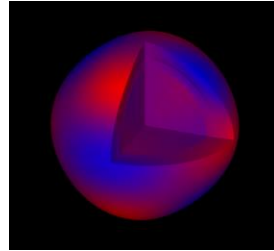


# The Impact of Asteroseismology across Stellar Astrophysics

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## The Empirical Mass Distribution of Hot B Subdwarfs derived by asteroseismology and other means

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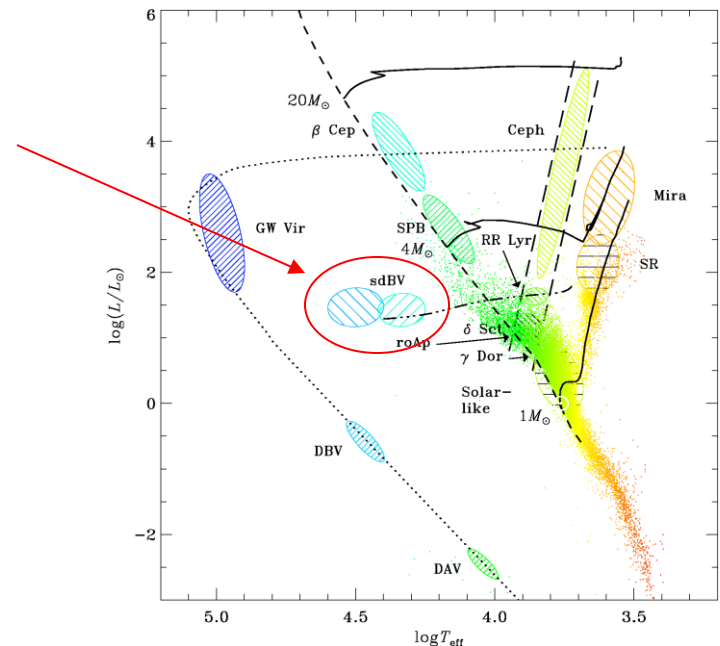
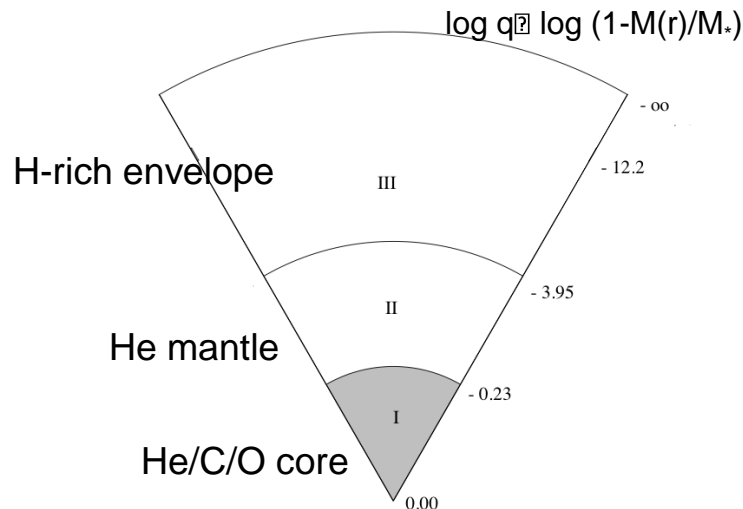
# 1. Introduction to sdB stars

Hot ( $T_{\text{eff}} = 20\,000 - 40\,000\text{ K}$ ) and compact ( $\log g = 5.2 - 6.2$ ) stars belonging to Extreme Horizontal Branch (EHB)

- convective He-burning core (I), radiative He mantle (II) and very thin H-rich envelope (III)
- lifetime of  $\sim 10^8\text{ yr}$  (100 Myr) on EHB, then evolve as low-mass white dwarfs
- At least 50% of sdB stars reside in binary systems, generally in close orbit ( $P_{\text{orb}} \leq 10\text{ days}$ )

## Two classes of multi-periodic sdB pulsators:

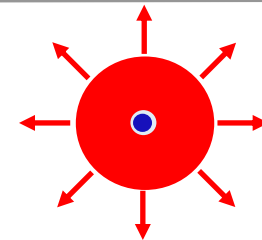
- > short-periods ( $P \sim 80 - 600\text{ s}$ ),  $A \leq 1\%$ , p-modes (envelope)
- > long-periods ( $P \sim 45\text{ min} - 2\text{ h}$ ),  $A \leq 0.1\%$ , g-modes (core). **Space observations required !**



## 2. Single and binary formation scenarios

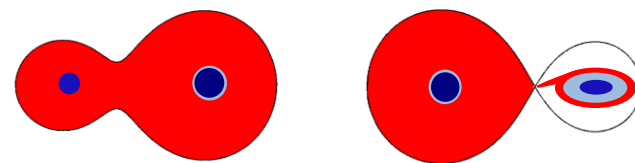
- Single star evolution (enhanced mass loss at tip of RGB)

Mass range in  $0.40 - 0.43 \leq M_*/M_s \leq 0.52$  (Dorman et al. 1993)

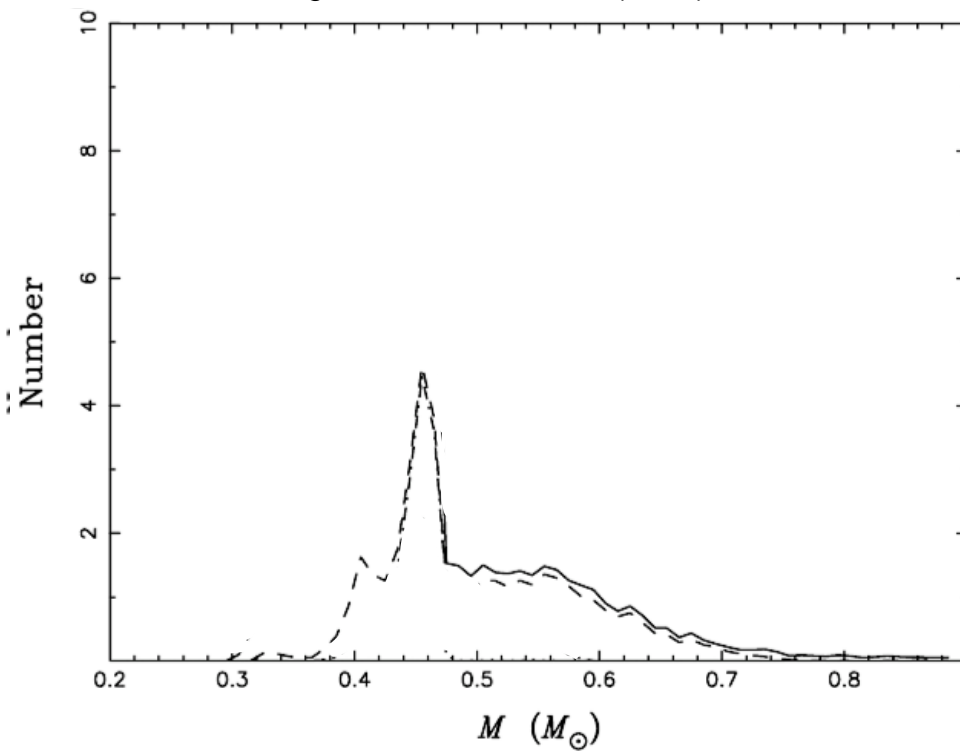


- Binary star evolution (Han et al. 2002, 2003)

Common envelope ejection (CE), stable mass transfer by Roche lobe overflow (RLOF), and He-white dwarf mergers



Figures from Han et al. (2003)



Weighted mean distribution  
for binary evolution:  
(including selection effects)

$0.30 \leq M_*/M_s \leq 0.70$   
peak  $\sim 0.46 M_s$  (CE, RLOF)  
high masses (mergers)

### 3. Method for sdB asteroseismology

Search the star model(s) whose theoretical periods best fit all the observed ones, in order to minimize

$$S^2 = \sum \frac{1}{\sigma} (P_{\text{obs}} - P_{\text{th}})^2$$

- Static models including detailed envelope microscopic diffusion (nonuniform envelope Fe abundance)
- Efficient optimization codes (based on *Genetic Algorithms*) are used to find the minima of  $S^2$ , i.e. the potential asteroseismic solutions

> Example: PG 1336-018, pulsating sdB + dM eclipsing binary

✓ Light curve modeling (Vuckovic et al. 2007):

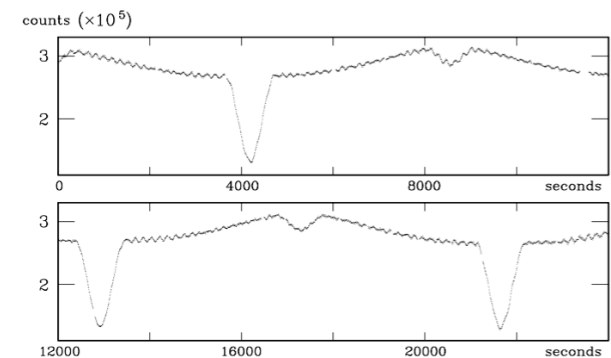
I.  $M_{\text{tot}} = 0.389 \pm 0.005 M_{\text{s}}$  et  $R = 0.14 \pm 0.01 R_{\text{s}}$

II.  $M_{\text{tot}} = 0.466 \pm 0.006 M_{\text{s}}$  et  $R = 0.15 \pm 0.01 R_{\text{s}}$

III.  $M_{\text{tot}} = 0.530 \pm 0.007 M_{\text{s}}$  et  $R = 0.15 \pm 0.01 R_{\text{s}}$

✓ Seismic analysis (Charpinet et al. 2008):

$M_{\text{tot}} = 0.459 \pm 0.005 M_{\text{s}}$  et  $R = 0.151 \pm 0.001 R_{\text{s}}$



⇒ Our asteroseismic method is sound and free of significant systematic effects

## 4. Available samples (of sdBs with known masses)

### I. The asteroseismic sample

Name	$\log g$ (cm s <sup>-2</sup> )	$T_{\text{eff}}$ (K)	$M$ ( $M_{\odot}$ )	$\log M_{\text{env}}/M$	References
PG 0014+067	5.780±0.008	33550±380	0.490±0.019	-4.31±0.22	Brassard et al. (2001)
	5.775±0.009	34130±370	0.477±0.024	-4.32±0.23	Charpinet et al. (2005a)
	5.772	34130±370	0.478	-4.13	Brassard & Fontaine (2008)
PG 1047+003	5.800±0.006	33150±200	0.490±0.014	-3.72±0.11	Charpinet et al. (2003)
PG 1219+534	5.807±0.006	33600±370	0.457±0.012	-4.25±0.15	Charpinet et al. (2005b)
Feige 48	5.437±0.006	29580±370	0.460±0.008	-2.97±0.09	Charpinet et al. (2005c)
	5.462±0.006	29580±370	0.519±0.009	-2.52±0.06	Van Grootel et al. (2008a)
EC 05217-3914	5.730	32000	0.490	-3.00	Billères & Fontaine (2005)
PG 1325+101	5.811±0.004	35050±220	0.499±0.011	-4.18±0.10	Charpinet et al. (2006a)
PG 0048+092	5.711±0.010	33300±1700	0.447±0.027	-4.92±0.20	Charpinet et al. (2006b)
EC 20117-4014	5.856±0.008	34800±2000	0.540±0.040	-4.17±0.08	Randall et al. (2006b)
PG 0911+456	5.777±0.002	31940±220	0.390±0.010	-4.69±0.07	Randall et al. (2007)
BAL 090100001	5.383±0.004	28000±1200	0.432±0.015	-4.89±0.14	Van Grootel et al. (2008b)
PG 1336-018	5.739±0.002	32780±200	0.459±0.005	-4.54±0.07	Charpinet et al. (2008)
PG 1605+072	5.248	32300±300	0.707	-5.78	van Spaandonk et al. (2008)
	5.217	32300±300	0.561	-6.22	
	5.226±0.004	32300±300	0.528±0.002	-5.88±0.04	Van Grootel (2008)
	5.276	32630±600	0.731	-2.83	Van Grootel et al. (2010a)
	5.278	32630±600	0.769	-2.71	
EC 09582-1137	5.788±0.004	34805±230	0.485±0.011	-4.39±0.10	Randall et al. (2009)
KPD 1943+4058	5.520±0.030	27730±270	0.496±0.002	-2.55±0.07	Van Grootel et al. (2010b)
KPD 0629-0016	5.450±0.034	26485±195	0.471±0.002	-2.42±0.07	Van Grootel et al. (2010c)
KIC02697388	5.489±0.033	25395±225	0.463±0.009	-2.30±0.05	Charpinet et al. (2011)
	5.499±0.049	25395±225	0.452±0.012	-2.35±0.05	

### 15 sdB stars modeled by asteroseismology

(we took the most recent value in case of several analyses)

## 4. Available samples

### II. The extended sample (sdB + WD or dM star)

Name	$\log g$ (cm s <sup>-2</sup> )	$T_{\text{eff}}$ (K)	$M_1$ ( $M_{\odot}$ )	Nature	Eclipses	References
KPD 0422+5421	5.565±0.009	25000±1500	0.511±0.049	sdB+WD	yes	Orosz & Wade (1999)
PG 1241-084	5.63±0.03	28490±210	0.48±0.09	sdB+dM	yes	Wood & Saffer (1999)
	5.60±0.12	28490±210	0.485±0.013			Lee et al. (2009)
HS 0705+6700	5.40±0.10	28800±900	0.48	sdB+dM	yes	Drechsel et al. (2001)
HS 2333+3927	5.70±0.10	36500±1000	0.38	sdB+dM	no	Heber et al. (2005)
NSVS 14256825	5.50±0.02	35000±5000	0.46	sdB+dM	yes	Wils et al. (2007)
PG 1336-018	5.74±0.05	31300±300	0.389±0.005	sdB+dM	yes	Vuckovic et al. (2007)
	5.77±0.06	31300±300	0.466±0.006			
	5.79±0.07	31300±300	0.530±0.007			
2M 1533+3759	5.57±0.07	29230±125	0.376±0.055	sdB+dM	yes	For et al. (2010)
2M 1938+4603	5.425±0.009	29565±105	0.48±0.03	sdB+dM	yes	Østensen et al. (2010)
KPD 1946+4340	5.452±0.006	34500±400	0.47±0.03	sdB+WD	yes	Bloemen et al. (2011)

Light curve modeling + spectroscopy  $\Rightarrow$  mass of the sdB component

Need uncertainties to build a mass distribution

$\Rightarrow$  5 sdB stars retained in this subsample

**Extended sample:** 15+5 = 20 sdB stars with accurate mass estimates

- 11 (apparently) single stars
- 9 in binaries (including 4 pulsators)

## 5. Mass distributions

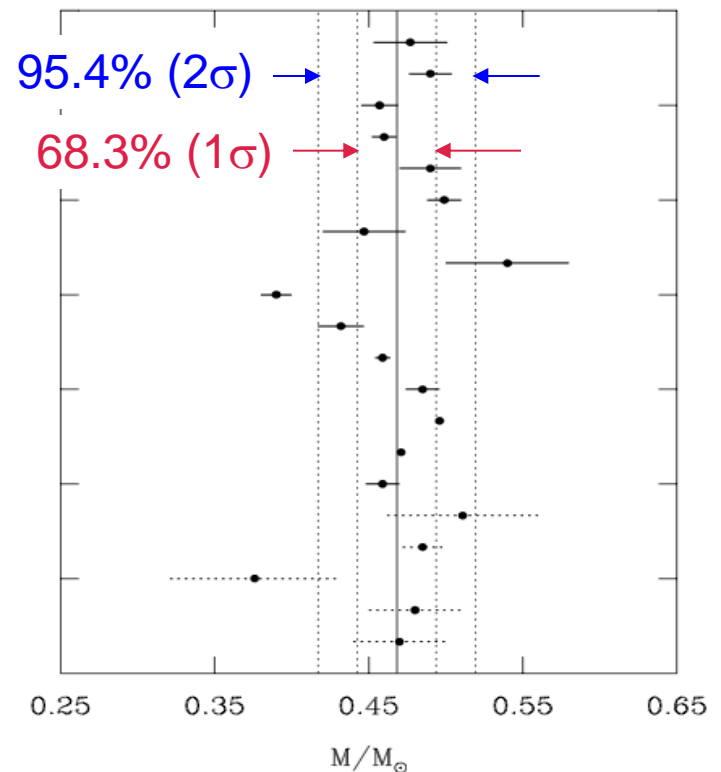
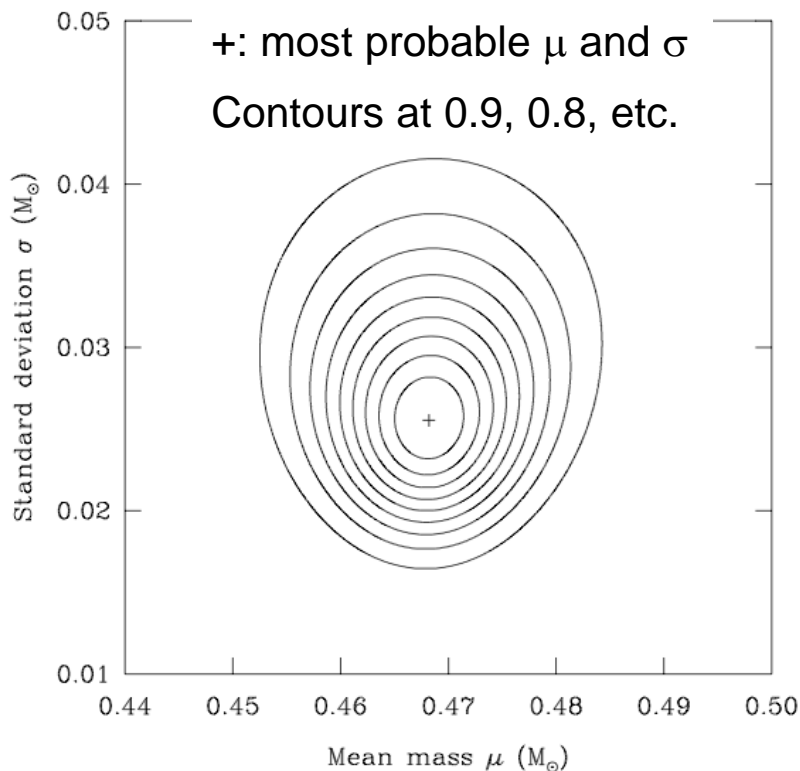
### I. Assumption of a normal distribution

$$L(\mu, \sigma) = \prod_{i=1}^N [2\pi(\sigma^2 + \sigma_i^2)]^{-1/2} \exp\left\{-\frac{(m_i - \mu)^2}{2(\sigma^2 + \sigma_i^2)}\right\}$$

$\mu$ : mean mass  
 $\sigma$ : standard deviation

Extended sample:  $\mu = 0.468 M_\odot$  and  $\sigma = 0.026 M_\odot$

Asteroseismic sample:  $\mu = 0.467 M_\odot$  and  $\sigma = 0.027 M_\odot$





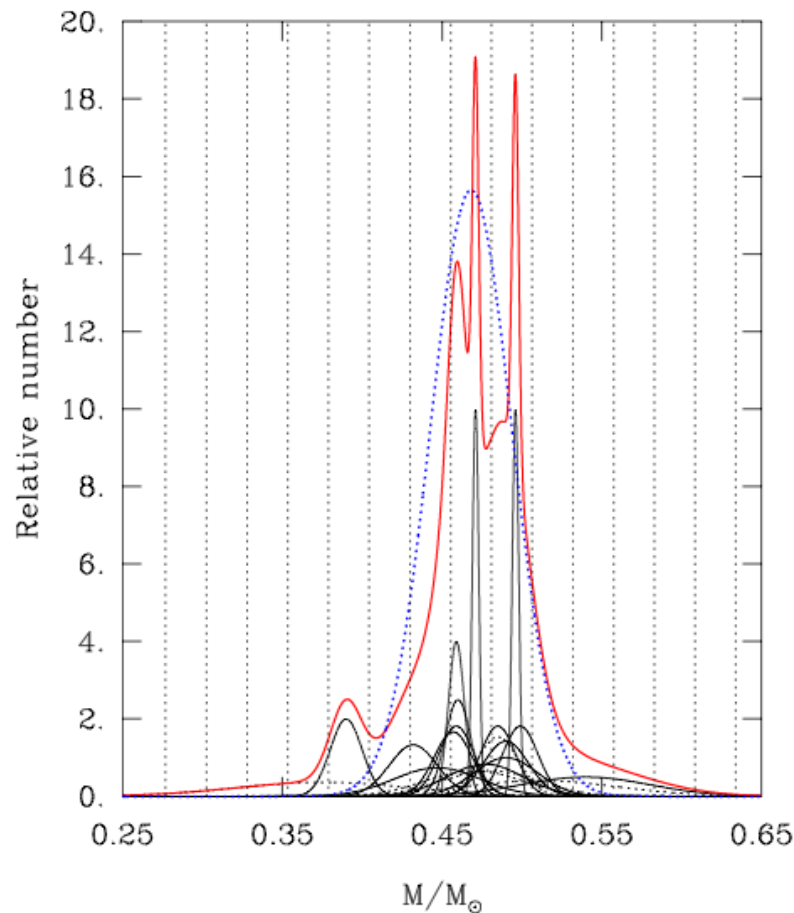
## 5. Mass distributions

### II. Model-free distribution

(only  $\sigma_i$ 's are assumed to obey normal distribution law)

**Red curve:** addition of all sdBs (mass with uncertainties) in extended sample

**Blue curve:** normal distribution ( $\mu = 0.468$  Ms and  $\sigma = 0.026$  Ms)





## 5. Mass distributions

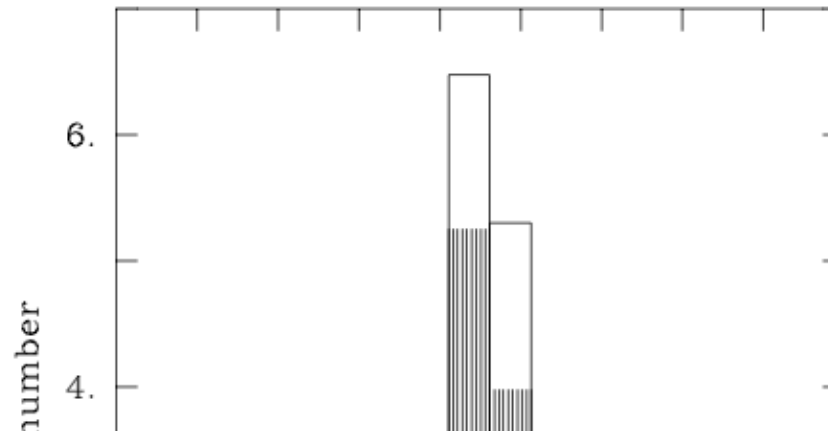
Binning the distribution in the form of an **histogram** (bin width =  $\sigma = 0.026 M_{\odot}$ )

Extended sample:  
(white)

Mean mass: 0.469  $M_{\odot}$

Median mass: 0.471  $M_{\odot}$

Range of 68.3% of stars:  
0.436-0.501  $M_{\odot}$



Asteroseismic sample:  
(shaded)

Mean mass: 0.470  $M_{\odot}$

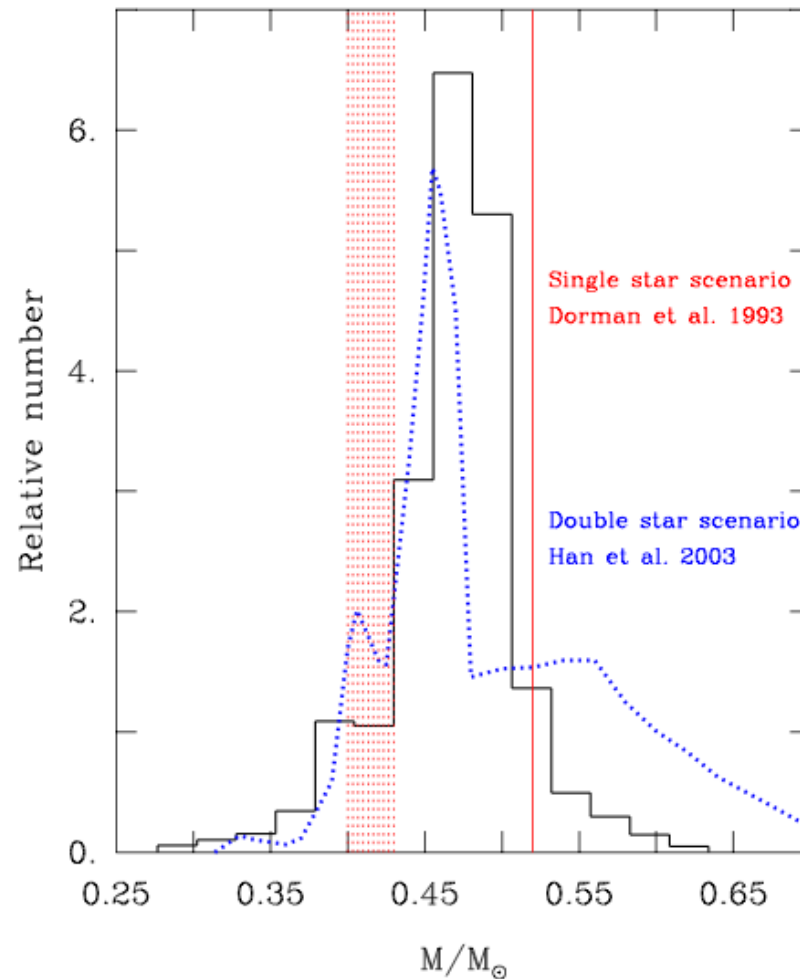
Median mass: 0.471  $M_{\odot}$

Range of 68.3% of stars:  
0.441-0.499  $M_{\odot}$

Sample	Mean mass ( $M_{\odot}$ )	Median mass ( $M_{\odot}$ )	Range of mass (68.3%; $M_{\odot}$ )
extended (20 stars)	0.469	0.471	0.436–0.501
15 pulsators	0.470	0.471	0.441–0.499
5 binaries (orbits)	0.464	0.476	0.411–0.510
9 binaries (total)	0.470	0.466	0.435–0.515
11 singles	0.468	0.473	0.437–0.498

No detectable significant differences between distributions  
(especially between singles and binaries)

## 6. Comparison with theoretical distributions

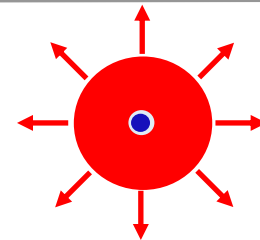


Empirical distribution agrees well with expectations of stellar evolution theory...but still small-number statistics !

## 2. Single and binary formation scenarios

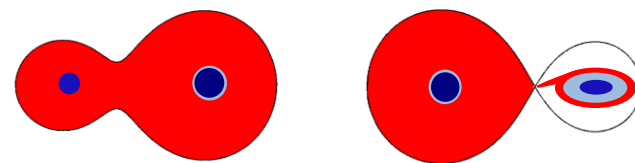
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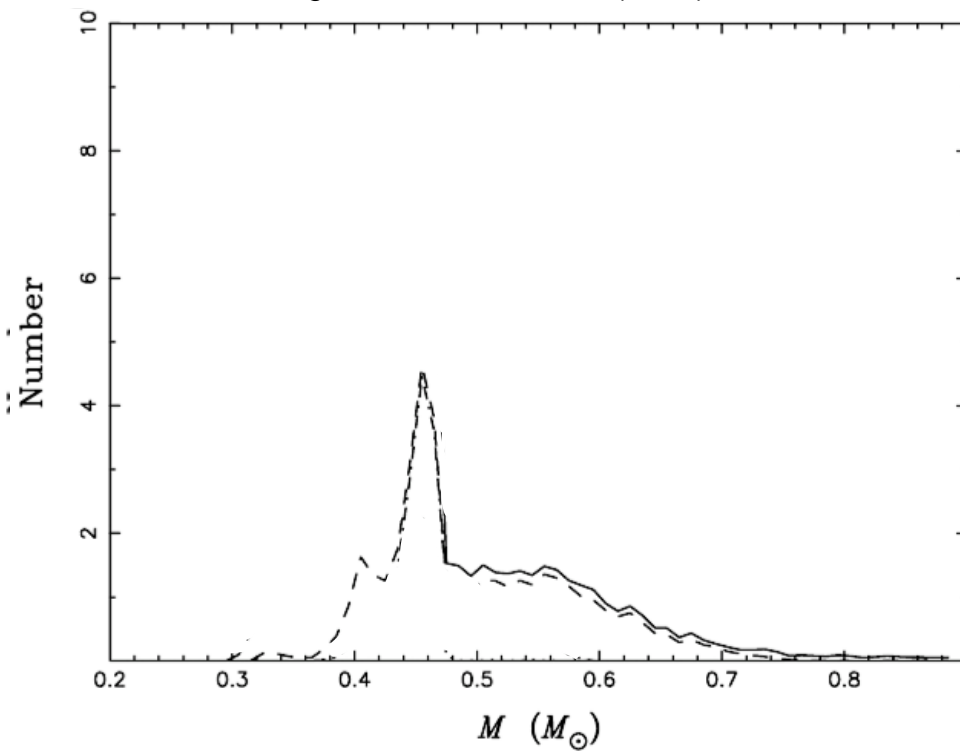


- Binary star evolution (Han et al. 2002, 2003)

Common envelope ejection (CE), stable mass transfer by Roche lobe overflow (RLOF), and He-white dwarf mergers



Figures from Han et al. (2003)



Weighted mean distribution  
for binary evolution:  
(including selection effects)

$0.30 \leq M_*/M_s \leq 0.70$   
peak  $\sim 0.46 M_s$  (CE, RLOF)  
high masses (mergers)

## Conclusions and room for improvement

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- ✓ No significant differences between distributions of various samples (asteroseismic, light curve modeling, single, binaries, etc.)
- ✓ Single star evolution scenario does exist
- ✓ Importance of the merger scenario ? (single stars with fast rotation)
- ✓ Our empirical mass distribution agrees well with theoretical expectations...

### But:

- ✓ Currently only 20 objects: 11 (apparently) single stars and 9 binaries
- ✓ Among  $> 2000$  known sdB,  $\sim 100$  pulsators are now known (e.g. thanks to *Kepler*)
- ✓ Both light curve modeling and asteroseismology are a challenge (accurate spectroscopic and photometric observations, stellar models, etc.)