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# Integration / blending of external information into genetic / genomic evaluations

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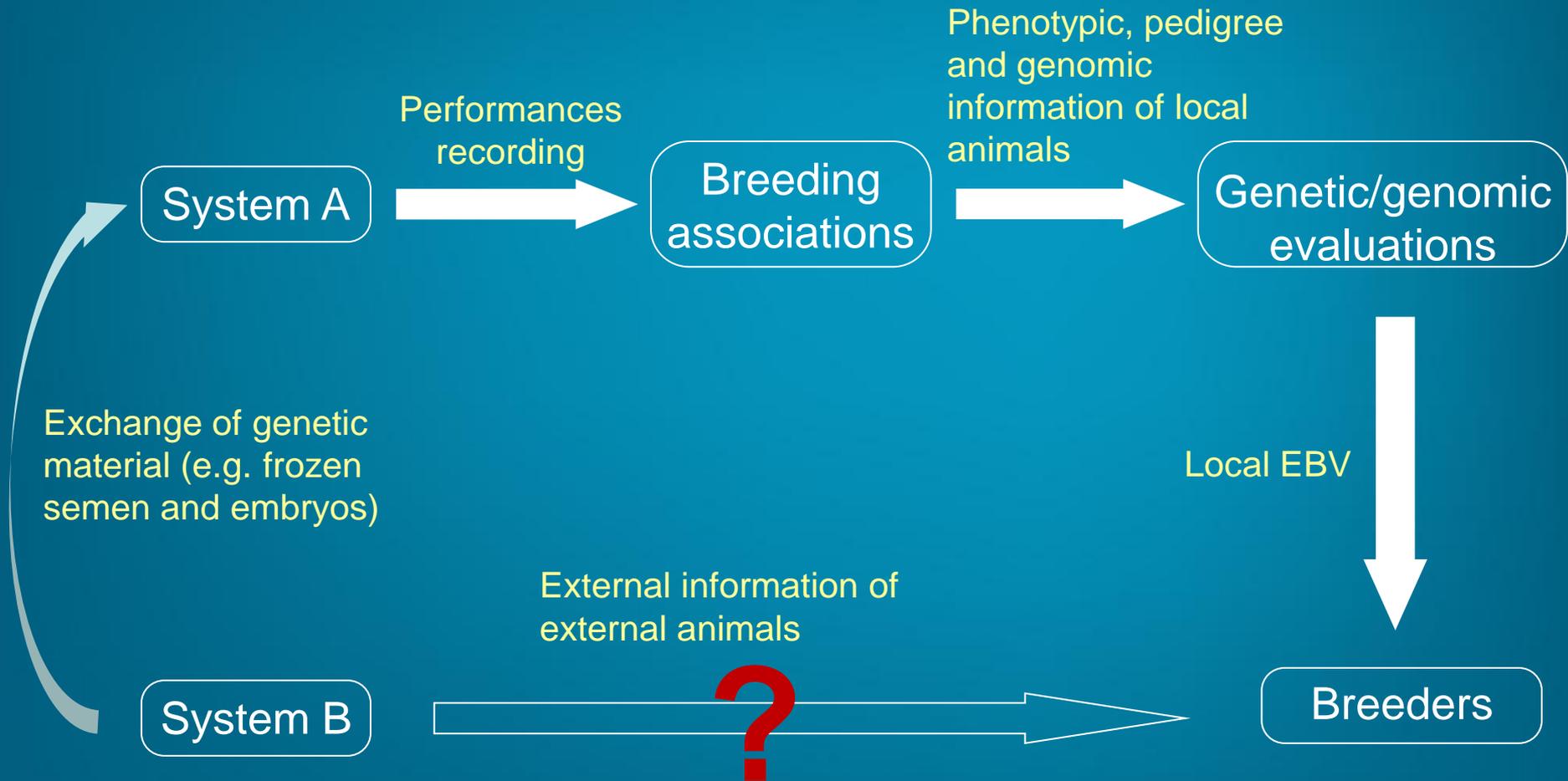
# Introduction

- Most reliable EBV if estimated from all available sources
- Most situations
  - Multiple sources (e.g., dairy breeds)
    - Traditional genetic evaluations
    - International second step (Interbull)
  - Animals with few (or no) local data: low accuracy
  - Development of genomic selection
    - New genomic information sources
- Strategies for integration / blending of those multiple sources of external information

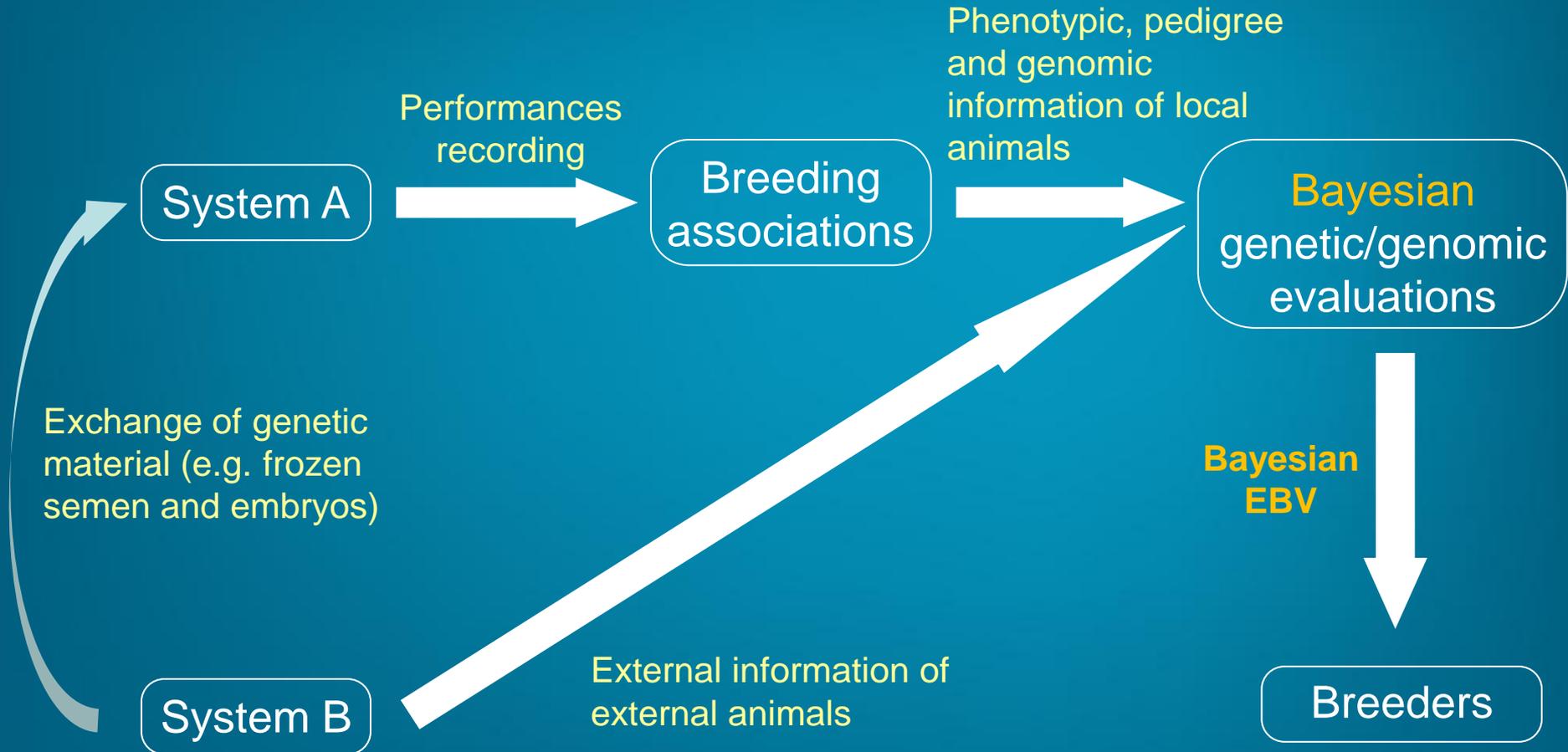
# Introduction

- Single-step genomic evaluation (ssGBLUP)
  - Genomic, pedigree and phenotypic information considered simultaneously
- Current limitation
  - Only available local records used
  - Disadvantage compared to multi-steps methods using e.g. MACE-EBV as a way to access to external phenotypic information

# Current situation



# Possible solution



# Aim

**To integrate/blend multiple *a priori* known external information into a local genetic/genomic evaluation**

→ Using a Bayesian approach

- Based on
  - Legarra et al. (2007)
  - Quaas and Zhang (2006)
  - Vandenplas and Gengler (2012a, 2012b)
  - Vandenplas et al. (2012a, 2012b)

# External information

- Most situations
  - EBV and REL from other genetic evaluations
  - Information not taken into account by a local (ssG)BLUP
    - Not an external genomic evaluation
    - No double-counting between local and external evaluations
  - Only available for some animals
    - Having, or not, phenotypic information in the local (ssG)BLUP
    - Present in the pedigree of the local (ssG)BLUP

# Regular (ssG)BLUP

- Mixed model equations

$$\begin{bmatrix} \mathbf{X}'\mathbf{R}^{-1}\mathbf{X} & \mathbf{X}'\mathbf{R}^{-1}\mathbf{Z} \\ \mathbf{Z}'\mathbf{R}^{-1}\mathbf{X} & \mathbf{Z}'\mathbf{R}^{-1}\mathbf{Z} + \mathbf{G}^{*-1} \end{bmatrix} \begin{bmatrix} \hat{\boldsymbol{\beta}}_L \\ \hat{\mathbf{u}}_L \end{bmatrix} = \begin{bmatrix} \mathbf{X}'\mathbf{R}^{-1}\mathbf{y}_L \\ \mathbf{Z}'\mathbf{R}^{-1}\mathbf{y}_L \end{bmatrix}$$

- $\mathbf{G}^{*-1}$  : Inverse of (combined genomic-) pedigree based (co)variances matrix
- $\mathbf{y}_L$  : vector of **local observations**
- $\hat{\boldsymbol{\beta}}_L$  : vector of estimated **local fixed effects**
- $\hat{\mathbf{u}}_L$  : vector of estimated **local (G)EBV**
- $p(\mathbf{u}_L) = MVN(\mathbf{0}, \mathbf{G}^*)$

# Integration of one source

- Assumption: Conditional distribution of  $\mathbf{u}_L$

$$p(\mathbf{u}_L | \mathbf{y}_E) = MVM(\hat{\mathbf{u}}_E, \mathbf{D})$$

- $\mathbf{y}_E$  : **unavailable** vector of **external observations**
  - $\hat{\mathbf{u}}_E$  : vector of **external EBV**
  - $\mathbf{D}$  : **prediction error (co)variances matrix** of  $\hat{\mathbf{u}}_E$
- **Issue:** only available for some animals
  - $\hat{\mathbf{u}}_E$  and  $\mathbf{D}$  : (partially) unknown

# Integration of one source

- Estimation of  $\hat{\mathbf{u}}_E$ 
  - Available: External EBV of external animals ( $\hat{\mathbf{u}}_{EE}^*$ )
  - Local animals: prediction of external EBV ( $\hat{\mathbf{u}}_{EL}$ )

$$p(\hat{\mathbf{u}}_{EL} | \hat{\mathbf{u}}_{EE}^*) = MVN(\mathbf{G}_{LE} \mathbf{G}_{EE}^{-1} \hat{\mathbf{u}}_{EE}^*, (\mathbf{G}^{EE})^{-1})$$

$$\rightarrow \hat{\mathbf{u}}_E = \begin{bmatrix} \hat{\mathbf{u}}_{EL} \\ \hat{\mathbf{u}}_{EE}^* \end{bmatrix}$$

Predicted external EBV

Available external EBV

→ Correct propagation of external information

# Integration of one source

- Estimation of  $\mathbf{D}$

$$\mathbf{D}^{-1} = \mathbf{G}^{-1} + \mathbf{\Lambda}$$

–  $\mathbf{G}^{-1} = \mathbf{A}^{-1} \otimes \mathbf{G}_0^{-1}$  : Inverse of genetic (co)variances matrix of  $\hat{\mathbf{u}}_E$

–  $\mathbf{\Lambda} = \text{block diag}(\mathbf{\Delta}_i \mathbf{G}_0^{-1} \mathbf{\Delta}_i)$ ;  $i = 1, \dots, n$  animals

{ For external animals :  $\mathbf{\Delta}_i = \text{diag}(\sqrt{\text{REL}_{ij}/(1 - \text{REL}_{ij})})$ ;  $j = 1, \dots, t$  traits  
{ For animals with only local information :  $\mathbf{\Delta}_i = \mathbf{0}$

# Integration of one source

- Integration of external EBV and REL

$$\begin{bmatrix} \mathbf{X}'\mathbf{R}^{-1}\mathbf{X} & \mathbf{X}'\mathbf{R}^{-1}\mathbf{Z} \\ \mathbf{Z}'\mathbf{R}^{-1}\mathbf{X} & \mathbf{Z}'\mathbf{R}^{-1}\mathbf{Z} + \mathbf{G}^{*-1} \end{bmatrix} \begin{bmatrix} \hat{\boldsymbol{\beta}}_L \\ \hat{\mathbf{u}}_L \end{bmatrix} = \begin{bmatrix} \mathbf{X}'\mathbf{R}^{-1}\mathbf{y}_L \\ \mathbf{Z}'\mathbf{R}^{-1}\mathbf{y}_L \end{bmatrix}$$



$$\begin{bmatrix} \mathbf{X}'\mathbf{R}^{-1}\mathbf{X} & \mathbf{X}'\mathbf{R}^{-1}\mathbf{Z} \\ \mathbf{Z}'\mathbf{R}^{-1}\mathbf{X} & \mathbf{Z}'\mathbf{R}^{-1}\mathbf{Z} + \mathbf{G}^{*-1} + \boldsymbol{\Lambda} \end{bmatrix} \begin{bmatrix} \hat{\boldsymbol{\beta}}_L \\ \hat{\mathbf{u}}_L \end{bmatrix} = \begin{bmatrix} \mathbf{X}'\mathbf{R}^{-1}\mathbf{y}_L \\ \mathbf{Z}'\mathbf{R}^{-1}\mathbf{y}_L + \mathbf{D}^{-1}\hat{\mathbf{u}}_E \end{bmatrix}$$

Least square parts of LHS of the hypothetical BLUP

RHS of the hypothetical BLUP

# Integration of one source: simulation

- 100 replicates
- 2 populations
  - $\pm 1000$  animals/population
  - 5 generations
  - Random matings / cullings
  - Observations (Van Vleck, 1994)
    - Milk yield for the first lactation
    - Heritability : 0.25
  - Fixed effect
    - Random herd effect within population

# Integration of one source: simulation

- Performed evaluations

Information	External BLUP	Local BLUP	Bayesian BLUP	Joint BLUP
<b>Pedigree</b>				
<b>External population</b>	✓			
Local population + 50 external sires used locally				
<b>Phenotypes</b>				
<b>External observations</b>	✓			
Local observations 50 external sires External EBV and REL				

# Integration of one source: simulation

- Performed evaluations

Information	External BLUP	Local BLUP	Bayesian BLUP	Joint BLUP
<b>Pedigree</b>				
External population	✓			
Local population + 50 external sires used locally		✓		
<b>Phenotypes</b>				
External observations	✓			
Local observations		✓		
50 external sires				
External EBV and REL				

# Integration of one source: simulation

- Performed evaluations

Information	External BLUP	Local BLUP	Bayesian BLUP	Joint BLUP
<b>Pedigree</b>				
External population	✓			
<b>Local population</b> <b>+ 50 external sires used locally</b>		✓	✓	
<b>Phenotypes</b>				
External observations	✓			
<b>Local observations</b>		✓	✓	
50 external sires				
<b>External EBV and REL</b>			✓	

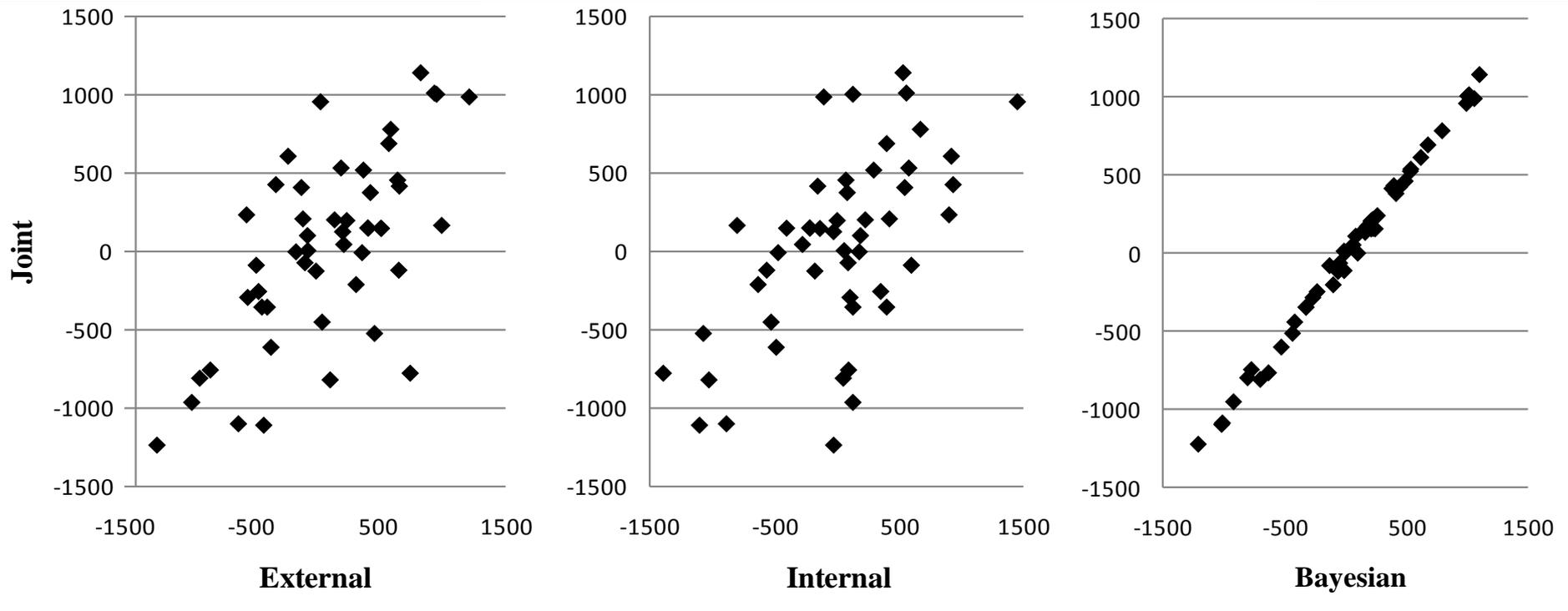
# Integration of one source: simulation

- Performed evaluations

Information	External BLUP	Local BLUP	Bayesian BLUP	Joint BLUP
<b>Pedigree</b>				
External population	✓			✓
Local population + 50 external sires used locally		✓	✓	✓
<b>Phenotypes</b>				
External observations	✓			✓
Local observations		✓	✓	✓
50 external sires				
External EBV and REL			✓	

# Comparison with joint BLUP

- EBV of the 50 external sires used locally



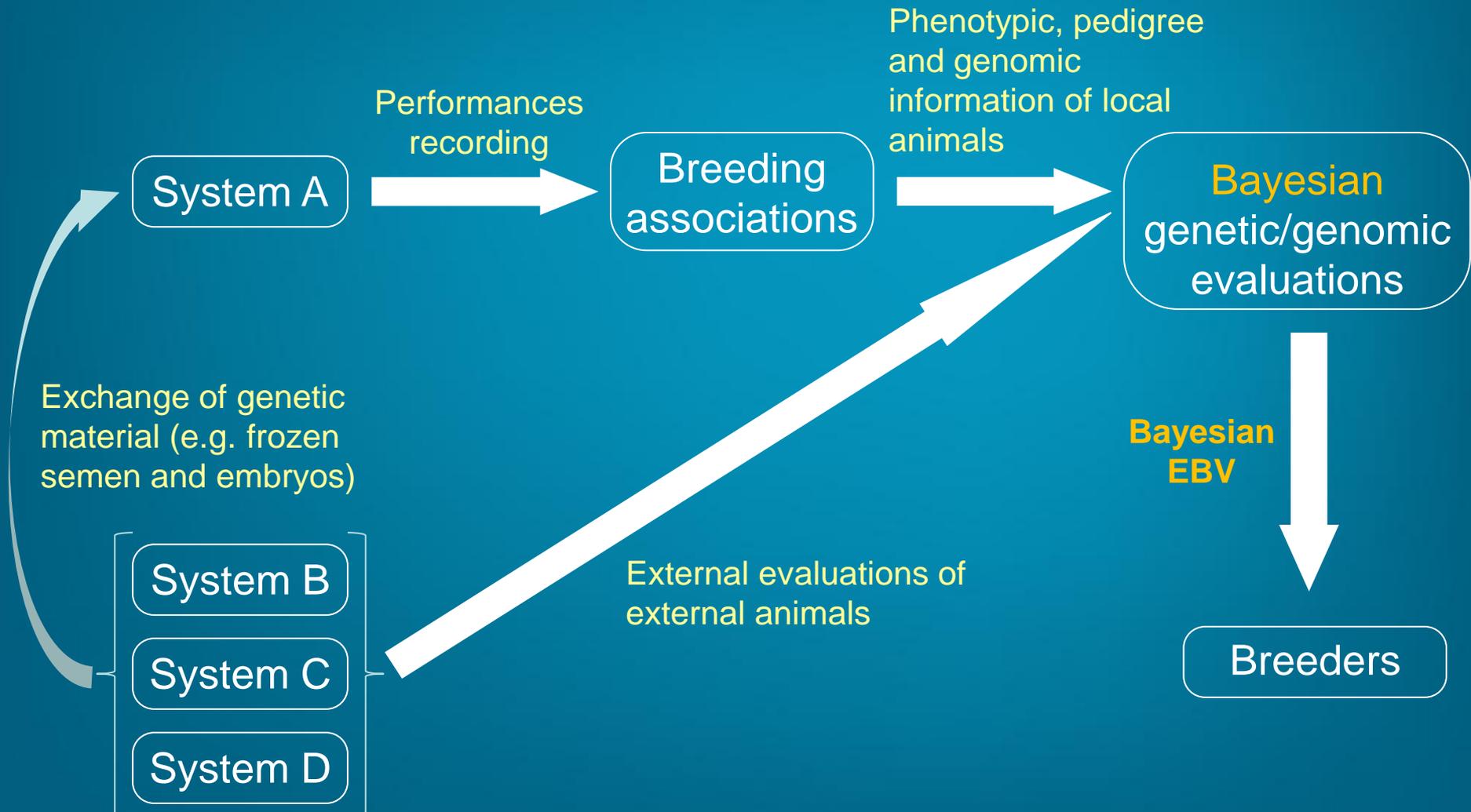
# Comparison with joint BLUP

- Rank correlations ( $r$ ) and mean squared errors (MSE) expressed as a percentage of the local MSE

Evaluation	Local animals		External sires	
	$r \pm \text{SD}$	MSE $\pm$ SD	$r \pm \text{SD}$	MSE $\pm$ SD
<b>Without external information</b>				
Local BLUP	$0.95 \pm 0.02$	$100.00 \pm 33.5$	$0.54 \pm 0.12$	$100.00 \pm 28.2$
<b>With external information</b>	$>0.99 \pm 0.000$	$0.79 \pm 0.52$	$0.99 \pm 0.002$	$0.49 \pm 0.25$

➔ Rankings more similar to those of the joint BLUP

# Integration of multiple sources



# Integration of multiple sources

- Assumption: *A priori* known information of  $\mathbf{u}_L$ 
  - $n$  sources of external information:

- $n$  vector of external EBV

$$\hat{\mathbf{u}}_{E_1}, \dots, \hat{\mathbf{u}}_{E_i}, \dots, \hat{\mathbf{u}}_{E_n}$$

- $n$  prediction error (co)variances matrices

$$\mathbf{D}_{E_1}, \dots, \mathbf{D}_{E_i}, \dots, \mathbf{D}_{E_n}$$

- Issue: only available for some animals

→  $\hat{\mathbf{u}}_{E_i}$  and  $\mathbf{D}_{E_i}$ : (partially) unknown

# Integration of multiple sources

- For each source  $i$ : Estimation of  $\hat{\mathbf{u}}_{E_i}$ 
  - Available: External EBV of external animals ( $\hat{\mathbf{u}}_{EE_i}^*$ )
  - Local animals: prediction of external EBV ( $\hat{\mathbf{u}}_{EL_i}$ )

$$p(\hat{\mathbf{u}}_{EL_i} | \hat{\mathbf{u}}_{EE_i}^*) = MVN(\mathbf{G}_{LE_i} \mathbf{G}_{EE_i}^{-1} \hat{\mathbf{u}}_{EE_i}^*, (\mathbf{G}^{EE_i})^{-1})$$

$$\rightarrow \hat{\mathbf{u}}_{E_i} = \begin{bmatrix} \hat{\mathbf{u}}_{EL_i} \\ \hat{\mathbf{u}}_{EE_i}^* \end{bmatrix}$$

Predicted external EBV

Available external EBV

→ Correct propagation of external information

# Integration of multiple sources

- For each source  $i$ : Estimation of  $\mathbf{D}_{E_i}$

$$\mathbf{D}_{E_i}^{-1} = \mathbf{G}^{-1} + \mathbf{\Lambda}_{E_i}$$

$\mathbf{G}^{-1} = \mathbf{A}^{-1} \otimes \mathbf{G}_0^{-1}$  : Inverse of genetic (co)variances matrix of  $\hat{\mathbf{u}}_{E_i}$

$\mathbf{\Lambda}_{E_i} = \text{block diag}(\mathbf{\Delta}_j \mathbf{G}_0^{-1} \mathbf{\Delta}_j)$ ;  $i = 1, \dots, n$  sources;  $j = 1, \dots, a$  animals

$\left\{ \begin{array}{l} \text{For external animals : } \mathbf{\Delta}_j = \text{diag}(\sqrt{REL_{ijk} / (1 - REL_{ijk})}); k = 1, \dots, t \text{ traits} \\ \text{For animals with only local information : } \mathbf{\Delta}_j = \mathbf{0} \end{array} \right.$

# Integration of multiple sources

- Integration of  $n$  external information

$$\begin{bmatrix} \mathbf{X}'\mathbf{R}^{-1}\mathbf{X} & \mathbf{X}'\mathbf{R}^{-1}\mathbf{Z} \\ \mathbf{Z}'\mathbf{R}^{-1}\mathbf{X} & \mathbf{Z}'\mathbf{R}^{-1}\mathbf{Z} + \mathbf{G}^{*-1} \end{bmatrix} \begin{bmatrix} \hat{\boldsymbol{\beta}}_L \\ \hat{\mathbf{u}}_L \end{bmatrix} = \begin{bmatrix} \mathbf{X}'\mathbf{R}^{-1}\mathbf{y}_L \\ \mathbf{Z}'\mathbf{R}^{-1}\mathbf{y}_L \end{bmatrix}$$



$$\begin{bmatrix} \mathbf{X}'\mathbf{R}^{-1}\mathbf{X} & \mathbf{X}'\mathbf{R}^{-1}\mathbf{Z} \\ \mathbf{Z}'\mathbf{R}^{-1}\mathbf{X} & \mathbf{Z}'\mathbf{R}^{-1}\mathbf{Z} + \mathbf{G}^{*-1} + \sum_{i=1}^n \boldsymbol{\Lambda}_{E_i} \end{bmatrix} \begin{bmatrix} \hat{\boldsymbol{\beta}}_L \\ \hat{\mathbf{u}}_L \end{bmatrix} = \begin{bmatrix} \mathbf{X}'\mathbf{R}^{-1}\mathbf{y}_L \\ \mathbf{Z}'\mathbf{R}^{-1}\mathbf{y}_L + \sum_{i=1}^n (\mathbf{D}_{E_i}^{-1}\hat{\mathbf{u}}_{E_i}) \end{bmatrix}$$

Sum of  $n$  least square parts of LHS of  $n$  hypothetical BLUP of  $n$  sources of external EBV

Sum of  $n$  RHS of  $n$  hypothetical BLUP of  $n$  sources of external EBV

# Blending of multiple sources

- Blending of  $n$  external information
  - Assumption: no local records in  $\mathbf{y}_L$

$$\left[ \mathbf{G}^{*-1} + \sum_{i=1}^n \boldsymbol{\Lambda}_{E_i} \right] \hat{\mathbf{u}}_L = \left[ \sum_{i=1}^n \left( \mathbf{D}_{E_i}^{-1} \hat{\mathbf{u}}_{E_i} \right) \right]$$

# Issues

- Some issues arise before the implementation of a Bayesian evaluation like:
  - Compatibility between external and local traits
    - Same expression of external and local traits
    - ➔ Need to translate external information (e.g., using conversion equations (e.g., Vandenplas et al., 2012a))
  - Double counting of information
    - Due to relationships among external animals
    - Among external and local information
    - Among multiple external information

# Issues

- Double counting due to relationships
  - The animal's EBV and REL combine contributions:
    - due to own records (if present)
    - due to relationships (Misztal and Wiggans, 1988)
- Multiple considerations of parts of integrated external EBV for related external animals
- Estimation of contributions due to relationships and due to own records through a two-step algorithm (Vandenplas and Gengler, 2012)
- All  $\Lambda_{E_i}$  only depend on contributions due to own records

# Issues

- Double counting among external (and local) information
  - Each external information has to be free of local or other external information.
  - Ex.: Integration of MACE-EBV
    - Included local information
    - Estimation of external information free of local information:

$$\mathbf{D}_E^{-1} \hat{\mathbf{u}}_E = \mathbf{D}_M^{-1} \hat{\mathbf{u}}_M - \mathbf{D}_L^{*-1} \hat{\mathbf{u}}_L^*$$

# Issues

- Integration of MACE-EBV

$$\begin{bmatrix} \mathbf{X}'_L \mathbf{R}^{-1} \mathbf{X}_L & \mathbf{X}'_L \mathbf{R}^{-1} \mathbf{Z}_L \\ \mathbf{Z}'_L \mathbf{R}^{-1} \mathbf{X}_L & \mathbf{Z}'_L \mathbf{R}^{-1} \mathbf{Z}_L + \mathbf{G}^{*-1} \end{bmatrix} \begin{bmatrix} \hat{\beta}_L \\ \hat{u}_L \end{bmatrix} = \begin{bmatrix} \mathbf{X}'_L \mathbf{R}^{-1} \mathbf{y}_L \\ \mathbf{Z}'_L \mathbf{R}^{-1} \mathbf{y}_L \end{bmatrix} + \begin{bmatrix} \mathbf{D}_M^{-1} \hat{u}_M - \mathbf{D}_L^{*-1} \hat{u}_L^* \end{bmatrix}$$

# Issues

- Integration of MACE-EBV

$$\begin{bmatrix} \mathbf{X}'_L \mathbf{R}^{-1} \mathbf{X}_L & \mathbf{X}'_L \mathbf{R}^{-1} \mathbf{Z}_L \\ \mathbf{Z}'_L \mathbf{R}^{-1} \mathbf{X}_L & \mathbf{Z}'_L \mathbf{R}^{-1} \mathbf{Z}_L + \mathbf{G}^{*-1} + \mathbf{D}_M^{-1} - \mathbf{D}_L^{*-1} \end{bmatrix} \begin{bmatrix} \hat{\beta}_L \\ \hat{u}_L \end{bmatrix} = \begin{bmatrix} \mathbf{X}'_L \mathbf{R}^{-1} \mathbf{y}_L \\ \mathbf{Z}'_L \mathbf{R}^{-1} \mathbf{y}_L + \mathbf{D}_M^{-1} \hat{u}_M - \mathbf{D}_L^{*-1} \hat{u}_L^* \end{bmatrix}$$

Inverse of (combined genomic -) pedigree based (co)variances matrix

# Issues

- Integration of MACE-EBV

$$\begin{bmatrix} \mathbf{X}'_L \mathbf{R}^{-1} \mathbf{X}_L & \mathbf{X}'_L \mathbf{R}^{-1} \mathbf{Z}_L \\ \mathbf{Z}'_L \mathbf{R}^{-1} \mathbf{X}_L & \mathbf{Z}'_L \mathbf{R}^{-1} \mathbf{Z}_L + \mathbf{G}^{*-1} + \mathbf{D}_M^{-1} - \mathbf{D}_L^{*-1} \end{bmatrix} \begin{bmatrix} \hat{\beta}_L \\ \hat{u}_L \end{bmatrix} = \begin{bmatrix} \mathbf{X}'_L \mathbf{R}^{-1} \mathbf{y}_L \\ \mathbf{Z}'_L \mathbf{R}^{-1} \mathbf{y}_L + \mathbf{D}_M^{-1} \hat{u}_M - \mathbf{D}_L^{*-1} \hat{u}_L^* \end{bmatrix}$$

Inverse of **(combined genomic -) pedigree based** (co)variances matrix

Inverse of **prediction error (co)variances** matrix of **MACE-EBV**

# Issues

- Integration of MACE-EBV

$$\begin{bmatrix} \mathbf{X}'_L \mathbf{R}^{-1} \mathbf{X}_L & \mathbf{X}'_L \mathbf{R}^{-1} \mathbf{Z}_L \\ \mathbf{Z}'_L \mathbf{R}^{-1} \mathbf{X}_L & \mathbf{Z}'_L \mathbf{R}^{-1} \mathbf{Z}_L + \mathbf{G}^{*-1} + \mathbf{D}_M^{-1} + \mathbf{D}_L^{*-1} \end{bmatrix} \begin{bmatrix} \hat{\beta}_L \\ \hat{u}_L \end{bmatrix} = \begin{bmatrix} \mathbf{X}'_L \mathbf{R}^{-1} \mathbf{y}_L \\ \mathbf{Z}'_L \mathbf{R}^{-1} \mathbf{y}_L + \mathbf{D}_M^{-1} \hat{u}_M - \mathbf{D}_L^{*-1} \hat{u}_L^* \end{bmatrix}$$

Inverse of **(combined genomic -) pedigree based (co)variances matrix**

Inverse of **prediction error (co)variances matrix of MACE-EBV**

Inverse of **prediction error (co)variances matrix of local EBV**

# Issues

- Integration of MACE-EBV

$$\begin{bmatrix} X'_L R^{-1} X_L & X'_L R^{-1} Z_L \\ Z'_L R^{-1} X_L & Z'_L R^{-1} Z_L + G^{*-1} + D_M^{-1} + D_L^{*-1} \end{bmatrix} \begin{bmatrix} \hat{\beta}_L \\ \hat{u}_L \end{bmatrix} = \begin{bmatrix} X'_L R^{-1} y_L \\ Z'_L R^{-1} y_L + D_M^{-1} \hat{u}_M - D_L^{*-1} \hat{u}_L^* \end{bmatrix}$$

Inverse of (combined genomic -) pedigree based (co)variances matrix

Inverse of prediction error (co)variances matrix of MACE-EBV

Inverse of prediction error (co)variances matrix of local EBV

RHS of an hypothetical BLUP of MACE-EBV

# Issues

- Integration of MACE-EBV

$$\begin{bmatrix} X'_L R^{-1} X_L & X'_L R^{-1} Z_L \\ Z'_L R^{-1} X_L & Z'_L R^{-1} Z_L + G^{*-1} + D_M^{-1} + D_L^{*-1} \end{bmatrix} \begin{bmatrix} \hat{\beta}_L \\ \hat{u}_L \end{bmatrix} = \begin{bmatrix} X'_L R^{-1} y_L \\ Z'_L R^{-1} y_L + D_M^{-1} \hat{u}_M - D_L^{*-1} \hat{u}_L^* \end{bmatrix}$$

Inverse of **(combined genomic -) pedigree based (co)variances matrix**

Inverse of **prediction error (co)variances matrix of MACE-EBV**

Inverse of **prediction error (co)variances matrix of local EBV**

**RHS** of an hypothetical BLUP of **MACE-EBV**

**RHS** of an hypothetical BLUP of **local EBV**

# Bayesian ssGBLUP: simulation

- 100 replicates
- 2 populations
  - $\pm 1000$  animals/population
  - 5 generations
  - Random matings / cullings
  - Observations (Van Vleck, 1994)
    - Milk yield for the first lactation
    - Heritability : 0.25
  - Fixed effect
    - Random herd effect within population

# Bayesian ssGBLUP: simulation

- Performed evaluations

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Information	External BLUP	Local ssGBLUP	Bayesian ssGBLUP	Joint ssGBLUP
<b>Pedigree</b>				
<b>External population</b>	✓			
Local population + 50 external sires used locally				
<b>Phenotypes</b>				
<b>External observations</b>	✓			
Local observations				
50 external sires				
Genotypes				
External EBV and REL				

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# Bayesian ssGBLUP: simulation

- Performed evaluations

Information	External BLUP	Local ssGBLUP	Bayesian ssGBLUP	Joint ssGBLUP
<b>Pedigree</b>				
External population	✓			
Local population + 50 external sires used locally		✓		
<b>Phenotypes</b>				
External observations	✓			
Local observations		✓		
50 external sires				
Genotypes		✓		
External EBV and REL				

# Bayesian ssGBLUP: simulation

- Performed evaluations

Information	External BLUP	Local ssGBLUP	Bayesian ssGBLUP	Joint ssGBLUP
<b>Pedigree</b>				
External population	✓			
Local population + 50 external sires used locally		✓	✓	
<b>Phenotypes</b>				
External observations	✓			
Local observations		✓	✓	
50 external sires				
Genotypes		✓	✓	
External EBV and REL			✓	

# Bayesian ssGBLUP: simulation

- Performed evaluations

Information	External BLUP	Local ssGBLUP	Bayesian ssGBLUP	Joint ssGBLUP
<b>Pedigree</b>				
<b>External population</b>	✓			✓
<b>Local population + 50 external sires used locally</b>		✓	✓	✓
<b>Phenotypes</b>				
<b>External observations</b>	✓			✓
<b>Local observations</b>		✓	✓	✓
<b>50 external sires</b>				
<b>Genotypes</b>		✓	✓	✓
<b>External EBV and REL</b>			✓	

# Comparison with joint ssGBLUP

- Rank correlations ( $r \pm SD$ )

Evaluation	Local animals		External sires	
<b>Without external information</b>				
Local ssGBLUP	0.94	$\pm$ 0.02	0.52	$\pm$ 0.14
<b>With external information</b>				
<b>Bayesian ssGBLUP</b>				
With double counting	>0.99	$\pm$ 0.000	0.99	$\pm$ 0.01
Without double counting	>0.99	$\pm$ 0.000	0.99	$\pm$ 0.01

→ Rankings more similar to those of the joint ssGBLUP

# Comparison with joint ssGBLUP

- Mean squared errors (MSE+SD)
  - Expressed as a percentage of the local MSE

Evaluation	Local animals			External sires		
Without external information						
Local ssGBLUP	100.00	±	32.8	100.00	±	29.1
With external information						
Bayesian ssGBLUP						
With double counting	2.37	±	2.2	1.35	±	1.2
Without double counting	1.97	±	2.1	1.12	±	1.2

→ Importance of double-counting

# Blending: simulation

- 100 replicates
- 2 populations
  - $\pm 1000$  animals/population
  - 5 generations
  - Random matings / cullings
  - Observations (Van Vleck, 1994)
    - Milk yield for the first lactation
    - Heritability : 0.25
  - Fixed effect
    - Random herd effect within population

# Blending: simulation

- Performed evaluations

Information	External BLUP	Local BLUP	Blending BLUP	Joint BLUP
<b>Pedigree</b>				
<b>External population</b>	✓			
Local population + 50 external sires used locally				
<b>Phenotypes</b>				
<b>External observations</b>	✓			
Local observations				
<b>External information</b>				
External EBV and REL (50 external sires)				
Local EBV and REL (all population)				

# Blending: simulation

- Performed evaluations

Information	External BLUP	Local BLUP	Blending BLUP	Joint BLUP
<b>Pedigree</b>				
External population	✓			
Local population + 50 external sires used locally		✓		
<b>Phenotypes</b>				
External observations	✓			
Local observations		✓		
<b>External information</b>				
External EBV and REL (50 external sires)				
Local EBV and REL (all population)				

# Blending: simulation

- Performed evaluations

Information	External BLUP	Local BLUP	Blending BLUP	Joint BLUP
<b>Pedigree</b>				
External population	✓			
Local population + 50 external sires used locally		✓	✓	
<b>Phenotypes</b>				
External observations	✓			
Local observations		✓		
<b>External information</b>				
External EBV and REL (50 external sires)			✓	
Local EBV and REL (all population)			✓	

# Blending: simulation

- Performed evaluations

Information	External BLUP	Local BLUP	Blending BLUP	Joint BLUP
<b>Pedigree</b>				
External population	✓			✓
Local population + 50 external sires used locally		✓	✓	✓
<b>Phenotypes</b>				
External observations	✓			✓
Local observations		✓		✓
<b>External information</b>				
External EBV and REL (50 external sires)			✓	
Local EBV and REL (all population)			✓	

# Comparison with joint BLUP

- Rank correlations (r+SD)

Evaluation	Local animals		External sires	
<b>Without external information</b>				
Local BLUP	0.95	± 0.02	0.54	± 0.11
<b>Only external information</b>				
<b>Blending BLUP</b>				
With double counting	0.99	± 0.004	0.97	± 0.01
Without double counting	>0.99	± 0.000	>0.99	± 0.001

➔ Rankings more similar to those of the joint BLUP

# Comparison with joint BLUP

- Mean squared errors (MSE+SD)
  - Expressed as a percentage of the local MSE

Evaluation	Local animals		External sires	
Without external information				
Local BLUP	100.00	± 26.7	100.00	± 24.5
Only external information				
Blending BLUP				
With double counting	21.20	± 6.2	6.83	± 1.9
Without double counting	0.48	± 0.2	0.23	± 0.1

→ Importance of double counting

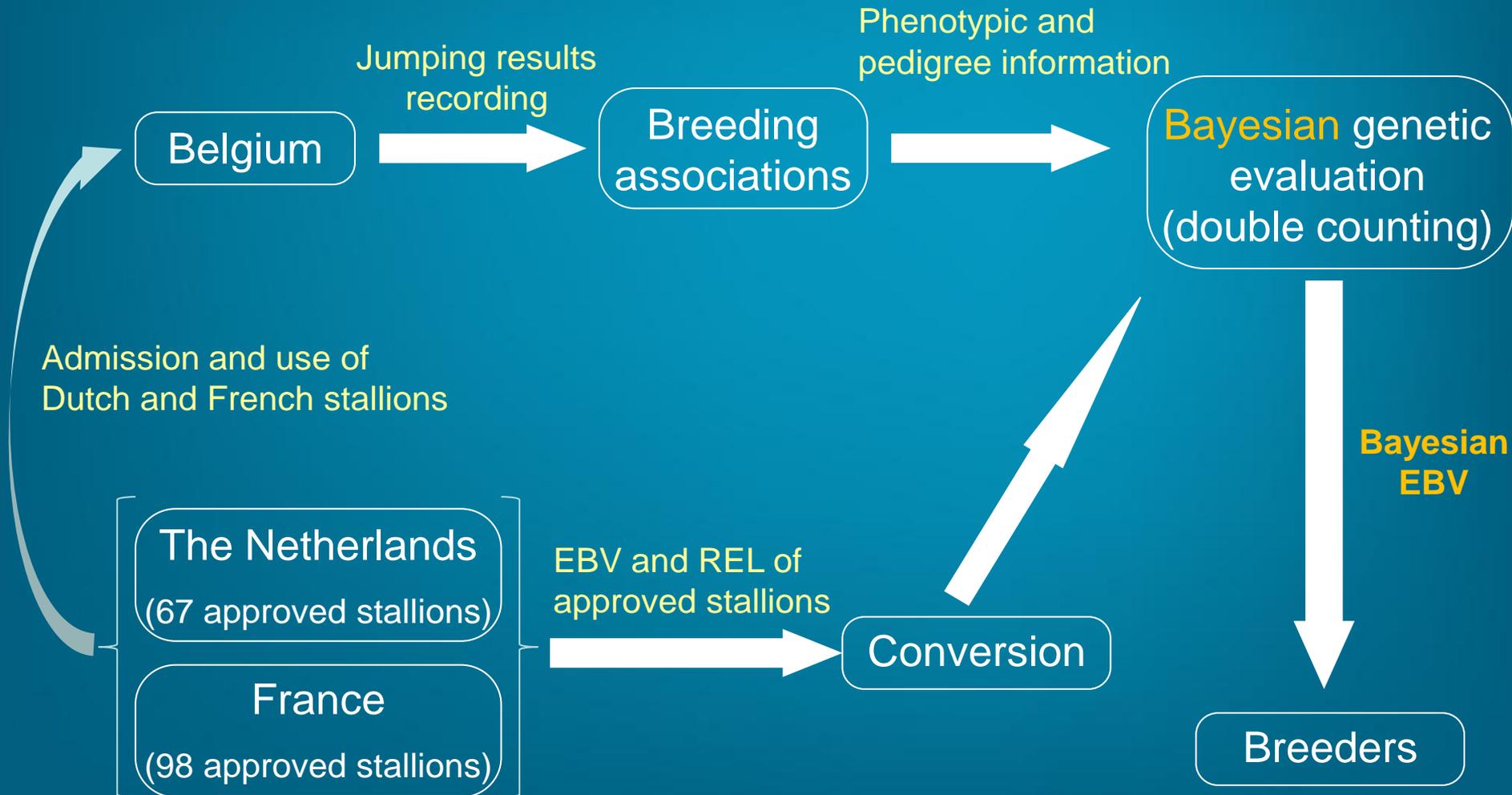
# Conclusion

- Bayesian (ssG)BLUP
  - Rankings most similar to those of a joint (ssG)BLUP
  - Importance of double counting among animals
- Bayesian procedure
  - Reliable integration/blending of multiple external information
  - Simple modifications of current programs
  - Applicable to multi-traits models

# Practical example: jumping horses

- Belgium = crossroad of sport horse populations
  - 2008: >50% approved foreign stallions
  - Export of sport horses
  - Limited Belgian population (~ 4500 foals/year)
- Limited amount of information for reliable local EBV

# Practical example: jumping horses



# Practical example: jumping horses

- Spearman rank correlations

Group of horses	Nb	Spearman rank correlations		
		$EBV_{AI} / EBV_{BI}$	$EBV_{AI} / EBV_E$	$EBV_{BI} / EBV_E$
All horses	101,382	>0.99	-	-
French stallions	98	0.87	0.69	0.90
Dutch stallions	67	0.95	0.61	0.73

# Practical example: jumping horses

- Reliabilities

Group of horses	Genetic evaluation <sup>1</sup>	Datasets <sup>2</sup>					
		I		II		III	
		Mean	SD	Mean	SD	Mean	SD
All horses	A	0.21	0.17	0.17	0.16	0.21	0.17
	B	0.21	0.17	0.17	0.16	0.21	0.17
French stallions	A	0.58	0.23	0.54	0.24	0.52	0.26
	B	0.61	0.20	0.58	0.20	0.57	0.21
Dutch stallions	A	0.51	0.26	0.46	0.26	0.47	0.27
	B	0.52	0.25	0.47	0.25	0.49	0.26

<sup>1</sup>A =Belgian genetic evaluation; B = Bayesian evaluation

<sup>2</sup>I = complete data; II = data for which all performances after December 31th, 2005 were assumed to be missing; III = data for which all French and Dutch stallions' own performances were assumed to be missing

# Practical example: jumping horses

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# Practical example: jumping horses

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# Practical example: jumping horses

- Conclusions
  - External information partially to totally equivalent to 4 years of contemporary horses' performances or to their own performances
  - Resulting Belgian ranking more similar to foreign rankings
  - Improvement of REL
- ➔ Interesting for foreign stallions having no or few Belgian performances

# Further work

- Integration of external genomic information
- Integration of correlated external information
  - To improve the accuracy of (ssG)BLUP for only locally available traits (e.g., fatty acids)

# Thank you for your attention!

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