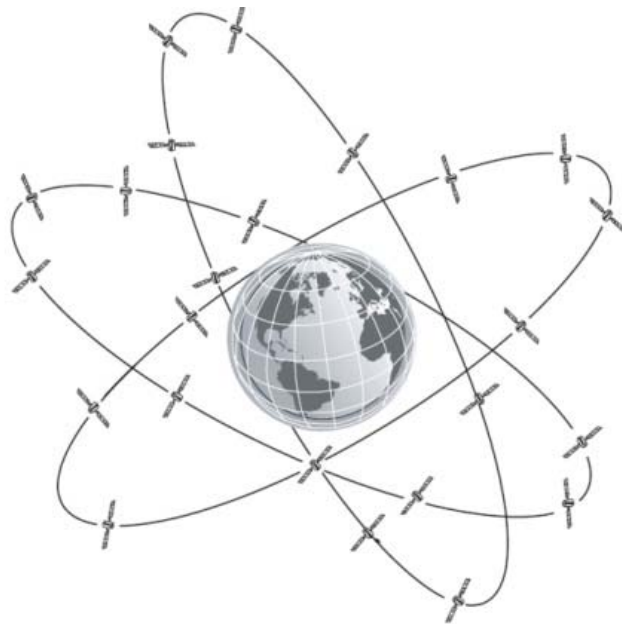


# Precise Point Positioning

## Performances under Ionospheric Scintillations



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Geomatics Unit

University of Nottingham, UK  
Nottingham Geospatial Institute

New Navigator Seminar 2012  
14 June 2012  
NGI, The University of Nottingham



Project

Geometry

Stochasticity

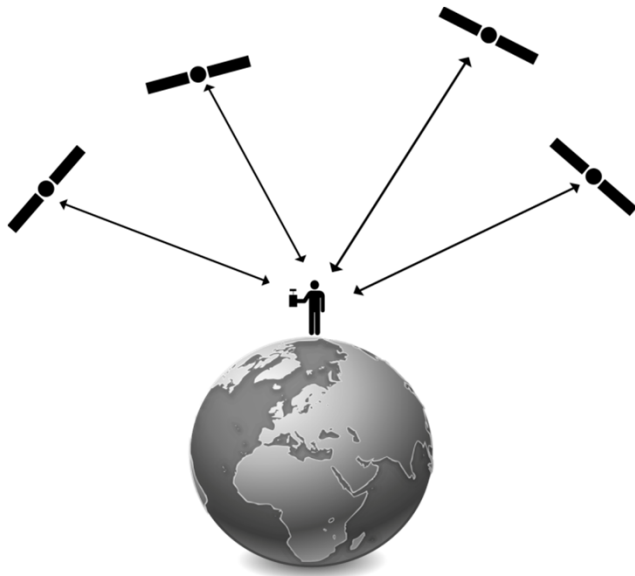
**Project**

Geometry

Stochasticity

# The Precise Point Positioning – PPP – is an advanced satellite positioning technique

## SPP – Standard Point Positioning



$$P_p^i = D_p^i + \underline{T_p^i} + \underline{I_{p,m}^i} + c(\underline{\Delta t^i} - \underline{\Delta t_p}) + \underline{\varepsilon_{p,m}^i}$$

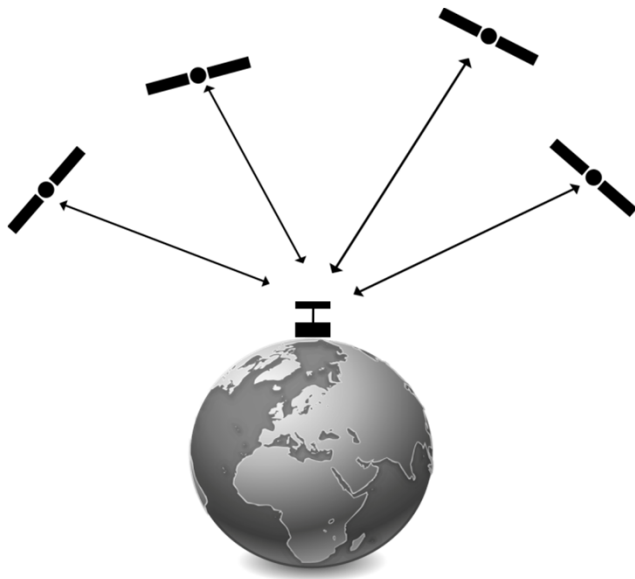
...

...

...

# The Precise Point Positioning – PPP – is an advanced satellite positioning technique

## PPP – Precise Point Positioning



$$i, p \left\{ \begin{array}{l} P_{IF} = D + T + c(\Delta t^i - \Delta t_p) + \varepsilon_{P_{IF}} \\ \phi_{IF} = D + T + c(\Delta t^i - \Delta t_p) + N\lambda + \varepsilon_{\phi_{IF}} \end{array} \right.$$

Ionospheric Free (IF) model

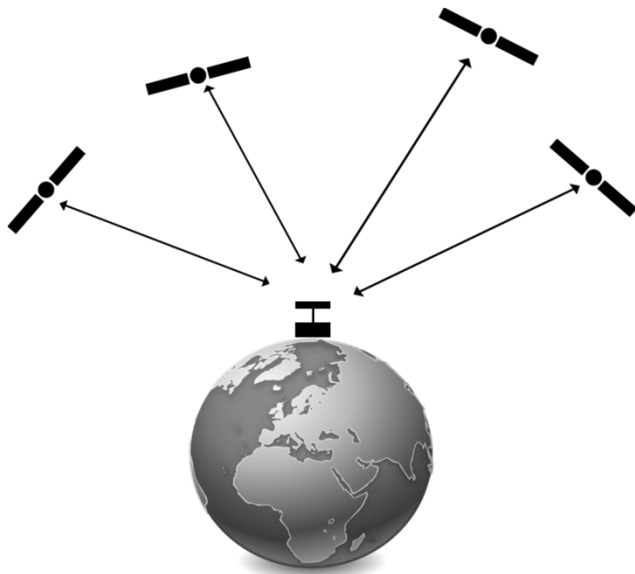
Tropospheric delay is estimated

Code pseudorange and carrier-phase

Precise satellite clock and orbits products

# The Precise Point Positioning – PPP – is an advanced satellite positioning technique

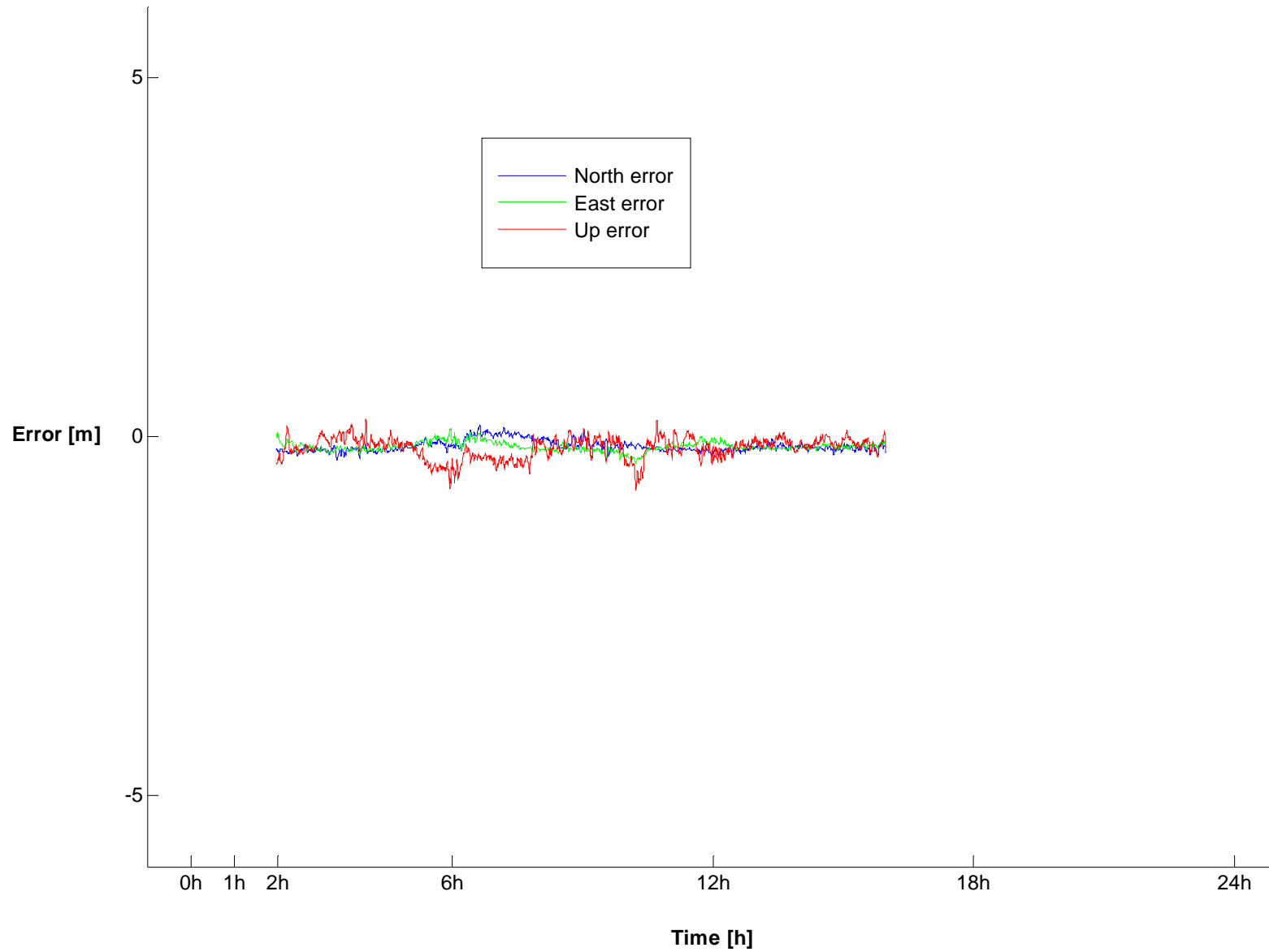
## PPP – Precise Point Positioning



$$i, p \left\{ \begin{array}{l} P_{IF} = D + T + c(\Delta t^i - \Delta t_p) + \varepsilon_{P_{IF}} \\ \phi_{IF} = D + T + c(\Delta t^i - \Delta t_p) + N\lambda + \varepsilon_{\phi_{IF}} \end{array} \right.$$

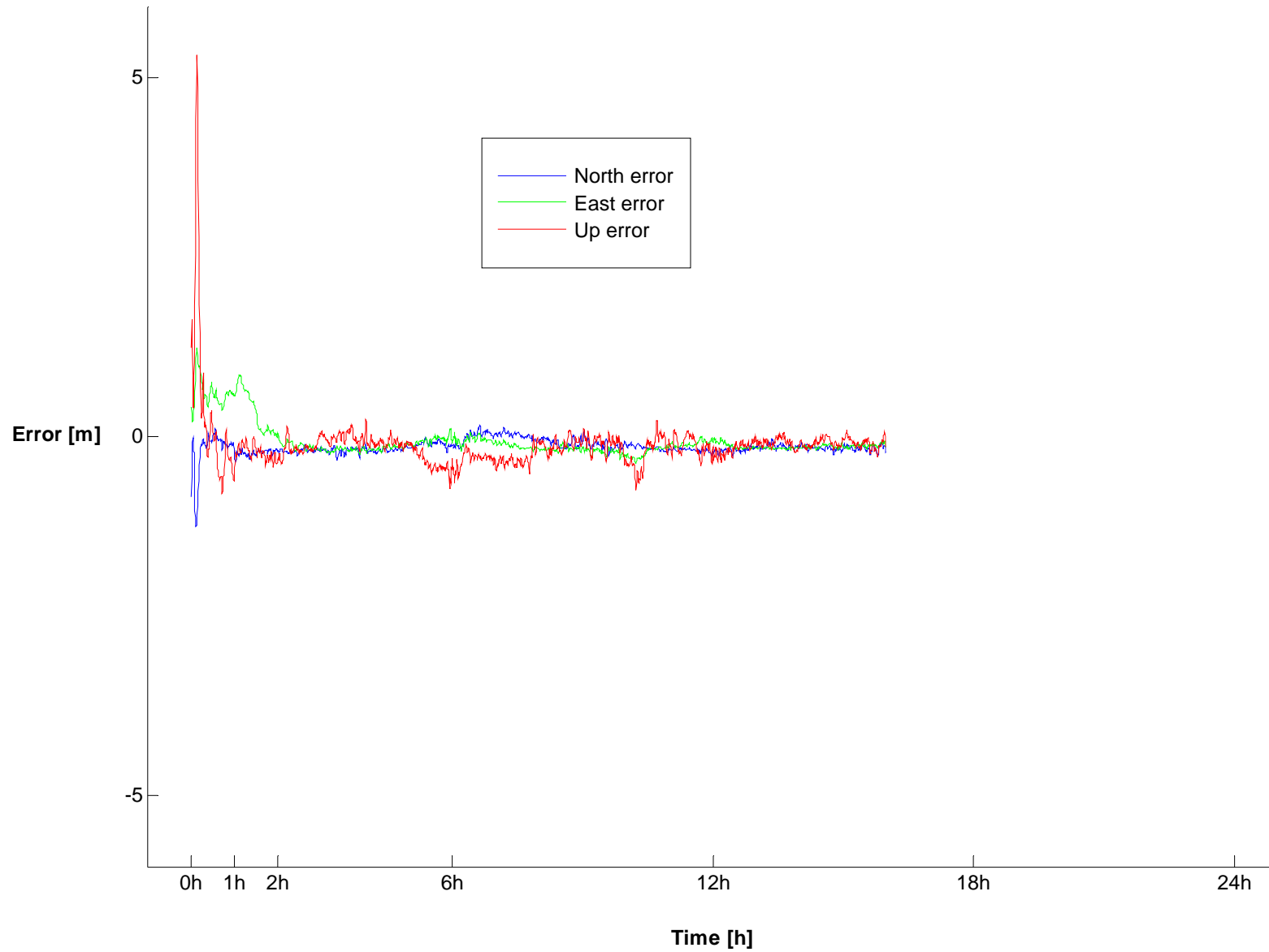
→ Iterative Least Square Adjustment (LSA)

# The PPP is a performant technique

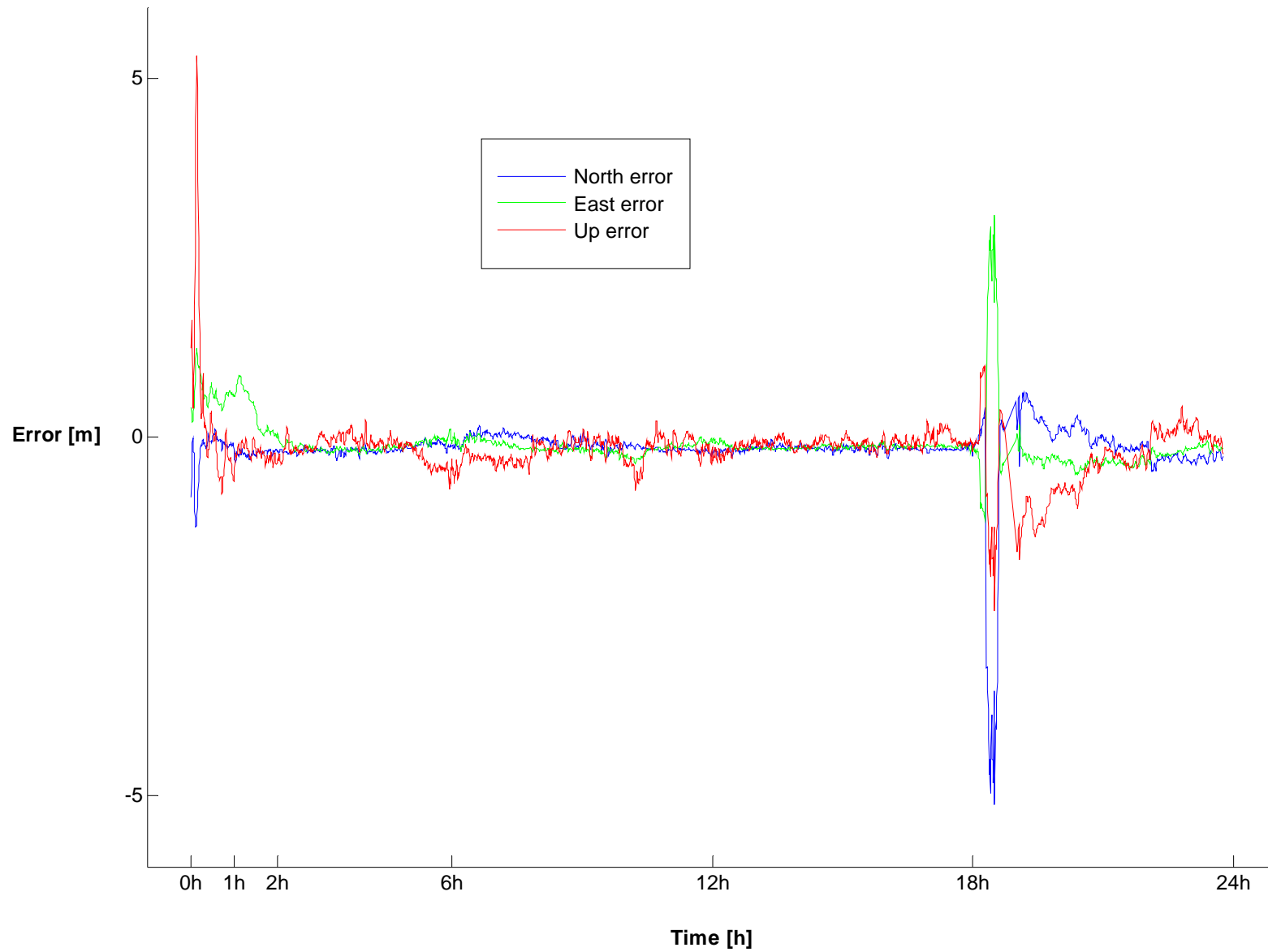




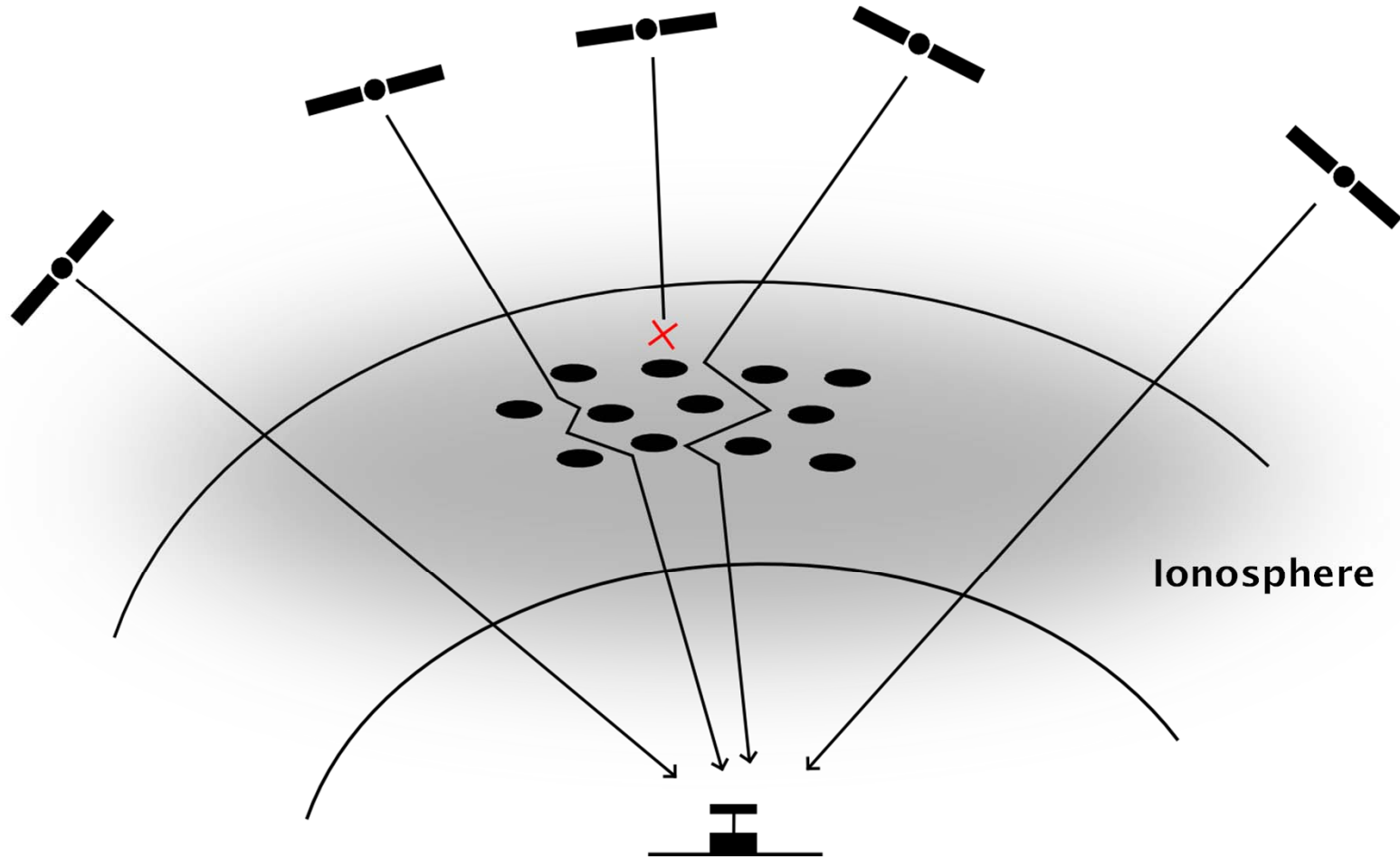
# The PPP suffers from several weaknesses



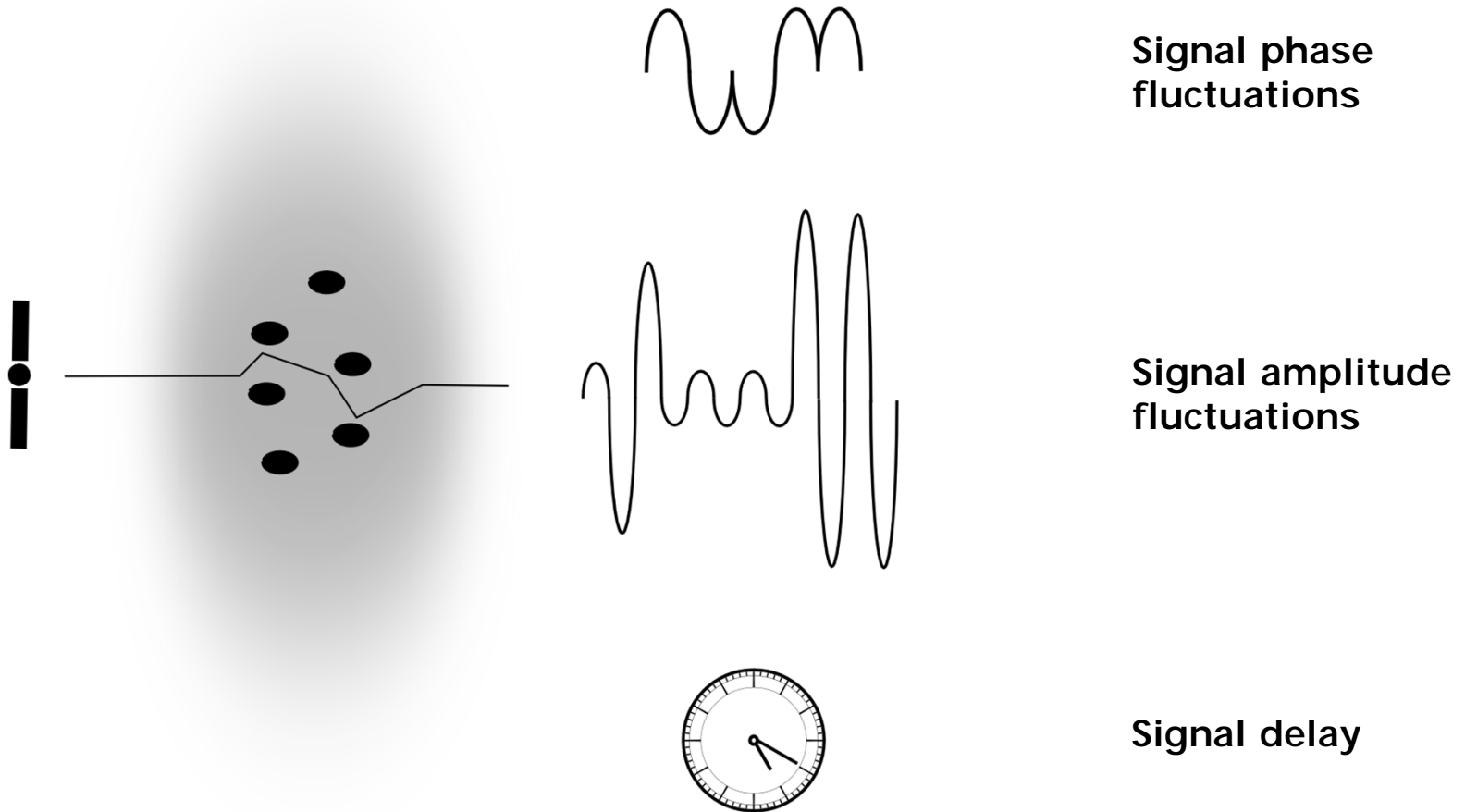
# The PPP suffers from several weaknesses



# Ionospheric scintillations disrupt satellite signals propagation



# Ionospheric scintillations degrade satellite signals quality



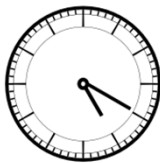
# Ionospheric scintillations degrade satellite signals quality



Signal phase fluctuations



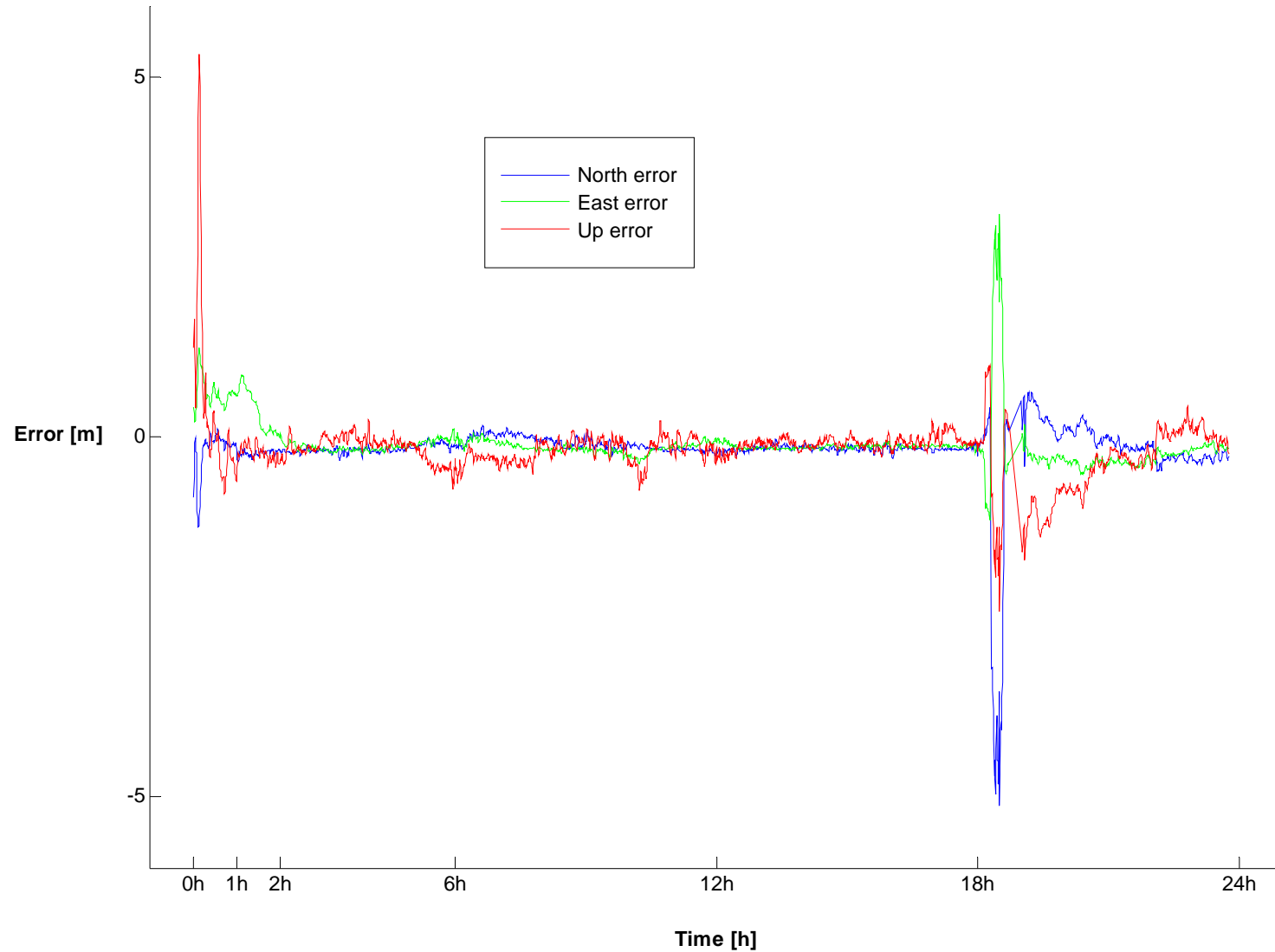
Signal amplitude fluctuations



Signal delay

- *Cycle slips*
- *Ambiguity resolution processes*
- *Additional convergence time*
  
- *Measurement noise*
- *Signal power fluctuations*
  
- *Lost signals*
- *Geometry troubles*
  
- *Signal delay*

# Ionospheric scintillations decrease PPP performances



# PPP performances under ionospheric scintillations can be improved

WP0 – GNSS Tools

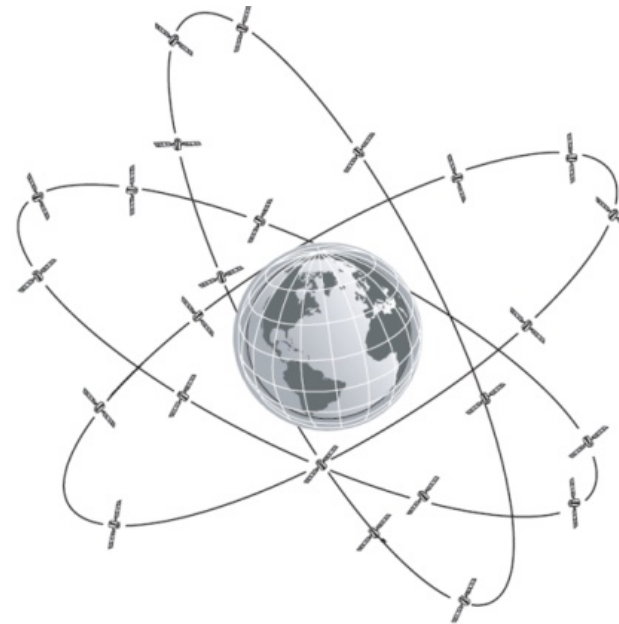
WP1 – Signals

**WP2 – Geometry**

**WP3 – Stochasticity**

WP4 – Model

WP5 – Ambiguity



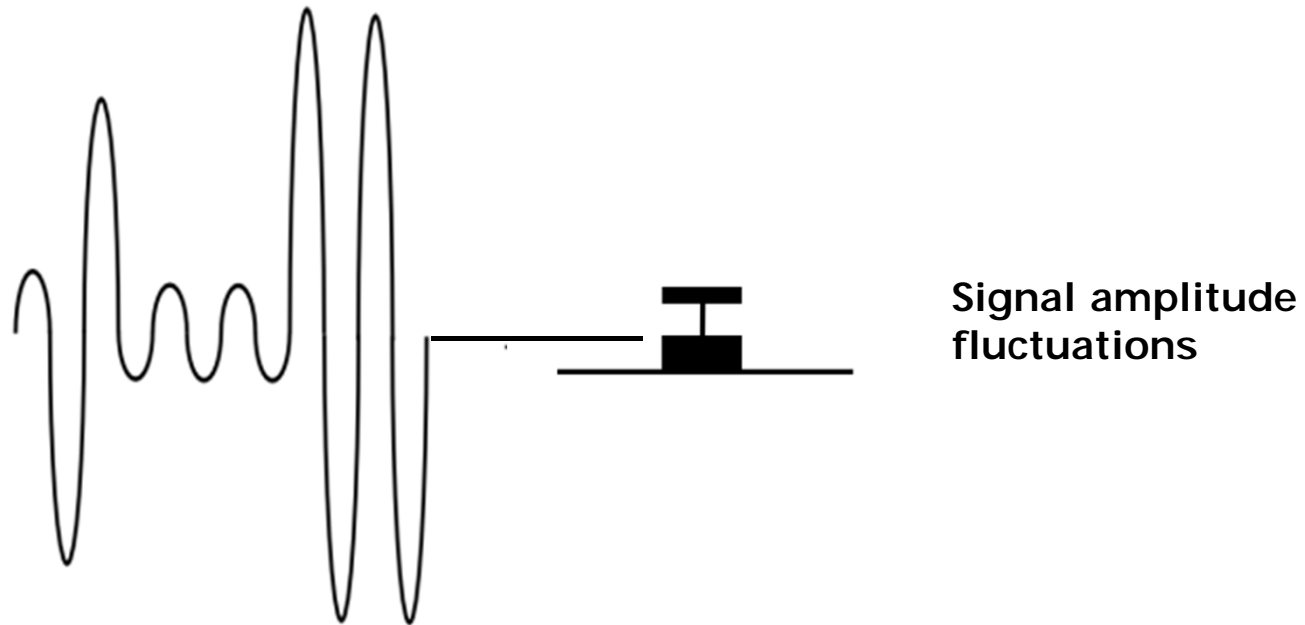
Project

**Geometry**

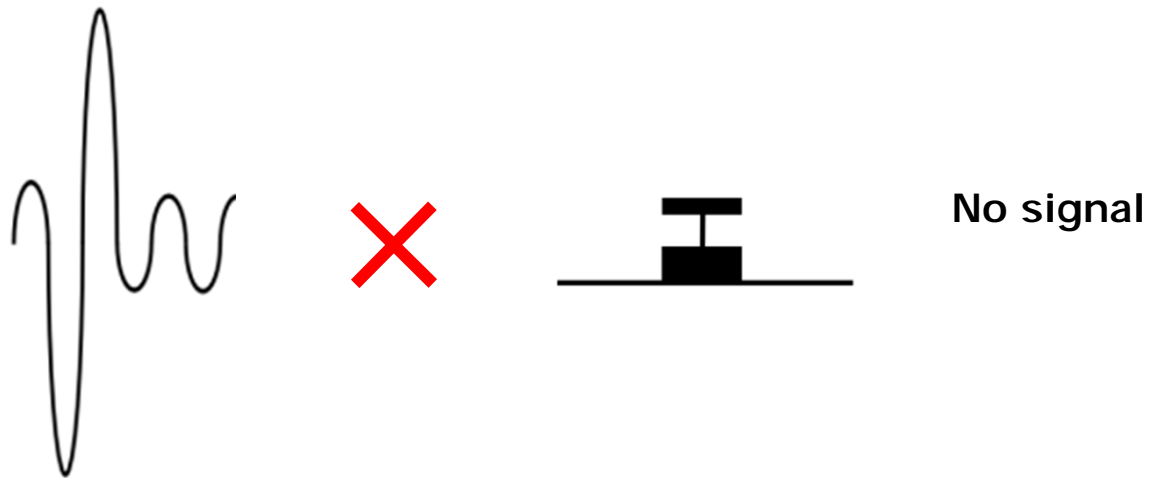
Stochasticity



Ionospheric scintillations reduce the number of available satellites

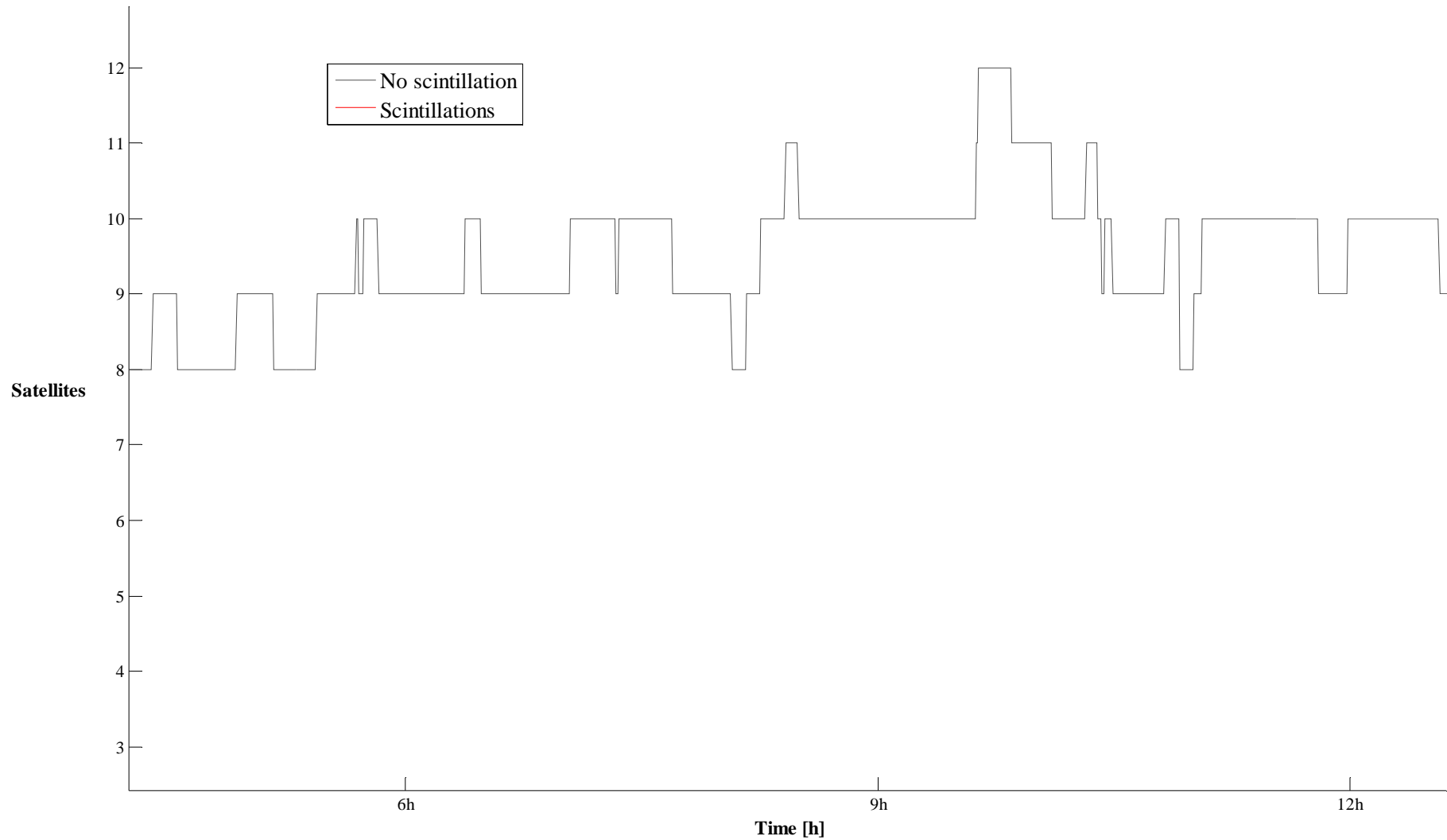


Ionospheric scintillations reduce the number of available satellites

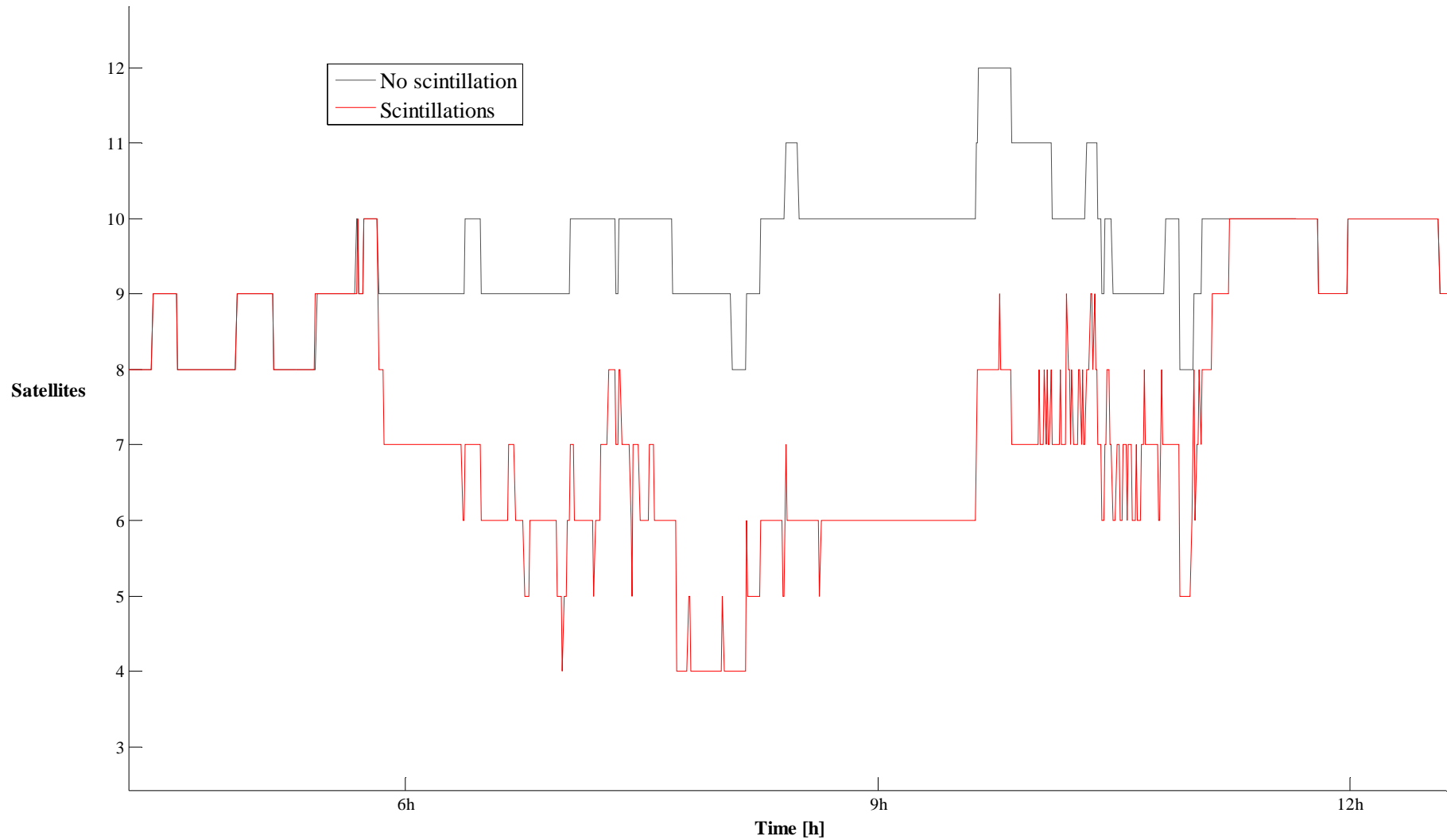


$$\sigma_{POS} = \underline{DOP} \times \sigma_P$$

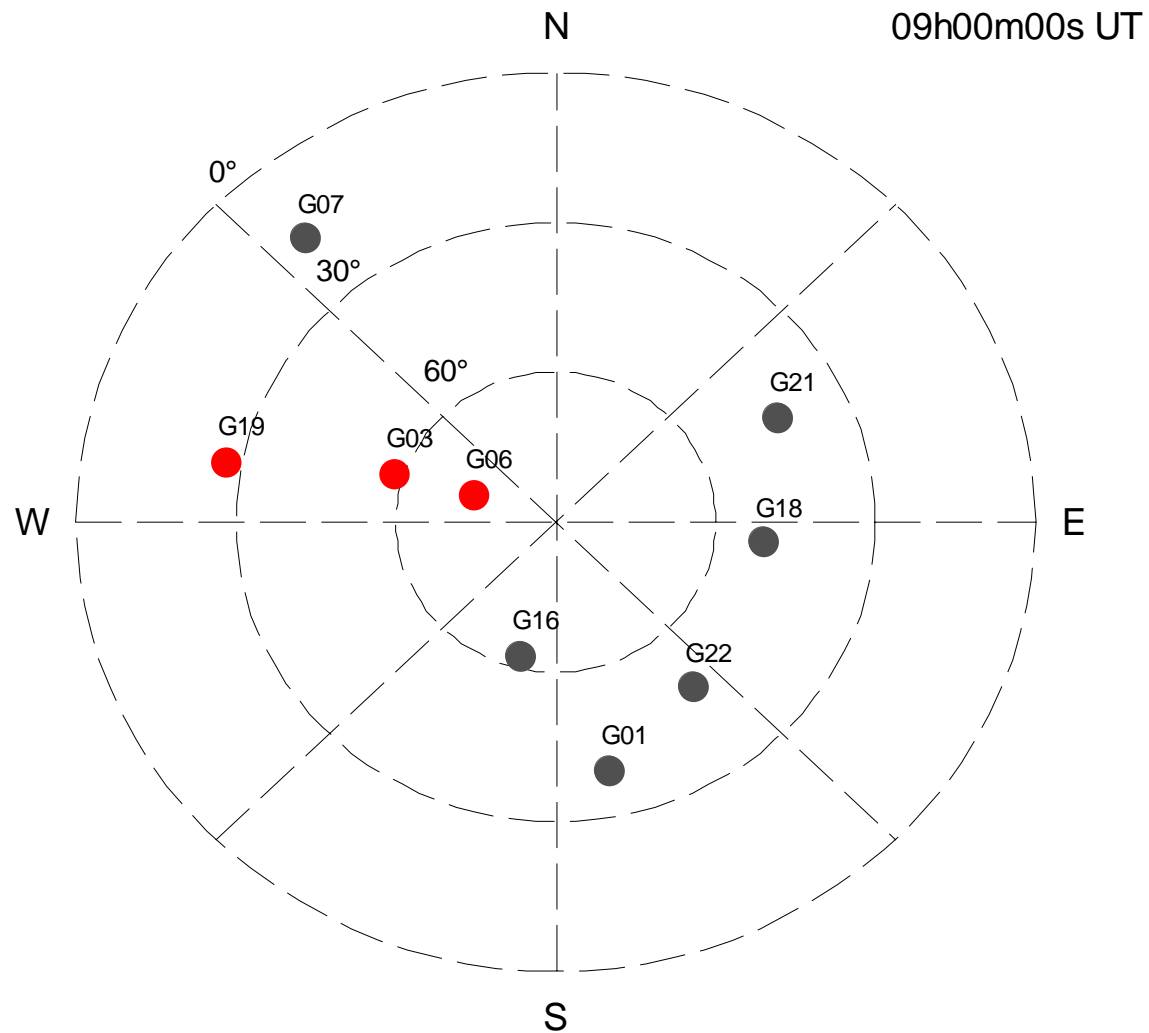
# Ionospheric scintillations reduce the number of available satellites



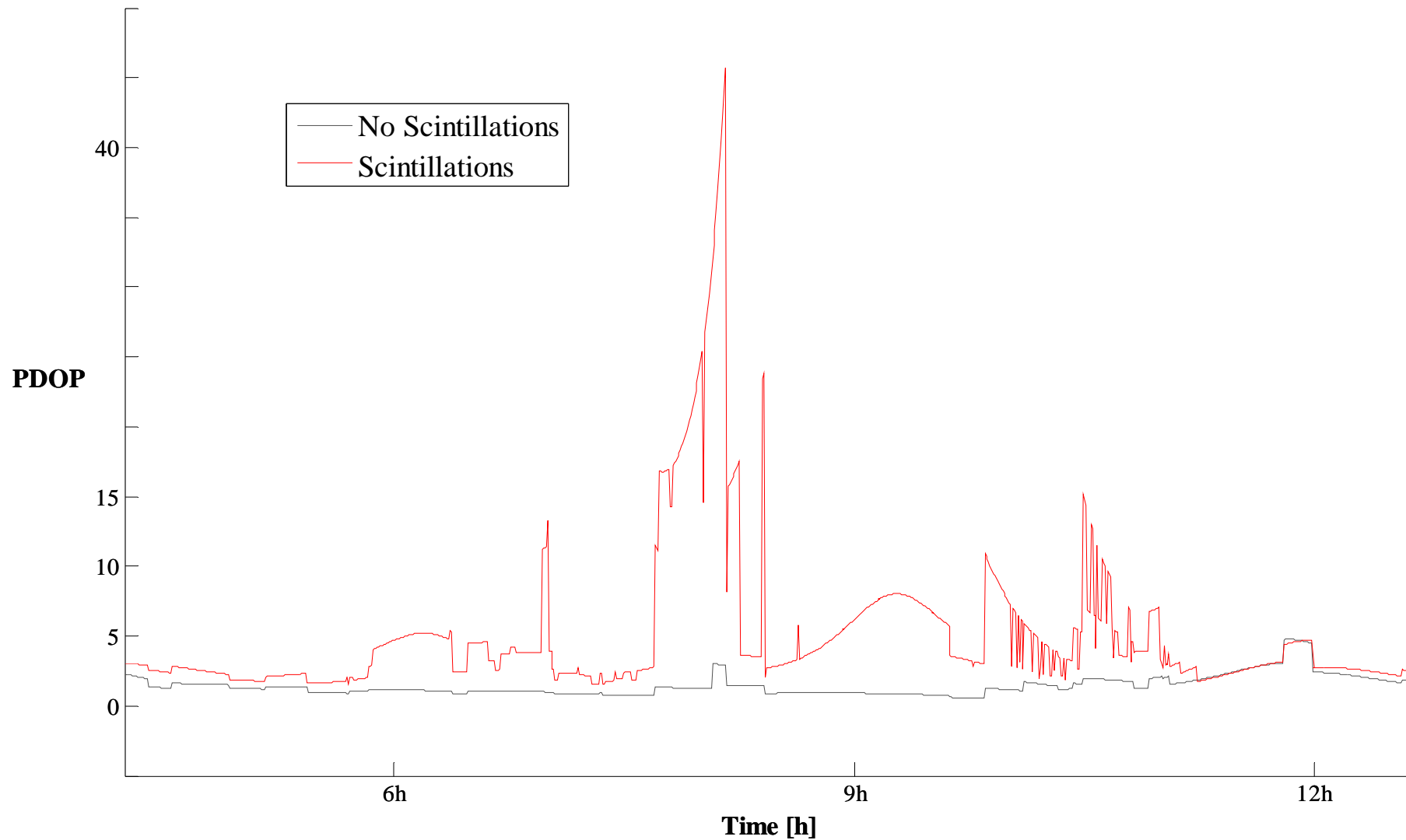
# Ionospheric scintillations reduce the number of available satellites



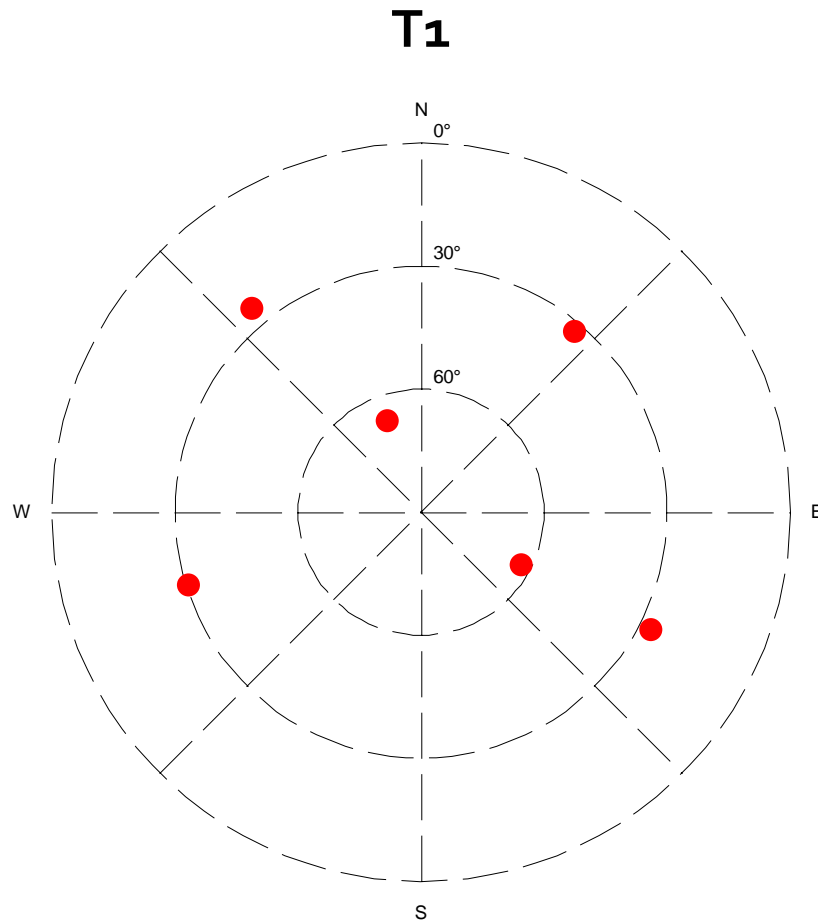
# Ionospheric scintillations reduce the number of available satellites



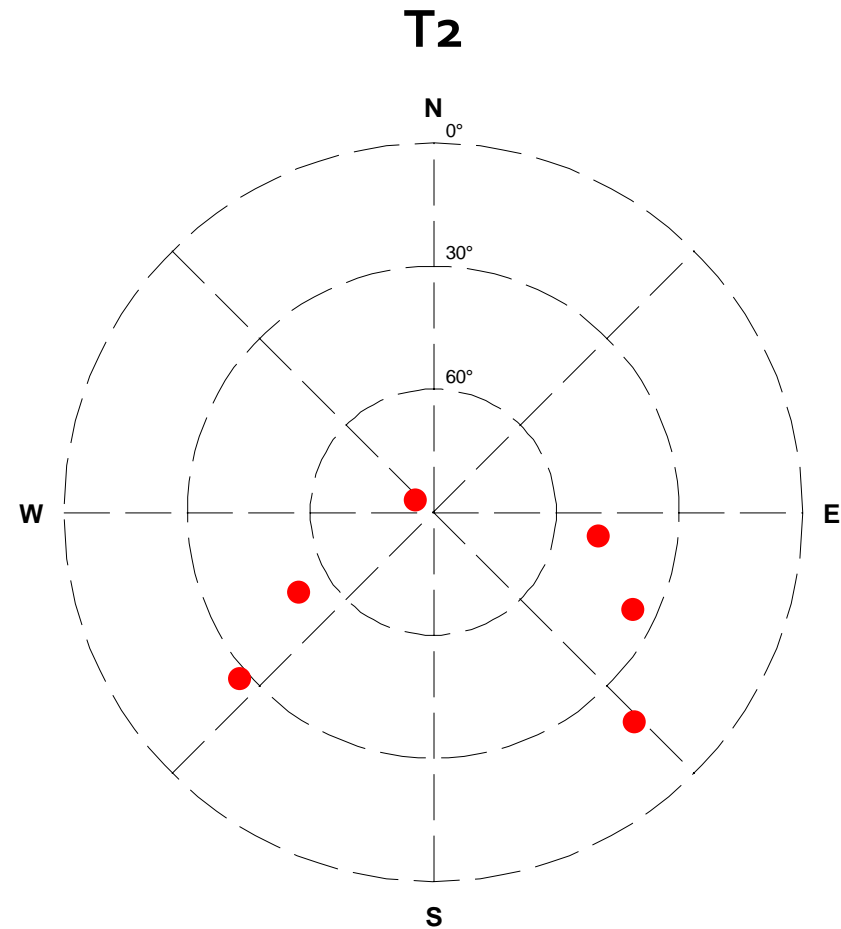
# Ionospheric scintillations reduce the satellite geometry quality



The high DOP values are not only involved by the low number of satellites

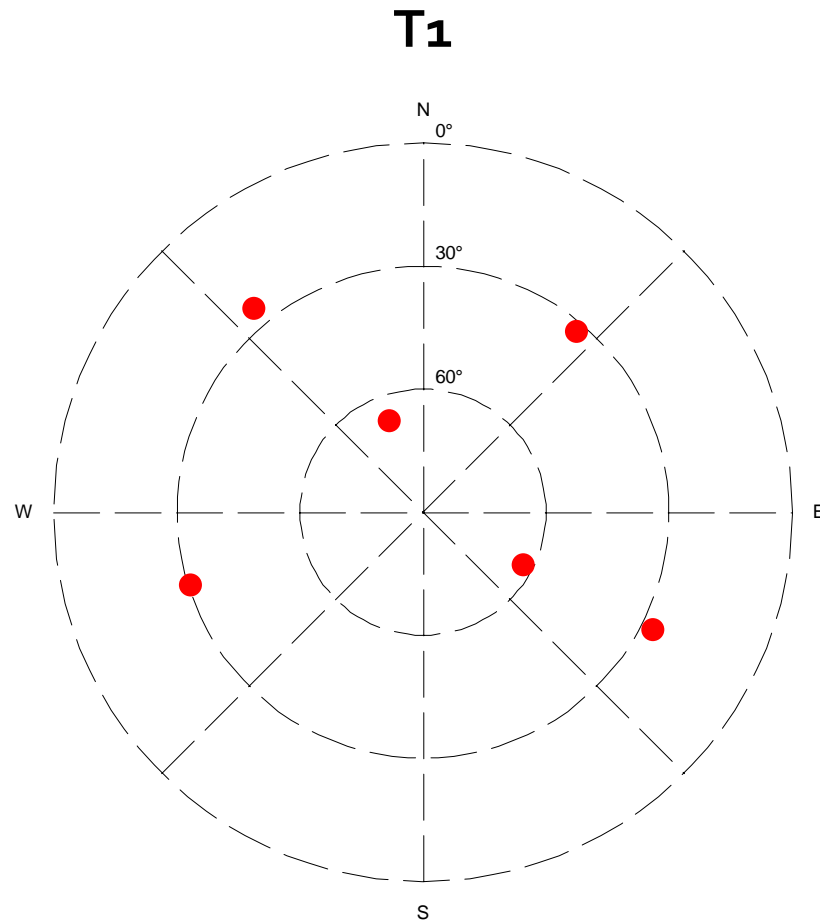


**DOP = 2.36**

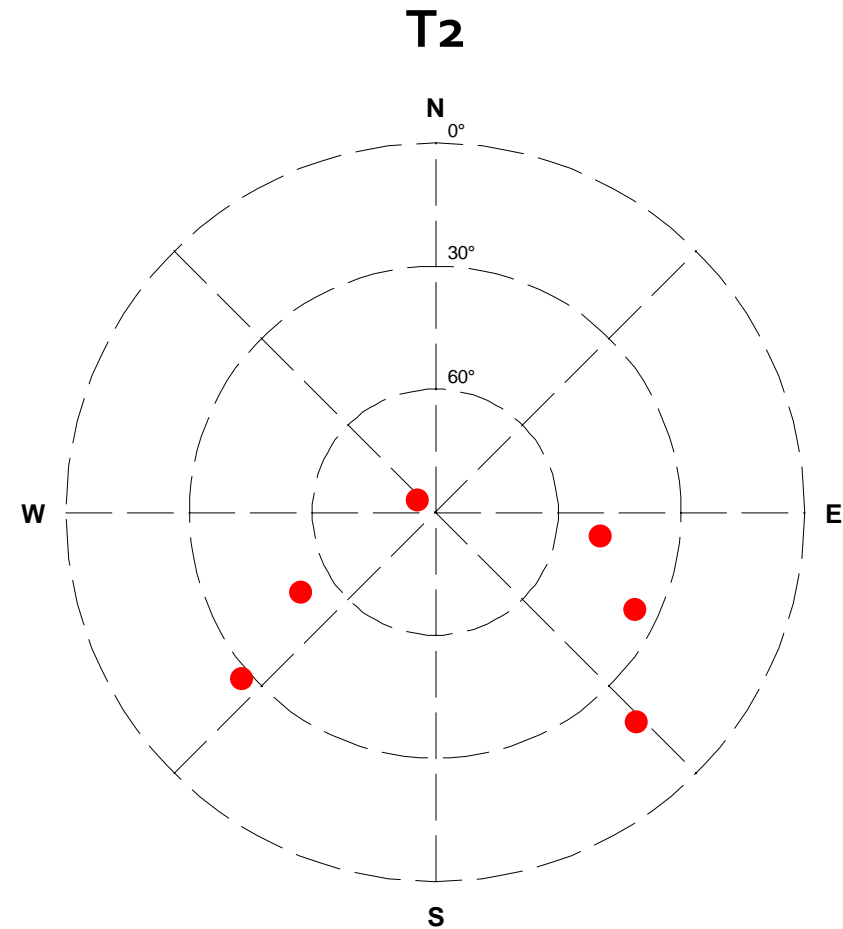


**DOP = 13.78**

The high DOP values are not only involved by the low number of satellites



$$|N| = 3.47$$



$$|N| = 0.04$$

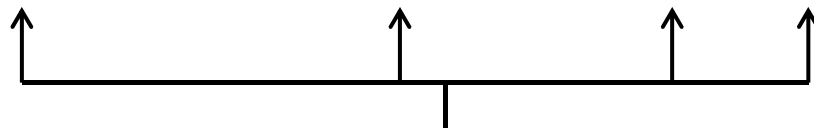


# A conical satellite geometry involves infinite DOP values

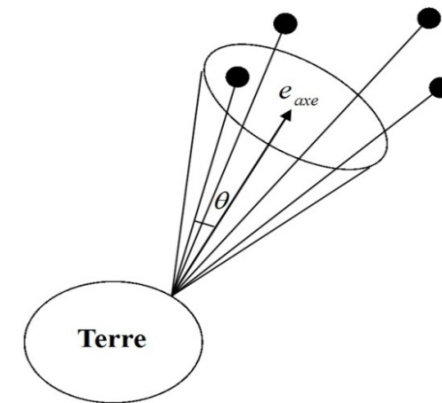
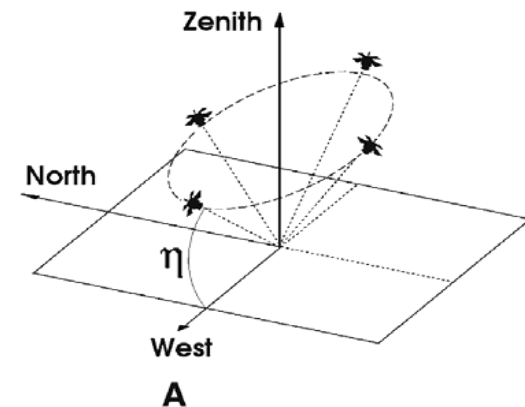
$$|N| = 0$$

$$Q_{\hat{x}} = N^{-1} = (A^T A)^{-1}$$

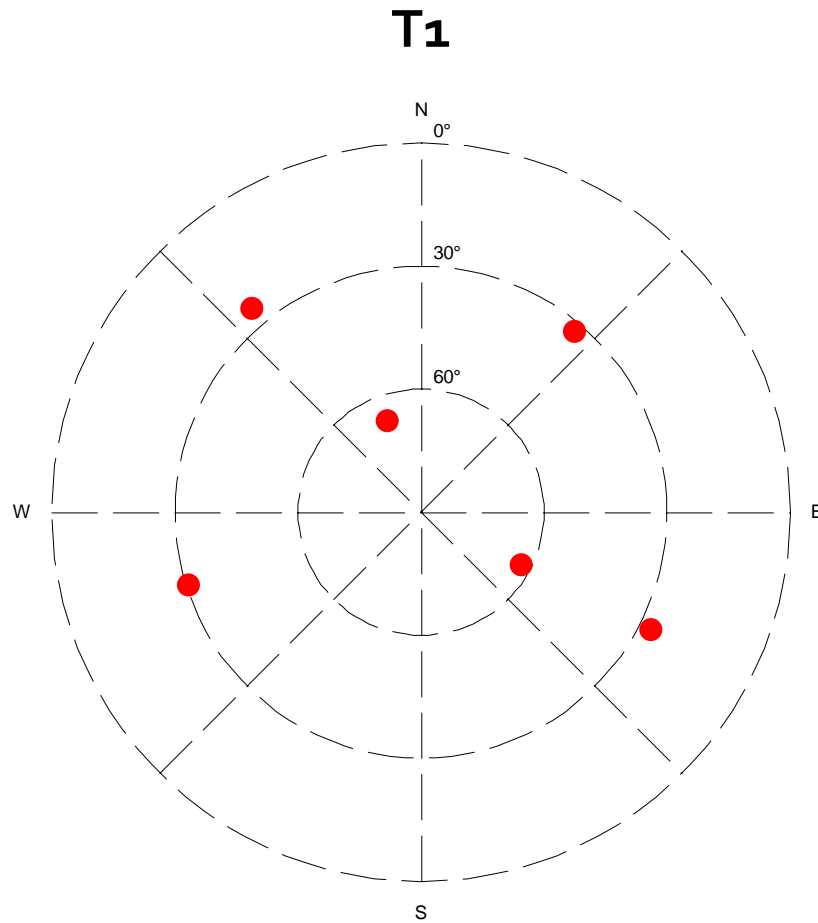
$$A = \begin{bmatrix} -\cos\eta^1 \sin\chi^1 & -\cos\eta^1 \cos\chi^1 & -\sin\eta^1 & 1 \\ -\cos\eta^2 \sin\chi^2 & -\cos\eta^2 \cos\chi^2 & -\sin\eta^2 & 1 \\ \dots & \dots & \dots & \dots \\ -\cos\eta^n \sin\chi^n & -\cos\eta^n \cos\chi^n & -\sin\eta^n & 1 \end{bmatrix}$$



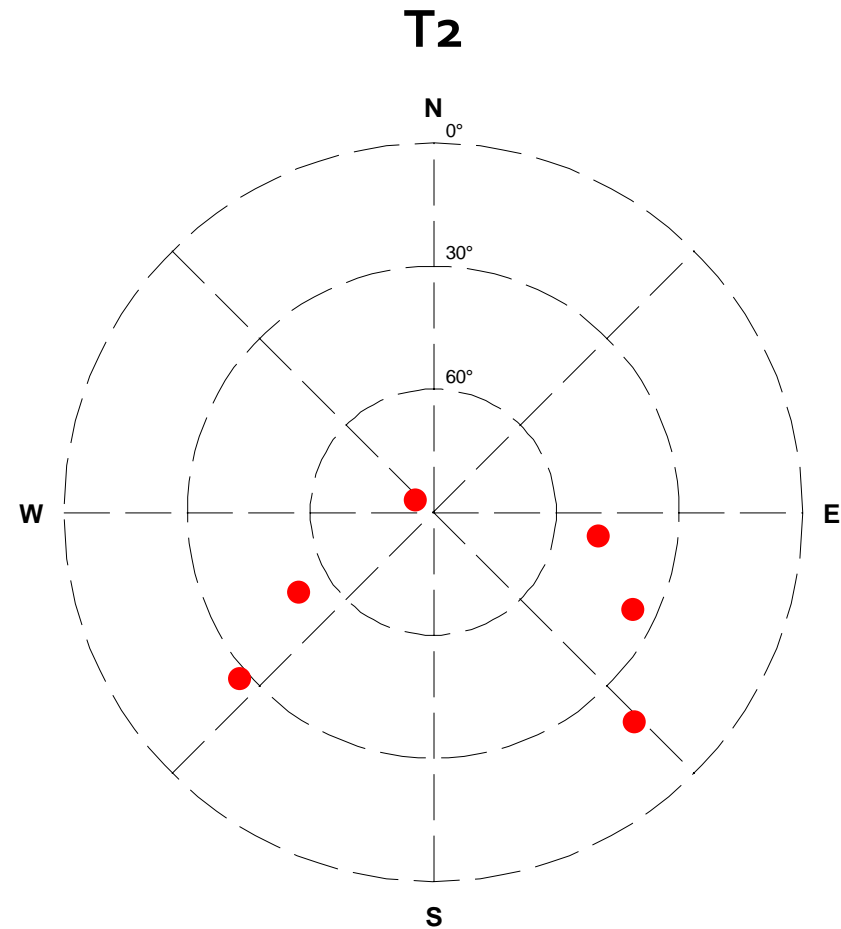
Any linear dependence?



The high DOP values are not only involved by the low number of satellites

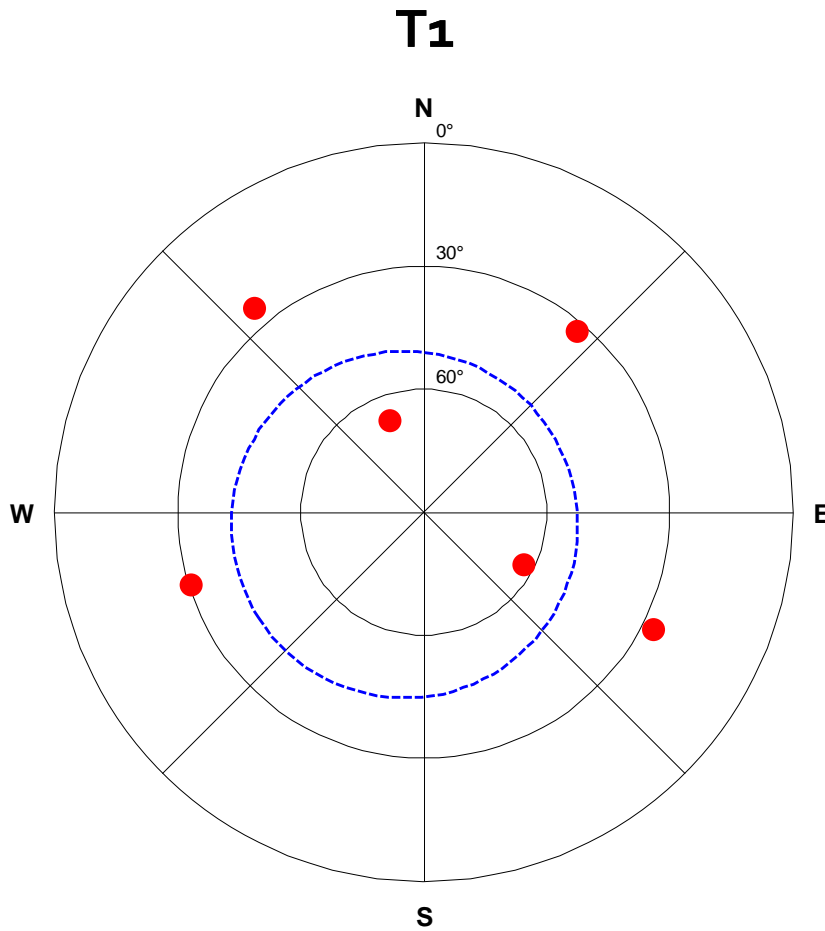


**DOP = 2.36**

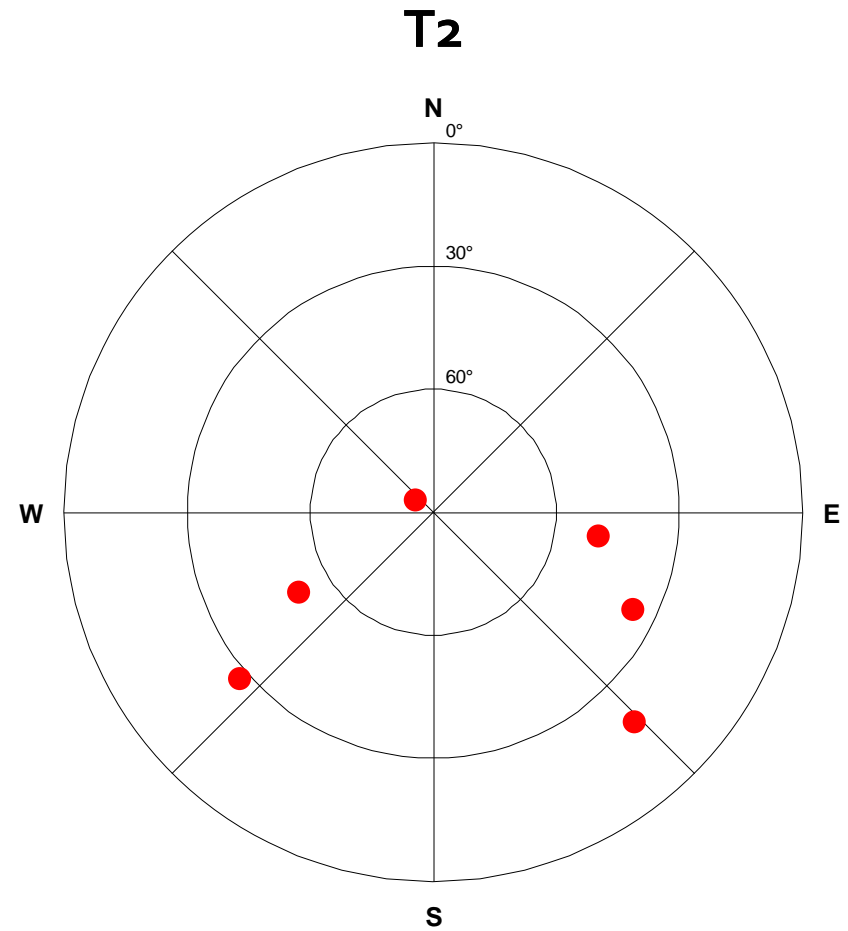


**DOP = 13.78**

The high DOP values are not only involved by the low number of satellites

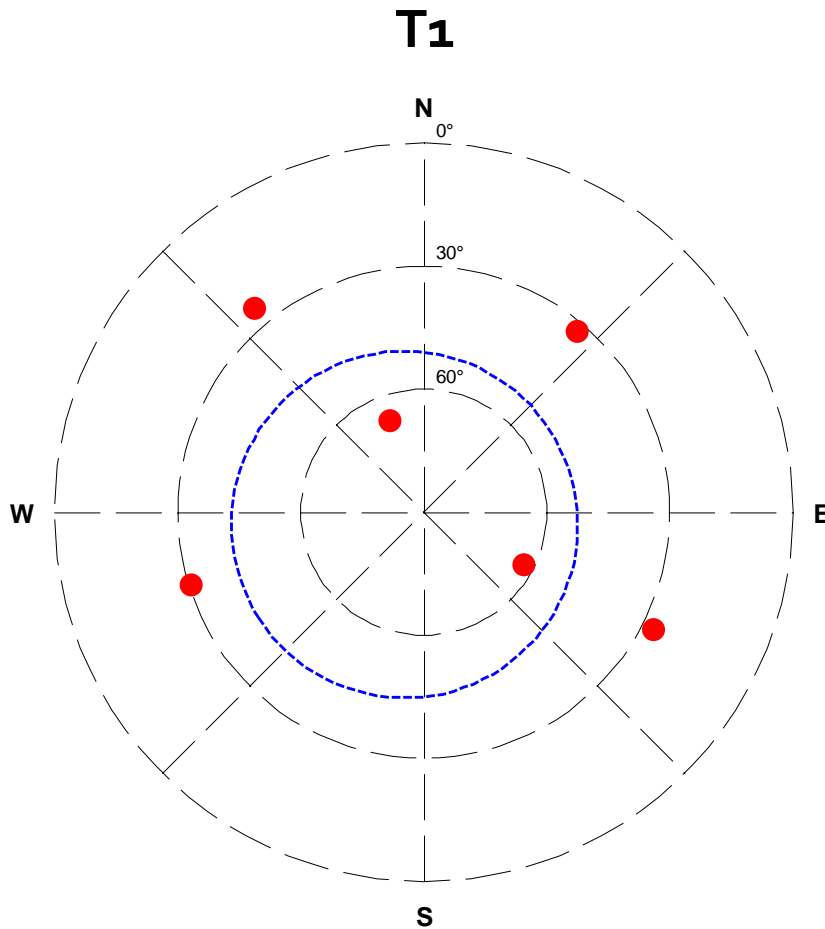


**DOP = 2.36**

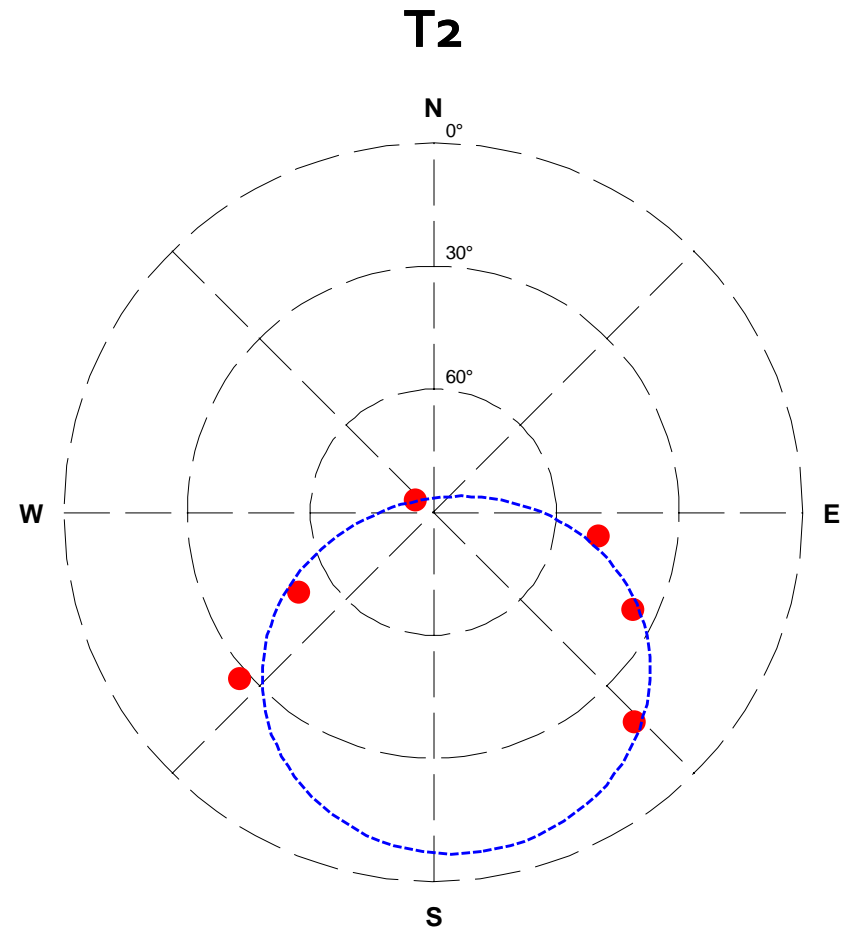


**DOP = 13.78**

The high DOP values are not only involved by the low number of satellites

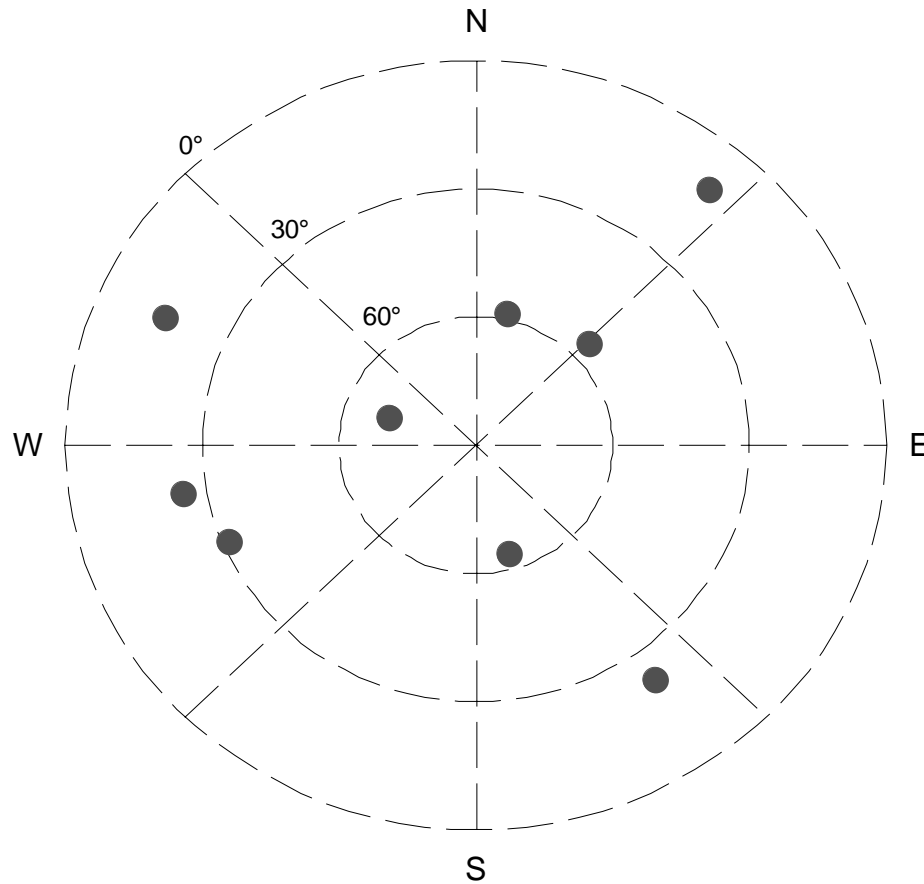


**DOP = 2.36**

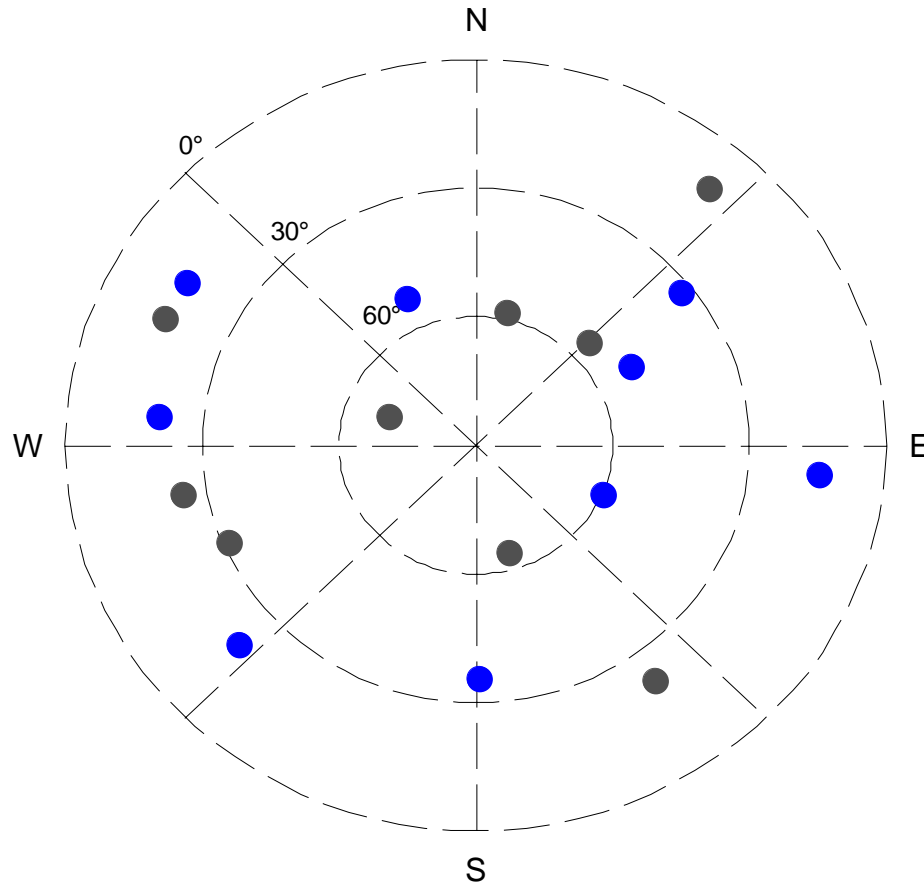


**DOP = 13.78**

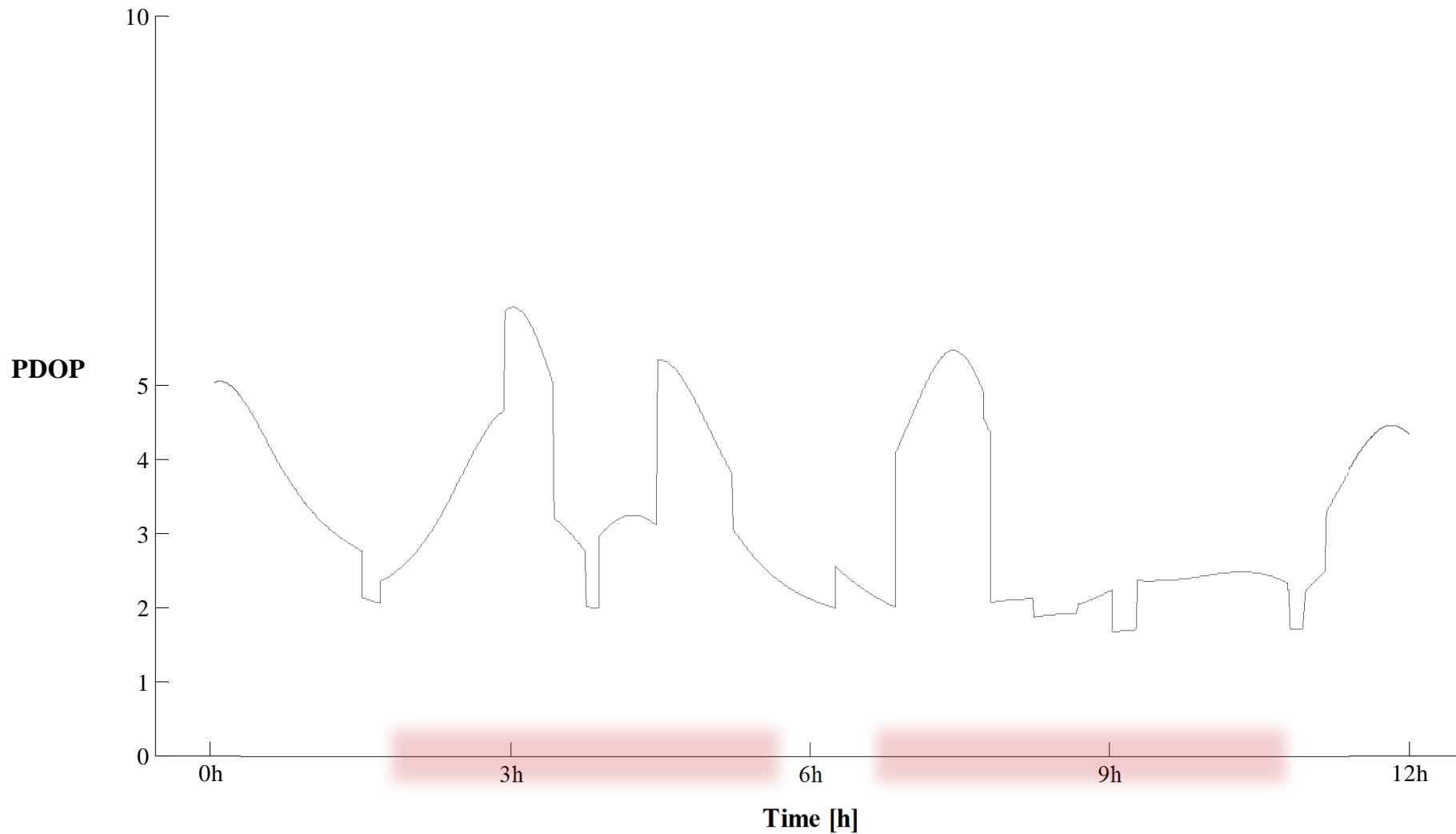
The combined use of GPS and Galileo strongly improves the satellite geometry



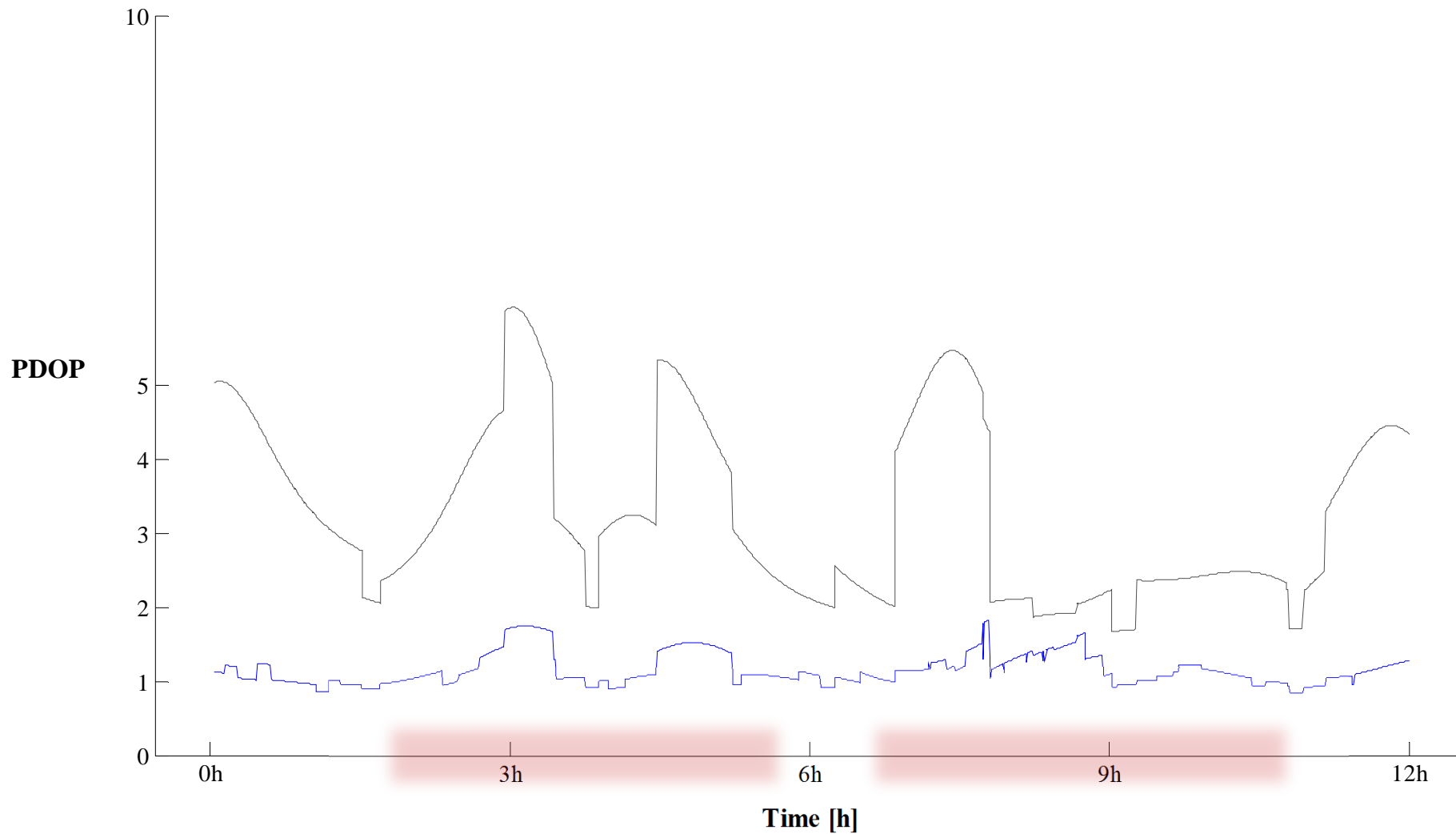
The combined use of GPS and Galileo strongly improves the satellite geometry



The combined use of GPS and Galileo strongly improves the satellite geometry



The combined use of GPS and Galileo strongly improves the satellite geometry





# Project - WP2 Geometry - Objectives

Quantify the improvement of PPP's performances involved by the expanded GPS-Galileo satellite geometry

- Precision
- Time convergence
- Reliability



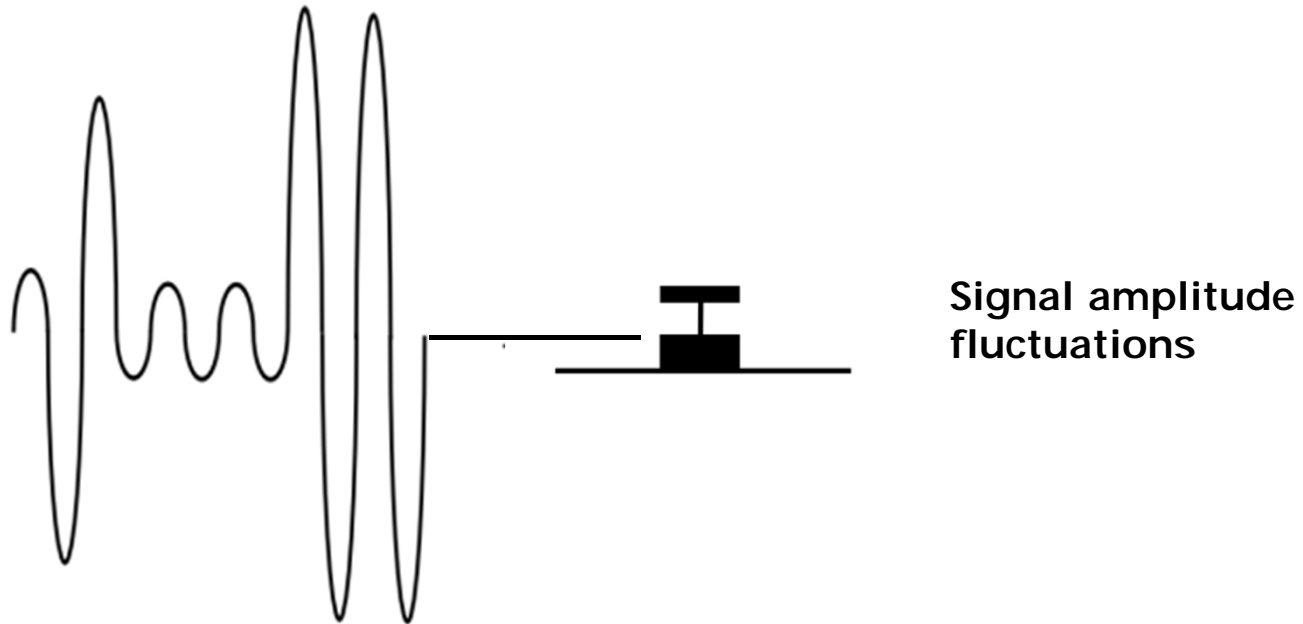
**Ionospheric  
Scintillations**

Project

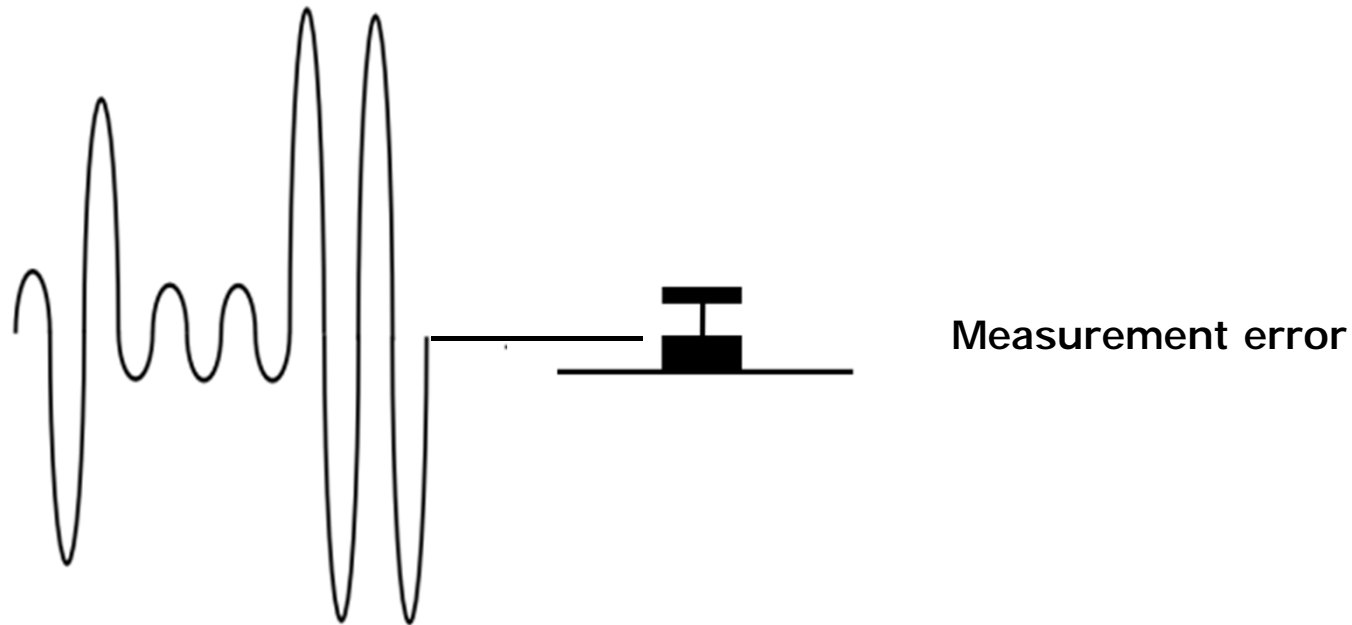
Geometry

**Stochasticity**

# Ionospheric Scintillations degrade satellite signal quality



# Ionospheric Scintillations degrade receiver measurement precision



$$\sigma_{POS} = DOP \times \sigma_P$$

The PPP stochastic model considers receiver measures to be independent

$$\Sigma = \begin{pmatrix} \sigma_1^2 & \sigma_{12} & \dots & \sigma_{1n} \\ \sigma_{21} & \sigma_2^2 & \dots & \sigma_{2n} \\ \dots & \dots & \dots & \dots \\ \sigma_{n1} & \sigma_{n2} & \dots & \sigma_n^2 \end{pmatrix}$$

The PPP stochastic model considers receiver measures to be independent

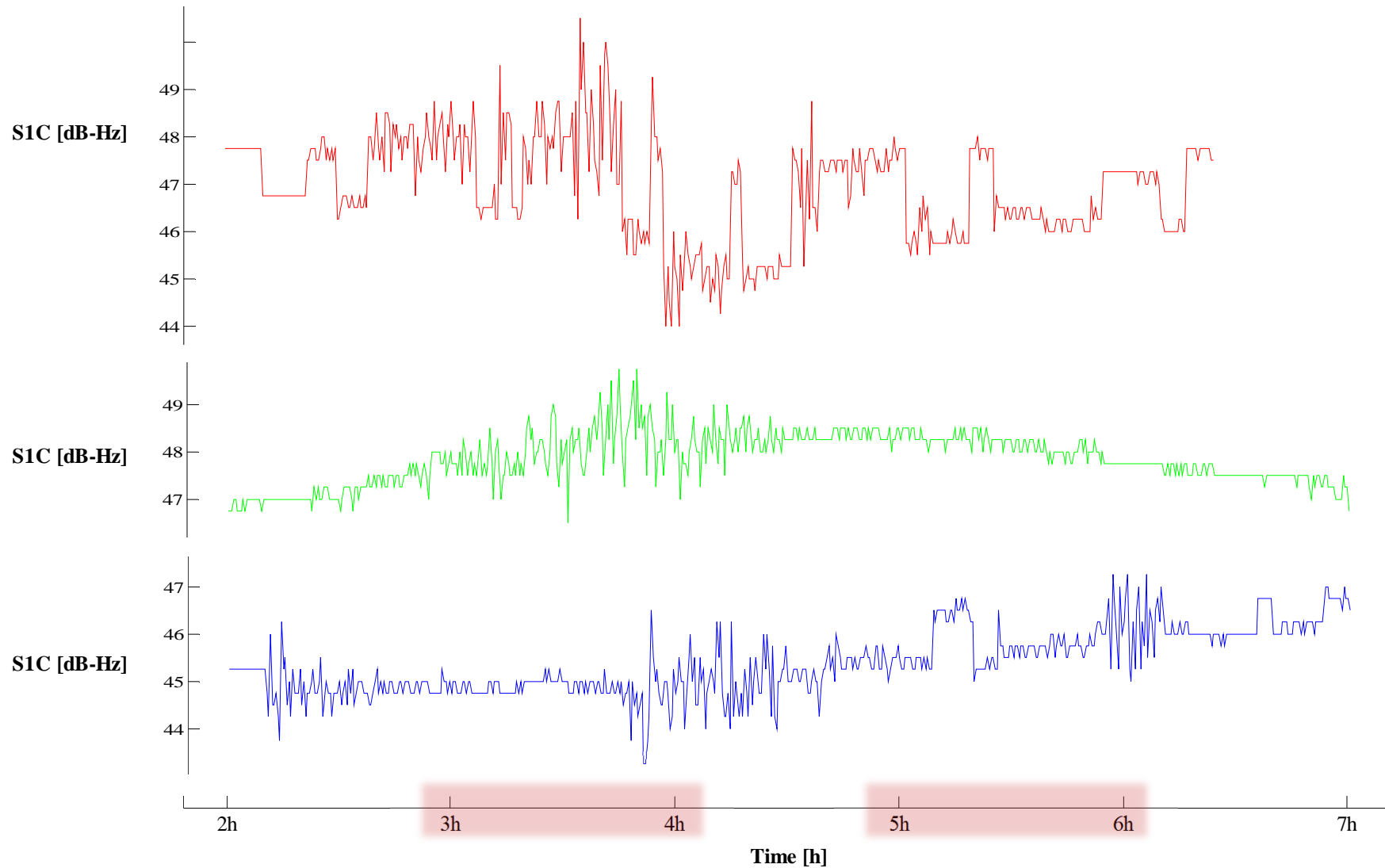
$$\Sigma = \begin{pmatrix} \sigma_1^2 & 0 & \dots & 0 \\ 0 & \sigma_2^2 & \dots & 0 \\ \dots & \dots & \dots & \dots \\ 0 & 0 & \dots & \sigma_n^2 \end{pmatrix}$$

First law of Geography...

*“Everything is related to everything else,  
but near things are more related than  
distant things.”*

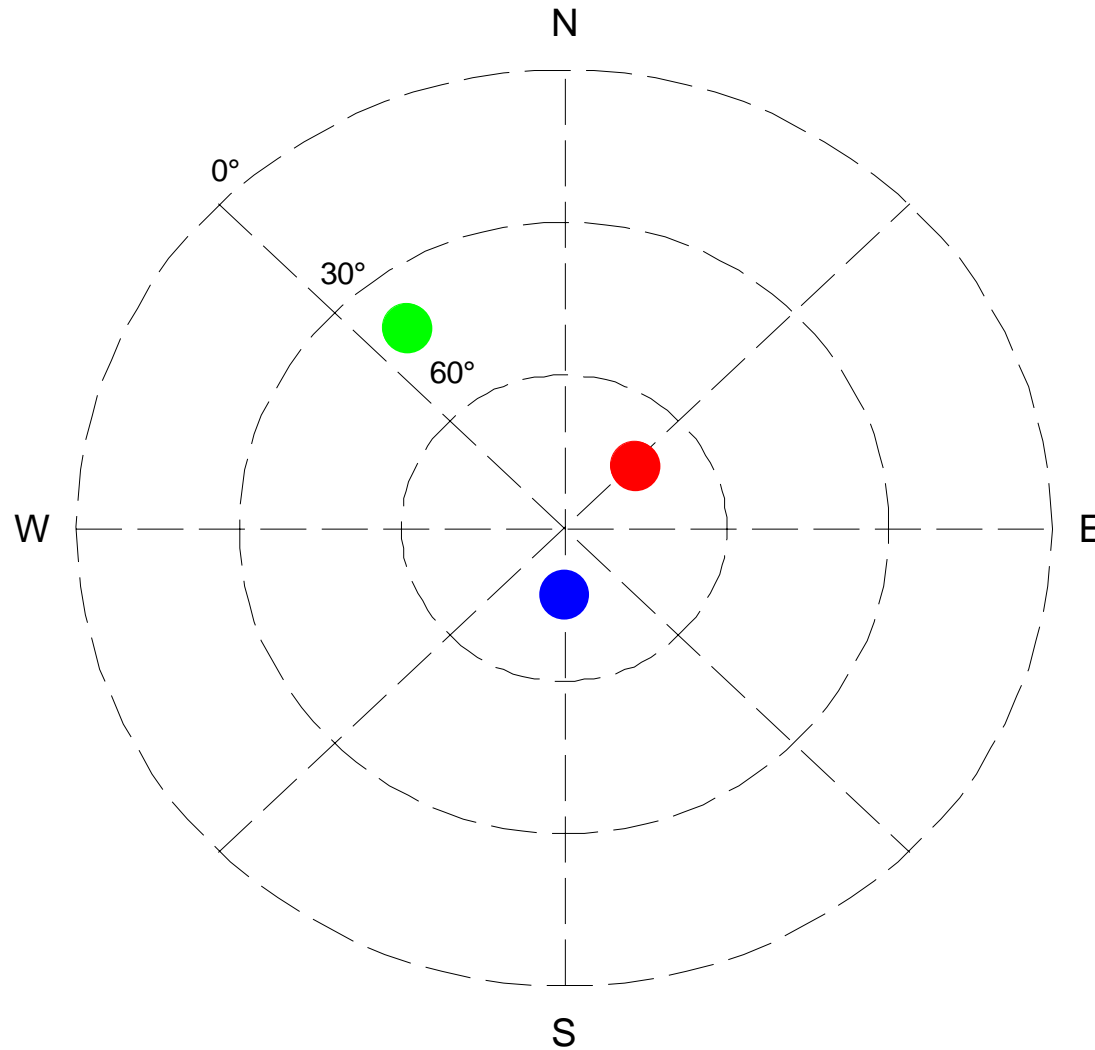
Waldo Tobler

# Satellite signals are affected differently in case of scintillations

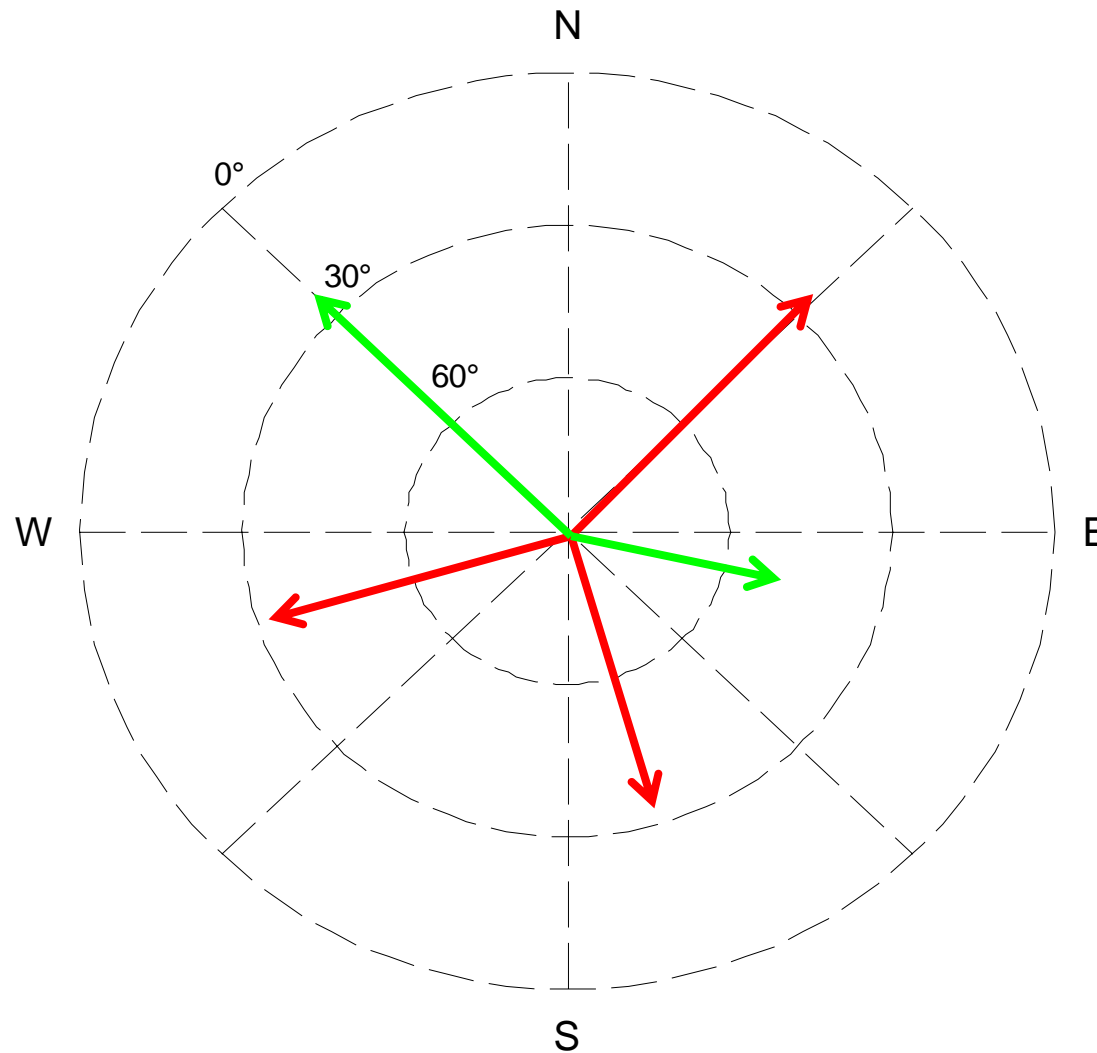




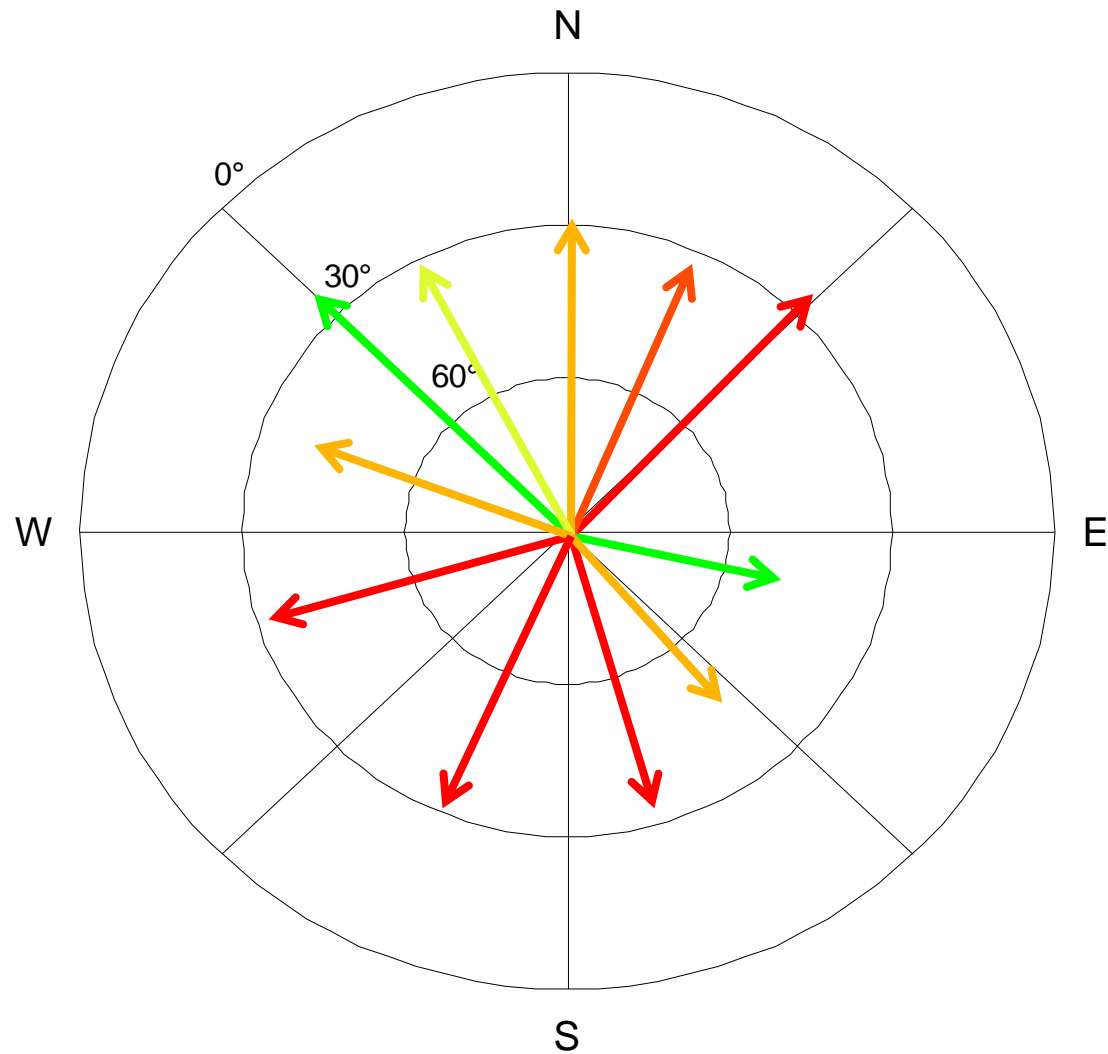
# Satellite signals are affected differently in case of scintillations



Spatial Auto-Correlation (SAC) can be used to generate a new PPP stochastic model



Spatial Auto-Correlation (SAC) can be used to generate a new PPP stochastic model

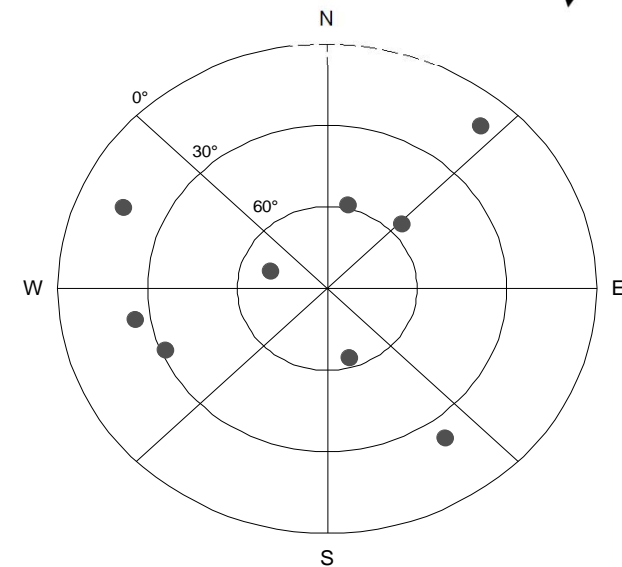
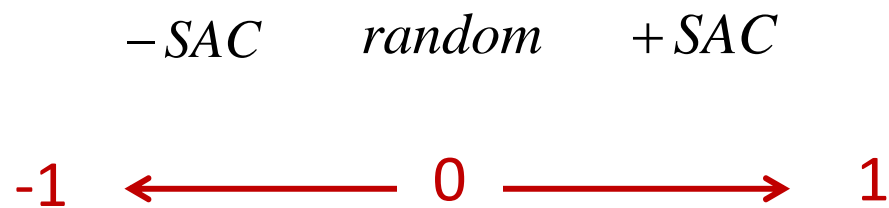
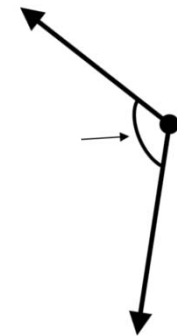


Spatial Auto-Correlation index are computed on satellite geometry

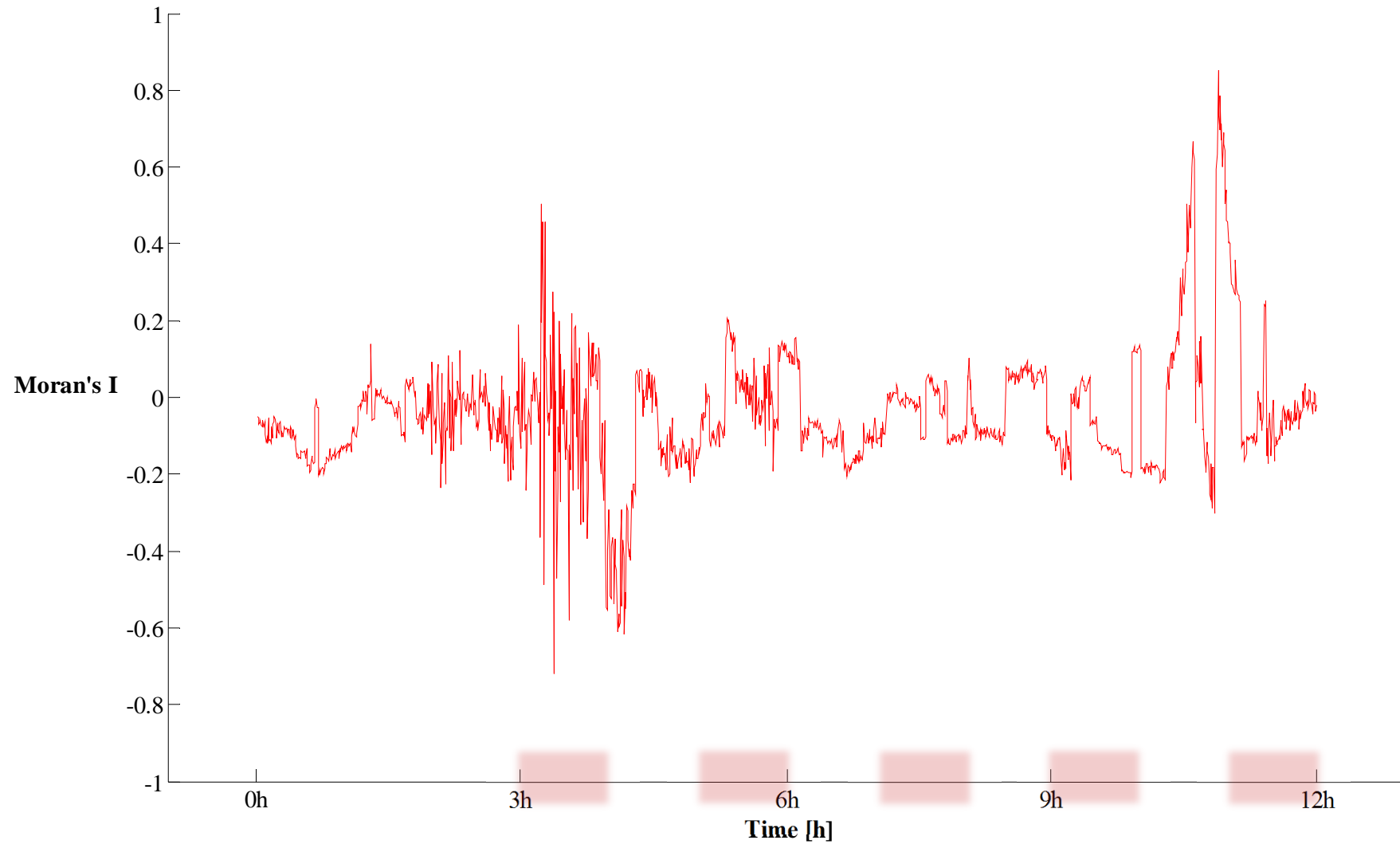
$$I = \frac{N}{\sum_i \sum_j w_{ij}} \frac{\sum_i \sum_j w_{ij} (v_i - \bar{v})(v_j - \bar{v})}{\sum_i (v_i - \bar{v})^2}$$

$$v_i = S1C_i$$

$$w_{ij} = \frac{1}{d_{ij}}$$



# Spatial Auto-Correlation is fluctuating



# Spatial Auto-Correlation research will be expanded

## Perspectives

- Other SAC indices (Geary'C, ...)
- Realistic simulations
- Tracking error vs. Power signal
- ...

Project

Geometry

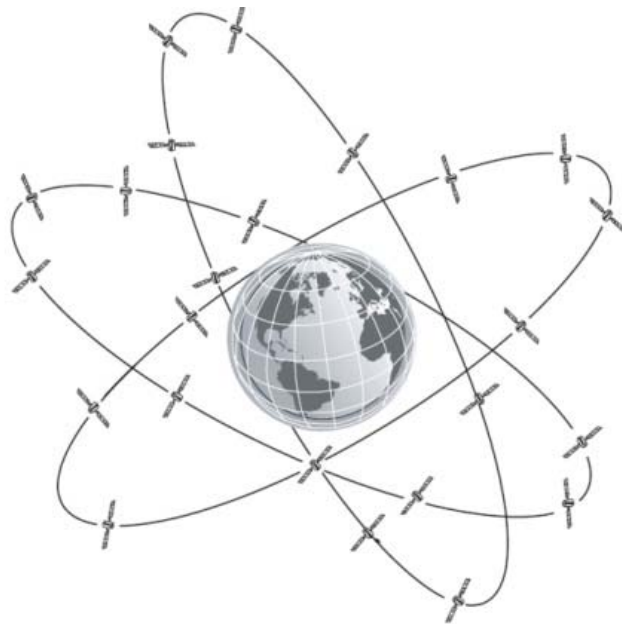
Stochasticity





# Precise Point Positioning

## Performances under Ionospheric Scintillations



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