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NeuroImage

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# Rejection of pulse related artefact (PRA) from continuous electroencephalographic (EEG) time series recorded during functional magnetic resonance imaging (fMRI) using constraint independent component analysis (cICA)

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## ARTICLE INFO

### Article history:

Received 5 June 2008

Revised 31 August 2008

Accepted 10 October 2008

Available online xxxx

## ABSTRACT

Rejection of the pulse related artefact (PRA) from electroencephalographic (EEG) time series recorded simultaneously with fMRI data is difficult, particularly during NREM sleep because of the similarities between sleep slow waves and PRA, in both temporal and frequency domains and the need to work with non-averaged data. Here we introduce an algorithm based on constrained independent component analysis (cICA) for PRA removal. This method has several advantages: (1) automatic detection of the components corresponding to the PRA; (2) stability of the solution and (3) computational treatability. Using multichannel EEG recordings obtained in a 3 T MR scanner, with and without concomitant fMRI acquisition, we provide evidence for the sensitivity and specificity of the method in rejecting PRA in various sleep and waking conditions.

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## Introduction

In recent years, the combination of functional Magnetic Resonance Imaging (fMRI) and electroencephalography (EEG) has been increasingly used to characterize human brain function, with the objective of harvesting the high spatial resolution of the former and the exquisite temporal precision of the latter. Although also its use to characterize evoked response (Czisch et al., 2002; Liebenthal et al., 2003). The full benefit of combining EEG and fMRI is particularly obvious when one is interested in spontaneous brain states or events characterized by specific EEG oscillations or transients, the time course of which is hardly predictable. Accordingly, EEG–fMRI has proven particularly successful in characterizing the cerebral correlates of normal brain oscillations as waking brain rhythms (Goldman et al., 2000; Laufs et al., 2003; Moosmann et al., 2003; Niazy et al., 2004), or sleep transients (Schabus et al., 2007), as well as in localizing the hemodynamic correlates of epileptic activities (Seeck et al., 2001).

A major problem of EEG–fMRI consists of the contamination of EEG recordings by gradient switching (gradient artefacts) and pulse related artefacts (PRA). The former is related to the echoplanar sequence used in fMRI. The latter is thought to have multiple causes related to the

interaction between the static magnetic field and the heart beat, such as pulsatile motion of recording electrodes, cardio-ballistic head movements and Hall effects in blood vessel (Allen et al., 1998; Goldman et al., 2000; Srivastava et al., 2005; Nakamura et al., 2006). Both artefacts are larger than the genuine EEG signal and have to be removed before EEG can be properly analyzed.

Because the gradient artefact is very reproducible across consecutive volume acquisitions, it is satisfactorily removed from raw data by subtracting an averaged artefact waveform (Average Artefact Subtraction (AAS)), followed by adaptive noise cancellation to reduce any residual artefact (Allen et al., 1998). In contrast, PRA is much harder to reject. Indeed, its morphology and its topography substantially vary from beat to beat. Because of this non stationarity, methods based on a simple AAS, although reasonably efficient, result in residual artefacts in the data because they assume that the PRA is a slowly changing signal that can be accurately characterized by a moving average. Various methods were derived from AAS modelled PRA using exponential weighted average (Goldman et al., 2000), median filter (Sijbers et al., 2000) or adaptive filters (Han et al., 2004; Wan et al., 2006) but eventually produced similar results (Grouiller et al., 2007).

To allow more flexibility in the characterization of PRA, other channel-wise model-explicit rejection algorithms were based on temporal Principal Component Analysis (PCA, Niazy et al., 2005) or a moving General Linear Model (mGLM, Vincent et al., 2007). Others used estimates of the motion artefact noise by piezoelectric motion

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sensors (Bonmassar et al., 2002; Masterton et al., 2007) and an adaptive filtering algorithm based on the Kalman filter (Bonmassar et al., 2002). These led to relatively efficient solutions but required extra equipment to be placed on and around the subject.

Another class of PRA removal techniques is based on blind source separation. Methods using Independent Component Analysis (ICA) decompose the EEG recordings into independent components (ICs) and suppress the PRA-related ones (Benar et al., 2003; Nakamura et al., 2006; Finelli et al., 2003; Han et al., 2004; Mantini et al., 2007). The problems of these methods are non-reproducibility of the results (Briselli et al., 2006; Grouiller et al., 2007) and the difficulty in objectively selecting the PRA-related ICs. To address the issue of ICA variability, it was suggested to apply the ICA algorithm iteratively and to average the results across multiple executions (MICA) but this procedure requires an overwhelming computational power (Briselli et al., 2006; Phillips et al., 2006) and is very time-consuming. To address the issue of IC selection, an automatic method based on the correlation between the IC and the ECG was developed (Srivastava et al., 2005) but this type of detection does not always perform well in detecting PRA-related ICs (Debener et al., 2007). Finally, it has also been argued that ICA could not be used to reject PRA for recordings obtained in a high-field scanner without additional pre-processing because ICA is a fixed spatial filter and the PRA was observed to have a variable within-cycle topography (Debener et al., 2008).

In the framework of sleep studies, the conditions for PRA rejection can be particularly difficult. During the deepest stages non rapid eye movement (NREM) sleep, also called slow-wave-sleep (SWS), EEG recordings are characterized by abundant high-amplitude slow waves. In that case, the difficulty in rejecting PRA from EEG recordings arises from the similarity between slow waves and PRA both in the temporal and frequency domains. Slow waves and PRA typically recur about every second and their amplitudes are in the same order of magnitude (typically several hundred  $\mu\text{V}$  peak to peak at 3 T). Similarly, the bulk of the spectral power of both sleep slow waves and PRA lies between 0.5 and 5 Hz. Consequently, the estimation of a model of PRA using classical methods (non-ICA based) is likely to be confounded by genuine neurally-generated slow waves and the ability of these methods to retrieve slow waves during NREM sleep is questionable.

Yet, slow waves of deep NREM sleep represent a fundamental brain activity associated with important functional properties. For instance, they have been used as a measure of sleep depth and their power density (between 0.75 and 4 Hz) is used as a reliable parameter quantifying the dissipation of the homeostatic sleep pressure (Dijk et al., 1997). Slow waves have also been implicated in offline memory processing either because they would allow for a local synaptic downscaling (Huber et al., 2004) or because they might promote the replay of neuronal firing sequence supposedly representing the learned material (Buzsaki, 1996).

In order to allow the study of SWS using EEG-fMRI, we developed a new efficient, robust, and computationally efficient PRA-rejection technique based on constrained ICA (cICA). This novel method is equally efficient in rejecting PRA for EEG data recorded during wakefulness and NREM sleep.

## PRA rejection algorithm

In this section we will introduce our cICA-based PRA rejection algorithm as well as former ones which we will use for comparison. Since each of these techniques uses a QRS peak detection algorithm in ECG, we decided to use the same algorithm for each of them and describe this one in the next subsection. Note that we use the FMrib plug-in for EEG, provided by the University of Oxford Centre for Functional MRI of the Brain (<http://users.fmrib.ox.ac.uk/~rami/fmribplugin/index.html>), for the practical implementation of the QRS peak detection and AAS and PCA-based methods for PRA rejection. We will then describe the available techniques used for comparison before introducing our new cICA algorithm.

## QRS peak detection

The peak detection algorithm we use was developed by Niazy et al. (2005) and its performance has been evaluated in the same article. The ECG peak detection is a modification of the algorithm proposed by Christov (2004). In this algorithm, a complex lead is computed from several single ECG channels. Yet, in most EEG/fMRI application the ECG is measured by only one lead, so an alternative complex lead has to be found. This complex lead is computed using a  $k$ -Teager operator (Kim et al., 2004; Mukhopadhyay and Ray, 1998) to the filtered (Bandpass filtered from 7 to 40 Hz) ECG channel and then setting all negative values to zero:

$$\text{ECG}_{\text{complex}}(t) = \max(E^2(t) - E(t-k)E(t+k), 0); \quad (1)$$

where  $\text{ECG}_{\text{complex}}$  is the complex lead,  $t$  the time index,  $E$  the filtered ECG and  $k$  a frequency selection parameter (Kim et al., 2004). The peaks are then detected using the original adaptive threshold algorithm (Christov, 2004). This produces a binary vector  $\mathbf{P}$  where the 1 in this vector indicates the peaks in the ECG channel.

## False positive removal

The vector  $\mathbf{P}$  is divided into segments of 20 s interval with an overlap of 5 s. For each segment, a peak is considered as false positive if the time between two peaks is smaller than  $3\sigma_{RR}$  and  $\mathbf{P}$  is corrected accordingly.  $\sigma_{RR}$  is the median of the R-R intervals of this segment and  $\sigma_{RR}$  is the standard deviation of the R-R intervals of this segment.

After  $\mathbf{P}$  is corrected, the ECG is divided according to vector  $\mathbf{P}$  and then the average is computed to form an average ECG template. This template is then taken as a reference and the peaks in the vector  $\mathbf{P}$  are corrected to correspond to the maximum correlation between the ECG template and the original ECG.

## False negative correction

As in the previous paragraph, the vector  $\mathbf{P}$  is divided into 20 s segments with 5 s of overlap and  $\sigma_{RR}$  are then calculated for each segment. If an R-R interval exceeds 1.5 times  $\sigma_{RR}$  a peak is added in the  $\mathbf{P}$  vector after a time  $\sigma_{RR}$  after the first peak of this interval. Once all false negatives were corrected, the peaks of vector  $\mathbf{P}$  are adjusted to correspond to the maximum correlation between the ECG template computed using the new  $\mathbf{P}$  and the original ECG as explained in the previous paragraph.

Note that the standard delay between an ECG peak and the occurrence of the PRA in EEG channel was observed to be 210 ms by Allen et al. (1998). The influence of the quality of ECG on QRS peak detection was investigated by Niazy et al. (2005).

## Former PRA rejection algorithms

We have considered 3 reference methods (AAS, PCA and MICA) to assess the performance of our cICA-based correction method.

## AAS

The PRA template in each EEG channel is computed by averaging the sections of EEG signals  $\pm$  half the mean R-R interval centered on the ECG peaks delayed by the average time difference between the heart contraction and the occurrence of the PRA in the EEG. Before using an EEG section in the average computation, each section is tested for artefacts which would corrupt the PRA template. Sections of EEG with a mean amplitude 3 times higher than the minimum section are rejected. If fewer than two sections are artefact-free, the previous PRA template is used instead. Because high frequency phenomena are poorly rejected by an average subtraction, a first order polynomial is fitted to each section of EEG and subtracted before estimating the PRA template.

Once the PRA template is calculated, it is subtracted from the original EEG signal and this gives the corrected signal as a result.

## PCA

After shifting the QRS peaks by 210 ms (to account for the standard delay between QRS complexes and artefact occurrence), a matrix  $\mathbf{S}$  (dimension  $p \times q$ ) is formed for each channel: each row is filled with one occurrence of the PRA.  $p$  is the number of artefact occurrences on this channel and  $q$  the number of points spanning each artefact interval.

Then PCA is performed on  $\mathbf{S}$  such that the different variations of the artefact are captured by the principal components of  $\mathbf{S}$  and ordered according to the variance explained by each component. The projection of  $\mathbf{S}$  onto the principal component coefficients are referred to as PCs. The first 3 PCs are placed in matrix  $\mathbf{B}$  (dimension  $q \times 3$ ) and are considered as an optimal basis. Each segment of the original signal  $\mathbf{Y}_j$  (which is equal to a row of  $\mathbf{S}$ ) can be expressed in term of  $\mathbf{B}$  through a linear model:

$$\mathbf{Y}_j = \mathbf{B}\beta_j + \varepsilon_j \quad (2)$$

where  $\beta_j$  is a  $3 \times 1$  parameter vector and  $\varepsilon_j$  is the error term for the segment  $j$  of the considered channel. The model is then fitted in a least squares sense to each row of  $\mathbf{S}$  and subtracted to the corresponding artefact occurrence in the considered EEG channel. This process is repeated for each channel.

## MICA

This section introduces ICA (for a more technical presentation see Bell and Sejnowski (1995); Hyvarinen (1999) and Hyvarinen (2000)) and MICA (cf. (Briselli et al., 2006; Phillips et al., 2006)).

ICA stands for Independent Component Analysis and is used to decompose data (in our case, EEG recordings) as a linear combination of statistically independent sources. EEG data are represented by a matrix  $\mathbf{X}$  of dimension  $N_{ch} \times N_s$ , where  $N_{ch}$  is the number of EEG channels and  $N_s$  the number of samples per channel. From a statistical point of view, EEG recordings are observations of  $\mathbf{x} = (x_1, x_2, \dots, x_{N_{ch}})^T$ , where each  $x_i$  is a random process. Each sample of the  $i^{\text{th}}$  row of the matrix  $\mathbf{X}$  is thus considered as a realization of the  $x_i$  random process.

Let  $\mathbf{x} = (x_1, x_2, \dots, x_m)^T$  be the observations of an  $m$ -dimensional Random Process, and  $\mathbf{s} = (s_1, s_2, \dots, s_n)^T$  an  $n$ -dimensional random process so that the  $s_i$  are statistically independent from each other. Each  $s_i$  is called an Independent Component (IC) or a source. Each  $x_i$  is supposed to be a linear mixture of the  $s_i$ . Then the problem of ICA is to determine a constant weight (or demixing) matrix  $\mathbf{W}$ , given  $\mathbf{x}$  so that the following equation is verified:

$$\mathbf{s} = \mathbf{W}\mathbf{x} \quad (3)$$

If the mixing matrix is defined as  $\mathbf{A} = \mathbf{W}^{-1}$  then:

$$\mathbf{x} = \mathbf{A}\mathbf{s} \quad (4)$$

Classically, ICA searches for as many statistically independent sources as there are for channels using an iterative scheme. Once all sources have been detected, artefact-related sources are identified and removed from EEG recordings by reconstructing EEG signals only from supposedly neural sources. In mathematical terms, the algorithm finds a demixing matrix  $\mathbf{W}$  which is used to project the EEG from the signal space to the source space. The artefact sources are then replaced by a null vector, i.e. by sources generating no signal (void sources). Neural and void sources are projected back into the signal space, thereby reconstructing a clean EEG signal devoid of the artefactual contribution.

MICA consists in using the ICA algorithm iteratively  $t$  times. The main idea is to increase the reliability of the estimate of the weight vectors by selecting the ones that occur more often over all the executions. This technique requires a high number of executions of ICA to achieve a reliable estimate of the solution.

In our implementation, once the weight vectors for one execution have been computed, the ICs to be suppressed are identified by computing the correlation between the ICs and a BCG template as described in Srivastava et al. (2005). The cleaned data are then computed. This process is repeated

for each execution of the ICA algorithm. After  $t$  versions of the cleaned data are available, their mean is computed.

## cICA rejection algorithm

A mathematical account of constrained ICA (cICA) is presented in detail in Appendix 1. Independent Component Analysis assumes that EEG signals consist of a linear mixture of statistically independent (neural and artefact) sources. As the number of sources is generally assumed to be the same as the number of channels, its size is  $[N_{ch} \times T]$  time points].  $\mathbf{x}$  corresponds to recorded EEG signals  $[N_{ch} \times T]$  time points] and  $\mathbf{W}$  a fixed scalar matrix, composed of  $N_{ch}$  row-vectors of dimension  $N_{ch}$  (square matrix of size  $N_{ch}$ ).

Here we reasoned that, if EEG signals are assumed to be a linear mixture of two (neural and artefact) sets of sources, one could in principle identify one set of sources and deduce the second one in a more efficient way than through the cumbersome iterative search of all sources. The row vectors of  $\mathbf{W}$  can be viewed as a non-orthonormal base of an  $N$ -dimensional space. During preprocessing, an orthonormal matrix is deduced from  $\mathbf{W}$  (Appendix A.2). The identification of the artefact-related row-vectors could make it possible to find the complementary orthonormal set of vectors, i.e. the neural-related vectors of  $\mathbf{W}$  using a Gram–Schmidt scheme. Because there are more neural than artefact sources (for a 62-electrode EEG recording system, 3 to 8 sources corresponding to PRA are typically identified) the computational load would be considerably reduced by computing only the latter.

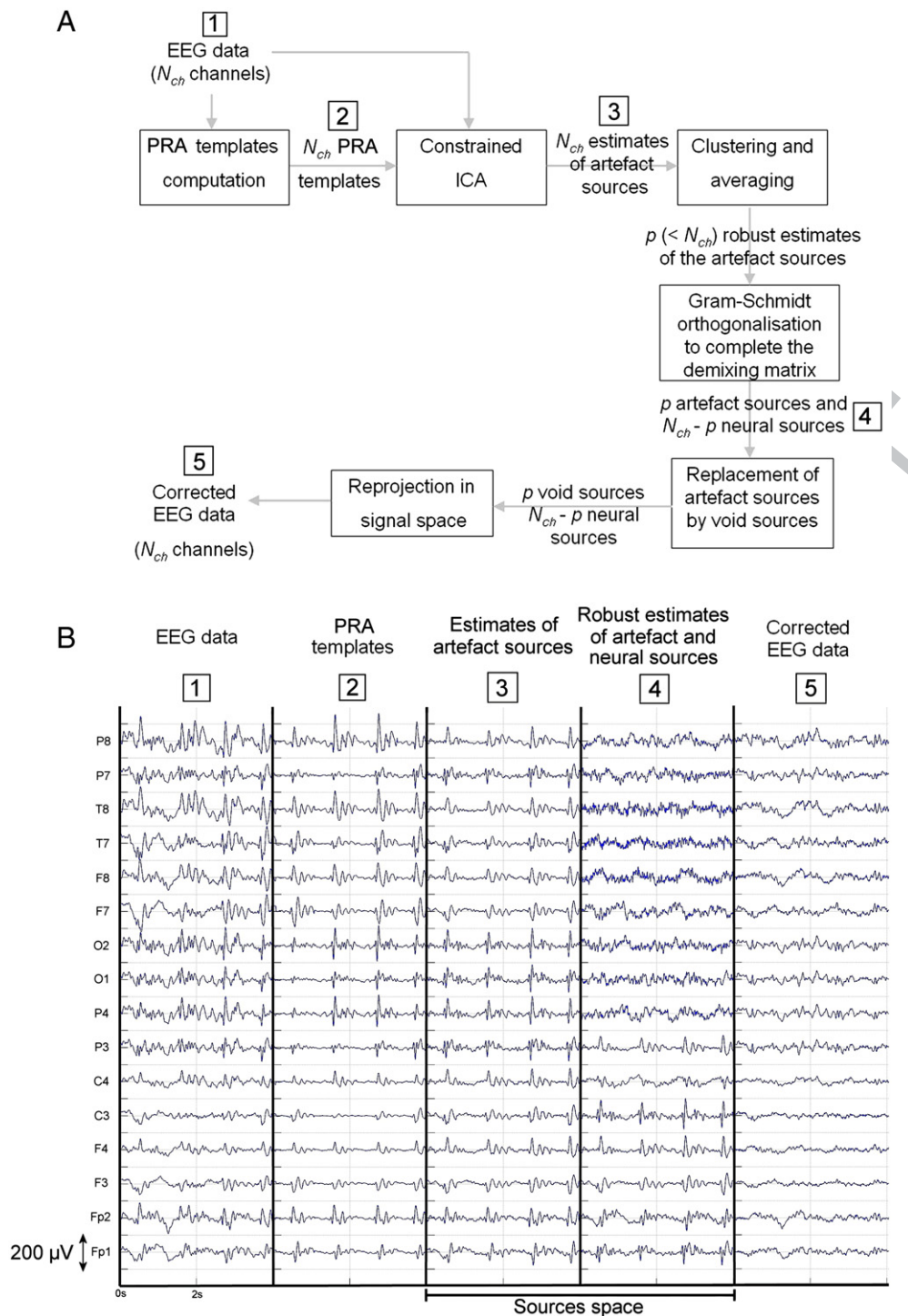
In the present paper, constrained ICA was used to identify PRA sources. In contrast to classical ICA, cICA does not converge to the source closest to its random initialization but finds the closest source to a given constraint. This implies that the time course of the identified components closely matches the constraint. In our application, the constraint consists in a model of the PRA, as classically computed by the AAS method (Allen et al., 1998). For each channel an average PRA is computed across the sections of EEG signal centered on the last 10 electrocardiogram (ECG) QRS peaks. As stated above, the resulting model of the PRA is not perfect because the averaging does not account for the beat-to-beat variability in heart rate and in the shape of the PRA. However, it captures the essential features of PRA necessary to seed the cICA analysis.

The cICA algorithm provides  $N_{ch}$  estimates of the artefact sources. Since the number of artefact sources is largely inferior to the number of channels (64 in our case), some estimates will converge to the same artefact source. A clustering is thus performed through a classic  $K$ -means algorithm (Appendix A.3) to group corresponding estimates. The clustering algorithm gives also a measure of the variance expressed by the  $K$  clusters:

$$ev_K = 1 - \frac{\sum_{k=1}^K \frac{n_k}{N_{ch}} var_k}{Var} \quad (5)$$

where  $K$  is the number of clusters,  $var_k$  the variance in the  $k$ th cluster,  $Var$  the variance of the initial set of vectors,  $n_k$  the number of vectors in the  $k$ th cluster and  $N_{ch}$  the number of vectors in the initial set of vectors. Since each component was constrained by a template of the PRA, most of the variance (at least 70%) of the estimates should be expressed by a few clusters (typically less than 8). On the other hand if more clusters are necessary, it means that the estimates are more randomly or independently distributed, i.e. the data are unlikely to be contaminated by PRA.

Practically, our approach redirects the computational power used to find the neural sources in classic ICA algorithm to increase the robustness of the artefact source estimates. In other words, our algorithm acts in a similar way to multiple executions of an ICA algorithm (MICA), which has been shown to improve the robustness of the sources (Briselli et al., 2006; Phillips et al., 2006), but only for the artefact sources. Indeed, each



**Fig. 1.** (A) Block diagram of our cICA rejection algorithm, the numbers refers to the corresponding EEG time series in part B of the figure. (B) 4 s of signal are displayed in the different step of our algorithm. Note that the scale is not relevant in source space. B1 shows the original EEG recordings. B2 shows the constraint used to feed the cICA part of our algorithm. B3 shows the sources found using cICA. B4 shows the sources after clustering and Gram-Schmidt orthogonalization. Note that the last seven ICs are artefact-related. B5 shows the cleaned signal.

313 clustered artefact component is the average of various similar compo- 320  
 314 nents. Crucially the problem of identifying the artefact related 321  
 315 components (as met with classical ICA) is completely avoided here.

316 To summarize, our algorithm consists in (see Figs. 1A, B for a sample 322  
 317 signal in each step):

- 318 • Computing a PRA template for each of the  $N_{ch}$  channels of the EEG 325  
 319 signal;

- Computing the artefact related components based on these 320  
 constraints using the cICA algorithm; 321
- Clustering the estimated artefact components and computing the 322  
 average of each cluster to produce more robust estimates of the 323  
 artefact sources; 324
- Finding the subspace of neural sources within the demixing matrix, 325  
 i.e. the complementary space of the artefact sub-space, using a 326  
 Gram-Schmidt procedure; 327

328 • Replacing artefact sources by void sources and reprojecting all sources  
329 in signal space.

330 This algorithm potentially leads to a more robust estimation than  
331 other ICAs of the PRA sources without increasing the computational  
332 cost. In addition, the identification of sources to suppress is automated,  
333 data driven and not observer-dependent.

## 334 Methods and materials

335 The section is organized in two parts. In the first one, EEG data  
336 recorded on 2 sleeping volunteers are processed. They were simply placed  
337 in the static field of the MRI scanner, but in the absence of fMRI  
338 acquisitions (in order to avoid any gradient artefact in the EEG signal)  
339 during NREM sleep. The second part uses EEG data acquired on 9  
340 volunteers in various consciousness states (wakefulness, light and deep  
341 non rapid eye movement sleep), during simultaneous fMRI imaging. All  
342 volunteers were fully informed and gave their written consent. In both  
343 cases, EEG was recorded utilizing two MR-compatible 32-channel  
344 amplifiers (Brainamp MR plus, Brain Products GmbH, Gilching, Germany)  
345 and an MR-compatible EEG cap (Braincap MR, Falk Minow Services,  
346 Herrsching Breitbrunn, Germany) with 64 ring-type electrodes. EEG caps  
347 included 62 scalp electrodes as well as one electrooculogram (EOG) and  
348 one electrocardiogram (ECG) channel which were online referenced to  
349 FCz. Electrode-skin impedance was kept below 5 k $\Omega$  in addition to the 5 k  
350  $\Omega$  resistor built into the electrodes. EEG was digitized at 5000 Hz sampling  
351 rate with a 500 nV resolution. Data were analog-filtered by a bandlimiter  
352 low pass filter at 250 Hz (30 dB/Octave) and a high pass filter with 10 s time  
353 constant corresponding to a high pass frequency of 0.0159 Hz. Data were  
354 transferred outside the scanner room through fibre optic cables to a  
355 personal computer where the EEG system running Brain Recorder Soft-  
356 ware v1.03 (Brain Products GmbH, Gilching, Germany) was synchronized  
357 to the scanner clock. For analysis, EEG data were low-pass filtered (FIR  
358 filter, -36 dB at 70 Hz), and down-sampled to 250 Hz. The power spectra of  
359 the raw data were computed using fast Fourier transform on successive 4 s  
360 epochs, overlapping by 2 s and weighted by a Welch window.

### 361 EEG recordings without gradient artefact

362 Two healthy volunteers were completely sleep deprived during  
363 one night (corresponding to about 24 h of continuous wake). During  
364 the following morning, they were recorded in the scanner room (3 T  
365 MR scanner, Allegra, Siemens, Germany) in 2 consecutive conditions:  
366 (1) lying on the scanner couch in reverse position, i.e. the head outside  
367 the scanner<sup>1</sup> and (2) lying in standard position, i.e. installed head first  
368 in the scanner bore. Conditions (1) and (2) are therefore as close as  
369 possible for the volunteers and should not affect their sleep EEG.  
370 Nonetheless, the recordings in condition (1) are expected to be much  
371 less contaminated by PRA due to the lower magnetic field at  
372 electrodes level. In both cases, recordings were obtained without  
373 simultaneously scanning. For each session, recordings were carried on  
374 until subjects reached steady slow wave sleep, the deepest stage of  
375 non REM sleep. Analyses were run on two minute periods of these  
376 recordings. They consisted in cleaning the EEG time series with four  
377 different methods: AAS, PCA, MICA and cICA. To assess the quality of  
378 PRA rejection by these four methods, two quality indices were  
379 computed. Two indices of quality are then computed. Firstly, the  
380 Improvement of Normalized Power Spectrum introduced by Tong et  
381 al. (2001) measures the power attenuation in the corrected signal:

$$\text{INPS}(\text{Chan}, N) = \frac{\sum_{j=1}^N p_j^{\text{before}}}{\sum_{i=1}^N p_i^{\text{after}}} \quad (6)$$

<sup>1</sup> Since this is a head only scanner, the subject has his feet near the scanner bore and his head as far as possible from the magnet center (about 2m). The magnetic field at the head level has a theoretical value of about 20mT given the scanner's specifications.

where  $p^{\text{before}}$  and  $p^{\text{after}}$  are mean power in a 1 Hz window centered on  
382 the  $j$ th harmonic of the heart frequency respectively before and after  
383 PRA removal for a particular channel Chan. The INPS thus represents  
384 the quality of power rejection in these windows, hypothesizing that  
385 most of the power in the latter are PRA-related. 387

For our computations, we chose  $N=5$  to take into account the first  
388 four harmonics of the PRA, hypothesizing that most of the PRA-related  
389 power is taken into account.  $N$  is usually chosen between 4 and 6 in  
390 the literature (cf. Briselli et al., 2006; Srivastava et al., 2005; Nakamura  
391 et al., 2006). INPS is larger than 1 when power is around spectral  
392 modes characteristic of pulse artefact: the larger INPS, the larger the  
393 power attenuation. 394

Second, the Distortion Index introduced by Nakamura et al. (2006)  
395 measures the distortion introduced by the PRA rejection method: 396

$$\text{DI}(f) = \frac{1}{N_{\text{ch}}} \sum_{\text{Chan}=1}^{N_{\text{ch}}} \left( \frac{\int_{f-\Delta f}^{f+\Delta f} \sqrt{\phi_{\text{cleaned, Chan}}(u) du}}{\int_{f-\Delta f}^{f+\Delta f} \sqrt{\phi_{w/o \text{PRA, Chan}}(u) du}} \right)^2 \quad (7)$$

where  $\phi_{w/o \text{PRA, Chan}}(u)$  (resp.  $\phi_{\text{cleaned, Chan}}(u)$ ) is the value of the power  
397 spectrum frequency  $u$  at the electrode Chan=1 for the dataset  
398 recorded in reverse position, with the head outside the scanner and  
399 with minimal PRA (respectively recorded with the head inside the  
400 scanner and corrected for the large PRA).  $N_{\text{ch}}$  is the number of EEG  
401 channels and the DI is computed for a frequency interval between  $f$   
402  $-\Delta f$  and  $f+\Delta f$ . For our computation, we used  $\Delta f=0.25$  Hz, i.e. frequency  
403 windows of 0.5 Hz. 405

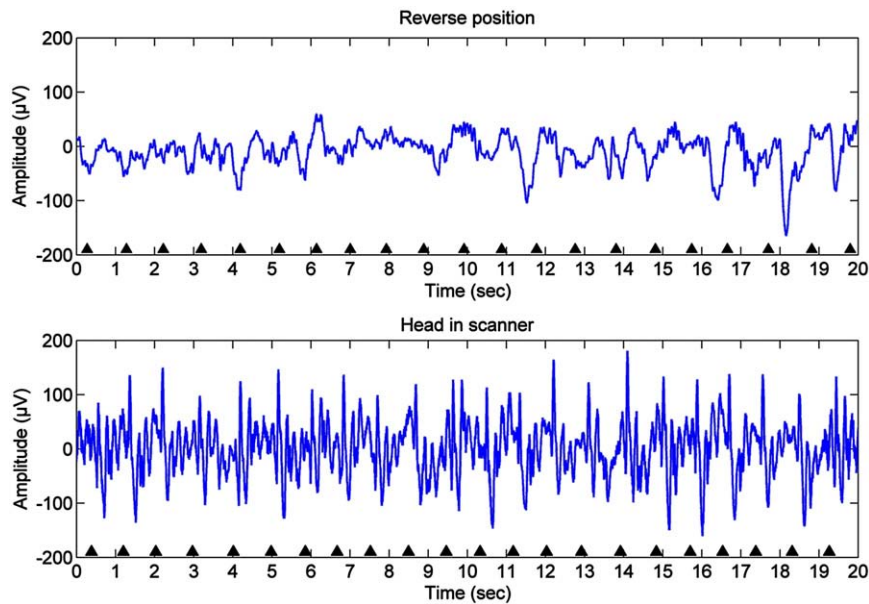
### 406 EEG recordings with gradient artefact

The aim of this experiment is to generalize the findings of the previous  
407 case to a larger set of data acquired during effective fMRI scanning, and to  
408 various states of consciousness characterized by typical oscillations other  
409 than slow waves, namely alpha rhythm during wakefulness and spindles  
410 during stage 2 sleep. EEG data used in this section were recorded from 9  
411 healthy volunteers (4 females; age range: 18–25), who participated in an  
412 EEG/fMRI sleep study. Functional MRI time series were acquired  
413 continuously using a 3 T MR scanner (Allegra, Siemens, Germany).  
414 Multisliced, T2\*-weighted fMRI images were obtained with a gradient  
415 echo-planar sequence using axial slice orientation and reduced slew rate  
416 for efficient gradient rejection (32 slices; voxel size:  $3.4 \times 3.4 \times 3$  mm<sup>3</sup>;  
417 matrix size  $64 \times 64 \times 32$ ; TR=2460 ms; TE=40 ms; flip angle=90°;  
418 FOV=220×220 mm<sup>2</sup>). Some of these data have been previously  
419 published (Schabus et al., 2007) but have not been corrected by cICA.  
420 Gradient artefacts were removed in Vision Analyzer (Brain Products  
421 GmbH, Gilching, Germany) using a method adapted from Allen et al.  
422 (2000). Sleep staging followed standard criteria (Rechtschaffen and Kales,  
423 1968), and identified periods of wakefulness, stage 2 and slow wave sleep.  
424 Analyses were conducted on 2-minute EEG epochs acquired in each of  
425 these three states and again assessed the PRA rejection by AAS, PCA, MICA  
426 and cICA. The INPS was computed as in the previous section. For 24 two-  
427 minute EEG epochs, an expert was blindly presented with the 4  
428 differently corrected signals, knowing in which consciousness stage the  
429 EEG was recorded. His duty was then to sort the corrected recording by  
430 quality of the signal (1 being the worse correction and 4 the best one),  
431 taking into account the residue of PRA left in the signal and the  
432 suppression of stage-related activity. 433

## 434 Results

### 435 EEG recordings without gradient artefact

The PRA was obviously much larger when the head of the subject  
436 was placed within the MR scanner than outside the scanner (Fig. 2).  
437 The comparison of these recordings thus allowed for the estimation of  
438 the sensitivity and specificity of various artefact rejection methods. 439

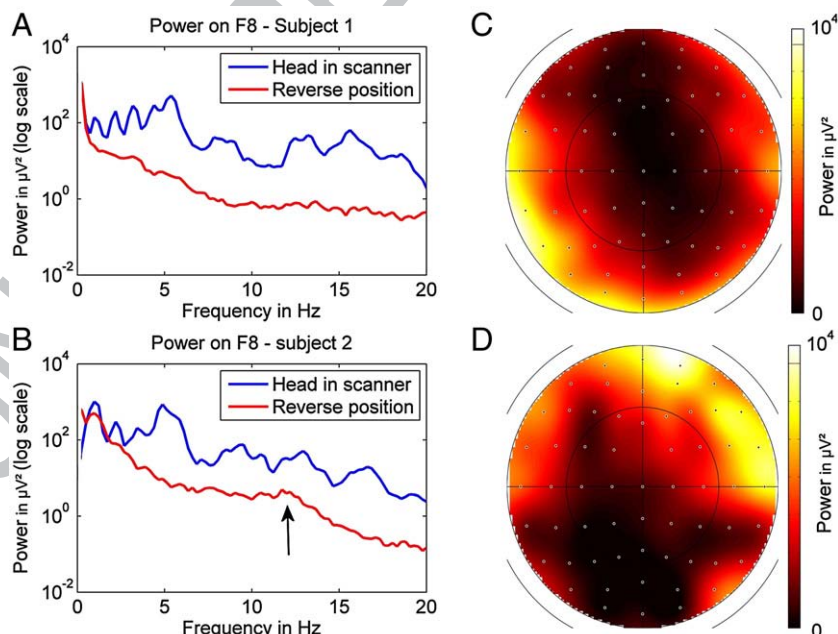


**Fig. 2.** EEG recording at electrode F8 with the head outside (top) and inside (bottom) the MR scanner, both without MR acquisition. The PRA is clearly identified in the latter condition. The black triangle indicates a QRS peak in the ECG channel.

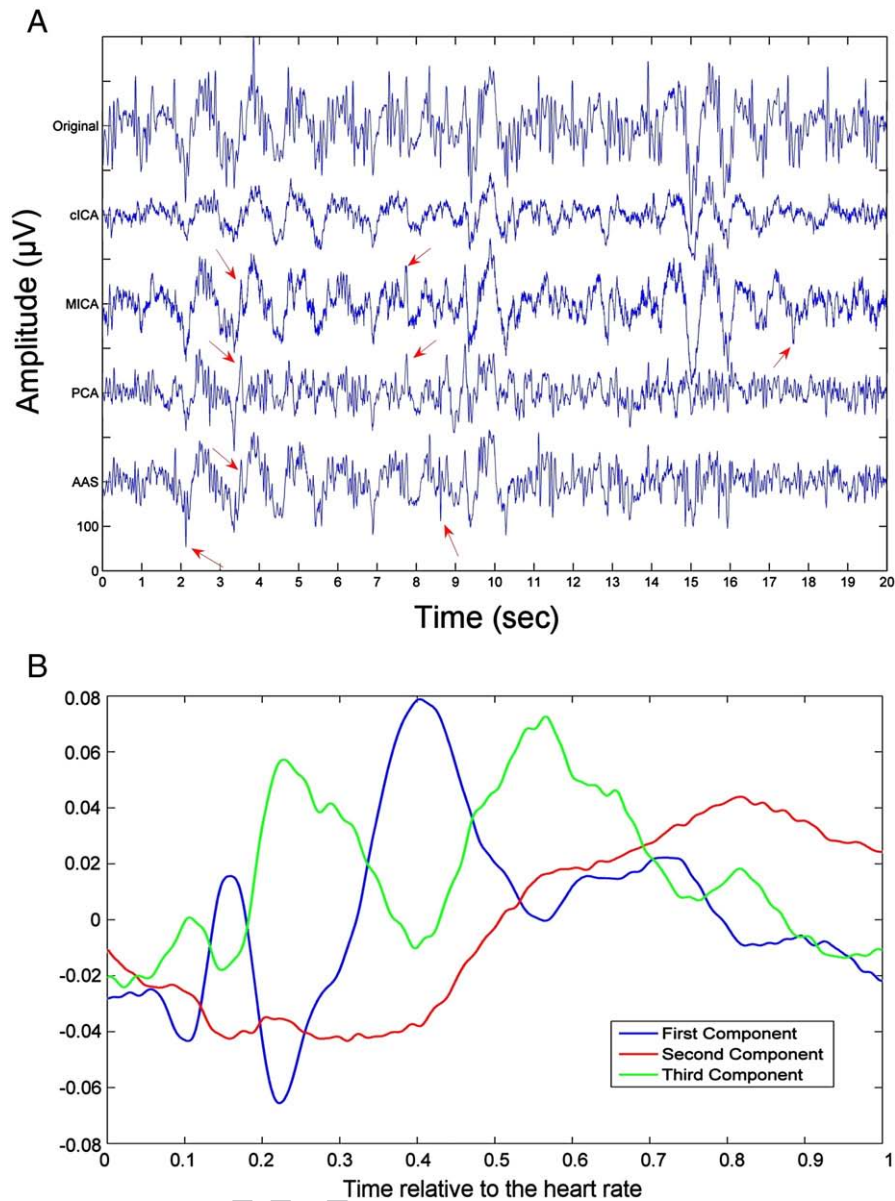
440 We first characterized the power spectrum of PRA and its scalp  
 441 topography (Fig. 3). We computed the power spectrum of data recorded  
 442 inside and outside the scanner bore. The power spectrum of data  
 443 recorded outside the scanner bore is characterized by a component  
 444 around 1 Hz (0.5 Hz and 1 Hz in subjects 1 and 2, respectively), consistent  
 445 with the prominent slow rhythm typical of deep NREM sleep (Figs. 3 A, B,  
 446 red curves). A secondary mode is observed in subject 2 in the spindle  
 447 frequency range (Fig. 3B, arrow). The power spectrum of data recorded  
 448 within the scanner bore is dominated by several modes between 1 and  
 449 5 Hz as well as broadband modes around 8, 13 and 17 Hz (Figs. 3 A, B, blue  
 450 curves). The scalp topography of PRA power, computed as the difference  
 451 between the 2 conditions, is not homogeneous (Figs. 3 C, D). Most of the

power difference is located in the right fronto-temporal (subject 1) and  
 452 left fronto-temporo-occipital regions (subject 2). The low power  
 453 observed around fronto-central electrodes is in part related to referen-  
 454 cing to FCz but not entirely so. The origin of these variations has not been  
 455 systematically evaluated and could also be linked to the orientation of  
 456 the electrodes relative to the static field, or their position relative to the  
 457 heart and blood vessels. 458

Fig. 4A shows the signal recorded in subject 1 for 20 s during slow  
 459 wave sleep on electrode Fz before and after correction by different  
 460 methods. This electrode was chosen because it suffers from a large PRA in  
 461 this particular recording (see above). In the original recordings (top row),  
 462 the PRA is so prominent that the sleep slow waves are barely identifiable. 463



**Fig. 3.** Power spectrum at electrode F8 with the head inside or outside the MR scanner, both without image acquisition for 2 subjects. The topography of the PRA (computed as the power difference between the 2 conditions) is showed in C and D.



**Fig. 4.** (A) Example of original data, recorded on electrode Fz during slow wave sleep, and the corrected signal obtained by different method of PRA rejection. (B) First three components retrieved by the Principal Component Analysis method.

464 Slow waves are efficiently retrieved by all methods except PCA which  
 465 suppresses most of them. With this technique (row 4), large-amplitude  
 466 sleep waves are mistakenly included in the first principal components,  
 467 and removed as PRA (Fig. 4B). On the other hand, PRA is still easily  
 468 identifiable (red arrows) after artefact rejection by AAS (row 5) or MICA  
 469 (row 3), but hardly so after cICA (row 2).

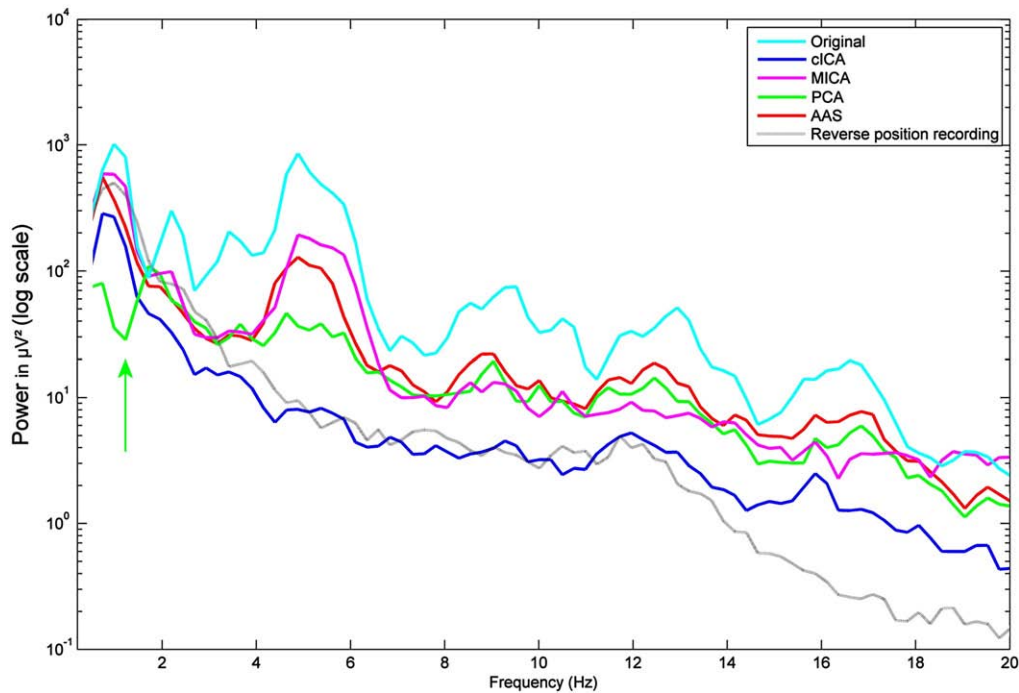
470 In the frequency domain, all correction methods globally decrease  
 471 signal power (Fig. 5). As compared to other methods, cICA (blue line)  
 472 is the method which removes the most power in all frequency bands  
 473 and pleasingly provides the spectrum closest to the recording obtained  
 474 outside the scanner bore (grey line). Constrained ICA removes  
 475 marginally more power than AAS (red) and MICA (cyan) in the lowest  
 476 frequency range although it retains the characteristic spectral mode  
 477 of deep slow wave sleep around 0.8 Hz. In contrast, PCA considerably  
 478 reduces the power density in the frequency range of sleep slow waves  
 479 (green line and arrow).

480 To quantify these power changes after PRA correction and character-  
 481 ize their scalp topography, we computed the INPS over all channels for

subject 1. Fig. 6 displays INPS topography over the entire scalp for the four  
 482 methods. 483

484 More power is suppressed by PCA than by any other method as  
 485 indicated by a large INPS value (8.49, mean over all EEG electrodes, Fig.  
 486 6B). However, as suggested earlier, the specificity of PCA in removing  
 487 only PRA is questionable. A topographical structure can be observed for  
 488 INPS computed with cICA, AAS or MICA (Figs. 6A, C, D, respectively),  
 489 characterized by large INPS values in right frontal and left temporal areas,  
 490 a scalp topography reminiscent of PRA power distribution (Fig. 3). In  
 491 contrast, PCA suppresses power homogeneously over the scalp,  
 492 suggesting a non specific rejection of both PRA and genuine cerebral  
 493 oscillations. Characterized by a mean INPS over all channels of 5.93, cICA  
 494 suppresses more power than the AAS and MICA (mean INPS of 1.92 and  
 495 3.96, respectively). However, cICA still preserves a regionally specific  
 496 effect which again speaks for the selective removal of PRA.

To further compare the different PRA removal methods, the distortion  
 497 index was computed from 0.5 Hz to 20 Hz, corresponding to the  
 498 bandwidth of sleep-related activity, by steps of 1 Hz. An index equal to one  
 499



**Fig. 5.** Power spectrum of the EEG recorded at electrode F8 after correction by the different PRA rejection methods. The power spectrum of the original signal and signal recorded with the head outside the MR scanner are given as references.

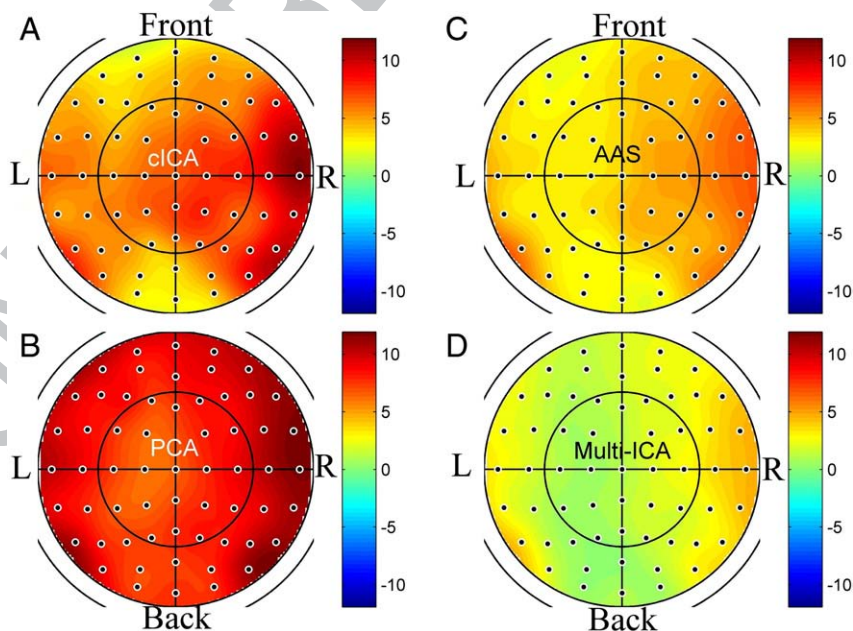
would mean that there is the same amount of power in the reference signal without PRA as in the artefacted signal after cleaning. An ideal PRA suppression method would therefore have an index of 1 across all frequency bins. The results are shown in Fig. 7.

All correction methods suppress too much power ( $I(f) < 1$ ) at frequencies below 5 Hz and not enough power ( $I(f) > 1$ ) from 15 to 25 Hz. Constrained ICA clearly outperforms the other methods for frequencies from 5 Hz to 25 Hz. Note that the indices of the other methods have a peak around 5 Hz, which is successfully avoided by cICA (Fig. 7, inset). Below 5 Hz, the cICA algorithm removes more power than AAS or MICA (Fig. 7, inset). Although this is a potential problem for low frequency

processes such as slow waves in deep sleep, we previously showed that cICA successfully preserves them albeit with a reduced amplitude compared with AAS and MICA (as shown on Figs. 4 and 5). In keeping with results presented above, PCA has an alarmingly low index ( $I(f) @ 0.1$ ) around 1 Hz and strongly affects the slow waves.

#### EEG recordings with gradient artefact

Fig. 8 illustrates the effect of various PRA rejection methods on a typical individual recording during wakefulness. The upper panel shows EEG recorded at Oz during a 20 s period of wakefulness. Although PRA is



**Fig. 6.** INPS values interpolated (from the values calculated at each electrode) over a flat-map representation of the scalp for all the tested correction methods.

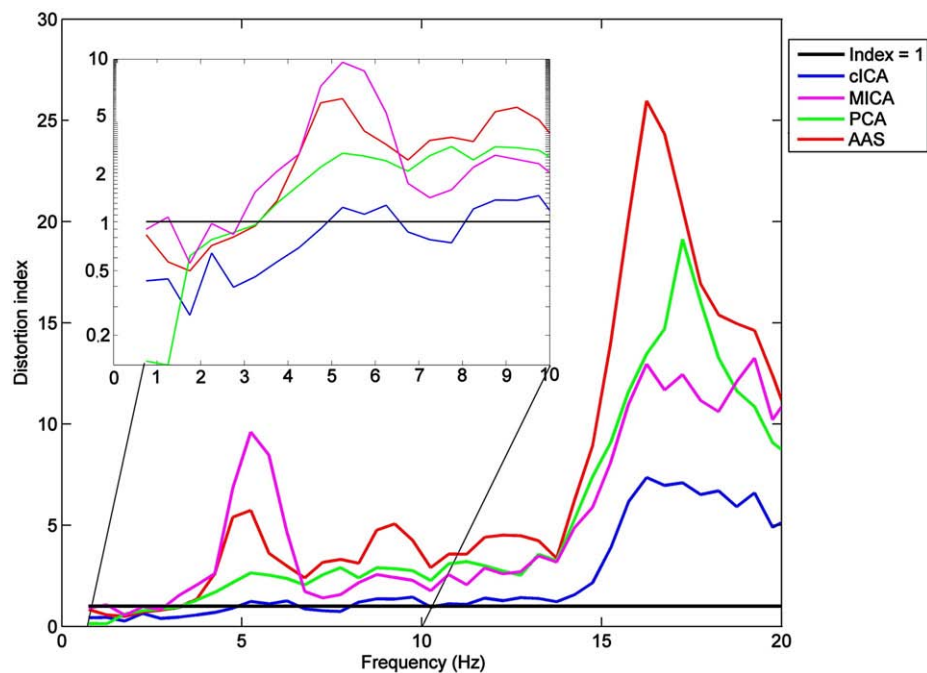


Fig. 7. Distortion index computed for frequencies from 0.5 to 20 Hz by steps of 1 Hz for all the tested methods. A value of 1 means no distortion.

considerably reduced by all techniques, it is still easily visually detected after rejection by AAS and MICA (arrows). PRA is hardly visible after correction by PCA and cICA which seems to reduce the artefact to a similar extent. The lower panel shows the corresponding power spectrum. The peak around 10 Hz, corresponding to the alpha rhythm, is most clearly identified after correction by cICA or MICA, and much less so after correction by AAS or PCA.

Likewise, during stage 2 sleep, sleep spindles are readily identified after correction by all methods (Fig. 9, top). From the power spectrum (Fig. 9, bottom), cICA rejects more power than all other correction methods for nearly all frequencies between 0 and 20 Hz. Nevertheless cICA clearly preserves power modes corresponding to typical activities

of this state, i.e. the spindles and the slow waves. As already noticed above, PCA considerably reduces power between 0.5 and 2 Hz.

At the group level, we computed the power attenuation as the power ratio between corrected and original signals, averaged across the 9 subjects. Although computed on an independent data set, this analysis confirms findings previously observed on the individual data of 2 subjects (cf. previous section). First, in all states of vigilance, cICA method rejects more power than all other methods (except PCA around 1 Hz), especially between 1 and 5 Hz, the frequency band mainly affected by PRA. Second, during stage 2 and slow wave sleep (respectively characterized by *K* complexes and slow waves), power around 1 Hz is marginally more attenuated by cICA than AAS or MICA

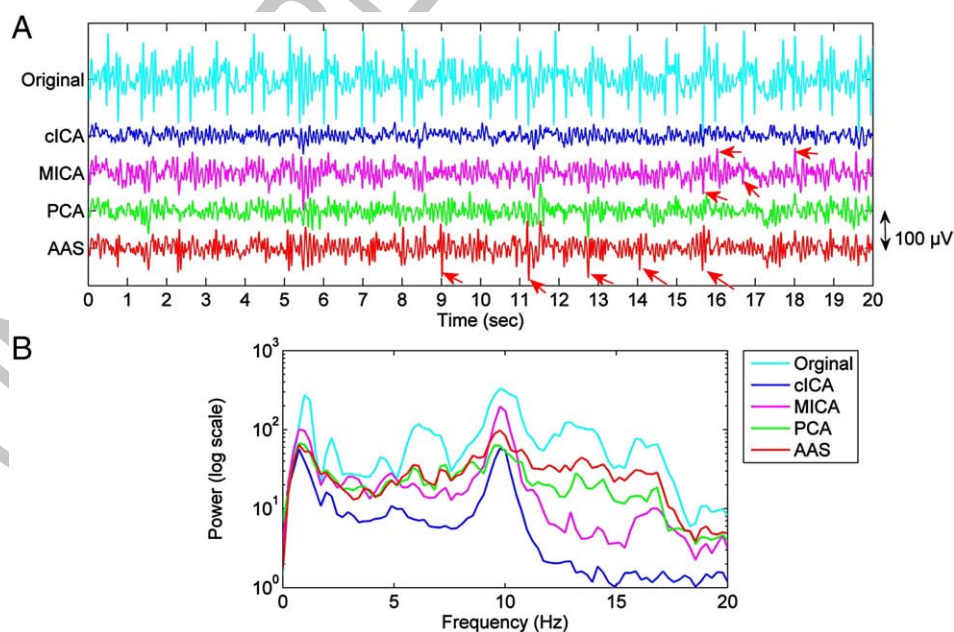
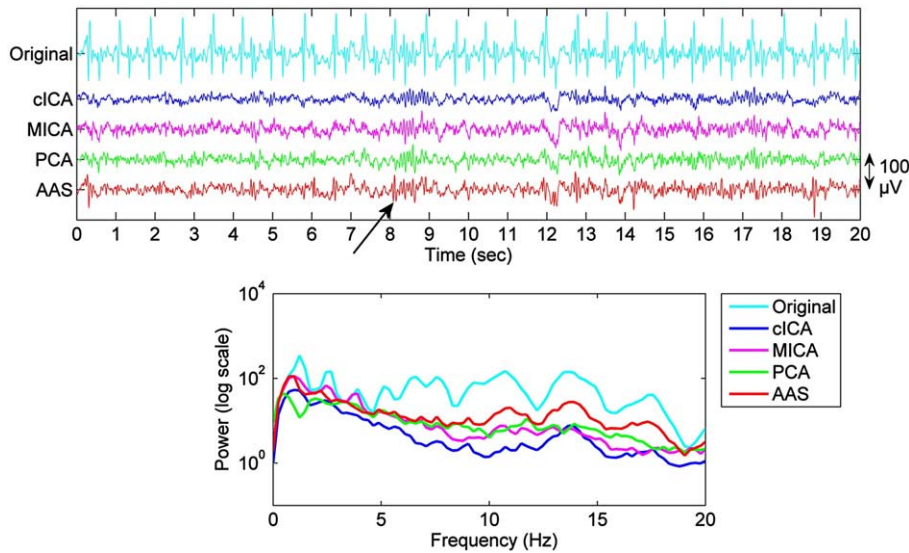


Fig. 8. Time course (panel A) and power spectrum (panel B) of EEG recording corrected by all tested PRA correction methods at electrode Oz during a wake state. The time course and the power of the original signal are given for reference.



**Fig. 9.** Time course (panel A) and power spectrum (panel B) of EEG recording corrected by all tested PRA correction methods at electrode Oz during sleep stage 2 state. The time course and the power of the original signal are given for reference. The arrow indicates spindle activity.

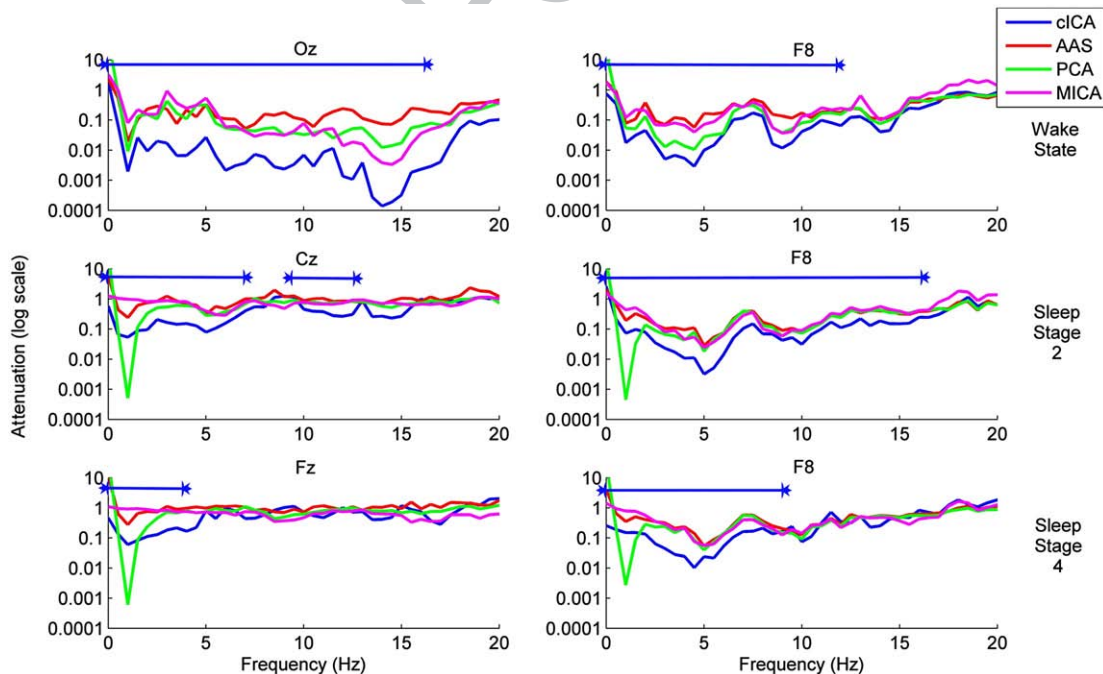
Q1

544 but much less than by PCA. As shown in Fig. 10, the cICA corrected  
 545 signals are significantly different (Friedman test,  $p < .05$ ) from the  
 546 original ones between 0.5 and 4 Hz in every state and every tested  
 547 electrode, i.e. over the frequency band traditionally associated with  
 548 PRA. Moreover for the particular case of Oz in wake state, the  
 549 correction is significant from 0.5 to 16 Hz. This is also the case for F8  
 550 in sleep stage 2 while the correction is significant for Cz from 0.5 to  
 551 12 Hz and from 9 to 13 Hz in sleep stage 2, suggesting that the  
 552 frequency content of the artefact can be different across electrodes.

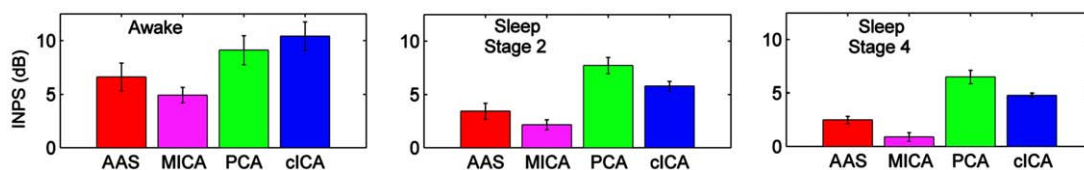
553 We computed the mean INPS for the 4 correction methods across  
 554 all electrodes and subjects (Fig. 11). For all methods, INPS varies  
 555 between states and progressively decreases from wakefulness to light

and deep sleep stages. This result arises from the smaller proportion of  
 556 total power related to PRA during sleep than wakefulness, due to the  
 557 abundance of large amplitude slow waves during the former. During  
 558 wakefulness, cICA INPS is larger than that of any other methods.  
 559 During sleep states, cICA INPS is still larger than that of MICA and AAS.  
 560 However, PCA INPS is now larger than cICA INPS because, as indicated  
 561 before, PCA non selectively suppresses a large amount of power  
 562 around 1 Hz. All these results are statistically significant (Wilcoxon  
 563 signed-rank test;  $p < 0.01$ ).  
 564

565 Fig. 12 shows the mean score of the blind expert's classification for  
 566 each correction methods. The cICA ranks significantly better than PCA  
 567 (Wilcoxon signed-rank test;  $p < 0.0003$ ). However even if cICA has the



**Fig. 10.** Mean attenuation over 9 subjects for the different PRA correction methods and for 3 different wake/sleep stages. Two different electrodes are displayed per stage. The blue lines above the different plot shows over which frequency band is the cICA correction significant relative to no correction (Friedman test;  $p < 0.05$ ).



**Fig. 11.** Mean INPS over the 9 subjects and over all EEG electrodes for different sleep stages. The cICA mean INPS is significantly different from the other method mean INPS for all sleep stages (Wilcoxon signed-rank test;  $p < 0.01$ ).

568 best mean score, it is not significantly better than AAS (Wilcoxon signed-  
569 rank test;  $p < 0.1$ ) or MICA (Wilcoxon signed-rank test;  $p < 0.11$ ).

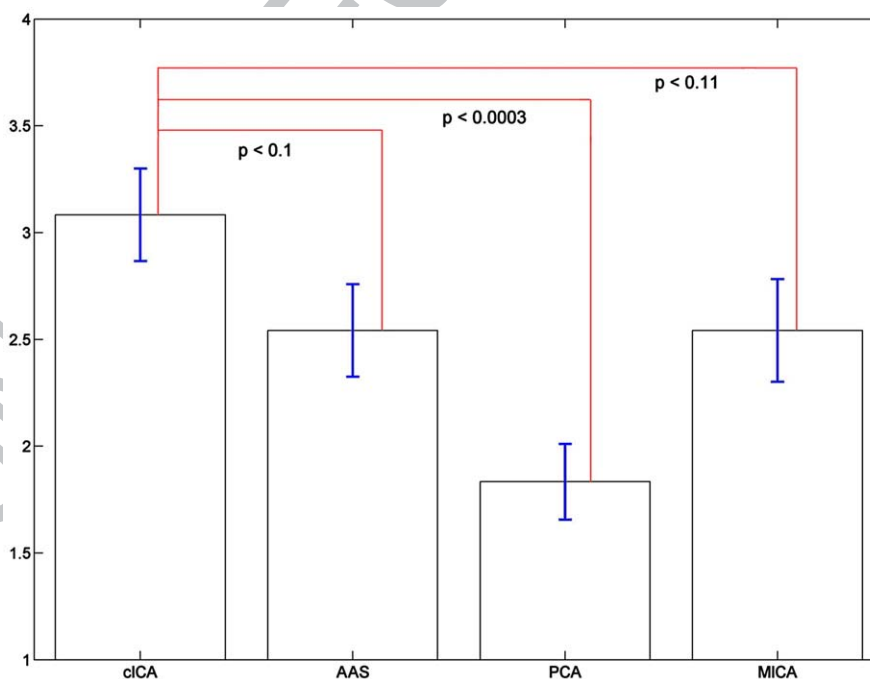
## 570 Discussion

571 On EEG recordings, deep non rapid eye movement sleep is  
572 characterized by large amplitude slow waves which typically lasts  
573 about 1 s. In the framework of EEG–fMRI studies on deep NREM sleep,  
574 removal of PRA from EEG recordings are problematic because the  
575 period and amplitude of sleep slow waves and PRA overlap. In this  
576 paper, we introduce constrained ICA as a novel method for PRA  
577 rejection from EEG recorded simultaneously with fMRI during slow  
578 wave sleep. We first evaluated cICA in datasets obtained during slow  
579 wave sleep in 2 subjects positioned consecutively in a large static  
580 magnetic field (head within the scanner) then in a negligible field (on  
581 the scanner table but head away from the bore). Only the former  
582 recording was detectably contaminated by PRA. Our evaluation  
583 indicates that cICA is both efficient and specific in rejecting PRA. The  
584 power spectrum obtained after correction by cICA was very close to  
585 the spectrum obtained away from the magnetic field, as confirmed by  
586 a favorable distortion index between 1 and 20 Hz. As indicated by the  
587 INPS, cICA remove more power than the AAS, PCA or MICA. Below  
588 1 Hz, cICA retained the characteristic spectral mode of slow oscillation  
589 whereas PCA significantly reduced the power of slow waves. These  
590 findings were statistically confirmed on a larger dataset collected in 9  
591 subjects not only during slow wave sleep but also during wakefulness  
592 and light non rapid eye movement sleep. Finally, the quality of PRA

rejection by cICA also compared favorably with other techniques,  
593 when visually assessed by an expert. 594

The main advantages of cICA are that, although using the classical  
595 ICA machinery, (1) it considerably reduces the computational load of  
596 PRA rejection, relative to classical ICA; (2) it eschews the problem of  
597 component identification and (3) it provides an efficient and robust  
598 rejection of PRA, which by many aspects outperforms earlier classical  
599 methods. The only parameter, the threshold of the clustering step, is  
600 easily calculated given the number of channels. One disadvantage of  
601 cICA is that, as for ICA methods in general, it requires a large number of  
602 sensors (i.e., EEG channels). The cICA solution also relies on the  
603 accurate detection of the QRS peak detection which in turn depends  
604 on the quality of ECG recording and the detection algorithm used. We  
605 found that the solution proposed by Niazy et al. (2005) was very  
606 reliable for our data. Our simulation shows that the quality of PRA  
607 rejection substantially decreases when the number of channels is  
608 smaller than about 30. Another drawback of the method, also common  
609 to other ICA algorithms, is that the propagation of noise from a single  
610 bad channel (due to muscular artefact or electrode disconnection) to  
611 all other channels after PRA rejection. This problem is easily fixed by  
612 rejecting the bad channel before PRA removal. 613

Finally, this novel technique is equally efficient in removing PRA  
614 from continuous EEG time series recorded in other states of vigilance  
615 (wakefulness and light sleep). We also successfully tested our  
616 algorithm on an EEG recording obtained in an epileptic patient who  
617 fortuitously fell asleep during the EEG/fMRI session (see [Supplemental](#)  
618 [material](#)). However, the efficiency of this technique in other types of  
619



**Fig. 12.** Mean score obtained by the 4 correction methods with a blind expert's evaluation. The  $p$ -value, obtained by performing a Wilcoxon signed-rank test, indicates that cICA and PCA are significantly different but that cICA and AAS or MICA are not.

620 recording such as event-related potentials, for instance, has not been  
621 evaluated and should be subjected to further investigation.

## 622 Acknowledgments

623 This study was supported by the Belgian Fonds National de la  
624 Recherche Scientifique (F.R.S.-F.N.R.S.), the Fondation Médicale Reine  
625 Elisabeth, the Research Fund of ULg, and PAI/IAP Interuniversity Pole of  
626 Attraction. Y.L., E.B., T.D., P.M. and C.P. are supported by F.N.R.S. (Belgium).

## 627 Appendix A. Mathematical appendix

### 628 Introduction to cICA

629 The problem of Constrained Independent Component Analysis  
630 (cICA) consists in (1) maximizing the negentropy of the sources  
631  $\sum_{i=1}^l J(s_i)$ , as in classical ICA algorithm but (2) subject to constraints  $\mathbf{g}$   
632  $(\mathbf{W}) \leq 0$  and  $\mathbf{h}(\mathbf{W}) = 0$ , where

- 633  $\mathbf{h}(\mathbf{W}) = 0$ , where
- 634 •  $l$  is the desired number of components to be extracted;
- 635 •  $\mathbf{g}(\mathbf{W}) = (g_1(\mathbf{w}_1) \dots g_l(\mathbf{w}_l))^T$  in which each  $g_i(\mathbf{w}_i) = \varepsilon_i(s_i, r_i) - \xi_i$  for  $i = 1, \dots,$   
636  $l$ ;
- 637 •  $\mathbf{h}(\mathbf{W}) = (h_1(\mathbf{w}_1) \dots h_l(\mathbf{w}_l))^T$  with  $h_i(\mathbf{w}_i) = E\{s_i^2\} - 1$  for  $i = 1, \dots, l$ .

638 The first constraint forces the distance between each source  
639 estimates and its respective reference  $\varepsilon_i(s_i, r_i)$  to stay under a specified  
640 distance  $\xi_i$ . The second constraint is just a normalization term.

641 To solve this problem, the Kuhn–Tucker conditions, i.e. the  
642 generalization of the Lagrange multiplier, are used. The augmented  
643 Lagrangian function  $L_2(\mathbf{W}, \underline{\boldsymbol{\mu}}, \underline{\boldsymbol{\lambda}})$  is given by:

$$L_2 = \sum_{i=1}^l \left( J(y_i) - \frac{\max\{\mu_i + \gamma_i g(\mathbf{w}_i, 0) - \mu_i^2\}}{2\gamma_i} \right) - \lambda^T \mathbf{h}(\mathbf{W}) - \frac{1}{2} \gamma^T \|\mathbf{h}(\mathbf{W})\|^2 \quad (8)$$

644 where  $\underline{\boldsymbol{\mu}} = (\mu_1 \dots \mu_l)^T$  and  $\underline{\boldsymbol{\lambda}} = (\lambda_1 \dots \lambda_l)^T$  are two sets of Lagrange multi-  
645 pliers for the inequality and equality constraints respectively, and  $\underline{\boldsymbol{\gamma}} =$   
646  $(\gamma_1 \dots \gamma_l)^T$  are the parameters to form the penalty terms to ensure that  
647 the optimization problem is held at the condition of local convexity  
648 assumption.

649 To find the decorrelation matrix, a Newton-like iteration process is  
650 used:

$$\mathbf{W}_{k+1} = \mathbf{W}_k - \langle \mathbf{ss}(\mathbf{W}) \rangle \mathbf{L}_k^{-1} \mathbf{R}_{\mathbf{xx}}^{-1} \quad (9)$$

653 where  $\langle \mathbf{ss}(\mathbf{W}) \rangle$  is a vector depending of the negentropy of each  $s_i$  and  
654  $\mathbf{R}_{\mathbf{xx}}$  is the autocorrelation matrix of the original recordings  $\mathbf{x}$ .

$$\underline{\boldsymbol{\mu}}_{k+1} = \max\{0, \underline{\boldsymbol{\mu}}_k + \langle \gamma \rangle \mathbf{g}(\mathbf{W})\} \quad (10)$$

$$\underline{\boldsymbol{\lambda}}_{k+1} = \underline{\boldsymbol{\lambda}}_k + \langle \gamma \rangle \mathbf{h}(\mathbf{W}) \quad (11)$$

658 The stopping criteria for the iterative process was simply that the  
660 relative difference between the norm of 2 successive estimates of  $\mathbf{W}$   
661 be smaller than  $10^{-5}$ .

662 Decorrelation of the different estimates can be used to prevent the  
663 convergence of two estimates towards the same IC. In our case, the  
664 decorrelation is not used since different estimates are wanted to  
665 converge to the same independent components (to increase robust-  
666 ness of our estimates, see section cICA rejection algorithm).

667 Importantly, in classic cICA algorithms, the constraint on  $\mathbf{g}$  is relaxed  
668 once, along the iterative process, the estimation of the independent  
669 component is in the neighborhood of the reference. This is similar to an  
670 ICA algorithm where the initialization is the reference. The sources the

algorithm will find are the nearest ones to the reference since the Kuhn–  
Tucker conditions are a local maximum finder.

Yet, in our implementation the constraint is not relaxed and thus  
our algorithm does not find the statistically independent component  
but a tradeoff between the constraint and this component. The choice  
of the  $\xi_i$  is said to be critical in Lu and Rajapakse (2001). However since  
the constraint is not relaxed we choose  $\xi_i = 0$  and whatever value we  
choose for  $\xi$ , the algorithm always tries to minimize the value of  $\mathbf{g}$ . Our  
algorithm is thus not an ICA algorithm, strictly speaking.

### Preprocessing and mathematical assumptions

#### Assumptions

Since, the variance of the independent components cannot be  
recovered (see Hyvarinen, 2000), it is hypothesized that  $E\{\mathbf{ss}^T\} = \mathbf{I}$  for  
simplicity. To ensure that it holds true, we have to fix the norm of each  
row-vector of the demixing matrix equal to one and to center and  
whiten the data.

#### Preprocessing

The data are preprocessed in the classical way: they are centered  
and whitened. After centering the  $x_i$ , all the  $s_i$  will have a zero mean  
since we find them through a linear combination of the  $x_i$  using the  
demixing matrix  $\mathbf{W}$ .

Whitening consists in transforming the data  $\mathbf{x}$  linearly to obtain a  
new vector  $\tilde{\mathbf{x}}$  where the components of are uncorrelated and their  
variances equal one. A whitened vector  $\tilde{\mathbf{x}}$  has a covariance matrix  
equal to

$$E\left\{ \tilde{\mathbf{x}} \tilde{\mathbf{x}}^T \right\} = \mathbf{I} \quad (12)$$

This whitening is commonly achieved using the eigenvalue  
decomposition of the covariance matrix  $E\{\mathbf{xx}^T\} = \mathbf{E}\mathbf{D}\mathbf{E}^T$ , where  $\mathbf{E}$  is the  
orthogonal matrix of eigenvectors of  $E\{\mathbf{xx}^T\}$  and  $\mathbf{D}$  its eigenvalues,  
 $\mathbf{D} = \text{diag}(d_1, \dots, d_n)$ . Whitening is achieved through

$$\tilde{\mathbf{x}} = \mathbf{E}\mathbf{D}^{-1/2}\mathbf{E}^T\mathbf{x} \quad (13)$$

which obviously leads to  $E\left\{ \tilde{\mathbf{x}} \tilde{\mathbf{x}}^T \right\} = \mathbf{I}$ . In the framework of the ICA  
problem, whitening transforms the mixing matrix  $\mathbf{A}$  into a new one:  $\tilde{\mathbf{A}}$   
which can be found using Eqs. (4) and (13)

$$\tilde{\mathbf{x}} = \mathbf{E}\mathbf{D}^{-1/2}\mathbf{E}^T\mathbf{A}\mathbf{s} = \tilde{\mathbf{A}}\mathbf{s} \quad (14)$$

The main advantage of the whitening step is that this new mixing  
matrix  $\tilde{\mathbf{A}}$  is orthogonal:

$$E\left\{ \tilde{\mathbf{x}} \tilde{\mathbf{x}}^T \right\} = \tilde{\mathbf{A}}E\left\{ \mathbf{ss}^T \right\}\tilde{\mathbf{A}}^T = \tilde{\mathbf{A}}\tilde{\mathbf{A}}^T = \mathbf{I} \quad (15)$$

and if  $\tilde{\mathbf{A}}$  is orthogonal, so is its inverse  $\tilde{\mathbf{W}}$ .

#### Sorting out the artefact sources using K-means clustering

We use a “K-means” (MacQueen, 1967) clustering method. The idea  
is to gather the sources which are similar together, in the same cluster.  
Once the sources have been sorted in clusters, the mean vectors of  
each cluster are calculated.

However instead of applying the clustering program to the  
observations of the sources directly (which have a length equal to  
the number of time bins in the time series), it is computationally more  
efficient and theoretically equivalent to apply the clustering algorithm  
to the row-vector of the demixing matrix (which has a length equal to  
the number of channels) provided by the cICA program.

K-means-based algorithms have the advantage to be quick and  
simple. However they have two drawbacks: they do not find the best  
clusters at each execution (due to local convergence and random

initialization) and the number  $K$  of clusters must be specified a priori. The quality of the clustering can be measured by the expressed variance,  $ev_K$ , which is defined by:

$$ev_K = 1 - \frac{\sum_{k=1}^K \frac{n_k}{N} \text{var}_k}{\text{Var}} \quad (16)$$

where  $K$  is the number,  $\text{var}_k$  the variance in the  $k$ th cluster,  $\text{Var}$  the variance of the initial set of vectors,  $n_k$  the number of vectors in the  $k$ th cluster and  $N$  the number of vectors in the initial set of vectors.

The idea is to initialize  $K$  at 2, to run the  $K$ -means algorithm a sufficient number of times and to retain only the best clustering (which has the maximum expressed variance  $ev_2$ ).  $K$  is then incremented to 3 and the algorithm is run the same number of times and the maximum value of the expressed variance is stored:  $ev_3$ . The difference between  $ev_2$  and  $ev_3$  represents the gain of representing the set of vectors by 3 clusters instead of 2. If this gain is sufficiently high, we again increment  $k$  by one. We repeat these steps until the increment of expressed variance:  $ev_{p+1} - ev_p$  is below an arbitrarily chosen threshold value and, the clustering of  $p$  clusters is kept. The algorithm returns the means of these  $p$  clusters which are  $p$  row-vectors projecting the EEG recordings onto source space resulting in robust estimation of the artefact sources.

We empirically fixed the stopping threshold at 3%. Too large a value of this threshold could lead to a poor description of the set of vector and different artefact-related estimates may be merged in the same cluster. Too small a value could lead to an over-description of the artefact-related estimates, reducing the dimension available to describe the neural related-activity. Note that for a fixed number  $N_{ch}$ , the  $ev_K$  is increasing with the number of cluster while the difference of consecutive  $ev$  ( $ev_{p+1} - ev_p$ ) is decreasing. The rate of this decrease is dependent of the number of vectors in the set to cluster. The threshold used for the clustering stopping criteria should be empirically adjusted for the number of EEG channels, as a rule of thumb we found that with half the channels (32), we should use the double of the threshold (6%) to obtain similar results.

## Appendix B. Supplementary data

Supplementary data associated with this article can be found, in the online version, at doi:10.1016/j.neuroimage.2008.10.017.

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