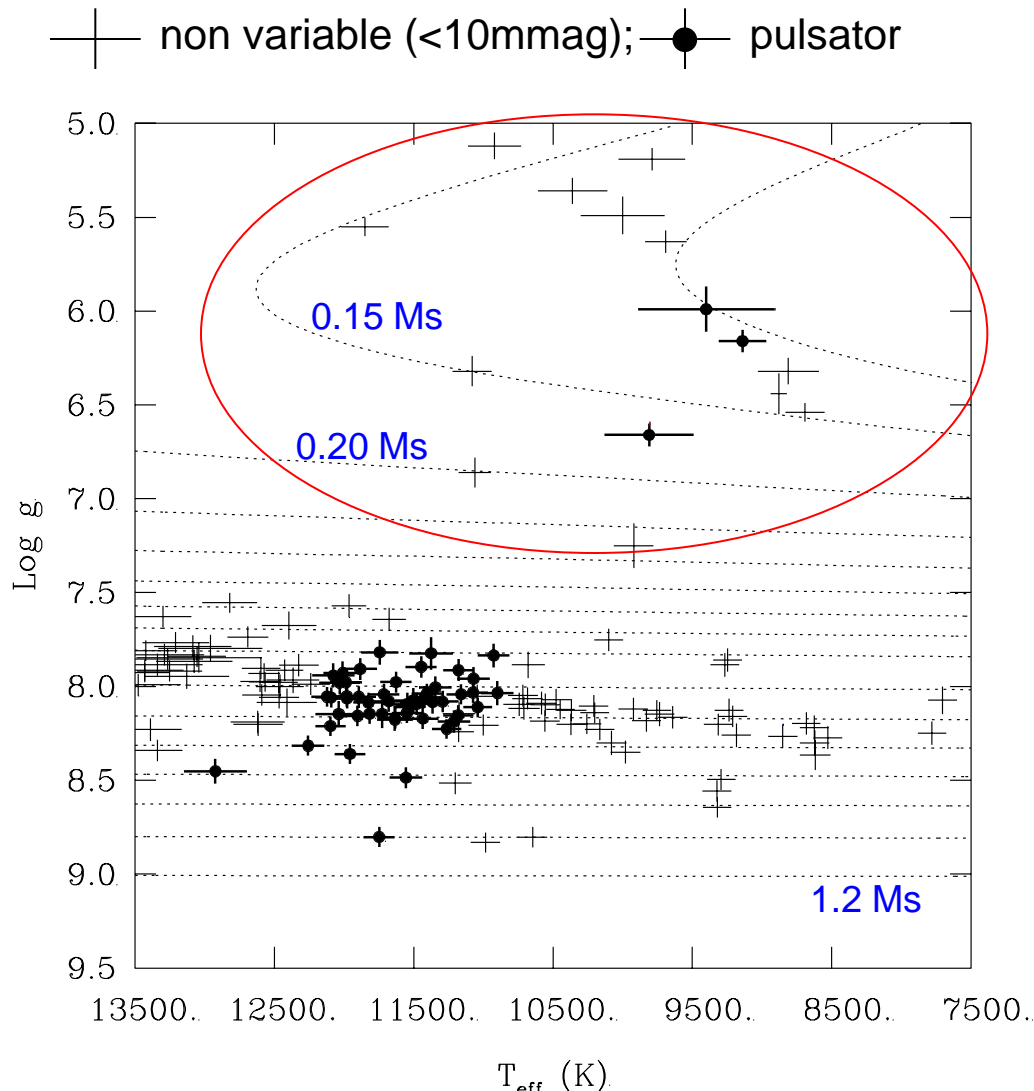
- Observed pulsator ; ○ non-variable DA white dwarf



- Multiperiodic pulsators, observed period range: 100-1500 s (g-modes)
- Reliable atmospheric parameters: work of Bergeron et al., $ML2/\alpha=0.6$
- Long-term observational efforts: Montreal (Gianninas et al.), Texas (McGraw et al.), Brazil (Kepler et al.), etc. + SDSS
- (most probably) a **pure** strip
- $\log g/T_{\text{eff}}$ correlation (with a more pronounced slope for red edge): the lower $\log g$, the lower edge T_{eff}

1. Pulsating DA white dwarfs

Empirical ZZ Ceti instability strip (2012 view)



~40 Extremely Low Mass (ELM)
DA white dwarfs known
(Kilic et al., Brown et al. 2010-2012)

Spectroscopic estimates from model
atmospheres of D. Koester, $ML2/\alpha=0.6$

Hermes et al. (2012a,b):

3 ELM pulsators

(SDSS J1840+6423, J1112+1117, J1518+0658)

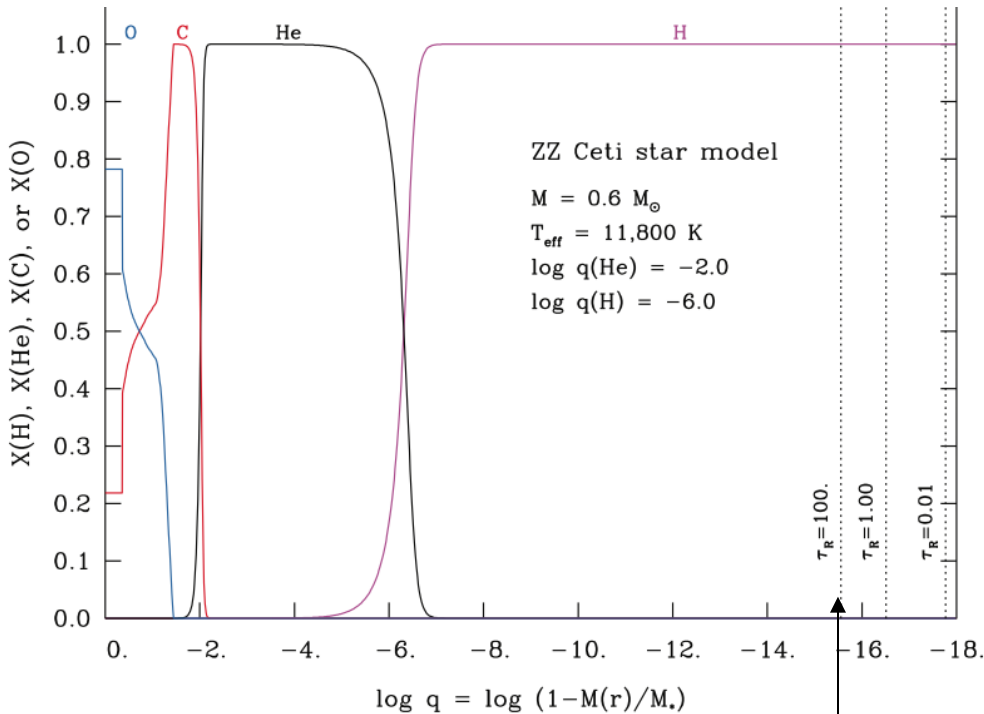
Multiperiodic pulsators, 1500-5000 s

2. Evolutionary ZZ Ceti Models

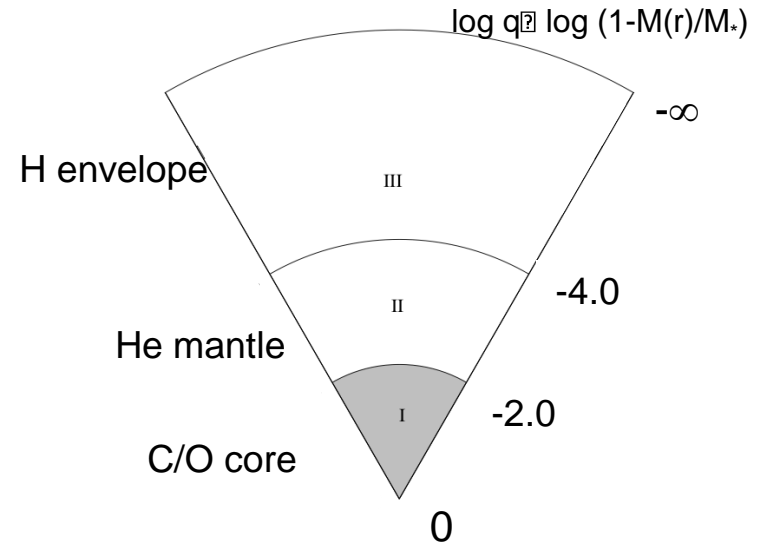
2. Evolutionary ZZ Ceti models

- A standard ZZ Ceti model (C/O core)

“onion-like” stratification

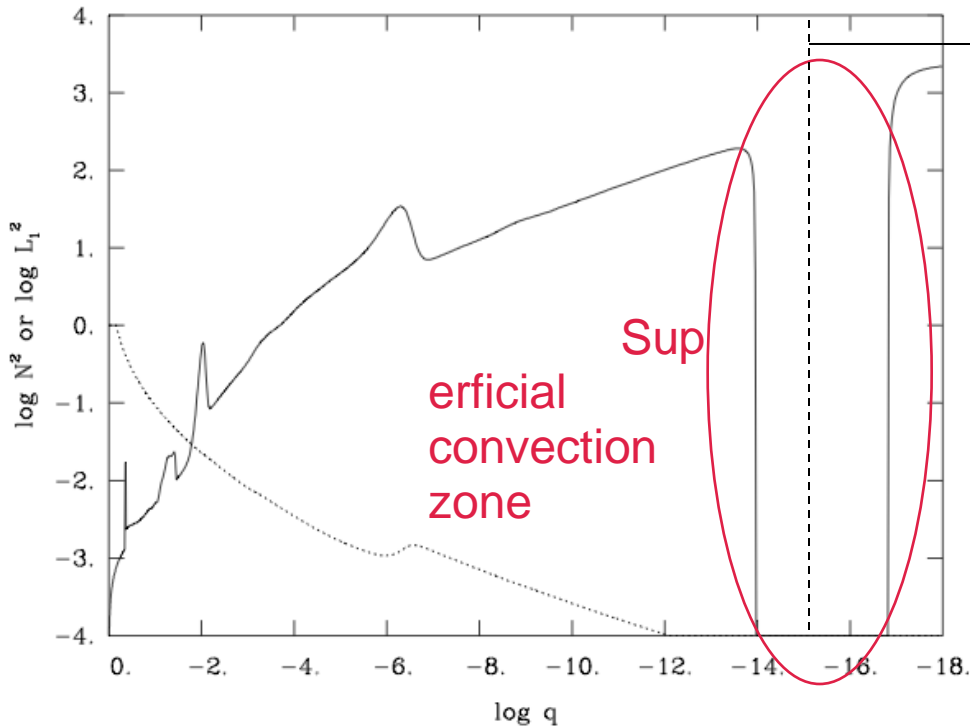


Base of the atmosphere



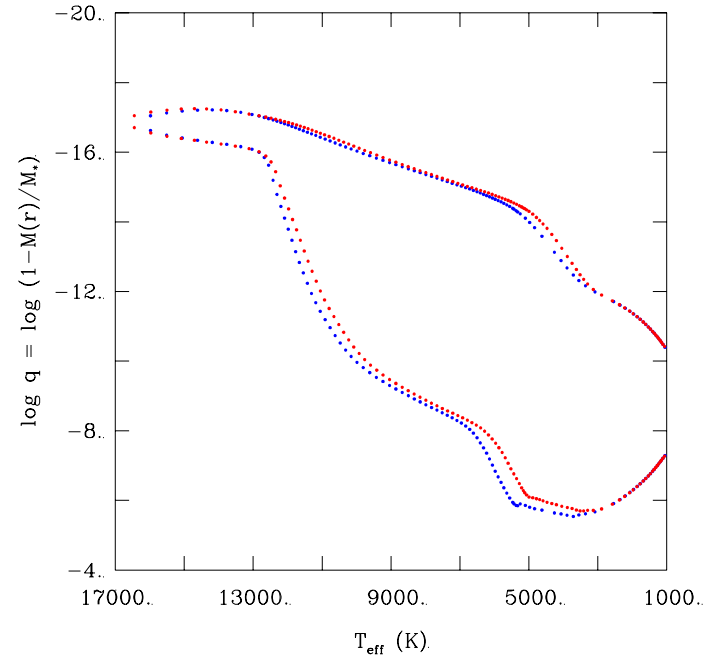
- Evolutionary tracks computed for $0.4M_{\odot}$ to $1.1M_{\odot}$ ($0.1M_{\odot}$ step)
- from $T_{\text{eff}}=35,000 \text{ K}$ to $2,000 \text{ K}$ (~ 150 models)
- with ML2 version ($a=1, b=2, c=16$); $\alpha = 1$ (ie $l = Hp$)

2. Evolutionary ZZ Ceti models



Base of the atmosphere

Detailed modeling of the superficial layers



Our evolutionary models have the same T stratification as the complete model atmospheres
 \Rightarrow "feedback" of the convection on the global atmosphere structure

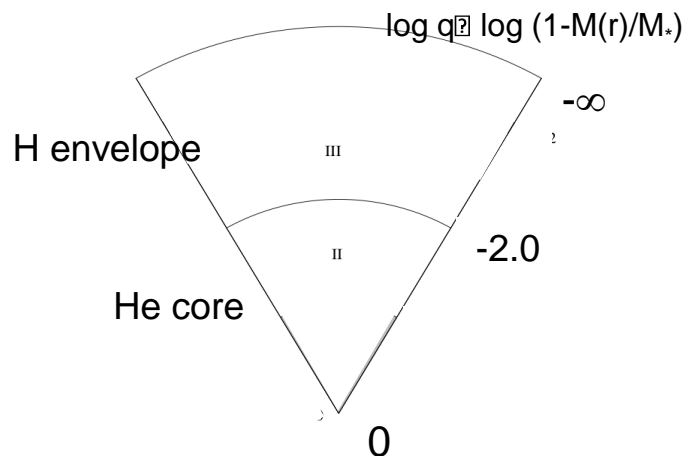
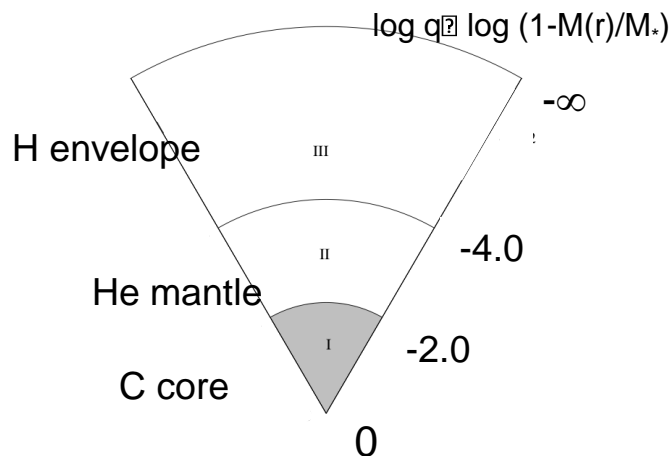
- Standard grey atmosphere
- Detailed atmosphere

2. Evolutionary ZZ Ceti models

- Extremely Low Mass (ELM) DA white dwarf:
H envelope on top of He core

ELM white dwarfs come from stars that never experienced any He-flash, because of extreme mass loss on RGB (from binary interactions or due to high Z)

- 2 kinds of evolutionary tracks computed here:
 - Standard C core models, but for $0.125M_{\odot}$ and $0.15-0.4M_{\odot}$ (steps $0.05M_{\odot}$)
 - Pure He core/H envelope models, for the same masses, but thick envelopes



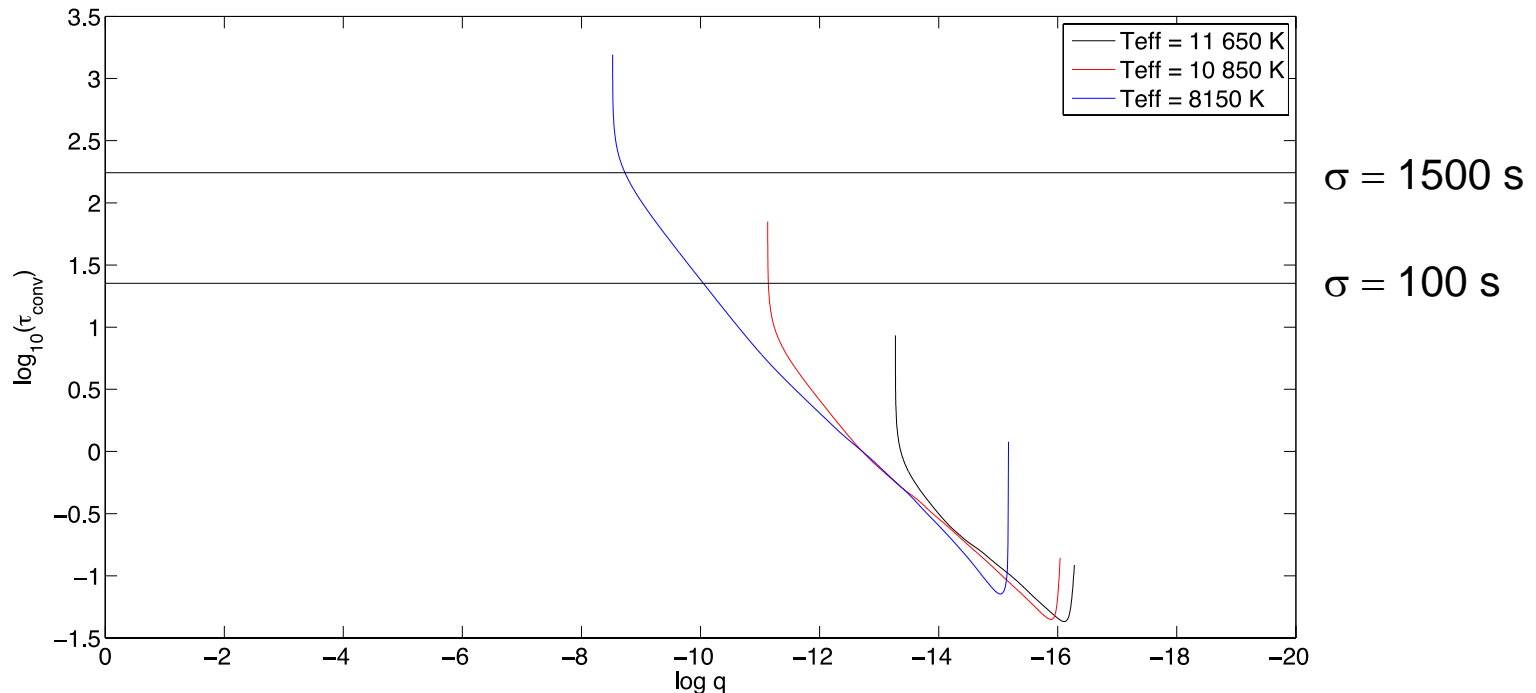
Instability location in $T_{\text{eff}}-\log g$ plane insensitive to detailed core structure and envelope layering

3. Time-Dependent Convection (TDC) approach

3. Time-Dependent Convection approach

For a standard $0.6M_{\odot}$ ZZ Ceti model:

- $T_{\text{eff}} \sim 12,000$ K: convective turnover timescale $\tau_{\text{conv}} \ll \sigma$ (pulsation periods)
 \Rightarrow convection adapts quasi-instantaneously to the pulsations
- $T_{\text{eff}} \sim 11,000$ K: $\tau_{\text{conv}} \approx \sigma \Rightarrow$ NEED full Time-Dependent Convection (TDC)
- Frozen convection (FC), i.e. $\tau_{\text{conv}} \gg \sigma$: NEVER justified in the ZZ Ceti T_{eff} regime
(FC is the usual assumption to study the theoretical instability strip...)



3. Time-Dependent Convection theory

- The Liege nonadiabatic pulsation code **MAD** (Dupret 2002) is the only one to implement convenient TDC treatment
- Full development in Grigahcène et al.(2005), following the theory of M. Gabriel (1974,1996), based on ideas of Unno et al. (1967)
- The timescales of pulsations and convection are **both** taken into account
- Perturbation of the convective flux taken into account here:

$$\delta F_C = \overline{F_C} \left(\frac{\delta \rho}{\overline{\rho}} + \frac{\delta T}{\overline{T}} \right) + \overline{\rho T} (\overline{\delta \Delta s V} + \overline{\Delta s \delta V})$$

- Built within the mixing-length theory (MLT), with the adopted perturbation of the mixing-length:

$$\frac{\delta l}{l} = \frac{1}{1 + (\sigma \tau_c)^2} \frac{\delta H_p}{H_p}$$

if $\sigma \gg \tau_{\text{conv}}$ (instantaneous adaption): $\delta l/l \rightarrow \delta H_p/H_p$

if $\sigma \ll \tau_{\text{conv}}$ (frozen convection): $\delta l/l \rightarrow 0$

4. Stability survey: the theoretical instability strip

4. Results: computing the theoretical instability strip

- We applied the MAD code to all evolutionary sequences

- “normal” C-core ZZ Ceti models, $0.4 - 1.1 M_{\odot}$, $\log q(H) = -4.0$
- ELM, C-core models: $0.125 - 0.4 M_{\odot}$, $\log q(H) = -4.0$
- ELM, He-core models: $0.125 - 0.4 M_{\odot}$, $\log q(H) = -2.0$
- $0.17 M_{\odot}$, He-core models, “thin” envelope $\log q(H) = -3.7$

with $ML2/\alpha = 1$, detailed atmospheric modeling, and TDC treatment

- We computed the degree $l=1$ in the range 10-5000 s (p- and g-modes)
- For the red edge (long-standing problem):

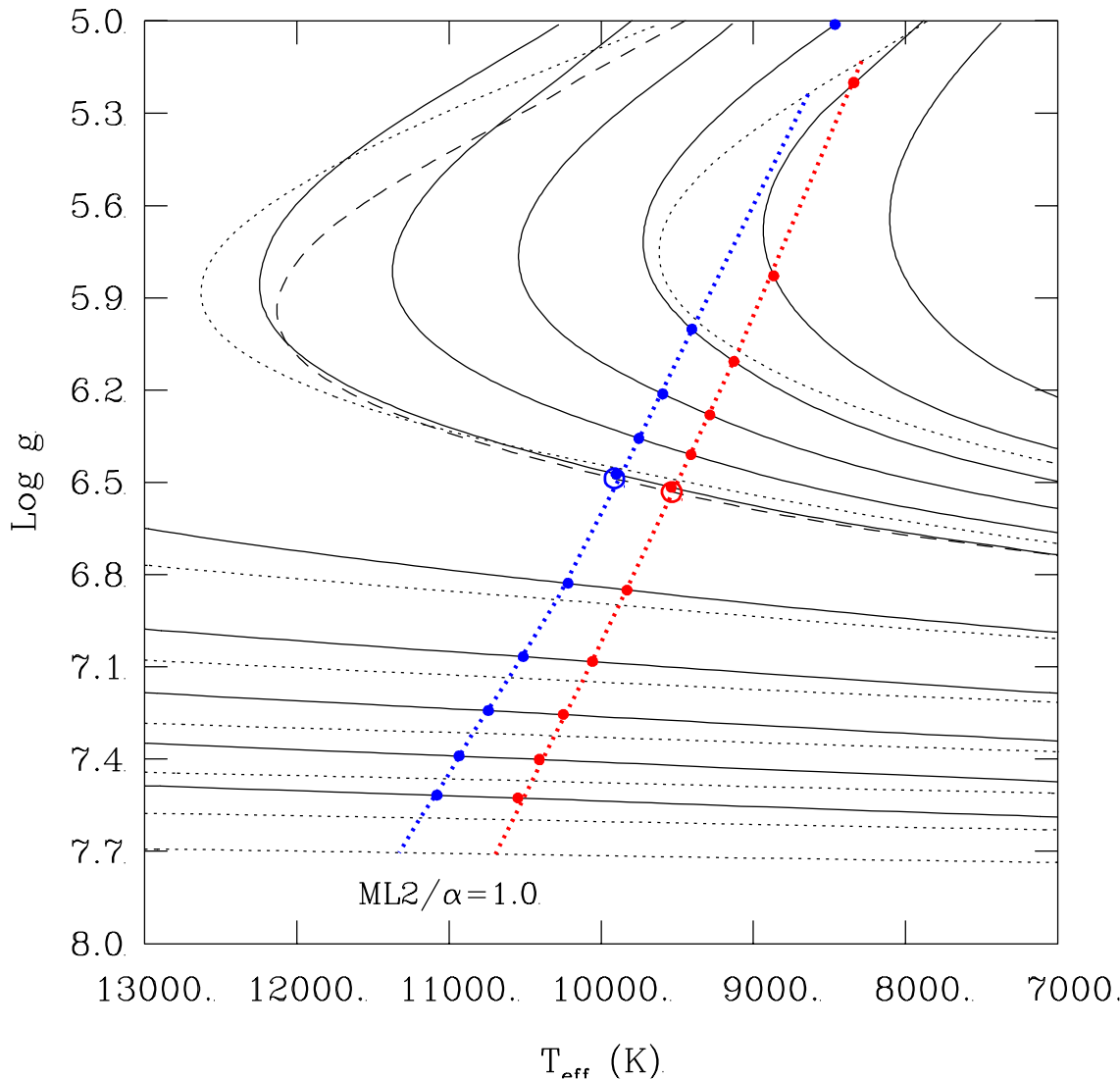
based on the idea of Hansen, Winget & Kawaler (1985): red edge arises when

$$\tau_{\text{th}} \sim P_{\text{crit}} \propto (l(l+1))^{-0.5}$$

(τ_{th} : thermal timescale at the base of the convection zone),

which means the mode is no longer reflected back by star’s atmosphere

Universality of the instability domain



Tracks:

Solid lines: He core, thick env.
Dotted lines: C-core, thin env.
Dashed line: $0.17M_{\odot}$, thin env.

Edges:

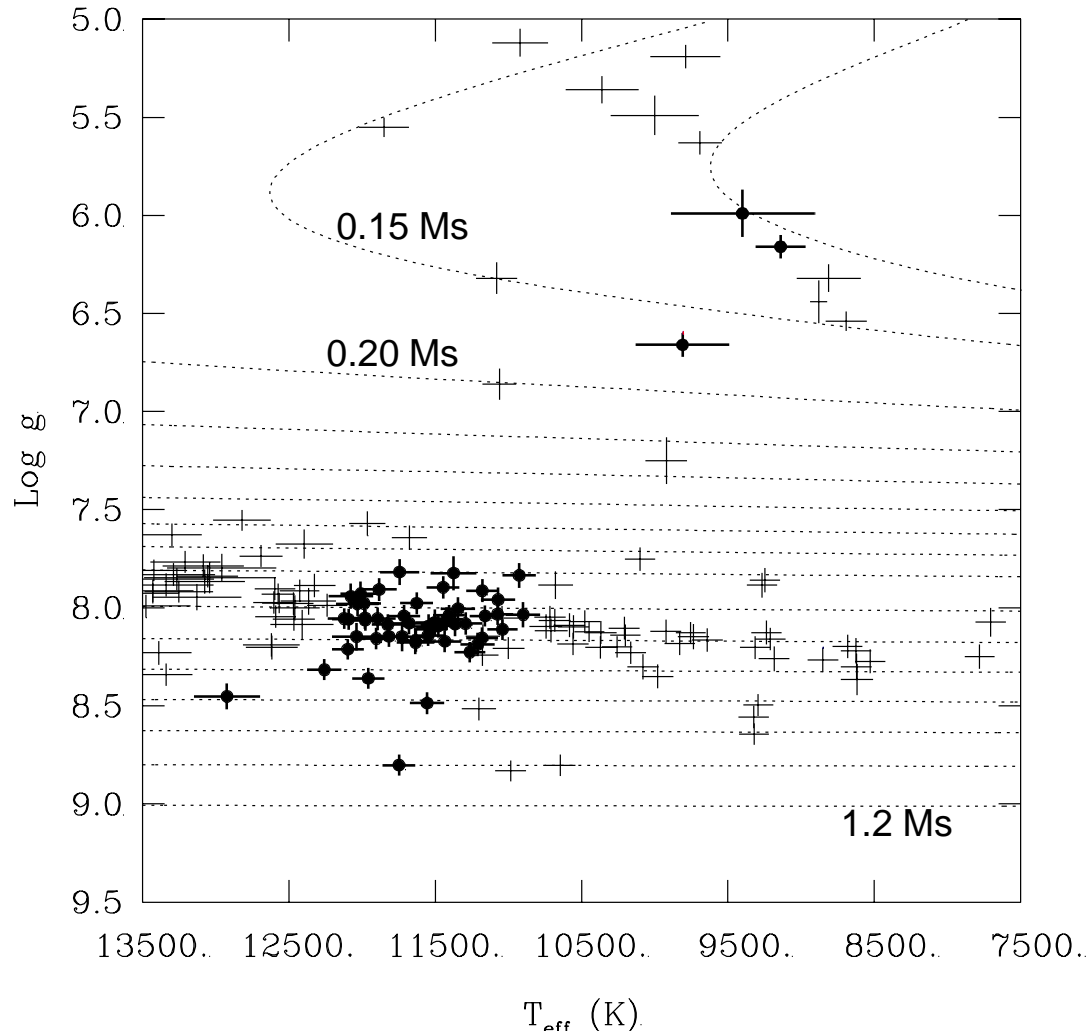
- ⋯ Edges C-core tracks
- Edges He-core tracks
- edges $0.17M_{\odot}$ track



Instability domain is insensitive to the exact core structure and envelope layering for models with same $T_{\text{eff}}/\log g$

Empirical ZZ Ceti instability strip (2012 view)

⊕ non variable (<10mmag); ● pulsator



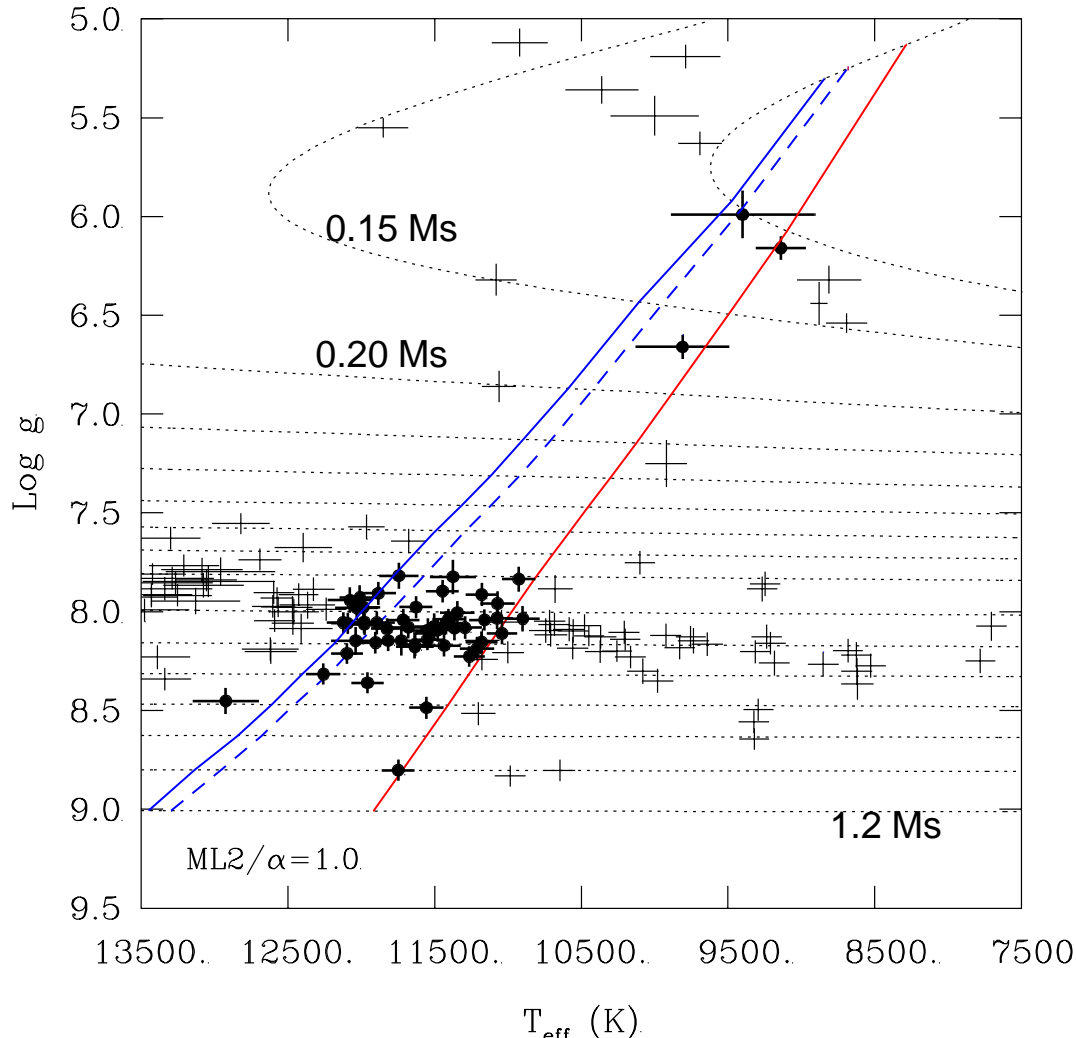
Spectroscopic estimates:

- ELM white dwarfs: D. Koester
- Standard ZZ Ceti: P. Bergeron

But both **ML²/α=0.6**

Theoretical instability strip (g-modes l=1)

⊕ non variable (<10mmag); ● pulsator



— TDC blue edge
 - - - FC blue edge
 — Red edge

- Narrower strip at low masses (larger slope for the red edge)

- Evolutionary models:
 $ML2/\alpha = 1$

Model atmospheres:
 $ML2/\alpha = 0.6$

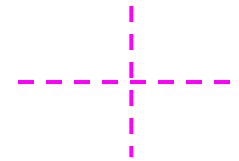
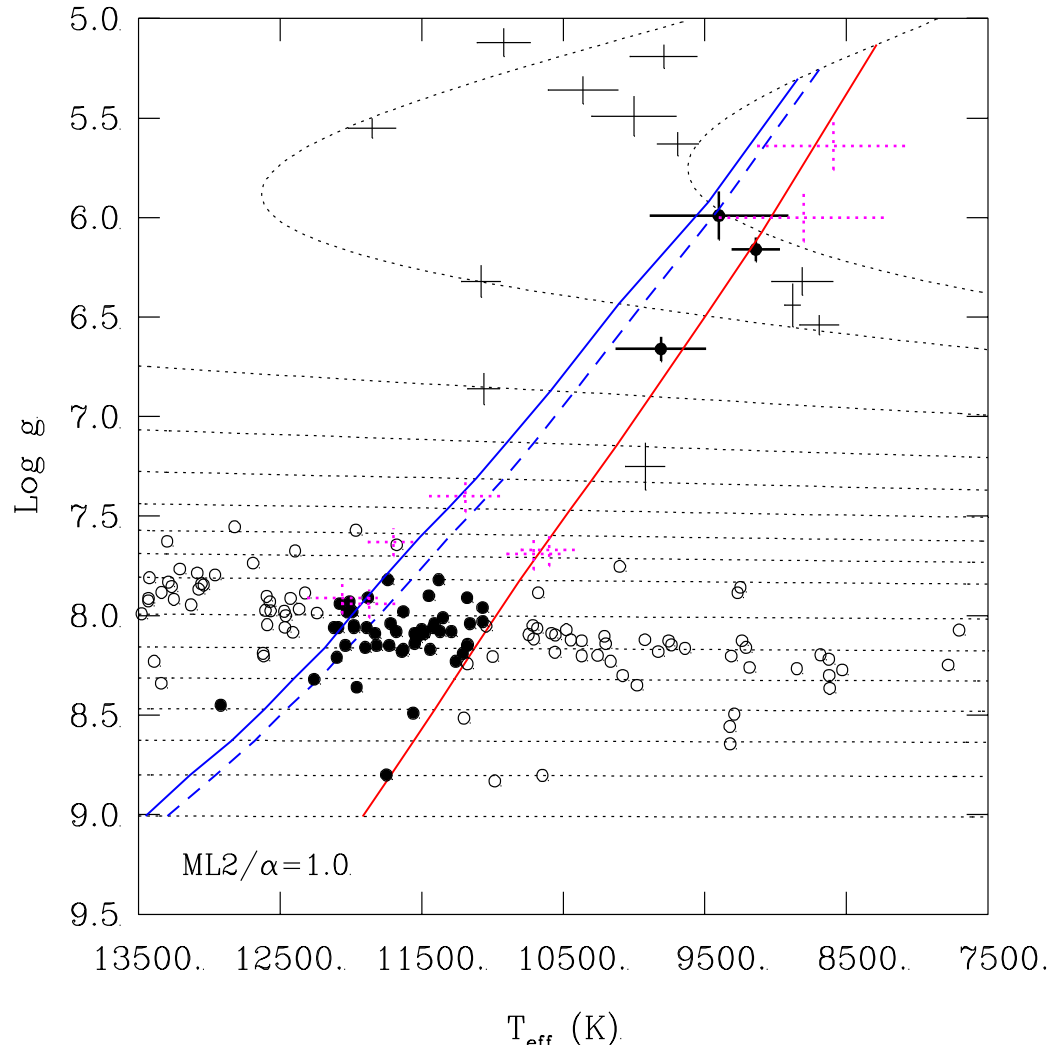


Convective efficiency increases with depth?

(consistent with hydrodynamical simulations; Ludwig et al. 1994, Tremblay & Ludwig 2012)

Other ELM/standard ZZ Ceti pulsators ?

Is the whole ZZ Ceti instability strip **pure**?

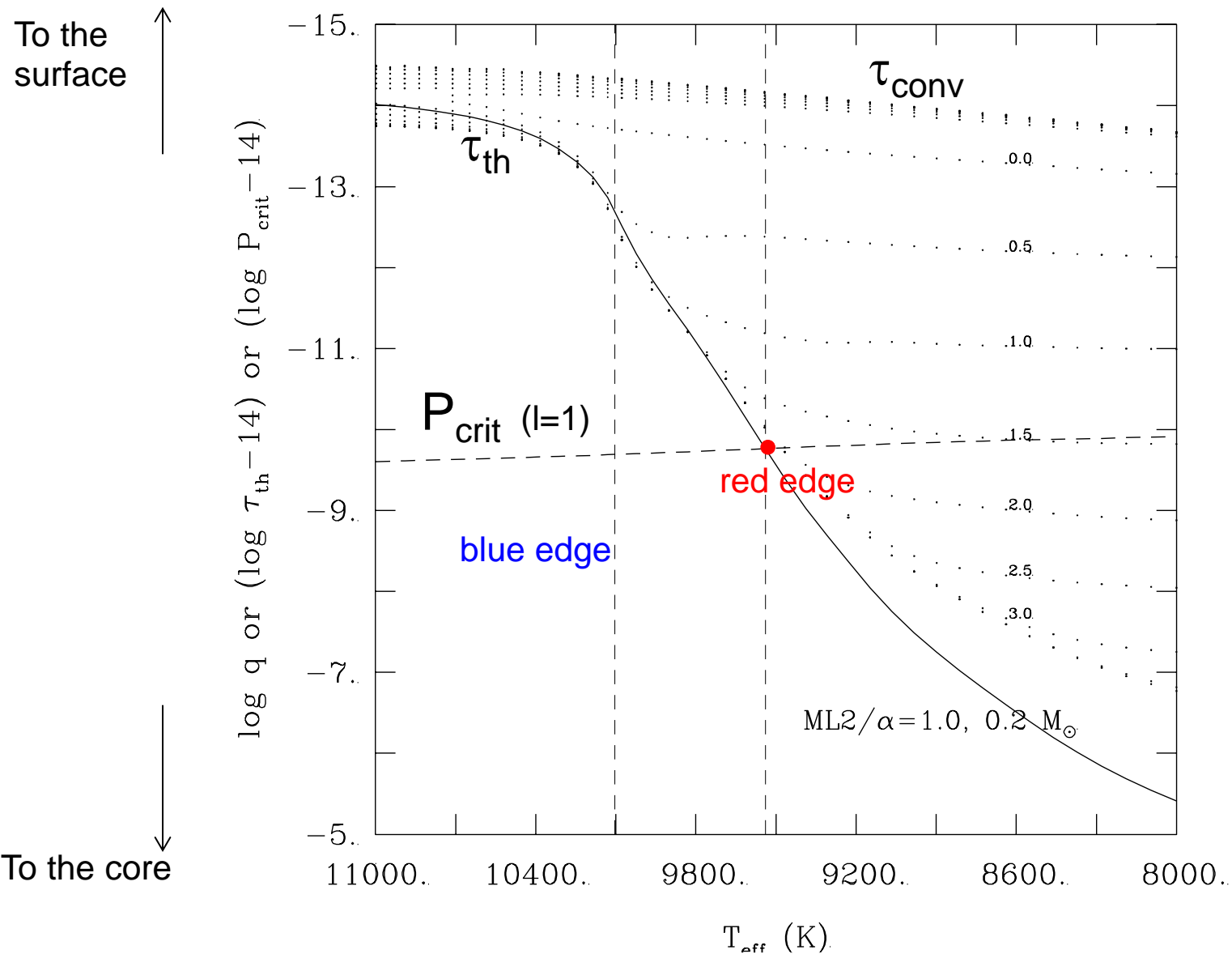


Suggestion for observations

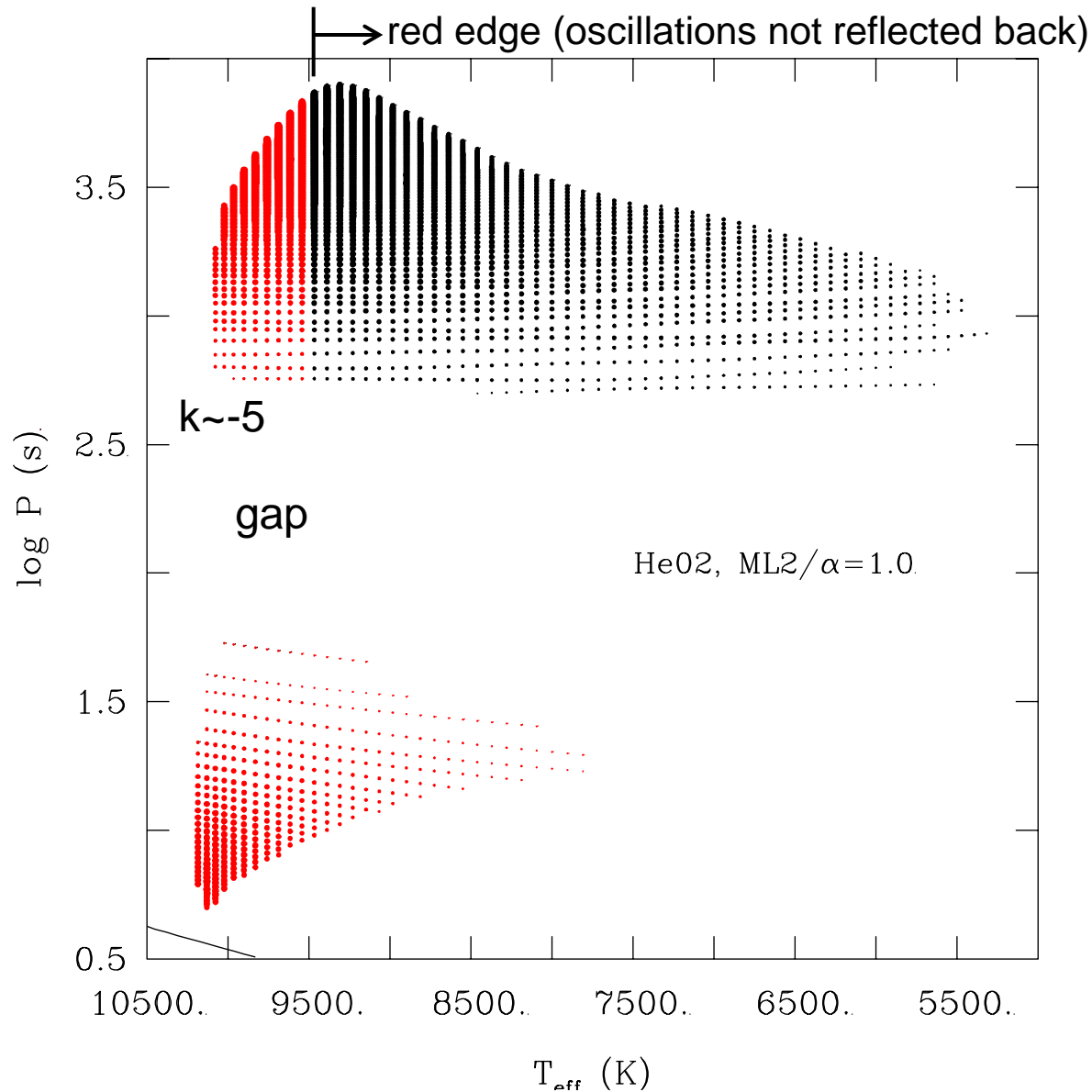
DA white dwarfs with $T_{\text{eff}}/\log g$
close to our instability strip

Not checked for variability so far

Ex: zoom to the 0.2Ms He-core track, $l_q(H)=-2.0$



Excited $l=1$ periods for the 0.2Ms He-core track

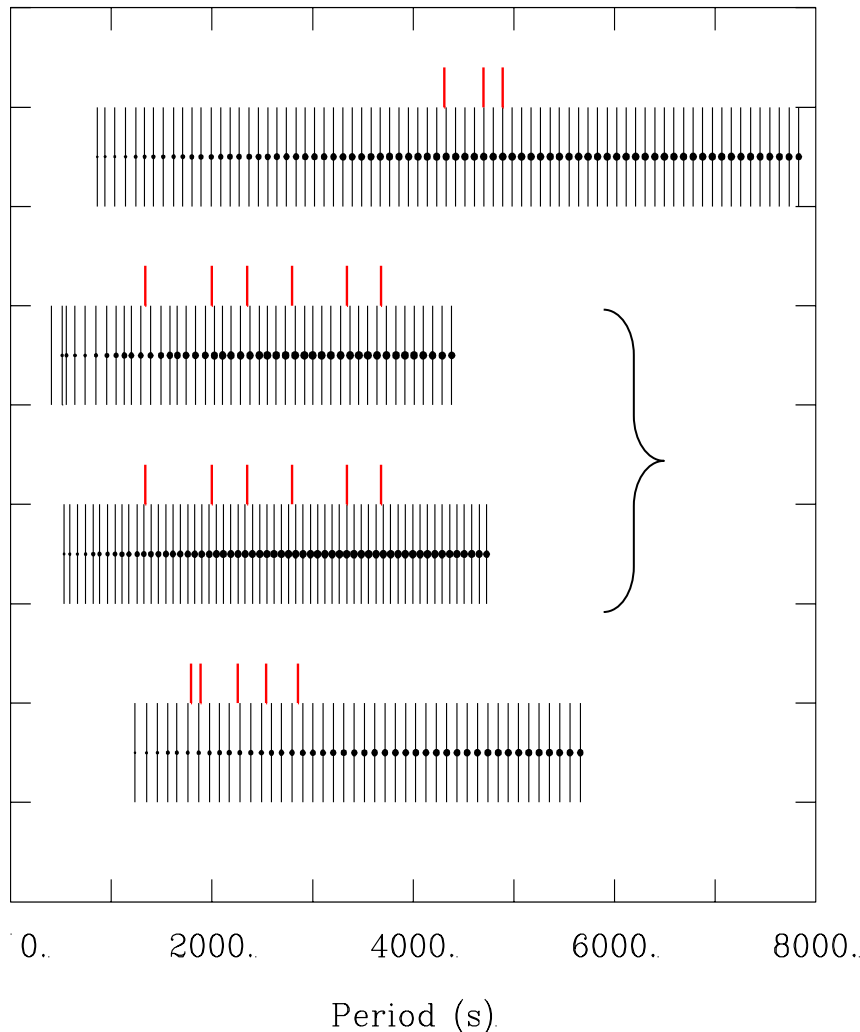


g-modes

p-modes ($P \sim 50$ s)

Observable?

Qualitative fit to the observed periods of the 3 ELM pulsators



SDSS J1840+6423

$T_{\text{eff}} \sim 9140 \pm 170 \text{ K}$, $\log g \sim 6.16 \pm 0.06$

He-core model, $\log q(\text{H}) = -2.0$

SDSS J1518+0658

$T_{\text{eff}} \sim 9810 \pm 320 \text{ K}$, $\log g \sim 6.66 \pm 0.06$

He-core model, $\log q(\text{H}) = 4.0$ and -2.0

SDSS J1112+1117

$T_{\text{eff}} \sim 9400 \pm 490 \text{ K}$, $\log g \sim 5.99 \pm 0.12$

He-core model, $\log q(\text{H}) = -2.0$

Adiabatic properties are sensitive to exact interior structure

5. Conclusion and prospects

5. Conclusion and Prospects

Conclusions:

- ELM pulsators are low mass equivalent to standard ZZ Ceti pulsators
⇒ such pulsators exist from 0.15 to 1.1 M_{\odot} ($\log g = 5 - 9$!)
- Excellent agreement between theoretical and observed instability strip:
 - Blue edge, TDC approach
 - Red edge, by energy leakage through the atmosphere
- Is $ML2/\alpha=1.0$ the good flavor for convection inside white dwarfs?
Related to spectroscopic calibration ($ML2/\alpha=0.6$) and hydrodynamical simulations (Tremblay & Ludwig 2011,2012)

Prospects:

- Detection of p-modes in white dwarfs?
- Is the ZZ Ceti instability strip **pure**?
- Asteroseismology of ELM/standard ZZ Ceti white dwarf pulsators
 1. internal structure & fundamental parameters
 2. **age**
 3. understanding of matter under extreme conditions

Why TDC and FC blue edges are not dramatically different?

1. The difference (~ 250 K) is **not** negligible !

Width of instability strip: ~ 1000 K at $\log g = 8$ and ~ 600 K at $\log g = 6$

2. Van Grootel et al. (2012) and Saio (2012, Liege colloquium)

eigenfunctions TDC/FC are really different, and excitation mechanisms too:

- TDC: convective driving (convective flux can be modulated)
- FC: κ -mechanism with radiative luminosity ($\ll L_{\text{conv}}$)

But both mechanisms occurs at the same layers (partial ionization zone)