Digital holographic interferometry with CO$_2$ lasers and diffuse illumination applied to large space reflector metrology

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Digital holographic interferometry in the long-wave infrared domain has been developed by combining a CO$_2$ laser and a microbolometer array. The long wavelength allows large deformation measurements, which are of interest in the case of large space reflectors undergoing thermal changes when in orbit. We review holography at such wavelengths and present some specific aspects related to this spectral range on our measurements. For the design of our digital holographic interferometer, we studied the possibility of illuminating specular objects by a reflective diffuser. We discuss the development of the interferometer and the results obtained on a representative space reflector, first in the laboratory and then during vacuum cryogenic test. © 2012 Optical Society of America

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1. Introduction

Coordinate and deformation metrology of complex shape space structures and reflectors is a recurrent problem addressed by space agencies and companies worldwide. Accurate knowledge of a space structure deformation or a reflector’s surface shape under realistic operational conditions is essential to accurately predict in orbit performance. Consequently, suitable measurement techniques have to be developed and validated to support relevant on-ground qualification and verification testing. The application presented in this paper is related to a continuous need for the European Space Agency (ESA) to support studies of metrology for aspheric reflectors in the infrared, far-infrared and submillimeter ranges. Interest for new methods was also shown in the case of strongly asymmetric radio-frequency reflectors that depart from a global parabolic shape through localized areas of free-form curvature and that are used for producing asymmetric spot beams for specific ground coverage telecommunications. The search for adapted metrology techniques is made more complex because the reflectors can be several meters in diameter. In particular, in the project supporting our study, deformation measurements were to be demonstrated on reflectors with typical diameter of 1 m (with possible extension of the method to 4 m), with deformations ranging from 1 to 250 μm, with the highest possible spatial resolution. For that purpose we have first analyzed the potential optical noncontact methods that were available on the market or described in literature.
In general these can be grouped into two main categories: (1) those using coherent light illumination, e.g., classical interferometry [1] and holography/speckle interferometry [2], and (2) noncoherent optical techniques based on imagery, such as photogrammetry (or its recent digital videogrammetry version) [3], stereo-correlation [3,4], and fringe projection [3,5].

The second category relies on the determination of surface coordinate points from which deformations are obtained by subtracting two measurements. In the case of videogrammetry, targets have to be attached to or projected on the surface, while in digital image correlation a random pattern (made of black dots sputtered on white paint covering the object) is necessary. In fringe projection the surface has to be scattering enough to be able to observe the projected two-dimensional line pattern, which is also the case with digital image correlation using a random projected pattern. In all cases, surfaces under test have to be specially prepared, and this is not acceptable in most space testing. Indeed the surface of flight models cannot be equipped with targets nor covered by paints because the recovery of the surface would be at too high risk for the specimen. Also vacuum thermal tests generally would provoke outgassing of any paint or retroreflector targets, which has to be avoided, so preventing contamination. Despite this, videogrammetry has proven recently that it was a choice method for testing some types of space structures, making use of projected dots [6]. However, the resolution in position of points, and thus deformation, is still too low for our purpose. Indeed the resolution and measurement ranges of these techniques are influenced by the size of object, the number of pixels of the camera, and other factors specific to the technique. For examples in the best cases we found in literature for videogrammetry, resolutions of 10 parts per million (ppm) (i.e., 10 μm on a 1 m wide object) or even 1 ppm [7,8] are achievable, but a large number of measurements and camera positions are required, preventing fast single-shot captures.

The first category of interferometry methods allows fast single-shot measurements of optical phase differences between the object surface and a reference surface (classical interferometry) or between the object itself at different instants (holographic/speckle interferometry), the resolution being driven by the laser wavelength. In classical interferometry [1], several configurations exist but generally one considers reference waves reflected by a high wavefront quality element (plane or spherical) that interfere on an image sensor with the object wave travelling independently from the test object. For testing an aspheric mirror, one has to arrange to illuminate it through diverging or converging beams, depending on the configuration. The interference between both reference and object waves leads to a fringe pattern corresponding to the localized optical path differences, where the distance between two fringes is proportional to the wavelength. When large wavefront differences are present (which is the case with aspheres illuminated by spherical wavefront), interferometers at visible wavelengths quickly show a larger fringe density than cannot be resolved for areas with large slopes. For solving this problem, interferometers at long-wave infrared (LWIR) range (e.g., 10.6 μm with CO₂ lasers) were developed in the past under various configurations like Twyman–Green [9] or Fizeau [10].

However, in the case of deep aspheric mirrors (e.g., parabola with very low f-number) like those found in space telescopes, the slope variations can still generally be too high to allow use of simple spherical illumination lenses even in LWIR. Consequently, complex custom-built null lenses need to be used instead to match the aspheric wavefront [1]. Refractive null-lens correctors are quite usual in the visible, but development of such elements can become expensive in the LWIR with the use of zinc selenide (ZnSe) or germanium (Ge) materials. Despite this, we developed in the past a high-resolution LWIR Twyman–Green interferometer [11] specifically for testing aspheric reflectors of the submillimeter Planck telescope [12,13].

Holographic interferometry (HI) is also a viable alternative used in the thermo-optical and cryogenic performance testing of space reflectors. The advantage of HI compared to classical interferometry is that it can be applied on any kind of surface provided that the object reflects some light toward the hologram sensor. Then, instead of using an expensive null lens, a simple spherical one that collects the necessary rays is sufficient.

An important point for HI is the performance of the recording medium and its ability to be used under realistic conditions (e.g., under vacuum). For continuous monitoring of large deformations, dual wavelength techniques can be envisaged but are difficult to implement [14]. The use of photorefractive crystals as a user-friendly recording medium has been intensively investigated by Centre Spatial de Liège (CSL) group [15,16]. It was then applied for a thermal-vacuum test of large reflectors [17,18], but this technique is also very sensitive to environmental disturbances that required development of specific phase stabilization techniques that were complex to implement [19]. These previous experiments motivated the study presented in this paper. Indeed the idea came to develop an HI method in LWIR that will relax the stability constraints in the setup while providing large deformation displacements in a single-shot interferogram. Given the fact that deformations to be measured on such large reflectors are ranged between 1 and 250 μm, HI in the LWIR domain imposed itself. In particular we consider digital holography (DH), which allows instant recording and readout of holograms. Although evidence of DH can be found during the early years of holography [20], it has gained a considerable interest in the past two decades due to significant improvements of electronic imaging sensors [21,22]. The technique allows numerical reconstruction of diffracted orders (among which is the image of the object of interest) through various algorithms that have been developed by many groups
All these developments were made in visible light. Recent literature presents efforts in extending DH to other spectral ranges, from the ultraviolet [27] to LWIR [28] and terahertz [29,30].

In Section 2 of this paper, we review holography in the LWIR domain. In Section 3, we present some particular aspects related to the use of thermal LWIR radiation that is of great importance to consider and that plays no role in the visible. In Section 4, we discuss the potential setup configurations necessary to observe large specular reflectors. We see that an interesting possibility is to use diffuse illumination of the specular object prior to numerical reconstruction by DH. Since this was never shown in the past, we demonstrate this principle through a series of experiments that are presented in Section 5. In Section 6, we present the DH LWIR setup for monitoring deformation of large reflectors and the results obtained in the laboratory. Section 7 presents the implementation of the setup in the cryogenic vacuum facility at the CSL and verification of the method during thermal cycling.

2. Holography with CO₂ Lasers: A Review

A. Analog Recording of Holograms with CO₂ Lasers

Holography with CO₂ lasers is not a new subject since it was first shown in 1969 by Chivian et al., who used a thermochromic material (cuprous mercuric iodide) for recording at 10.6 μm and readout in the visible with an He–Ne laser [31]. Many works followed by other groups that used a similar setup and recording medium [32] or other recording media: liquid crystals [33], wax and gelatin films [34], bismuth thin films [32,35,36], acrylic and thin films [37], wax [38,39], oil films deposited on glass plates [40], resists [41], poly (acrylic acid) films [42,43], and albumen [44]. All these materials are able to record patterns through relief variations, producing phase holograms that can be processed in situ. Also they show relatively good figures of merit in term of diffraction efficiency. But what seems to remain limited is the resolution of such media with a rapid drop of diffraction efficiency for line spacings larger than 10 lines per millimeter. Also, they all use visible wavelengths for readout, which does not make the application of these materials for real-time HI easy. Double-exposure holograms that are readout with visible lasers have also been tried [35,40].

B. Electronic Recording of Holograms with CO₂ Lasers

The very first evidence of LWIR holographic electronic recording was provided by Løkberg and Kwon [45], who demonstrated electronic speckle pattern interferometry (ESPI) with CO₂ lasers and pyroelectric vidicon cameras. ESPI consists in recording the interference of object wave \( U_o(x,y) \) and a reference wave \( U_R(x,y) \) at the level of a camera focal plane. In ESPI this interference is called a specklegram, and the optical imaging system has its aperture small enough to generate speckles in the object wavefront. Also, to obtain a specklegram that can be resolved by the array sensor, the object and reference wavefronts need to match as closely as possible to each, and in-line reference beams (RBs) are used [2]. Specklegrams recorded at different instants are subtracted from each other to obtain fringe patterns that can be related to the object deformation undergone between these instants.

Applying ESPI with pyroelectric cameras is not easy since the latter are sensitive only to changes in the radiation energy. Therefore, Løkberg and Kwon worked exclusively with vibrating objects for which the speckle pattern intensity was intrinsically varying.

The second evidence of electronic recording of holograms in the LWIR was made by an Italian group who showed for the first time to our knowledge the use of DH at 10.6 μm [28]. DH is a more modern approach of holography, which consists of recording holograms directly on an imaging array sensor. In DH the intensity pattern (hologram) \( I_H(\xi,\eta) \) recorded in the plane of the array sensor \( (\xi,\eta) \) is used to reconstruct numerically the complex object wave field \( U_o(x,y) \) located in the plane \( (x,y) \) situated at a distance \( d \) from the hologram plane/sensor. If the reference complex amplitude in the hologram plane is given by \( R(\xi,\eta) \), the object field is given by the Fresnel transform [23,46]:

\[
U_o(x,y) = \frac{i}{\lambda d} \exp \left( -\frac{2\pi i}{\lambda} d \right) \exp \left[ -\frac{\pi}{\lambda d} (x^2 + y^2) \right] \times \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} I_H(\xi,\eta) R(\xi,\eta) \exp \left[ -\frac{\pi}{\lambda d} (\xi^2 + \eta^2) \right] \times \exp \left[ i\frac{2\pi}{\lambda d} (x\xi + y\eta) \right] d\xi d\eta.
\]

(1)

In practice, the hologram is sampled by the array sensor on \( M \times N \) pixels, of dimensions \( \Delta\xi \times \Delta\eta \). Therefore, Eq. (1) can be written in a discrete form, yielding the computation of the object on \( M \times N \) points, say \( U_o(m,n) \), with \( m = 0,1,\ldots,M-1 \) and \( n = 0,1,\ldots,N-1 \). Noting the similarities between Fourier transform (FT) and Eq. (1), the computation of this field consists in applying an inverse discrete FT to the product of the three first factors under the integral of Eq. (1), say:

\[
U_o(m,n) = \frac{i}{\lambda d} \exp \left( -\frac{2\pi i}{\lambda} d \right) \times \exp \left[ -\frac{\pi}{\lambda d} \left( \frac{m^2}{M^2 \Delta\xi^2} + \frac{n^2}{N^2 \Delta\eta^2} \right) \right] \times \sum_{k=0}^{M-1} \sum_{l=0}^{N-1} R(k,l) I_H(k,l) \times \exp \left[ -\frac{\pi}{\lambda d} (k^2 \Delta\xi^2 + l^2 \Delta\eta^2) \right].
\]

(2)

The authors in [23] point out that the terms outside the sum only affect the overall phase of the
object field. In a typical HI application, where we are
only interested in the object deformation, these
terms remain constant, and they can be neglected
in the computation.

The deformation (or displacement field) is related
to the phase difference between two states of the
object. The phase of the object wave in every point
of the object plane is given by

$$\varphi(m, n) = \tan^{-1} \left[ \frac{\text{Im}(U_o(m, n))}{\text{Re}(U_o(m, n))} \right].$$  (3)

In digital HI (DHI), one computes the phases for two
consecutive states \( \varphi_1 \) and \( \varphi_2 \) of the object and sub-
tracts one from the other to deduce the displacement.
An advantage of DH over ESPI is that it allows the
phase to be retrieved from a single acquisition. An-
other advantage of DH is that the setup does not
necessitate an imaging lens in front of the sensor
(like in ESPI) because the image of the object is re-
constructed numerically and correct focusing of the
image is obtained by setting the distance \( d \) in Eq. (2)
at the same value as the one used experimentally.

DH in the LWIR was first demonstrated by
Allaria et al. \[28\]. They recorded holograms in Mach–
Zehnder optical configuration with pyroelectric array
sensors \[47\] for reconstructing transmission objects.
More recently the same group showed further results
in measuring the three-dimensional (3D) shape of re-
flexive objects, again with the same Mach–Zehnder
configuration \[48\] and pyroelectric camera.

Other LWIR array sensor technologies offer advan-
tages over pyroelectric cameras, in particular un-
cooled microbolometer arrays \[49\]. Recently George
et al. showed DH based on a microbolometer array
\[50\] with an optical setup similar to that of \[28\] and
\[48\]. Microbolometers are now an emerging tech-
nology with a growing market and apply to thermogra-
phy in many civilian, military, and industrial sectors
\[47,51\]. Recently manufacturers have shown mega-
pixel formats \[51\], which make them really attractive
for developments of DH at such wavelengths.

Microbolometer arrays with medium resolutions
(320 × 240 pixels) were considered in ESPI with CO\(_2\
lasers in our early experiments with in-plane ESPI
\[52\] and later with out-of-plane ESPI and lensless
off-axis DH \[53\] with the purpose of measuring large
specular objects. We recently showed nondestructive
testing of larger objects with a 640 × 480 pixel micro-
bolometer camera (Variocam hr from Jenoptik)
\[54,55\]. With the purpose of display of increasingly
larger objects, the Italian group also considered
medium pyroelectric array to larger microbolometer
array formats (640 × 480) under several configura-
tions \[56–58\].

Both groups note the interest of using such long
wavelengths in DH \[53,56–58\] for reconstructing
large objects when compared with similar setup in
the visible: the maximum admissible angle between
the reference and object beams is given by

$$\theta_{\text{max}} = 2 \arcsin \left( \frac{\lambda}{4\Delta} \right).$$  (4)

for square pixels with dimensions \( \Delta = \Delta \xi = \Delta \eta \). The
angle \( \theta_{\text{max}} \) sets the observable size of the object if the
+1 diffracted orders needs to be clearly separated
from other terms. When analyzing the ratio \( \lambda/\Delta 
for visible and CO\(_2\) wavelengths and current sensors
in both domains, one easily determines that \( \theta_{\text{max}} \)
is from 5 to 10 times larger in the LWIR than in the
visible.

3. Particular Aspects of LWIR for DH

A. Thermal Background

The microbolometer arrays that are used in conjunc-
tion with CO\(_2\) lasers in our experiments have a spec-
tral sensitivity ranging from 8 to 14 μm. As is known
in fundamental physics, black bodies at a given tem-
perature emit radiation in a certain wavelength
range (Planck’s law) and Wien’s law states that
the product of wavelength of maximum spectral
radiance and the temperature is a constant equal
to 2.8977 × 10\(^{6}\) nm.K.

It can be calculated that the wavelength of CO\(_2\) la-
sers corresponds to ambient temperatures around
20°C. Radiation emitted by anything in the environ-
ment of work could reach the sensor directly or by
reflection on either the object itself or some parts
of the setup. It is then important to understand
the effect of such thermal backgrounds in DH. Let
us first note that this background is incoherent.
Therefore, it does not participate in the building of
the hologram and then cannot be propagated by
DH. Nevertheless, it will appear as an additive noise
component in the intensity of hologram \( I_H(\xi, \eta) \).
We have analyzed what a typical contribution of thermal
background could be in DH. We consider a lensless
DH setup [like what will be presented in Section 3
(e.g., Fig. 6)] but without either an object in the field
or a laser beam switched on. Then the camera
catches some radiation from the environment of the
setup, as is shown in Fig. 1(a). We call the thermal
contribution \( I_{\text{Thermal}}(\xi, \eta) \) in the plane of the sensor.
When injecting this image in Eq. (2), in place of
the product \( I_H(\xi, \eta)R(\xi, \eta), \) and using a typical recon-
struction distance \( d \) of 1 m, we obtained a central
peak shown in Fig. 1(b). The extent of this peak will
strongly depend on the presence of any object acting

![Fig. 1. (Color online) (a) Typical thermal background in an LWIR lensless DH setup and (b) contribution to the numerical reconstruction.](image-url)
as heat source in the field of view, and therefore we cannot draw any generality from the example shown.

Therefore, we propose to filter this noise in the same way as other authors remove noise in DH. In all experiments presented in this paper, we apply DC-term filtering [59] as well subtraction of reference (R) and object (O) components from the hologram (H), called HRO subtraction, introduced by Skotheim for removing the halo term [60].

The HRO subtraction consists of using modified hologram intensity $I_H(\xi, \eta)$ in place of $I_H(\xi, \eta)$ in Eq. (2) and from which images of reference and object beams, $I_R(\xi, \eta)$ and $I_O(\xi, \eta)$, respectively, are deduced. These images are captured independently by using shutters in both beams, prior to hologram capture. Here we will use the same approach but subtract also the thermal background (T) in addition to the reference and object components from the hologram H, what we will call "HROT subtraction." The intensity of the hologram to be injected in the numerical reconstruction is then given by (leaving aside the $(\xi, \eta)$ dependency)

$$I_H = I_H - I_R - I_O - I_{\text{Therm}}.$$  

We must also take into account that the images of reference and object beams contain the same thermal background. Assuming that the latter has not changed between acquisitions, we can deduce it from the measurements of both other beams. If we add the suffix $m$ to designate the measured images, we can write the hologram intensity to be used in the reconstruction as follows:

$$I_H = I_{H,m} - [I_{R,m} - I_{\text{Therm},m}] - [I_{O,m} - I_{\text{Therm},m}] - I_{\text{Therm},m}$$

$$= I_{H,m} - I_{R,m} - I_{O,m} + I_{\text{Therm},m}.$$  

B. Relationship between Surface Roughness and Reflectivity

The relationship between the observed surfaces roughness and the illumination wavelength shall be considered with importance if one wishes to know with which kind of reflectivity one deals prior to developing an optical instrument. In the case of holography/specule methods, generally having pure (diffuse) scattering reflectivity is preferred because therefore classical imaging systems can be used to focus on the object. In DH, the same is true, and a pure scattering surface will allow numerical focusing without difficulty. Working at longer wavelengths than visible will strongly impact the reflectivity type, as was already mentioned by authors working in LWIR [45]. Yamaguchi [61] has shown that, when the wavelength is close to the surface roughness or smaller, the surface becomes completely scattering and speckle appears. On the other side, specular reflection appears as soon as the wavelength is larger than the roughness and quickly dominates the speckle pattern intensity. Nevertheless, up to some extent the speckle pattern still can be observed, but its intensity is smaller than the specular peak. The total integrated scatter (TIS) represents the scattered light intensity normalized by the intensity of the reflected beam. It is proportional to the square of the ratio between the roughness and the wavelength [62]. Consequently, if the wavelength is 20 times larger, the TIS will be 400 times smaller. Thus, the speckle intensity will be 400 times smaller using a CO$_2$ laser than with an equivalent experiment using a visible laser. In the visible, this problem is well known, and holography/ESPI observation of surfaces having a strong specular reflection requires spraying surfaces under test with scattering powder.

We already discussed this in our earlier works [53], and for metallic surfaces with roughness in the range of a few nanometers, we dealt with this problem by spraying the surface with a white removable powder (developer for liquid dye penetrant nondestructive technique), which is largely used by holographers. In the frame of more recent works related to ESPI with CO$_2$ lasers for nondestructive testing on aeronautical composite structures, we measured the roughness of various materials of interest for that application and found that they were of the same order as the wavelength [63]. This allowed producing speckles in LWIR without spraying the surface, and we were able to apply DHI for successful measurement of large deformations and detection of defects in such samples [54, 55].

In the intermediary cases where both specular and scattering reflectivities are observed, one has to be highly cautious to avoid specular peaks that could saturate or overload the microbolometer array, either by tilting the object (hence placing the specular peak out of the field of view of the sensor) or by spraying the surface with a diffuse scattering material [53].

4. Choice of the Most Appropriate DH Configuration

The request for our project is that the LWIR DH technique has to be adapted to aspheric reflectors, which can be either astigmatic (such as parabolas) or stigmatic (such as ellipses), with slopes that can be quite high as well as showing asymmetric slope changes (like in the case of free-form RF reflectors). Another constraint is that these reflectors can be purely specular or partially specular and scattering, as a function of their roughness and the test wavelength used. It must be noted that, most of time, these reflectors have roughness very small compared to the wavelength, yielding specular reflection.

Having this in mind, two basic cases have been distinguished in our study, which are illustrated in Fig. 2 in the case of a parabolic reflector but can be extended to other shapes. The first one considers the reflector in pure specular illumination and observation configurations [Fig. 2(a)]. The second one considers intermediary diffusers, either at the illumination stage [Fig. 2(b)] or at the observation [Fig. 2(c)]. In the figure, the illumination and observation are not coaligned, but this is for sake of simplicity.
The pure specular case shown in Fig. 2(a) is in fact similar to classical interferometer (of the Mach–Zehnder type) and makes use of illumination through a spherical lens with the point source at typically two times the parabola focal length. In this case rays do not converge in a single point, and a collecting lens (CL) is necessary to intercept the external rays prior to make them interfere with the RB through the beam combiner (BC). The diameter of CL has to be adapted to the optics under test without being necessarily matching perfectly the object wavefront, as would be the case with dedicated null lenses. This non-perfect-matching between the object and RB is not a problem for DH since the technique allows the reconstruction of different parts of the object by adapting the distance $d$ in the numerical reconstruction process.

The second case, presented in Fig. 2(b), makes use of diffuse illumination produced by enlarging the object beam (here with a negative lens), which illuminates a transparent ground glass diffuser, generating a speckled wavefront, which is then reflected by the specimen. This principle has been already demonstrated in HI and ESPI for testing specular objects in visible wavelengths [64–66] and also in the case of transparent objects (for fluid convection analysis) [67]. The scattered light reaches the mirror, which reflects all rays specularly. Part of these rays reaches the camera through the imaging system. These authors note that the imaging system should be focused on the specular object to achieve maximum of contrast in the fringes [65]. Here the CL can be either an imaging lens or any lens to ease collection but not necessarily imaging the object.

Alternatively, no collection lens could be used. In any case, the DH reconstruction algorithm has to be adapted to the situation.

In the third case, the illumination is similar to the pure specular case in Fig. 2(a) but the rays are directed on a diffuser which acts as an intermediary scattering object for DH. We already have used such approach with HI using photorefractive crystals [17,18] at 532 nm for measurements of smaller deformations.

We have analyzed the different scenarios and made a trade-off between the pure specular and the scattering cases. In the specular case, we computed by ray tracing the spot sizes that are obtained with typical parabolic reflectors of interest, taking into account realistic figures of slopes provided by the ESA. It appears that, apart from some examples, the spot size is often too large for the state-of-the-art detectors when no CL is used. In other cases, lenses needed to be built to either illuminate and/or collect light in the case of very large aperture (e.g., for elliptic reflectors). Despite this limitation, the specular case is expected to provide the best interference quality (like in classical interferometry) since it is not disturbed by speckle.

As mentioned above, similar setups of HI and ESPI have been demonstrated at visible wavelengths, making use of ground glass transmission diffusers. Nevertheless, transmission diffusers made of infrared transparent material (ZnSe, Ge) for working with CO$_2$ lasers were not found on the market and had to be custom made. Therefore, we envisaged using roughened metal plate reflecting diffusers. On that basis we kept the principle depicted in
Fig. 2(b) and not Fig. 2(c). Indeed the design of the setup appeared easier with a diffuser replacing a folding mirror in the illumination arm than in the observation, specifically in view of incorporation in our vacuum facility.

Although we did not suspect any counterindication to apply such schemes to DH in LWIR, we have performed simple experiments for checking the validity of using diffuse illumination in DH, prior to full scale implementation. This is presented in detail in Section 5.

5. Diffuse Illumination in DH for Specular Objects

A simple experiment for demonstrating the possibility of using diffuse illumination with DH has first been set up in visible light as shown in Fig. 3. A diode-pumped solid-state laser at 532 nm is first expanded, and part of the collimated beam (RB) is reflected by a beam splitter (BS) and directly travels to a CCD camera after reflection by a BC. Another part of the laser beam is transmitted by BS and is further expanded and folded to reach a reflective diffuser D. The latter consists of a metallic plate roughened by sanding. Although we have not measured its roughness, we can say that it reflects partially specularly and diffusively. The setup configuration is a lensless Fresnel DH setup with off-axis RB. The size of the object has been limited, and the angle between reference and object beams has been chosen for having good separation of the different terms at the reconstruction. Fig. 4 shows the result of the numerical reconstruction [Fig. 4(a)], the masked image of the focused object selected [Fig. 4(b)], and a zoom of the speckle pattern located in the plane of the mirror object [Fig. 4(c)]. It can be seen that the average intensity of the speckle image is not homogeneous. This is because the surface of the diffuser was partially specular and a perfect Lambertian scattering profile proved difficult to obtain by means of a sanding process.

We have analyzed the behavior of the speckle pattern when the mirror object is rotated and for different distance of DH reconstruction. Fig. 5 shows the zoomed speckles in two situations. The first one [Fig. 5(a)] concerns the case of correct numerical focusing; i.e., the hologram is reconstructed with distance $d$ equal to the true distance between the specular object and the sensor plane. The second one [Fig. 5(b)] concerns out-of-focus reconstruction. Each shows speckle grains of which positions are compared before and after rotation, left and right images, respectively. In the case of correct numerical focusing, when the mirror object is rotated out of plane, no speckle movement appears. The only variations are intensity changes of speckle grains. On the contrary, in the case of incorrect numerical focusing, speckle movement is observed during object rotation. This should cause decorrelation degrading the fringe visibility, as was observed by Hansen with HI and ESPI using an imaging lens [65, 66].

On the basis of this first experiment in the visible, we settled a similar setup with a CO$_2$ laser and a microbolometer array camera to perform displacement field metrology on a specular surface (Fig. 6). The beam from the CO$_2$ laser (from the VM-TIM company, emitting 8 W at 10.6 μm) is split in two parts by a BS that reflects 90% of the beam and transmits 10% (ratio $R_{90}/T_{10}$). The transmitted part is the RB that is folded, expanded, collimated, and then directed onto the microbolometer camera through the BC. The latter is a Jenoptik Variocam hr camera module (640 × 480 pixels, pixel size $Δ = 25$ μm) without objective lens attached. The BC is a $R_{50}/T_{50}$ BS. Both BS and BC are BSs made of ZnSe glass with suitable coating. The beam reflected by BS is expanded and folded to illuminate the diffuser. The latter is made
of a metallic plate (Invar) that is coated by a scattering powder yielding generation of speckle that can be resolved after reflection onto the specular object. The object is a plane mirror (80 mm diameter) coated with aluminum mounted on a rotation stage for performing well-controlled out-of-plane rotation (tilt). Since the laser is polarized, the setup also includes a polarizer $P$ that allows the reduction of the RB power and then equalizing reference and object beam intensities at the level of the array sensor for maximizing the hologram contrast. The angle between both beams has been arranged to allow off-axis DH and clear separation of diffracted orders.

Fig. 7(a) shows the result of DH reconstruction in amplitude, and Fig. 7(b) the same after applying filtering of DC term \[ \text{\textsuperscript{59}} \] and HROT subtraction explained in Section 3.A. To apply the HROT subtraction, one must record separately the thermal background and object and RBs independently to one another during a preliminary step, which is possible by adding shutters placed in the object and reference arms, Sh1 and Sh2 in Fig. 6, respectively. Figure 7(c) shows the difference of the reconstructed phases obtained after rotation of the mirror. Figure 7(d) shows the useful part of the mirror from which we deduced the displacement, knowing the geometry the rotation angle.

To perform analysis of the metrological performances of the technique, we have used a commercial interferometer from HP (model 5519A) for simultaneous high-accuracy measurement of the rotation angle by attaching necessary retroreflecting elements to the rotation stage of the test reflector. We varied the angle and captured the hologram and subsequently performed computation of the angle from the recovered phase differences. The angles obtained by DHI are plotted, in Fig. 8, as a function of those measured directly by the HP interferometer, as is shown. These measurements show a good agreement except for higher angles where the fringes cannot be resolved anymore. The measurement uncertainty of the commercial interferometer is 0.1 arc sec and corresponds to a displacement of 0.036 $\mu$m for the tested mirror. Therefore, one can consider that the difference between the measurement performed by the DH with diffuse illumination and the commercial interferometer corresponds to the uncertainty of the DH method. These results allowed us to determine that the uncertainty of DH is 1.5 $\mu$m as long as the number of pixels per fringes is higher than 13.

It must be noted that, if the diffuse illumination works well with small plane objects, it can become more difficult to apply with large mirrors, especially

![Fig. 5. Observation of speckle (zoomed image) reflected by a specular object rotated out of plane: (a) DH reconstruction correctly focused on specular object and (b) DH not correctly focused.](image)

![Fig. 6. Setup for studying DH in LWIR on specular object illuminated by a reflective diffuser.](image)

![Fig. 7. Numerical reconstruction of a plane mirror by DH in the LWIR: (a) amplitude, (b) amplitude after filtering of DC term and HROT, (c) phase difference after rotation of mirror, (d) excerpt of phase difference on the mirror zone.](image)
convex ones, or with specular surfaces with arbitrary shapes. In the cases of interest in our applications, we most often have to test concave mirrors, which are probably the easiest ones to deal with, even with very large reflector sizes.

6. DH Setup for Observation of Aspheric Reflectors

The test specimen that is used in the experiment is a demonstration reflector of the ESA space mission HERSCHEL [68]. Technological demonstrators of submillimeter reflectors were developed during early studies of the mission (earlier named FIRST, for Far InfraRed and Submillimetre Telescope), and one of them is considered for demonstration of our technique, as was also the case in previous developments [17,18]. The test object (Fig. 9) is a concave parabola made of a carbon fiber reinforced plastic structure with gold coating. It has a diameter of 1.1 m and focal length \( f = 1.58 \) m.

As already discussed, we selected a scheme corresponding to Fig. 2(b), with diffuse illumination provided by a reflective scattering plate. To limit aberrations, it is preferable to work with illumination and observation in line. Therefore, the design is based on a Mach–Zehnder configuration and is shown in Fig. 10. The elements of the drawings are at the same scale except the reflector, of which size and distance to the setup are reduced, as well as the least confusion circle (LCC), which is drawn larger that actual size. The laser beam is expanded by combination of lenses L1–L2. The beam is split in two by the beam splitter BS1 (R1/T99). The transmitted part is expanded by lens L3 and illuminates the reflective diffuser D. The latter is an Invar plate that is covered by white scattering powder already discussed in Section 5 and that has a roughness of typically 4 \( \mu \)m. This makes the diffuser partially specular and scattering. It is placed at 45° incidence, which folds the beam toward beam splitter BS2 (R50/T50), which in turn illuminates the reflector. The diffuser is placed at around 2\( f \), i.e., 3.16 m, and the parabola reflects the beam backward in the direction of BS2. The rays are focused in a blur spot (LCC). A ray tracing allowed location of the LCC near 2\( f \), at 3.194 m from the reflector. This spot could be located directly at the sensor S position and superposed to the RB. However, as is shown in the figure, we placed a relay system formed by combination of lenses L4 and L5. Therefore, the LCC is imaged on the array sensor of the camera. The reason for this addition is twofold. First, it allows resampling of the object image to adapt its size to the detector by adjusting the focal length ratio between L4 and L5. Second, it is related to the implementation of this setup in a vacuum chamber, which we will present in Section 7. Because both the laser and the LWIR camera are not vacuum compatible, they have to stay out of the chamber and beams have to pass through LWIR windows of which thickness must be adequate to avoid bending and failure due to the pressure difference. In function of these constraints and other ones related to the geometry of the vacuum chamber access flange, the only position for these windows is as shown by the dotted line in Fig. 10. One window will be placed in the enlarged collimated beam between L2 and BS1, and a second one between L4 and L5.

The RB is formed by the part of the beam reflected by BS1. It is first made incident to a mirror mounted on a piezo translator (MPZT), which reflects it backward through BS1 and the BC (R50/T50), which in turn reflects it partly onto the sensor. A lens L6 is placed in the collimated RB and forms an afocal

![Fig. 8. (Color online) Comparison between the measurements of rotation angle from LWIR DHI of a mirror illuminated by reflective diffuser and those measured directly on the same mirror using a commercial interferometer.](image)

![Fig. 9. (Color online) FIRST demonstration reflector on its mount.](image)
system with lens L5 in such a way the RB is collimated on the sensor. The RB can be made incident at an adequate angle on the sensor for applying off-axis DH. A variable neutral density filter is placed in the reference arm for equalizing the intensities of object and RBs on the sensor. Two beam dumps are placed in transmitted beams which are not used in the setup. At last two shutters (Sh1 and Sh2) are used for separate acquisition of object and reference images for filtering noise in the image, as discussed earlier in the paper.

It is possible to calculate analytically the maximum size of the object from the sampling requirements as well as the geometry of the object and RB. For that, we followed an approach similar to the authors considered the case of in-line Fresnel DH. Here we apply it to off-axis DH. First, let us consider that the sensor with pair L4–L5 in front is equivalent to a lensless system because it only acts as relay imagery from the LCC to the sensor (with possible magnification). Therefore, we have a recording situation depicted in Fig. 11 where the object is the LCC and rays from the object interact with the RB, which is collimated and is oriented to avoid overlapping of reconstructed orders. We can determine the largest angle \( \theta \) between the object and RBs. As is shown in Fig. 11, this angle is formed by the ray issued from the lowest point of the LCC and reaching the highest point of the sensor \( S \), on the one side, and the lowest ray of the RB on the other side. The maximum value of this angle \( \theta_{\text{max}} \) is deduced from the sampling theorem and given by Eq. (4), which can be simplified in the case of small angles to \( \theta_{\text{max}} = \lambda / 2\Delta \). The pixel dimension of the Variocam is \( \Delta = 25 \mu \text{m} \), which gives a maximum angle of 0.212 rad. From Fig. 11, it comes that the size of the object is related to this angle by

\[
\frac{L + N \Delta}{2d} = \tan \frac{\theta}{2} = \frac{\theta}{2} = \frac{\lambda}{4\Delta}.
\]  

(7)

from which we find that the maximum size of the LCC is

\[
L_{\text{max}} = \frac{\lambda d - 2N\Delta^2}{2\Delta}.
\]

(8)

Since L4 and L5 can have different focal lengths, \( f_4 \) and \( f_5 \), respectively, they can be used for optimizing the sampling of the object image to benefit as much as possible of the sensor resolution. If we define the sampling interval in the plane LCC by \( \Delta' = (f_4 / f_5) \Delta \), the size of the object \( L'_{\text{max}} \) is now given by

\[
L'_{\text{max}} = \frac{\lambda d - 2N(\frac{f_4}{f_5} \Delta)^2}{2(\frac{f_4}{f_5} \Delta)}.
\]

(9)

with \( d' \) the distance between LCC and the reflector of which value was found by ray tracing to be equal to 3.194 m. With equal focal lengths for L4 and L5 and considering \( N = 480 \), it is found that \( L'_{\text{max}} = 0.665 \text{ m} \). This value is smaller than the actual size of the reflector, which is 1.1 m. Therefore, we will have an overlap of the reconstructed orders. For avoiding this, we can use different focal lengths

Fig. 10. Final design of the LWIR DH interferometer with diffuse illumination for large space reflector.

Fig. 11. Geometry of the DH recording setup.
for the pair \(L_4-L_5\). We found stock ZnSe lenses with \(f_4 = 75\) mm and \(f_5 = 127\) mm, which gives \(L_{\text{max}} = 1.139\) m and is compatible with the reflector.

Although the image and its conjugate are well separated under these conditions, the resolution of the useful image is not maximized because it occupies one quadrant of the detector, i.e., maximum \(240 \times 240\) pixels, which is poor. To maximize the spatial resolution, we have another possibility, which is to allow overlapping orders and using the phase shifting to separate orders [70], which is typical to the in-line DH configuration. The phase-shifting technique has been implemented in the setup by means of the MPZT (in Fig. 10). Several images are recorded in sequence between which the mirror is shifted perpendicularly to the beam to create a piston effect between the images. This technique has the disadvantage that it takes a longer time for capture compared to the single-shot capability of off-axis DH. Moreover, it further imposes some stability in the setup during the acquisition sequence. Therefore, we lose the interest of off-axis DH and its possibility to access the phase of high-speed phenomena in single shot. Nevertheless, in the case of cryogenic tests, as presented in the Section 7, the temperature changes are quite slow and the acquisition times can be considered extremely small in comparison. From equations similar to Eq. (9) but dedicated to the in-line case [69], we calculate that, with \(f_4 = f_5\), we obtain \(L_{\text{max}} = 1.34\) m. Figure 12 shows the results obtained after application of this technique to reconstruct the parabolic reflector, both in modulus [Fig. 12(a)] and in phase difference [Fig. 12(b)] after an out-of-plane rotation is applied to the reflector. It must be noted that the object is not on the same optical bench than the DH setup. Despite this, we were able to capture holograms without difficulty and with perturbations in the laboratory (vibration and equipment noise, people circulating, etc.), whereas this was not possible with interferometers in the visible.

### 7. Application in Cryogenic Test

Following the laboratory validation, the interferometer has been implemented in the FOCAL5 vacuum chamber of the CSL [71] to measure the deformation of the reflector at cryogenic temperatures. The facilities of the CSL are all equipped with optical benches that are standing on a seismic block disconnected from the building and the vacuum chamber itself. The throughputs of the feet of the optical bench are especially designed to not allow for leakage when the vacuum is made into the chamber. Such optical benches are a prerequisite for interferometric monitoring of large specimens because they damp any vibration coming from the building or outside. The chamber has a 5 m diameter and is 10 m long. It is fully equipped with nitrogen and helium circulation circuits with regulation for reaching specific temperature sequences on specimens.

The configuration of the thermal-vacuum test uses the same optical configuration as in Fig. 10. However, the optical setup has been split in two parts, as shown in Fig. 13. The first part is outside the vacuum chamber (outer bench) and holds the vacuum-incompatible equipment (i.e., the laser and the thermographic camera). The second part (inner bench) is inside the chamber and contains the interferometer. The separation and combination of the object beam and RB is realized in the chamber to minimize the impact of differential vibration between the inner and outer bench. The dimensions of the optical setup (inner and outer benches) are exaggerated with respect to the facility and reflector dimensions. Also, the DH setup is drawn vertically, whereas it is actually horizontal. The reflector is located at the adequate distance from the interferometer and surrounded by a thermal shroud. The latter is made of copper plates painted in black on their inner part and connected to nitrogen circulation pipes. The shroud allows changing the temperature on the reflector through radiative transfer, and it is completely closed except for a small aperture for the beams to reach the reflector and be reflected backward to the DH setup.

Several thermal cycles were operated and the holograms were captured on a regular basis. Numerical reconstruction was performed, and the phase difference was computed between pairs of temperature states during the cycle.

The measurement of the displacement field for a temperature variation from 224 K (where the initial digital hologram is recorded) down to 107.5 K of the reflector is shown in Fig. 14: Fig. 14(a) is the raw phase difference, Fig. 14(b) is the masked region of interest obtained after applying a median filtering on Fig. 14(a), and Fig. 14(c) is the unwrapped phase [2] from which the displacement field can be deduced [2]. Figure 14(d) shows the total displacement field, and Fig. 14(d) (Media 1) shows the displacement evolving in function of temperature. We are interested in the deformation that is obtained by removing the rigid body motions from the total displacement field. These are tilts and defocus that were removed from the phase by Zernike analysis [1]. The remaining result is shown in Fig. 15(b).

For validating the performance of the LWIR DH interferometer, the results have been compared to measurements made on the same reflector some years before, with a high spatial resolution LWIR interferometer also developed at CSL [11] and which

![Fig. 12. Application of phase-shifting DH to the FIRST reflector with diffuse illumination. (a) Modulus and (b) phase difference after out-of-plane rotation of the reflector.](image-url)
made use of a null lens. We compare the deformation measured with the two techniques in Fig. 15 for the same temperature range. The RMS difference is 1.6 μm, which is close to the measurement uncertainty that we found for the DH technique with diffuse illumination (Section 5).

Fig. 13. (Color online) Scheme of the DH interferometer implemented in the vacuum chamber FOCAL5 of the CSL.

Fig. 14. (Color online) Displacement field obtained between 224 and 107.5 K. (a) Phase difference, (b) after masking and median filtering, (c) after phase unwrapping, (d) 3D plot of total displacement (Media 1 shows increasing displacement when temperature changes).
8. Conclusions: Future Prospects

We have presented the development of a digital holographic interferometer in the LWIR and which uses a CO₂ laser and a microbolometer array sensor. The target application is the cryogenic test of large space aspheric reflectors working in the far-infrared and submillimeter ranges.

The advantage of an LWIR digital holographic interferometer is twofold: first, it is able to measure deformations 20 times larger than similar interferometers working in the visible, and second, the stability constraint of the holographic setup is relaxed. The second advantage of LWIR DH is that it can reconstruct objects 5–10 times larger than in the visible. We have discussed some features related to the LWIR. First, an incoherent thermal background is present in the hologram, and we proposed a simple way to filter it. Second, the reflectivity appears more specular in the LWIR than in the visible. This difficulty coupled to the fact that the aspheric space reflectors are intrinsically specular led us to study the possibility of diffuse illumination. Starting from similar experiments in visible ESPI, we show that a reflective diffuse illumination can be used for illuminating specular objects that are further reconstructed numerically by DH. We first have proven this in the visible and then in the LWIR spectrum, prior to applying it to the measurement of the rotation of plane mirrors.

Then we presented in details the design of our LWIR DH interferometer, which makes use of diffuse illumination and which is used for observation of a parabolic reflector [coming from the ESA FIRST (HERSCHEL) project]. We have shown that, among the different existing DH geometries, the in-line configuration with phase shifting is the most appropriate in terms of resolution for our object. The fact that phase shifting implies a longer time of image capture is not a problem because the deformations that will be observed during cryogenic tests are much slower than the phase-shifting sequence.

After development of the DH setup and verification on the FIRST reflector in the laboratory, the whole setup and specimen was implemented in a cryogenic facility of the CSL, where vacuum-thermal cycling was operated and the deformation measured during this time. The results are found in very good agreement with similar tests performed with classical LWIR interferometry making use of null lens.

We point out here that, compared to classical null-lens interferometry, DHI allows a much simpler approach and that components of the shelf can be used. Indeed, DH can reconstruct image of object at arbitrary distances, and there is a priori no need of closely matching the aspheric wavefront with an expensive and dedicated optical assembly like a null lens. The diffuse illumination helps in the fact that it generates rays that can be collected easily by simple lenses and that form an object beam that can interfere with a RB in a DH setup. This simple principle opens the way for testing more complex specular reflectors, either aspheric (astigmatic or stigmatic like ellipses) or arbitrary shapes like free-form RF reflectors used for Earth telecommunications from space.

At the time of writing this paper, new experiments are ongoing for comparing the diffuse illumination with the specular case, as is discussed in Section 4. Also the case of an elliptic reflector (such as secondary reflector of the Planck telescope) will be treated as well. We also investigate the possibility of testing free-form telecommunication antenna reflectors, which is an even more challenging application.

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